

Supplementary Information

Self-destructive altruism in a synthetic developmental program enables complex feedstock utilization

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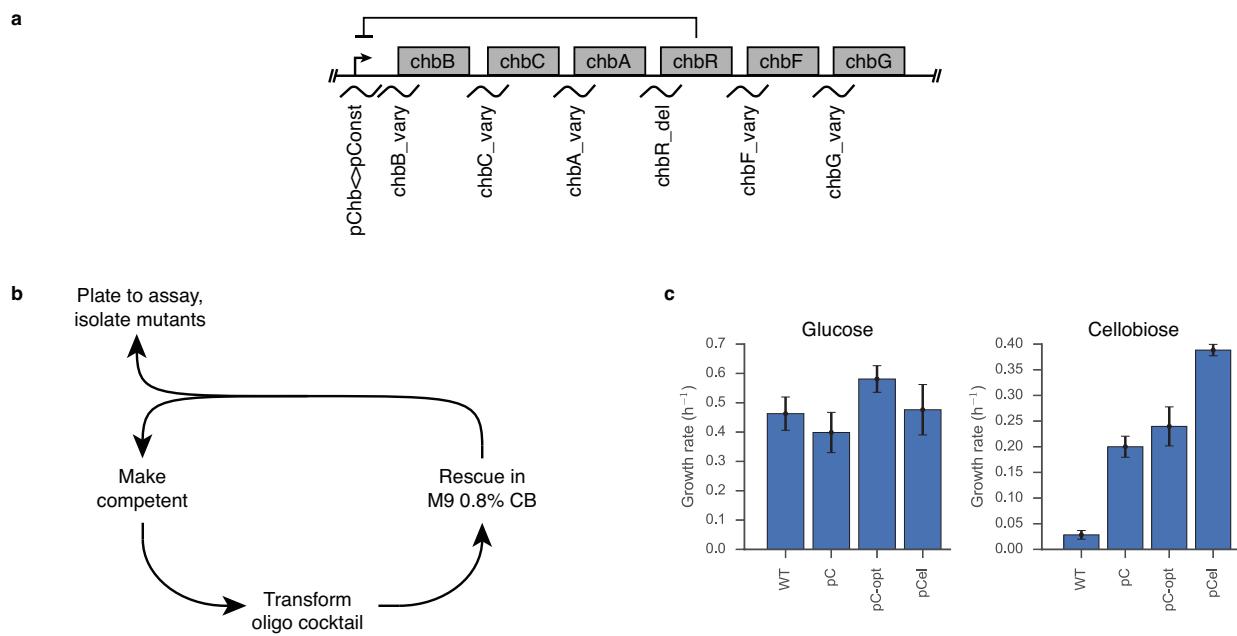
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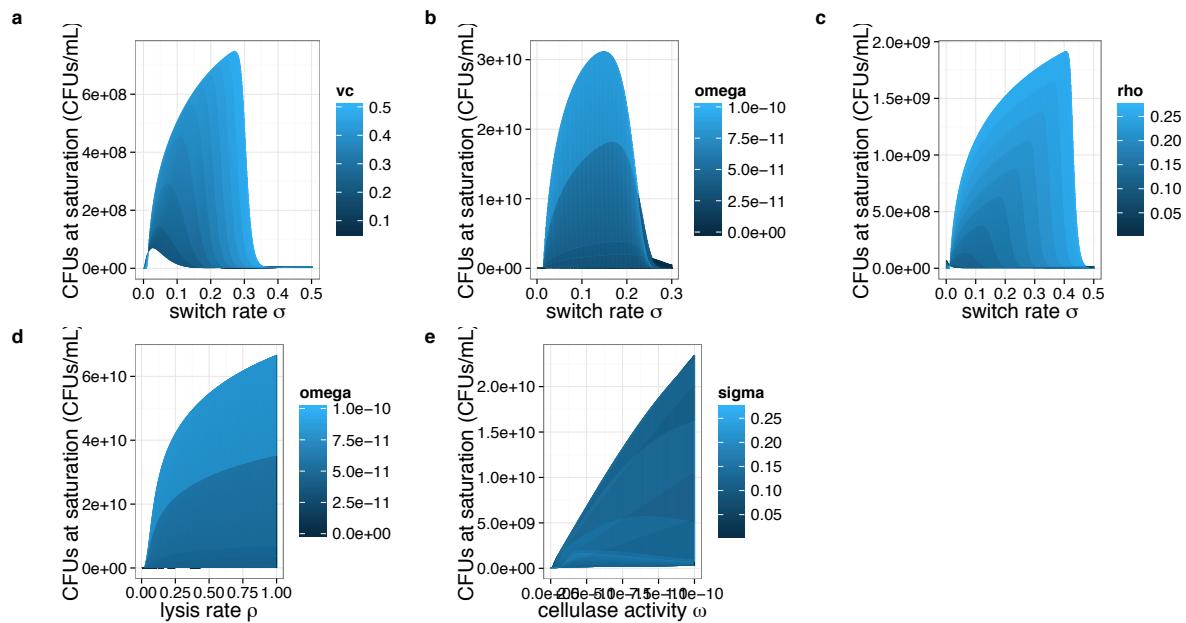
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Supplementary Figure 1. Engineering cellobiose utilization for SDAc strains



