Modeling the consequences of regional heterogeneity in human papillomavirus (HPV) vaccination uptake on transmission in Switzerland

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Abstract

Background: Completed human papillomavirus (HPV) vaccination by age 16 years among women in Switzerland ranges from 17 to 75% across 26 cantons (states). The consequences of regional heterogeneity in vaccination coverage on transmission and prevalence of HPV-16 are unclear.

Methods: We developed a deterministic, population-based model that describes HPV-16 transmission among young adults within and between the 26 cantons of Switzerland. We parameterized the model using sexual behavior data from Switzerland and data from the Swiss National Vaccination Coverage Survey. First, we investigated the general consequences of heterogeneity in vaccination uptake between two sub-populations. We then compared the predicted prevalence of HPV-16 after the introduction of heterogeneous HPV vaccination uptake in all of Switzerland with homogeneous vaccination at an uptake that is identical to the national average (52%).

Results: HPV-16 prevalence in women is 3.34% when vaccination is introduced and begins to diverge across cantons, ranging from 0.14 to 1.09% after 15 years of vaccination. After the same time period, overall prevalence of HPV-16 in Switzerland is only marginally higher (0.55 %) with heterogeneous vaccination uptake than with homogeneous uptake (0.49%). Assuming inter-cantonal sexual mixing, cantons with low vaccination uptake benefit from a reduction in prevalence at the expense of cantons with high vaccination uptake.

Conclusions: Regional variations in uptake diminish the overall effect of vaccination on HPV-16 prevalence in Switzerland, although the effect size is small. Cantonal efforts towards HPV-prevalence reduction by increasing vaccination uptake are impaired by cantons with low vaccination uptake. Harmonization of cantonal vaccination programs would reduce heterogeneity in uptake and increase impact.

Keywords: human papillomavirus, vaccination, sexual behavior, mathematical model, Switzerland

1. Introduction

The first vaccine against human papillomavirus (HPV) was licensed in 2006 and is now widely used in many countries. At the population-level, HPV vaccination has led to a substantial reduction in the prevalence of the targeted HPV types (HPV-16/18/6/11 for the quadrivalent vaccine) as well as anogenital warts [1]. Most vaccination programs target girls or young women before they become sexually active. Regional differences in vaccination uptake have emerged in some countries after implementation of the vaccination programs [2, 3]. These differences are very pronounced in Switzerland where the proportion of complete three dose vaccination schedule in 16 year old girls ranges from 17 to 75% in 26 cantons (states) (Fig. 1) [4, 5]. The cantonal heterogeneity in vaccination uptake can be partly explained by differences in the way the vaccine is offered

to women (e.g., school-based programs, general practitioners or gynecologist). Other factors, such as cultural differences between the cantons might play a role too. To date, the potential epidemiological consequences of regional variation in vaccination uptake on transmission and prevalence of HPV in Switzerland and other countries are not well understood.

Mathematical models have played an important role in estimating the expected impact of vaccination on the transmission of HPV [6–8] and other infections [9]. Investigating the consequences of spatial heterogeneity in vaccination uptake has received less attention, with some mentionable exceptions. Studies on measles vaccination [10, 11] and canine rabies [12] showed that spatial vaccination heterogeneity leads to less effective control of the targeted disease when compared with homogeneous vaccination. The debate about heterogeneity in HPV vaccination uptake has focused on sex-specific vaccination [13, 14]. Sex-specific vaccination is expected to be more beneficial than to homogeneous (male/female) vaccination in a heterosexual population because both sexes are required for the transmission. Therefore if only one sex is targeted by the vaccine, although around 50% of the total population would be

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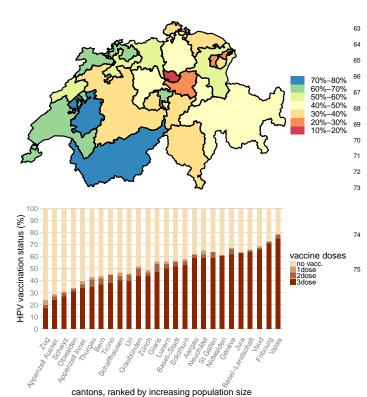


Fig. 1. HPV vaccination uptake in 16 year old girls in Switzerland. Data represent the last completed survey period (2011-2013) of the Swiss National Vaccination Coverage Survey (SNVCS). Data for Geneva and Appenzell Innerrhoden are from 2010 and 2014, respectively.

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vaccinated, the transmission would be blocked as the vaccinetargeted sex would act as a dead-end host. Spatial variation in HPV vaccination uptake between states in the United States of America (USA) has been taken into account in a modeling study that quantified the epidemiological impact and costeffectiveness of adopting a new, nonavalent HPV vaccine [15]. This study illustrated that expanding vaccination coverage in states with low coverage would result in the greatest health impact because of the decreasing marginal returns of herd immunity. This finding is supported by another modeling study from Canada showing that the effect of unequal vaccination uptake 76 among school girls by ethnicity on cervical cancer incidence may be lower than with equal vaccination [16]. The effects of spatial heterogeneity in vaccination uptake crucially depend on 79 sexual mixing between between different regions, as well as 80 herd immunity thresholds and other disease-specific characteristics. A better understanding of how these factors affect the transmission and prevalence of HPV may help to better inter-83 pret the expected or observed impact of HPV vaccination pro-

The aim of this study was to investigate the impact of het-86 erogeneous vaccination uptake and different sexual mixing sce- 87 narios on the prevalence of HPV-16 in Switzerland. Our main 88 hypothesis was that heterogeneous vaccination would substan-89 tially reduce the impact of vaccination. We developed a math- 90 ematical model of HPV-16 transmission among young hetero- 91 sexual adults. We parameterized the model using Swiss sexual behavior data and calculated the pre-vaccination prevalence and the basic reproduction number (R_0) of HPV-16. First, we investigated the general consequences of heterogeneous vaccination uptake in a simple model with two sub-populations. We then simulated the transmission of HPV-16 within and between the 26 cantons of Switzerland assuming three different scenarios for inter-cantonal sexual mixing. We compared the predicted post-vaccination prevalence of HPV-16 after the introduction of heterogeneous HPV vaccination uptake with a default scenario of homogeneous vaccination.

