

1 **Quartet Sampling distinguishes lack of support from conflicting support**

2 **in the plant tree of life¹**

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13 **Short Title: Quartet Sampling of discordance in the plant tree of life**

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14 **ABSTRACT**

15 **Premise of the Study**— Phylogenetic support has been difficult to evaluate within the plant
16 tree of life partly due to the inability of standard methods to distinguish conflicted versus poorly
17 informed branches. As phylogenomic and broad-scale datasets continue to grow, support
18 measures are needed that are more efficient and informative.

19 **Methods**— We describe the Quartet Sampling (QS) method that synthesizes several
20 phylogenetic and genomic analytical approaches into a quartet-based evaluation system. QS
21 rapidly characterizes discordance in large-sparse and genome-wide datasets, overcoming issues of
22 sparse alignment and distinguishing strong conflict from weak support. We test this method with
23 simulations and recent plant phylogenies inferred from variously sized datasets.

24 **Key Results**— QS scores decrease in variance with increasing replicates and are not strongly
25 affected by branch depth. Patterns of QS support from different phylogenies leads to a coherent
26 understanding of ancestral branches defining key disagreements, including *Ginkgo*+cycad,
27 magnoliids+eudicots (excluding monocots), and mosses+liverworts. The relationships of ANA
28 grade angiosperms, major monocot groups, and bryophytes and fern families are found to likely
29 be the result of discordant evolutionary histories, rather than poor information. Also, analyses of
30 phylogenomic data show QS can detect discordance due to introgression.

31 **Conclusions**— The QS method represents an efficient and effective synthesis of phylogenetic
32 tests that offer more comprehensive and specific information on branch support than conventional
33 measures. The QS method corroborates growing evidence that phylogenomic investigations that

34 incorporate discordance testing are warranted to reconstruct the complex evolutionary histories
35 surrounding in particular ANA grade angiosperms, monocots, and non-vascular plants.

36 **Key words:** bootstrap; branch support; discordance; introgression; lineage sorting;
37 phylogenetics; phylogenetic methods; phylogenomics; plant tree of life; quartet sampling

38 INTRODUCTION

39 Discordance and uncertainty have emerged as a consistent feature throughout the history of our
40 evolving model of the plant tree of life (Crane, 1985; Chase et al., 1993; Palmer et al., 2004;
41 Soltis et al., 2011; Wickett et al., 2014). Furthermore, key points of uncertainty and contention
42 occur at pivotal transitions in the evolution of plant life on earth, such as the development of
43 vascular tissue (Pryer et al., 2001; Steemans et al., 2009; Banks et al., 2011), the rise of
44 seed-bearing plants (Chase et al., 1993; Chaw et al., 1997; Bowe et al., 2000; Qiu et al., 2006;
45 Jiao et al., 2011), and the explosive radiation of flowering plants (Crane, 1985; The Amborella
46 Genome Project, 2013; Goremykin et al., 2015; Taylor et al., 2015; Simmons, 2016; Edwards
47 et al., 2016). Modern phylogenomic datasets, rather than quelling these disagreements, have now
48 repeatedly shown that these phylogenetic conflicts are not only caused by methodological error or
49 data bias, but also are often the result of genuine biological processes. These forces most
50 commonly include incomplete lineage sorting (ILS), introgressive hybridization, and paralog
51 duplication-loss (e.g., Zhong et al., 2013b; Wickett et al., 2014; Zwickl et al., 2014; Yang et al.,
52 2015; Eaton et al., 2016; Pease et al., 2016b; Goulet et al., 2017; Walker et al., In Press). While
53 several methods have been proposed to deal with these issues in the context of species tree
54 inference (e.g., Zwickl and Hillis, 2002; Ogden and Rosenberg, 2006; Shavit Grievink et al.,

55 2010; Aberer et al., 2012; Anderson et al., 2012; Roure et al., 2012; Hinchliff and Roalson, 2013;
56 Mirarab et al., 2014), we still lack a generalized framework to quantify phylogenetic uncertainty
57 (specifically branch support) that distinguishes poorly informed branches from the increasingly
58 common case of multiple strongly supported, but mutually exclusive, phylogenetic histories.
59 Therefore, the development of systems of phylogenetic evaluation designed to utilize and describe
60 discordance (rather than minimize or control for it as error) offers strong promise to provide a
61 more holistic picture of the current state of the plant tree of life.

62 Quantification of branch support for molecular phylogenies has been proposed under many
63 methods over the last few decades (Felsenstein, 1985; Farris et al., 1996; Larget and Simon, 1999;
64 Anisimova and Gascuel, 2006; Anisimova et al., 2011; Ronquist et al., 2012; Larget, 2013).
65 Historically, one of the most commonly used tests has been the non-parametric bootstrap (NBS;
66 Felsenstein, 1985), which, along with recent variants like the rapid bootstrap (RBS; Stamatakis
67 et al., 2008), resamples the original data with replacement assuming that aligned sites are
68 independent and identically distributed (i.i.d.) samples that approximate the true underlying
69 distribution (Efron, 1992; Felsenstein, 1985). In practice, the assumptions of NBS (in particular
70 site independence) may rarely be met and can deteriorate under a variety of conditions
71 (Felsenstein, 1985; Felsenstein and Kishino, 1993; Hillis and Bull, 1993; Sanderson, 1995;
72 Andrews, 2000; Alfaro, 2003; Cummings et al., 2003). More recently the UltraFast bootstrap
73 approximation (UFboot) method, utilizing a likelihood-based candidate tree testing, was proposed
74 to address speed and score interpretation issues for NBS (Minh et al. (2013); and see comparison
75 in Simmons and Norton (2014)).

76 The other most common branch support metric has been the Bayesian posterior probability
77 (PP). PP scores are typically calculated from posterior distributions of trees generated using a

78 Markov chain Monte Carlo (MCMC) sampler and then summarized using a majority-rule
79 consensus tree (e.g, Larget and Simon, 1999; Drummond and Rambaut, 2007; Ronquist et al.,
80 2012; Larget, 2013). The interpretation of PP values is arguably more straightforward than
81 bootstrap proportions, as PP values represent the simple probability that a clade exists in the
82 underlying tree (conditioned on the model of evolution employed, and assuming the data have
83 evolved in a treelike fashion), and do not involve data resampling. The individual and relative
84 performance of PP has been well-documented and generally favorable (Wilcox et al., 2002;
85 Alfaro, 2003; Cummings et al., 2003; Huelsenbeck and Rannala, 2004). However, it has been
86 recognized that in some scenarios (e.g., oversimplified substitution models) PP may give liberal
87 support (Suzuki et al., 2002; Douady et al., 2003; Nylander et al., 2004), and there are indications
88 that PP also may fail under a multi-species coalescent framework with conflicting phylogenies
89 (e.g., Reid et al., 2013). Some studies have noted the disproportionate effects of a few genes in
90 tipping the scales in the case of low information in large datasets (Brown and Thomson, 2016;
91 Shen et al., 2017).

92 Modern phylogenetic datasets being assembled to model the plant tree of life are currently
93 trending in two directions. Ongoing efforts to expand genetic sampling to as many plant species
94 as possible have produced increasingly species-rich, but data-sparse, alignments (i.e., large-sparse
95 matrices). Meanwhile, the accelerating accretion of new genomes and transcriptomes will
96 continue to deepen genome-wide datasets with millions of aligned sites. Both types of data
97 present particular challenges to both the tractability and interpretation of phylogenetic branch
98 support methods. NBS scores are known to perform poorly for large-sparse matrices (Wiens and
99 Morrill, 2011; Smith et al., 2011; Roure et al., 2012; Hinchliff and Roalson, 2013; Hinchliff and
100 Smith, 2014b), where the sampling procedure generates uninformative pseudo-replicates that

101 mostly omit informative sites (or consist of mostly missing data). The problem of uninformative
102 pseudo-replicates also applies to alignment jackknifing used on sparse alignments, where
103 alignments are sampled without replacement. Therefore, alignment jackknifing also does not
104 offer a functional solution for large alignments with missing data.

105 Quantifying phylogenetic support from complete datasets brings unique challenges. By
106 “complete” dataset, we refer to any molecular data that is not a smaller subset of some larger
107 whole, which means not only whole genomes, but also whole transcriptomes, and even whole
108 plastid/mitochondrial genomes. PPs provide an appropriate testing framework and
109 straightforward interpretation, but available Bayesian methods of analysis and computational
110 speeds do not scale to typical phylogenomic datasets. Resampling methods (including NBS)
111 gauge how well the resampled dataset replicate the initial result, but complete datasets are not
112 samples of any larger whole. PP and NBS scores therefore both appear unsuitable for use on large
113 datasets, the former due to feasibility and the latter due to its assumption (Smith et al., 2009;
114 Hinchliff and Smith, 2014b).

115 A relatively well-studied, but less frequently applied, family of tests are the likelihood ratio
116 tests, such as the approximate likelihood ratio test (aLRT), the Shimodaira–Hasegawa [SH]-like
117 aLRT (SH-aLRT), and the Bayesian-like LRT (bLRT) (Anisimova and Gascuel, 2006; Guindon
118 et al., 2010; Anisimova et al., 2011). These tests conduct an approximated LRT of the alternative
119 nearest-neighbor interchange (NNI) moves at each branch of an optimized tree topology.
120 SH-aLRT has been shown to perform well (Anisimova et al., 2011; Simmons and Norton, 2014;
121 Simmons and Randle, 2014) and is computationally efficient enough to be run on large datasets in
122 large part because it does not require generation of multiple topology replicates (as in NBS).
123 Despite multiple implementations in PhyML and RAxML, and being the default support measure

124 in FastTree, this test has rarely been used in published studies (Guindon et al., 2010; Price et al.,
125 2010; Stamatakis, 2014).

126 As phylogenomics has developed over the last decade, a variety of methods have been
127 introduced to factor the increased data and inherent gene tree-species tree conflict. These methods
128 measure the concordance of gene trees (broadly referring to a phylogeny from any sub-sampled
129 genomic region), including the internode and tree certainty scores (IC/TC; Rokas et al., 2003;
130 Salichos et al., 2014; Kobert et al., 2016), Bayesian concordance factors (Ané et al., 2006), and
131 other concordance measures (Allman et al., 2017). These various certainty scores are developed
132 around the central concept of a branch support statistic that measures concordance of various
133 trees with a particular tree hypothesis. This perspective on phylogenetic evaluation offers much in
134 terms of partitioning phylogenetic discordance and analyzing larger alignments more rapidly in a
135 phylogenomic coalescent-based framework, but these methods that address discordance using
136 gene trees may not be as suitable for large-sparse alignments.

137 Finally, quartet methods—in particular quartet puzzling methods—have been examined
138 extensively in phylogenetics, especially in relation to phylogenetic reconstruction (Strimmer
139 et al., 1997; Strimmer and von Haeseler, 1997; Ranwez and Gascuel, 2001; Chifman and
140 Kubatko, 2014; Mirarab et al., 2014). A quartet support method called “reliability values,” which
141 correlates with NBS values, is calculated as a side effect of the quartet puzzling procedure
142 (Strimmer et al., 1997; Strimmer and von Haeseler, 1997). More recently, quartet procedures have
143 been explored to facilitate sampling of large-sparse alignments (Misof et al., 2013) and as part of
144 coalescent-based quartet inference methods (Gaither and Kubatko, 2016; Sayyari and Mirarab,
145 2016). These quartet methods benefit not only from the speed advantages of a smaller alignment,
146 but also from the statistical consistency of quartet trees, which avoid complex lineage sorting

147 issues that occur with more speciose phylogenies (Rosenberg, 2002; Degnan and Salter, 2005).