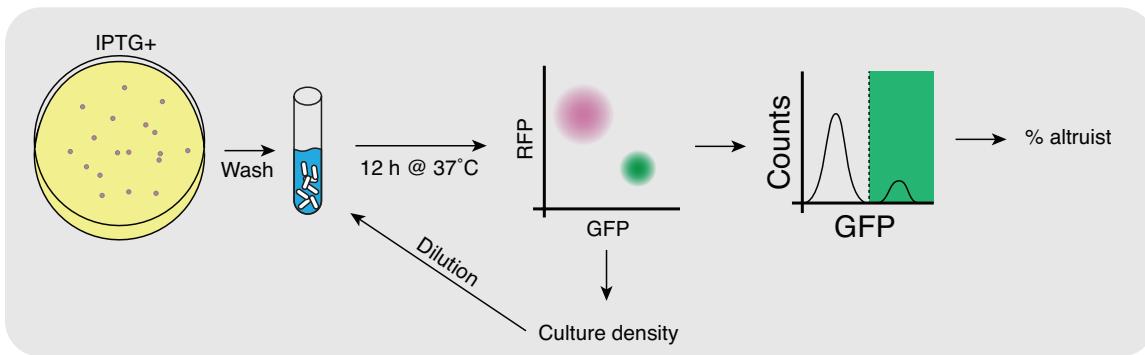
(a) Chitobiose (*chb*) operon with targeted sites for promoter replacement (pChb), overexpression (*chbA*, *chbB*, *chbC*, *chbF*, *chbG*) or deletion (*chbR*). See Supplementary Table 11 for oligonucleotide sequences. **(b)** Workflow to select for variants that grow faster on cellobiose. **(c)** Growth rates for a selection of variants: wild-type (WT, *EcNR1* Δ fim Δ lacI Z), the native *chb* promoter replaced with a constitutive promoter (pC, RGE531), the fastest growing recombinant mutant (pC-opt, DL069) and a control strain (pCel, DL180) that expresses a membrane-bound beta-glucosidase from *Cellvibrio japonicas*¹. Growth rates were measured at 32°C in a Biotek Synergy plate reader (n=3) using 200 μL cultures grown in 96-well microwell plates.

Supplementary Figure 2. Parameter sweeps for cellulose utilization model



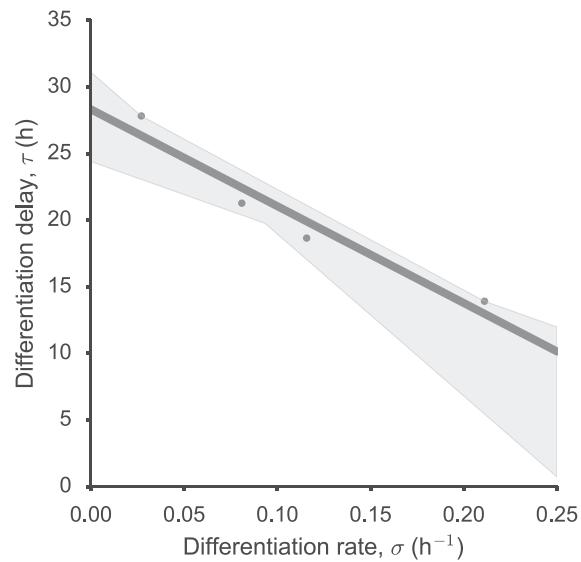
Parameter sweeps of core SDAc model parameters to develop intuition for circuit behavior and to guide system implementation. When plots do not vary parameters, nominal values are $v_c = v_a = 0.4$, $\sigma = 0.1$, $\rho = 0.25$, $\omega = 1.0 \times 10^{-11}$. **(a-c)** Expected biomass yield as a function of differentiation rate for discrete growth **(a)**, cellulase activity **(b)** and lysis **(c)** rates. **(d, e)** Expected biomass yield as a function of lysis rate for discrete cellulase activity rates **(d)** and as a function of cellulase activity rates for discrete differentiation rates **(e)**.

