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1 Estimating the effect of competition on trait evolution using maximum likelihood inference

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- 7 Running head: INTERSPECIFIC COMPETITION & TRAIT EVOLUTION
- 8

9 Abstract

10 Many classical ecological and evolutionary theoretical frameworks posit that competition 11 between species is an important selective force. For example, in adaptive radiations, resource 12 competition between evolving lineages plays a role in driving phenotypic diversification and 13 exploration of novel ecological space. Nevertheless, current models of trait evolution fit to 14 phylogenies and comparative datasets are not designed for incorporating the effect of 15 competition. The most advanced models in this direction are diversity-dependent models where 16 evolutionary rates depend on lineage diversity. However, these models still treat changes in traits 17 in one branch as independent of the value of traits on other branches, thus ignoring the effect of 18 species similarity on trait evolution. Here, we consider a model where the evolutionary dynamics 19 of traits involved in interspecific interactions are influenced by species similarity in trait values 20 and where we can specify which lineages are in sympatry. We develop a maximum-likelihood 21 based approach to fit this model to combined phylogenetic and phenotypic data. Using 22 simulations, we demonstrate that the approach accurately estimates the simulated parameter 23 values across a broad range of parameter space. Additionally, we develop tools for specifying the 24 biogeographic context in which trait evolution occurs. In order to compare models, we also apply 25 these biogeographic methods to specify which lineages interact sympatrically for two diversity-26 dependent models. Finally, we fit these various models to morphological data from a classical 27 adaptive radiation (Greater Antillean Anolis lizards). We show that models that account for 28 competition and geography perform better than other models. The matching competition model 29 is an important new tool for studying the influence of interspecific interactions, in particular 30 competition, on phenotypic evolution. More generally, it constitutes a step toward a better 31 integration of interspecific interactions in many ecological and evolutionary processes.

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32

33 *Keywords*: interspecific competition, trait evolution, phylogenetic comparative methods, 34 adaptive radiation, community phylogenetics, Anolis, maximum likelihood 35 36 Interactions between species can be strong selective forces. Indeed, many classical 37 evolutionary theories assume that interspecific competition has large impacts on fitness. 38 Character displacement theory (Brown and Wilson 1956; Grant 1972; Pfennig and Pfennig 39 2009), for example, posits that interactions between species, whether in ecological or social 40 contexts, drive adaptive changes in phenotypes. Similarly, adaptive radiation theory (Schluter 41 2000) has been a popular focus of investigators interested in explaining the rapid evolution of 42 phenotypic disparity (Grant and Grant 2002; Losos 2009; Mahler et al. 2013; Weir and Mursleen 43 2013), and competitive interactions between species in a diversifying clade are a fundamental 44 component of adaptive radiations (Schluter 2000; Losos and Ricklefs 2009; Grant and Grant 45 2011). 46 Additionally, social interactions between species, whether in reproductive (Gröning and 47 Hochkirch 2008; Pfennig and Pfennig 2009) or agonistic (Grether et al. 2009, 2013) contexts, are 48 important drivers of changes in signal traits used in social interactions. Several evolutionary 49 hypotheses predict that geographical overlap with closely related taxa should drive divergence in 50 traits used to distinguish between conspecifics and heterospecifics (e.g., traits involved in mate 51 recognition; Wallace 1889; Fisher 1930; Dobzhansky 1940; Mayr 1963; Gröning and Hochkirch 52 2008; Ord and Stamps 2009; Ord et al. 2011). Moreover, biologists interested in speciation have

53 often argued that interspecific competitive interactions are important drivers of divergence

54 between lineages that ultimately leads to reproductive isolation. Reinforcement, or selection

against hybridization (Dobzhansky 1937, 1940), for example, is often thought to be an important
phase of speciation (Grant 1999; Coyne and Orr 2004; Rundle and Nosil 2005; Pfennig and
Pfennig 2009).

58 In addition to the importance of interspecific competition in driving phenotypic 59 divergence between species, competitive interactions are also central to many theories of 60 community assembly, which posit that species with similar ecologies exclude each other from 61 the community (Elton 1946). In spite of the importance of interspecific competition to these key 62 ecological and evolutionary theories, the role of competition in driving adaptive divergence and 63 species exclusion from ecological communities has been historically difficult to measure (Losos 64 2009), because both trait divergence and species exclusion resulting from competition between 65 lineages during their evolutionary history has the effect of eliminating competition between those 66 lineages at the present. Community phylogeneticists have aimed to solve part of this conundrum 67 by analyzing the phylogenetic structure of local communities: assuming that phylogenetic 68 similarity between two species is a good proxy for their ecological similarity, competitive 69 interactions are considered to have been more important in shaping communities comprised of 70 phylogenetically (and therefore ecologically) distant species (Webb et al. 2002; Cavender-Bares 71 et al. 2009). However, there is an intrinsic contradiction in this reasoning, because using 72 phylogenetic similarity as a proxy for ecological similarity implicitly (or explicitly) assumes that 73 traits evolved under a Brownian model of trait evolution, meaning that species interactions had 74 no effect on trait divergence (Kraft et al. 2007; Cavender-Bares et al. 2009; Mouquet et al. 2012; 75 Pennell and Harmon 2013).

More generally, and despite the preponderance of classical evolutionary processes that
 assume that interspecific interactions have important fitness consequences, existing phylogenetic

78 models treat trait evolution within a lineage as independent from traits in other lineages. For 79 example, in the commonly used Brownian motion and Ornstein-Uhlenbeck models of trait 80 evolution (Cavalli-Sforza & Edwards 1967, Felsenstein 1988, Hansen and Martins 1996), once 81 an ancestor splits into two daughter lineages, the trait values in those daughter lineages do not 82 depend on the trait values of sister taxa. Some investigators have indirectly incorporated the 83 influence of interspecific interactions by fitting models where evolutionary rates at a given time 84 depend on the diversity of lineages at that time (e.g., the "diversity-dependent" models of Mahler 85 et al. 2010, Weir and Mursleen 2013). While these models capture some parts of the interspecific 86 processes of central importance to evolutionary theory, such as the influence of ecological 87 opportunity, they do not explicitly account for trait-driven interactions between lineages, as trait 88 values in one lineage do not vary directly as a function of trait values in other evolving lineages. 89 Recently, Nuismer and Harmon (2015) proposed a model where the evolution of a 90 species' trait depends on other species' traits. In particular, they consider a model, which they 91 refer to as the model of phenotype matching, where the probability that an encounter between 92 two individuals has fitness consequences declines as the phenotypes of the individuals become 93 more dissimilar. The consequence of the encounter on fitness can be either negative if the 94 interaction is competitive, resulting in character divergence (matching competition, e.g. resource 95 competition), or positive if the interaction is mutualistic, resulting in character convergence 96 (matching mutualism, e.g. Müllerian mimicry). Applying Lande's formula (Lande 1976) and 97 given a number of simplifying assumptions—importantly that all lineages evolve in sympatry 98 and that competitive interactions are approximately equivalent across sympatric taxa— this 99 model yields a simple prediction for the evolution of a population's mean phenotype.

100 Here, we develop inference tools for fitting a simple version of the matching competition 101 model (i.e., the phenotype matching model of Nuismer and Harmon incorporating competitive 102 interactions between lineages) to combined phylogenetic and trait data. We begin by showing 103 how to compute likelihoods associated with this model. Next, we use simulations to explore the 104 statistical properties of maximum likelihood estimation of the matching competition model 105 (parameter estimation as well as model identifiability). While the inclusion of interactions 106 between lineages is an important contribution to quantitative models of trait evolution, applying 107 the matching competition model to an entire clade relies on the assumption that all lineages in 108 the clade are sympatric. However, this assumption will be violated in most empirical cases, so 109 we also developed a method for incorporating data on the biogeographical overlap between 110 species for this model and for the linear and exponential diversity-dependent trait models of Weir 111 & Mursleen (2013), wherein the evolutionary rate at a given time in a tree varies as a function of 112 the number of lineages in the reconstructed phylogeny at that time (see also Mahler et al. 2010). 113 We then fit the model to data from a classical adaptive radiation: Greater Antillean Anolis 114 lizards (Harmon et al. 2003; Losos 2009). Many lines of evidence support the hypothesis that 115 resource competition is responsible for generating divergence between species in both habitat use 116 (e.g., Pacala and Roughgarden 1982) and morphology (Schoener 1970; Williams 1972; see 117 review in Losos 1994). Thus, we can make an *a priori* prediction that model comparison will 118 uncover a signature of competition in morphological traits that vary with habitat and resource 119 use. Given the well-resolved molecular phylogeny (Mahler et al. 2010, 2013) and the relatively 120 simple geographical relationships between species (i.e., many species are restricted to single 121 islands, Rabosky and Glor 2010; Mahler and Ingram 2014), the Greater Antillean Anolis lizards

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provide a good test system for exploring the effect of competition on trait evolution using thematching competition model.

