Co-estimating Reticulate Phylogenies and Gene Trees from Multi-locus Sequence Data

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Abstract.— The multispecies network coalescent (MSNC) is a stochastic process that captures how gene trees grow within the branches of a phylogenetic network. Coupling the MSNC with a stochastic mutational process that operates along the branches of the gene trees gives rise to a generative model of how multiple loci from within and across species evolve in the presence of both incomplete lineage sorting (ILS) and reticulation (e.g., hybridization). We report on a Bayesian method for sampling the parameters of this generative model, including the species phylogeny, gene trees, divergence times, and population sizes, from DNA sequences of multiple independent loci. We demonstrate the utility of our method by analyzing simulated data and reanalyzing three biological data sets. Our results demonstrate the significance of not only co-estimating species phylogenies and gene trees, but also accounting for reticulation and ILS simultaneously. In particular, we show that when gene flow occurs, our method accurately estimates the evolutionary histories, coalescence times, and divergence times. Tree inference methods, on the other hand, underestimate divergence times and overestimate coalescence times when the evolutionary history is reticulate. While the MSNC corresponds to an abstract model of "intermixture," we study the performance of the model and method on simulated data generated under a gene flow model. We show that the method accurately infers the most recent time at which gene flow occurs. Finally, we demonstrate the application of the new method to a 106-locus yeast data set. [Multispecies network coalescent; reticulation; incomplete lineage sorting; phylogenetic network; Bayesian inference; RJMCMC.]

The availability of sequence data from multiple loci 1 across the genomes of species and individuals within species is enabling accurate estimates of gene and species evolutionary histories, as well as parameters such as divergence times and ancestral population sizes (Rannala and Yang 2003). Several statistical methods have been developed for obtaining such estimates (Bouckaert et al. 2014; Edwards et al. 2007; Heled and Drummond 2010; Rannala and Yang 2003). All these methods employ the multispecies coalescent (Degnan and Rosenberg 2009) 10 as the stochastic process that captures the relationship 11 between species trees and gene genealogies. 12

As evidence of hybridization (admixture between 13 different populations of the same species or across 14 different species) continues to accumulate (Arnold 1997; 15 Barton 2001; Gogarten et al. 2002; Koonin et al. 16 17 2001; Mallet 2005, 2007; Rieseberg 1997), there is a pressing need for statistical methods that infer species 18 phylogenies, gene trees, and their associated parameters 19 in the presence of hybridization. We recently introduced for this purpose the *multispecies network coalescent* 21 (MSNC) along with a maximum likelihood search 22 heuristic (Yu et al. 2014) and a Bayesian sampling 23 technique (Wen et al. 2016a). However, these methods 24 use gene tree estimates as input. Using these estimates, 25 instead of using the sequence data directly, has at least 26 three drawbacks. First, the sequence data allows for 27 learning more about the model than gene tree estimates 28 (Rannala and Yang 2003). Second, gene tree estimates 29 could well include erroneous information, resulting in 30 wrong inferences (DeGiorgio and Degnan 2014; Wen 31 et al. 2016a). Third, co-estimating the species phylogeny 32 and gene trees results in better estimates of the gene 33 trees themselves (Bayzid and Warnow 2013; DeGiorgio and Degnan 2014). 35

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We report here on a Bayesian method for co-estimating 36 species (or, population) phylogenies and gene trees along 37 with parameters such as ancestral population sizes and 38 divergence times using DNA sequence alignments from 39 multiple independent loci. Our method utilizes a two-40 step generative process (Fig. 1) that links, via latent 41 variables that correspond to local gene genealogies, the 42 sequences of multiple, unlinked loci from across a set of 43 genomes to the phylogenetic network (Nakhleh 2010a) 44 that models the evolution of the genomes themselves 45

Our method consists of a reversible-jump Markov 46 chain Monte Carlo (RJMCMC) sampler of the posterior 47 distribution of this generative process. In particular, 48 our method co-estimates, in the form of posterior 49 distribution samples, the phylogenetic network and its 50 associated parameters for the genomes as well as the 51 local genealogies for the individual loci. We demonstrate 52 the performance of our method on simulated data. 53 Furthermore, we analyze three biological data sets, 54 and discuss the insights afforded by our method. In 55 particular, we find that methods that do not account, 56 wrongly, for admixture in the data tend to underestimate 57 divergence times of the species or populations and 58 overestimate the coalescent times of individual gene 59 genealogies. Our method, on the other hand, estimates 60 both the divergence times and coalescent times with high 61 accuracy. Furthermore, we demonstrate that coalescent 62 times are much more accurately estimated when the 63 estimation is done simultaneously with the phylogenetic 64 network than when the estimation is done in isolation. 65

An important contribution of this manuscript is 66 also to study the performance of the MSNC on data 67 generated under gene flow scenarios. In particular, the 68 population genetics community has developed models of 69 reticulate evolution (i.e., admixture) at the population 70

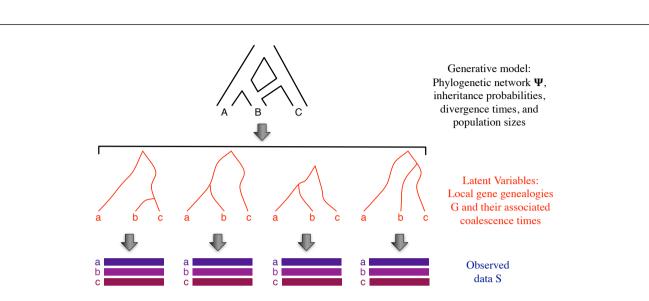


FIGURE 1. From a phylogenetic network to multi-locus sequences via latent gene genealogies. The multispecies network coalescent (Yu *et al.* 2014) is a stochastic process that defines a probability distribution on gene genealogies along with their coalescent times. The parameters of the process consist of a phylogenetic network topology, inheritance probabilities, divergence times, and population sizes. Each gene genealogy, when coupled with model of sequence evolution, defines a probability distribution on sequence alignments.

level. An important question is: How do phylogenetics
network methods perform on data generated under such
scenarios? To answer this question, it is important to
highlight the difference in abstraction employed in the
MSNC model as opposed to a gene flow model. It turns
out that this difference was well articulated in (Long
1991), where two models of admixture were presented:
the intermixture model and the gene flow model (Figure 2). The MSNC employs the intermixture model, whereas

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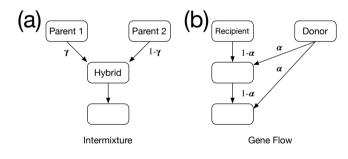


FIGURE 2. Two admixture models for a hybrid population (Long 1991). (a) The hybrid population is formed by a single intermixture event between two parental populations, where γ is the inheritance probability measuring the proportion of the parental populations. (b) The hybrid population (recipient) receives gene flow from a donor population, where α is the migration rate.

10 the population genetics community mostly uses the gene flow model (Gronau et al. 2011; Hey and Nielsen 11 2004, 2007; Leaché et al. 2013; Slatkin and Maddison 12 1989; Strasburg and Rieseberg 2010; Whitlock and 13 Mccauley 1999). Note that the intermixture model also 14 underlies the admixture graph model of (Pickrell and 15 Pritchard 2012; Reich *et al.* 2009) where γ is the 16 admixture proportion. In the admixture graph model, 17

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the branch lengths correspond to genetic drift values that measure variation in allele frequency corresponding to random sampling of alleles from generation to generation in a finite-size population.

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Hudson's ms program (Hudson 2002) allows for 22 generating data under each of the two admixture 23 models—intermixture and gene flow. In this paper, 24 we generate data under both models and study the 25 performance of inference under the MSNC in both cases. 26 For an empirical data set, we analyzed the yeast data 27

set of (Rokas *et al.*, 2003), which consists of 106 loci from seven Saccharomyces species, and contrasted our results to those obtained from the method of (Wen *et al.*, 2016a) on gene tree estimates.