Supplementary Figure 3. Data collection for growth, differentiation and lysis rates



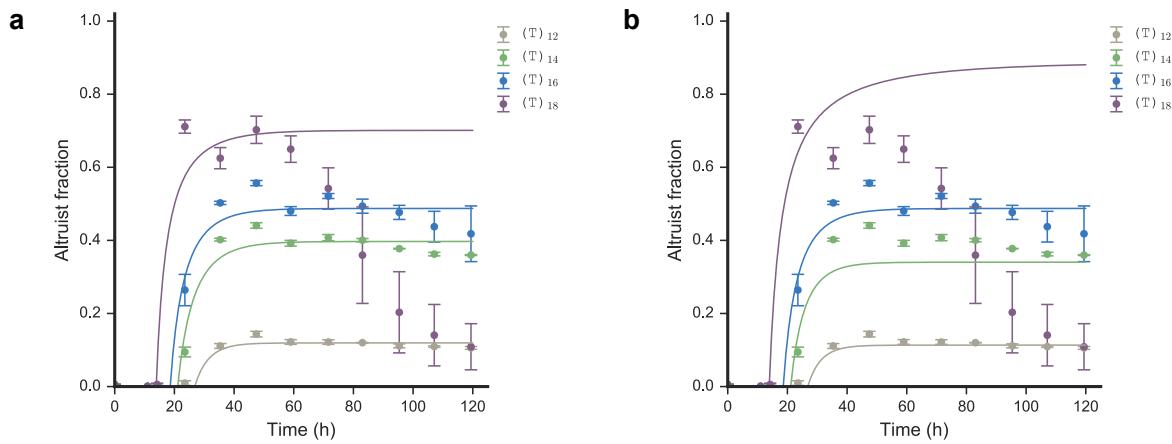
Experimental workflow to estimate growth, differentiation and lysis rates using low-density continuous culture and flow cytometry. Cultures are initialized in the consumer state by growing individual colonies on LB agar supplemented with IPTG. Colonies are washed and diluted into M9 minimal cellobiose media and periodically sampled in the flow cytometer to calculate the population fraction of differentiated cells and the dilution factor for the next growth passage.

Supplementary Figure 4. Mapping differentiation rate to differentiation delay



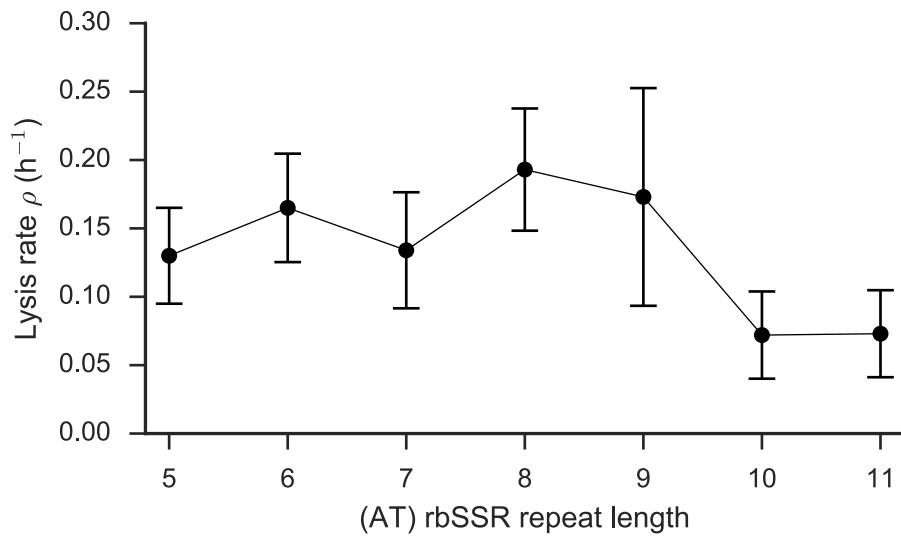
Relationship between the differentiation rate to the delay in the initiation of switching following the removal of IPTG inducer for strains DL046, DL112, DL110 and DL108. Linear fit line is $y = 28.3 - 72.7x$ h. The shaded area represents the 95% confidence interval for the fit.