148 Few measures of support (except concordance methods) explicitly operate with the
149 expectation of multiple histories, or fail to distinguish different causes of poor support for a
150 branch in the phylogeny. In practice, this means when a phylogenetic relationship shows poor
151 support under NBS or PP, the specific cause is not apparent since these tests do not distinguish
152 between the case of multiple supported-but-conflicting phylogenetic relationships and the case of
153 simply low information. Being able to distinguish among these causes of low phylogenetic
154 support and to identify branches that have a strong consensus and a strong secondary evolutionary
155 history would provide valuable insight into the plant tree of life (among others; and see also
156 Brown and Lemmon, 2007).

157 Here, we describe the Quartet Sampling (QS) method (Fig. 1 and Table 1), which blends
158 aspects from many of the evaluation methods described above and leverages the efficiency of
159 quartet-based evaluation. The goal of the QS method is to evaluate phylogenies (particularly
160 large-sparse and genome-wide) by dissecting phylogenetic discordance to distinguish among (1)
161 differences in phylogenetic branch support due to lack of information (the general goal of
162 bootstrap or Bayesian posteriors), (2) poor support due to discordance as a result of lineage
163 sorting or introgression (as in concordance measures), and (3) low support due to particular taxa
164 with poor or conflicted information (i.e., “rogue taxa”; Wilkinson, 1996; Aberer et al., 2012).
165 These various causes of discordance are frequently surveyed separately in many modern
166 phylogenetic and particularly phylogenomic studies (e.g., Xi et al., 2014a; Wickett et al., 2014;
167 Yang et al., 2015; Pease et al., 2016b; Walker et al., In Press), but the QS method provides a
168 unified method for their execution, interpretation, and reporting. Additionally, the QS method
169 offers a viable means to describe branch support in large phylogenies built from sparse

170 alignments (10,000–30,000 tips with >80% missing data), datasets for which Bayesian analyses
171 are simply not tractable. We also describe how QS enhances analysis of both genome-wide
172 datasets and smaller-scale multi-gene data sets conventionally used in systematics.

173 In this study, we will (1) describe the features, parameters, and interpretation of the QS
174 method, (2) validate the QS method with simulations that demonstrate its effectiveness, and (3)
175 evaluate and discuss the plant tree of life by testing the QS method on recently published
176 large-sparse and phylogenomic datasets at timescales spanning from Viridiplantae to sub-generic
177 clades. The goal of the re-analysis of these phylogenies is not to compare the methods of tree
178 inference or dataset composition, but instead to use the QS method to collectively analyze these
179 data as a diverse set of alternative phylogenetic hypotheses of the plant trees of life. We show
180 consistently through these datasets that the QS method acts as a more conservative test of branch
181 support that provides greater discrimination between highly supported and poorly supported
182 branches than other support measures. We also show that the QS method can identify branches in
183 a phylogeny where biological conflict is likely occurring, which can inform targeting of more
184 detailed investigations within a clade. Finally, we show several cases where low support for the
185 given phylogenetic relationship and strong counter-support for an alternative relationship together
186 indicate a coherent consensus. In other cases, QS specifically indicate the likely presence of
187 alternative phylogenetic histories, as distinct from low branch support. We hope this study
188 encourages additional discussion, testing, and innovation of new phylogenetic evaluation
189 methods. We also hope it contributes to the broader discussion about moving the plant tree of life
190 beyond the increasingly difficult goal of resolving a single unified ‘Species Tree’ (Hahn and
191 Nakhleh, 2015; Smith et al., 2015), and into a future where the complex “multiverse” of
192 phylogenetic relationships that is manifest throughout the plant tree of life are more fully

193 explored and appreciated.

194 **MATERIALS AND METHODS**

195 *Quartet Sampling*— The Quartet Sampling (QS) procedure outlined here was inspired by
196 aspects from several quartet-based and concordance methods, most particularly the process
197 originally outlined by Hinchliff and Smith (2014b). The QS method takes an existing
198 phylogenetic topology (which can be inferred by any method) and a molecular dataset (not
199 necessarily the one that generated the phylogeny) and separately evaluates one or more internal
200 branches on the given phylogeny. The QS method (Fig. 1) was designed to rapidly and
201 simultaneously assess the confidence, consistency, and informativeness of internal tree
202 relationships, concurrent with an analysis of the reliability of each terminal branch.

203 For a given phylogeny, each observed internal tree branch partitions the tree into four
204 non-overlapping subsets of taxa (Fig. 1A). These four sets of taxa can exist in three possible
205 relationships: the concordant relationship that matches the configuration in the given topology
206 and two alternative discordant configurations. The QS method repeatedly and randomly samples
207 one taxon from each of the four subsets and then evaluates the likelihood all three possible
208 phylogenies given the sequence data for the randomly selected quartet spanning that particular
209 branch.

210 For each quartet sampled for the focal branch, the likelihood is evaluated (using RAxML or
211 PAUP*; Stamatakis, 2014; Swofford and Sullivan, 2003) for all three possible topologies that
212 these four sampled taxa can take. The quartet topology with the best likelihood is then recorded
213 and tabulated across all replicates, generating a set of counts (across all replicates per branch) for

214 the concordant and each of the two discordant relationships. If a minimum alignment overlap is
215 specified, then quartets must contain the minimum number of overlapping non-empty sites for all
216 four taxa to be considered suitable for any calculations. Additionally, a parameter of a minimum
217 likelihood differential may be set. If the most-likely topology (of the three) does not exceed the
218 likelihood of the second-most-likely phylogeny by the set threshold then the quartet is considered
219 “uninformative” and tabulated separately. Therefore, for a given internal branch, the QS method
220 generates counts of the three possible topologies (and uninformative replicates) sampled from
221 different quartets of taxa spanning the particular branch.

222 The QS method uses these resampled quartet tree counts to calculate three scores for each
223 internal branch of the focal tree (Fig. 1B, Table 1, and Appendix S1; see Supplemental Data with
224 this article). The QC (Quartet Concordance) score is an entropy-like measure (similar to the ICA
225 score; Salichos et al. 2014) that quantifies the relative support among the three possible
226 resolutions of four taxa. When the most commonly sampled topology is concordant with the input
227 tree, then the QC takes positive values in the range (0,1]. Thus, QC=1 when all quartet trees are
228 concordant with the focal branch. When one of the discordant topologies is the most commonly
229 resampled quartet, QC takes negative values in the range [-1,0), approaching -1 when all quartet
230 trees are one of the two discordant phylogenies. When support is evenly split among the three
231 alternative topologies (or two if only two of the three possible are sampled), QC equals 0.

232 The QD (Quartet Differential) score uses the logic of the f - and D -statistics for introgression
233 (Reich et al., 2009; Green et al., 2010; Durand et al., 2011; Pease and Hahn, 2015) and measures
234 the disparity between the sampled proportions of the two discordant topologies (though with gene
235 tree proportions, rather than site frequencies). The QD score does not specifically quantify
236 introgression nor identify introgressing taxa, but does indicate that one alternative relationship is

237 sampled more often than the other. High values of QD report that there is one clearly preferred
238 topology among the two discordant topologies, a potential indication of a biased biological
239 process beyond background lineage sorting on the given branch, including introgression, strong
240 rate heterogeneity, heterogeneous base compositions, etc. QD varies in the range [0,1] with a
241 value of 0, meaning no skew in the proportions of discordant trees, and the extreme value of 1,
242 which means all discordant trees sampled are only from one of the two possible alternative
243 relationships.

244 The QU score (Quartet Uncertainty) quantifies the overall proportion of quartets for a given
245 branch where the tree with the best likelihood value has a likelihood that is not higher than the
246 next most likely tree by a given differential cutoff. This ensures that replicates are not counted as
247 being concordant or discordant when the molecular data itself is effectively equivocal on the
248 topology by all three options having nearly indistinguishable likelihood scores. QU is measured
249 in the range [0,1], which indicates the proportion of sampled quartets that did not exceed of the
250 cutoff. A QU of 0 means no “uncertain” quartets (i.e., highly informative data), while a value of 1
251 indicates 100% of quartets were uncertain (i.e., no information for the given branch). QU reports
252 the informativeness of the branch, which in conjunction with QD and QC distinguishes between
253 branches that have low information versus those with conflicting information (i.e., high
254 discordance).

255 Finally, for each terminal taxon, a QF (Quartet Fidelity) score is calculated to report what
256 proportion of the time inclusion of a given taxon in a quartet (across all branches) results in a
257 discordant quartet topology. QF is therefore similar in approach to a “rogue taxon” test
258 (Wilkinson, 1996; Aberer et al., 2012). For a given taxon, the QF score is measured in the range
259 [0,1] as the proportion of quartet topologies involving the taxon that are concordant with the focal

260 tree branch. Therefore, $QF=1$ indicates a given taxon always produces concordant topologies
261 when used in a quartet replicate. QF values approaching zero indicate mostly discordant
262 topologies involving this taxon, and may indicate poor sequence quality or identity, a
263 lineage-specific process that is distorting the phylogeny, or that the taxon is significantly
264 misplaced in the given tree. Note that QF differs specifically from $QC/QD/QU$ by being a
265 taxon-specific test across internal branch tests rather than a branch-specific test.

266 Collectively, these four tests represent a means to distinguish the consistency of a branch
267 (QC), the presence of a secondary evolutionary history (QD), the amount of information
268 regarding a branch (QU), and the reliability of individual taxa in the tree (QF ; Fig. 1B and see
269 Table 1). Taken together these tests provide a means to disentangle these effects rather than have
270 them conflated under a summary score as in standard measures of phylogenetic support. For a full
271 technical description of the QS method, see Appendix S1.

272 ***Guidelines for implementation of QS***— We implemented the above procedure in Python in
273 a program `quartetsampling` that samples an alignment randomly to generate many
274 representative quartet topology replicates for each internal branch in a corresponding focal tree
275 (<https://github.com/fephyfofum/quartetsampling>). This procedure has a number of advantages
276 over NBS for larger datasets. First, alignment columns are not resampled (as in NBS and RBS),
277 which allows even very sparse alignments to be used. Second, the number of likelihood
278 calculations that are required is the number of internal branches in the tree multiplied by the
279 number of replicates per branch multiplied by three possible topologies. Since computation time
280 scales linearly with the number of taxa, individual replicates are fast, and the computations can be
281 readily parallelized across processors and furthermore discretized across systems (with results

282 combined later). This allows QS to be efficiently applied to large alignments beyond the practical
283 limits of NBS and PP. The most extensive computational time was for the Zanne et al. (2014b)
284 31,749 taxon dataset (see below), which we ran on the Wake Forest University DEAC
285 high-performance cluster using 8 nodes with 16 CPU each. This analysis completed 200
286 replicates for the full tree in 13 hours. Smaller genome-wide datasets finished 1000 gene-tree
287 replicates on quad-core desktops approximately 12 hours, and conventional multi-gene datasets
288 took only a few minutes to a few hours to run on a standard desktop.

289 Although the SH-aLRT was by far the fastest method we consider here, the QS was fast
290 enough for large scale analyses. QS can also be applied separately to only a few branches,
291 allowing for more thorough exploration of particular branches of interest. Furthermore, the QS
292 does not require the tree tested to be the maximum likelihood topology, a requirement for
293 SH-aLRT. For our simulated data, we found that performing 200 QS replicates per branch was
294 adequate to achieve low variance in QS score. As would be expected, more replicates per branch
295 should generally be used for larger trees to sample a greater fraction of the total possible quartets.