Finally, as the model underlying our method extends 32 the multispecies coalescent to cases that include 33 admixture, our method is applicable to data from 34 different sub-populations, not only different species, and 35 to data where more than one individual per species or 36 sub-population is sampled. The method is implemented 37 and publicly available in the PhyloNet software package 38 (Than et al. 2008). 39

METHODS

0.1 Phylogenetic networks and their parameters

A phylogenetic \mathscr{X} -network, or \mathscr{X} -network for short, Ψ , is a directed, acyclic graph (DAG) with $V(\Psi) = \{s,r\} \cup V_L \cup V_T \cup V_N$, where

- indeg(s) = 0 and outdeg(s) = 1 (s is a special node, that is the parent of the root node, r); 46
- indeg(r) = 1 and outdeg(r) = 2 (r is the root of Ψ); 47
- $\forall v \in V_L$, indeg(v) = 1 and outdeg(v) = 0 (V_L are the external tree nodes, or leaves, of Ψ);

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- $\forall v \in V_T$, indeg(v) = 1 and $outdeg(v) \ge 2$ (V_T are the *internal tree nodes* of Ψ); and,
- $\forall v \in V_N$, indeg(v) = 2 and outdeg(v) = 1 (V_N are the reticulation nodes of Ψ).

 $E(\Psi) \subseteq V \times V$, consist The network's edges, of 7 reticulation edges, whose heads are reticulation nodes, 8 tree edges, whose heads are tree nodes, and special edge $(s,r) \in E$. Furthermore, $\ell: V_L \to \mathscr{X}$ is the *leaf-labeling* 10 function, which is a bijection from V_L to \mathscr{X} . Each node 11 in $V(\Psi)$ has a species divergence time parameter and 12 each edge in $E(\Psi)$ has an associated population size 13 parameter. The edge $er(\Psi) = (s, r)$ is infinite in length so 14 that all lineages that enter it coalesce on it eventually. 15 Finally, for every pair of reticulation edges e_1 and e_2 16 that share the same reticulation node, we associate an 17 inheritance probability, γ , such that $\gamma_{e_1}, \gamma_{e_2} \in [0,1]$ with 18 $\gamma_{e_1} + \gamma_{e_2} = 1$. We denote by Γ the vector of inheritance 19 probabilities corresponding to all the reticulation nodes 20 in the phylogenetic network (for each reticulation node, 21 Γ has the value for one of the two incoming edges only). 22 Given a phylogenetic network Ψ , we use the following 23 notation: 24

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$$\Psi_{top}$$
: The leaf-labeled topology of Ψ ; that is, the
pair (V, E) along with the leaf-labeling ℓ .

- Ψ_{ret} : The number of reticulation nodes in Ψ . • $\Psi_{ret} = 0$ when Ψ is a phylogenetic tree.
- Ψ_{τ} : The species divergence time parameters of Ψ . • $\Psi_{\tau} \in (\mathbb{R}^+)^{|V(\Psi)|}$.
- Ψ_{θ} : The population size parameters of Ψ . $\Psi_{\theta} \in (\mathbb{R}^+)^{|E(\Psi)|}$

We use Ψ to refer to the topology, species divergence times and population size parameters of the phylogenetic network.

It is often the case that divergence times associated
with nodes in the phylogenetic network are measured in
units of years, generations, or coalescent units. On the
other hand, branch lengths in gene trees are often in units
of expected number of mutations per site. We convert
estimates back and forth between units as follows:

- Given divergence time in units of expected number of mutations per site τ , mutation rate per site per generation μ and the number of generations per year g, $\tau/\mu g$ represents divergence times in units of years.
- Given population size parameter in units of population mutation rate per site θ , $2\tau/\theta$ represents divergence times in coalescent units.

⁵⁰ Bayesian Formulation and Inference

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The data in our case is a set $\mathscr{S} = \{S_1, \ldots, S_m\}$ where S_i is a DNA sequence alignment from locus *i* (the bottom part in Fig. 1). A major assumption is that there is

no recombination within any of the m loci, yet there is free recombination between loci. The model \mathscr{M} consists of a phylogenetic network Ψ (the topology, divergence times, and population sizes) and a vector of inheritance probabilities Γ (the top part in Fig. 1).

The posterior distribution of the model is given by (41, 62) = (42, 62) = (42, 62)

$$p(\mathcal{M}|\mathcal{S}) \propto p(\mathcal{S}|\mathcal{M})p(\mathcal{M}) \\ = p(\mathcal{M})\prod_{i=1}^{m} \int_{G} p(S_{i}|g)p(g|\mathcal{M})dg, \quad (0.1)$$

where the integration is taken over all possible gene 60 trees (the middle part in Fig. 1). The term $p(S_i|g)$ 61 gives the gene tree likelihood, which is computed using 62 Felsenstein's algorithm (Felsenstein 1981) assuming 63 a model of sequence evolution, and $p(g|\mathcal{M})$ is the 64 probability density function for the gene trees, which 65 was derived for the cases of species tree and species 66 network in (Rannala and Yang 2003) and (Yu et al. 67 2014), respectively. 68

The integration in Eq. (0.1) is computationally infeasible except for very small data sets. Furthermore, in many analyses, the gene trees for the individual loci are themselves a quantity of interest. Therefore, to obtain gene trees, we sample from the posterior distribution as given by 74

$$p(\Psi,\Gamma,G|S) \propto p(\mathscr{M}) \prod_{i=1}^{m} p(S_i|g_i) p(g_i|\mathscr{M}) = p(\Psi) p(\Gamma) \prod_{i=1}^{m} p(S_i|g_i) p(g_i|\Psi,\Gamma), \quad (0.2)$$

where $G = (g_1, ..., g_m)$ is a vector of gene trees, one for each of the *m* loci. This co-estimation approach is adopted by the two popular Bayesian methods *BEAST (Heled and Drummond 2010) and BEST (Liu 2008), both of which co-estimate species trees (hybridization is not accounted for) and gene trees.

The Likelihood Function

Felsenstein (Felsenstein 1981) introduced a pruning algorithm that efficiently calculates the likelihood of gene tree q and DNA evolution model parameters Φ as

$$p(S|g,\Phi) = \prod_{i=1}^{l} p(s_i|g,\Phi),$$

where s_i is *i*-th site in S, l is the sequence length, and

$$p(s_i|g,\Phi) = p(s_i|g_{top},g_\tau,\pi,q,\mu).$$

Here, g_{top} is the tree topology, g_{τ} is the divergence 82 times of the gene tree, $\pi = \{\pi_A, \pi_T, \pi_C, \pi_G\}$ is a vector 83 of equilibrium frequencies of the four nucleotides, q =84 $\{q_{AT}, q_{AC}, q_{AG}, q_{TC}, q_{TG}, q_{CG}\}$ is a vector of substitution 85 rates between pairs of nucleotides, and μ is the mutation rate. Over a branch j whose length (in expected number 87 of mutations per site) is t_j , the transition probability is 88 calculated as $e^{\mu q t_j}$. In the implementation, we use the 89 BEAGLE library (Ayres et al. 2011) for more efficient 90 implementation of Felsenstein's algorithm. 91

⁵¹ Yu *et al.* (Yu *et al.* 2012, 2013a, 2014) fully derived the mass and density functions of gene trees under the multispecies network coalescence, where the lengths of a 94

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phylogenetic network's branches are given in coalescent units. Here, we derive the probability density function (pdf) of gene trees for a phylogenetic network given by its topology, divergence/migration times and population size parameters following (Rannala and Yang 2003; Yu et al. 2014). Coalescence times in the (sampled) gene 6 trees posit temporal constraints on the divergence and migration times of the phylogenetic network.

We use $\tau_{\Psi}(v)$ to denote the divergence time of node v in phylogeny Ψ (tree or network). Given a gene 10 tree g whose coalescence times are given by τ' and a 11 phylogenetic network Ψ whose divergence times are given 12 by τ , we define a coalescent history with respect to times 13 to be a function $h: V(g) \to E(\Psi)$, such that the following 14 condition holds: 15

 $\bullet \hspace{0.1 if} \text{ if } \hspace{0.1 in} (x,y) \! \in \! E(\Psi) \hspace{0.1 in} \text{and} \hspace{0.1 in} \tau_{\Psi}(x) \! > \! \tau_{g}'(v) \! \geq \! \tau_{\Psi}(y), \hspace{0.1 in} \text{then}$ 16 h(v) = (x, y).17

• if r is the root of Ψ and $\tau'_q(v) \ge \tau_{\Psi}(r)$, then h(v) =18 $er(\Psi).$ 19

The quantity $\tau'_g(v)$ indicates at which point of branch 20 (x,y) coalescent event v happens. We denote the set of 21 coalescent histories with respect to coalescence times for 22 gene tree g and phylogenetic network Ψ by $H_{\Psi}(g)$. 23

Given a phylogenetic network Ψ , the pdf of the gene 24 tree random variable is given by 25

$$p(g|\Psi,\Gamma) = \sum_{h \in H_{\Psi}(g)} p(h|\Psi,\Gamma), \qquad (0.3)$$

where $p(h|\Psi,\Gamma)$ gives the pdf of the coalescent history 26 (with respect to divergence times) random variable. 27