Supplementary Figure 5. Altruist fraction fits combining growth, differentiation and lysis parameters



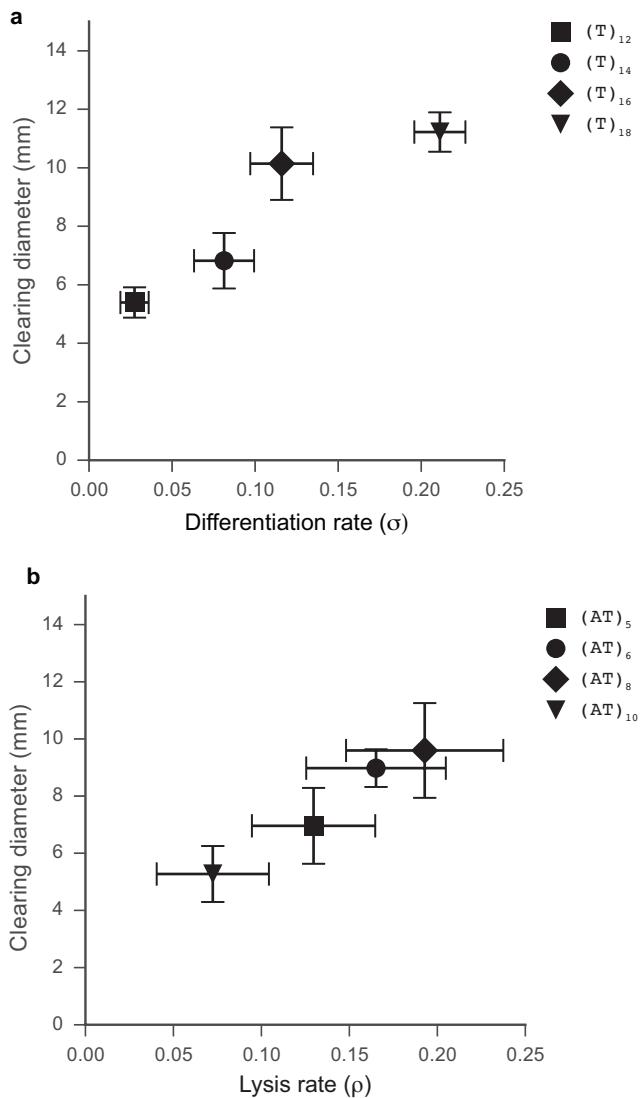
(a) Altruist fractions as a function of time for multiple differentiation variants. Altruist fractions were calculated from flow cytometry measurements of the continuous culture in cellobiose. Curves are derived from model predictions using growth rates of DL147, differentiation rates as estimated for the lysis-deficient switch variants and lysis rate fits for each strain. The lysis rate fit for (T)₁₈ was truncated at 65 h. Each strain uses rbSSR (ΔT)_o for lysis gene expression. Data for labels (T)₁₂, (T)₁₄, (T)₁₆ and (T)₁₈ correspond to measurements for strains DL046, DL112, DL110 and DL108, respectively (n=3). (b) Fits as in (a), but with a common lysis rate of 0.192 h^{-1} from DL110.