296 Furthermore, some branches, especially in large trees, may be entirely unsupported by the
297 alignment due to a lack of sampling overlap among appropriate taxa (i.e., no sites in the
298 alignment contain data from each of the four subsets of taxa; Fig. 1A). Therefore, no
299 phylogenetic information exists to inform the branch (i.e., are “indecisive” *sensu* Steel and
300 Sanderson, 2010), and the QS procedure identifies these branches rather than discarding them or
301 marking them as simply low support.

302 ***Guidelines for interpretation of QS support values***— An important consideration with any
303 measure used to ascertain confidence is the precise interpretation. In order to facilitate accurate

304 interpretation of the QS scores, we provide a concise visual description of the tests (Fig. 1) and a
305 table describing example scores and their interpretations (Table 1). Particularly notable as shown
306 in Table 1 and in the results, the QS method can not only “support” or “fail to support” a given
307 branch hypothesis, but also can offer “counter-support” for an alternative branch (as in the
308 IC/ICA scores; Salichos et al., 2014; Kobert et al., 2016). Therefore, even “inaccurate” branch
309 hypotheses can offer information in the form strength of the “counter-support” for an alternative
310 quartet topology (i.e., the degree of negativity of the QC score; for examples see Fig. 6).

311 The QS scores we have described calculate the sensitivity of the resolution of a particular
312 branch to different combinations of taxa sampled around that branch. Each QS replicate
313 calculates whether the four sampled taxa support the resolution of the branch found in the tree
314 over the alternative resolutions. This framework is similar to the interpretation made by those
315 using taxon jackknife analyses for outgroup sensitivity (e.g., Edwards et al., 2005) and the IC
316 score when used with incomplete trees (Kobert et al., 2016). We argue that this interpretation is
317 richer in information than the NBS, and in our simulations the QC score also appears to more
318 conservatively and accurately assign high support values to branches that are present in the true
319 tree (i.e., relatively low false positive rates, at least when the likelihood threshold is small, i.e., in
320 the range of ~ 2 used here; Appendix S2). QC scores are particularly helpful in terms of clarifying
321 strength of support for branches with concordant tree frequencies not close to 1 (Appendix S3).

322 ***Generation and evaluation of simulated phylogenies***— We first tested the method by
323 generating simulated phylogenies under the pure birth (birth = 1) model of evolution with 50,
324 100, and 500 tips using `pxbdsim` from the `phyx` toolkit (Brown et al., 2017). Using these trees,
325 we generated 1000 bp alignments (no indels) under the Jukes-Cantor model with INDELible v.

326 1.03 (Fletcher and Yang, 2009). Trees were scaled so that the average branch lengths were about
327 0.2, based on the observation that this generated reasonable trees with most branches recovered
328 correctly from ML analyses. Using the same procedure, we also simulated trees with 500 tips and
329 associated alignments with ten nucleotide partitions, each with 500 sites under the Jukes-Cantor
330 model. We simulated both the full alignment with partitions and a modified randomly resampled
331 sparse alignment to examine the behavior of QS in the presence of missing data (see Appendix S1
332 for details). These partitioned and sparse alignments had the same qualitative features as the full
333 alignment.

334 Unlike the NBS method, which generates a set of trees from which branch support is
335 estimated, the QS method requires only a single input topology for which branch support will be
336 measured. We calculated QC, QD, QU, and QF scores for the true underlying tree as well as the
337 ML tree generated by RAxML, but we focus on results for the ML tree. To examine how the
338 number of replicates impacts the QS precision, we conducted simulations varying the number of
339 replicates for randomly drawn branches in the simulated trees (Fig. 2A; Appendix S4). Based on
340 these simulations, we elected to use 200 replicates per branch, since the variation in the QC score
341 was generally low across all tree sizes when this many replicates were performed. We used
342 RAxML and PAUP* to estimate the ML for the three alternative topologies for each QS replicate
343 (using the $-f N$ option and the GTRGAMMA model in RAxML). We also calculated
344 branch-specific QC/QD/QU and taxon-specific QF scores using likelihood differential cutoffs of
345 $\Delta L = 0$ (no filtering) and $\Delta L = 2.0$, which requires stronger conflicting signal to interpret
346 branches in the input tree as unsupported.

347 **Testing of Empirical Datasets**— While the simulations show the general reliability of the
348 method, our primary goal was to use this test to holistically evaluate recent large-scale plant
349 phylogenies, and also to show the utility and versatility of this method in subgroup and even
350 sub-genera analyses. Using published phylogenies and public datasets, we evaluated five recent
351 large-scale phylogenies, including (1) an 103-transcriptome dataset spanning Viridiplantae from
352 Wickett et al. (2014, abbreviated hereafter as WI2014), (2) two large-sparse phylogenies spanning
353 land plants from Hinchliff and Smith (2014b, abbreviated HS2014) and Zanne et al. (2014b,
354 abbreviated ZN2014), and (3) phylogenies spanning Magnoliophyta (angiosperms) with hundreds
355 of genes from Xi et al. (2014a, abbreviated XI2014) and Cannon et al. (2015b, abbreviated
356 CN2015). Additionally, to demonstrate the utility of this method at medium and short time scales,
357 we evaluated two whole transcriptome datasets from the wild tomato clade *Solanum* sect.
358 *Lycopersicon* from Pease et al. (2016b, abbreviated PE2016) and carnivorous plants from the
359 order Caryophyllales from Walker et al. (In Press, abbreviated WA2017). Finally, we tested this
360 method on a more typical medium-sized multi-locus dataset from Polypodopsida (ferns) from
361 Pryer et al. (2016b, abbreviated PR2016), such as might appear in many phylogenetic studies of
362 large subgroups. Data for these studies were obtained from datadryad.org and iplant.org
363 (Hinchliff and Smith, 2014a; Matasci et al., 2014; Xi et al., 2014b; Zanne et al., 2014a; Cannon
364 et al., 2015a; Pease et al., 2016a; Pryer et al., 2016a; Walker et al., 2017).

365 In addition, we analyzed the datasets using 200 individual gene trees for XI2014 and
366 WA2017, and 1000 gene trees for PE2016 and WI2014. For these datasets, quartets are sampled
367 as usual, but only the individual gene sequence alignments are assessed. These phylogenies were
368 all evaluated using a minimum alignment overlap per quartet of 100 bp and a minimum likelihood
369 differential of 2 (i.e., the optimal tree's log-likelihood must exceed the second-most likely tree by

370 a value of at least 2). We also calculated the phylogenies with and without partitioning in
371 RAxML, but in all cases the partitioned datasets did not qualitatively differ from the results of the
372 unpartitioned datasets. These data are provided as supplementary data, but are not shown here.

373 We also either re-calculated other measures of branch support or used values from the
374 published studies for comparison to the QS method for each phylogeny, except HS2014 and
375 ZN2014 where the size and sparseness of the datasets prohibited the calculation of other measures
376 of support. For the datasets from CN2015, PR2016, WA2017, and XI2014 100 replicates each of
377 RAxML NBS and SH-test were performed. Additionally, PP scores for PR2016 were calculated
378 using MrBayes (Ronquist and Huelsenbeck, 2003; Ronquist et al., 2012), and IC scores for
379 calculated for Walker et al. (In Press). For PE2016 and WI2014, RAxML NBS, MP-EST, or IC
380 scores were taken from published values.

381 **RESULTS AND DISCUSSION**

382 *Analysis of simulated and empirical datasets shows that QS components are consistent,*
383 *convergent, and complementary*— In order to examine the consistency and reliability of the
384 Quartet Sampling method, we first tested QS on a set of simulated phylogenies. As expected, the
385 QC score was generally correlated in a sigmoid fashion with the frequency of concordant trees
386 (Appendix S5). In order to determine the appropriate number of testing replicates and
387 demonstrate convergence, we conducted an analysis of the variance of the QS score by running
388 the QS analysis 100 times on randomly selected branches with different numbers of per-branch
389 replicates for trees with 50, 100, and 500 taxa. This analysis showed that the QC scores converge
390 (with decreasing variance as expected) on a consistent mean value for each branch as the number

391 of replicates increased (Fig. 2A). Sampling 200 quartets per branch reduced the variance to less
392 than 0.003 in all cases. Similar patterns of convergence were also found for QD values, though
393 with high variance (Appendix S5). We also note that since QS is a branch-specific test (not a
394 tree-wide test), key branches of interest can be tested individually at much higher numbers of
395 replicates without the need to re-test the entire tree.

396 QC and QD both incorporate the frequencies of discordant quartets in different ways, but for
397 that same reason run the risk of redundancy. However, we observed in the Hinchliff and Smith
398 (2014b) dataset (abbreviated as HS2014) that QD can take on a range of values for QC (Appendix
399 S5). As QC goes to the limits of its range (-1,1), QD values tend to have more extreme values.
400 These extreme values for QD were either due to a lack of discordant trees that limits sampling
401 (when QC approaches 1) or a high amount of one discordant tree (when QC approaches -1). This
402 made QC and QD related, but not strictly correlated, measures. Overall, the mean QC for the
403 HS2014 (0.15; interquartile range (IQR) = [-0.13, 0.46]) and Zanne et al. (2014b) (abbreviated
404 ZN2014; 0.17; IQR = [-0.10, 0.63]) were low compared to the less speciose phylogenies (Fig.
405 2B; Appendix S5). Applying a minimum log-likelihood differential threshold to small trees
406 tended to push scores toward extremes, resulting in more 0s and 1s (Appendix S2). As expected,
407 given the sparsity of the matrices for ZN2014 and HS2014, the proportion of uninformative
408 quartets was high in both cases (mean QU of 0.65 and 0.85, respectively).

409 Notably, QS found that 33.4% and 29.8% of branches in HS2014 and ZN2014, respectively,
410 had QC values less than -0.05. This meant that about a third of the branches in these consensus
411 phylogenies reported not just “low support” for the given branch, went further to report
412 “counter-support” for one of the two alternative topological arrangements at that branch (see
413 Table 1). Many empirical cases have been documented where one anomalous lineage can distort

414 not only its own phylogenetic placement, but can exert a wide-ranging set of distortions on the
415 topology (e.g., Fig. 8A, among many others). Resampling methods that infer a complete set of
416 tips (like NBS) will produce replicates that may also be distorted and thus firmly support these
417 relationships rather than highlight this discordance. Therefore, as pointed out by many other
418 quartet methods (Mirarab et al., 2014; Sayyari and Mirarab, 2016), the use of quartets breaks
419 down the problem in more manageable units that cannot be distorted by these complex lineage
420 sorting effects.

421 ***QS indicates strong relationships within, but not among, major land plant lineages—*** While
422 simulations and general characterizations of the QS method are necessary to demonstrate its
423 effectiveness, the primary goal of this study was to use QS to reanalyze and compare several
424 recent speciose and phylogenomic datasets to address ongoing debates of phylogenetic
425 relationships in the plant tree of life. We used QS methods to evaluate two of the most speciose
426 phylogenies of land plants presently assembled by Hinchliff and Smith (2014b) and Zanne et al.
427 (2014b), and one of the most comprehensive phylogenies of Viridiplantae from Wickett et al.
428 (2014) (abbreviated as WI2014). HS2014 spanned 13,093 taxa with a total alignment of 148,143
429 sites (Fig. 3), but extremely sparse overall coverage (96.4% missing characters). The alignment
430 used for ZN2014 (Fig. 4) contained 31,749 taxa and an alignment length of 12,632 bp, but also
431 with sparse coverage (82.3% missing characters). However, the QS method accommodates large,
432 sparse matrices, by evaluating alignment overlap only for each replicate quartet without requiring
433 complete occupancy for any partition of the alignment. Finally, the WI2014 (Fig. 5) contains only
434 80 taxa, but, as the pilot study for the 1000 Plants Project (1KP), spans the deepest time scale of
435 these three (including Chlorophyta) and had a highly occupied alignment of 290,718 bp with only

436 10.7% missing data.

