

## **Positive Feedback Between Contractile Ring Myosin and Ring-Directed Cortical Flow Drives**

### **Cytokinesis**

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## ABSTRACT

During cytokinesis, an equatorial actomyosin contractile ring rapidly transforms cell shape by constricting at a relatively constant rate despite its progressively decreasing size. The closure rate per unit length of the ring must accelerate as the ring gets smaller to maintain the overall constant rate of closure. Here, by generating a 4D map of cortical flow in conjunction with monitoring of ring component dynamics, we show that the acceleration in ring closure rate arises due to positive feedback between the ring and the surrounding cortex. Ring myosin pulls on the adjacent cortex generating ring-directed cortical flow that, in turn, accelerates constriction by delivering cortical myosin into the ring. We derive an analytical mathematical formulation that captures the positive feedback-dependent evolution of the contractile ring and use this formulation to provide a non-intuitive explanation for why reducing myosin activation by rho kinase inhibition slows contractile ring closure.

**KEYWORDS:** contractile ring, cortical flow, positive feedback, analytical mathematical model, rho kinase, LET-502, myosin II, anillin

## INTRODUCTION

During cytokinesis in animal cells, constriction of an equatorial actomyosin ring cinches the mother cell surface to generate a dumbbell-shaped structure with an intercellular bridge that connects the two daughter cells<sup>1, 2</sup>. The contractile ring assembles in response to the equatorial activation of RhoA<sup>2-4</sup>, which patterns the cortex by recruiting contractile ring components from the cytoplasm<sup>5-7</sup>. Recent work in the *C. elegans* embryo suggests that the equatorial cortex is compressed after this initial patterning, leading to the alignment of actin filament bundles as the ring forms<sup>8</sup>. After its assembly, the ring is thought to progressively disassemble as it constricts<sup>9, 10</sup>. Ring constriction must complete within a short cell cycle window during mitotic exit<sup>11-13</sup>. Timely constriction relies on the conserved ability of contractile rings to maintain a relatively constant closure rate despite their progressively decreasing perimeter<sup>14-21</sup>. This property implies that rings close at a faster rate per unit length as they get smaller. Prior work postulated that this acceleration arises because force generators, either myosin motors<sup>22</sup> or actin filament-based contractile units<sup>17</sup>, are retained during constriction, leading to an increase in their amount per unit length. This retention model presumes that acceleration arises from processes intrinsic to the contractile ring, ignoring potential influence of interactions between the ring and the adjacent cortex.

Here, we examine the role of interactions between the ring and surrounding cortex on contractile ring dynamics in the *C. elegans* embryo. Through 4D analysis of cortical flow in conjunction with monitoring of ring component dynamics during closure, we show that acceleration of the per unit length constriction rate does not arise from ring-intrinsic component retention, but instead results from positive feedback between ring myosin and ring-directed cortical flow. We derive an analytical mathematical formulation that captures the positive feedback-dependent evolution of the contractile ring and employ it to analyze experimental data to assess the effects of rho kinase inhibition, uncovering a new, non-intuitive explanation for why reducing myosin activation by rho kinase inhibition slows ring closure.

## RESULTS

### ***The cortex at the poles expands in response to tension generated by the constricting ring, whereas the intervening cortex flows towards the ring without expansion***

To assess the significance of interactions between the contractile ring and surrounding cortex on contractile ring dynamics, we generated a 4D map of cortical flow to determine how the cortex responds to ring pulling. We monitored cortical movement at high time resolution (**Fig. 1a, Movie S1**) in embryos expressing a GFP fusion with the heavy chain of non-muscle myosin II (NMY-2; hereafter myosin::GFP; **Supplementary Fig. 1a,b**), while also monitoring ring constriction at lower time resolution in the same embryos (**Fig. 1a, Supplementary Fig. 1d**). Myosin::GFP flows together with actin (LifeAct::mKate2) on the embryo surface (**Supplementary Fig. 1c**), consistent with the entire cell surface moving in a coordinated fashion during cytokinesis<sup>8, 23-28</sup>. Because the contractile ring closes asymmetrically within the division plane<sup>(29; Figs. 1a, Supplementary Fig. 1d)</sup>, the pattern of cortical movement cannot be inferred from imaging individual embryos. Therefore, we generated an average 4D map of cortical flow by computationally combining data from 93 embryos imaged in random rotational orientations (**Fig. 1a**). We defined the top of the embryo as the side where the furrow ingresses first, the bottom as the opposite side, and referenced positions around the embryo circumference by the angle  $\theta$  (**Fig. 1a**). For temporal alignment, we fit a line to normalized ring size ( $\bar{R} = R/R_{emb}$ ) versus time between 30% and 80% closure for each embryo (**Fig. 1a**), and extrapolated this line to 1 and 0 to define  $t_0$  (cytokinesis onset) and  $t_{ck}$  (time of cytokinesis), respectively. Cortical flow could not be monitored in the division plane or at the cell poles, due to their high curvature. Thus, this approach provided a quantitative picture of cortical movement in the central 2/3 of the embryo throughout cytokinesis (**Fig. 1b; Movie S2**).

The 4D map of cortical flow allowed us to determine where new cortical surface is gained as the ring closes. New cortical surface could be gained uniformly, immediately behind the contractile ring, or at the cell poles<sup>21, 27, 30-35</sup>; each pattern predicts a different profile of cortical velocity along the embryo axis (**Supplementary Fig. 1e**). The cortical velocity profiles measured from the flow map indicated that cortical surface is gained at the poles and subsequently moves with constant velocity towards the division plane (**Fig. 1b**). The velocity of cortical flow was higher on the top of the embryo during the first

half of cytokinesis when the furrow ingresses from the top (**Fig. 1b, black traces**) and became higher on the bottom of the embryo towards the end when the furrow ingresses from the bottom (**Fig. 1b, grey traces; Movie S2**).

Cutting the cortex parallel or perpendicular to the division plane using a laser revealed that the cortex is under tension during cytokinesis (**Fig. 2a**). However, parallel laser cuts had no effect on the constriction rate (**Fig. 2b,c**) indicating that cortical tension does not impose significant resistance to ring pulling. Inhibiting the Arp2/3 complex by depleting its ARX-2 subunit, which is expected to reduce effective cortical viscosity and thus cortical tension<sup>36-38</sup>, also did not alter the constriction rate (**Supplementary Fig. 2a-b**). Together, these results indicate that the cortex at the poles expands in response to tension generated by the constricting ring, whereas the cortex in the region between the ring and the poles flows towards the ring without expansion or compression. This differential response of the polar cortex to ring-generated tension, which results in a flow of myosin and other cortical components towards the cell equator, is consistent with hypotheses presented in early conceptual models of cytokinesis<sup>27, 39-44</sup>.

### ***The contractile ring pulls in extra cortex during constriction, leading to an exponential increase in the levels of ring components and in the ring constriction rate***

Recent work in the *C. elegans* embryo suggested that recruitment of contractile ring proteins following anaphase onset leads to compression of the equatorial cortex that aligns actin filaments to form the contractile ring<sup>8</sup>. Consistent with this, a gradient of cortical flow velocity that spans the cell equator is observed in our flow map at early timepoints prior to furrow ingression (**Supplementary Fig. 2c**). After contractile ring assembly, the ring has been proposed to constrict in an autonomous manner via continuous disassembly<sup>9, 45</sup>. In this view, the constricting ring would generate the division plane by pulling the cortex behind it, and the amount of cortex entering the division plane would equal the area of the division plane. To test this prediction, we analyzed the 4D cortical flow map to measure the total cortical surface area entering the division plane and compare it to the area of the division plane (accounting for the fact that two surfaces are generated—*red outline in Fig. 3a*). Surprisingly, this analysis

revealed that significantly more cortical surface entered the division plane than is necessary to build the plane: the flux of cortical area into the division plane was 1.5 to 2-fold higher than the rate of change in the area of the division plane throughout cytokinesis (**Fig. 3a,b**). In control embryos, more cortex flowed in from the posterior side than from the anterior side, likely due to distinct mechanical cortical properties downstream of the polarity machinery. Consistent with this, and with prior work showing that Arp2/3 inhibition impairs the recruitment of PAR-2 to the posterior cortex and makes myosin and actin dynamics on the posterior cortex more similar to those in embryo anterior<sup>46</sup>, inhibiting the Arp2/3 complex by depleting ARX-2 abolished the difference between the two sides, but did not change the imbalance between the total amount of cortex entering the division plane and the area of the plane (**Supplementary Fig. 2d; Movie S3**). Thus, significantly more cortical surface enters the division plane during cytokinesis than expected if the cortex passively trails behind the closing ring (**Fig. 3a**).

The extra cortex delivered into the division plane could concentrate in the ring and contribute to its closure, distribute within the division plane, or be lost due to disassembly (**Fig. 3c**). To distinguish between these and other possibilities, we monitored *in situ*-tagged myosin::GFP<sup>47</sup> (**Fig. 3d**) and GFP::anillin (**Supplementary Fig. 3a**) in the division plane. Both probes exhibited similar behavior, accumulating primarily within the ring (**Fig. 3d, Supplementary Fig. 3b**). Quantification of mean per unit length fluorescence around the ring (after attenuation correction; **Supplementary Fig. 3c**) revealed a steady increase for both markers as constriction proceeded. The increase began on the top, which ingresses first, and initiated later on the bottom, which ingresses after the constriction midpoint (**Fig. 3d, Supplementary Fig. 3b**). Thus, monitoring of myosin and anillin suggests that the extra cortical surface flowing into the division plane is incorporated into the ring and predicts that the amount of ring myosin and anillin should increase in proportion to the flux of extra cortical surface into the ring (**Fig. 3e**). To test this prediction, we compared the per unit length rate of ring-directed cortical flow to the per unit length amounts of myosin and anillin. All were well-fit by the same single exponential (**Fig. 3e,f**), consistent with the idea that cortical surface flowing into the division plane delivers components to the contractile ring during constriction.

The exponential increase in the per unit length levels of ring myosin and anillin during constriction (**Fig. 3f**) is best explained by positive feedback: ring myosin pulls in adjacent cortex, bringing additional myosin motors into the ring that in turn increase the velocity of ring-directed cortical flow (**Fig. 3g**). The per unit length constriction rate also increases with the same exponential kinetics as the per unit length rate of ring-directed cortical flow and the per unit length amounts of anillin and myosin (**Fig. 3h**). This coupling likely arises because the constriction rate, like the rate of ring-directed cortical flow, depends on the amount of ring myosin. The exponential increase in the per unit length constriction rate explains the ability of contractile rings to close at a relatively constant rate despite their progressively decreasing perimeter<sup>14-21</sup>. A relatively constant rate of closure is observed over a significant portion of ring constriction (**Fig. 1a**;  $t = 50-200s$ ) because the exponential increase in the per unit length constriction rate balances the decrease in ring size.

#### ***Component levels and fluorescence recovery after photobleaching of the division plane support constriction rate acceleration due to ring-directed flow versus component retention***

Our results indicate that the per unit length amount of contractile ring components increases exponentially, and suggest that this increase is due to delivery by cortical flow along the direction perpendicular to the ring. In this model, constriction in the around-the-ring direction does not alter the per unit length amount of ring components, but instead drives ring disassembly that reduces the total amount of ring components in proportion to the reduction in ring length (**Fig. 4a, left panel**). An alternative model for the increase in the per unit length amount of ring components, proposed based on work in fission yeast<sup>22</sup>, is that ring myosin and anillin accumulate in the ring because they are retained rather than lost during constriction (**Fig. 4a, middle panel**). In the retention model, the total amount of both components remain constant as the ring closes resulting in an increase in their per unit length amount that is inversely proportional to the reduction in ring size. Comparison with the total amounts of ring myosin and anillin suggested that, whereas the retention model fits the data well for  $t/t_{ck}$  between 0.2 and 0.6, there was significant deviation for timepoints outside of this range. In contrast, the ring-directed cortical flow model fit the data for the entire measured interval ( $t/t_{ck} = 0.0$  to 0.8; **Fig. 4b, Supplementary Fig. 3b**).

To distinguish between the retention and ring-directed flow models using an independent approach, we photobleached myosin in the entire division plane at ~30% closure, and monitored its subsequent recovery in the ring (**Fig. 4c**). The ring-directed cortical flow model predicts that the per unit length amount of bleached myosin should be constant and, since cortical myosin turns over faster than myosin in the ring ( $t_{1/2}$  of ~30s<sup>48, 49</sup>), cortical flow should rapidly deliver unbleached fluorescent myosin to the ring, leading to an exponential increase comparable to that in controls. In contrast, the retention model predicts that the per unit length amount of bleached myosin and any residual fluorescent myosin that is retained in the ring will increase in proportion to the decrease in the ring size (~1/R). We found that the per unit length amount of fluorescent myosin in the ring increased exponentially following bleaching, and the difference between the control and the bleached embryos, which reflects the amount of bleached myosin, remained constant, both of which agree with the predictions of the ring-directed cortical flow model (**Fig. 4c**). We note that this data also suggests that the recovery of myosin fluorescence in the ring is not due to exchange with myosin in the cytoplasm. If ring myosin were turning over due to exchange with cytoplasmic myosin, we would expect the FRAP curve to approach the control curve and the difference between the FRAP and control curves to disappear. Instead, the two curves remained parallel and the difference remained constant (**Fig. 4c**). This data suggest that rather than being due to exchange with cytoplasmic myosin, the recovery of ring fluorescence is due to a mechanism in which myosin on the cortex adjacent to the ring turns over, allowing resumption of delivery of myosin to the ring by cortical flow.

The conclusion that the per unit length amount of contractile ring components increases exponentially during constriction is in apparent contradiction to analysis in 4-cell stage *C. elegans* embryos, where we had previously reported an ~1.3-fold increase in myosin, anillin and septins as the ring perimeter decreased 2-fold (from 50 $\mu$ m to 25  $\mu$ m). However, this is in fact precisely what would be predicted by the ring-directed cortical flow model (see **Supplementary Figs. 4 and 5** for an analysis of ring component levels and recovery following photobleaching at the 4-cell stage).



Together these data suggest that, the acceleration of the per unit length constriction rate during closure, a conserved feature of contractile rings, does not arise from ring component retention, but from positive feedback between ring myosin and ring-directed cortical flow.

### ***An analytical mathematical formulation for the positive feedback-mediated evolution of the contractile ring***

The exponential accumulation of contractile ring components during constriction due to positive feedback complicates analysis of phenotypes observed following molecular perturbations. To enable analysis of experimental data, we therefore translated our experimental findings into an analytical mathematical framework (see **Methods** for detailed derivation), which we named the Cortical Flow Feedback (CoFFee) model. Based on our photobleaching data we assume that: (1) constriction in the around-the-ring direction does not alter the per unit length amount of ring components, but leads to ring disassembly that reduces the total amount of ring components in proportion to the reduction in ring length, and (2) myosin in the contractile ring does not turn over by exchange with myosin in the cytoplasm. Thus, increases in the per unit length amount of ring myosin are due to delivery by cortical flow along the direction perpendicular to the ring. We posit that myosin increases exponentially during constriction due to positive feedback between the per unit length amount of ring myosin and the velocity of cortical flow that delivers myosin into the ring (**Fig. 5a**). Positive feedback arises from the fact that the velocity of ring-directed cortical flow is proportional to the amount of ring myosin, and the amount of ring myosin increases in proportion to the velocity of cortical flow. The velocity of ring-directed cortical flow ( $v_{flow}(t)$ ) is related to the amount of ring myosin ( $M_{ring}(t)$ , per unit length) by a proportionality constant  $\alpha$  that reflects the ability of the cortex to be compressed (**Fig. 5b**, Eqn. (1)). Ring myosin increases at a rate proportional to the velocity of ring-directed cortical flow and the concentration of cortical myosin ( $m_{cort}$ ; **Fig. 5b**, Eqn. (2)). As a result of the positive feedback, ring myosin increases exponentially with a characteristic time  $\tau := 1/\alpha m_{cort}$  (time required for ring myosin to increase  $\sim 2.7$  fold; **Fig. 5b**, lower left). The per unit length constriction rate is proportional to the amount of ring myosin, being related by a constant  $\beta$  that reflects the ability of the ring to be constricted (**Fig. 5b**, Eqn. (3)).