Supplementary Figure 6. Mapping *coIE3L* (AT) rbSSR length to lysis rate



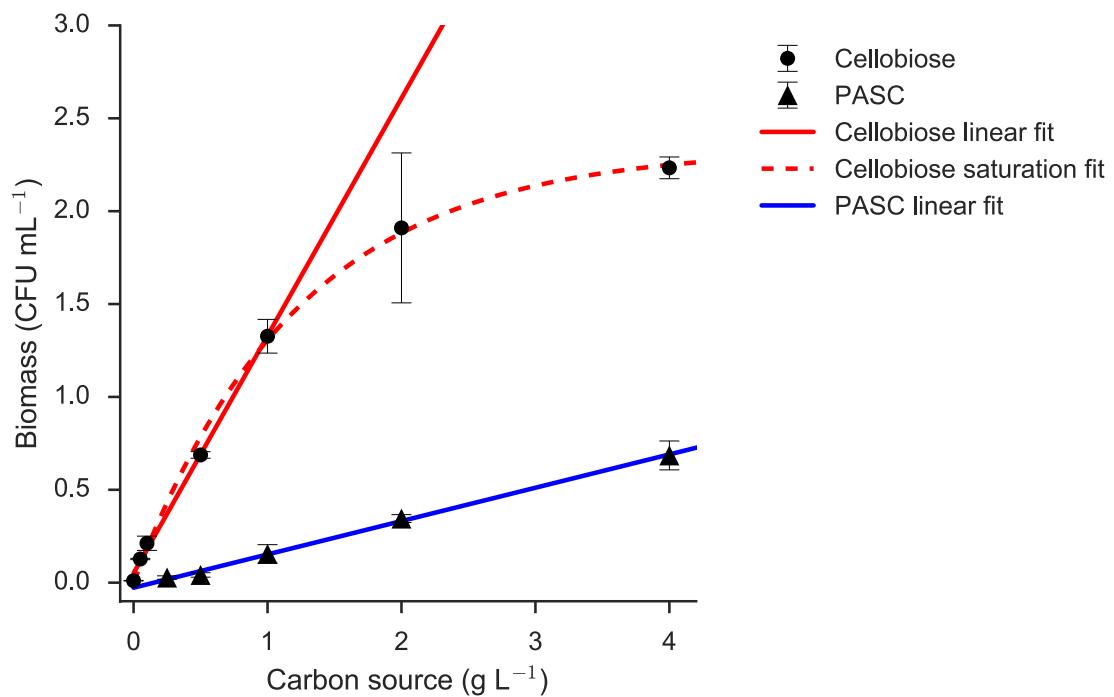
Lysis rate fits as a function of (AT) repeat length for multiple strains with switch $(\text{T})_{16}$. Error bars represent parameter estimate uncertainty, inclusive of measurement error and parameter bootstrapping from growth rates and differentiation rates.

Supplementary Figure 7. Mapping cellulose degradation clearings to differentiation and lysis rates



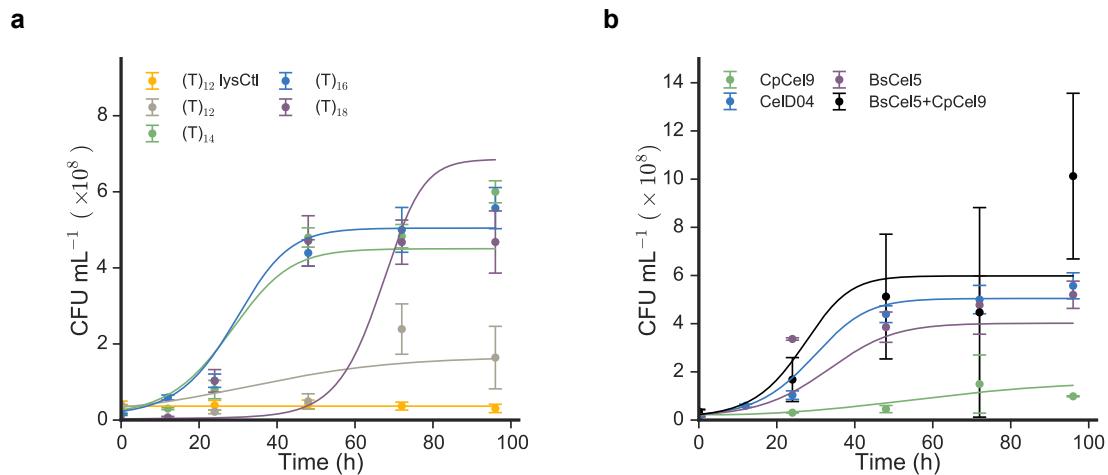
(a) Plot of cellulose degradation clearings as a function of differentiation rate for SDAc variants of the *tetR* rbSSR. (b) Plot of cellulose degradation clearings as a function of lysis rate for SDAc variants of the *colE3L* lysis gene rbSSR. For each panel the x-axis error bars represent uncertainty of experimental measurements and parameter bootstrapping and the y-axis error bars represent standard error from at least six replicate clearings of individual colonies (see Figure 3 caption).