437 Most major plant groups showed strong support in HS2014 and ZN2014, including
438 angiosperms (QC=0.68 and 0.75, respectively), Anthocerotophyta (hornworts; QC=0.54,0.92),
439 Acrogymnospermae (gymnosperms; QC=0.37,0.32), and Polypodopsida (ferns; QC=0.23,0.46).
440 Marchantiophyta (liverworts), rosids, and asterids all showed low support in HC2014 (QC<0.2).
441 Monocots (both including and excluding *Acorus*) had poor support in both HS2014 and ZN2014
442 ($-0.05 < QC < 0.05$). In WI2014, all the major groups (i.e., labeled internal branches in Fig. 5)
443 showed high support. In contrast to the generally high support for these major established groups,
444 we frequently found low support on the “backbone” relationships among these groups, in a
445 manner consistent with most previous phylogenies of land plants.

446 The relationships among Marchantiophyta, Bryophyta (mosses), Anthocerotophyta,
447 lycophytes, and “euphyllophytes” (i.e., ferns and seed-bearing plants) has also been under
448 substantial ongoing debate (Shaw et al., 2011). HS2014 places mosses as sister to the remaining
449 land plants, followed successively by liverworts, hornworts, and lycophytes. However, HS2014
450 indicates QC=-0.04 for a branch defining liverworts + all other land plants the exclusion of
451 mosses (Figs. 3B, 6A), indicating that the most common quartet branch among the replicates was
452 not the branch shown in the tree. By contrast WI2014 shows strong support (QC=0.67) for the
453 branch leading to a moss+liverwort common ancestor (Fig. 5). While ZN2014 contains only
454 embryophytes, it shows weak support (QC=0.15) for the branch separating moss+liverwort from
455 the rest of land plants. WI2014 has hornworts (represented by two *Nothoceros*) as sister to a clade
456 of mosses and liverworts+tracheophytes (as in Renzaglia et al., 2000), with high support for all
457 relationships. However, note that WI2014 showed substantial counter-support against a common
458 mosses+liverworts+tracheophyte ancestor to the exclusion of hornworts. Coalescent analyses in

459 WI2014 also support this finding of a monophyletic Bryophyta+Marchantiophyta clade.
460 Therefore, while the topology of HS2014 was consistent with the order of many previous
461 phylogenies (Nickrent et al., 2000; Qiu et al., 2006; Chang and Graham, 2011), QS supported the
462 alternative configuration of mosses and liverworts as sister groups (as in WI2014 and ZN2014;
463 see also Zhong et al., 2013a).

464 In all three datasets, the monophyly of vascular plants was strongly maintained, despite the
465 inclusion of *Selaginella* that have unusual GC content (Banks et al., 2011). However, the branch
466 leading to *Selaginella* often was accompanied by a higher QD value, which could be a result of
467 the biased composition or indication of a secondary evolutionary history. The QF value for
468 *Selaginella* in all cases was moderate, indicating that overall it did not more often produce
469 discordant topologies compared to other lineages. We also observed substantial discordance and
470 counter-support for relationships tested among various bryophyte groups and key taxa in HS2014,
471 possibly indicative of substantially under-appreciated hybridization among mosses (Nylander
472 et al., 2004). The collective results indicated a (perhaps complicated) monophyly of liverworts
473 and mosses, inconsistent placement of hornworts, and strong support for tracheophytes.

474 ***QS analysis of ferns confirms close relationship to seed plants and shows QS is effective on***
475 ***smaller datasets***— Another notable similarity of both HS2014 and ZN2014 was the poor score
476 at the base of “euphyllophytes” that placed ferns in a clade with seed plants. QC scores on this
477 branch were near zero in HS2104 and ZN2014 (0.02 and -0.06, respectively) and relatively low
478 for the WI2014 tree (QC=0.33); QD values were also relatively large (0.44–1). Within ferns the
479 arrangement of major clades in ZN2014 (Fig. 4E) was mostly consistent with the recently
480 published phylogeny by The Pteridophyte Phylogeny Group (PPG I, 2016). Those clades whose

481 relationships were counter-supported (Marratiales, Salviniiales, Hymenophyllales) were
482 discordant with the PPG I consensus and other recent phylogenies (Pryer et al., 2004; Testo and
483 Sundue, 2016) demonstrating the utility of QS in highlighting suspect relationships. Some key
484 areas of known high uncertainty (e.g., *Saccoloma* and *Lindsaea*) were highlighted with low and
485 negative QC scores. Additionally, the debated position of *Equisetum* was also reflected by low
486 scores.

487 While QS was designed for large datasets, we also found that QS can perform well on smaller
488 multi-gene datasets conventionally used for systematics studies. Using the phylogeny and data
489 from Pryer et al. (2016b), we reanalyzed the 5778 bp alignment using QS, NBS, SH, and PP
490 scores (Fig. 7). The QS scores were more conservative, but confirmed the conclusions of Pryer
491 et al. (2016b) regarding the monophyly of maidenhair ferns (*Adiantum*) and its placement in a
492 clade with the Vittarioids. In terms of QC/QD/QU scores, ZN2014 also supported the monophyly
493 of *Adiantum* (0.11/0/0.83; 14 taxa), the Vittarioids (0.20/1/0.71; 8 taxa), and their common
494 ancestor (0.22/1/0.87). We also found that among different branches in PR2016 with fairly similar
495 NBS and PP values, QS offers a wide range of support values (including negative-QC
496 counter-support).

497 ***Gymnosperms are monophyletic under QS and support Ginkgo in a clade with cycads—***

498 Another question that has attracted substantial debate is the relationships among the major
499 gymnosperm lineages and angiosperms. Under QS evaluation, HS2014, ZN2014, XI2014, and
500 WI2014 all indicate strong support for monophyly of recognized gymnosperm lineages. However,
501 the relationships among cone-bearing lineages differ among these four phylogenies. ZN2014 and
502 WI2014 place *Ginkgo* in a clade with cycads (consistent with Qiu et al., 2006; Bowe et al., 2000;

503 Lee et al., 2011; Xi et al., 2013, ; Fig. 6B). While the HS2014 topology places cycads as sister to
504 the remaining gymnosperms (i.e., not monophyletic with *Ginkgo*), the QS evaluation
505 counter-supports this relationship. Therefore, even though HS2014/WI2014 and ZN2014 had
506 different topological arrangements of these taxa, the QS analyses of these datasets indicates a
507 consistent message of a *Ginkgo*+cycads clade separate from the rest of gymnosperms.

508 This pattern of disagreement in topology but consistent QS interpretation was observed again
509 in the placement of Gnetales relative to the conifer lineages (Fig. 6C). ZN2014 indicates Gnetales
510 in a clade with a monophyletic Pinales (consistent with Lee et al. 2011) whereas HS2014 and
511 WI2014 show a Gnetales+Pinaceae ancestor distinct from other conifers (i.e., the “Gnepine”
512 hypothesis; Bowe et al., 2000; Xi et al., 2013). However, again the HS2014 and WI2014 QS
513 scores offer counter-support against the “Gnepine” relationship (QC=-0.19 and -0.67,
514 respectively) and show that one alternative was strongly preferred (QD=0.5 and 0.1). Here again,
515 in evaluating different competing topologies the QS method can offer consistent interpretations
516 that in this case indicates the monophyly of Pinales, but perhaps also offer some (albeit weak)
517 evidence that warrants further examination of possible gene flow between Gnetales and Pinales.

518 Finally, among the non-Pinaceae conifers, we observed conflicting patterns of poor backbone
519 support for monophyletic clades. In both ZN2014 and HS2014, *Amentotaxus* and *Torreya* form a
520 clade with the rest of Taxaceae to the exclusion of *Cephalotaxus*. Relationships between these
521 three Taxaceae lineages are both strongly counter-supported by QS. The high values of QD
522 (0.56–0.8) offer indication of possible introgression among these lineages. Therefore, again QS
523 scores highlight a part of the phylogenetic tree that may be mis-modeled by these consensus
524 phylogenies.

525 *Quartet Sampling indicates biased conflict among the ANA grade angiosperms*— Few
526 issues in angiosperm evolution have garnered more recent debate than the relationship among the
527 so-called “ANA grade” angiosperms, which include *Amborella*, Nymphaeales, and
528 Austrobaileyales. Of the four datasets where this phylogenetic relationship was testable, only
529 WI2014 inferred the “*Amborella*-first” hypothesis (Figs. 5, 6D; Qiu et al., 1999; Stefanović et al.,
530 2004; Qiu et al., 2006; Moore et al., 2007; Soltis et al., 2011; The Amborella Genome Project,
531 2013). ZN2014 shows a “Nymphaeales-first” relationship (Fig. 4B), and HS2014 and XI2014
532 indicate “*Amborella*+Nymphaeales”-first (Fig. 3B; Appendix S6). Regardless of the resolution
533 inferred in the consensus phylogenies from each dataset, the branches surrounding the
534 ANA-grade were all counter-supported ($QC < 0$) and biased in their discordance ($QD > 0.8$; Fig.
535 6D). ZN2014 offers weak support for *Amborella*+Nymphaeales, while XI2014 counter-supports
536 this relationship. In HS2014, WI2014, and ZN2014, the scores on the branch that placed
537 Austrobaileyales as the closest relative group to the remainder of angiosperms were strongly
538 QC-counter-supported and QD-biased.

539 Two questions surround the relationships of the ANA grade angiosperms. First, what was the
540 relationship among these lineages? Second, are the longstanding disagreements in inference of
541 these relationships the result of genuine biological conflict (i.e., introgression, horizontal transfer,
542 etc.), limitations in the data, or a methodological artifact arising from the depth of this branch, the
543 monotypic status of *Amborella*, and/or the rapidity of the angiosperm radiation? On the first
544 question, QS lacks support for “Nymphaeales-first”. Whether there more support exists for
545 *Amborella*+Nymphaeales or “*Amborella*-first” (as found also by The Amborella Genome Project,
546 2013) is unclear. The results we present suggest that both relationships have support in the data,
547 depending on changes in the dataset composition (as also found by Wickett et al. 2014).

548 On the second question, however, the strong QD values indicate a biased conflict that suggests
549 a secondary evolutionary history conflicting with the primary tree in a way that has so far evaded
550 comprehensive characterization. Demonstrations that bryophyte mitochondrial sequences are
551 present in *Amborella* (Rice et al., 2013; Taylor et al., 2015) indicate that these lineages have
552 experienced ancient introgressive events that might create competing evolutionary narratives in
553 the manner indicated by the QS results shown here (and see also Shen et al., 2017). Given the
554 intensity of effort to address these relationships without a broad community consensus and the
555 specific evidence of long-range introgression in *Amborella*, a greater understanding of
556 ANA-grade evolution likely lies in an examination of complex evolutionary histories rather than
557 in a continuation of the debate over appropriate sampling or models.

558 ***QS supports a magnoliid+eudicot ancestor and raises questions about the placement of the***
559 ***Chloranthaceae and Ceratophyllaceae***— The timings and order of the relationships among the
560 three “core angiosperm” lineages (eudicots, monocots, and magnoliids) represent the evolution of
561 three clades that have transformed the biosphere. ZN2014, WI2014, and XI2014 all indicate the
562 existence of a magnoliid+eudicot clade (Figs. 4B, 5 Fig. 6E, Appendix S6; also in Qiu et al.,
563 2006; Burleigh et al., 2009; Lee et al., 2011). An alternative monocot+eudicot clade appears in
564 HS2014 (Fig. 3B), which has been suggested by many other past phylogenies (Jansen et al., 2007;
565 Moore et al., 2007; Qiu et al., 2010; Soltis et al., 2011). However, in HS2014 the QS scores
566 counter-support both eudicot+monocots and magnoliids/monocot+eudicot clades. Here again,
567 despite disagreement among the topologies of the three large-scale phylogenies, the supporting
568 and counter-supporting QS scores indicate a common evolutionary history.