We solved the model equations in a specific time reference to obtain expressions for contractile ring size and component levels that can be used to fit data. Instead of  $t = 0$  being defined by extrapolation of plots of  $\bar{R}$  ( $:= R/R_{emb}$ ) versus time (**Fig. 1a**), which is not ideal in a mathematical formulation, we set  $t = 0$  as the halfway point of ring closure ( $\bar{R}(t = 0) = \frac{1}{2}$ ). This time reference also avoids the difficulty of assessing cytokinesis onset. In this time reference, the equation for ring size is:

$$\bar{R}(\bar{t}) = \bar{R}_{ini}(2\bar{R}_{ini})^{-\exp(\bar{t})}, \quad (4)$$

where  $\bar{t} := t/\tau$  and  $\bar{R}_{ini}$  is the dimensionless characteristic ring size (held fixed at a value of 1.1; see Methods). Any component that localizes to the cell cortex will be delivered to the contractile ring via the same process as myosin, so contractile ring components all accumulate in a similar fashion, with

$$C_{ring}(\bar{t}) - C_{ring,base} = \frac{\alpha c_{cort}}{\beta} \ln(2\bar{R}_{ini}) e^{\bar{t}}, \quad (5)$$

$$C_{ring,base} := C_{0,ring} - \ln(2\bar{R}_{ini}) \frac{\alpha c_{cort}}{\beta}, \quad (6)$$

where  $C_{0,ring}$  is the per unit length amount of the component at the half-way point of ring closure,  $C_{ring,base}$  is the baseline amount of the ring component that does not increase exponentially, and  $c_{cort}$  ( $m_{cort}$  for myosin) is the concentration of the component on the cortex that is delivered to the ring. The velocity of cortical flow and the constriction rate are

$$v_{flow}(\bar{t}) = \frac{\alpha}{\beta} \ln(2\bar{R}_{ini}) e^{\bar{t}}, \quad (7)$$

$$-\frac{1}{\bar{R}} \frac{d\bar{R}}{d\bar{t}} = \ln(2\bar{R}_{ini}) e^{\bar{t}}. \quad (8)$$

Thus, the per unit length constriction rate, velocity of cortical flow, and ring component amounts all increase exponentially with the characteristic time of ring myosin accumulation ( $\tau = 1/\alpha m_{cort}$ ) set by the feedback loop between ring myosin and cortical flow (**Fig. 5b**), as we observe experimentally (**Fig. 3e-h**).

**Reducing the concentration of cortical myosin reduces the ability of the ring to be constricted by ring myosin**

To address the effect of reducing myosin activation on cytokinesis and evaluate the utility of the mathematical formulation for analyzing experimental data, we characterized the effects of depleting rho kinase (LET-502). Rho kinase contributes to myosin activation by promoting regulatory light chain phosphorylation. Due to parallel pathways for myosin activation, penetrant rho kinase inhibition slows, but does not prevent, ring constriction<sup>29, 50, 51</sup>. We imaged control and rho kinase-depleted embryos expressing *in situ* tagged myosin::GFP. To assess the impact of rho kinase inhibition on the properties of the ring and cortex, we measured  $m_{cort}$  and fit experimental measurements of ring size and ring myosin to equations (4) and (5) to determine the effect on the parameters  $\alpha$  and  $\beta$  (**Fig. 6a**). Direct measurement revealed that the amount of cortical myosin,  $m_{cort}$ , was reduced by 20% ( $m_{cort}^{RKdep} = 0.8 m_{cort}^{WT}$ ; **Fig. 6b**). Next, we fit traces of ring size versus time ring size equation (4) to determine characteristic times, ( $\tau = 1/\alpha m_{cort}$ ), for each embryo (**Fig. 6c**). This analysis revealed that  $\tau$  was 1.3-fold higher in rho kinase-depleted embryos compared to controls ( $120 \pm 20$  s versus  $90 \pm 10$  s in controls; **Fig. 6c, middle row**) indicating that  $\alpha^{RKdep} m_{cort}^{RKdep} = 0.8 \alpha^{WT} m_{cort}^{WT}$ . Since  $m_{cort}^{RKdep} = 0.8 m_{cort}^{WT}$ , we conclude that  $\alpha^{RKdep} = \alpha^{WT}$ , i.e., the ability of the cortex to be compressed by ring myosin is unchanged. Measuring the mean per unit length amount of myosin::GFP in the ring in control and rho kinase depleted embryos and fitting the data to the equation for ring myosin (5) revealed that the exponential prefactor was equivalent for the two conditions ( $\alpha^{RKdep} m_{cort}^{RKdep} / \beta^{RKdep} = \alpha^{WT} m_{cort}^{WT} / \beta^{WT}$ ; **Fig 6c, bottom row**). This indicates that the per unit length amount of myosin for a given ring size is the same in control and rho kinase depleted embryos and that the ability of the ring to be constricted by ring myosin is reduced in rho kinase depleted embryos compared to controls ( $\beta^{RKdep} = 0.8 \beta^{WT}$ ).

The effects of rho kinase inhibition identified by our analysis are schematically summarized in Figures 7a and b. Rho kinase inhibition decreases  $m_{cort}$  to 80% of its value in controls, which slows myosin accumulation via the feedback loop and increases  $\tau$ . Normalizing time by  $\tau$  and setting  $\bar{t} = 0$  at 50% closure superimposes the constriction rate curve with the control (**Fig. 7b, Supplementary Fig. 6a**). This is a convenient reference frame because comparing component levels and flow velocity at the same  $\bar{t}$  corresponds to comparing them for the same ring size. The fact that rho kinase inhibition reduces the ability of the ring to be constricted by ring myosin ( $\beta$ ) causes the onset of constriction to be delayed

relative to the feedback loop between ring myosin and cortical flow (see **Supplementary Fig. 6c** for a detailed explanation). Thus, in the  $\bar{t}$  frame of reference the velocity of cortical flow is predicted to be 1.25 fold higher for all ring sizes in rho kinase depleted embryos compared to controls (**Fig. 7b**, middle panel). The increased velocity of cortical flow precisely compensates for the reduction in the concentration of cortical myosin. As a result, rho kinase-depleted rings of any given size contain the same amount of myosin as controls (**Fig. 7b, Fig. 6c, Supplementary Fig. 6b**).

Filming control and rho kinase depleted embryos expressing GFP::anillin and performing a similar analysis, revealed that the concentration of cortical anillin ( $c_{ani,cort}$ ) is not altered by rho kinase inhibition. Our model would predict that the per unit length amount of cortical anillin would be 1.25-fold higher in rings of all sizes due to the increase in cortical flow, which delivers more anillin into the ring. Consistent with this prediction, we observed a 1.21 fold increase in mean per unit length GFP::anillin fluorescence in the ring (**Fig. 7c**). Thus, an analysis of rho kinase-depleted embryos employing the mathematical formulation of the positive feedback model for cytokinetic ring closure leads to the counterintuitive conclusion that reducing the concentration of cortical myosin makes it more difficult for rings of the same size with the same amount of myosin to constrict. We suggest that this is because the compensatory increase in cortical flow that restores ring myosin to control levels leads to an overabundance of other components (e.g. anillin) that increase resistance of the ring to constriction. More broadly, the analysis of rho kinase inhibition, employing straightforward-to-measure experimental parameters, highlights the utility of the mathematical formulation we present to explain the complex and non-intuitive effects of molecular perturbations on cytokinesis.

## DISCUSSION

Our identification of a feedback loop between ring myosin and ring-directed cortical flow that fuels constriction explains the conserved ability of the cytokinetic ring to close at a relatively constant rate despite decreasing perimeter, which is critical to allow cytokinesis to complete in a temporally restricted cell cycle window<sup>11-13</sup>. In contrast to prior models proposing that the acceleration in the per unit length constriction rate results from the retention of force generating units<sup>17, 22</sup>, our data indicate that this

acceleration arises from continuous delivery of myosin into the ring by ring-directed cortical flow. In addition to ensuring timely cell content partitioning, such a mechanism may render the ring robust to mechanical challenges that it encounters while ingressing through the crowded cell interior. The analytical mathematical formulation that we built captures the evolution of the contractile ring and associated cortical network during cytokinesis and enables analysis of experimental data and interpretation of the effects of molecular perturbations on this complex dynamic process. Ring-directed flows have been observed in the context of wound healing<sup>52</sup> and similar types of cortical dynamics driven by coordinated patterns of contractility and relaxation are relevant in many contexts including cell polarization, cell motility, and tissue morphogenesis<sup>49, 53, 54</sup>, suggesting that the positive feedback between myosin in contractile structures and cortical flow may act in physiological contexts beyond cytokinesis.

## METHODS

### *C. elegans* strains used in this study

Strain Name	Genotype	Reference
OD821	<i>ItSi200</i> [pOD1997; <i>Pnmy-2::nmy-2::gfp</i> ; <i>cb-unc-119(+)</i> II; <i>unc-119(ed3)</i> III	This study
OD857	<i>ItSi200</i> [pOD1997; <i>Pnmy-2::nmy-2::gfp</i> ; <i>cb-unc-119(+)</i> II; <i>unc-119(ed3)</i> ; <i>ruls32</i> [pAZ132; <i>pie-1/GFP::histone H2B</i> ] III	This study
OD858	<i>ItSi803</i> [pOD1998; <i>Parx-7::GFP::arx-7</i> ; <i>cb-unc-119(+)</i> II; <i>unc-119(ed3)</i> III;	This study
LP162	<i>nmy-2(cp13[nmy-2::gfp + LoxP]) I</i>	Dickinson et al. 2013 <sup>47</sup>
OD95	<i>unc-119(ed3)</i> III; <i>ItIs37</i> [pAA64; <i>Ppie-1::mCherry::his-58</i> ; <i>unc-119(+)</i> ] IV; <i>ItIs38</i> [pAA1; <i>Ppie-1::GFP::PH(PLC1delta1)</i> ; <i>unc-119 (+)</i> ]	Essex et al., 2009 <sup>55</sup>
OD3011	<i>ItSi1123</i> [pSG017; <i>Pani-1::GFP::ani-1 RE-encoded-exon5::ani-1 3'-UTR</i> ; <i>cb unc-119(+)</i> ]III; <i>unc-119(ed3)</i> III	This study
GOU2047	<i>cas607</i> [ <i>arx-2::gfp knock-in</i> ] V	Zhu et al., 2016 <sup>56</sup>

The *C. elegans* strains listed in the table were maintained at 20°C using standard methods. OD821 and OD858, expressing NMY-2::GFP, GFP::anillin, and GFP::ARX-7 were generated using a transposon-based strategy (MosSCI;<sup>57</sup>). Genomic regions encoding *nmy-2* (including 2079 bp and 1317 bp up and downstream of the stop codon, respectively), *ani-1* (including 2015 bp and 1215 bp up and downstream of the stop codon), and *arx-7* (including 3056 bp and 634 bp up and downstream of the stop codon) were cloned into pCFJ151 and sequences encoding GFP were inserted either just before (*nmy-2*) or after (*arx-7* and *ani-1*) the start codon. The single copy *nmy-2* transgene was generated by injecting a mixture of repairing plasmid (pOD1997, 50ng/μL), transposase plasmid (pJL43.1, Pglh-2::Mos2 transposase, 50ng/μL), and fluorescence selection markers (pGH8, Prab-3::mCherry neuronal, 10ng/μL; pCFJ90, Pmyo-2::mCherry pharyngeal, 2.5ng/μL; pCFJ104, Pmyo-3::mCherry body wall, 5ng/μL) into EG6429 (ttTi5605, Chr II). Single copy *ani-1* and *arx-7* transgenes were generated by injecting a mixture of repairing plasmid (pSG017 (*ani-1*) or pOD1998 (*arx-7*), 50ng/μL), transposase plasmid (CFJ601, Peft-3::Mos1 transposase, 50ng/μL), selection markers (same as for *nmy-2* strain) and an additional negative selection marker (pMA122; Phsp-16.41::peel-1, 10ng/μL) into EG6429 (ttTi5605, Chr II). After one week, progeny of injected worms were heat-shocked at 34°C for 2-4 hours to induce PEEL-1 expression and

kill extra chromosomal array containing worms<sup>58</sup>. Moving worms without fluorescent markers were identified and transgene integration was confirmed in their progeny by PCR spanning both homology regions in all strains.

### C. elegans RNA-mediated interference

Gene	Oligonucleotide 1	Oligonucleotide 2	Template	mg/ml
<i>arx-2</i> (K07C5.1)	TAATACGACTCACTA TAGGTCAGCTTCGTC AAATGCTTG	AATTAACCCTCACTA AAGGTGCAATACGC GATCCAAATA	N2 DNA	1.7
<i>let-502</i> (C10H11.9)	TAATACGACTCACTA TAGGCAGCGATCGT CTGCTTATCA	AATTAACCCTCACTA AAGGTGGCTGTCTCGA GTTACGAATG	N2 DNA	1.9

Single-stranded RNAs (ssRNAs) were synthesized in 50µL T3 and T7 reactions (MEGAscript, Invitrogen, Carlsbad, CA) using cleaned DNA templates generated by PCR from N2 DNA using the oligos in the table above. Reactions were cleaned using the MEGAclean kit (Invitrogen, Carlsbad, CA), and the 50 µL T3 and T7 reactions were mixed with 50µL of 3× soaking buffer (32.7mM Na<sub>2</sub>HPO<sub>4</sub>, 16.5mM KH<sub>2</sub>PO<sub>4</sub>, 6.3mM NaCl, 14.1mM NH<sub>4</sub>Cl), denatured at 68°C for 10min, and then annealed at 37°C for 30 min to generate dsRNA. L4 hermaphrodite worms were injected with dsRNA and allowed to recover at 16°C for 44-50 hours prior to imaging.

### Monitoring cortical flow

Cortical flow was monitored in images of the cortical surface in embryos expressing myosin::GFP obtained from adult hermaphrodites by dissection. Embryos were mounted followed by sealing with a coverslip on double thick (1 mm) low percentage agarose (0.5%) pads to prevent compression that biases the initial angle of furrow ingression (**Supplementary Fig. 1b**). Images were acquired on an inverted microscope (Axio Observer.Z1; Carl Zeiss) equipped with a spinning-disk confocal head (CSU-X1; Yokogawa) and a 63× 1.40 NA Plan Apochromat lens (Zeiss) using a Hamamatsu Orca-ER digital camera (Model C4742-95-12ERG, Hamamatsu photonics). Images were collected using custom software, written in Python, that utilizes the Micro-Manager (open source software,<sup>59</sup>) microscope control library. A 3 x 0.75 µm z-series was collected (400ms exposure, 10-20% laser power) every 2s. After 15

time points, a 15 x 1 $\mu$ m z-stack, offset by 3 $\mu$ m from the cortical surface, was imaged to monitor the position of the closing contractile ring. The entire imaging series was repeated every 36s until the end of cytokinesis. Cortical flow was measured in maximum intensity projections of the 3 x 0.75 $\mu$ m z-stacks of the cortical surface, after orientation of the images to place the embryo anterior at the top and the posterior at the bottom, by correlating myosin fluorescence between consecutive images using Gunnar Farneback's algorithm<sup>60</sup> implemented within the openCV library with a 30-pixel window size. The threshold was calculated for every image by maximizing the ratio of total intensity inside a 200x350 pixel box positioned in the center of the embryo to the total intensity outside that box.

### ***Measurement of contractile ring position and size***

Automated methods were employed to identify the edges of the embryo, determine the position of the contractile ring, and reconstruct the rings for each time point in an end-on view to determine the initial ingression axis (**Supplementary Fig. 1d**). Ring size and position were determined using custom Python software that: (1) identifies the orientation of the anterior-posterior (AP) axis and rotates the embryo to place the embryo anterior at the top and the embryo posterior at the bottom, (2) finds the embryo center in different x-z planes along the AP axis and calculates embryo radius, and (3) calculates the radius of the contractile ring and determines its position within the division plane. Details of each step are outlined below.

Orienting embryos with their anterior end to the top: Acquired z-plane images were convolved with a 10-pixel Gaussian kernel to reduce noise. An optimal signal threshold that partitioned the embryo interior from exterior was identified by finding a local minimum in the intensity histogram that produced a binary mask with expected area ( $\sim 120000 \pm 50000$  pixel<sup>2</sup>). The orientation of the AP axis was identified by fitting an ellipse to the thresholded area in the middle plane of the z stack. The anterior side was identified by higher cortical myosin fluorescence and all images were rotated to place the embryo anterior at the top of the image and the embryo posterior at the bottom.