124

125 METHODS

126 Likelihood Estimation of the Matching Competition Model

127 We consider the evolution of a quantitative trait under the matching competition model of 128 Nuismer & Harmon (2015) wherein trait divergence between lineages will be favored by 129 selection. We make the assumption that the outcome of competitive interactions is similar 130 between all members of an evolving clade rather than sensitive to pairwise phenotypic similarity 131 (i.e., that α in Eq. 1 of Nuismer and Harmon 2015 is small). This assumption is crucial, as it 132 ensures that the evolution of a population's mean phenotype is given by a linear model (Eq. S38 133 in Nuismer and Harmon 2015). Importantly, this implies that the expected distribution of trait 134 values on a given phylogeny follows a multivariate normal distribution (Manceau *et al.*, in prep), 135 as is the case for classical models of quantitative trait evolution (Hansen and Martin 1996, 136 Harmon et al. 2010, Weir and Mursleen 2013). In our current treatment of the model, we remove 137 stabilizing selection to focus on the effect of competition (see Discussion). Under these two 138 simplifying assumptions, the mean trait value for lineage *i* after an infinitesimally small time step 139 dt is given by (Eq. S38 in Nuismer and Harmon 2015 with $\psi = 0$):

140

141
$$z_i(t+dt) = z_i(t) + S(\mu(t) - z_i(t))dt + \sigma dB_i$$
 (Eq. 1)

142

143 where $z_i(t)$ is the mean trait value for lineage *i* at time t, $\mu(t)$ is the mean trait value for the 144 entire clade at time t, *S* measures the strength of interaction (more intense competitive 145 interactions are represented by larger negative values), and drift is incorporated as Brownian motion σdB_i with mean = 0 and variance = $\sigma^2 dt$, Note that when S = 0 or n = 1 (i.e., when a 146 147 species is alone), this model reduces to Brownian motion. Under the model specified by Eq. 1, if 148 a species trait value is greater (or smaller) than the trait value average across species in the clade, 149 the species' trait will evolve towards even larger (or smaller) trait values. We discuss the 150 strengths and limitations of this formulation of the matching competition in the Discussion. 151 Given that the expected distribution of trait values on a phylogeny under the matching 152 competition model specified in Eq. 1 follows a multivariate normal distribution, it is entirely 153 described with its expected mean vector (made of terms each equal to the character value at the 154 root of the tree) and variance-covariance matrix. Nuismer & Harmon (2015) provide the system 155 of ordinary differential equations describing the evolution of the variance and covariance terms 156 through time (their Eqs.10b and 10c). These differential equations can be integrated numerically 157 from the root to the tips of phylogenies to compute expected variance-covariance matrices for a 158 given set of parameter values and the associated likelihood values given by the multivariate 159 normal distribution.

Additionally, to relax the assumption that all of the lineages in a clade coexist sympatrically, we included a term to specify which lineages co-occur at any given time-point in the phylogeny, which can be inferred, e.g., by biogeographical reconstruction. We define piecewise constant coexistence matrices **A**, where $\mathbf{A}_{i,j}$ equals 1 at time *t* if *i* and *j* are sympatric at that time, and 0 otherwise (Fig. 1). The evolution of the trait value for lineage *i* is then given by: 165

166
$$z_i(t+dt) = z_i(t) + S\left(\left(\frac{1}{n_i}\sum_{l=1}^n \mathbf{A}_{i,l} z_l(t)\right) - z_i(t)\right) dt + \sigma dB_i$$
 (Eq. 2)

168 where $n_i = \sum_{j=1}^{n} \mathbf{A}_{ij}$ is the number of lineages interacting with lineage *i* at time *t* (equal to the

169 number *n* of lineages in the reconstructed phylogeny at time *t* if all species are sympatric) such

170 that trait evolution is only influenced by sympatric taxa.

- We show (Appendix S1) that the corresponding system of ordinary differential equations
 describing the evolution of the variance and covariance terms through time is:
- 173

174
$$\frac{dv_{i,i}}{dt} = -\frac{2S(n_i-1)}{n_i}v_{i,i} + \frac{2S}{n_i} \left(\sum_{\substack{l=1\\(l\neq i)}}^n \mathbf{A}_{i,l}v_{l,i} \right) + \sigma^2$$
(Eq. 3a)

175

176
$$\frac{dv_{i,j}}{dt} = -S\left(\frac{n_i-1}{n_i} + \frac{n_j-1}{n_j}\right)v_{i,j} + \frac{s}{n_i}\sum_{\substack{k=1\\k\neq i}}^n \mathbf{A}_{i,k}v_{k,j} + \frac{s}{n_j}\sum_{\substack{l=1\\l\neq j}}^n \mathbf{A}_{j,l}v_{l,i}$$
(Eq. 3b)

177

where $v_{i,i}$ is the variance for each species *i* at time *t* and $v_{i,i}$ is the covariance for each species 178 179 pair *i*, *j* at time *t*. Using numerical integration, we solve this system of ordinary differential 180 equations from the root of the tree to the tips in order to calculate the values of the variance-181 covariance matrix expected under the model for a given phylogeny and set of parameter values. 182 Specifically, Eq. 3a and 3b dictate the evolution of the variance and covariance values along the 183 branches of the tree; at a given branching event, the variance and covariance values associated to 184 the two daughter species are simply inherited from those of the ancestral species. With the 185 expected variance-covariance matrix at present, we calculate the likelihood for the model using 186 the likelihood function for a multivariate-normal distribution (e.g. Harmon et al. 2010). Then, 187 using standard optimization algorithms, we identify the maximum likelihood values for the 188 model parameters. The matching competition model has three free parameters: σ^2 , S and the ancestral state z_0 at the root. As with other models of trait evolution, the maximum likelihood 189

190 estimate for the ancestral state is computed through GLS using the estimated variance-covariance

191 matrix (Grafen 1989; Martins and Hansen 1997).

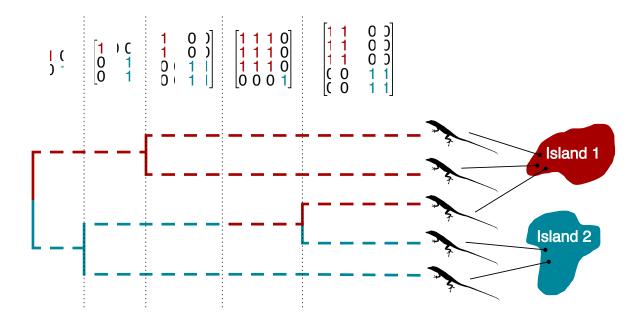
192 We used the ode function in the R package deSolve (Soetaert et al. 2010) to perform the

numerical integration of the differential equations using the "lsoda" solver, and the Nelder-Mead

algorithm implemented in the optim function to perform the maximum likelihood optimization.

195 Codes for these analyses are freely available on github (https://github.com/hmorlon/PANDA)

and included the R package RPANDA (Morlon et al. MS).



197

Figure 1. Illustration of geography matrices (defined between each node and after each dispersal event inferred, e.g., by stochastic mapping) delineating which lineages interact in sympatry in an imagined phylogeny. These matrices were used to identify potentially interacting lineages for the matching competition and both diversity-dependent models of character evolution (see Eqs. 3-5 in the main text). *Anolis* outline courtesy of Sarah Werning, licensed under Creative Commons.