Consider gene tree g for locus j and an arbitrary 28 $h \in H_{\Psi}(g)$. For an edge $b = (x, y) \in E(\Psi)$, we define $T_b(h)$ 29 to be a vector of the elements in the set $\{\tau_q(w): w \in$ 30 $h^{-1}(b) \} \cup \{ \tau_{\Psi}(y) \}$ in increasing order. We denote by 31 32 $T_b(h)[i]$ the *i*-th element of the vector. Furthermore, we denote by $u_b(h)$ the number of gene lineages entering 33 edge b and $v_b(h)$ the number of gene lineages leaving 34 edge b under h. Then we have

$$p(h|\Psi,\Gamma) = \prod_{b \in E(\Psi)} \left[\prod_{i=1}^{|T_b(h)|-1} \frac{2}{\theta_b} e^{-(\frac{2}{\theta_b})\binom{u_b(h)-i+1}{2}(T_b(h)_{i+1}-T_b(h)_i)} \right] \times e^{-(\frac{2}{\theta_b})\binom{v_b(h)}{2}(\tau_{\Psi}(x_b)-T_b(h)_{|T_b(h)|})} \times \Gamma_b^{u_b(h)},$$
(0.4)

where x_b is the source node of edge b, $\theta_b = 4N_b\mu$ and N_b 36 is the population size corresponding to branch b, μ is 37 the mutation rate per-site per-generation, and Γ_b is the 38 inheritance probability associated with branch b. 39

Prior Distributions

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We extended the prior of phylogenetic network 41 composed of topology and branch lengths in (Wen et al. 2016a) to phylogenetic networks composed of topology. divergence times and population sizes, as given by Eq.

(0.5),

$$p(\Psi|\nu,\delta,\eta,\psi) = p(\Psi_{ret}|\nu) \times p(\Psi_d|\Psi_{top},\Psi_\tau,\eta) \\ \times p(\Psi_\tau|\delta) \times p(\Psi_\theta|\psi)$$
(0.5)

where $p(\Psi_{ret}|\nu)$, the prior on the number of reticulation nodes, and $p(\Psi_d|\Psi_{top},\Psi_{\tau},\eta)$, the prior on the diameters 47 of reticulation nodes, were defined in (Wen et al. 2016a). 48

It is important to note here that if Ψ_{top} does not follow the phylogenetic network definition, then $p(\Psi|\nu,\delta,\eta,\psi) =$ 0. This is crucial since, in the MCMC kernels we describe 51 below, we allow the moves to produce directed graphs that slightly deviate from the definition; in this case, having the prior be 0 guarantees that the proposal is rejected. Using the strategy, rather than defining only "legal" moves simplifies the calculation of the Hastings ratios. See more details below.

Rannala and Yang used independent Gamma distributions for time intervals (branch lengths) instead of divergence times. However, in the absence of any information on the number of edges of the species network as well as the time intervals, it is computationally intensive to infer the hyperparameters of independent Gamma distributions. Currently, we use a uniform distribution (as in BEST (Liu 2008)).

We assume one population size per edge, including the edge above the root. Population size parameters are Gamma distributed, $\theta_b \sim \Gamma(2, \psi)$, with a mean 2ψ and a shape parameter of 2. In the absence of any information on the population size, we use the noninformative prior $P_{\psi}(x) = 1/x$ for hyperparameter ψ (Heled and Drummond 2010). The number of elements in θ is $|E(\Psi)|+1$. To simplify inference, our implementation also supports a constant population size across all branches, in which case θ contains only one element.

For the prior on the inheritance probabilities, we use $\Gamma_b \sim \text{Beta}(\alpha, \beta)$. Unless there is some specific knowledge on the inheritance probabilities, a uniform prior on [0,1] is adopted by setting $\alpha = \beta = 1$. If the amount of introgressed genomic data is suspected to be small in the genome, the hyper-parameters α and β can be appropriately set to bias the inheritance probabilities to values close to 0 and 1 (a U-shaped distribution).

The RJMCMC Sampler

As computing the posterior distribution given by Eq. 85 (0.2) is computationally intractable, we implement a 86 Markov chain Monte Carlo (MCMC) sampling procedure 87 based on the Metropolis-Hastings algorithm. In each 88 iteration of the sampling, a new state (Ψ', Γ', G') is 89 proposed and either accepted or rejected based on the 90 Metropolis-Hastings ratio r that is composed of the 91 likelihood, prior, and Hastings ratios. When the proposal 92 changes the dimensionality of the sample by adding a 93 new reticulation to or removing an existing reticulation 94 from the phylogenetic network, the absolute value of the determinant of the Jacobian matrix is also taken into

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account, which results in a reversible-jump MCMC, OB8 RJMCMC (Green 1995, 2003).

Our sampling algorithm employs three categories ${\scriptstyle 0}$ of moves: One for sampling the phylogenetic $\operatorname{network}_1$ and its parameters (divergence times and population₂ mutation rates), one for sampling the inheritance probabilities, and one for sampling the gene trees (topologies and coalescence times). To propose a new state of the Markov chain, one element from $(\Psi,\gamma_1,\ldots,\gamma_{\Psi_{ret}},g_1,\ldots,g_m)$ is selected at random, then a move from the corresponding category is applied. The workflow, design and full derivation of the Hastings ratios 10 of the moves are given in Supplementary Materials. 11

We implemented our method in PhyloNet (Than *et al.*) 12

2008), a publicly available, open-source software package 13 for phylogenetic network inference and analysis. 14

RESULTS

Our Method and *BEAST Perform Similarly in Cases 16 17 of No Reticulation

*BEAST (Heled and Drummond 2010) is the most 18 commonly used software tool for Bayesian inference 19 of species trees from multi-locus data. In our first 20 experiment, we set out to study how our method 21 performs compared to this well-established software tool 22 on simulated data whose evolutionary history is treelike. 23

To accomplish this task, we used the phylogenetic tree 24 shown in Fig. 3 as the model species phylogeny. Using

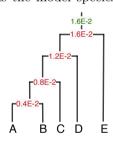


FIGURE 3. A model species tree used to generate multi-locus data sets. The divergence times in units of expected number of mutations per site and the population size parameter in units of population mutation rate per site are marked in red and green, respectively. The population mutation rate was assumed to be constant across all branches of the tree.

25 the program ms (Hudson 2002), we simulated 20 data 26 sets each consisting of 10 conditionally independent gene 27 trees with the command 28

We then used the program Seq-gen (Rambaut and₅ 31 Grassly 1997) to simulate the evolution of 1000-site, 32 sequences under the Jukes-Cantor model of evolution, 33 (Jukes and Cantor 1969) with the command 34

For each of the 20 10-locus data sets, we ran two₁ MCMC chains, each with 5×10^5 iterations and 5×10^{12} 37

 10^4 burn-in, using our method as well as *BEAST. Que sample was collected from every 500 iterations, resulting in a 900 collected samples per data set and a total of 18,000 collected samples from all 20 data sets. In comparing the two tools, we used all 18,000 collected samples to evaluate the estimates obtained for the various parameters of interest: population size parameter, divergence times, and the topology of the inferred species phylogeny.

Both our method and *BEAST inferred exactly the same 95% credible set, which consists of the six topologies shown in Fig. 4. Our method sampled the true



FIGURE 4. The trees that constitute the 95% credible set of each of our method and *BEAST. The proportions of these trees from left to right as sampled by our method were 77.7%, $5.7\%,\ 5.0\%,\ 3.0\%,\ 3.0\%,\ and\ 2.8\%,\ respectively,\ and\ as\ sampled$ by *BEAST were 70.7%, $6.0\%,\ 6.7\%,\ 4.7\%,\ 4.5\%,\ and\ 3.6\%,$ respectively.

phylogeny with higher frequency than *BEAST.

Fig. 5 shows histograms of the estimates obtained for the divergence times at each node of the maximum a posteriori (MAP) species tree estimate of our method and *BEAST, which was identical in both cases to the true species tree. The histograms of both methods are

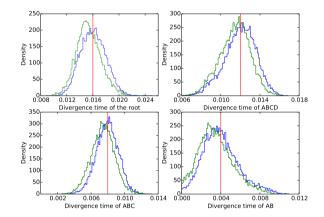


FIGURE 5. Histograms of divergence times of each node of the true species phylogeny as estimated by our method (blue) and *BEAST (green). The red vertical line indicates the true divergence time

very similar. In fact, the histograms obtained by our method have peaks that are closer to the true divergence time values than those obtained by *BEAST.