Defining the central axis of embryo and determining embryo width: The central axis of the embryo was defined by drawing a horizontal line across the oriented embryo at the midpoint between its anterior



and posterior ends and identifying the first and last points along this line with signal above the threshold for each z-plane. The identified pixels were virtually projected in an end-on (x-z) view and fit to a circle by minimizing residuals. To account for fluctuations in the embryo boundary due to noise and fluorescence variation, the procedure was repeated 9 more times after shifting the position of the horizontal line towards the anterior pole by 10 pixels, covering approximately 1/5 of the embryo length (500 pixels). The position of the AP axis and the radius of the embryo were determined by averaging the 10 measurements.

Measuring contractile ring size and position: As illustrated for the central plane images shown in Supplementary Figure 1d, the position of the contractile ring was determined by identifying pairs of points with the highest myosin fluorescence intensity on the opposite edges of the embryo in each z-plane that were not more than 20 pixels apart in the horizontal direction and were located at a y-axis position near the embryo middle. Contractile ring radius and position were determined by projecting the points to generate an end-on (x-z) view and fitting the data with a circle. The ring fit was iteratively improved by calculating predicted positions of myosin fluorescence at the ring in each z-plane using initially fitted parameters. Intensity maxima within 5 pixels of the predicted location were identified and the ring was refit. The initial guesses for the contractile ring size and position at the next time point were estimated from the previously calculated ring values. The algorithm restricted the ring position fluctuations to 20 pixels along anterior-posterior axis and the size was estimated assuming constant rate of ring constriction. The automatic ring measurements were manually confirmed for each embryo. The initial ingress axis was determined as illustrated (**Supplementary Fig. 1d**) by fitting a line through the centers of the rings with a normalized ring size ( $\bar{R} := R/R_{emb}$ ) > 0.3.

### ***Embryo time alignment for averaging***

Sequences from individual embryos were time aligned by defining zero time ( $t_0$ ) and the total time of cytokinesis ( $t_{CK}$ ) for each embryo, and normalizing time by  $t_{CK}$  prior to averaging,  $\hat{t} := \frac{t-t_0}{t_{CK}}$ . An initial determination of  $t_0$  and  $t_{CK}$  was made by fitting a line to the plot of normalized ring size ( $\bar{R}(t) := R/R_{emb}$ ) versus time between 30% and 80% closure for each embryo as outlined in Figure 1a. Extrapolation of

this line for each embryo defined  $t_0$  as the time where the fitted line intersects 1, and the time of cytokinesis,  $t_{CK}$  as the time where the fitted line intersects 0. Due to the small number of measurements from each embryo available for fitting (3-5 values where  $0.8 > \bar{R} > 0.3$ ), the values of  $t_0$  and  $t_{CK}$  were refined by fitting  $\bar{R}(\hat{t})$  for each embryo to the average dimensionless ring size,  $\langle \bar{R} \rangle(\hat{t})$ . The calculation of the average dimensionless ring size was performed in iterative manner. The time for each embryo was aligned by  $t_0$  and normalized by  $t_{CK}$  using estimates from the fitted line in the first iteration. The average dimensionless ring size ( $\langle \bar{R} \rangle(\hat{t})$ ) was calculated by averaging normalized ring sizes of all embryos at corresponding normalized time. Contractile ring size was approximated for intermediate time points by linear interpolation. In further iterations,  $t_0$  and  $t_{CK}$  were refined for every embryo by minimizing the residuals between its normalized ring size,  $\bar{R}(\hat{t})$ , and the average dimensionless ring size,  $\langle \bar{R} \rangle(\hat{t})$ , throughout the entire timecourse of cytokinesis, thus increasing the number of time points available for fitting  $t_0$  and  $t_{CK}$  (6-10 values per embryo). After refining time alignment and normalization for each embryo, average dimensionless ring size was re-calculated and  $t_0$  and  $t_{CK}$  were refined for each embryo again. The refinement process was repeated until changes in average dimensionless ring size,  $\langle \bar{R} \rangle(\hat{t})$ , were smaller than 0.001 on average (achieved within a few iterations). The collective fitting of all  $t_0$  and  $t_{CK}$  at every iteration was performed under restriction that the line fit through  $\langle \bar{R} \rangle(\hat{t})$  between 0.8 and 0.3 intercepted 0 at  $\hat{t} = 0$  and 1 at  $\hat{t} = 1$ . This restriction ensured that  $t_0$  and  $t_{CK}$  determined from fits of individual embryos to the average ring size would be consistent with their original definition. The dimensional ring kinetics,  $\langle R \rangle(t)$ , can be recovered using the following equation

$$\langle R \rangle(t) = \langle R_{emb} \rangle \langle \bar{R} \rangle(\hat{t} \langle t_{CK} \rangle), \quad (9)$$

where  $\langle R_{emb} \rangle = 14.7 \pm 0.7 \mu m$  and  $\langle t_{CK} \rangle = 200 \pm 30 s$  are average embryo radius and time of cytokinesis accordingly.

### **Cortical flow averaging**

Cortical flow averaging was performed after spatial and temporal alignment of data collected in different embryos (n=93 embryos from 93 worms filmed over the course of 5 days for control, **Movie S2**; n=68 embryos from 68 worms filmed over the course of 4 days for *arx-2(RNAi)*, **Movie S3**). The number

of embryos was chosen to achieve at least 10-fold coverage for all areas of the cortical map for controls and 5-fold coverage for *arx-2(RNAi)*. Linear interpolation was used to approximate the flow between consecutive time points. Because our imaging regime required periodic z-stack acquisition to determine the trajectory of ring closure, no flow approximation was done during those time periods (~6s gap every 30s). The flow data for each time point was represented as a set of vectors with direction and magnitude corresponding to the direction and magnitude of the cortical flow at the base of the vector. The base of each vector had two spatial coordinates:  $x$ , the position along the anterior-posterior axis (where the position of the contractile ring was defined as 0), and  $\theta$ , the angular position relative to the initial ingression axis (defined as described in **Fig. 1a** and **Supplementary Fig. 1d**). We note that mitotic exit is accompanied by a brief (~50-60s) period of rotational flow (<sup>61, 62</sup>; see **Movie S1**);, which dissipates soon after initiation of cytokinesis ( $\sim \hat{t}=0.2-0.3$ ). As this rotational contribution is not relevant here, we removed it by averaging the data from the right and left halves of the embryo (in an end-on view), allowing us to focus on rotation-independent flows. Thus the flow with angular positions greater than 180 degrees was mirrored in angular direction

$$f_{\theta}(\hat{t}, x, \theta > 180) \rightarrow -f_{\theta}(\hat{t}, x, 360 - \theta), \quad (10)$$

$f_{\theta}$  is the angular component of the flow vector  $\vec{f}$ . The flows were normalized by the embryo size and cytokinesis rate  $\vec{f}(\hat{t}, x, \theta) := \frac{t_{CK}}{R_{emb}} \vec{f}(\hat{t}, x, \theta)$  and averaged according to its position and time

$$\langle \vec{f} \rangle (\hat{t}, x, \theta) = \frac{\sum_{emb} \vec{f}(\hat{t}, x, \theta)}{N_{emb}}. \quad (11)$$

### **Calculation of expected cortical surface flow profiles**

To aid in the interpretation of experimental results, expected profiles for cortical surface movement were calculated for defined patterns of cortical surface increase and plotted in **Figure 1b** and **Supplementary Figure 1e**. The general form of surface movement velocity is given by the following equation

$$v(x) = \int_0^x g(x') dx' + u, \quad (12)$$

where  $g(x)$  is the amount surface gain and  $u$  is the velocity of asymmetric ring movement, which could be positive or negative, depending on whether the ring is moving towards or away from the surface.

From equation (12) we obtain the following predictions

Uniform surface increase:  $v(x) = Cx + u$ ;

Polar surface increase:  $v(x) = C + u$ ;

Behind the ring surface increase:  $v(x) = u$  (if the asymmetry of cytokinetic furrowing arises due to global surface movement) or  $v(x) = 0$  (if the asymmetry in surface increase is related to the asymmetric furrowing).

### ***Cortical laser ablation***

Cortical laser ablations, presented in Figure 2, were performed using a robotic laser microscope system (RoboLase)<sup>63</sup>. Embryos expressing myosin::GFP were mounted using standard procedures. A cortical cut, approximately 10  $\mu\text{m}$  long, was made on the anterior side of the embryo when the ring was at ~50% closure (7 $\mu\text{m}$  radius). The cut was confirmed by comparison of cortical fluorescence images before and after the cut and was considered successful if the foci moved away from the cut area (~3.5 $\mu\text{m}$  distance), indicating cortical tension release. Contractile ring closure rate was calculated by measuring the difference in ring sizes before and after the cut, assessed from two 4x2 $\mu\text{m}$  z-stacks acquired immediately before the cut and 13s later. Errors in measuring the radius at the two timepoints were determined from the procedure used to fit the data to a circle and were propagated to determine the errors in the constriction rate measurements for individual embryos; mean errors are S.E.M. The cortical opening after ablation was approximately 35 $\mu\text{m}^2$ ; this translates into an additional reduction in ring radius by ~0.8 $\mu\text{m}$ , if the cortical surface tension dominates the ring closure rate. This additional decrease in ring size within 13s should correspond to increase of the control rate (0.22 $\mu\text{m/s}$ ) by ~30% (0.06 $\mu\text{m/s}$ ). The experiment was repeated 19 times for no cut condition, 14 times for parallel cut, and 15 times for perpendicular cut. All imaging was performed over the course of 5 days. The number of embryos was chosen to achieve sufficient accuracy in the determination of mean ring closure rates to determine if it was altered by the cuts.

### Calculation of the surface area flowing into the division plane

We calculated the amount of surface area flowing into the division plane from flow measurements made 7  $\mu\text{m}$  away from the position of the furrow on the anterior and posterior sides (as illustrated in **Figure 3a**). The rate of the surface flow is

$$\frac{dA_{surf}}{d\hat{t}}(\hat{t}) = 2R_{emb} \int_0^\pi \langle \vec{f} \rangle(\hat{t}, x_0, \theta) d\theta, \quad (13)$$

where  $x_0$  is -7  $\mu\text{m}$  and 7  $\mu\text{m}$  for the rate of flow from the anterior or the posterior sides, respectively. The total amount of surface area that entered the division plane from any time  $\bar{t}_0$  to  $\bar{t}$  is obtained by integrating equation (13) **Error! Reference source not found.** over time

$$A_{surf}(\hat{t}) = \int_{\hat{t}_0}^{\hat{t}} \left. \frac{dA_{surf}}{d\hat{t}} \right|_{ant} + \left. \frac{dA_{surf}}{d\hat{t}} \right|_{post} (t') dt'. \quad (14)$$

The increase in area of the division plane was calculated as following

$$A_{div\ plane}(\hat{t}) = 2\pi(\langle R \rangle^2(\hat{t}_0) - \langle R \rangle^2(\hat{t})). \quad (15)$$

In Figure 3a we used  $\hat{t}_0 = -0.2$ . The extra cortex delivered into the ring can be inferred from the difference between the surface area entering the division plane and the area of the division plane

$$A_{flow}(\hat{t}) := A_{surf}(\hat{t}) - A_{div\ plane}(\hat{t}). \quad (16)$$

### Division plane imaging

For quantification of myosin::GFP and GFP::anillin amounts in the contractile ring, adult worm dissection and one-cell stage embryos imaging was performed in a custom microdevice<sup>64</sup>. The device was mounted on an inverted microscope (Axio Observer.Z1; Carl Zeiss) and embryos were imaged with a 63x1.4NA Plan Achromat objective using an electron-multiplying charge-coupled device camera (QuantEM:512SC, Photometrics; 100ms exposure, EM gain set to 500, 10% laser power). Division planes were reconstructed from 40 x 0.5 $\mu\text{m}$  z-stacks collected every 30s after background subtraction and attenuation correction. All imaging was done at 20°C.

### ***Contractile ring photo-bleaching and imaging***

1-cell stage embryos were mounted in microdevices as for division plane imaging and 4-cell stage embryos were mounted on slides with 2% agarose pads. Embryos were imaged on a Nikon TE2000-E inverted microscope equipped with a 60x1.40NA objective, an EM-CCD camera (iXon; Andor Technology; EM-Gain=220, Exposure =100ms), and a krypton-argon 2.5 W water-cooled laser. For 1-cell stage embryos, division planes were reconstructed from 30x1 $\mu$ m stacks acquired every 20s with 20% laser power and photo-bleaching was performed by 2 sweeps of a 488nm laser with 100% power and 500 $\mu$ s dwell time. For 4-cell stage embryos, division planes were reconstructed from 16x1 $\mu$ m stacks acquired every 10s with 50% laser power and photo-bleaching was performed by 2 sweeps of a 488nm laser with 100% power and 100 $\mu$ s dwell time. For 4-cell stage embryos, the time between the prebleached and first postbleached images was 6s.

### ***Estimation of depth attenuation***

To estimate depth attenuation within the division plane, we quantified the intensity of the division plane in two cell embryos expressing a GFP-tagged probe expected to be uniformly present on the plasma membrane. From each image, we subtracted a background intensity calculated as the average value inside two 4x4  $\mu$ m rectangles positioned 2  $\mu$ m away from the division plane inside the anterior and posterior cells. The division plane intensity profile was obtained by performing a 30 pixel maximum intensity projection along the AP axis, with the division plane positioned approximately in the middle (**Supplementary Fig. 3c**). The intensity profiles in z from 13 embryos were fitted to an exponential using the same characteristic attenuation depth for all embryos

$$I = I_0 e^{-z/z_{att}}, \quad (17)$$

which yielded a characteristic depth of attenuation,  $z_{att}$ , of 15  $\mu$ m.

### ***Quantification of myosin and anillin intensity in the contractile ring and on the cortex***

For embryos at the 1-cell stage, myosin::GFP and GFP::anillin intensities in the contractile ring and on the cortex were quantified in 40x0.5  $\mu$ m z-stacks containing the ring after correction for depth

attenuation and subtraction of background fluorescence. Average intensity along the ring was calculated across a set of embryos in 30 degree arcs (for myosin::GFP, n=36 embryos from 18 worms filmed over 5 days for controls and 24 embryos from 15 worms filmed over 5 days for *let-502(RNAi)*; for anillin::GFP, n= 26 embryos from 14 worms filmed over 4 days and 30 embryos from 18 worms filmed over the course of 4 days for *let-502(RNAi)*). The number of embryos was chosen to determine mean fluorescence with sufficient accuracy to derive appropriate conclusions. Positions along the ring were referenced based on the angle between the line from the position on the ring to the ring center and the initial ingression axis. Linear interpolation in time was used for every embryo to estimate intensity in the intermediate time points to perform averaging. Measured intensities were divided by arc length and averaged between different embryos to obtain mean GFP fluorescence per unit length for different angular ranges and the average for all angles. Total ring GFP fluorescence was calculated by integrating over ring perimeter. Cortical intensities were quantified by choosing the time point with the ring size closest to  $\bar{R} = 0.8$  and measuring total fluorescence in the 15<sup>th</sup> plane after correction for depth attenuation and subtraction of background fluorescence.

Measurements of myosin::GFP fluorescence in the ring at the 4-cell stage were performed as described in Carvalho et. al., 2009. However background fluorescence was determined as the mean fluorescence within a variable size circle at least 10 pixels in diameter, instead of fixed at 10 pixels, to improve measurement quality.