2. Methods

2.1. HPV-16 transmission model

We developed a deterministic, population-based model of HPV-16 transmission that is based on well-establish work on modeling sexually transmitted infections (STIs) [17–19]. We implemented the spatial (cantonal) structure into a metapopulation model, and considered the population of 18–24 year old heterosexual Swiss adults who can be susceptible (S), infected (I), recovered (R) or vaccinated (V). These compartments are further divided into sub-compartments that reflect the individuals' sex, sub-population/canton and sexual activity level, and can be described by the following system of ordinary differential equations (ODEs):

$$\frac{dS_{skr}}{dt} = (1 - p_{sk})\mu N_{skr} - \lambda_{skr} S_{skr} + \omega R_{skr} - \mu S_{skr}$$

$$- mS_{skr} + mn_r \sum_{u} S_{sku},$$
(2)

$$-mS_{skr} + mn_r \sum_{u} S_{sku}, \tag{2}$$

$$\frac{dI_{skr}}{dt} = \lambda_{skr}S_{skr} - \gamma I_{skr} - \mu I_{skr} - mI_{skr} + mn_r \sum_{u} I_{sku}, \quad (3)$$

$$\frac{dR_{skr}}{dt} = \gamma I_{skr} - \omega R_{skr} - \mu R_{skr} - mR_{skr} + mn_r \sum R_{sku}, \quad (4)$$

$$\frac{dV_{skr}}{dt} = p_{sk}\mu N_{skr} - \mu V_{skr} - mV_{skr} + mn_r \sum_{u} V_{sku}. \tag{5}$$

Here, the subscripts s, k and r denote sex, population/canton and sexual activity group, respectively. Susceptible individuals (S) can become infected at rate λ_{skr} (force of infection). Infected individuals (I) spontaneously clear HPV-16 at rate γ to become temporarily immune. Recovered individuals (R) loose their immunity at rate ω and become susceptible again. All individuals enter and leave the population at rate μ with $N_{skr} = S_{skr} + I_{skr} + R_{skr} + V_{skr}$ being the population size of individuals that have sex s, reside in sub-population/canton kand belong to sexual activity group r. p_{sk} is the sub-populationor canton-specific proportion of individuals that are vaccinated upon entering the population. We assumed vaccine efficacy is 100% (3 doses) and lasts for an individual's sexual lifetime. Individuals can change their sexual behavior at rate m, i.e., they are redistributed to either the same or another sexual activity group proportional to the size of the target group [19, 20].

2.2. Data and parameters

2.2.1. Vaccination uptake

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We used data from the Swiss National Vaccination Cover-147 age Survey (SNVCS) to obtain the proportion of women who 148 are vaccinated in each canton (Fig. 1, table, A.4). The SNVCS¹⁴⁹ monitors immunization coverage of children and adolescents¹⁵⁰ and compiles them into three-year bands. For HPV vaccina-151 tion, the survey focuses on 16 years old girls. In this study, we used data from the last available survey period (2011-152 2013), except for the canton of Geneva (GE) and Appenzell¹⁵³ Innerrhoden (AI) where we used data from the years 2010 and₁₅₄ 2014, respectively. Two HPV vaccines are currently authorized 155 in Switzerland: Gardasil® (Sanofi Pasteur MSD) which tar-156 gets four HPV types (HPV-6/11/16/18), and Cervarix® (Glax-157 oSmithKline) which targets two HPV types (HPV-16/18). In,150 Switzerland 95% of vaccinated women recieved the quadri-159 valent vaccine [4]. We used the proportion of fully vaccinated women (completed three doses) as a model parameter. Although Switzerland adopted the two-dose HPV vaccination schedule in 2012, we assumed that this has not been imple-160 mented in the cantonal programmes at the time the survey was led. We did not consider HPV vaccination in boys and young men, as uptake in Switzerland is negligible at present.

2.2.2. Sexual behavior

We used data from the SIR (Screening, Impfung und Risikofaktoren) survey [4]. The Swiss Federal Office of Public Health (FOPH) conducted this survey in 2014 and collected data on the sexual behavior of 18–24 year old Swiss women (n = 1, 291). We categorised the study participants into two sexual activity groups and estimated the sexual partner change rates by assuming that the reported numbers of new heterosexual partners in the last year can be described by two Poisson distributions, weighted by the proportion of individuals in each sexual activity group [19, 21]. The survey did not include men, so we assumed their sexual activity to be the same as for women. Furthermore, we assumed that sexual behavior does not differ between cantons. We compared the modeled prevalence of HPV-16 based on the Swiss sexual behavior data to the expected prevalence¹⁶¹ based on data from the third British National Survey of Sexual¹⁶² Attitudes and Lifestyles 3 (Natsal-3, n = 1,611) [22].

2.2.3. Inter-cantonal mixing

We used mobility data from the Swiss Federal Office for Spa-166 tial Development (ARE) as a proxy for sexual mixing between 167 different cantons. The data set contains the average daily com-168 muting data by public transport and individual vehicles from 169 Monday to Friday in 2010 [23].