Fig. 6 shows the histograms of the population mutation rate (one value across all branches of the species tree was assumed) estimated by the two methods. As in the case of divergence time estimates, the two methods obtain similar results in the case of population mutation rate estimates. However, we observe here a histogram of our method with a single peak around the true value, whereas we observe a bimodal histogram obtained by *BEAST.

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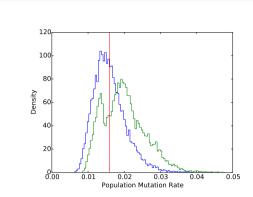


FIGURE 6. Population mutation rate estimated by our method (blue) and *BEAST (green). The red vertical line indicates the true population mutation rate.

All the results reported above were obtained by 13 running the code on NOTS (Night Owls Time-Sharing 14 Service), which is a batch scheduled High-Throughput 15 Computing (HTC) cluster. We used 2 cores, with two 16 threads per core running at 2.6GHz, and 1G RAM 17 per thread. The runtime for *BEAST is around $28\pm$ 18 1 seconds for each data set, while our method takes 19 20 longer time: 185 ± 7 seconds per data set. This can be explained by the fact that *BEAST has been under 21 continued development for several years now, while our 22 implementation hardly has any optimization components 23 24 yet.

When we ran *BEAST on multi-locus sequence data 25 simulated under species phylogenies with reticulations, 26 we found that *BEAST overestimated the coalescence 27 times in individual loci and underestimated the 28 divergence times of the species phylogeny. We report 29 these results in Supplementary Materials as *BEAST is 30 31 not intended for evolutionary analyses with gene flow. Furthermore, there are existing, extensive studies on the 32 impact of gene flow on the inference of species trees 33 (Leaché et al. 2013; Solís-Lemus et al. 2016). 34

Our Method Provides Accurate Estimates of the 35 Network and Its Associated Parameters 36

We used the phylogenetic network shown in Fig. 7 37 as the model species phylogeny. The scale parameter of 38 the divergence times s was varied to take on values in the set $\{0.1, 0.25, 0.5, 1.0\}$. Setting s = 0.1 results in very 40 short branches and, consequently, the hardest data sets on which to estimate parameters. Setting s = 1.0 results in longer branches and higher signal for a more accurate estimate of the parameter values. It is important to note that the topology, reticulation event, divergence times (with s=1.0) and population size are inspired by the species phylogeny recovered from the Anopheles mosquitoes data set (Fontaine et al. 2015; Wen et al. 2016b).

For the four settings of s values, 0.1, 0.25, 0.5, and 1.0, we used the program ms (Hudson 2002) to simulate 20 data sets each with 128 gene trees of conditionally

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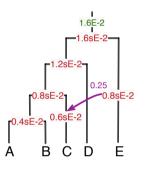


FIGURE 7. A model phylogenetic network used to generate simulated data. The divergence times in units of expected number of mutations per site, the population size parameter in units of population mutation rate per site, and the inheritance probability are marked in red, green, and purple, respectively. Parameter s is used to scale the divergence times

independent loci with the four following commands 53 respectively: 54

- ms 5 128 -T -I 5 1 1 1 1 1 1 -ej 0.025 4 3 -es 0.0375 1 55 0.3 -ej 0.05 6 3 -ej 0.05 2 1 -ej 0.075 5 3 -ej 0.1 3 1 56
- ms 5 128 -T -I 5 1 1 1 1 1 1 -ej 0.0625 4 3 -es 0.09375 57 1 0.3 -ej 0.125 6 3 -ej 0.125 2 1 -ej 0.1875 5 3 -ej $0.25 \ 3 \ 1$ 59
- ms 5 128 -T -I 5 1 1 1 1 1 1 -ej 0.125 4 3 -es 0.1875 1 60 0.3 -ej 0.25 6 3 -ej 0.25 2 1 -ej 0.375 5 3 -ej 0.5 3 1 61
- ms 5 128 T I 5 1 1 1 1 1 1 ej 0.25 4 3 es 0.375 1 62 0.3 -ej 0.5 6 3 -ej 0.5 2 1 -ej 0.75 5 3 -ej 1.0 3 1 63

The program Seq-gen (Rambaut and Grassly 1997) was used to generate sequence alignments down the gene 65 trees under the Jukes Cantor model (Jukes and Cantor 66 (1,969) with lengths seqLen in $\{250,500,1000\}$ using the 67 çommand

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seq-gen -m HKY -l seqLen -s 0.008

To vary the number of loci used in the inference, we produced data sets with 32, 64, and 128 loci by sampling loci without replacement from the full data set of 128 loci. Each of these sequence data sets was then used as imput to the inference method.

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To assess the signal in the sequence data sets we₆ obtained, we quantified the percentage of variable sites for each setting, averaged over all 20 replicates for that setting. The percentages of variable sites in the generated alignments for s = 0.1, 0.25, 0.5, 1.0 (varying the sequence length had negligible effect for the same scaling factor s) are $\sim 0.039 \pm 0.02$, $\sim 0.048 \pm 0.02$, $\sim 0.061 \pm 0.02$, and $\sim\!0.088\pm\!0.02,$ respectively.

For each data set, we ran an MCMC chain of 8×10^6 iterations with 1×10^6 burn-in. One sample was collected from every 5,000 iterations, resulting in a total of 1,400 collected samples. We summarized the results based on 28,000 samples from 20 replicates for each of the 36 simulation settings (four values of s, three sequence lengths, and three numbers of loci). In the boxplots below, the five bars from bottom to top correspond to the minimum, first-, second-, third-quantile, and the maximum, respectively, from the 20 replicates for each setting. In the other figures, the error bars correspond to standard deviations calculated from the 20 replicates for each setting.

In assessing the performance of our method, we estimates obtained for the various evaluated the parameters of interest: divergence times, population mutation rates, the number of reticulations, and the topology of the inferred species phylogeny. Fig. 8 shows the estimates obtained for the divergence time at the root of the network. Three observations are in order.

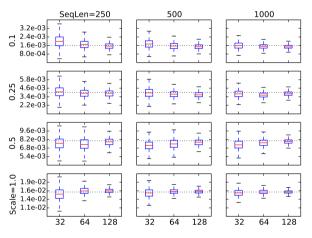


FIGURE 8. Divergence time estimates at the root under different values of the scaling parameter s (different rows), sequence lengths (different columns), and numbers of loci (three values within each panel). The dashed line indicates the true value in the model network

First, for any combination of sequence length and scaling 6 parameter value, the divergence time estimate converges 7 to the true value as the number of loci increases. Second, 8 for any combination of number of loci and scaling parameter value, the divergence time estimate converges 10 to the true value as the sequence length increases. Third, 11 the estimates are relatively poor only under the extreme 12 settings of scaling parameter value 0.1 and sequence 13 length 250. In this case, the signal in the sequence data 14 is too weak to obtain good estimates. However, it is 15

worth noting that even under this setting, using 128 loci produces a very accurate estimate of the divergence time. 77 Fig. 9 shows the estimates obtained for the population mutation rate parameter (one value across all branches of the species network was assumed). The results show

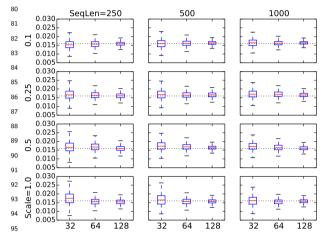


FIGURE 9. Population mutation rate estimates under different alues of the scaling parameter s (different rows), sequence lengths (different columns), and numbers of loci (three values within each panel). The dashed line indicates the true value in the model network.

very similar trends to those obtained for the divergence time estimates, with the main difference being that the estimates now are very accurate even for the hardest of cases: s=0.1 and sequence length 250, regardless of the number of loci used.