### ***Derivation of the Cortical Flow Feedback (CoFFee) model for cytokinesis***

The CoFFee model formalizes the following conceptual view of cytokinesis: Active RhoA recruits contractile ring components to the equatorial cortex, where myosin engages with actin to exert an isotropic force that compresses the underlying cortex. Polar relaxation releases tension in the direction perpendicular to the ring, but not in the around-the-ring direction, generating anisotropic boundary conditions that cause the system to exhibit distinct behavior in the two directions. Disassembly in the around-the-ring direction reduces ring components in proportion to the reduction in length, and does not alter the per unit length amount of myosin. Thus, changes in myosin levels are determined solely by ring-directed cortical flow along the direction perpendicular to the ring, which can be solved as a one-

dimensional problem. We assume that the cortical compression rate (between  $x$  and  $x + dx$ ) is proportional to local myosin concentration,  $m(x, t)$ , which exerts stress onto the actin network resulting in

$$\frac{\delta \varepsilon}{\delta t}(x, t) = -\alpha m(x, t), \quad (18)$$

where  $\varepsilon$  is the cortical strain (i.e. change in length of cortical surface per unit length) and  $\alpha$  is a proportionality constant that reflects the ability of the cortex to be compressed by ring myosin. The velocity of cortical surface movement is obtained from the following relationship (see also equation (12)).

$$v(x, t) = \int_0^x \frac{\delta \varepsilon}{\delta t}(x', t) dx'. \quad (19)$$

The conservation of mass for myosin flow results in the following

$$\frac{\partial m}{\partial t}(x, t) = -\frac{\partial}{\partial x}(m(x, t)v(x, t)) = \frac{\partial}{\partial x}(m(x, t) \int_0^x \alpha m(x', t) dx'). \quad (20)$$

If we integrate equation (20) over  $x$  on  $(-w, w)$  domain we obtain

$$dM_{ring}(t)/dt = \alpha m_{cort} M_{ring}(t), \quad (21)$$

where  $M_{ring}(t) := \int_{-w}^w m(x, t) dx$  is the total per unit length amount of engaged ring myosin,  $2w$  is the width of the contractile ring/active zone where myosin is engaged and compressing cortex and  $m_{cort} := m(w, t)$  is the concentration of myosin on the cortex delivered into the contractile ring. The velocity of ring-directed cortical flow is

$$v_{flow}(t) = \alpha M_{ring}(t)/2, \quad (22)$$

The one half is included to account for the fact that flow comes in from both sides. The solution of equation (21) is

$$M_{ring}(t) = M_{0\ ring} e^{t/\tau}, \quad (23)$$

where we define the characteristic time of myosin accumulation,  $\tau$ , as  $\frac{1}{\alpha m_{cort}}$ . Note that the total amount of myosin in the ring will be the amount of engaged myosin plus an added baseline that would include any myosin not involved in compression (see equation (5)). We assume the rate of ring shrinkage is proportional to the amount of ring myosin, as observed in our data,



$$\frac{1}{R} \frac{dR}{dt} = -\beta M_{ring}(t), \quad (24)$$

where  $\beta$  is a proportionality coefficient that reflects the ability of the ring to be constricted by ring myosin. Using equations (23) and (24), we obtain the dynamics of contractile ring size over time

$$\bar{R}(t) = \bar{R}_{ini} e^{-\beta \tau M_{0 ring} \exp(t/\tau)}, \quad (25)$$

where  $\bar{R}_{ini}$  is the dimensionless characteristic size of the ring; essentially the radius at minus infinity if the same exponential process controlling contractile ring assembly extended back in time infinitely. Instead, *in vivo* cytokinesis initiates when spindle-based signaling activates RhoA on the equatorial cortex leading to the abrupt recruitment of contractile ring components. If the time frame of reference is chosen so that  $t = 0$  is cytokinesis onset immediately following the initial patterning of the cortex by RhoA,  $M_{0 ring}$  is the amount of ring myosin immediately following this event and the initial size of the ring is

$$\bar{R}_0(t) = \bar{R}_{ini} e^{-\beta \tau M_{0 ring} t}. \quad (26)$$

To compare our model with data we use the time frame of reference where  $t = 0$  is the point of 50% closure (i.e.  $\bar{R}(t = 0) = \frac{1}{2}$ ). In this reference,  $M_{0 ring} = \frac{\ln(\bar{R}_{ini})}{\beta \tau}$ , and by defining dimensionless velocity as  $\bar{v} := \tau v$ , we obtain equations (4-8). Note that equation (4) can be rewritten in the following way

$$\bar{R}(\bar{t}) = \bar{R}_{ini} e^{-\frac{1}{\bar{R}} \frac{d\bar{R}}{d\bar{t}}}, \quad (27)$$

where  $\bar{t} := t/\tau$ . This relationship implies that in this dimensionless time, where  $\bar{R}(\bar{t} = 0) = \frac{1}{2}$ , any two rings of the same size have the same dimensionless constriction rate.

### **Data availability**

All data is available from the authors upon request.

### **Code availability**

The custom computer code used in this study is freely available from the authors upon request.

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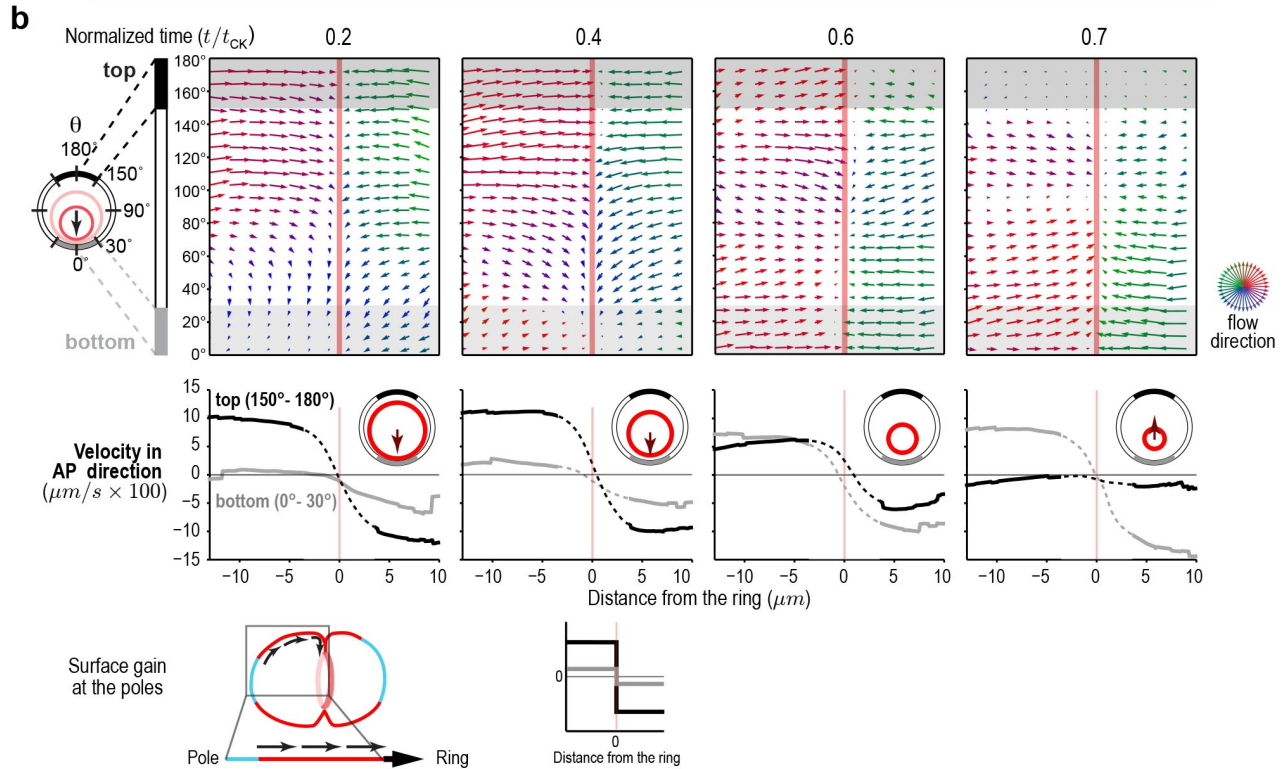
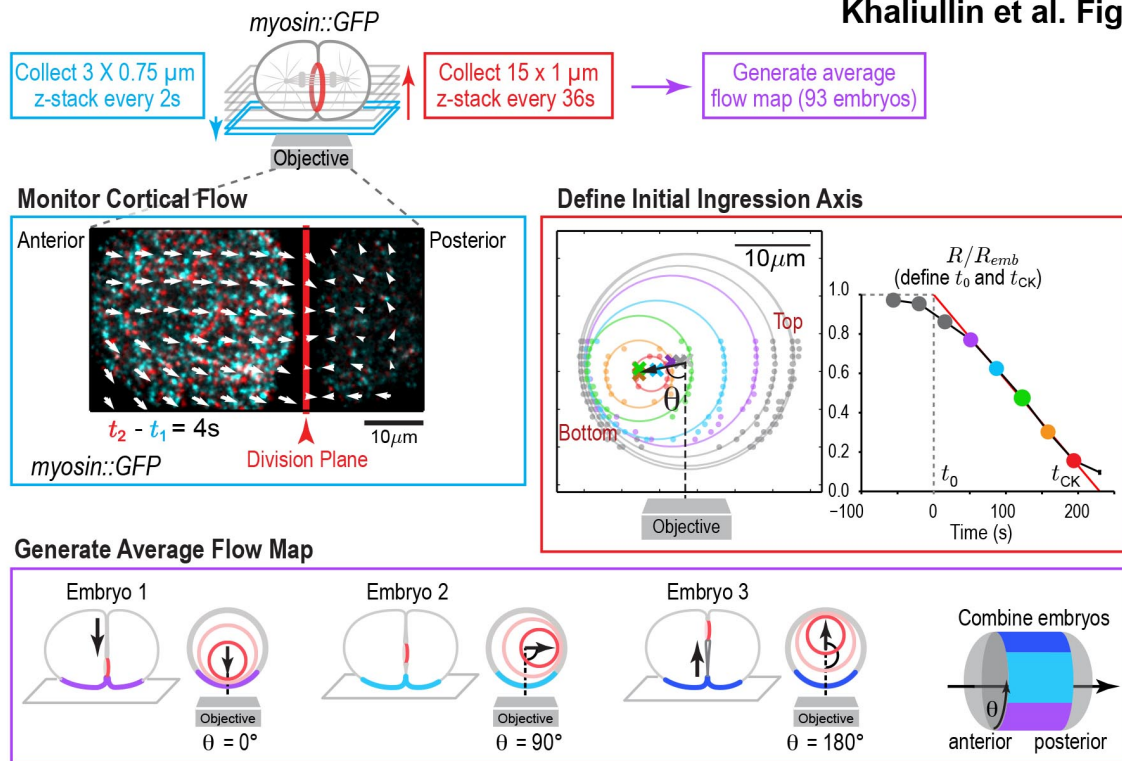
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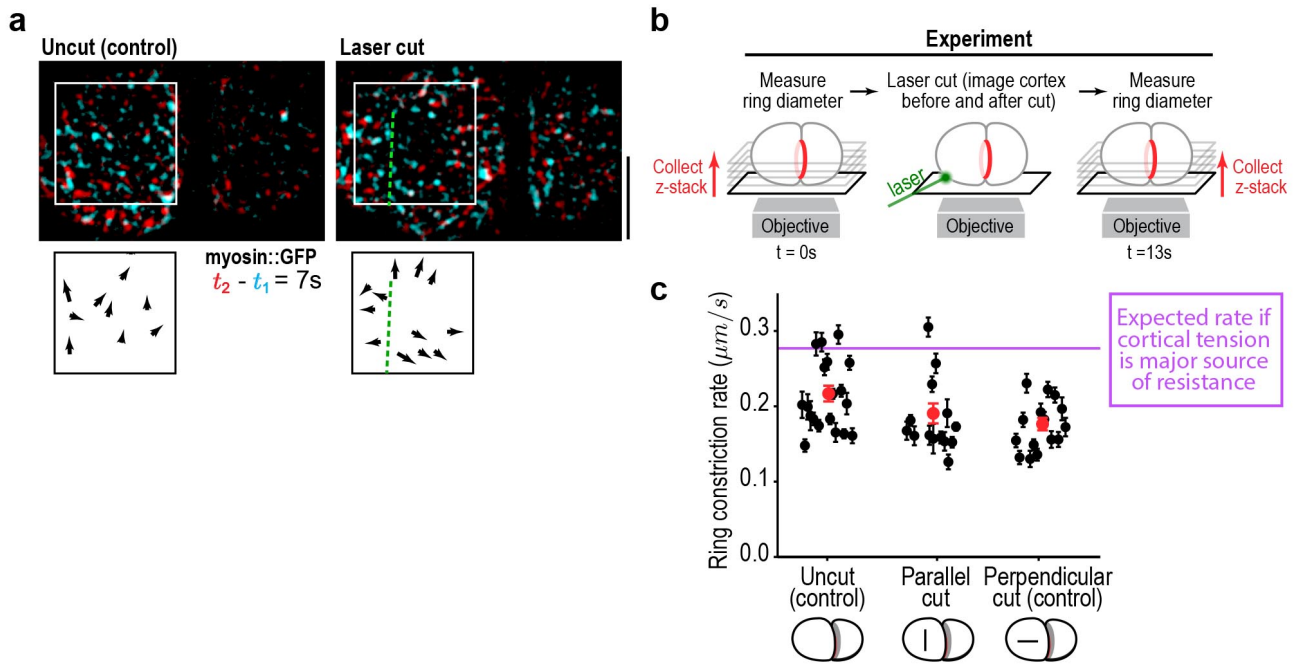
## FIGURES AND FIGURE LEGENDS

**a** Khaliullin et al. Figure 1



**Figure 1. An average cortical flow map reveals that surface gain occurs at the cell poles. (a) (top)** Schematic of the experimental procedure. *(middle, left)* Superposition of images of the cortex acquired 4s apart. Arrows indicate cortical flow (magnified 2.5X). *(middle, right)* The initial ingression axis,  $t_0$ , and  $t_{CK}$  were defined as shown for a representative embryo. The angle  $\theta$  specifies the position of the imaged cortex relative to the initial ingression axis. Image and quantification are representative of the 93 imaged embryos. *(bottom)* Angular position was used to combine data from 93 embryos to generate an average flow map. **(b) (top)** Average flow at the indicated timepoints. Arrows show direction and magnitude of the displacement in 2s (magnified 20X). *(middle)* Graphs are average velocity in the A-P direction versus position along the A-P axis for the cortex on the top (*black*) and bottom (*grey*) of the embryo (*shaded in flow maps*). Surface movement changes direction across the division plane, the apparent velocity gradient close to the division plane is a projection artifact due to surface curvature (dotted regions on velocity curves). *(bottom)* Schematics show a one-dimensional representation and expected cortical velocity plot for surface gain at the poles.

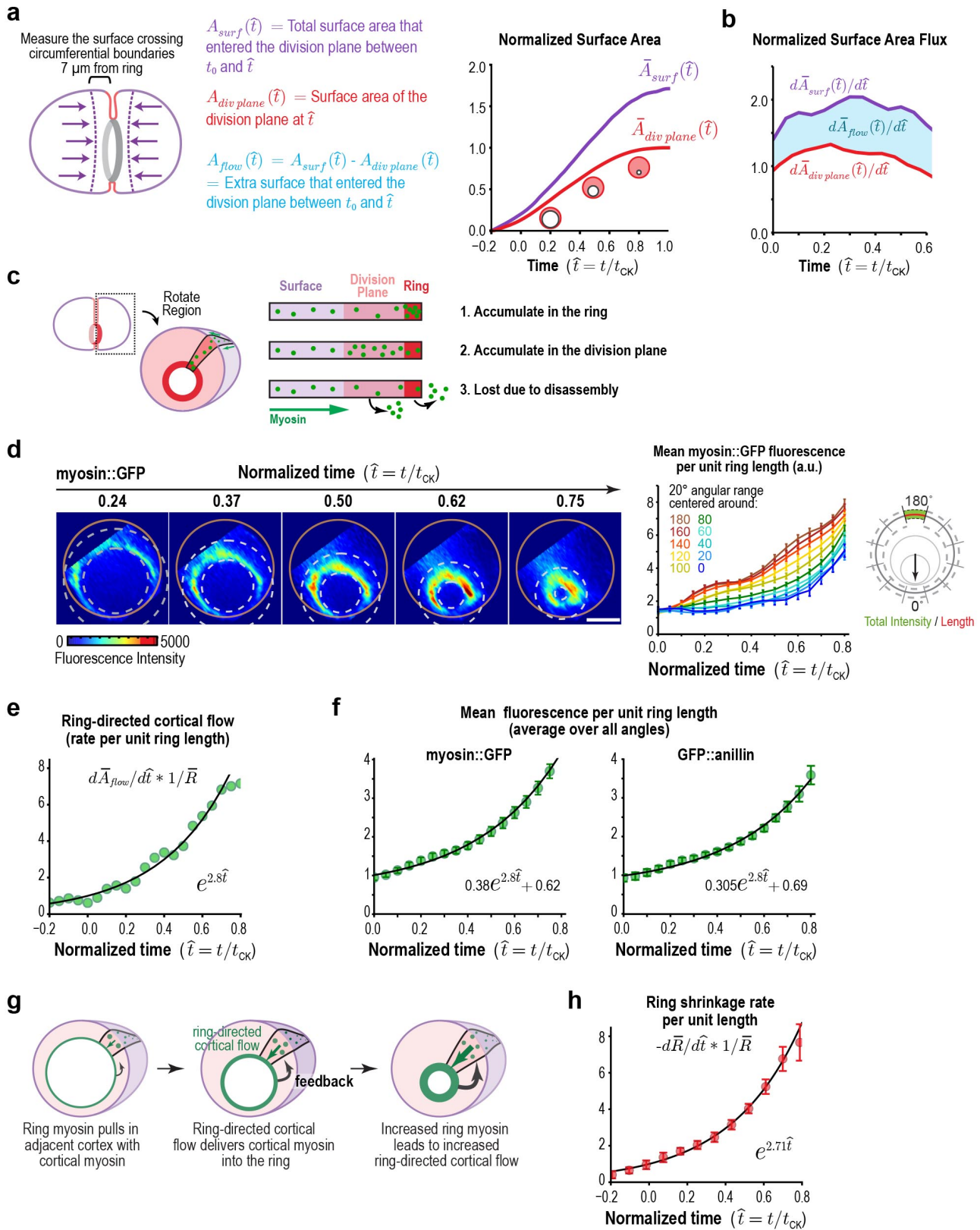
## Khaliullin et al. Figure 2



**Figure 2. Cortical tension does not limit the rate of ring closure.** (a) The success of cortical cuts was assessed by comparing surface images of cortical myosin before (cyan) and after (red) the cut to monitor the movement of myosin foci away from the cut site. Representative images from 1 out of 48 embryos imaged are shown. Scale bar is 10  $\mu\text{m}$ . (b) Schematic of laser ablation experiment to determine if cortical resistance limits the rate of contractile ring closure. Contractile ring sizes were measured from z-stacks acquired before and after a cut was made across the cortex with a laser. (c) Graph plots the rates of ring closure derived from before and after ring size measurements for uncut controls (n=19 embryos) and embryos with cuts perpendicular (n=15 embryos) or parallel (n=14 embryos) to the ring. Black symbols are single embryo measurements with measurement errors. Red symbols are the means; error bars are the SEM. The purple line marks expected closure rate if cortical tension is a major source of resistance. Scale bars are 10  $\mu\text{m}$ .