Supplementary Figure 8. Carbon to biomass yield estimates



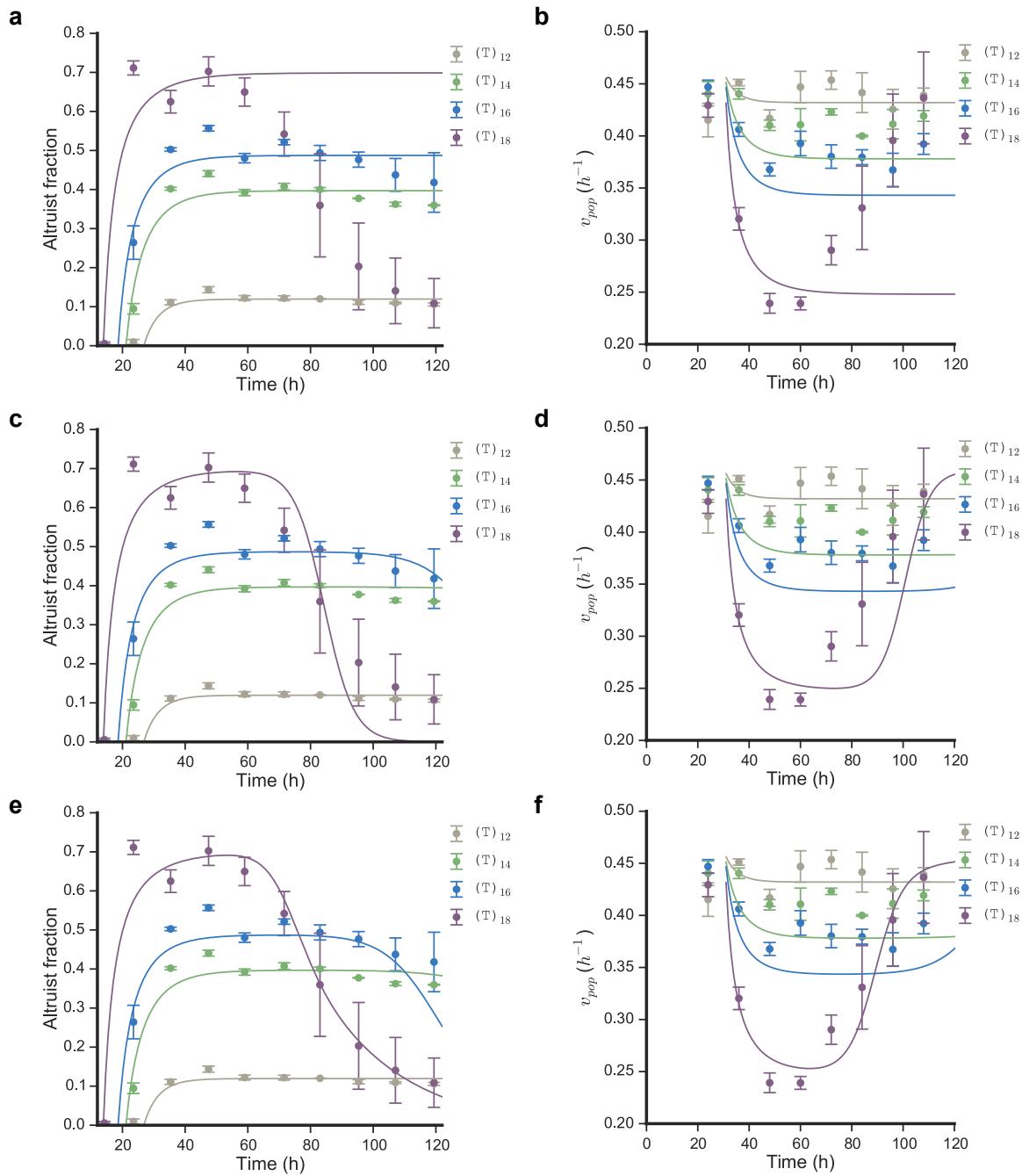
Carbon utilization measurements and fits for DL146 (cellobiose) and DL110 (PASC).