2.2.4. Other parameters

We used publicly available data about the number of 18–24₁₇₃ year olds in each canton in 2013 from the website of the Swiss₁₇₄ Federal Statistical Office (FSO) [24]. Parameters that describe₁₇₅ the transmission and life-history of HPV-16 were informed by₁₇₆ the literature [25, 26] and assumed to be the same for women₁₇₇ and men. All parameter values and their sources are specified₁₇₈ in Table 1.

2.3. Sexual mixing and force of infection

The force of infection, λ_{skr} , depends on assumptions about sexual contact preferences between individuals from different sexual activity groups and sub-populations/cantons. We devised three different scenarios of increasing complexity to account for different spatial mixing patterns (Fig. 2):

- 1. Assortative sexual mixing: Sexual contacts only occur between individuals from the same sub-population/canton.
- Proportional sexual mixing: A fraction of sexual contacts occur between individuals from the same sub-population/canton, while the remaining contacts are proportionally distributed across all sub-populations/cantons.
- 3. *Mobility-informed sexual mixing*: Swiss mobility data are used as a proxy for inter-cantonal sexual mixing.

2.3.1. Assortative and proportional sexual mixing

The first two scenarios where we assumed fully assortative or partial proportional mixing between sub-populations/cantons result in the following force of infection:

$$\lambda_{skr} = \beta c_r \sum_{k'} \sum_{r'} \rho_{ss'kk'rr'} \frac{I_{s'k'r'}}{N_{s'k'r'}},$$
 (6)

where β is the per partnership transmission probability and c_r is the sexual partner change rate for individuals of sexual activity group r. The elements of the sexual mixing matrix

$$\rho_{ss'kk'rr'} = \rho_{ss'kk'}\rho_{rr'}$$

$$\left[\epsilon_k \delta_{kk'} + (1 - \epsilon_k) \frac{\sum_{\nu} c_{\nu} N_{s'k'\nu}}{\sum_{u} \sum_{\nu} c_{\nu} N_{s'u\nu}}\right]$$
(7)

$$\times \left[\epsilon_r \delta_{rr'} + (1 - \epsilon_r) \frac{c_{r'} N_{s'k'r'}}{\sum_{\nu} c_{\nu} N_{s'k'\nu}} \right]$$
(8)

describe the conditional probability of an individual of sex s, sub-population/canton k and sexual activity group r to have a sexual contact with an individual of the opposite sex s', sub-population/canton k' and sexual activity group r'. and ϵ_r are the sexual mixing coefficients with respect to subpopulation/canton and sexual activity group, respectively. Values of 1 represent fully assortative mixing where individuals only have sexual contacts with other individuals from the same sub-population/canton or sexual activity group. A value of 0 corresponds to proportional (random) mixing where sexual partners are chosen in proportion to the size of their subpopulation/canton and their sexual activity group. $\delta_{kk'}$ and $\delta_{rr'}$ are the Kronecker deltas that are equal to 1 if k = k' or r = r'and to 0 otherwise. In the first scenario (assortative sexual mixing), we set $\epsilon_k = 1$. In the second scenario (proportional sexual mixing), we set ϵ_k to 0.6 (model with two sub-populations) and 0.8 (cantonal model). Throughout all simulations, we set $\epsilon_r = 0.5$, which corresponds to partially assortative mixing with respect to sexual activity [19, 20].

Table 1. Summary of parameters for the HPV-16 transmission model.

Parameter	Description	Value	Unit	Reference/Comment
N_{skr}	Number of 18–24 year olds of sex s, sub-	See Table A.3	_	Swiss FSO
	population/canton k and activity group r			
n_l	Proportion in the low sexual activity group	0.85	_	Estimated
n_h	Proportion in the high sexual activity group	0.15	_	Estimated
c_l	Heterosexual partner change rate in low activity group	0.17	per year	Estimated
c_h	Heterosexual partner change rate in high activity group	2.41	per year	Estimated
μ	Rate at which individuals enter and leave the population	0.14	per year	7-year age band
m	Rate at which individuals can change activity groups	1.0	per year	[19, 20]
ϵ_r	Assortativity index for sexual mixing between activity	0.5	_	[19, 20]
	groups			
ϵ_k	Assortativity index for sexual mixing between sub-	0.6,0.8,1.0	_	Assumption
	populations/cantons			
S	Scaling factor for mobility-informed sexual mixing ma-	0.035	-	Calculated
	$\operatorname{trix} \sigma_{kk'}$			
$oldsymbol{eta}$	Transmission probability per partnership	80%	_	[25]
γ	Rate at which infection is cleared spontaneously	0.55	per year	[26]
ω	Rate at which immunity is lost	0.024	per year	[26]
p_{sk}	Proportion of vaccinated individuals in canton k	Fig. 1	-	Swiss FOPH