569 In addition to the three major core angiosperm groups, the Chloranthaceae have frequently

570 been placed in a clade with magnoliids (as in Jansen et al. 2007; Moore et al. 2007; Soltis et al.
571 2011; Group et al. 2016, and Fig. 3 in Wickett et al. 2014). However, both HS2014 and ZN2014
572 place Chloranthaceae in a clade with magnoliids, monocot, and eudicots, while WI2014 places it
573 in a clade with just eudicots (excluding monocots and magnoliids) that is, however,
574 counter-supported by the sampled quartets (QC=-0.54, QD=0.95).

575 *Ceratophyllum*, often placed as the most closely related group to eudicots (Jansen et al., 2007;
576 Soltis et al., 2011), in HS2014 appears in a clade with the Chloranthaceae among the prior to
577 monocot/magnoliid/eudicot splits. However, the branch placing Chloranthaceae+*Ceratophyllum*
578 lineage in a clade with magnoliids+monocots+eudicots was counter-supported (Fig. 3B) with a
579 strongly biased QD (0.81). ZN2014 supports *Ceratophyllum* as separate from the core
580 angiosperms. Given that this question is inextricably linked with the relationships of the three
581 core angiosperm groups, a consensus was not reached by this information alone. However, this
582 evidence reopens the question of the relationship of Chloranthaceae and Ceratophyllaceae, both to
583 each other and to the ANA grade angiosperm lineages (see discussion in Eklund et al., 2004).

584 ***Relatively consistent topology but poor support found within monocots***— Within monocots,
585 *Acorus* was weakly but consistently supported as a separate clade from the rest of monocots in
586 HS2014, ZN2014, and WI2014 (Figs. 3B, 4B, 5). In general, the arrangement of monocot orders
587 in both HS2014 (Fig. 3C) and ZN2014 (Fig. 4C) agreed with recent consensus phylogenies
588 (Givnish et al., 2010; Soltis et al., 2011; Barrett et al., 2015; Givnish et al., 2016; McKain et al.,
589 2016).

590 One exception was the placement of Liliales, which has varied in consensus trees and, here,
591 either was sister to commelinids with weak support (HS2014) or was sister to Asparagales

592 (ZN2014). The commelinid orders were resolved inconsistently between studies. The
593 commelinid stem branch was counter-supported in both ZN2014 and HS2014 with high QD
594 values. In HS2014, Arecales were separate from the rest of the commelinids, but the ancestral
595 commelinid branches both including and excluding Arecales were counter supported. In ZN2014,
596 Arecales was supported in a clade with Zingiberales and Commelinales, but the ancestral branch
597 for these three orders has a QD=0.79. This arrangement was consistent with previous phylogenies
598 (e.g., Givnish et al. (2010)) that have poor support to these relationships. From the QS results, we
599 would cautiously infer that (1) the relationships among the commelinids are still unknown, (2)
600 there may be uncharacterized secondary evolutionary history distorting the phylogenetic
601 placement of these groups, and (3) likely the variable data from both Liliales and Arecales
602 together have a joint effect that is causing inconsistency in the phylogenetic inference.

603 Finally, in Poaceae, Quartet Sampling made clear the well-characterized discordance and
604 complex relationships (e.g., Washburn et al., 2015; McKain et al., 2016). The “BOP” clade
605 (Bambusoideae, Oryzae, Pooideae) was counter-supported in HS2014 and both paraphyletic and
606 counter-supported in ZN2014. Within the “PACMAD” clade, many of the named subgroupings
607 were counter-supported with negative QC values. There were particularly high QU values in both
608 HS2014 and ZN2014 for this clade indicating not only complex support but also low information.
609 Therefore, even if someone were unfamiliar with the controversies surrounding monocot
610 phylogenetics (as a whole and within groups), the QS evaluation framework clearly highlights
611 this group as one with consistently high conflict and counter-support values for the consensus
612 phylogenies in HS2014 and ZN2014.

613 *Non-rosid/asterid eudicot lineages show substantial disagreement and rogue taxa*— Within
614 eudicots, Ranunculales were supported as a separate clade from the rest of eudicots by WI2014,
615 HS2014, XI2014, and CN2015, or among the non-rosid/asterid eudicots in ZN2014 (Figs. 3B,
616 4B, 5; Appendix S6, Appendix S7). Notably in both ZN2015 and HS2014, *Nelumbo* (sacred
617 lotus) was placed sister to a highly supported Proteales clade, but support for the
618 Proteales+*Nelumbo* clade was strongly counter-supported by the QC and QD scores. This again
619 demonstrates a situation where QS effectively highlights this lineage’s conflicted relationship
620 with the Proteales in a way that raises questions about a possible genuine biological (rather than
621 artifactual) cause of phylogenetic discordance.

622 *Vitis vinifera* (common grape vine) has also had variable inferred positions throughout
623 eudicots. WI2014, XI2014, and CN2015 all place *Vitis* as a “superrosid” and most closely related
624 clade to the rosids, but with widely ranging support and skew (QC=−0.13 to 0.63, QD=0.56 to
625 1.0) consistent with the conflict noted by Cannon et al. (2015b) (abbreviated CN2015; Appendix
626 S7). HS2014 (which sampled 64 Vitales) supported a Dilleniales+Gunnerales+Vitales clade,
627 while ZN2014 places Vitales+*Tetrastigma* among the rosids in a Vitales+malvid clade to the
628 exclusion of fabids. In the case of the grape vine, the high support in WI2014 (analyzed by gene
629 trees) accompanied by a high QD value (1.0) gives strong indication that while Vitales may
630 belong among the superrosids, an investigation of a secondary evolution history for grapes might
631 be warranted.

632 For the relationships among the superasterid groups (Caryophyllales, Berberidopsidales,
633 Santalales, and asterids), a common pattern was found in HS2014, ZN2015, WI2014, and XI2014
634 of near-zero QC values (−0.03 to 0.08), modest QD values (0–0.03), and high QU values
635 (0.49–0.86). This led to a consensus QS interpretation of low phylogenetic information, likely as a

636 result of the rapid radiation of these lineages. Generally, these phylogenies tended to support
637 weakly the controversial placement of Caryophyllales as most closely related to the eudicot
638 ancestor.

639 ***QS shows strong support for the consensus rosid phylogeny, but substantial discordance***
640 ***both within and among asterid clades***— HS2014 (Fig. 3D) find similar resolutions among rosid
641 lineages (Wang et al., 2009; Moore et al., 2010; Soltis et al., 2011; Zhao et al., 2016) (the lone
642 exception was the Sapindales+Huertales clade). Among the branches leading to major groups, all
643 were supported and most of the backbone branches were either supported or only weakly
644 negative. The QS scores also correctly identified a poorly supported relationship in HS2014
645 between *Cynomorium* and Cucurbitales (QC=-0.31). *Cynomorium*, a non-photosynthetic
646 parasitic plant with unusual morphology, has been placed tenuously and variably in groups as
647 diverse as Rosales (Zhang et al., 2009) and Saxifragales (Nickrent et al., 2005), so its poor score
648 here was expected and confirms the QS method's ability to detect poorly placed species. This
649 “rogue” status was corroborated by the below-average QF score of QF=0.18 (mean 0.21 for
650 HS2014). This means that for quartets that include *Cynomorium* as a randomly sampled taxon,
651 only 18% produced a quartet topology concordant with the HS2014 tree.

652 In contrast to the analysis of the rosid phylogeny from HS2014, the asterid phylogeny from
653 ZN2014 (Fig. 4D) appears to have substantial discordance and disagreement with most published
654 phylogenies (Soltis et al., 2011; Beaulieu et al., 2013; Refulio-Rodriguez and Olmstead, 2014).
655 ZN2014 QS scores supported the unusual hypothesis of a common Ericales+Cornales ancestor,
656 weakly support the campanulid clade, and counter-support a common lamiid ancestor. The
657 arrangement of families within Asterales either roughly conforms to Soltis et al. (2011) and

658 Beaulieu et al. (2013), or counter-supported branches ($QC < 0$) that do not agree with these
659 consensus phylogenies. However, most of the branches that define the relationships among asterid
660 orders in ZN2014 were counter-supported by the data, though most have QC and QD values close
661 to zero. This indicates a scenario of a rapid radiation rather than hybridization (though these are
662 not mutually exclusive). The lamiid groups show strong support for the monophyly of the
663 *Lamianae* core orders, though in an order different from Stull et al. (2015). Among the asterids
664 there were also several notably low QF scores for singular genera like *Oncotheca*, *Vahlia*, and
665 *Pentaphragma* (all $QF < 0.16$). Thus, the QS method in asterids does not necessarily add clarity to
666 this group, but perhaps more concretely puts into focus the combinations of discordance and low
667 information occurring in this group.

668 ***QS of shallow-timescale phylotranscriptomic datasets***— So far, we have demonstrated the
669 utility of quartet sampling on large, sparse alignments which are often computationally intractable
670 with other support measures. We have also shown, in the case of WI2014, that a relatively large
671 and full occupied matrix from deep-timescale transcriptomic data can also be evaluated by QS.
672 However, the QS method can be used to rapidly evaluate phylogenetic support on genome-wide
673 datasets with little missing data for shorter evolutionary timescales. We tested the QS method on
674 two phylotranscriptomic datasets for the wild and domesticated tomato clade *Solanum* sect.
675 *Lycopersicon* (Fig. 8A; Pease et al., 2016b) and carnivorous plants spanning the Caryophyllales
676 (Fig. 8B; Walker et al., In Press).

677 The *Solanum* phylogeny from Pease et al. (2016b) was inferred from coding sequence
678 alignment of 33,105,168 nucleotide sites for 30 populations spanning all 13 wild and
679 domesticated tomato species, and two outgroup species. As described in Pease et al. 2016b, this

680 dataset contains a high level of phylogenetic discordance, but had a consensus phylogeny with
681 100% NBS support at all but two branches (occurring within a large species complex). However,
682 gene tree analysis of this group clearly showed evidence of massive phylogenetic discordance.
683 When we applied QS to this phylogeny using the entire alignment, scores for many branches were
684 also perfect (i.e., 1/0/0; Table 1). However, several of the other branches in the “Peruvianum
685 group” species complex had lower QS scores in the full alignment (Fig. 8A). When gene trees
686 were used (both a quartet of taxa and a gene alignment were randomly chosen for 1000 QS
687 replicates), all branches had $QC < 1$ in a manner consistent with the gene tree discordance found
688 previously in this clade. We also observed the presence of high QD values within the major
689 subgroups reported for this clade, while nodes defining these groups showed high QC and low
690 QD values. This accurately captures the results found by Pease et al. (2016b) in terms of the low
691 discordance between groups versus high discordance within the major groups.