198

200 Incorporating Geography into Diversity-Dependent Models

Using the same geography matrix A described above for the matching competition model (Fig. 1), we modified the diversity-dependent linear and exponential models of Weir & Mursleen (2013) to incorporate biological realism into the models, because ecological opportunity is only relevant within rather than between biogeographical regions. The resulting variance-covariance matrices, V, of these models have the elements:

206

207
$$\mathbf{V}_{ij} = \sum_{m=2}^{M} (\sigma_0^2 + bn_i) (\max(s_{ij} - t_{m-1}, 0) - \max(s_{ij} - t_m, 0))$$
(Eq. 4)

208

209 for the diversity-dependent linear model, and

210

211
$$\mathbf{V}_{ij} = \sum_{m=2}^{M} (\sigma_0^2 \times e^{rn_i}) (\max(s_{ij} - t_{m-1}, 0) - \max(s_{ij} - t_m, 0))$$
(Eq. 5)

212

for the diversity-dependent exponential model, where σ_0^2 is the rate parameter at the root of the 213 tree, b and r are the slopes in the linear and exponential models, respectively, s_{ii} is the shared 214 215 path length of lineages i and j from the root of the phylogeny to their common ancestor, n_i is the 216 number of sympatric lineages (as above) between times t_{m-1} and t_m (where t_1 is 0, the time at the root, and t_M is the total length of the tree) (Weir & Mursleen 2013). When b or r = 0, these 217 218 models reduce to Brownian motion. For the linear version of the model, we constrained the maximum likelihood search such that the term $(\sigma_0^2 + bn_i)$ in Eq. $3 \ge 0$ to prevent the model 219 220 from having negative evolutionary rates at any $t_{\rm m}$.

221

222 Simulation-based Analysis of Statistical Properties of the Matching Competition Model

223 To verify that the matching competition model can be reliably fit to empirical data, we 224 simulated trait datasets to estimate its statistical properties (i.e., parameter estimation and 225 identifiability using AICc). For all simulations, we began by first generating 100 pure-birth trees 226 using TreeSim (Stadler 2014). To determine the influence of the number of tips in a tree, we ran 227 simulations on trees of size n = 20, 50, 100, and 150. We then simulated continuous trait datasets 228 by applying the matching competition model recursively from the root to the tip of each tree 229 (Paradis 2012), following Eq. 1, assuming that all lineages evolved in sympatry. For these simulations. we set $\sigma^2 = 0.05$ and systematically varied S (-1.5, -1, -0.5, -0.1, or 0). Finally, we 230 231 fit the matching competition model to these datasets using the ML optimization described above. 232 To determine the ability of the approach to accurately estimate simulated parameter 233 values, we first compared estimated parameters to the known parameters used to simulate 234 datasets under the matching competition model (S and σ^2). We also quantified the robustness of 235 these estimates in the presence of extinction by estimating parameters for datasets simulated on 236 birth-death trees; in addition, we compared the robustness of the matching competition model to 237 extinction to that of the diversity-dependent models. These two latter sets of analyses are 238 described in detail in the Supplementary Appendix 2. 239 To assess the ability to correctly identify the matching competition model when it is the 240 generating model, we compared the fit (measured by AICc, Burnham and Anderson 2002) of this

model to other commonly used trait models on the same data (i.e. data simulated under the

matching competition model). Specifically, we compared the matching competition model to (1)

241

242

- 243 Brownian motion (BM), (2) Ornstein-Uhlenbeck/single-stationary peak model (OU, Hansen &
- 244 Martin 1996), (3) exponential time-dependent (TD_{exp}, i.e., the early burst model, or the ACDC
- 245 model with the rate parameter set to be negative, Blomberg et al. 2003; Harmon et al. 2010), (4)

246	linear time-dependent evolutionary rate (TD_{lin} , Weir and Mursleen 2013), (5) linear rate
247	diversity-dependent (DD _{lin} , Mahler et al. 2010; Weir and Mursleen 2013), and (6) exponential
248	rate diversity-dependent (DD _{exp} , Weir and Mursleen 2013). These models were fitted using
249	geiger (Harmon et al. 2008) when available there (BM, OU, TD_{exp} , TD_{lin}), or using our own
250	codes, available in RPANDA (Morlon et al. MS) when they were not available in geiger (DD_{lin} ,
251	DD_{exp}). With the exception of TD_{exp} , which we restricted to have decreasing rates through time
252	since it has recently been shown that the accelerating rates version of the model is unidentifiable
253	from OU (Uyeda et al. 2015), we did not restrict the ML search for the parameters in TD_{lin} or DD
254	models.
255	We assessed the identifiability of other trait models against the matching competition
256	model by calculating the fit of this model to datasets simulated under the same trait models
257	mentioned above. For BM and OU models, we generated datasets from simulations using
258	parameter values from the appendix of Harmon et al. 2010 scaled to a tree of length 400 (BM, σ^2
259	= 0.03; OU, σ^2 = 0.3, α = 0.06). For both the linear and exponential versions of the time- and
260	diversity-dependent models, we simulated datasets with starting rates of $\sigma^2 = 0.6$ and ending
261	rates of $\sigma^2 = 0.01$, declining with a slope determined by the model and tree (e.g., for time-
262	dependent models, the slope is a function of the total height of the tree; for the TD_{exp} model,
263	these parameters result in a total of 5.9 half-lives elapsing from the root to the tip of the tree,
264	Slater and Pennell 2014). In another set of simulations, we fixed the tree size at 100 tips and
265	varied parameter values to determine the effect of parameter values on identifiability (see
266	Results). As above, we calculated the AICc for all models for each simulated dataset.
267	

268	Finally, to understand how removing stabilizing selection from the likelihood of the
269	matching competition model affects our inference in the presence of stabilizing selection, we
270	simulated datasets with both matching competition and stabilizing selection on 100 tip trees,
271	across a range of parameter space (S = -1, -0.5, and 0, α = 0.05, 0.5, and 5, holding σ^2 at 0.05).
272	We fit BM, OU, and matching competition models to these simulated datasets. All simulations
273	were performed using our own codes, available in RPANDA (Morlon 2014).
274	

275 Fitting the Matching Competition Model of Trait Evolution to Caribbean Anolis Lizards

276 To determine whether the matching competition model is favored over models that ignore 277 interspecific interactions in an empirical system where competition likely influenced character 278 evolution, we fit the matching competition model to a morphological dataset of adult males from 279 100 species of Greater Antillean Anolis lizards and the time calibrated, maximum clade 280 credibility tree calculated from a Bayesian sample of molecular phylogenies (Mahler et al. 2010, 281 2013; Mahler and Ingram 2014). We included the first four size-corrected phylogenetic principal 282 components from a set of 11 morphological measurements, collectively accounting for 93% of 283 the cumulative variance explained (see details in Mahler et al. 2013). Each of these axes is 284 readily interpretable as a suite of specific morphological characters (see Discussion), and 285 together, the shape axes quantified by these principal components describe the morphological 286 variation associated with differences between classical ecomorphs in Caribbean anoles (Williams 287 1972). In addition to the matching competition model, we fit the six previously mentioned 288 models (BM, OU, TD_{exp}, TD_{lin}, DD_{exp}, and DD_{lin}) separately to each phylogenetic PC axis in the 289 Anolis dataset.

For the matching competition model and diversity-dependent models, to determine the influence of uncertainty in designating clades as sympatric and allopatric, we fit the model for each trait using 101 sets of geography matrices (i.e., **A** in Eq. 1b, 2, & 3, see Fig. 1): one where all lineages were set as sympatric, and the remaining 100 with biogeographical reconstructions from the output of the make.simmap function in phytools (Revell 2012). To simplify the ML optimization, we restricted *S* to take negative values while fitting the matching competition model including the biogeographical relationships among taxa.