2.3.2. Mobility-informed sexual mixing

We used mobility data as a proxy for inter-cantonal sexual 186 mixing by assuming that the heterosexual partner preference 187 across cantons is proportional to the corresponding commut-188 ing patterns. The symmetrical matrix $P_{\rm mob}$ provides absolute 189 numbers of commuters between cantons without specifying the 190 commuters' canton of residence. We converted $P_{\rm mob}$ into an 191 asymmetrical inter-cantonal mixing matrix $\sigma_{kk'}$ that provides 192 the conditional probabilities that a sexual contact from an in-193 dividual from canton k occurs with someone from canton k'. 194 To this end, we first rescaled $P_{\rm mob}$ by a scaling factor s and weighted all columns with the inverse of the cantonal population size:

$$\sigma_{kk'} = s \frac{P_{\text{mob}}}{N_k}.$$
 (9)19

We then replaced the diagonal entries of $\sigma_{kk'}$ with the sum of all entries that are outside canton k:

$$\sigma_{kk} \mapsto 1 - \sum_{i \neq k} \sigma_{ki}. \tag{10}_{20}^{20}$$

The force of infection for the mobility-informed sexual mix-203 ing scenario is given by Eq. 6 with $\rho_{ss'kk'rr'}$ being replaced by²⁰⁴ $\sigma_{kk'}\rho_{ss'rr'}$. We chose the scaling factor s such that the weighted²⁰⁵ proportion of intra-cantonal heterosexual contacts across all²⁰⁶ cantons is 80% (Fig. A.8), i.e., is the same as in the propor-²⁰⁷ tional sexual mixing scenario:

$$\sum_{k} \sigma_{kk} \frac{N_k}{\sum_{k} N_k} = 0.8. \tag{11}^{210}$$

2.4. Model simulations

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We simulated the different model scenarios by numerically₂₁₃ integrating the ODEs until the system approached the endemic₂₁₄ pre-vaccination equilibrium ($p_{sk}=0$). We then initiated₂₁₅

the HPV vaccination program by setting $p_{sk} > 0$, and ran the model for a further number of years. The ODEs were solved in the R software environment for statistical computing [27] using the function *ode* from the package *deSolve*. We calculated the basic reproduction number (R_0) using the next-generation matrix method as described by Diekmann et al. [28, 29] (Appendix A.1). This allowed us to compute the vaccination threshold $V_C = 1 - 1/R_0$. All code files can be downloaded from GitHub (https://github.com/mauraner/HPV-regional-vaccine-heterogeneity-model).

3. Results

3.1. HPV-16 dynamics

Using the parameters from Table 1, the transmission model provides a realistic description of the HPV-16 dynamics in Switzerland. The pre-vaccination prevalence of HPV-16 is 3.34% among 18-24 year olds. While this is somewhat lower than the expected and observed HPV-16 prevalence in Britain (Appendix A.2), it is in the range that is typically observed among women in other European countries [30]. The functional relationship between vaccination coverage and the reduction in HPV-16 prevalence 2 to 4 years post-vaccination is in good agreement with the findings of a systematic review (Appendix A.3) [1]. The basic reproduction number, R_0 , of HPV-16 in our model is 1.29. This value corresponds to a vaccination threshold of 22% in the general population. If vaccination is targeting only one sex, the threshold increases to 39%.

3.2. Vaccination in two sub-populations

To better understand the effects of spatially heterogeneous vaccination uptake on infection transmission, we focused on a simplified model with just two sub-populations of the same size. We calculated the expected HPV-16 prevalence after 50

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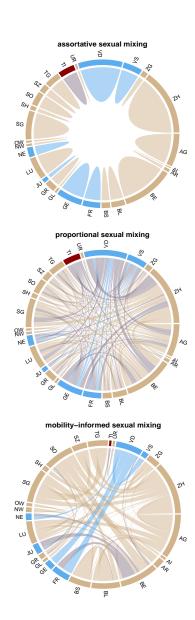
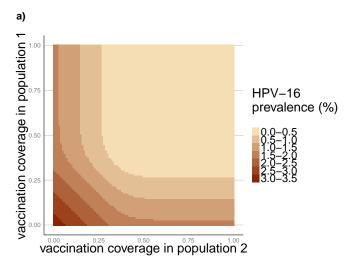
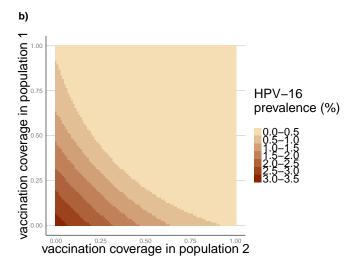


Fig. 2. Chord diagram of inter-cantonal sexual mixing according the different scenarios. The diagrams shows the number of sexual contacts between individuals who live in different cantons. In the scenarios where sexual mixing between cantons occurs (proportional and mobility informed sexual mixing), sexual contacts between individuals that reside in the same canton are excluded for better visibility. Cantons with a French-, German- or Italian-speaking majority are indicated in blue, beige and red, respectively.





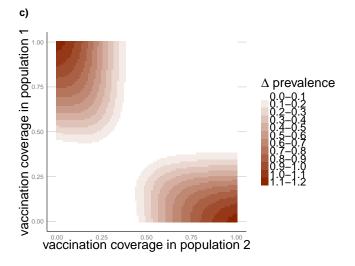


Fig. 3. Heterogeneous vaccination uptake and HPV-16 prevalence. The graphs show the expected prevalence of HPV-16 after 50 years of vaccinating two subpopulations at different coverage rates. a) HPV-16 prevalence when there is no sexual mixing between the two populations. b) HPV-16 prevalence when 20% of sexual contacts are made between the two populations ($\varepsilon_k=0.6$). c) Difference in HPV-16 prevalence between scenario a and b.