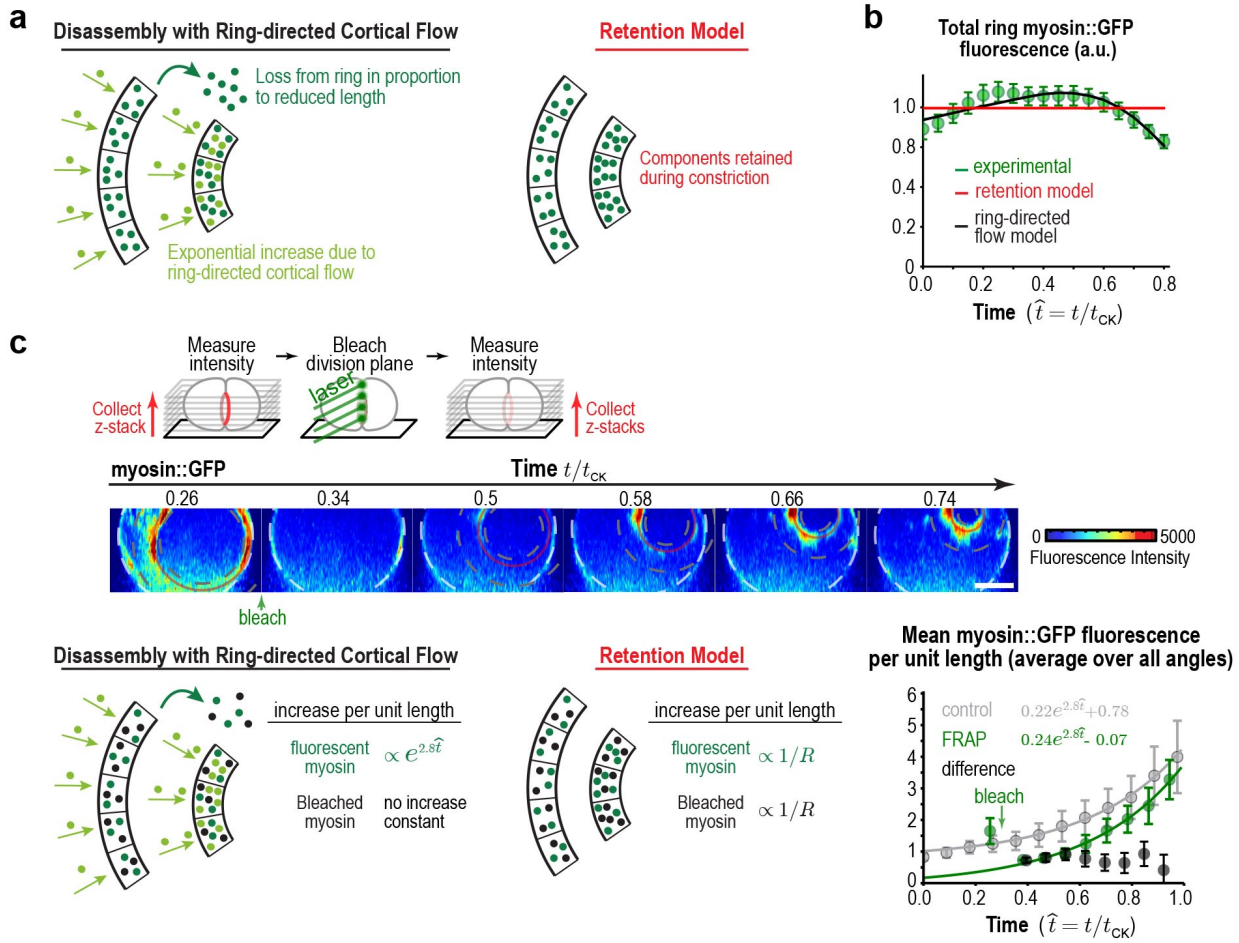


### Khaliullin et al. Figure 3



**Figure 3. Cortical surface is compressed into the contractile ring during constriction leading to an exponential increase in the amount of ring components and in the rates of cortical flow and ring constriction.** (a) Plot comparing the area of the forming division plane (*red*) with the total cortical surface area that entered the division plane from the start of cytokinesis (*purple*; calculated as indicated in the schematic). (b) Plot comparing the rate of cortical flow into the division plane (*purple*) with the rate of division plane growth (*red*). (c) Possible fates for extra cortical surface delivered to the division plane. (d) (*left*) Images of the division plane reconstructed from 40-plane z-stacks. Gold circles mark the embryo boundary and dashed circles mark the boundaries used for ring intensity measurements. (*right*) Graph plots per unit length myosin::GFP fluorescence for the indicated angular ranges (n=36 embryos). Image series is representative of 36 imaged embryos. (e,f) Graphs plot per unit length rate of ring-directed cortical flow (n=93 embryos) and mean per unit length myosin::GFP (n=36 embryos) or GFP::anillin (n=26 embryos) fluorescence (n=36 embryos). (g) Schematic illustrating the proposed feedback loop that drives the parallel exponential increases in ring myosin and in the rates of cortical flow and constriction. (e) Graph plots the per unit length rate of ring closure. Black lines are fitted single exponentials. Error bars are the SEM.

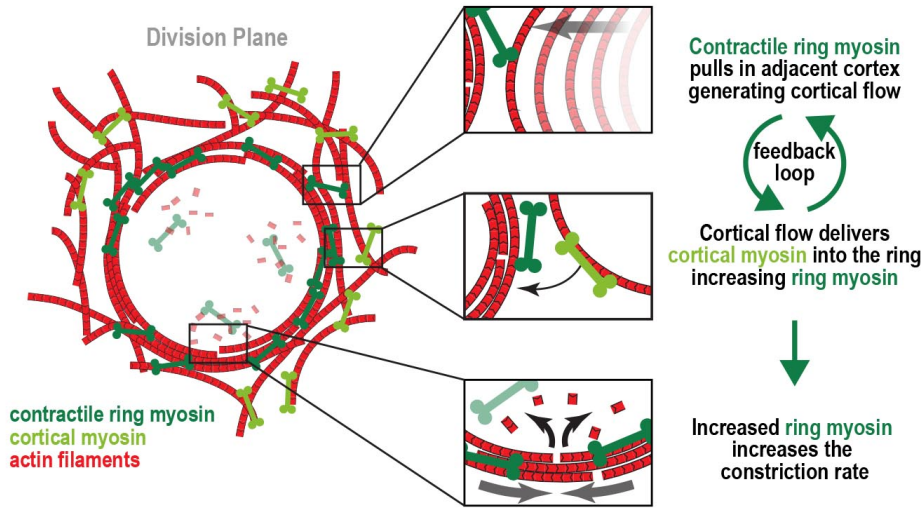
Khaliullin et al. Figure 4



**Figure 4. Recovery of myosin::GFP fluorescence after division plane bleaching supports delivery of myosin into the ring by ring-directed cortical flow.** (a) (*left*) Two models that could explain the increase in the per unit length amount of myosin during constriction. (b) Graph plotting mean total ring fluorescence (average over all angles; *green*) for myosin::GFP with the predictions for the ring-directed cortical flow (*black*) and the retention (*red*) models (n= 36 embryos). Error bars are the SEM. (c) (*top*) Schematic of the photobleaching experiment to discriminate between the two models. (*middle*) Images of the division plane reconstructed from 30x1 $\mu$ m z-stacks of an embryo expressing myosin::GFP whose division plane was bleached at  $t/t_{CK} \sim 0.3$ . Red circle marks the contractile ring and dashed circles mark the boundaries used for ring intensity measurements. (*bottom left*) Schematics illustrate the expected concentration changes for fluorescent and bleached myosin::GFP. (*bottom right*) Graph plotting the mean per unit length amounts of fluorescent myosin::GFP in the ring for controls (*grey*, n=24 embryos) and after bleaching (*green*, n=8 embryos). The amount of bleached myosin::GFP in the ring (*black*), calculated as the difference between the control and FRAP curves is also shown. Continuous lines are exponential fits to the data. Error bars for controls and FRAP are SD and error bars for the difference are SEM. Scale bar is 10  $\mu$ m. Image series in (c) is representative of 8 imaged embryos.

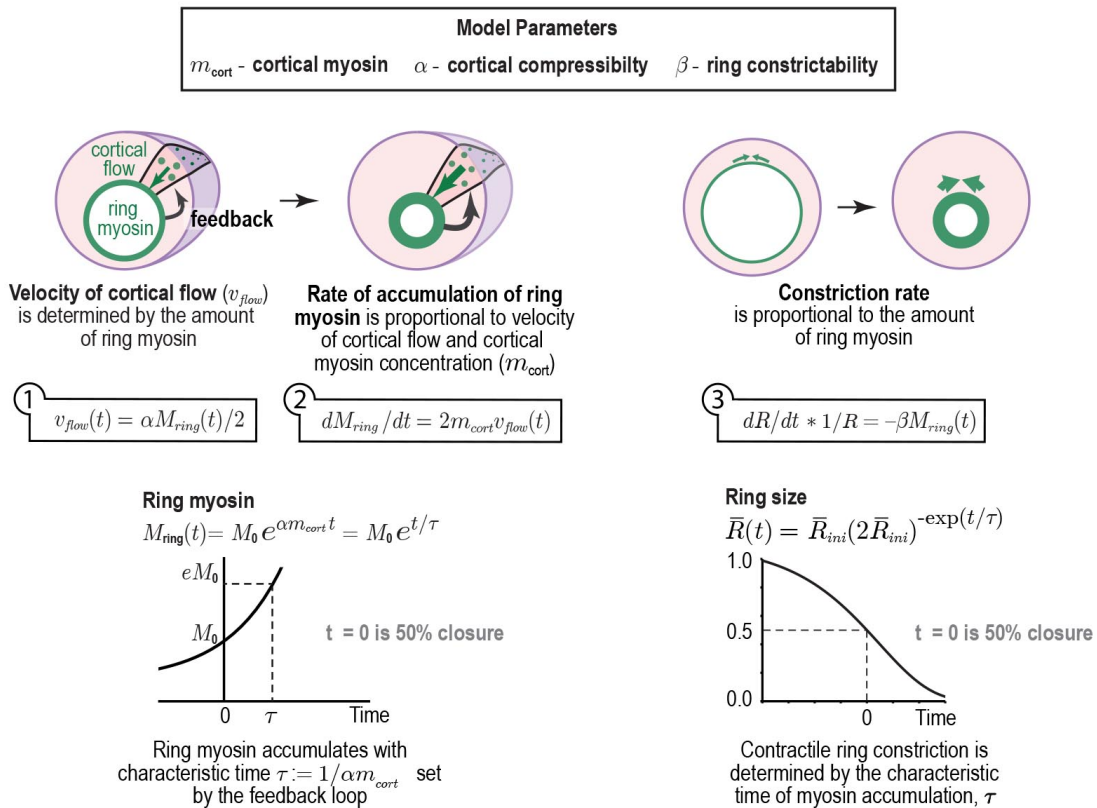
## Khaliullin et al. Figure 5

a



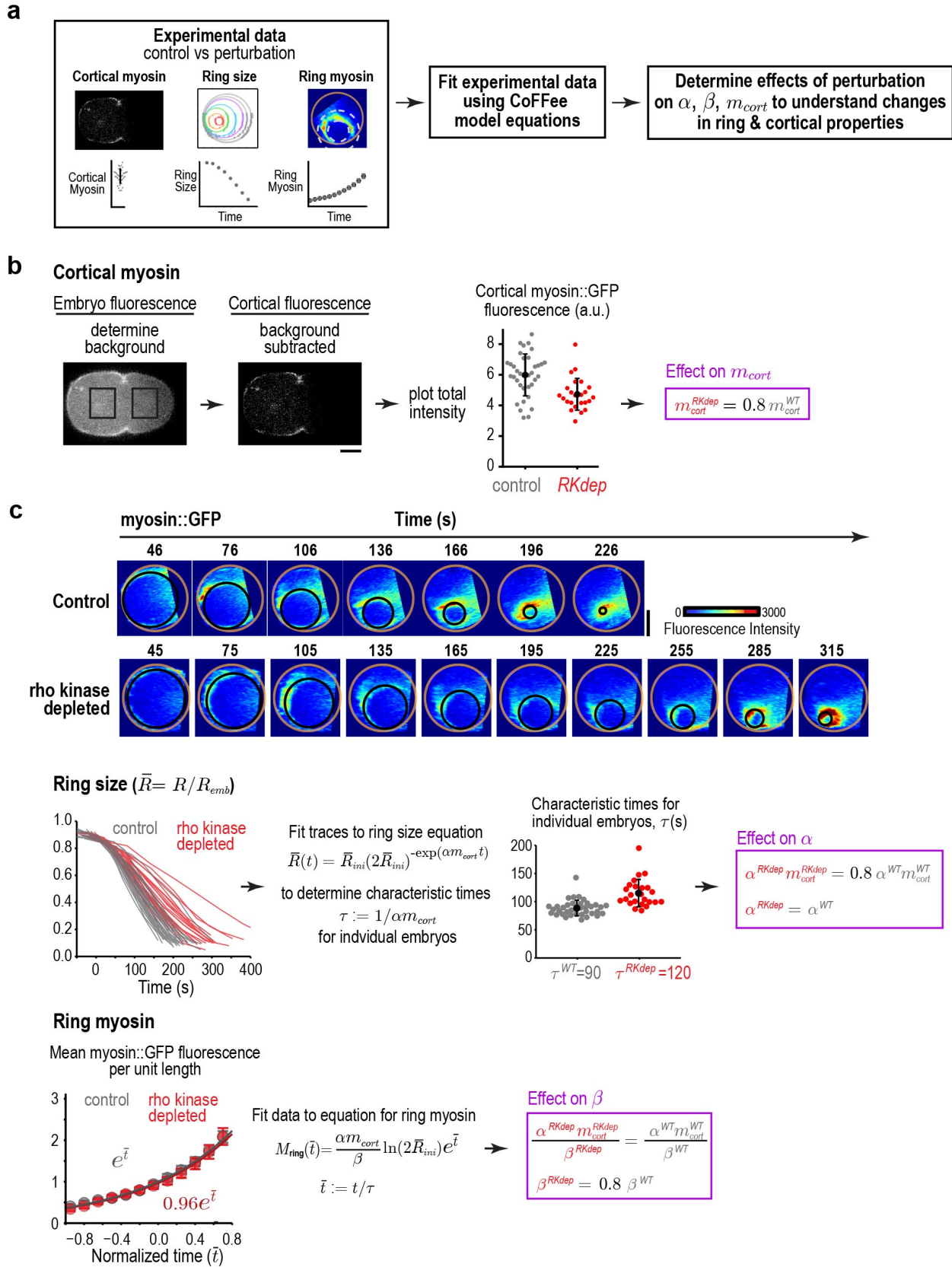
b

### Cortical Flow Feedback (CoFFee) model



**Figure 5. Cortical Flow Feedback (CoFFee) model of cytokinesis.** (a) Schematic model incorporating the conclusions arising from our experimental analysis and proposed underlying molecular mechanism. (b) Formulation of the proposed mechanisms as an analytical mathematical model consisting of three equations and three model parameters that reflect properties of the cortex and ring. (*left*) Equations (1) and (2) describe the feedback loop between the amount of ring myosin and the velocity of cortical flow that leads to the exponential increases in the amount of ring myosin and the velocity of cortical flow. (*right*) Equation (3) describes the coupling of ring constriction to the amount of ring myosin.