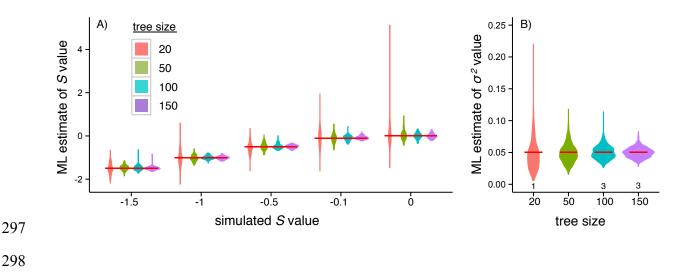
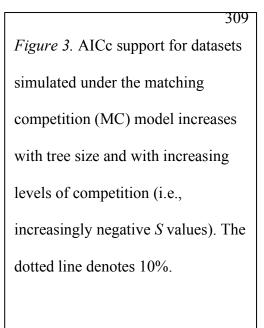


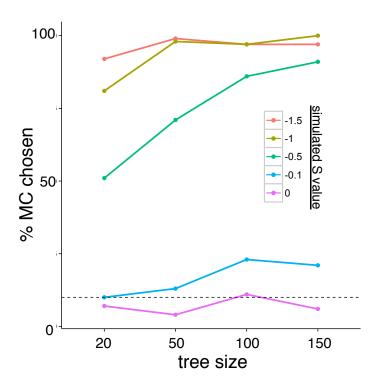
Figure 2. Parameter estimation under the matching competition model. As tree size increases and/or the magnitude of competition increases (i.e., the *S* parameter in the matching competition model becomes more negative), so does the accuracy of ML parameter estimates of (A) *S* (n = 100 for each tree size and *S* value combination; red horizontal lines indicate the simulated *S* value) and (B) σ^2 (n = 500 for each tree size; red horizontal lines indicate the simulated value). In a small number of cases (7/2000), the ML estimate for σ^2 was unusually large (> 0.25), and we removed these rare cases for plotting. The numbers below the violin plots in (B) show the number of outliers removed for each tree size.

299 **RESULTS**

300 Statistical Properties of the Matching Competition Model

301 Across a range of S values, maximum likelihood optimization returns reliable estimates 302 of parameter values for the matching competition model (Fig. 2). As the number of tips 303 increases, so does the reliability of maximum likelihood parameter values (Fig. 2). Parameter 304 estimates remain reliable in the presence of extinction, unless the extinction fraction is very large 305 (i.e., ≥ 0.6 ; Supplementary Appendix 2). When datasets are simulated under the matching 306 competition model, model selection using AICc generally picks the matching competition model 307 as the best model (Figs. 3, S1); the strength of this discrimination depends on both the S value 308 used to simulate the data and the size of the tree (Figs. 3, S1).







312	Simulating datasets under BM, OU, DD_{exp} , and DD_{lin} generating models, we found that in
313	most scenarios, and in most parameter space, these models are distinguishable from the matching
314	competition model (Fig. 4a,b,e,f, Fig. S2). As with the matching competition model, the ability
315	to distinguish between models using AICc generally increases with increasing tree sizes (Fig. 4)
316	and with increasing magnitude of parameter values (Fig. S2). When character data were
317	simulated under a TD_{lin} model of evolution, the matching competition and/or the diversity-
318	dependent models tended to have lower AICc values than the TD_{lin} model, especially among
319	smaller trees (Figure 4d). For data generated under a TD _{exp} model, model selection always
320	favored the matching competition model over the TD_{exp} model (Fig. 4c).
321	As the strength of stabilizing selection increases relative to the strength of competition
322	(i.e., α as increases relative to S) AICc model selection shifts from favoring the matching
323	competition model (under large S, small α scenarios) to favoring the OU model (under small S,
324	large α scenarios) (Fig. S3). Likewise, maximum likelihood increasingly underestimates the
325	value of S as the value of α increases (Fig. S4).
326	
327	Competition in Greater Antillean Anolis Lizards
328	For the first four phylogenetic principal components describing variation in Anolis
329	morphology, we found that models that incorporate species interactions fit the data better than
330	models that ignore them (Table 1). PC1, which describes variation in hindlimb/hindtoe length
221	

- 331 (Mahler et al. 2013), is fit best by the matching competition model. PC2, which describes
- 332 variation in body size (snout vent length) is fit best by the linear diversity-dependent model.
- 333 PC3, which describes variation in forelimb/foretoe length, and PC4, which describes variation in

- 334 lamellae number are fit with mixed support across the models included, but with models
- incorporating species interactions providing the best overall fits.

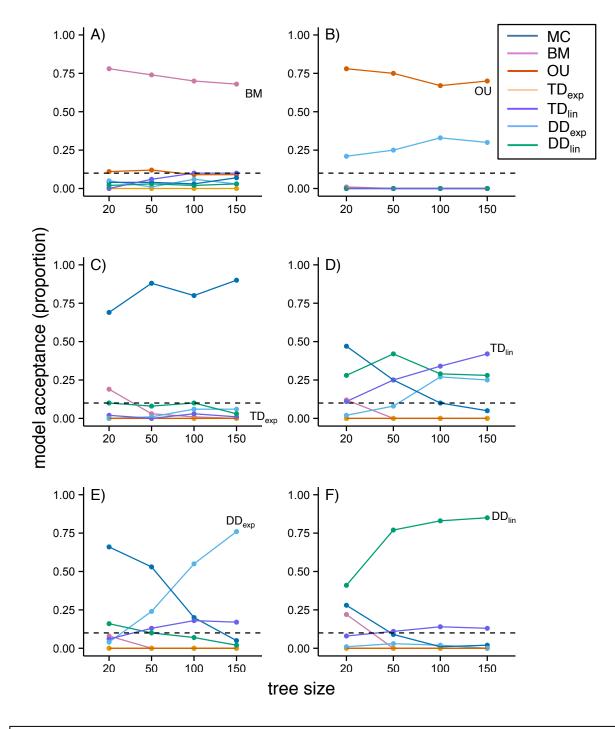


Figure 4. Identifiability simulation results for the matching competition (MC) model. When the generating model is either (A) BM, (B) OU, (E) DD_{exp} (for larger trees) or (F) DD_{lin} , the generating model is largely favored by model selection. However, both (C) TD_{exp} and (D) TD_{lin} (for smaller 18 trees) are erroneously rejected as the generating model. The dotted lines denote 10%.

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337 Additionally, for every PC axis, the best-fit models were ones that incorporated the geographic

relationships among species in the tree, and these conclusions were robust to uncertainty in

ancestral reconstructions of sympatry (Table 1).

340

Table 1. Comparison of model fits for the first four phylogenetic principal components of a morphological dataset of Greater Antillean anoles. Models run incorporating geography matrices are indicated by "+ GEO", and models with the lowest AICc for each trait are shaded and written in bold text. Parameter values presented follow the nomenclature of Eqs. 2-4 in the main text, and *k* represents the number of parameters estimated for each model. Note that TD_{exp} is the ACDC model (or the early-burst model when r < 0). OU model weights were excluded because the ML estimates of α equaled 0 for all PC axes, and thus the OU model was equivalent to BM. Median (standard error) of parameter estimates, Δ AICc values, and Akaike weights are presented for fits across 100 sampled stochastic maps of *Anolis* biogeography (standard errors are omitted for Akaike weights < 0.05).