692 Most notably, the tree shown in Fig. 8A includes *S. huaylasense* accession LA1360. This
693 accession has been known (both from this and other datasets) to mostly likely be a hybrid
694 between populations from the green-fruited and red-fruited lineages (essentially those accessions
695 above and below LA1360, respectively, in Fig. 8A). Thus, the inclusion of this putative hybrid
696 lineage distorted the phylogeny as tree inference methods tried to cope with inherited and
697 introgressed alleles from two separate groups to place this accession in a consensus location on
698 the tree. While NBS scores were high for the branches surrounding the placement of LA1360, QS
699 showed negative QC scores and high QD scores ($QD=1$ for full alignment). This supports the
700 presence of the alternative phylogenetic history that has been previously corroborated by other
701 studies (see additional discussion in the Supplementary Results of Pease et al. 2016b). These data
702 show clearly that QS was able to distinguish between consistently supported relationships and

703 branches known to have conflict due to introgression (whereas NBS does not).

704 An analysis of transcriptomes of carnivorous plants from Caryophyllales (Fig. 8B; Walker
705 et al. In Press) showed QC scores consistent with IC scores. The QS scores for the ancestor of
706 “core Caryophyllales” were near zero and the high QD value when gene trees were used
707 (QD=0.68) supported the hypothesis of Walker et al. (In Press) that introgressive gene flow may
708 have occurred among these lineages. The evidence for placing *Drosophyllum* among the
709 carnivorous Caryophyllales has always been tenuous. The QS analysis here showed not only a
710 low QF value (QF=0.76, average for WA2017 was 0.89) for this taxon, but also low-QC/high-QD
711 values for the two branches that form the clade with *Ancistrocladus* and *Nepenthes*. As with the
712 tomato example above, this example demonstrates how QS scores can highlight an entire region
713 that may be distorted by the inclusion of a taxon with a strong potential for a secondary
714 evolutionary history (i.e., possible introgression).

715 **CONCLUSION**

716 In this study, our goal was to reanalyze several key and long-contested conflicts in the plant tree
717 of life by embracing the apparently complex relationships in the plant tree of life. The Quartet
718 Sampling method that we have described and demonstrated here synthesizes a blend of
719 phylogenetic and phylogenomic methods to provide a coherent framework for distinguishing
720 several causes of low phylogenetic branch support. QS also provides a tractable means to analyze
721 sparse datasets with tens of thousands of taxa but poor sequence overlap. Bootstrap and posterior
722 probability values have been shown to exhibit irregular behavior or to report uniformly high
723 confidence scores for large-scale datasets, despite substantial underlying conflict. Even when

724 conventional support measures do report low support, the specific cause of the low support is not
725 indicated, leaving it open to broad interpretation and speculation. Despite the decades of
726 documented concerns about the limitations of these support measures, bootstrap proportions
727 remain the dominant support measure in systematics. Our results, as well as those reported in
728 many other studies cited here, demonstrate the need for continuing discussion about the nature of
729 phylogenetic disagreement itself and how best to quantify this complexity. While much testing
730 and refinement of the QS method is undoubtedly left to be done, we find it provides a key
731 function that has been missing from other support measures, namely the ability to distinguish
732 among different causes of low support that commonly occur in modern molecular phylogenies.

733 The application of the QS method to the plant tree of life has also yielded some intriguing
734 results. The comparison of several recent consensus phylogenies showed that they differ at
735 several key, disputed relationships. However, when QS scores were compared, only one topology
736 was supported with the alternatives showing weak support, conflicted support, or even
737 counter-support (e.g., *Ginkgo* placed in a clade with cycads, Gnetales in a clade with a common
738 conifer ancestor, monocots separate from a magnoliid+eudicot clade, and Caryophyllales sister to
739 asterids). QS scores for some other relationships indicated the existence of multiple conflicting
740 but supported evolutionary histories (e.g., the placement of *Amborella*, possible widespread gene
741 flow in the monocots, and notoriously difficult-to-place genera like *Haplomitrium*, *Nelumbo*, and
742 *Cynomorium*). The artist Man Ray once remarked that “We have never attained the infinite variety
743 and contradictions that exist in nature.” Overall, the picture painted by QS is one of substantial
744 contradiction, but this conflict can be a richly informative (not just confounding) illustration of
745 the interwoven evolutionary histories contained within the plant tree of life.

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Table 1: Quartet Sampling (QS) score interpretation. See text for details.

Example QS Score (QC/QD/QU)*	Interpretation
1.0/-/0.0	Full support: All sampled quartet replicates support the focal branch (QC=1) with no uncertainty when likelihood cutoffs are used (QU=0).
0.5/0.02/0.03	Strong support: A strong majority of quartets support the focal branch (QC=0.5) and the low skew in discordant frequencies (QD≈0) indicate no alternative history is favored.
0.7/0.9/0.03	Strong support with discordant skew: A strong majority of quartets support the focal branch (QC=0.7), but the skew in discordance (QD=0.9) indicates the possible presence of a supported secondary evolutionary history.
0.05/0.04/0.03	Weak support: Only a weak majority of quartets support the focal branch (QC=0.05), and the frequency of all three possible topologies are similar (QD≈0).
0.1/0.9/0.03	Weak support with discordant skew: Only a weak majority of quartets support the focal branch (QC=0.1), and the skew in discordance (QD=0.9) indicates the possible presence of a supported secondary evolutionary history.
-0.5/0.9/0.07	Counter-support: A strong majority of quartets support one of the alternative discordant quartet arrangements history (QC<0; QD expected to be high).
1/0.03/0.95	Poorly informed: Despite supportive QC/QD values, 95% of quartets failed the likelihood cutoff (QU=0.95), likely indicating few informative sites.
0.0/0.0/0.0	Perfectly conflicted: The (unlikely) case where the frequency of all three possible trees was equal with no uncertainty, indicating a rapid radiation or highly complex conflict.

1102 Notes: * QC = Quartet Concordance; QD = Quartet Differential; QU = Quartet Uncertainty.

1103 FIGURE LEGENDS

1104 **Fig. 1.** Description of the Quartet Sampling method. (A) The focal branch “*b*” divides the phylogeny into four
1105 subclades $\{S_1, S_2, S_3, S_4\}$ from which tips (A–J) are sampled. Two replicates with different sampled tips for the
1106 given branch are shown with the three possible unrooted topologies (one concordant and two discordant). (B) Each
1107 internal branch is labeled with a set of three scores (QC/QD/QU), which offer different, but complementary,
1108 information. Terminal branches are evaluated by the QF score, which reports the frequency of a taxon generating
1109 concordant topologies. (See Materials and Methods for full details and Supplementary Methods for a technical
1110 description.)

1111
1112 **Fig. 2.** Results of Simulation Testing of the Quartet Sampling Method. (A) QC values converge on a central value
1113 with increasing numbers of replicates from randomly selected branches from simulated trees with 50, 100, and 500
1114 taxa. (B) Distributions of QC, QU, and QF values for HS2014 (black), ZN2014 (dotted black), and
1115 XI2014/CN2015/PR2016/WA2017 (similar distributions; gray solid). (C) Mean QC values (diamond) with 5%ile to
1116 95%ile (whiskers) for branches in HS2015 binned by the number of subtending taxa (i.e., moving root-ward in the
1117 tree left-to-right). Overall mean is shown with horizontal dotted line.

1118
1119 **Fig. 3.** Phylogeny from Hinchliff and Smith (2014b). (A) Full phylogeny with heat map coloration of branches by
1120 QC scores for internal branches: dark green ($QC > 0.2$), light green ($0.2 \leq QC < 0$), light orange ($0 \leq QC \leq -0.05$), or
1121 dark orange ($QC < -0.05$). (B) QC/QD/QU scores (200 replicates of full alignment) for major plant groups and key
1122 orders within angiosperms. QC/QD/QU scores after group names are for the ancestral branch (i.e., the “stem”
1123 branch), and a single QF score is shown for monotypic tips. Major subgroups groups are highlighted with vertical
1124 labels. (C) QS scores for monocots (excluding *Acorus*). (D,E,F) QS scores for rosids, Bryophyta, and gymnosperms.
1125 Abbreviations: Acro, Acrogymnospermae; ANA, ANA grade; Aru, Arundinoideae; Bry, Bryophyta, Chl,
1126 Chloridoideae; Dan, Danthonioideae; Mar, Marchantiophyta; Poly, Polypodopsida.

1127

1128 **Fig. 4.** Phylogeny from Zanne et al. (2014b). (A) Full phylogeny with heat map coloration of branches by QC scores

1129 for internal branches using same color scheme as (Fig. 3). (B) QC/QD/QU scores (200 replicates of full alignment)
1130 for major plant groups and key orders within angiosperms, using same color scheme as (Fig. 3). (C) QS scores shown
1131 for monocots (except *Acorus*). (D) QS scores for asterids. (E) QS scores for fern lineages and (F) QS scores for
1132 gymnosperm lineages respectively. Abbreviations: Alseu, Alseuosmiaceae; ANA, ANA grade angiosperms; Argo,
1133 Argophyllaceae; Aster, Asteraceae; Bory, Boryaceae; Caly, Calycanthaceae; Eriach, Eriachneae; Good,
1134 Goodeniaceae; gym, gymnosperms; Hypox, Hypoxidaceae; Isach, Isachneae; Phell, Phellinaceae; Poly,
1135 Polypodopsida.

1136

1137 **Fig. 5.** Maximum likelihood phylogeny spanning Viridiplantae from Fig. 2 in Wickett et al. (2014) with QC/QD/QU
1138 scores for 200 replicates of the full alignment. Nodes are colored according to QC score using same color scheme as
1139 (Fig. 3). Bootstrap values (italicized in square brackets) from Wickett et al. (2014) are shown for comparison.
1140 Missing QS or bootstrap values indicate a perfect score. The three taxa with the lowest QF values are highlighted.
1141 Species names have been excluded or abbreviated in the case where two congeners are included.

1142

1143 **Fig. 6.** Key phylogenetic disagreements with QC scores using compared across various datasets. Branches for
1144 HS2014 and ZN2014 were resampled with 10000 replicates. Branches for WI2014 and XI2014 were exhaustively
1145 sampled (>1000 replicates). Highlighting on QC values follows the same colors as Fig. 3. “Conifers-II” refers to a
1146 hypothesized clade comprising the non-Pinales orders in Pinidae. Abbreviations: Gnet, Gnetidae; Pin, Pinidae.

1147

1148 **Fig. 7.** Phylogeny of Pteridaceae ferns from Pryer et al. (2016b) with QC/QD/QU scores for 200 replicates of the full
1149 alignment. Nodes are colored according to QC score using same color scheme as (Fig. 3).

1150 Bootstrap/SH-test/posterior probability values (italicized in square brackets) are shown for comparison. Omitted
1151 values indicate a perfect score. The three taxa with the lowest QF values are highlighted. Abbreviations: *Pityro*,

1152 *Pityrogramma*.

1153

1154 **Fig. 8.** QS scores for phylogenies from whole-transcriptome data. Omitted values indicate a perfect score. Nodes are
1155 colored according to QC score using same color scheme as (Fig. 3). (A) Phylogeny of *Solanum* sect. *Lycopersicon*

1156 from Pease et al. (2016b) Bootstrap values (italicized in square brackets) are shown for comparison. (B) Phylogeny
1157 of Caryophyllales from Walker et al. (In Press) IC scores (light grey) are shown for comparison (all bootstrap and
1158 SH-test scores were 100). The three taxa with the lowest QF values are highlighted.

1159 APPENDICES

1160 **Appendix S1.** Supplementary Methods providing a technical description of the QS method

1161

1162 **Appendix S2.** Comparison of QC and bootstrap ICA (information criterion-all; Salichos, et al. 2014) scores on trees

1163 reconstructed from 100 simulated datasets with 50 taxa with 1,000 base pairs under a Jukes-Cantor model of

1164 evolution. Blue circles represent branches in the true tree, with the size of the circle proportional to the log of the

1165 number of substitutions. Red triangles represent branches not in the true tree.