Supplementary Figure 9. Cellulose growth dynamics predictions for SDAc strains



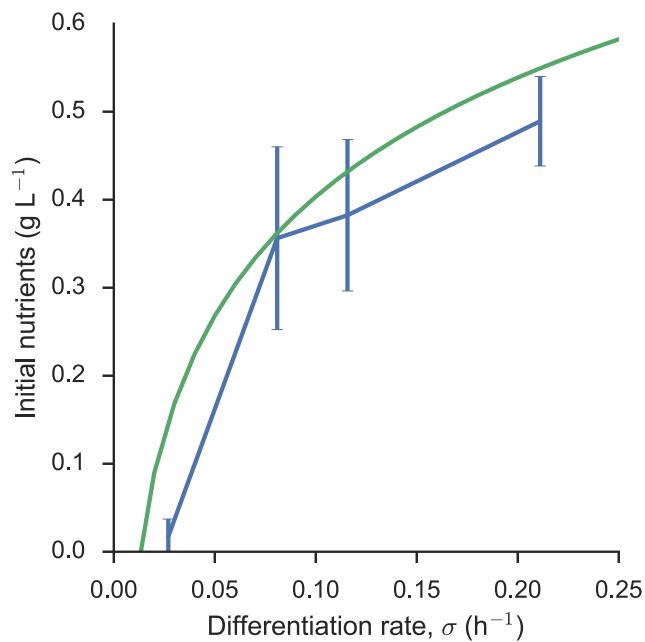
(a) Growth dynamics and model predictions for multiple differentiation variants and a lysis control. (b) Growth dynamics and model predictions for multiple cellulase variants using intermediate differentiator $(T)_{16}$. C4: CelD04, B5: BsCel5, C9: CpCel9, B5C9: BsCel5 + CpCel9 cocktail.

Supplementary Figure 10. Model fits to altruist fraction and overall growth for SDAc switch variants



Model fits to altruist fraction dynamics from continuous growth in cellobiose for no cheating (a), switch-deficient cheaters (c) and both switch-deficient and lysis-deficient cheaters (e). Fits for Growth rate variation with fit to null model.

Supplementary Figure 11. Model fit of initial nutrients to differentiation rate



Logarithmic fit of differentiation rate σ to initial nutrients measured in supernatant from differentiation rate variants using cellulase- and lysis-deficient DL146. Initial nutrients are generated by cellulase transferred into PASC with the culture inoculum.

Supplementary Movie

Movie S1 shows the growth and differentiation dynamics of individual microcolonies derived from individual cells of the (T)10/(A)12 rbSSR-BSS switch variant with an inactive cellulase gene and colicin E3 lysis gene expression controlled by an (AC)₁₁ rbSSR, transformed in strain 2.320. The movie demonstrates the stochastic differentiation and delayed lysis dynamics underlying SDAc behavior. The movie scale bar is 5 μ m.

Supplementary Table 1. SDAc model parameters

Parameter	Description	Units
v_C, v_A	Consumer, altruist growth rates	h^{-1}
k_C, k_A	Half maximal growth constants	g
σ	Differentiation rate	h^{-1}
k_σ	Half maximal differentiation constant	g
ρ	Lysis rate	h^{-1}
ω	Cellulase activity	CFU $^{-1}$ mL
γ	Nutrient to biomass conversion efficiency	CFU g $^{-1}$

Materials and methods

Media

Rich media was prepared as LB Miller broth (Cat #244620, Difco), supplemented with 15 g L⁻¹ bacto agar (Cat# 214030, Difco) when making solid media and with bacto agar and 0.1% carboxymethylcellulose (C5678, Sigma) to quantify cellulase clearings. M9 minimal media was prepared with M9 salts (Cat# 248510, Difco), 1 mM MgSO₄, 100 µM CaCl₂, supplemented with 1 mg mL⁻¹ biotin and a carbon source (glucose, cellobiose or PASC) at concentrations specified in the text. M9 minimal 0.4% cellobiose plates for isolating cellobiose utilizer strains were prepared as above supplemented with 15 g L⁻¹ bacto agar. Ampicillin and kanamycin antibiotics were supplemented when required at 20 µg mL⁻¹ and 20 µg mL⁻¹, respectively, unless indicated.

PASC preparation

Phosphoric acid swollen cellulose (PASC) was prepared following a reported protocol¹. Briefly, a cellulose slurry was created from sterile water and cellulose powder (Sigmacell 20, Sigma), combined with ice-cold 85% phosphoric acid (Sigma) and incubated at 4°C for 2 hours. Cellulose was precipitated in sterile water and washed repeatedly to remove the acid and bring the slurry to neutral pH.