PPC1 BM OU TD6 TD1 TD1 DD	N	c	0.000						
				I		I	-13.68	21 36 (0 10)	<0.01
		1 (1	0.0033				12.69		10.02
		n d					00.01-		
11 II II	ILLexp	r	0.0324		-0.068		07.6-	(61.0) 16.0	0.03
DI	TDlinear	m	0.0113	-0.019			-4.88	5.89(0.19)	0.04
	DDexp	ę	0.0184		-0.028		-4.37	4.87(0.19)	0.06(0.004)
D	DDexp + GEO	ς	0.0087 (1.48E-5)		-0.043 (7.29E-5)		-8.00 (0.050)	12.05 (0.19)	<0.01
DI	DDlin	б	0.0089	-0.00008			-4.89	5.91 (0.19)	0.04
DI	DDlin + GEO	۲	0 0060 (6 25E-6)	-0 00011 (1 24E-7)			-8 23 (0 034)	12 49 (0 18)	<0.01
W	MC	. "	0.0010		I	-0.037	-3.67	2 96 (0 19)	0 16 (0 01)
M		n 4	0.0010 (6.75F 6)			0.038 (0.0017)	1 04 /0 10)	0.00.031)	(10.0) 01.0
		- - -	0.0010 0100.0			(TTOOP) 0000-	(01.0) +(.1-		770.00 00.0
pPC2 BM	М	ы	0.0027				-4.69	9.64(0.036)	0.01
00	Ĺ	m	0.0027				-4.69	1	
II	TDexp	m	0.0046		-0.014		-4.30	10.99 (0.036)	<0.01
TD	TDlinear	б	0.0047	-0.011			-4.23	10.85 (0.036)	<0.01
DI	DDexn	ć	0.0041		-0.006		-4.27	10.94 (0.036)	<0.01
JU	DDexn + GEO	"	0 0068 (1 36E-5)		-0 039 (9 72E-5)		0.51 (0.024)	1 37 (0 015)	0 33 (0 002)
DI	DDlin	5	0.0042	-0.00002			-4.21	10.82 (0.036)	<0.01
JU	DDlin + GEO	"	0 0054 (4 24F-6)	-0 00010 (9 17F-8)	I		1 20 (0 017)	0.00	0.64 (0.001)
		, 6	0.0001			0.05.2	2.05	0 70 /0 036)	
		n c	0.0019 /7 44E 6/			-9.90-3 0.015/1/27E 51		(0000) 61.6	10.0/
	MC + GEO	n	U.UUIS (2.44E-0)			(C-3/0.4) CIU.U-	-2.94 (0.010)	(140.0) UC.8	10.0
pPC3 BM	И	2	0.0010				45.57	2.56(0.021)	0.09(0.0003)
00	Ĺ	ŝ	0.0010				45.57	1	
TL	TDexp	ę	0.0020		-0.019		46.30	3.22 (0.021)	0.06(0.0002)
TL	TDlinear	ę	0.0019	-0.013			46.41	3.02 (0.021)	0.07 (0.0003)
DL	DDexp	б	0.0017		-0.008		46.40	3.02 (0.021)	0.07 (0.0003)
DI	DDexn + GEO	С	0.0015 (1.48E-6)		-0.017 (3.72E-5)		46.79 (0.006)	2.24 (0.024)	0.10 (0.0006)
JU	DDlin	"	0 0017	-0 000009			46.46	2.90 (0.021)	0.08 (0.0003)
IQ	DDlin + GEO) (r	0.0014 (8.76E-7)	-0.000016 (2.96E-8)			46 68 (0 005)	2.44 (0.023)	0.09 (0.0005)
ШW	MC	. "	0.0007			-0.012	46.75	2.33 (0.021)	0.10 (0.0004)
	MC + GEO	e	0.0006 (6.15E-7)			-0.017 (3.38E-5)	47.91 (0.011)	0 (0)	0.32 (0.002)
pPC4 BM	И	7	0.0006				69.07	2.50 (0.016)	0.06 (0.0002)
00	Ĺ	ę	0.0006				69.07	1	, ,
II	TDexp	б	0.0015		-0.025		70.55	1.66(0.016)	0.09 (0.0003)
TD	TDlinear	ę	0.0012	-0.013			70.45	1.86(0.016)	0.08 (0.0003)
DI	DDexn	С	0.0012		-0.010		70.52	1.73(0.016)	0.08 (0.0003)
DL	DDexp + GEO	ŝ	0.0010 (1.18E-6)		-0.020 (4.38E-5)		71.28 (0.011)	0.13 (0.020)	0.18 (0.001)
DL	DDlin	ę	0.0011	-0.00006			70.39	1.99(0.016)	0.07 (0.0002)
DI	DDlin + GEO	б	0.0009 (5.77E-7)	-0.000009 (1.98E-8)			70.78 (0.008)	1.12 (0.016)	0.11 (0.0006)
MC	D	ę	0.0004			-0.015	71.1	0.57(0.016)	0.15 (0.0005)
M	MC+GEO	e	0.0004 (4.21E-7)		I	-0.016 (3.56E-5)	71.34 (0.009)	0 (0.012)	(100.0)(0.10)
	-							(

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344 **DISCUSSION**

The inference methods we present here represent an important new addition to the comparative trait analysis toolkit. Whereas previous models had not accounted for the influence of trait values in other lineages on character evolution, the matching competition model takes these into account. Furthermore, extending both the matching competition model and two diversity-dependent trait evolution models to incorporate geographic networks of sympatry further extends the utility and biological realism of these models.

351 We found that the matching competition model has increasing AICc support and 352 accuracy of parameter estimation with increasing tree sizes and competition strength. We also 353 found that, for most of the generating models we tested, AICc-based model selection does not 354 tend to erroneously select the matching competition model (i.e., these models are identifiable 355 from the matching competition model). As with all other models, the statistical properties of the 356 matching competition model will depend on the size and shape of a particular phylogeny as well 357 as specific model parameter values. Future investigators can employ other approaches, such as 358 phylogenetic Monte Carlo and posterior predictive simulations directly on their empirical trees 359 (Boettiger et al. 2012, Slater & Pennell 2014), to assess the confidence they can have in their 360 results.

We did, however, find that data generated under time-dependent models were often fit better by models that incorporate interspecific interactions (i.e., density-dependent and matching competition models) (Fig. 4c,d). This was especially true for the TD_{exp} model, often referred to as the early-burst model—the matching competition model nearly always fit data generated under the TD_{exp} model better than the TD_{exp} model (Fig. 4c). We do not view this as a major limitation of the model for two reasons. First, the TD_{exp} model is known to be statistically

367 difficult to estimate on neontological data alone (Harmon et al. 2010; Slater et al. 2012a; Slater 368 and Pennell 2014). Secondly, and more importantly, time-dependent models are not process-369 based models, but rather incorporate time since the root of a tree as a proxy for ecological 370 opportunity or available niche space (Harmon et al. 2010; Mahler et al. 2010; Slater 2015). The 371 matching competition and density-dependent models explicitly account for the interspecific 372 competitive interactions that time-dependent models purport to model, thus we argue that these process-based models are more biologically meaningful than time-dependent models (Moen and 373 374 Morlon 2014).

375 We did not incorporate stabilizing selection in our model. Preliminary analyses suggested 376 that S and α are not identifiable, as competition and stabilizing selection operate in opposite 377 directions. As a result, when trait data are simulated with simultaneous stabilizing selection and 378 matching competition, the strength of competition is underestimated. In addition, which model is 379 chosen by model selection depends on the ratio of the strength of attraction toward an optimum 380 to the strength of competition, with Brownian model being selected at equal strengths (Figs. S3, 381 S4). Given that many traits involved in competitive interactions are also likely to have been subject to stabilizing selection (i.e., extreme trait values eventually become targeted by negative 382 383 selection), statistical inference under the matching competition model without stabilizing 384 selection is likely to underestimate the true effect of competition on trait evolution. Future work 385 aimed at directly incorporating stabilizing selection in the inference tool could provide a more 386 accurate quantification of the effect of competition, although dealing with the non-identifiability 387 issue may require incorporating additional data such as fossils.

388 Because the matching competition model depends on the mean trait values in an evolving 389 clade, maximum likelihood estimation is robust to extinction, whereas the diversity-dependent

models are less so (Appendix S2, Figs. S5-S8). Nevertheless, given the failure of maximum likelihood to recover accurate parameter estimates of the matching competition model at high levels of extinction (μ : $\lambda \ge 0.6$), we suggest that these models should not be used in clades where the extinction rate is known to be particularly high. In such cases, it would be preferable to modify the inference framework presented here to include data from fossil lineages (Slater et al. 2012a) by adapting the ordinary differential equations described in Eq. 3a and 3b for nonultrametric trees.