1166

1167 **Appendix S3.** Comparison of the rapid bootstrap and quartet sampling on the ML/PP consensus tree. For each

1168 branch, the RBS, QS (raw concordant frequency (Freq1), QC score), SH, and PP scores are presented (clockwise

1169 from top left in each legend). Black dots identify clades that are not in the true tree.

1170

1171 **Appendix S4.** Shows the consistency of the frequency of concordant quartets (f_1), QC, and QD toward a central

1172 value with increasing number of per-branch replicates for a randomly selected branch. Trees with 50 taxa (left), 100

1173 taxa (center), and 500 taxa (right) are shown. Boxes show median \pm IQR. Whiskers show 5th–95th percentile, with

1174 values outside this range shown as circle points.

1175

1176 **Appendix S5.** Histograms (top row) showing the distributions of QC (left), QU (middle), and QF (right) values for

1177 the HS2014 dataset (green), ZN2014 (black), and smaller dataset (XI2014, CN2015, PR2016, WA2017) with similar

1178 distributions (orange). Scatter plots (bottom row) showing the close (but non-linear) relationship between QC and

1179 raw concordant quartet frequency (f_1 ; left), bounded but otherwise uncorrelated relationships between QC and QD

1180 (middle), and QC and QU (right). See main text for dataset abbreviations.

1181

1182 **Appendix S6.** Phylogeny of angiosperms from Xi et al. (2014a) with QC/QD/QU scores for 200 replicates of the full

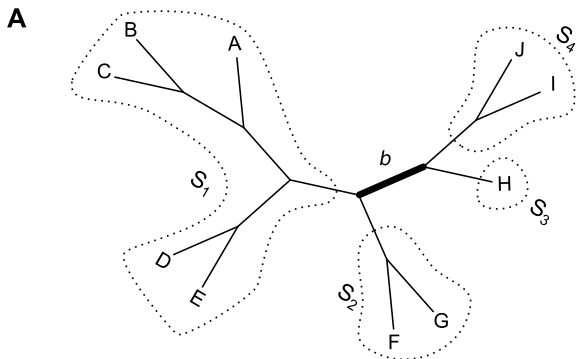
1183 alignment and for 200 replicates from individual gene trees (in parentheses). Nodes are colored according to QC

1184 score using same color scheme as (Fig. 3). MrBayes PP/RAxML NBS values (italicized in square brackets) from Xi

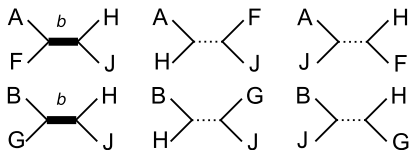
1185 et al. (2013). are shown for comparison. Perfect scores for any given test are omitted or shown as ‘*’ indicates
1186 bootstrap of 100, while ‘-’ indicates a missing value. The three taxa with the lowest QF values are highlighted.
1187

1188 **Appendix S7.** Phylogeny from Cannon et al. (2015b) with QC/QD/QU scores for 200 replicates of the full alignment.
1189 Nodes are colored according to QC score using same color scheme as (Fig. 3). Bootstrap values (italicized in square
1190 brackets) are shown for comparison. Perfect scores for any given test are omitted or shown as ‘*’ indicates bootstrap
1191 of 100, while “-” indicates a missing value. The three taxa with the lowest QF values are highlighted.
1192

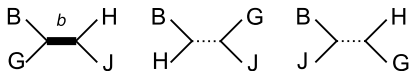
1193 **Appendix S8.** Relationship between QC and frequencies of the three possible alternative quartet topologies from QS
1194 runs on simulated data. Points represent branches in the trees, with the “test topology” axis identifying the frequency
1195 at which the topology consistent with the tree was recovered across all QS replicates for that branch, and the “alt n”
1196 axes identifying the frequencies of the two alternative (conflicting) topologies.



Replicate 1



Replicate 2



...

Concordant quartet topology Discordant topology #1 Discordant topology #2

B Quartet Sampling Internal Node Scores = **0.52** / **0.04** / **0.01**

Quartet Concordance (QC)

How often is the concordant quartet inferred over both discordant quartets?

QC=1 → all concordant
QC=0 → equivocal conc./disc.
QC<0 → disc. > concordant

Quartet Differential (QD)

Are discordant #1 and #2 frequencies equal or skewed?

QD=0 → all concordant
QD=0.3 → skewed
QD=1 → all #1 or #2

Quartet Uncertainty (QU)

What proportion of replicates were uninformative? (failed likelihood differential cutoff)

Examples:

QU=0 → no uninformative
QU=0.3 → 30% uninform.
QU=1 → none informative

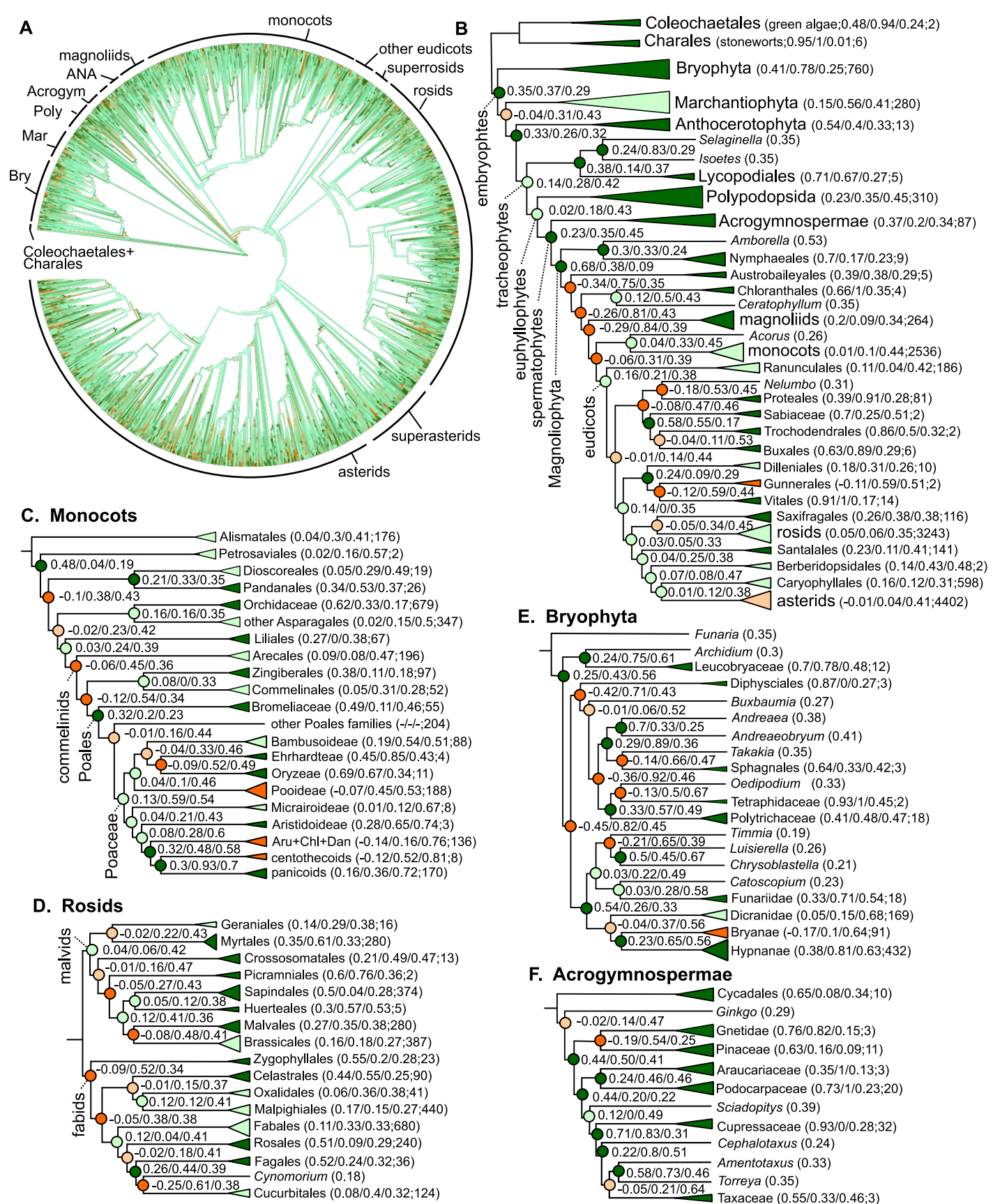
Quartet Sampling Terminal Node Scores = **(0.52)**

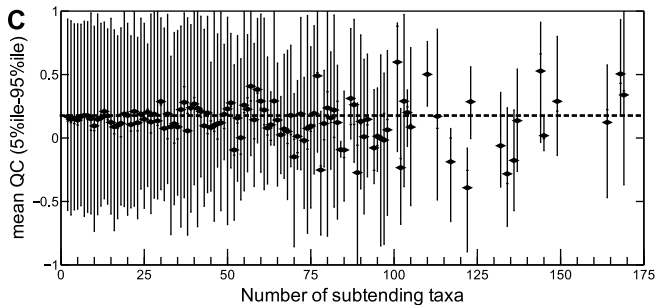
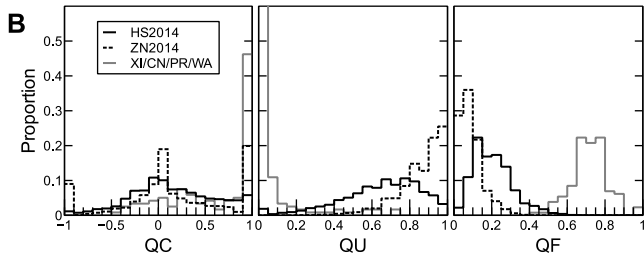
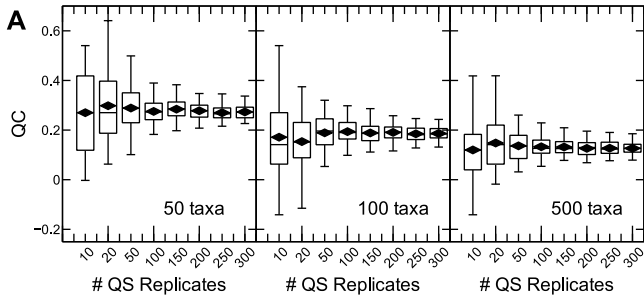
Quartet Fidelity (QF)