The results are quite different when it comes to estimating the number of reticulations and the topology of the phylogenetic network itself. Fig. 10 shows the estimates of the number of reticulations under different settings. As the figure clearly shows, under the case of

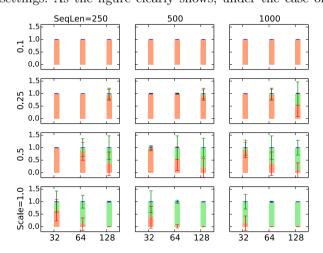


FIGURE 10. Proportions of trees (red), 1-reticulation networks (green) and 2-reticulations networks (blue) inferred under different simulation conditions. The model network has a single reticulation.

extremely short branches (s=0.1), the method recovers a tree; that is, it estimates the number of reticulations to be 0, regardless of the number of loci or sequence

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length used. Here, the signal is too weak to recover any reticulation. In the case of slightly longer branches (s=0.25), the estimate of the number of reticulations becomes slightly more accurate when the sequences are long and 128 loci are used. Given the observed trend, the method could recover the true number of reticulations if 6 a thousand or so loci are used. In the case of s=0.5, a fast convergence towards the true number is observed as the number of loci increases. It is worth pointing out that, in the case of s=0.5, increasing the number 10 of loci, even when the sequences are very short, is 11 much more advantageous than increasing the sequence 12 lengths of the individual loci. It is also important to 13 note here that in analyzing biological data sets, one 14 cannot use longer sequences without risking violating the 15 recombination-free loci assumption. In the case of s = 1.0, 16 the method does very well at estimating the number of 17 reticulations. Finally, observe that the method almost never overestimates the number of reticulations on these 1

data sets. In assessing the quality of the estimated network₃ topology itself, we analyzed the recovered networks in₄ two ways. First, we compared the inferred network to thes true network using a topological dissimilarity measure₆ (Nakhleh 2010b). Second, when the method infers a₇ tree, rather than a network, we compared the trees to the "backbone tree" of the true network (the tree₉ resulting from removing the arrow in Fig. 7) using the $\!\!\!\!\!\!\!$ Robinson-Foulds metric (Robinson and Foulds 1981)¹¹ The latter comparison allows us to answer the question12 When the method estimates the species phylogeny to₃ be a tree, how does this tree compare to the backbone₄ tree of the true network? It is important to note₁₅ though, that the relationship of a phylogenetic network₆ and its constituent trees can become too complex to₇ be captured by a backbone tree in the presence of₈ incomplete lineage sorting (Zhu et al. 2016). Fig. 11,9 shows the results. The results in terms of the topologicalo

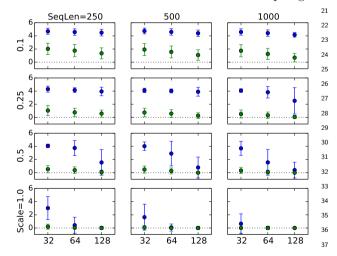


FIGURE 11. The topological difference between the true and inferred networks in blue and the Robinson-Foulds distance between the inferred tree (if a network is inferred, this case is not included) and the backbone tree of the true network in green.

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difference between the inferred and true networks parallel those that we discussed above in terms of the estimates 40 of the number of reticulations: Poor accuracy and no 41 sign of convergence to the true network in cases of very 42 small values of the scaling parameter, and very good 43 accuracy and fast convergence to accurate estimates in 44 cases of larger values of the scaling parameter. However, 45 the topological difference between the inferred trees (in the cases where trees were inferred) and the backbone 47 tree reveal an important insight: When the method fails 48 to recover the true network, it does a very good job at 49 recovering the backbone tree of the true network.

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Our Method Provides Accurate Estimates of the Gene Trees

18 Thus far, we have analyzed the accuracy of the inferred networks and their associated parameters. While MCMC methods in this context are deployed to approximate the integration over gene trees in a simulated manner. the methods do provide the sampled gene trees (topologies and coalescence times). The accuracy of those sampled gene trees is important for at least two reasons. First, their accuracy directly impacts and explains the accuracy of the networks. Second, the gene trees themselves are a quantity of interest in many applications.

28 It is important to note here two relevant studies that have addressed the issue of gene tree accuracy in the context of species tree estimation. First, (Bayzid and Warnow 2013) showed that *BEAST yields more accurate gene trees than would be estimated by RAxML, attributing the higher accuracy to the co-estimation nature of the former method. Second, (DeGiorgio and Begnan 2014) found that methods for estimating gene twees do a better job at estimating the topologies than the coalescence times and that this leads to more accurate species tree estimates when using gene tree topologies alone as opposed to using coalescence times as well. While both studies were conducted in the context of species trees, our goal here is not to reproduce these extensive studies in the context of phylogenetic networks. but rather to demonstrate that the main conclusions still hold even when the species phylogeny is reticulate.

In Fig. 12 we report the Robinson-Foulds distances between the true gene tree topologies and those sampled by our method, as well as the distance between the true gene tree topologies and those estimated by RAxML. The results demonstrate that the co-estimated gene tree topologies are, on average, slightly closer to the true gene tree topologies than those estimated in a standalone manner using RAxML. Nonetheless, it is worth point out that the error bars of our method are smaller than those pertaining to the RAxML gene trees. Both methods obtained improved accuracy as the sequence length increased.

As the results in the next section show, the networks inferred from sequences directly are more accurate than 40 those inferred from gene tree estimates. The question is: 41 What is causing this difference if the gene tree topologies 42 \oplus

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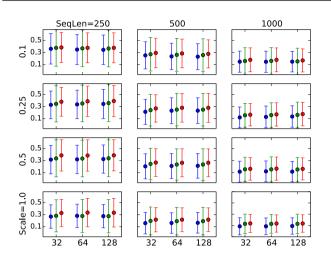


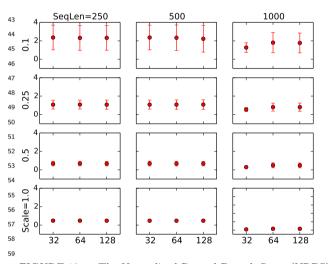
FIGURE 12. The Robinson-Foulds distances between the true gene tree topologies and those estimated by our method in blue, between the true gene tree topologies and those estimated by RAxML in green, and between the gene tree topologies estimated by our method and those estimated by RAxML in red.

estimated by both our method and RAxML are not that different? One interesting observation we make is that while both our method and RAxML infer gene tree topologies that, on average, are of equal distance from the true gene tree topologies, the two methods return different trees, as shown in Fig. 12. That is, under the Robinson-Foulds distance, both methods infer gene trees whose topologies could be considered to be, roughly, equally good. However, the topologies are not the same. This difference could explain, at least in part, the increased accuracy of the networks and their associated parameters when inferred from sequences as opposed to gene tree estimates.

To further investigae this question, we turned our attention to the accuracy of the coalescence times estimated by our method. Fig. 13 shows the Normalized Rooted Branch Score (NRBS) (Heled and Drummond, 2010) between the gene trees estimated by our method and the true gene trees. This measure takes into account the branch lengths of the gene trees and not only the topologies. These results clearly show that, except for the hardest case of 0.1 scaling factor, the method performs very well in terms of estimating the coalescence times, not only in terms of the mean value but also in terms of⁵ the very small standard deviations.

It is important to comment on a seeming discrepancy⁷ between Fig. 12 and Fig. 13. For example, in the case of scaling factor 1.0, Fig 12 shows a Robinson-Foulds distance of 0.3, yet Fig. 13 shows an NRBS value close₈ to 0. Given that the number of taxa is 5, a Robinson-₉ Foulds value of 0.3 amounts, roughly, to a single incorrect branch in the gene tree. However, while the true and ¹⁰ estimated gene tree differ by one branch, the difference¹¹ in coalescence times between the two trees could be¹² in the line of the true and ¹³ between the two trees are could be¹³ between the two trees are could be¹⁴ between the two trees are could be¹³ between the two trees are could be¹⁴ between the two trees are could be¹⁴ between the two trees are could be¹⁵ between the two trees are could be¹⁴ between the two trees are could be¹⁵ between the two trees are could be¹⁵ between the two trees are could be¹⁵ between the two trees are could be¹⁶ between the two trees are could be¹⁶ between the two trees are could be¹⁷ between the two trees are could be¹⁸ between the two trees are could be¹⁸ between the two trees are could be¹⁸ between the two trees are could be¹⁹ between the two trees are could be two trees are

negligible, which explains the small NRBS values. $^{13}_{14}$



 60 FIGURE 13. The Normalized Rooted Branch Score (NRBS) (Heled and Drummond, 2010) between the true gene trees and those estimated by our method. The branch lengths are scaled in coalescent units and divided by their corresponding scale parameter 0.1, 0.25, 0.5, 1.0 for better comparison.

⁶⁵ Next we show the effect of errors in gene tree estimates on the accuracy of and data requirement for accuracy p_{p}^{5} hylogenetic network estimates.