397 For all of the traits we analyzed, we found that models incorporating both the influence of 398 other lineages and the specific geographical relationships among lineages were the most strongly 399 supported models (though less strikingly for PC3 and PC4). Incorporating uncertainty in 400 biogeographical reconstruction, which we encourage future investigators to do in general, 401 demonstrated that these conclusions were robust to variation in the designation of allopatry and 402 sympatry throughout the clade. The matching competition model is favored in the phylogenetic 403 principal component axis describing variation in relative hindlimb size. Previous research 404 demonstrates that limb morphology explains between-ecomorph variation in locomotive 405 capabilities and perch characteristics (Losos 1990, 2009; Irschick et al. 1997), and our results 406 suggest that the evolutionary dynamics of these traits have been influenced by the evolution of 407 limb morphology in other sympatric lineages. These results support the assumption that 408 interspecific interactions resulting from similarity in trait values are important components of 409 adaptive radiations (Losos 1994, Schluter 2000), a prediction that has been historically difficult 410 to test (Losos 2009, but see Mahler et al. 2010). In combination with previous research 411 demonstrating a set of convergent adaptive peaks in morphospace to which lineages are attracted 412 (Mahler et al. 2013), our results suggest that competition likely played an important role in

413 driving lineages toward these distinct peaks. Because we expect the presence of selection toward 414 optima to lead to underestimation of the S parameter in the matching competition model (Figs. 415 S3, S4), we would have likely detected an even stronger effect of competition in *Anolis* dataset if 416 we had included stabilizing selection. Recently, Uyeda and colleagues (2015) demonstrated that 417 the use of principal components can bias inferences of trait evolution. We used BM-based 418 phylogenetic PC axes here, which should reduce this potential bias (Revell 2009). We recognize 419 that there is some circularity in assuming BM in order to compute phylogenetic PC axes before 420 fitting other trait models to these axes; a general solution to address this circularity problem 421 remains to be found (Uyeda et al. 2015). Uyeda & colleagues suggested that using phylogenetic 422 PC axes sorts the traits according to specific models. In the Greater Antillean Anolis lizards, the 423 first axes are easily interpretable as specific suite of traits relevant to competitive interactions, 424 and our results suggest that competition played an important role in shaping the evolution of 425 these traits.

426 The linear version of Nuismer & Harmon's (2015) model (Eq. 1) results from making the 427 simplifying assumption that competitive interactions are approximately equivalent across all 428 sympatric taxa. We used this version here, since currently available likelihood tools for trait 429 evolution rely on the multivariate normal distribution, which is to be expected only for this linear 430 form of the model. The current formulation (Eq. 1) corresponds to a scenario in which the rate of 431 phenotypic evolution in a lineage gets higher as the lineage deviates from the mean phenotype, 432 although character displacement theory, for example, posits that selection for divergence should 433 be the strongest when species are most ecologically similar (Brown and Wilson 1956). 434 Nevertheless, the developments presented here provide an important new set of tools for 435 investigating the impact of interspecific interactions on trait evolution, and researchers can

436 perform posterior simulations to assess the realism of the resulting inference. Future 437 development of likelihood-free methods, such as Approximate Bayesian Computation (Slater et 438 al. 2012b; Kutsukake and Innan 2013), may be possible for fitting the version of the model in 439 which the outcome of competitive interactions depend on distance in trait space. 440 We imagine that the matching competition model and biogeographical implementations 441 of diversity-dependent models will play a substantial role in the study of interspecific 442 competition. For example, by comparing the fits of the matching competition model with other 443 models that do not include competitive interactions between lineages, biologists can directly test 444 hypotheses that make predictions about the role of interspecific interactions in driving trait 445 evolution. In other words, while the effect of competition has been historically difficult to detect 446 (Losos 2009), it may be detectable in the contemporary distribution of trait values and their 447 covariance structure (Hansen and Martins 1996; Nuismer and Harmon 2015). The ability to 448 consider trait distributions among species that arise from a model explicitly accounting for the 449 effect of species interactions on trait divergence is also an important step toward a more coherent 450 integration of macroevolutionary models of phenotypic evolution in community ecology. 451 There are many possible extensions of the tools developed in this paper. In the future, 452 empirical applications of the model can be implemented with more complex geography matrices

that are more realistic for mainland taxa (e.g., using ancestral biogeographical reconstruction,
Ronquist and Sanmartín 2011; Landis et al. 2013), and can also specify degrees of sympatric
overlap (i.e., syntopy). Additionally, the current version of the model is rather computationally
expensive with larger trees (with 100 or more tips). Further work developing an analytical
solution to the model may greatly speed up the likelihood calculation and permit the inclusion of
stabilizing selection.

459	The current form of the model assumes that the degree of competition is equal for all
460	interacting lineages. Future modifications of the model, such as applications of stepwise AICc
461	algorithms (Alfaro et al. 2009; Thomas and Freckleton 2012; Mahler et al. 2013) or reversible-
462	jump Markov Chain Monte Carlo (Pagel and Meade 2006; Eastman et al. 2011; Rabosky 2014;
463	Uyeda and Harmon 2014), may be useful to either identify more intensely competing lineages or
464	test specific hypotheses about the strength of competition between specific taxa. Improvements
465	could also be made on the formulation itself of the evolution of a species' trait as a response to
466	the phenotypic landscape in which the species occurs. Moreover, a great array of extensions will
467	come from modeling species interactions not only within clades, but also among interacting
468	clades, as in the case of coevolution in bipartite mutualistic or antagonistic networks, such as
469	plant-pollinator or plant-herbivore systems.

470

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624 Supplementary Material625

- 626 Appendix S1 & S2
- 628 Table S1
- 630 Figure S1-S8

1 Supplementary Appendix 1

Considering that n lineages are interacting at time t, each trait i evolves following the equation :

$$dz_{i}(t) = z_{i}(t+dt) - z_{i}(t) = S\left(\left(\frac{1}{n_{i}}\sum_{l=1}^{n}A_{i,l}z_{l}(t)\right) - z_{i}(t)\right)dt + \sigma dB_{i}(t)$$

Where $A_{i,l}$ is equal to 1 if lineages *i* and *l* are sympatric, and to 0 otherwise, $n_i = \sum_{l=1}^n A_{i,l}$ is the total number of lineages in sympatry with lineage *i*, and $B_i(t)$ represents standard Brownian motion.

Here, we present the derivation of Equations 3a and 3b from the main text. To make the derivation easier to follow, we drop the dependence on time t, replacing $z_i(t)$ with z_i and $B_i(t)$ with B_i .

First, applying the Itô formula to these stochastic processes gives us :

$$d(z_i z_j) = z_i dz_j + z_j dz_i + d < z_i, z_j >$$

$$= S\left(\left(\frac{1}{n_j} \sum_{l=1}^n A_{j,l} z_l z_i\right) - z_j z_i\right) dt + \sigma z_i dB_j$$

$$+ S\left(\left(\frac{1}{n_i} \sum_{k=1}^n A_{i,k} z_k z_j\right) - z_j z_i\right) dt + \sigma z_j dB_i$$

$$+ \sigma^2 \mathbf{1}_{i=j} dt$$

where $1_{i=j}$ equals one if i = j and zero otherwise.

Taking this expectation, it follows that :

$$\frac{d}{dt}\mathbb{E}(z_i z_j) = S\left(\left(\frac{1}{n_j}\sum_{l=1}^n A_{j,l}\mathbb{E}(z_l z_l)\right) - \mathbb{E}(z_j z_i)\right)dt + S\left(\left(\frac{1}{n_i}\sum_{k=1}^n A_{i,k}\mathbb{E}(z_k z_j)\right) - \mathbb{E}(z_j z_i)\right)dt + \sigma^2 \mathbf{1}_{i=j}dt$$

Moreover, we get :

$$\frac{d}{dt}\mathbb{E}(z_i) = S\left(\left(\frac{1}{n_i}\sum_{l=1}^n A_{i,l}\mathbb{E}(z_l)\right) - \mathbb{E}(z_i)\right)dt$$

which leads to :

$$\frac{d}{dt} \left(\mathbb{E}(z_i) \mathbb{E}(z_j) \right) = \mathbb{E}(z_j) \frac{d}{dt} \mathbb{E}(z_i) + \mathbb{E}(z_i) \frac{d}{dt} \mathbb{E}(z_j)
= S\left(\left(\frac{1}{n_i} \sum_{k=1}^n A_{i,k} \mathbb{E}(z_k) \mathbb{E}(z_j) \right) - \mathbb{E}(z_i) \mathbb{E}(z_j) \right) dt
+ S\left(\left(\frac{1}{n_j} \sum_{l=1}^n A_{j,l} \mathbb{E}(z_l) \mathbb{E}(z_l) \right) - \mathbb{E}(z_j) \mathbb{E}(z_i) \right) dt$$