Khaliullin et al. Figure 6



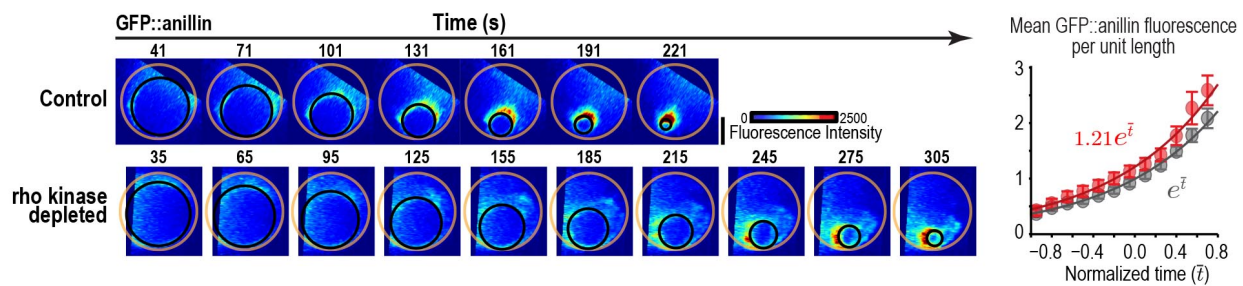
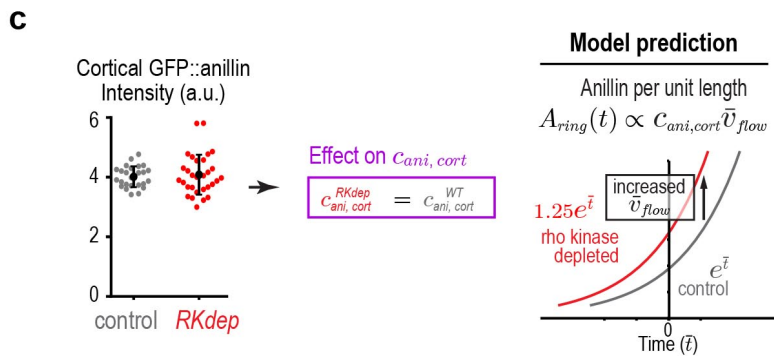
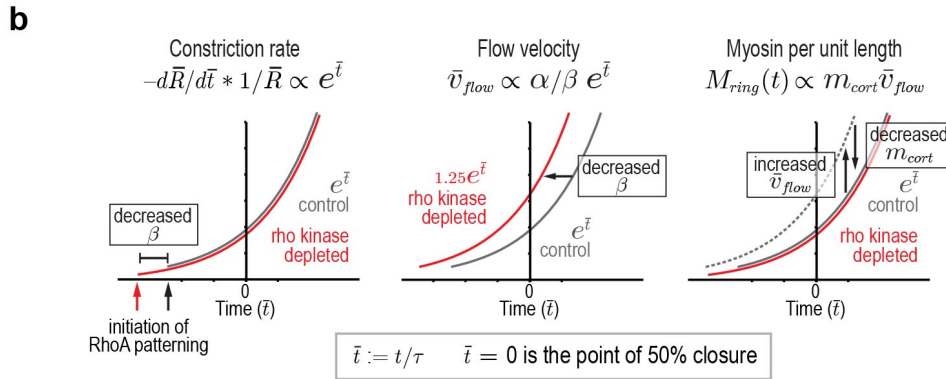
**Figure 6. Fitting experimental data using the CoFFee model equations reveals the effects of rho kinase inhibition on cortical and contractile ring properties.** (a) Flow chart illustrating how the CoFFee model can be used to fit experimental data to determine the effects of molecular perturbations on ring and cortical properties. (b) (*left*) images illustrating the method used to directly measure cortical myosin::GFP fluorescence. (*right*) Graph plotting cortical myosin::GFP fluorescence in control (*grey*, n=36) and rho kinase depleted (*red*, n=24) embryos. (c) (*top*) Images of the division plane in control and rho kinase depleted embryos expressing myosin::GFP. Gold circles mark the embryo boundaries and black circles mark the contractile ring. Image series shown are representative of the imaged embryos. Scale bar is 10  $\mu\text{m}$ . (*middle, left*) Graphs of ring size traces for individual control (*grey*, n=36) and rho kinase depleted (*red*; n=24) embryos. (*middle, center*). Characteristic times,  $\tau$ , for individual control (*grey*) and rho kinase depleted (*red*) embryos are plotted along with the mean and SD for each condition (*black*). (*bottom*) Graph plots mean myosin::GFP fluorescence per unit length (averaged over all angles with baseline subtraction) for control (*grey*) and rho kinase depleted (*red*) embryos. Error bars are SEM.



## Khaliullin et al. Figure 7

### a Effects of rho kinase depletion (from myosin::GFP data)

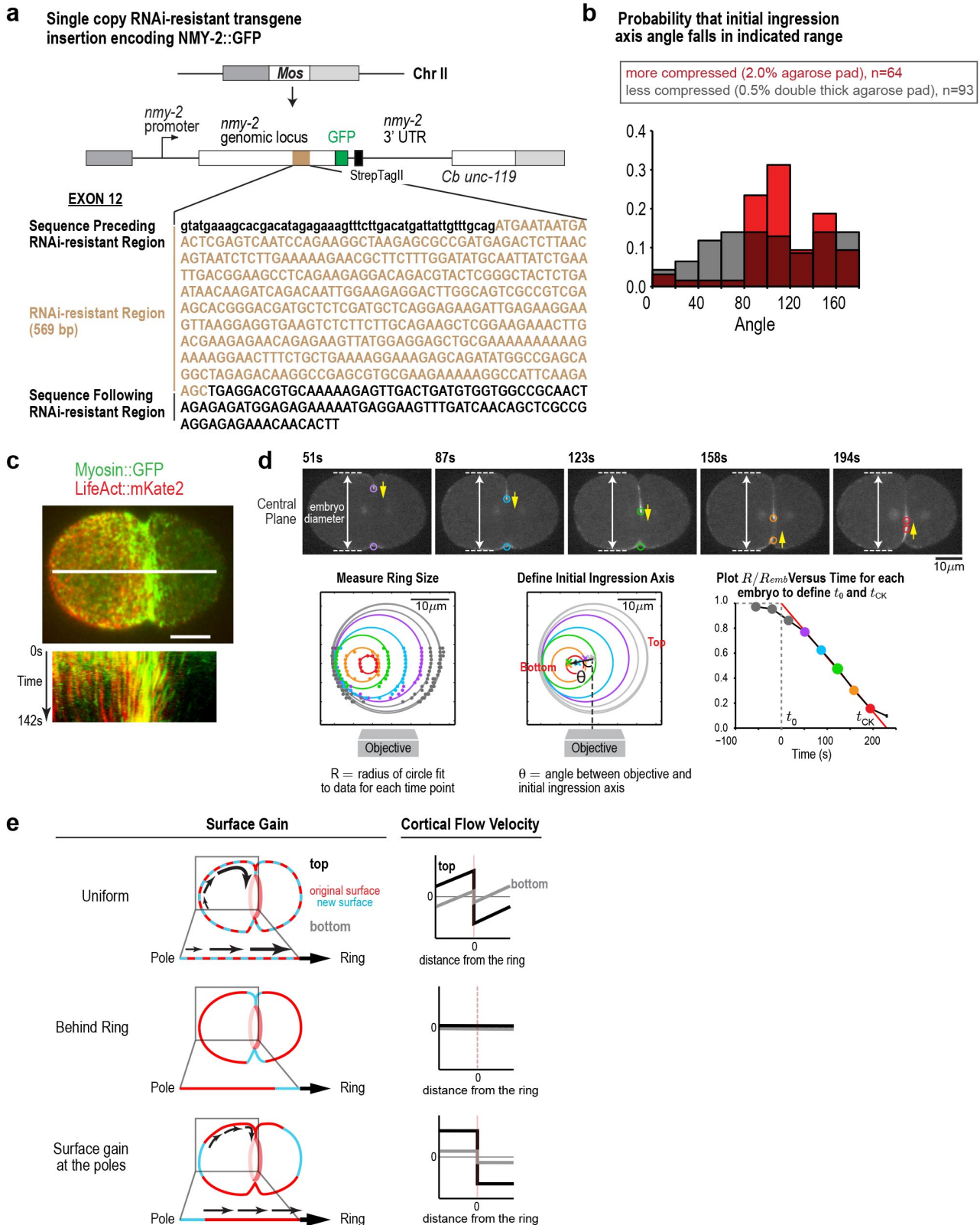
mechanical property	model parameter	value relative to wild type
cortical compressibility	$\alpha$	WT
cortical myosin	$m_{cort}$	0.8 WT
ring constrictability	$\beta$	0.8 WT



**Figure 7. Reducing myosin activation by inhibition of rho kinase reduces the ability of the ring to be constricted by ring myosin.** (a) (*top*) Table summarizing the effects of rho kinase depletion on model parameters. (*bottom*) Schematics summarizing the effects of rho kinase inhibition in the reference frame where time is normalized by dividing by  $\tau$  and  $\bar{t} = 0$  is 50% closure. In this time reference, comparing component levels and flow velocity at the same  $\bar{t}$  corresponds to comparing them for the same ring size. (b) (*top, left*) Graph plotting cortical GFP::anillin fluorescence in control (n=25) and rho kinase depleted (n=30) embryos. (*top, right*) Since the concentration of cortical anillin is not changed, the increased cortical flow in rho kinase depleted embryos is expected to lead to a 1.25-fold increase in the per unit length amount of anillin for rings of all sizes. (*bottom, left*) Images of the division plane in representative control and rho kinase depleted embryos expressing GFP::anillin. Gold circles mark the embryo boundaries and black circles mark the contractile ring. (*bottom, right*) Data for mean GFP::anillin fluorescence per unit length (averaged over all angles with baseline subtraction) for control (*grey*) and rho kinase depleted (*red*) embryos reveals that ring anillin levels are increased 1.21-fold.

SUPPLEMENTARY FIGURES AND SUPPLEMENTARY FIGURE LEGENDS

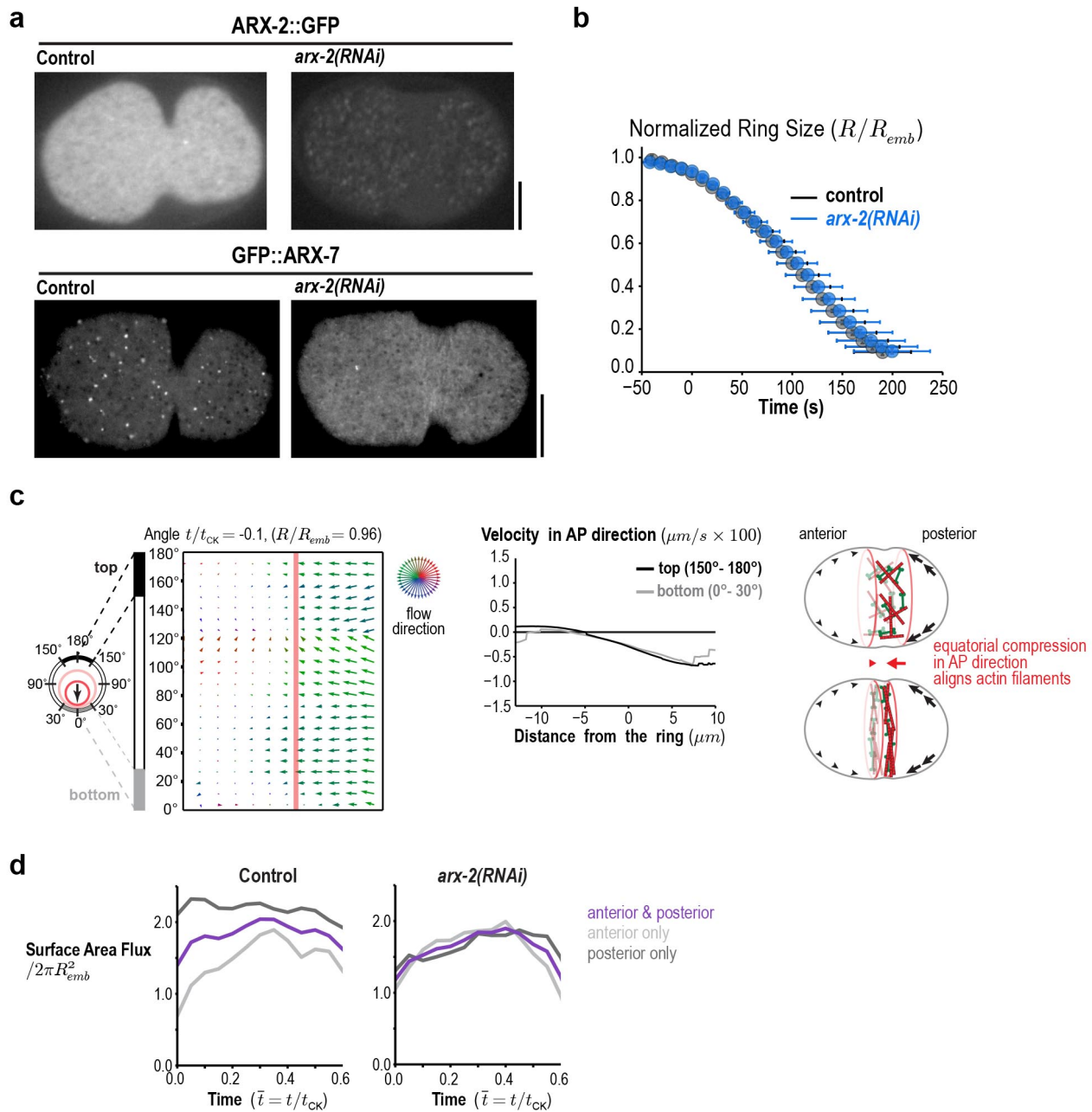
Khaliullin et al. Supplementary Figure 1



Supplementary Figure 1. Analysis of cortical flow during the first cytokinesis of the *C. elegans* embryo reveals that surface is gained at the cell poles. (a) Schematic of the single-copy *nmy-2::gfp*

transgene. Cb *unc-119*, the *unc-119* coding region from the related nematode *C. briggsae*, was used as a transformation marker. The transgene was re-encoded while maintaining amino acid sequence in the indicated region to render it resistant to RNAi targeting the endogenous gene for other experiments, we did not use this feature in the experiments reported here. **(b)** Graph plotting the probability that the angle between the objective axis and the initial ingression axis falls in the indicated range for embryos mounted with more (*red*) or less (*grey*) compression. **(c)** Image of actin and myosin moving together on the cortical surface of the embryo. The white line in the center of the image (*top*) indicates the region used for the kymograph (*bottom*). Image is representative of 5 imaged embryos. **(d)** (*top*) Central plane images from the embryo analyzed in Figure 1a. Panels on the lower left and lower right are reproduced from Figure 1a for comparison. An automated algorithm was used to identify the edges of the embryo (dashed lines) and the position of the contractile ring (colored circles) in each z-plane. Yellow arrows mark the direction of furrow ingression and illustrate how the furrow initially ingresses from the top and then changes directions to ingress from the bottom during the second half of cytokinesis. (*lower left*) Points marking contractile ring position in the z-planes were projected onto an end-on view of the division plane. Data for different timepoints in this representative embryo are shown in colors corresponding to the circles in the central plane images. Ring sizes were measured by fitting circles to the data. (*middle*) The initial axis of contractile ring closure was defined by the angle  $\theta$  between the objective axis and a line fit through the centers of the contractile rings with a normalized size  $> 0.3$ . (*right*) = A plot of normalized ring size versus time for this embryo defines  $t_0$  and  $t_{CK}$  as the times when a line fit through the points corresponding to ring sizes between 0.3 and 0.8 crossed 1 and 0, respectively. **(e)** Different profiles of cortical surface velocity along the A-P axis are predicted for different spatial patterns of surface gain. (*top row*) For surface gain behind the ring, no cortical movement is predicted on the embryo surface. (*middle row*) For uniform surface gain, a gradient of velocities will be observed, where the cortex immediately behind the ring moves at the speed of the ingressing furrow, and cortical velocity decreases linearly towards the cell poles. (*bottom row*) Reproduced from Figure 1b for comparison. If surface is gained only at the poles, cortical velocity will be constant in magnitude within the flow map region with opposite direction on the two sides of the embryo. Scale bars are  $10\mu\text{m}$ .