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⁷¹ Inference from Gene Tree Estimates Requires More ⁷² Data Than Inference from Sequences

⁷³ We also set out to compare the performance of our method to that of the method we developed earlier for Bayesian inference of phylogenetic networks from gene tree data (Wen *et al.* 2016a). This method is also implemented in PhyloNet (Than *et al.* 2008) and executed via the command MCMC_GT. The goal here is to assess the gains one obtains by using the sequence data

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directly rather than first estimating gene trees and then
using those as the data for species phylogeny inference.

For the purpose of this experiment we used the subset of the data sets described above and simulated on the phylogenetic network of Fig. 7 under the settings of s=1.0, sequence length 250, and 32, 64, and 128 loci. When using the method of (Wen *et al.* 2016a) we ran it once on the true gene trees and again using the gene tree estimates obtained by RAxML (Stamatakis 2014).

We ran the method of (Wen *et al.* 2016a) for 1,100,000 iterations with 100,000 burn-in and sampled every 1,000 iterations. The top five topologies sampled are shown in Fig. 14 (they were the same top topologies when either

the true gene trees or gene tree estimates were used).



FIGURE 14. The top five topologies sampled using the method (Wen *et al.*, 2016a) on the true gene trees, as well as the gene tree estimates. The leftmost topology is the true network topology and the second from left is the backbone tree of the true network topology. See the main text for details on the 95% credible sets in terms of these five topologies for the different data sets used.

When using the true gene tree topologies as input data,¹ the results were as follows: ²

For the 32-locus data set, the 95% credible³/₄
set contains 16.4% the true network, 59.6%
the backbone tree, 12.5% other 1-reticulation
networks, and 11.5% other trees.

• For the 64-locus data set, the 95% credible set contains 66.0% the true network, 27.1% the backbone tree, and 3.8% the 1-reticulation network resulting for the backbone tree with reticulation edge $C \rightarrow E$ (the network in the middle of Fig. 14).

For the 128-locus data set, the 95% credible set contains 91.7% the true network, and 4.4% the backbone tree.

When using the gene tree topology estimates as input data, the results were as follows:

- For the 32-locus data set, the 95% credible set contains 6.1% the true network, $47.3\%_6$ the backbone tree, 14.1% other 1-reticulation⁷ networks, and 32.5% other trees.
- For the 64-locus data set, the 95% credible set contains 24.7% the true network, 40.5% the backbone tree, and 8.6% the 1-reticulation network resulting for the backbone tree with reticulation edge $C \rightarrow E$, 18.4% other 1-reticulation networks and 7.8% other trees.
- For the 128-locus data set, the 95% credible set⁶ contains 49.9% the true network, 19.1 the 1¹⁷ reticulation network resulting for the backbone tree⁸ with reticulation edge $C \rightarrow E$, 5.7% the backbone⁹ tree, and 35.2% other 1-reticulation networks.²⁰

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More comprehensively, Fig. 15 shows the proportions of 0- (tree), 1-, and 2-reticulation networks in the 95% credible sets on each of the data sets when different numbers of loci are used and when the method of (Wen *et al.* 2016a) is run on true and estimated gene tree topologies.

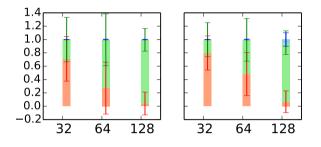


FIGURE 15. Proportions of trees (red), 1-reticulation networks (green) and 2-reticulations networks (blue) in the 95% credible sets sampled by the method of (Wen *et al.* 2016a) on data sets with 32, 64, and 128 loci. Left: the true gene tree topologies are used as the input data. Right: the gene tree estimates (using RAxML) are used as the input data.

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We also assessed the quality of the inferred network/tree topologies by comparing them to the true network using the topological dissimilarity measure (Nakhleh 2010b). When the method infers a tree, rather than a network, we compared the tree to the backbone tree of the true network using the Robinson-Foulds metric (Robinson and Foulds 1981). The results are in Fig. 16.

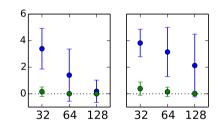


FIGURE 16. The topological difference between the true and inferred networks in blue and the Robinson-Foulds distance between the inferred tree (if a network is inferred, this case is not included) and the backbone tree of the true network. Left: the true gene tree topologies are used as the input data. Right: the gene tree estimates (using RAxML) are used as the input data.

⁴⁹ Clearly, the results indicate the method's performance ^{im} terms of phylogenetic inference improves as the number of loci increases, and, unsurprisingly, the method filas a much better performance when the true gene trees ^{äf}rue" gene trees are never known, and their estimates ^{ifi}tust be used for methods that utilize gene trees as data. ⁵⁵ Contrast these results to those obtained by our method ^{when} it is run on the sequence data as input (bottom left panel in Fig. 11). Estimation from sequence data outperforms inference from gene trees, even when using the true gene tree topologies. This is mainly due to the fact that the gene tree topology does not capture all the information that the sequence data do. In particular,

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we observe that inference from sequence data requires a much smaller number of loci than that required to achieve a similar accuracy when making inferences from

²⁴ gene tree topology estimates.

Intermixture vs Gene Flow: Comparing the Method's Performance on Data under Both Models

As we discussed above and illustrated in Fig. 2, 27 intermixture and gene flow provide two different abstract 28 models of reticulation. Furthermore, the program ms (Hudson 2002) allows for generating data under both, 30 models. While the MSNC is based on an intermixture 31 model, we study here how it performs on data simulated \bar{a}_3 32 under a gene flow model. We set up the experiment so 33 that data are generated under the same phylogenetic 34 networks and their parameters, yet under the scenarios 35 of intermixture and gene flow separately. Furthermore, in this part, we assess the performance when multiple reticulation events occur between the same pair of species—a very realistic scenario in practice. Fig. 17shows the six phylogenetic networks we used to generate data.

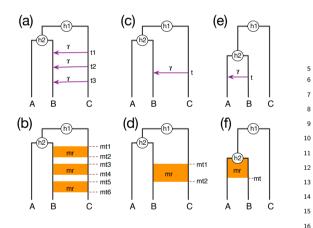


FIGURE 17. True phylogenetic histories with intermixture and gene flow models. Recurrent reticulations between non-¹⁷ sister taxa (a,b), a single reticulation between non-sister taxa⁸ (c,d), and a single reticulation between sister taxa (e,f) area captured under both the intermixture model (top) and gene flow₀ model (bottom). Parameters h_1 and h_2 denote divergence times² (in coalescent units), t_i parameters denote intermixture times², mt_i parameters denote start/end of migration epochs, γ is the² inheritance probability, and mr is the population migration rate³ (see main text).

For each simulation setting, we simulated 20 data²⁵ sets with 200 1-kb loci (in this part, we did not vary²⁷₇ the sequence lengths and numbers of loci). We set the²⁸ population mutation rate at 0.02 across all the branches²⁹ Furthermore we set the inheritance probability γ and the²⁹ migration rate mr each to 0.20 (here, mr = 2Nm, where³¹ N is the effective population size, and m is the fraction of³² the recipient population that is made up of migrants from³³ the donor population in each generation). We set $h_1 = 9^{33}_{34}$ $h_2 = 6$. For the intermixture model (Fig. 17(a)), we set³⁵ $t_2 = 3$, and varied (t_1, t_3) to take on the values $(4, 2)^{36}_{36}$ (5,1), and (6,0) so that the elapsed time, denoted by Δt_{7}^{4}

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between subsequent reticulation events is 1, 2, or 3. For the gene flow model (Fig. 17(b)), we set $(mt_1,...,mt_6)$ to (6,5,3.5,2.5,1,0), so that the duration of each gene flow epoch is 1 and the time elapsed between between two consecutive epochs, denoted by Δmt , is 1.5. The commands for the ms and Seq-gen programs are given in Supplementary Materials.

For each data set, we ran an MCMC chain of 8×10^6 iterations with 1×10^6 burn-in. One sample was collected from every 5,000 iterations, resulting in a total of 1,400 collected samples. We summarized the results based on 28,000 samples from 20 replicates for each parameter setting.