Taking together these different parts gives us the ODE satisfied by all covariances (denoted $v_{i,j} = Cov(z_i, z_j)$):

$$\frac{d}{dt}v_{i,j} = \frac{d}{dt} \left(\mathbb{E} \left(z_i z_j \right) - \mathbb{E} (z_i) \mathbb{E} (z_j) \right) \\
= -2Sv_{i,j} + \frac{S}{n_i} \sum_{k=1}^n A_{i,k} v_{k,j} + \frac{S}{n_j} \sum_{l=1}^n A_{j,l} v_{l,i} + \sigma^2 \mathbf{1}_{i=j} \tag{1}$$

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Using these derivations, the variance terms (i = j) are calculated using:

$$\frac{d}{dt}v_{i,i} = -\frac{2S(n_i - 1)}{n_i}v_{i,i} + \frac{2S}{n_i}\sum_{\substack{l=1\\l\neq i}}^n A_{i,l}v_{l,i} + \sigma^2$$
(2)

The covariance terms $(i \neq j)$ are calculated using:

$$\frac{d}{dt}v_{i,j} = -S\left(\frac{n_i - 1}{n_i} + \frac{n_j - 1}{n_j}\right)v_{i,j} + \frac{S}{n_i}\sum_{\substack{k=1\\k \neq i}}^n A_{i,k}v_{k,j} + \frac{S}{n_j}\sum_{\substack{l=1\\l \neq j}}^n A_{j,l}v_{l,i}$$
(3)

In the case where lineages i and j are in sympatry, this formula simplifies to:

$$\frac{d}{dt}v_{i,j} = -\frac{2S(n_i - 1)}{n_i}v_{i,j} + \frac{S}{n_i} \left(\sum_{\substack{k=1\\k\neq i}}^n A_{i,k}v_{k,j} + \sum_{\substack{l=1\\l\neq j}}^n A_{j,l}v_{l,i}\right)$$
(4)

To solve the ODEs for the variance and covariance terms from the root to the tip, we begin by fixing the variance v_0 for the process at the root to 0. At each speciation event, the starting value for both the variance of each of the new lineages and the covariance between the two new lineages is the variance of the immediate ancestor at the time of the speciation event, and the starting value for the covariance between the new lineages and any other persisting lineage is set to the value of the covariance between the persisting lineage and the ancestor of the new lineages at the time of speciation.

636 Supplementary Appendix 2: Estimating the effect of extinction on parameter estimation for 637 the matching competition and density-dependent models.

638

639 Given that the matching competition and diversity-dependent models take into account 640 the number of interacting lineages, extinction may affect our ability to recover true parameter 641 values. To estimate the impact of extinction, we simulated 100 trees with 100 extant species, 642 varying the extinction fraction (μ : $\lambda = 0.2, 0.4, 0.6, \text{ and } 0.8$). As above, we recursively simulated traits using the matching competition model with $\sigma^2 = 0.05$ and S = -1.5, -1, -0.5, -0.1, or 0, and 643 the linear and exponential diversity-dependent models with starting rates of $\sigma^2 = 0.6$ and ending 644 645 rates of $\sigma^2 = 0.01$. We then estimated the maximum likelihood parameter estimates for the 646 generating models by fitting the models to the trait values for extant species and the tree with 647 extinct lineages removed. In the case of the matching competition model, because many 648 simulated birth-death trees with high extinction rates have substantially older root ages, the 649 simulated trait datasets for some trees had very large variances. For these biologically unrealistic trait datasets (i.e., variance in trait values $\geq 1 \times 10^8$), ML does not yield reliable parameter 650 651 estimates, so we removed them from further analyses (the sample size of included simulations is 652 reported in Fig. S5, S6).

Parameter estimates are quite robust to extinction under the matching competition model (Fig. S5, S6), and much more so than under both diversity-dependent models (Fig. S7, S8). Under the matching competition model, the maximum likelihood optimization returns reliable estimates of *S* and σ^2 values used to simulate datasets on trees with extinct lineages (Fig. S5, S6), although the estimates become much less reliable with larger extinction fractions, likely because simulations under the matching competition model were unbounded, resulting in trait

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- 659 datasets with biologically unrealistic variances. Under both diversity-dependent models, the
- 660 magnitude of both the slope and σ^2 parameter values are increasingly underestimated with
- 661 increasing extinction fractions (Fig. S7, S8).

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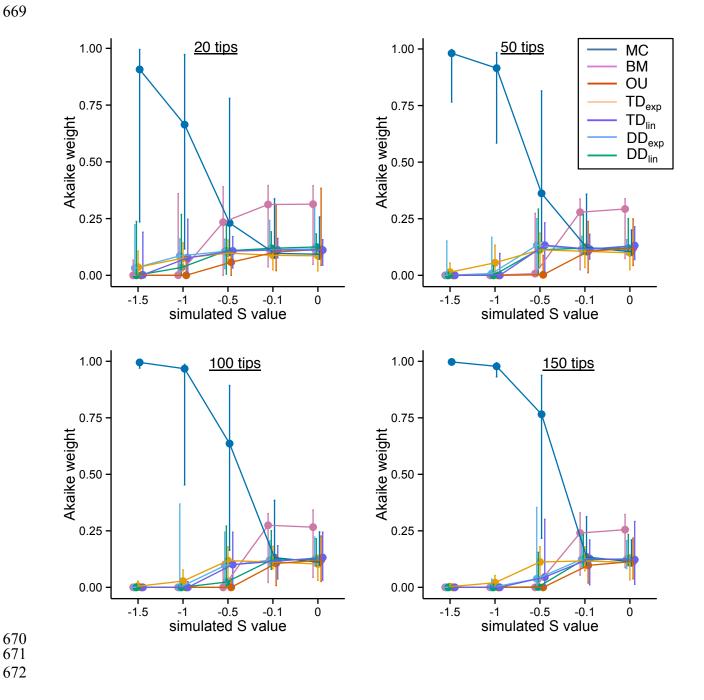
665 Supplementary Figure 1. As tree size and/or the degree of competition (S) increases, model

666 selection becomes more reliable. Comparison of Akaike weights (median & 90% CIs) for NH,

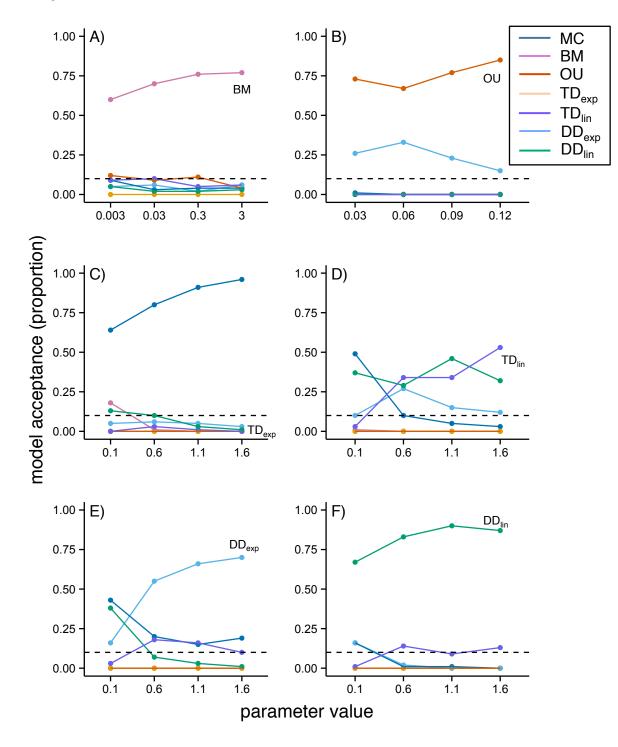
BM, OU, and EB models when simulated under various levels of competition (S = -1.5, -1, -0.5, 667

668 -0.1, and 0) for trees with 20, 50, 100, and 150 tips.