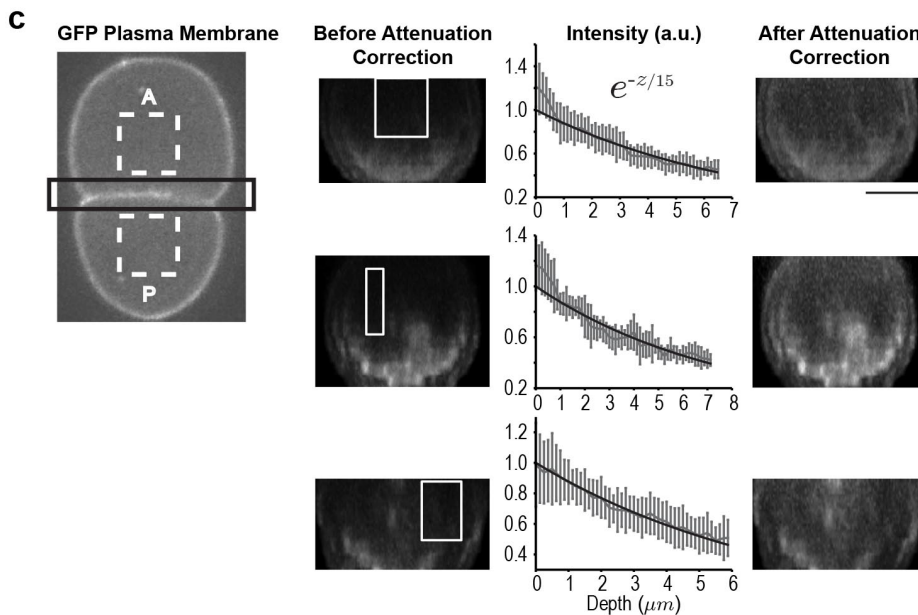
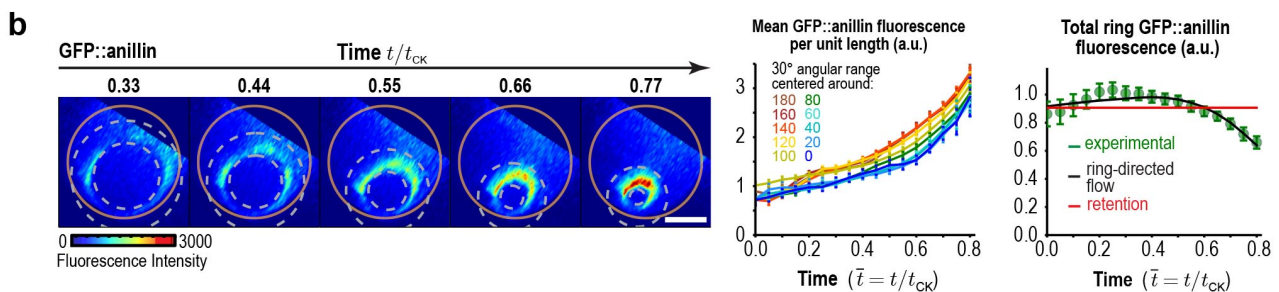
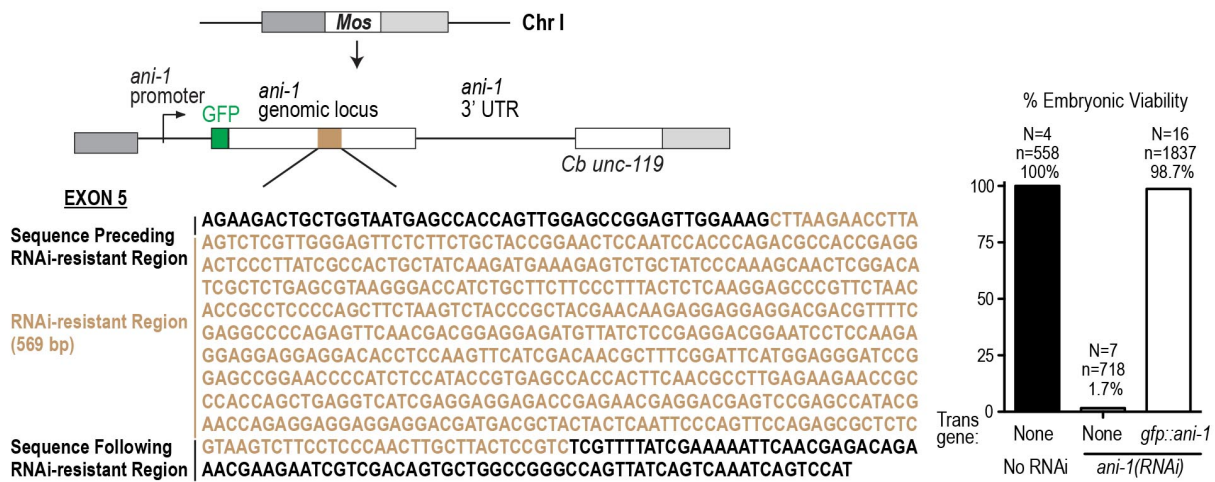
## Khaliullin et al. Supplementary Figure 2



**Supplementary Figure 2. Compression of the equatorial cortex along the A-P direction during ring formation.** (a) Images of cortical ARX-2::GFP (*top*) and GFP::ARX-7 (*bottom*) in control and *arx-2(RNAi)* embryos confirm loss of cortical Arp2/3 complex (images are representative of 10 imaged embryos for each condition in the GFP::ARX-7 strain and 15 for control and 13 for *arx-2(RNAi)* in the ARX-2::GFP strain). Scale bars are 10 $\mu$ m. (b) Graph of average contractile ring size versus time for control (grey) and *arx-2(RNAi)* (blue) embryos expressing myosin::GFP (n= 93 embryos for control and 68 embryos for *arx-2(RNAi)*). Error bars are standard deviation. (c) (*left*) Average flow map at ( $t/t_{CK}=-0.1$ ) immediately after RhoA-based signaling has recruited myosin and other contractile ring components to the equatorial cortex (n= 93 embryos). (*middle*) The surface velocity profile reveals a velocity gradient that spans the cell equator (-5 to +5  $\mu$ m), indicating a zone of cortical compression. (*right*) Schematic depicting how polar expansion in response to tension generated by the forming ring contributes to equatorial filament alignment during ring assembly. (d) The same procedure employed for control embryos (Fig. 1) was used to analyze 68 randomly oriented *arx-2(RNAi)* embryos. Graphs plot the rate of cortical flux across the anterior (*light grey*) and posterior (*dark grey*) boundaries (see schematic in Fig. 3a) versus the mean for the two sides (*purple*) for control and *arx-2(RNAi)* embryos.

### Khaliullin et al. Supplementary Figure 3

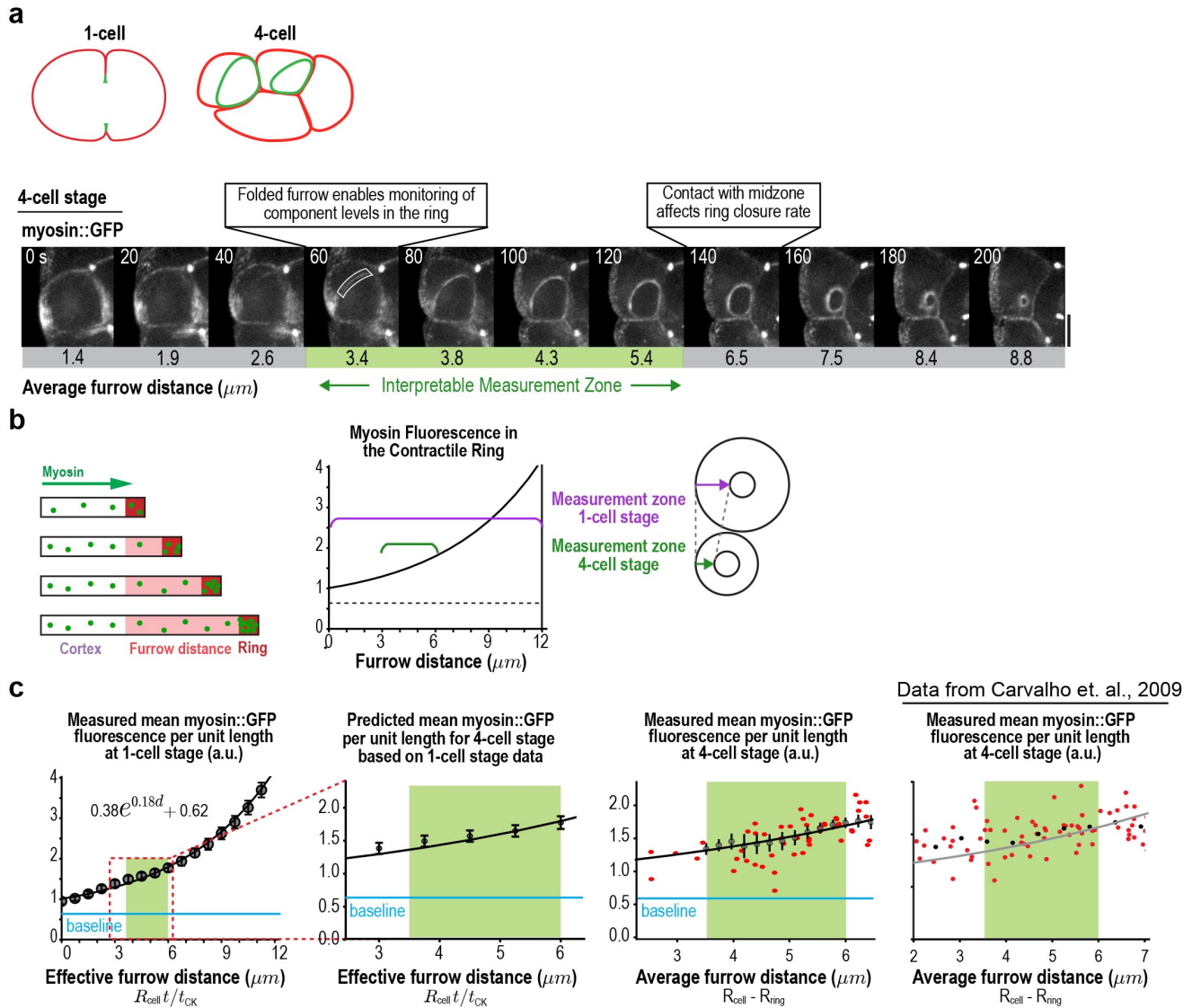
#### a Single copy RNAi-resistant transgene insertion encoding GFP::ANI-1



**Supplementary Figure 3. Correcting for signal attenuation with sample depth.** (a) (*left*) Schematic of the single-copy *gfp::ani-1* transgene. The transgene was re-encoded while maintaining amino acid sequence in the indicated region to render it resistant to RNAi targeting of the endogenous *ani-1* gene to allow testing of the functionality of the GFP::ANI-1 fusion. (*right*) Graph plotting embryonic lethality demonstrates functionality of the *gfp::ani-1* transgene. (b) (*left*) Images of the division plane in an embryo expressing GFP::anillin. (*center*) Graph plots GFP::anillin fluorescence per unit length of the ring for the indicated angular ranges. (*right*) Graph plotting mean total ring fluorescence (average for all angles; *green*) for GFP::anillin (n=26 embryos). The predictions for ring-directed cortical flow (*black*) and the retention (*red*) model are also shown. Error bars are the SEM. (c) Fluorescence attenuation with embryo depth was estimated from fluorescence intensity measurements made at the cell-cell boundary of the 2-cell embryos expressing a GFP-tagged plasma membrane marker. Cell-cell boundaries were reconstructed from 40 plane z-stacks. The intensity profile at each slice was calculated by subtracting the average background intensity estimated from dashed rectangles (*left*) from the cell-cell boundary region (*black rectangle*) at each slice and calculating the maximum intensity projection along AP axis. The effect of depth on signal was calculated from the reconstructed division planes by plotting the mean signal as a function of depth in 10 rectangular regions (*white boxes*) where the signal was expected to be uniform; three examples are shown here. All intensity profiles were simultaneously fitted using a single exponential. Error bars are the SD. On the right, the same cell-cell boundaries are shown after correction for depth attenuation. The scale bar is 10  $\mu\text{m}$ . Image series in (b) is a representative series of 26 imaged embryos.



## Khaliullin et al. Supplementary Figure 4

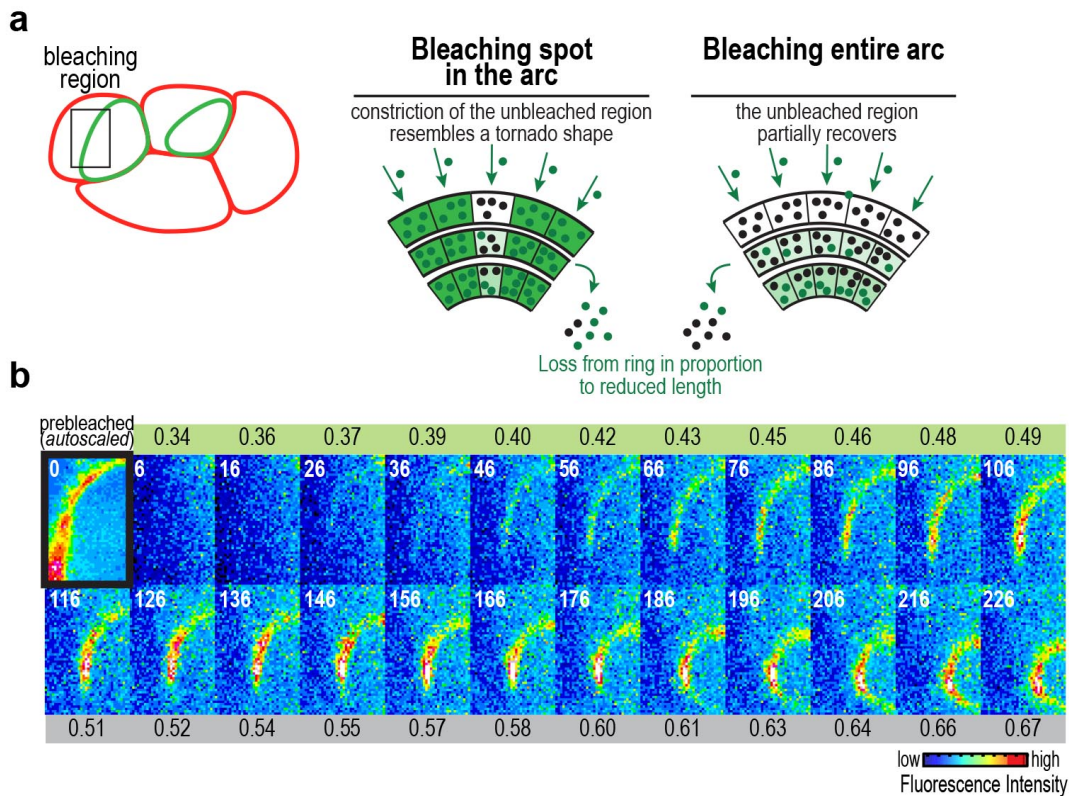


**Supplementary Figure 4. Ring component levels in 4-cell stage embryos are consistent with accumulation due to ring-directed cortical flow.** (a) At the 4-cell stage, cells often divide perpendicular to the imaging plane, providing an “end-on” view of the constricting ring relative to the imaging plane. However, a disadvantage of this division is that  $\sim 2/3$  of the ring runs along sides of the cell in contact with neighboring cells and cannot be used for measurements. To be able to monitor component dynamics in the entire ring over a larger range of ingression distances, we therefore developed the quantitative tools described in this manuscript to monitor ring constriction at the 1-cell stage. (top) Schematic illustrating the relative geometries of cytokinesis in 1- and 4-cell stage *C. elegans* embryos. (bottom) images of the division plane in a representative dividing cell at the 4-cell stage