Table 1 shows the population mutation rates, divergence times, and numbers of reticulations estimated by our method on data generated under the models of Fig. 17(a) and Fig. 17(b). As the results show,

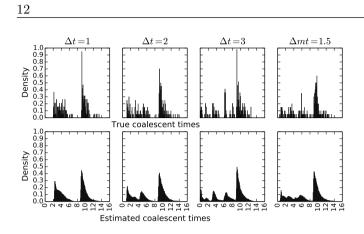
TABLE 1. Estimated population mutation rates (θ) , divergence times $(h_1 \text{ and } h_2)$, and numbers of reticulations (#reti) as a function of varying Δt in the model of Fig. 17(a) and Δmt in the model of Fig. 17(b). The divergence times were estimated in this of expected number of mutations per site and are reported in coalescent units by dividing by $\theta/2=0.01$.

| Case | $ $ θ | h_1 | h_2 | #reti | | |
|-------------------|----------------------|-----------------|-----------------|-----------------|--|--|
| $\Delta t = 1$ | $2.2 \pm 0.2 e^{-2}$ | 8.9 ± 0.1 | 5.9 ± 0.1 | 1.2 ± 0.4 | | |
| $\Delta t = 2$ | $2.2\pm0.2e^{-2}$ | 8.9 ± 0.1 | $5.9\!\pm\!0.1$ | 2.0 ± 0.0 | | |
| $\Delta t = 3$ | $2.1 \pm 0.3 e^{-2}$ | $9.0\!\pm\!0.1$ | 6.0 ± 0.1 | 2.6 ± 0.5 | | |
| $\Delta mt = 1.5$ | $2.3 \pm 0.3 e^{-2}$ | 8.9 ± 0.1 | 6.0 ± 0.1 | $2.1\!\pm\!0.3$ | | |

the method performs very well in terms of estimating the divergence times and population mutation rates, regardless of whether the data were generated under an intermixture model or a gene flow model. Furthermore, for these two parameters, the estimates are stable while varying the elapsed times between consecutive reticulation events.

As for the estimated number of reticulations, it becomes more accurate as the elapsed times between consecutive reticulations is larger. To better understand the factors that affect the detectability of reticulations, we plotted histograms of the true and estimated coalescence times of the most recent common ancestor (MRCA) of alleles from B and C in Fig. 18. Here, the true coalescence times are obtained from the true gene tree simulated generated by the program ms. The estimated coalescence times are sampled by our method along with the gene tree topologies. For the estimated coalescence times, we plot them based on all the collected stamples, which is why the histograms of estimated coalescence times are smoother than those of the true dones.

⁴⁴ As Fig. 17(a) and Fig. 17(b) show, the coalescence times of alleles from B and C would form a mixture off four distributions: three due to the three reticulation events, and one above the root of the phylogenetic nietwork. As the left three columns of panels in Fig 18 show, under an intermixture model, as Δt increases, the signal for a mixture of four distributions of (A,B)coalescence times becomes much stronger, thus pointing to three reticulations in addition to the coalescence



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FIGURE 18. Histograms of the true (top) and estimated (bottom) coalescence times (in coalescent units) of the MRCA of alleles from B and C on data generated under the models of Fig. 17(a) and Fig. 17(b).

³⁷ events above the root of the phylogeny. This is why, ³⁸ under the intermixture model, the method's performance ³⁹ in terms of the estimated number of reticulations ⁴⁰ improves as Δt increases. However, on data simulated

the under the gene flow model (the rightmost column of panels in Fig. 18), the signal of the mixture of four distributions of (A,B) coalescence times is surprisingly stronger than that under the intermixture model with the comparable $\Delta t = 1$ and $\Delta t = 2$.

Fig. 19 shows results similar to those reported in Fig. 18, with the only difference being that these are the coalescence times from all 4,000 loci generated from the 20 data sets of 200 loci each. Effectively, this is the

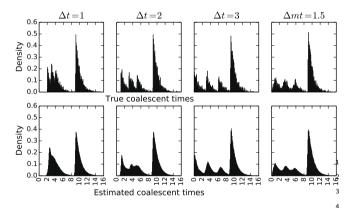


FIGURE 19. Histograms of the true (top) and estimateds (bottom) coalescence times (in coalescent units) of the MRCA of₆ alleles from B and C on 4,000 loci generated under the models of Fig. 17(a) and Fig. 17(b).

signal in a data set of 4,000 independent loci. Clearly,9 the signal is much stronger than in data sets of 2000 loci, and all reticulations would be recoverable under the1 intermixture model for $\Delta t=2,3$ and for the gene flow2 model.

We also ran simulations where we varied the numbers of individuals sampled from species B (we sampled 1, 3_{15} and 5 individuals). The results improve as the numbers of individuals increases from 1 to 3, but no discernible⁷

improvement is achieved under our simulation settings when the number of individual is increased to 5. Results are given in the Supplementary Materials.

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To assess the performance of our method on the 62 simpler case of a single reticulation event, we considered 63 the networks in Fig. 17(c) and Fig. 17(d), set $h_1 = 2.5$, 64 $h_2 = 1.5$, and $mt_1 = h_2$, and varied $t, mt_2 \in \{1, 0\}$. As the 65 mesults in Table 2 demonstrate, our method estimated 66 the population mutation rate θ , the divergence times h_1 67 and h_2 , and the inheritance probability/migration rate 68 very accurately under all cases. The method did very 48

⁴⁰ TABLE 2. Estimated population mutation rates (θ) , divergence times $(h_1 \text{ and } h_2)$, inheritance/migration rates, and numbers of reticulations (#reti) as a function of varying t in the model of Fig. 17(c) and mt_2 in the model of Fig. 17(d). The divergence times were estimated in units of expected number of mutations per site and are reported in coalescent units by dividing by $\theta/2=0.01$.

| | θ | h_1 | h_2 | $\gamma~(mr)$ | #reti |
|------------|-----------------------|-----------------|---------------|-----------------|---------------|
| t = 1 | $2.0\pm0.2e^{-2}$ | 2.5 ± 0.1 | 1.5 ± 0.1 | 0.20 ± 0.05 | 1.0 ± 0.0 |
| t = 0 | $2.0\!\pm\!0.2e^{-2}$ | | 1.5 ± 0.1 | 0.21 ± 0.04 | 1.0 ± 0.0 |
| $mt_2 = 1$ | $2.0 \pm 0.2 e^{-2}$ | 2.5 ± 0.1 | 1.5 ± 0.1 | 0.18 ± 0.05 | 1.0 ± 0.0 |
| $mt_2 = 0$ | $2.2 \pm 0.2 e^{-2}$ | $2.5\!\pm\!0.1$ | 1.5 ± 0.1 | 0.17 ± 0.04 | 1.0 ± 0.0 |

well also in terms of estimating t and mt_2 ; results in Supplementary Materials.

A single reticulation was detected for all cases of intermixture and gene flow. We plotted the histograms of the true and estimated coalescence times of the MRCA of alleles from B and C in Fig. 20. As the figure shows, the distributions of estimated coalescence times match the distributions of true coalescence times very well. Eurthermore, when using 4,000 loci, the signal becomes even stronger; results in Supplementary Materials.

⁵¹ Finally, we assessed the performance of our method on cases where the reticulation event involves sister taxa. Fig. 17(e) and Fig. 17(f) show the cases we considered, with setting $h_1=2.5$ and $h_2=1.5$, and varying $t,mt \in \{\pm,0\}$.

⁵⁶ As the results in Table 3 demonstrate, our method obtained very accurate estimates of the various parameters under t=0 and mt=0. Under the cases of



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 $\begin{array}{c} t = 1 \\ t = 0 \\$

FIGURE 20. Histograms of the true (top) and estimated (bottom) coalescence times (in coalescent units) of the MRCA of alleles from B and C on data generated under the models of Fig. 17(c) and Fig. 17(d).