669

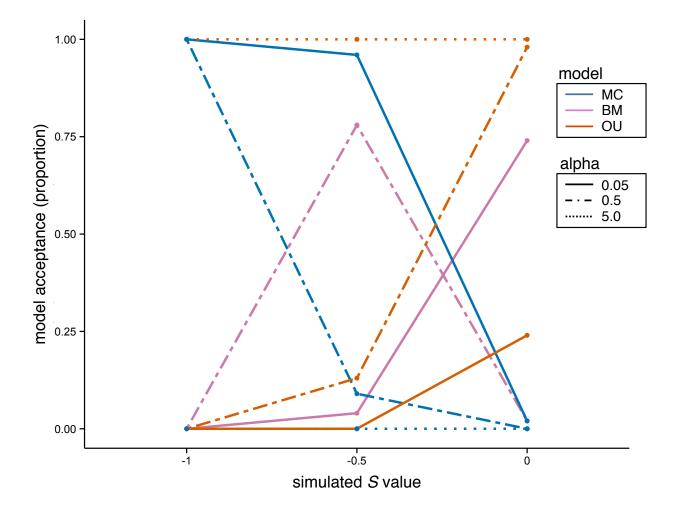


- 673 Supplementary Figure 2. Identifiability simulation results for the matching competition model as
- 674 a function of varying parameter values of the generating models. Parameter values are (A) σ^2 for
- 675 BM, (B) α for OU (σ^2 was fixed at 0.3), and the σ^2 value at the root for (C) TD_{exp}, (D) TD_{lin}, (E)
- 676 DD_{exp} , and (F) DD_{lin} (for C-F, σ^2 at the present was fixed at 0.01).

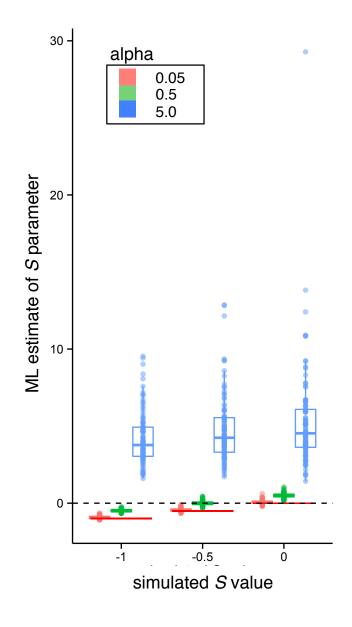


678 *Supplementary Figure 3.* The effect of incorporating stabilizing selection into trait evolution on 679 model selection. For datasets generated under the matching competition model with stabilizing 680 selection included, as the ratio of the strength competition (*S*) to the strength of selection toward 681 an optimum (α) varies, so does the model preferred by model selection.

682

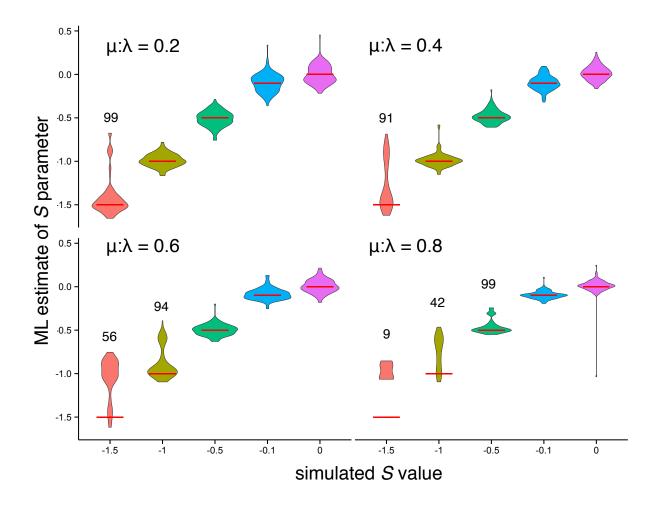


Supplementary Figure 4. The effect of incorporating stabilizing selection into trait evolution on parameter estimation. As the strength of stabilizing selection increases (i.e., as α increases), maximum likelihood under the matching competition model underestimates the true *S* value used to simulate datasets. Positive *S* values represent selection toward, rather than away, from the clade mean and are thus expected when the ratio of α to *S* is large. The horizontal red line represents the simulated *S* value, and the dashed horizontal line represents S = 0.

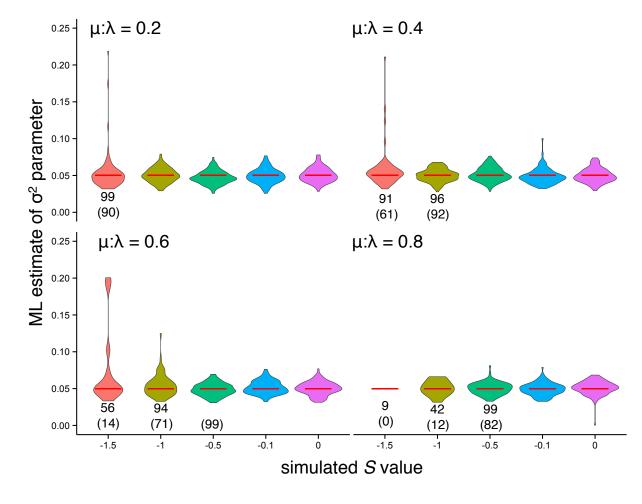




Supplementary Figure 5. Simulation results showing the effect of varying the extinction fraction
on estimation of the *S* parameter for the matching competition model. Red horizontal lines
indicate the simulated *S* values, and numbers above sets of simulations indicate the sample size
of included simulations under those scenarios (see main text for more details).

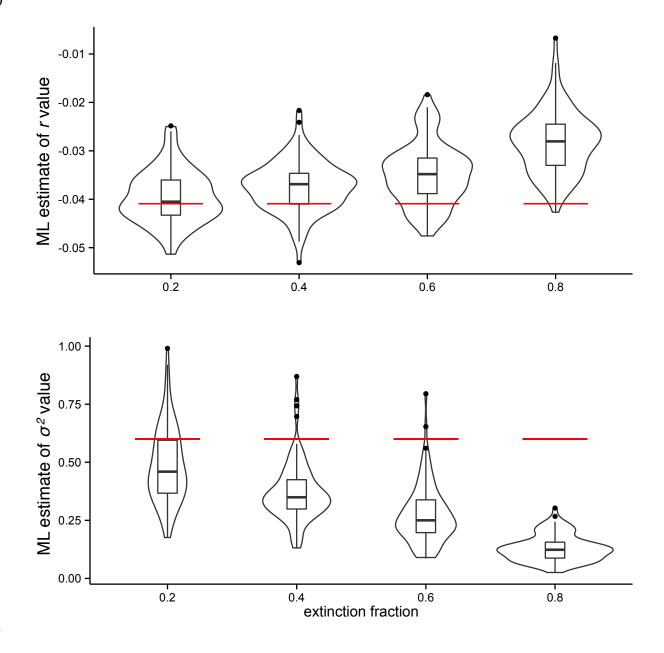


698 Supplementary Figure 6. Simulation results showing the effect of varying the extinction fraction 699 on estimation of the σ^2 parameter for the matching competition model. Red horizontal lines 700 indicate the simulated σ^2 value (0.05), the numbers below sets of simulations indicate the sample 701 size of included simulations under those scenarios (see main text for more details), and the 702 number in parentheses indicate sample size after σ^2 values > 0.25 were removed.





706Supplementary Figure 7. Simulation results showing the effect of varying the extinction fraction707on slope (top) and σ^2 (bottom) parameters for the exponential diversity-dependent model.708Increasing extinction levels result in increasingly underestimated slope values and σ^2 parameters.709Red horizontal lines indicate the simulated parameter values.



712 Supplementary Figure 8. Simulation results showing the effect of varying the extinction fraction 713 on slope (top) and sigma-squared (bottom) parameters for the linear diversity-dependent model. 714 Increasing extinction levels result in increasingly underestimated slope values and σ^2 parameters. 715 Red horizontal lines indicate the simulated parameter values.

716