years of vaccinating the two sub-populations at different cov-272 erage rates (Fig. 3). In the first scenario, we assumed fully as-273 sortative sexual mixing between the two sub-populations, i.e.,274 sexual contacts only occur between individuals from the same₂₇₅ sub-population (Fig. 3a). The concave relation between vac-276 cination coverage in the two sub-populations and the expected₂₇₇ prevalence of HPV-16 overall indicates that homogeneous vac-278 cination uptake always has the largest effect on reducing preva-279 lence. For example, a vaccination coverage of 25% in both sub-280 populations results in a lower prevalence than vaccinating ei-281 ther of them at 50%. In the second scenario, we assumed a282 certain level of proportional mixing where 20% of sexual con-283 tacts are made with individuals from the other sub-population284 (Fig. 3b). Sexual mixing between the two sub-populations di-285 minishes the negative effect of heterogeneous vaccination up-286 take, but homogeneous vaccination still results in the lowest287 prevalence of HPV-16. Fig. 3c shows the difference in the ex-288 pected HPV-16 prevalence between the first (no sexual mixing289 between the sub-populations) and second (sexual mixing be-290 tween the sub-populations) scenario. The higher the difference,291 the stronger the effect of sexual mixing is in reducing the nega-292 tive consequences of heterogeneous vaccination uptake. This is₂₉₃ particularly the case when vaccination is highly heterogeneous,294 i.e., when uptake is very high in one sub-population and very295 low in the other sub-population. In summary, these results il-296 lustrate that spatially heterogeneous vaccination uptake diminishes the effect of vaccination on reducing HPV-16 prevalence, but that sexual mixing between sub-populations can limit these undesired consequences by 'homogenizing' the overall popula-298

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3.3. Transmission of HPV-16 within and between cantons

We extended our analysis of heterogeneous vaccination up-302 take by simulating the transmission of HPV-16 within and be-303 tween the 26 cantons of Switzerland. The observed dynamics₃₀₄ generalize some of the insights from the simplified model with305 two-subpopulations. After vaccination is introduced, HPV-16306 prevalence begins to diverge across cantons (Fig. 4). After 15₃₀₇ years of vaccination, the range of expected HPV-16 prevalences308 depends on the assumed scenario for sexual mixing between309 cantons (see Methods). For fully assortative mixing, the highest310 and lowest prevalence are 2.40% (ZG, 17% vaccination cover-311 age) and 0.12% (VS, 75% vaccination coverage), respectively₃₁₂ (Fig. 4a). The range of cantonal HPV-16 prevalence narrows313 if sexual mixing between cantons is taken into account. The314 cantonal prevalence ranges from 1.28% to 0.23% for propor-315 tional mixing (Fig. 4b), and from 1.09% to 0.14% for mobility-316 informed mixing (Fig. 4c). Thus, sexual mixing between can-317 tons again 'homogenizes' the infection dynamics and the effect318 of vaccination on reducing prevalence.

This effect is also reflected in the overall prevalence of HPV-320 16 in Switzerland. The national prevalence of HPV-16 is321 slightly higher under heterogeneous vaccination uptake com-322 pared with homogeneous uptake (Fig. 4a). This difference be-323 comes smaller in the two scenarios that assume sexual mixing324 between the two cantons (Fig. 4b and 4c). In the most real-325 istic scenario (mobility-informed mixing), the national preva-326

lence of HPV-16 is expected to drop to 0.55% after 15 years of heterogeneous vaccination uptake, while homogeneous vaccination uptake would drop the prevalence to 0.49%.

Inter-cantonal sexual mixing helps to reduce the prevalence of HPV-16 in cantons with low vaccination coverage at the expense of cantons with high vaccination coverage. At the national level, increasing sexual mixing between cantons always results in a lower HPV-16 prevalence (Fig. 5, dashed red lines), while the effect of sexual mixing at the cantonal level is more complex. The number of cantons that achieve a specific reduction in prevalence – expressed as relative risk (RR) reduction - can either decrease or increase with varying degrees of sexual mixing (Fig. 5). For example, high levels of sexual mixing between cantons (low ϵ_k) increase the number of cantons that achieve a 50% reduction in prevalence after 15 years of vaccination (Fig. 5a). In contrast, low levels of sexual mixing between cantons (high ϵ_k) are required to increase the number of cantons that achieve a RR reduction of 90%. On a timescale of 50 years, the number of cantons that reach a RR reduction of 99% is lowest for low, but realistic, levels of sexual mixing between cantons ($\epsilon_k = 0.85 - 0.95$) (Fig. 5b). These levels of sexual mixing prevent the elimination of HPV-16 in highcoverage cantons, but they are too low for low-coverage cantons to sufficiently benefit from the herd immunity of high-coverage cantons.