TABLE 3. Estimated population mutation rates (θ) , divergence times $(h_1 \text{ and } h_2)$, inheritance/migration rates, and numbers of reticulations (#reti) as a function of varying t in the model of Fig. 17(e) and mt in the model of Fig. 17(f). The divergence times were estimated in units of expected number of mutations per site and are reported in coalescent units by dividing by $\theta/2=0.01$.

| | Case | θ | h_1 | h_2 | γ | #reti |
|---|--------|-----------------------|---------------|-----------------|---------------------|-----------------|
| | | $2.0\pm0.2e^{-2}$ | 2.5 ± 0.1 | 1.3 ± 0.1 | NA | 0.0 ± 0.0 |
| | | | 2.5 ± 0.1 | 1.5 ± 0.0 | 0.21 ± 0.06 | 1.0 ± 0.0 |
| 1 | mt = 1 | $2.0 \pm 0.2 e^{-2}$ | 2.5 ± 0.1 | 1.4 ± 0.1 | \mathbf{NA} | 0.0 ± 0.0 |
| 1 | mt = 0 | $2.2\!\pm\!0.2e^{-2}$ | 2.5 ± 0.1 | $1.5\!\pm\!0.1$ | $0.11 \!\pm\! 0.06$ | $1.0\!\pm\!0.0$ |

intermixture with t=1 and gene flow with mt=1, our 18 method did not detect the reticulation, which resulted 19 in an underestimation of h_2 . In the case of mt=0, the 20 migration rate was severely underestimated, most likely 21 due to the short time interval between the migration and 22 divergence events between A and B. The method did 23 very well also in terms of estimating t and mt; results in 24 Supplementary Materials. 25

We plotted the histograms of the true and estimated coalescence times of the MRCA of alleles from A and B in Fig. 21. When t=1 and mt=1, the signal of

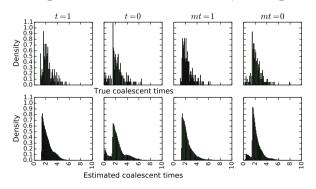


FIGURE 21. Histograms of the true (top) and estimated (bottom) coalescence times (in coalescent units) of the MRCA of alleles from A and B on data generated under the models of Fig. 17(e) and Fig. 17(f).

reticulation is very low, which explains the failure of our

method to detect it. In the cases of t=0 and mt=0, the distributions of estimated coalescence times match those of true coalescence times very well. When using 4,000 loci, the signal becomes even stronger; results in Supplementary Materials.

Analysis of a 106-locus Yeast Data Set

The yeast data set of (Rokas et al., 2003) consists of 36 106 loci from seven Saccharomyces species, S. cerevisiae 37 (Scer), S. paradoxus (Spar), S. mikatae (Smik), S. 38 kudriavzevii (Skud), S. bayanus (Sbay), S. castellii 39 (Scas), S. kluyveri (Sklu). Rokas et al. (Rokas et al., 40 2003) reported on extensive incongruence of single-41 gene phylogenies and revealed the species tree from 42 concatenation method (Fig. 22(a)). Edwards *et al.* 43 (Edwards et al., 2007) reported as the two main 44 species trees and gene tree topologies sampled from 45 BEST (Liu, 2008) the two trees shown in Fig. 22(a-b). 46 The other gene tree topologies (Fig. 22(c)) exhibited 47 weak phylogenetic signals among Sklu, Scas and the 48 other species. Bloomquist and Suchard (Bloomquist and 49 Suchard, 2010) reanalyzed the data set without Sklu 50 since it added too much noise to their analysis. Their 51 analysis resulted in many horizontal events between Scas 52 and the rest of the species because the Scas lineage-53 specific rate variation is much stronger than that of the 54 other species. Yu et al. (Yu et al., 2013b) analyzed the 55 f06-locus data set restricted to the five species Scer, 56

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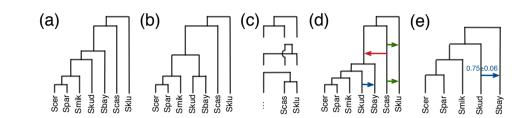


FIGURE 22. Results on the yeast data set of (Rokas *et al.*, 2003). (a) The species tree inferred using the concatenation method (Rokas *et al.*, 2003) and the main species tree and gene tree topology sampled using BEST (Edwards *et al.*, 2007). (b) The second most frequently sampled species and gene tree topology by BEST (Edwards *et al.*, 2007). (c) Many other gene tree topologies were sampled by BEST (Edwards *et al.*, 2007), indicating weak phylogenetic signals among Sklu, Scas, and the rest of the species. (d) The MAP phylogenetic network inferred by our method on all 106 loci. (e) The single phylogenetic network inferred using all 106 loci from the five species Scer, Spar, Smik, Skud, Sbay.

Spar, Smik, Skud, and Sbay and identified a maximum₆ parsimony network that supports a hybridization from⁷ Skud to Sbay with inheritance probability of 0.38. ²⁸

Analyzing the 106-locus data set using our method, the 95% credible set contains many topologies with similar hybridization patterns; the representative network is shown in Fig. 22(d). All the previous findings are encompassed by the networks inferred by our method.³⁰ The two hybridizations between Sklu and Scas (greenedges in 22(d)) indicate the weak phylogenetic signals² among Sklu, Scas and the rest of the species. The hybridization from Scas to the other species except for Sklu (red edge in 22(d)) captures the stronger lineages specific rate variation in Scas. Finally, the hybridization from Skud to Sbay (blue edge in 22(d)) resolves the incongruence between the two main species trees topologies in 22(a-b).

We then analyzed the 106-locus data set restricted too the five species Scer, Spar, Smik, Skud, and Sbay. Thei phylogenetic signal in this data set is very strong—the2 consensus trees of 99 out of the 106 loci contain two3 internal branches. The MPP phylogenetic network in Fig. 22(f) contains the hybridization from Skud to Sbay, which is identical to the sub-network in Fig. 22(d). See Supplementary Materials for full details. In summary, analysis of the yeast data set demonstrates the effect of phylogenetic signal in the individual loci on the inference and the care that must be taken when selecting loci of analysis of reticulate evolutionary histories.

We compared these analyses to ones obtained by the 11 method of (Wen *et al.* 2016a) when the input data consist 12 of gene tree estimates. When the gene tree estimates 13 on all seven Saccharomyces species are used, the 95%14 15 credible set consisted of a single network that is shown in Fig. 22(d), yet with only the single reticulation from 16 Skud to Sbay. When the gene tree estimates on the subset 17 of five species were used as input, the 95% credible set 18 consisted of a single network that is shown in Fig. 22(e), 19 in agreement with the results based on co-estimation 20 from the sequence data directly. 21

Finally, we quantified the Robinson-Foulds distances between the locus-specific gene tree estimates obtained by our method and by RAxML. The distances were 0.33 ± 0.19 for the 7-taxon data set, and 0.33 ± 0.16 for

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the 5-taxon data set. It is worth noting that these distances are very similar to those observed in Fig. 12 above. Full details and further results for this data set are given in Supplementary Materials.

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DISCUSSION

⁶⁵ To conclude, we have devised a Bayesian framework for sampling the parameters of the MSNC model, including the species phylogeny, gene trees, divergence times, and population sizes, from sequences of multiple independent loci. Our work provides the first general framework for Bayesian phylogenomic inference from sequence data in the presence of hybridization. The method is publicly available in the open-source software package PhyloNet (Than et al. 2008). We demonstrate the utility of our method on simulated data and three biological data sets. 75 Our results demonstrate several important aspects. First, ignoring hybridization when it had occurred results in underestimating the divergence times of species and overestimating the coalescence times of individual loci. Second, co-estimation of species phylogeny and gene 45 trees results in more accurate gene tree estimates than 46 the inferences of gene trees from sequences directly. 47 Third, comparing to existing phylogenetic network 48 inference methods (Wen et al. 2016a; Yu et al. 2014) 49 that use gene tree estimates as input, our method not 50 only estimates more parameters, such as divergence 51 times and population sizes, but also estimates more 52 accurate phylogenetic networks from fewer loci. Further, 53 we assessed the performance of our model and method 54 on simulated data generated under a gene flow model. 55 Our method performed very well on such data. However, 56 given the nature of our abstract phylogenetic network 57 model, a gene flow epoch is estimated as a single 58 reticulation event. Finally, we analyzed a 106-locus 59 veast data set and demonstrated for empirical data the 60 differences in results one obtains when co-estimating 61 the gene and species phylogenies when compared to 62 inferences from gene tree estimates. 63

Finally, we identify several directions for further improvements of our proposed approach. First, while priors on species trees, such as the birth-death model, have been developed and employed by inference methods, 67

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similar prior distributions on phylogenetic networks are₁ currently lacking. Second, while techniques such as² the majority-rule consensus exist for summarizing the⁴³ trees sampled from the posterior distribution, principled $\frac{4}{5}$ methods for summarizing sampled networks are needed₄₆ Last but not least, the sequence data used here, and in almost all phylogenomic analyses, consist of haploid⁸ sequences of randomly phased diploid genomes. The effect of random phasing on inferences in general needs to be studied in detail. Furthermore, the model could₂ be extended to work directly on unphased data by⁵³ integrating over possible phasings (Gronau *et al.* 2011). $_{55}^{54}$

SUPPLEMENTARY MATERIAL

Supplementary material, including data files and^o online-only appendices, can be found in the Dryad data repository at .

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