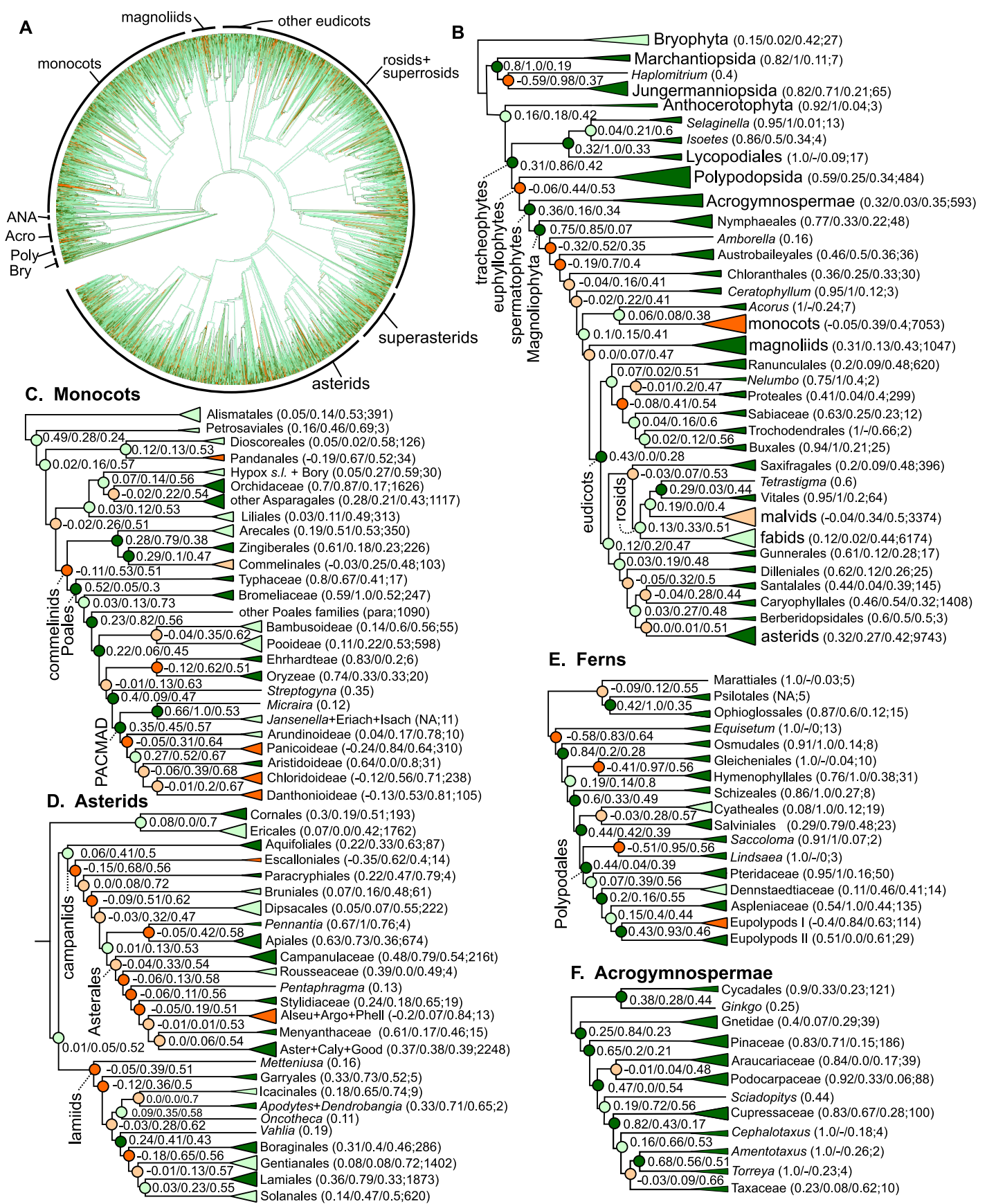
When this taxon is sampled, how often does it produce a concordant topology?

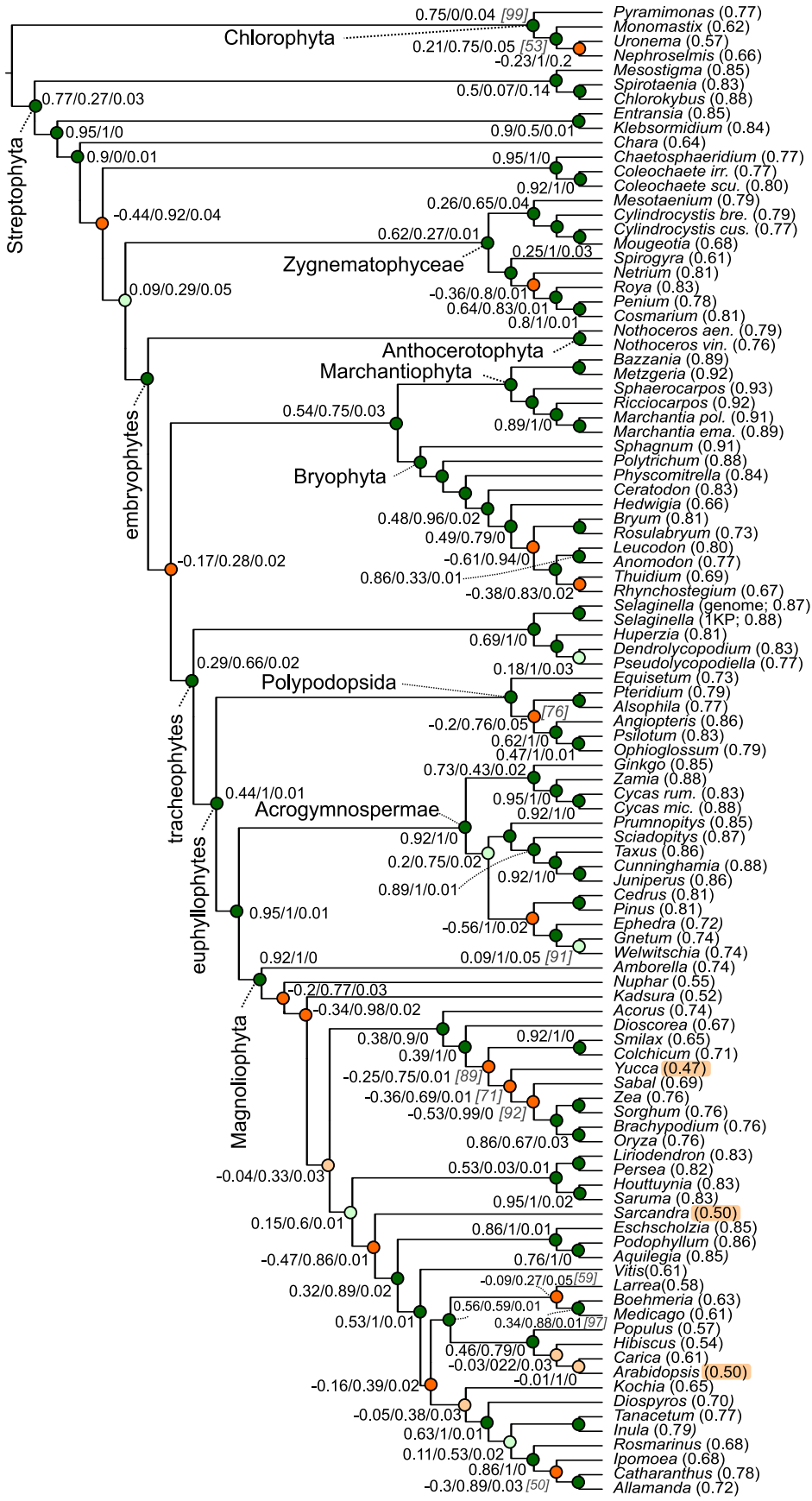
Examples:

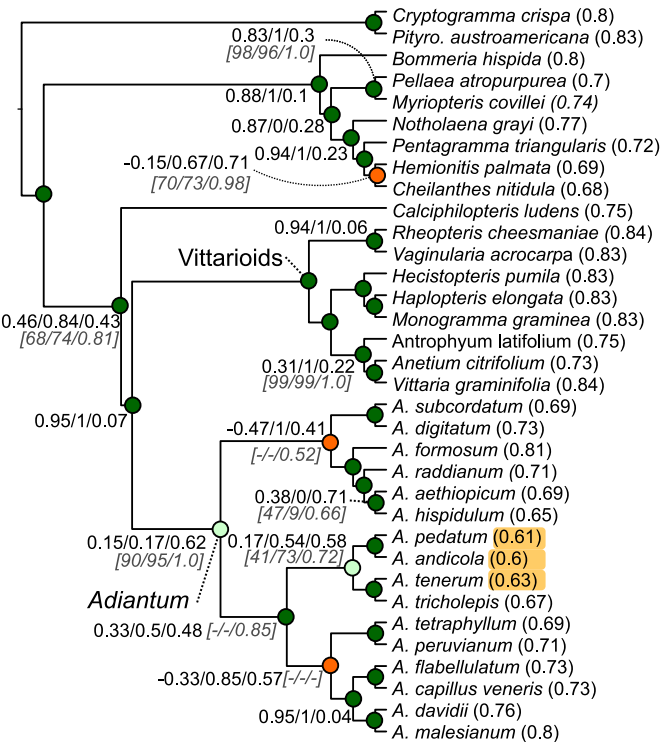
QF=1 → all concordant
QF=0.1 → 10% concordant
QF=0 → none concordant









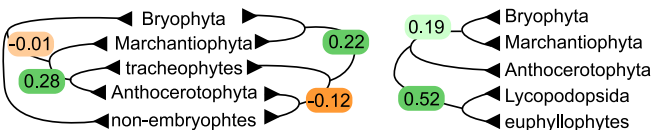


A. Non-vascular plants

HS2014

WI2014

ZN2014



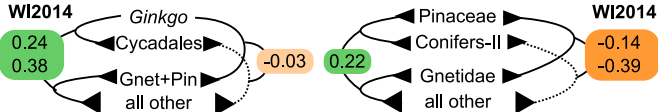
B. *Ginkgo* + cycads

ZN2014

WI2014

HS2014

ZN2014

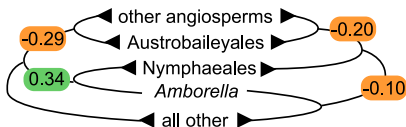


C. Gnetidae + conifers

D. "ANA grade" angiosperms

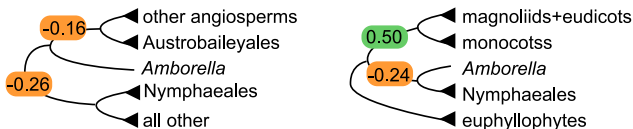
HS2014 ("Ambo+Nym-first")

WI2014 ("Amborella-first")



ZN2014 ("Nymphaeales first")

XI2014 ("Ambo+Nym-first")



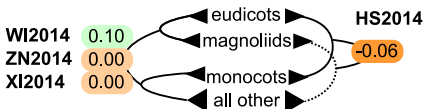
E. Magnoliids, monocots, and eudicots

WI2014

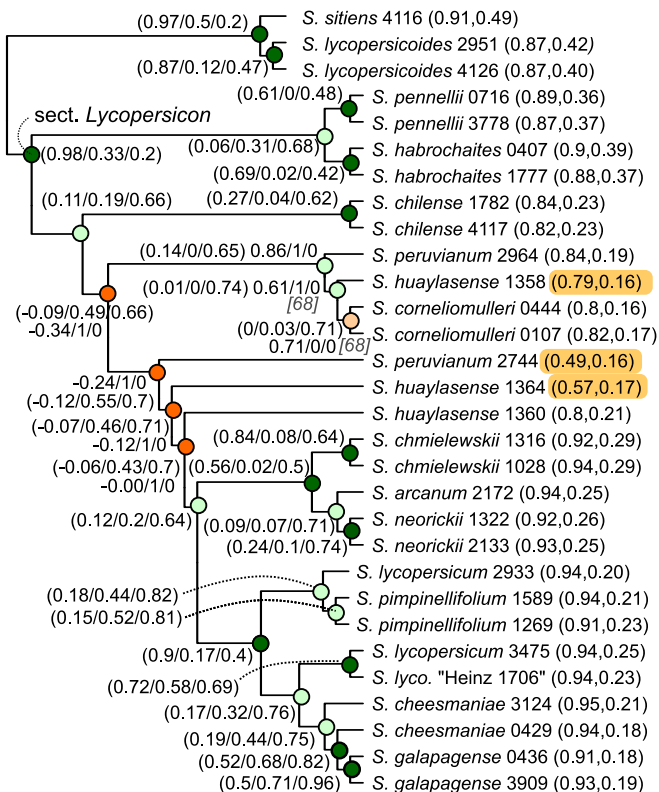
ZN2014

XI2014

HS2014



A. *Solanum* sect. *Lycopersicon*



B. Caryophyllales