reconstructed from 16x1 $\mu$ m z-stacks of an embryo expressing myosin::GFP (n=16 embryos imaged). **(b)** Our 1-cell stage analysis indicates that myosin levels in the ring increase exponentially as a function of furrow distance. The schematics show myosin::GFP fluorescence in the ring as a function of furrow ingression distance at the 1-cell stage, and the predicted change as the furrow ingresses through the interpretable measurement zone at the 4-cell stage if ring myosin accumulates via the same mechanism. Detecting an exponential increase at the 4-cell stage is significantly more difficult than at the 1-cell stage because the cells are smaller and the distance that the furrow ingresses between its formation and when it contacts the spindle midzone, which slows furrowing<sup>17</sup>, is about one quarter of what it is at the 1-cell stage (*Measurement zones*). **(c)** In comparing the 1- and 4-cell stage data, we took advantage of the fact that the initial per unit length constriction rates are the same at the two stages<sup>17</sup>. This makes it possible to predict the pattern of myosin accumulation that we would expect at the 4-cell stage if ring myosin accumulates via the same mechanism that it does at the 1-cell stage, and compare it with measured values from the 4-cell stage. (*left panel*) One complication is that, while our 1-cell stage data show that myosin levels increase exponentially as a function of furrow distance, they also suggest there is a baseline of fluorescence (*cyan*) whose precise nature we do not understand—we postulate this baseline could correspond to myosin associated with the plasma membrane but not the cortex. This baseline signal is not part of the exponentially increasing population but influences the measured fold increase in total ring fluorescence. Curve fitting of the 1-cell stage data indicates that the exponentially increasing population increases ~9 fold as the furrow ingresses 12  $\mu$ m; however, because of the baseline, the measured increase relative to initial ring fluorescence is only ~5-fold. (*middle and right panels*) At the 4-cell stage we can only measure ring component levels for furrow ingression distances between ~3 and 6  $\mu$ m. The 1-cell data predicts that the exponentially increasing population, which is approximately equal to the baseline at 3  $\mu$ m, and would increase 1.7 fold by 6  $\mu$ m, resulting in a 1.37-fold increase in total per unit length fluorescence. Fitting both new 4-cell data acquired with the *in situ* tagged myosin::GFP strain that we employed for the 1-cell analysis (*third panel*; n=14 embryos) and re-plotting our old data acquired using a myosin::GFP transgene (obtained from<sup>17</sup>; *right panel*) revealed excellent agreement with the predicted curve (*grey line*). We conclude that data from 4-cell stage embryos are consistent with an

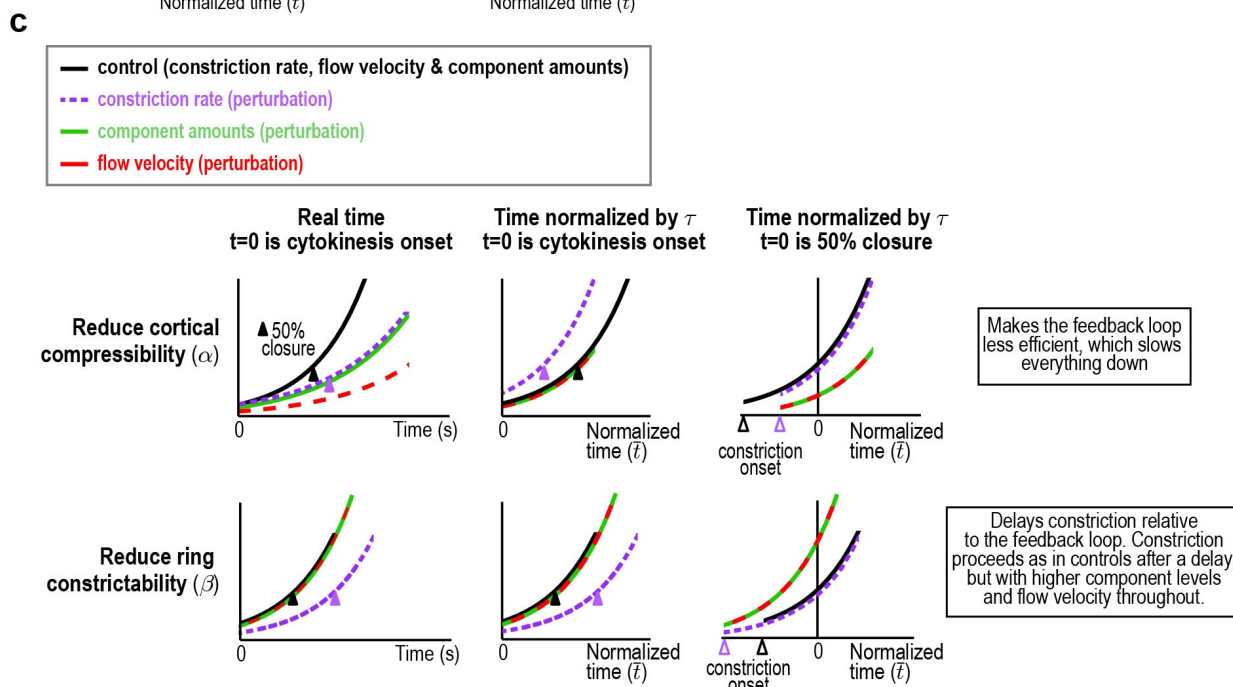
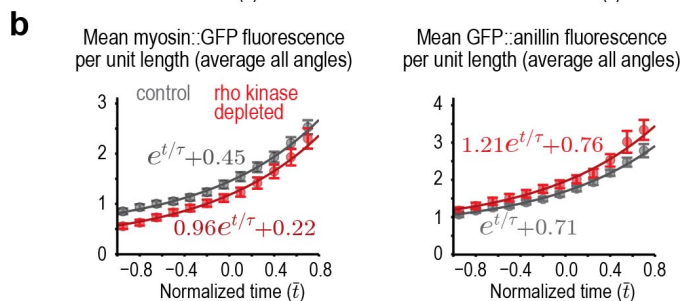
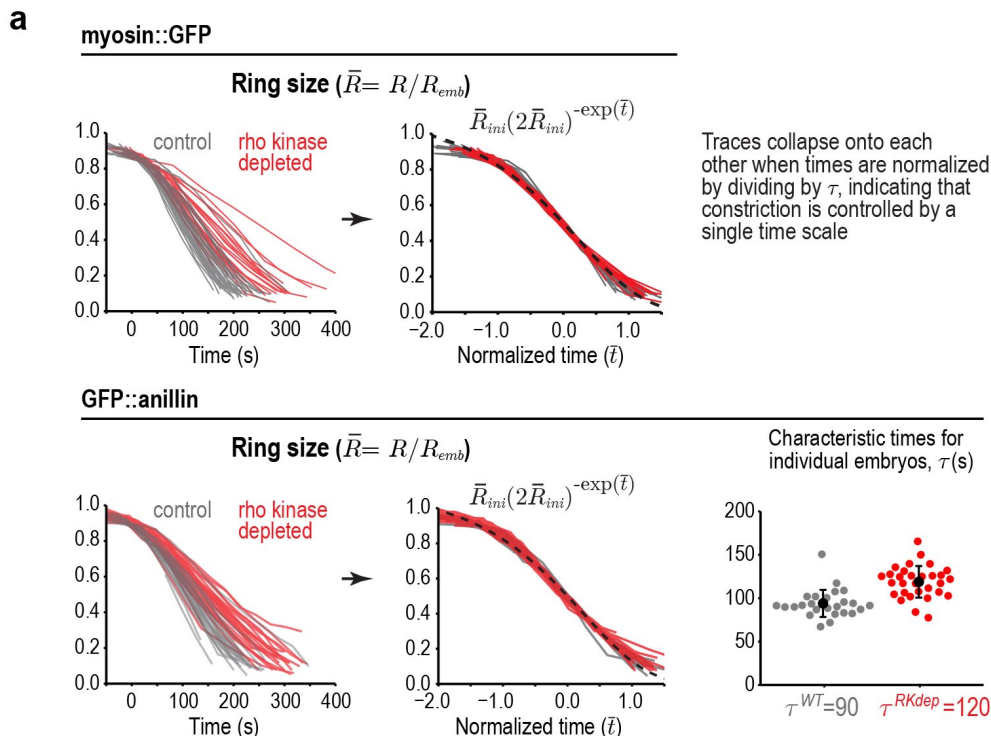
exponential increase in ring components during ingress due to ring-directed cortical flow, but technical challenges make clear evidence for an exponential increase significantly more challenging to obtain during this stage relative to 1-cell stage embryos.

## Khaliullin et al. Supplementary Figure 5



**Supplementary Figure 5. Recovery of myosin::GFP fluorescence after division plane bleaching at the 4-cell stage supports delivery of myosin into the ring by ring-directed cortical flow.** (a) We previously reported that following bleaching of a spot in the arc at the 4-cell stage, the bleached region progressively shrinks, generating a tornado shape in kymographs of a region drawn along the arc, and that the tornado thinning rate was slightly faster than predicted by shrinkage due to ring disassembly alone, which we could not explain<sup>17</sup>. The disassembly with ring-directed cortical flow model that we propose here predicts that after photobleaching a spot in the arc, the unbleached fluorescence in the flanking regions will dominate the fluorescence of the bleached region and ring disassembly will cause the bleached region to progressively shrink, leading to a tornado shape in the kymograph. At the same time, cortical myosin, which turns over faster than myosin in the ring, will recover and ring-directed cortical flow will begin to deliver myosin to the ring again. The increase in ring fluorescence due to cortical delivery would accelerate the rate of tornado thinning consistent with our prior observations. (b) As a better test of whether ring-directed cortical flow delivers components to the ring at the 4-cell stage, we monitored recovery after photobleaching the entire contractile arc similar to the experiment that we performed at the 1-cell stage (**Fig. 4**). Images show a representative bleached embryo (n=10). The observed recovery pattern was very similar to what we observed at the 1-cell stage, supporting delivery by ring-directed cortical flow. Scale bar is 10  $\mu\text{m}$ .

## Khaliullin et al. Supplementary Figure 6



**Supplementary Figure 6. Fitting experimental data using the CoFFee model equations reveals the effects of rho kinase inhibition of the properties of the cortex and contractile ring.** (a) (*left*) Graphs of ring size traces for individual control (*grey*, n=36 myosin::GFP or 26 GFP::anillin) and rho kinase depleted (*red*; n=24 myosin::GFP or 30 GFP::anillin) embryos. Graph for myosin::GFP expressing embryos is reproduced from Figure 6c for comparison. (*center*) Traces of ring size for all embryos collapse to the analytical curve (black dashed) when time is normalized by  $\tau$  and  $\bar{t} = 0$  is the point of 50% closure as expected if constriction is controlled by a single time scale. (*bottom, right*) Traces from GFP::anillin expressing embryos were fit to the ring size equation to determine characteristic times,  $\tau$ , for individual control (*grey*) and rho kinase depleted (*red*) embryos which are plotted along with the mean and SD for each condition (*black*). Rho kinase depletion increases  $\tau$  1.3-fold in GFP::anillin expressing embryos like it does in myosin::GFP expressing embryos. (b) Graphs plotting mean fluorescence per unit length (averaged over all angles) for GFP::anillin and myosin::GFP without baseline subtraction. (c) Schematics illustrate the effects predicted by the CoFFee model of reducing the ability of ring myosin to compress the cortex (*top*) or constrict the ring (*bottom*) on the dynamics of per unit length component amounts (*green*), constriction rate (*purple dashed*) and cortical flow velocity (*red dashed*). The effect on each curve relative to control (*black*) is shown in three time references: real time with t=0 set to constriction onset (*left*), time normalized by  $\tau$  with t=0 set to constriction onset (*center*), and time normalized by  $\tau$  with t=0 set to 50% closure (*right*). (*top*) Perturbations that decrease cortical compressibility ( $\alpha$ ) would increase  $\tau$ . (*top, right*) In real time, constriction rate and ring component amounts would increase with slower exponential kinetics ( $\propto e^{t/\tau}$ ) from the same starting point as in controls, whereas flow velocity would increase with slower kinetics from a lower starting point ( $\propto \alpha e^{t/\tau}$ ). (*top, center*) Normalizing time by  $\tau$ , causes rates to be per  $\tau$ ; this increases the flow velocity and constriction rate curves by a factor of  $1/\alpha$ , bringing the flow velocity back to the control and making the constriction rate start at a higher value than in controls. (*top, right*) Setting t=0 to the 50% closure point superimposes the constriction rate curve with the control, causing the curves for ring component amounts and flow velocity to fall below the controls. Since comparing properties for the same  $\bar{t}$  in this reference is equivalent to comparing properties for a given ring size, reducing  $\alpha$  would lead to a

reduction in component amounts for all ring sizes. (*bottom*) Reducing ring constrictability ( $\beta$ ) does not affect  $\tau$ . (*bottom, left*) In real time, flow velocity and ring component amounts increase with the same exponential kinetics as controls from the same starting point. The constriction rate also increases with the same exponential kinetics as in controls, but from a lower starting point due to the reduced  $\beta$ . Due to the exponential nature of the curves, the lower starting point effectively introduces a temporal offset, delaying constriction relative to the curves for ring component amounts and flow velocity. (*bottom, center*) Since reducing  $\beta$  does not affect  $\tau$ , normalizing time by  $\tau$  does not affect the relationship between the curves. (*bottom, right*) Setting  $t=0$  to the 50% closure point superimposes the constriction rate curve with the control and reveals that reducing  $\beta$  would lead to an increase in component amounts and flow velocity for all ring sizes.

## SUPPLEMENTARY MOVIE LEGENDS

### **Movie S1. Cortical flow imaged in a control embryo expressing myosin::GFP.**

Playback is 6x realtime. The movie is constructed from maximum intensity projection of 3 x 0.75  $\mu\text{m}$  plane z-stacks acquired at 2 s intervals. The red line marks the position of the division plane. The arrows represent the surface movement between consecutive frames at the base of the arrow. The length of the arrow is 5 times the magnitude of movement. The direction is also color coded according to the color wheel as shown in Figure 1b.

### **Movie S2. Average cortical flow map calculated from time lapse imaging of the cell surface in 93 control embryos expressing myosin::GFP.**

*(top, left)* Schematic illustrates location of the cylindrical surface covered by the map. *(top, right)* Dynamic schematic illustrates ring size and position for each value of  $t/t_{\text{ck}}$ . *(bottom, left)* The movement of each blue dot corresponds to surface movement at its location. The y-axis is the angular position relative to the initial ingression axis. The x-axis is the distance from the division plane along the anterior-posterior axis. *(bottom, right)* Dynamic graph plots the magnitude of the component of surface velocity aligned along the anterior-posterior axis for the top (150-180°; black) and bottom (0-30°; grey) regions of the cortex.

### **Movie S3. Average cortical flow map calculated from time lapse imaging of the cell surface in 68 *arx-2(RNAi)* embryos expressing Myosin::GFP.**

*(top, left)* Schematic illustrates the location of the cylindrical surface covered by the map. *(top, right)* Dynamic schematic illustrates ring size and position for each value of  $t/t_{\text{ck}}$ . *(bottom, left)* The movement of each blue dot corresponds to surface movement at its location. The y-axis is the angular position relative to the initial ingression axis. The x-axis is the distance from the division plane along the anterior-posterior axis. *(bottom, right)* Dynamic graph plots the magnitude of the component of surface velocity aligned along the anterior-posterior axis for the top (150-180°; black) and bottom (0-30°; grey) regions of the cortex.