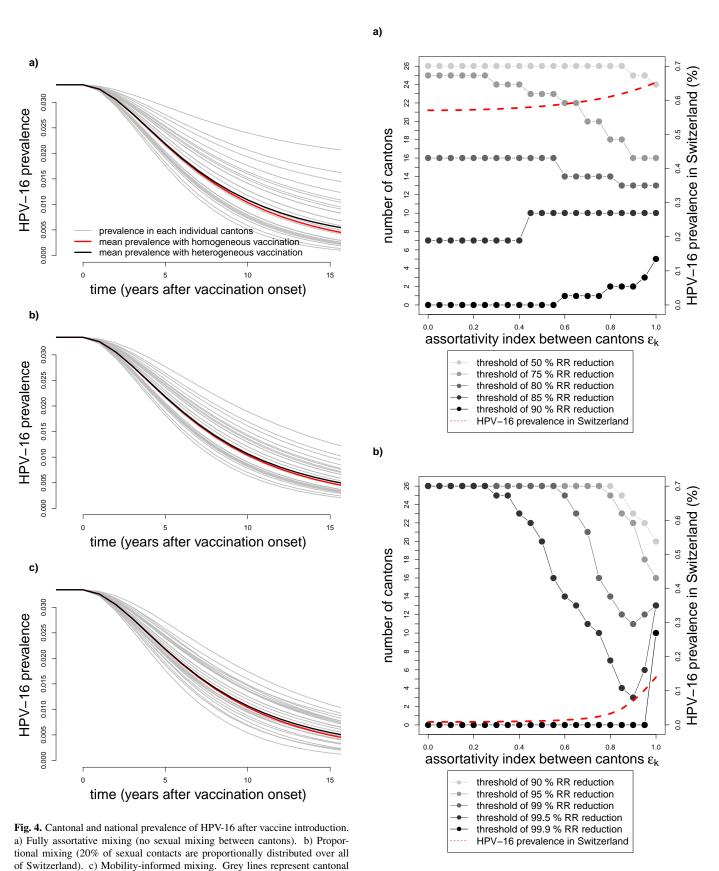
4. Discussion

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Uptake of HPV vaccination in 16 year old girls in Switzerland shows pronounced differences between different cantons ranging from 17 to 75%. We used a dynamic transmission model to study the expected consequences of this spatial heterogeneity in vaccination uptake on the transmission and prevalence of HPV-16 in Switzerland. Using a simple model with just two sub-populations, we found that heterogeneous vaccination uptake can diminish the effect of vaccination on reducing HPV-16 prevalence. This effect is particularly strong when vaccination is highly heterogeneous, i.e., when uptake is very high in one sub-population and very low in the other sub-population. These results were then corroborated with an extended model simulating the transmission of HPV-16 within and between the 26 cantons of Switzerland. Homogeneous vaccination uptake would generate a lower national HPV-16 prevalence compared to heterogeneous vaccination uptake, but the differences in prevalence are very small. We found that intercantonal sexual mixing homogenizes the infection dynamics, limits the undesired consequences of heterogeneous vaccination uptake, and reduces the inter-cantonal differences in HPV-16 prevalence.

This study describes the transmission of HPV-16 in Switzerland using a mathematical model to investigate how spatial heterogeneity in vaccination uptake affects prevalence. The example of Switzerland provides sufficient data for parameterizing a dynamic transmission model while exhibiting large variation in HPV-16 vaccine deployment. Using Swiss sexual behavior data, the model provided a realistic description of HPV-16 transmission in Switzerland, and allowed us to investigate the



HPV-16 prevalence. The black and red lines correspond to the national preva-Fig. 5. Relationship between inter-cantonal sexual mixing and HPV-16 prevalence for heterogeneous and homogeneous vaccination uptake, respectively. lence. The graphs show the number of cantons that achieve a specific relative risk (RR) reduction after 15 years (a) and 50 years (b) of vaccination. The dashed red lines correspond to the national prevalence which is lowest if sexual mixing is completely proportional ($\epsilon_k = 0$). For all simulations, we used the proportional sexual mixing scenario.

expected effect of HPV vaccination. Our results do not change₃₈₄ qualitatively when the number of cantons or parameter values₃₈₅ are varied within reasonable ranges. In the absence of data de-₃₈₆ scribing inter-cantonal sexual mixing in Switzerland, we used₃₈₇ commuting data and explored three different scenarios. The two₃₈₈ scenarios that assumed partial sexual mixing between cantons₃₈₉ – proportional sexual mixing and mobility-informed mixing –₃₉₀ gave rise to a similar pattern, strengthening the validity of our₃₉₁ findings.

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Our study has a number of limitations that need be consid-393 ered when interpreting the findings. First, we used a relatively₃₉₄ simple model to describe the transmission of HPV-16, not tak-395 ing into account potential sex-specific differences in sexual be-396 havior and the infection life-history. Due to our focus on the397 transmission and prevalence of HPV-16, we did not include the398 progression of HPV infections to cervical intraepithelial neo-399 plasia (CIN), as other modeling studies have done [7, 8, 25, 26].400 Further, we did not consider different age classes and assumed₄₀₁ that women can only become vaccinated before the age of 18.402 It is also important to note that our results depend on the as-403 sumption that the sexual behavior and the subsequent risk of 404 HPV infection is the same across different cantons. Second,405 the comparison of the sexual behavior data (i.e., the estimated₄₀₆ heterosexual partner change rates) between Swiss and British407 women needs to be treated with caution. Although the partic-408 ular question about the number of new heterosexual partners409 was the same in both surveys, the methods for sampling and410 data collection differed considerably. While the SIR survey in-411 terviewed participants by phone, Natsal-3 relied on individuals₄₁₂ filling in questionnaires at the participants' homes. This differ-413 ence could have introduced a social desirability bias that could414 result in an underestimation of the heterosexual partner changes₄₁₅ based on the SIR study. Given the sensitivity of our model with 416 regard to per partnership transmission probabilities (Fig. A.6)₄₁₇ and heterosexual partner change rates, our calculations of $R_{0.418}$ and the vaccination threshold should be interpreted with cau-419 tion. Third, in absence of data about the levels of sexual mixing₄₂₀ between cantons, we assumed that inter-cantonal sexual mixing421 is proportional to the observed commuting patterns. Further-422 more, we assumed that the national average of sexual contacts₄₂₃ that are made with individuals from the same canton is 80%,424 and that 20% are made with individuals from another canton.425 This assumption was informed by a Canadian study on couple426 composition regarding language membership (French, English₄₂₇ or other) led in 1981 [31]. On average, 18.2% of couples in₄₂₈ Quebec were exogamous, with some heterogeneity over differ-429 ent regions. Fourth, besides inter-cantonal variation in HPV430 vaccination uptake, there is also intra-cantonal variation. For₄₃₁ example, vaccination uptake in Geneva, which has a school-432 based vaccination program, varies significantly among differ-433 ent nationalities and socio-economical status [32]. Investigat-434 ing the causes and consequences of intra-cantonal variation in₄₃₅ HPV vaccination uptake in Switzerland is part of ongoing work.436

There are currently no population-based prevalence esti-437 mates of type-specific HPV in Switzerland. Our modeled pre-438 vaccination prevalence of HPV-16 is 3.34%, and is within a439 plausible range for women in European countries. A meta-440

analysis of more than 1 million women estimated HPV-16 prevalence at 4.8% and 3.2% in Europe and globally, respectively [30]. Only a few studies provide estimates for the basic reproduction number, R_0 , or equivalently, the vaccination threshold of HPV-16 or other HPV types. Ribassin-Majed et al. [33] estimated $R_0 = 1.73$ for HPV-16/18 in France, corresponding to a vaccination threshold of 67% for one sex. These values are higher than what we calculated for Switzerland, but in a similar range to what would be expected in Britain (Table A.2). The lower values that we calculated for Switzerland underline the possibility of underreporting in the Swiss sexual behavior survey.

Our results need to be interpreted in the context of the current HPV literature considering heterogeneity in vaccination. The finding that decreasing heterogeneity in vaccination uptake increases impact helps interpreting the result by Durham et al. [15] who showed that vaccination efforts should be targeted towards low-vaccination states in the USA. Increasing vaccination uptake in populations with low-vaccination uptake has the strongest effect for reducing vaccination heterogeneity overall. The study by Shafer et al. [16] on unequal HPV vaccination uptake among different ethnic groups in Canada, suggests that heterogeneous vaccination can lead to spillover effects across groups. Our study illustrates that the effect of heterogeneous vaccination uptake between different populations will largely depend on the amount of sexual mixing between them.

Our findings could have implications for the future planning of HPV vaccination programs at the cantonal and national level in Switzerland. From the point of view of a particular canton, the achieved reduction in HPV-16 prevalence will not only depend on the cantonal vaccination program, but also on the indirect effects of vaccination efforts in other (particularly neighboring) cantons and how these effects are dissipated via intracantonal sexual mixing. For the most plausible scenario for inter-cantonal mixing (mobility-informed sexual mixing), we found that cantons with high vaccination coverage experience a less effective reduction in HPV-16 prevalence to what would be expected if they were isolated (assortative sexual mixing). Conversely, this effect benefits those cantons with a low vaccination uptake that achieve a higher reduction in prevalence to what would be expected in absence of intra-cantonal sexual mixing. The intensity of cantonal dissipation of vaccination efforts is again mediated by intra-cantonal sexual mixing. The number of cantons that surpass a pre-defined RR reduction is highly sensitive to the level of assortative mixing between cantons (Fig. 5). The results of this study suggest that a harmonization of programs between cantons, and a reduction in vaccination heterogeneity, would result in a stronger effect of vaccination on reducing HPV-16 prevalence in Switzerland. The generality of our results on the effects of spatial heterogeneity in vaccination uptake are also of interest in the context of other infectious diseases.

In summary, we found that spatial heterogeneity in HPV vaccination uptake is expected to diminish the effect of vaccination on HPV-16 prevalence, but the overall effect is small. In the context of Switzerland, this means that cantonal efforts towards a reduction of HPV-prevalence are impaired by cantons with

low vaccination uptake. Harmonisation of cantonal vaccination programmes would reduce inter-cantonal differences in prevalence

Acknowledgment

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Appendix A. Supplementary material

Appendix A.1. Basic reproduction number

The basic reproduction number, R_0 , can be calculated using the next-generation matrix method as described by Diekmann et al. [28, 29]. As we did not consider sex-specific differences in sexual behavior or the natural history of HPV-16, and assumed that the sexual behavior of individuals is the same across all cantons, we can simplify the model into a single population with two different sexual activity groups. The transmission matrix F can then be given by

$$F = \begin{bmatrix} \beta c_l \rho_{ll} n_l / n_l & \beta c_l \rho_{lh} n_l / n_h \\ \beta c_h \rho_{hl} n_h / n_l & \beta c_h \rho_{hh} n_h / n_h \end{bmatrix}, \tag{A.1}$$

whereas the transition matrix V is given by

$$V = \begin{bmatrix} \gamma + \mu + mn_h & -mn_l \\ -mn_l & \gamma + \mu + mn_l \end{bmatrix}. \tag{A.2}$$

 R_0 is defined as the dominant eigenvalue of the next-generation matrix $G = FV^{-1}$.

Appendix A.2. HPV-16 dynamics: Comparison to Britain

In order to compare the modeled prevalence of HPV-16 in Switzerland and Britain, we parameterized the transmission model with data from the third British National Survey of Sexual Attitudes and Lifestyles 3 (Natsal-3) [22]. To this end, we estimated the sexual partner change rates for the same two sexual activity groups (Table A.2). For better comparison between Switzerland and Britain, we forced the size of the sexual activity groups to be the same between the two countries (see Table 1). The estimated heterosexual partner change rates for both sexual activity groups in Britain are higher than in Switzerland. Hence, the modeled pre-vaccination prevalence of HPV-16 for a given per partnership transmission probability is higher for the British model than the Swiss model (Fig. A.6). The per partnership transmission probability is a highly model-specific parameter with considerable uncertainty. Two different modeling studies estimated the transmission probability at 0.72 (95% posterior interval: [0.29 - 1.00]) [26] and 0.80 (95% posterior interval: [0.60, 0.99]) [25]. For our subsequent analyses, we chose a transmission probability of 0.80, as estimated by Bogaards et al. [25], because it results in realistic HPV-16 prevalences for Britain and Switzerland.

Table A.2. Comparison of model parameters and outputs between Switzerland (SIR survey) and Britain (Natsal-3). The model outputs are based on a per partnership transmission probability of 80% [25].

Parameter/Output	SIR	Natsal-3
Partner change rate low activity (y ⁻¹)	0.17	0.37
Partner change rate high activity (y^{-1})	2.41	3.60
Pre-vaccination prevalence of HPV-16	3.34%	7.72%
Basic reproduction number, R_0	1.29	1.90
Vaccination threshold for one sex	39.6%	72.3%

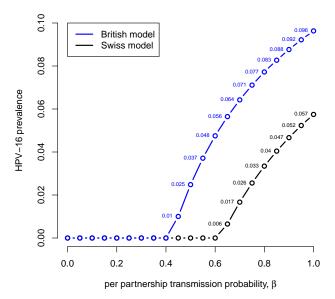


Fig. A.6. Prevalence of HPV-16 as a function of the per partnership transmission probability. The modeled pre-vaccination prevalences are based on Swiss (black) and British (blue) data (SIR and Natsal-3 survey, respectively).

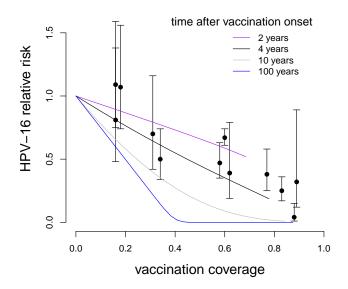


Fig. A.7. Reduction in HPV-16 prevalence as a function of vaccination coverage. The solid lines represent the modeled HPV-16 prevalence, normalized and expressed as a relative risk (RR), after 2, 4, 10 and 100 years of vaccination. The data represent the change in HPV-16/18 prevalence between the pre- and post-vaccination periods from several countries as reported in the systematic review by Drolet et al. [1]. Individual points represent data with different vaccination coverage from either 13–19 or 20–24 year old girls in the US, United Kingdom or Australia. The difference between the pre-vaccination and post-vaccination periods ranged between 1–4 years.

Appendix A.3. HPV-16 dynamics: Vaccination coverage and prevalence

We compared the functional relationship between the vaccination coverage and the expected reduction in HPV-16 prevalence from our model with data from a systematic review [1]. In the model described in the main text, we assumed that women can only become vaccinated before they enter the population of 18–24 year olds. For a given proportion of women that become vaccinated p, it typically takes a number of years until the proportion of vaccinated women across the 18-24 year age band approaches the same value. In order to compare our model results with the data, we did a modification in how vaccination is modeled and assumed that all 18-24 year old susceptible women can become vaccinated at rate p per year. And when we look at the vaccination coverage we consider the proportion of the population which is effectively vaccinated at a given time point. The modeled reduction in HPV-16 prevalence 2-4 years after onset of vaccination is in good agreement with the reported data from several studies that covered a time span of 1–4 years (Fig. A.7).

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Table A.3. Cantonal population sizes of 18–24 year old women and men in Switzerland. For the transmission model, we assumed a 1:1 sex ratio. Data are from the Swiss Federal Statistical Office (FSO).

Canton	Acronym	Population size
Zürich	ZH	105,586
Bern	BE	80,549
Luzern	LU	35,656
Uri	UR	3269
Schwyz	SZ	12,641
Obwalden	OW	3269
Nidwalden	NW	3513
Glarus	GL	3477
Zug	ZG	8838
Fribourg	FR	27,666
Solothurn	SO	22,161
Basel-Stadt	BS	13,441
Basel-Landschaft	BL	21,313
Schaffhouse	SH	6587
Appenzell Ausserrhoden	AR	4847
Appenzell Innerrhoden	AI	1595
St.Gallen	SG	46,129
Graubünden	GR	16,474
Aargau	AG	52,832
Thurgau	TG	23,722
Ticino	TI	25,780
Vaud	VD	69,060
Valais	VS	29,800
Neuchâtel	NE	15,849
Genève	GE	40,033
Jura	JU	6418

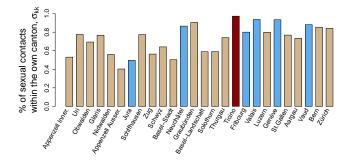


Fig. A.8. Proportion of intra-cantonal contacts (σ_{kk}) for the mobility-informed sexual mixing scenario. The weighted average across all cantons was set to 0.8. Cantons with a French-, German- or Italian-speaking majority are indicated in blue, beige and red, respectively. Cantons are ranked by increasing population size.

Table A.4. HPV vaccination uptake in 16 year old girls in Switzerland. Data from the last completed survey period (2011-2013) if the Swiss National Vaccination Coverage Survey (SNVCS). Data from Geneva and Appenzell Inner. are from 2010 and 2014, respectively.

Canton	Acronym	% three dose	% two dose	% one dose
Zürich	ZH	44	3	2
Bern	BE	37	5	2
Luzern	LU	50	4	2
Uri	UR	40	5	1
Schwyz	SZ	27	3	1
Obwalden	OW	31	2	1
Nidwalden	NW	61	0	0
Glarus	GL	47	7	2
Zug	ZG	17	3	4
Fribourg	FR	71	1	1
Solothurn	SO	53	3	2
Basel-Stadt	BS	52	4	0
Basel-Landschaft	BL	64	1	1
Schaffhouse	SH	40	4	3
Appenzell Ausserrhoden	AR	24	3	2
Appenzell Innerrhoden	ΑI	34	3	3
St.Gallen	SG	59	5	0
Graubünden	GR	44	6	2
Aargau	AG	59	3	0
Thurgau	TG	35	6	2
Ticino	TI	38	7	0
Vaud	VD	66	1	2
Valais	VS	75	3	1
Neuchâtel	NE	59	3	3
Genève	GE	62	5	0
Jura	JU	63	0	1

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