Strains and plasmid construction

All strains used for assays in this study were derived from a variant of EcNR1² with genomic deletions of the *fim* operon, *ampR* and *lacZ* (CT009). Cellobiose utilizer DL069 was used as parent strain for all SDAC variants. Control strains for cellobiose utilization were derived from progenitor strain CT009. All strains are listed in Supplementary Table 2.

Plasmid construction was carried out using standard Gibson assembly protocols (Gibson et al. 2009). PCRs were performed using Phusion PCR Master Mix (NEB, M0531L) with a T-100 thermal cycler (Bio-Rad). Synthetic oligonucleotides for cloning were synthesized by Integrated DNA Technologies. Gibson assemblies were transformed into cloning strain DH5alpha. Transformations were performed by electroporation at 1250 V using an Eppendorf 2510 electroporator. Transformants were cultured on LB Miller agar plates with appropriate antibiotic or LB liquid media (Difco) at 37°C. Plasmids were extracted using the QIAprep Spin Miniprep Kit. Plasmids were sequenced by Genewiz (Seattle, WA). All plasmid assemblies were performed with vector pSC101 vector pGA4A5 or p15A vector pGA3K3³.

Cellulase genes were synthesized following standard polymerase cycling assembly (PCA) protocols⁴ using synthetic oligonucleotides provided by OligoCo, Inc. PCA was performed with Phusion polymerase and cloned into plasmids for sequence verification using Gibson Assembly.

Genome engineering

Cellobiose utilizer strain RGE531 was engineered using multiple cycles of multiplex genome engineering following Wang *et al.*². *E. coli* strain CT009 was grown in LB Miller broth to OD 0.4-0.6 at 30°C, then heat shocked in a water bath for 15 minutes at 42°C. The culture was chilled via ice slurry and centrifuged for 3 minutes at 5000 rpm in a centrifuge (Legend XR1, Thermo Scientific) pre-chilled to 4°C. The supernatant was decanted and cells were resuspended in 3 mL of ice-cold sterile water. The resuspension was centrifuged again for 3 minutes at 5000 rpm and the supernatant decanted. The cell pellet was resuspended in 800 µL of ice-cold sterile water and transferred to a 1.5 mL microcentrifuge tube. Cells were centrifuged at 4000 x g for 1 minute (Accuspin Micro 17R, Fisher Scientific) pre-chilled to 4°C. Supernatants were aspirated by pipette and cell pellets were resuspended in 40 mL ice-cold sterile water.

Competent cells were transformed with an oligonucleotide cocktail targeting ribosome binding site variation of *chbB/A/C/F/G* or deletion of *chbR* (synthesized by OligoCo, Inc., see Supplementary Table 10) by electroporation at 1800V using an Eppendorf electroporator 2510. Transformants were recovered in 10 mL of M9 0.4% cellobiose media in a shaker flask and grown for 48-72 hours at 30°C with shaking. This process was repeated for two additional cycles, using the saturated recovery culture from the previous as the inoculum for the next cycle of mutagenesis. Following each outgrowth in cellobiose, individual colonies were screened for rapid growth on M9 0.4% cellobiose agar plates, and several variants were isolated for *chb* operon sequencing and further use.

Microscopy

Fluorescence microscopy of SDAc microcolonies was carried out using equipment and procedures described previously³. *E. coli* strain 2.320 was transformed with a differentiation plasmid (*tetR/lacI* switch with (T)₁₀/(A)₁₂ repeats, p15A origin) and a payload delivery plasmid (colicin E3 lysis gene with (AC)₁₁ repeat, colE1 origin). Individual colonies were grown to saturation in minimal M9CA media (M8010, Teknova), 50 µg mL⁻¹ kanamycin and 20 µg mL⁻¹ ampicillin. Cultures were diluted 100:1, grown for two hours with shaking at 32°C and vortexed to break up cell aggregates. 1 µL of the culture was added to a glass-bottomed microscopy dish (GWSB-3512, WillCo Wells BV) and cells were immobilized on the dish surface using a nutrient agar slab prepared with M9CA media, as described above, and 1% bacto agar (Difco). Microscopy dishes were transferred to a Nikon Ti-S inverted microscope (Nikon Instruments) equipped with a Coolsnap-HQ camera (Roper Scientific) and an environmental chamber (In Vivo Scientific). Microcolony growth and fluorescent states were recorded every 15 min by capturing phase contrast, GFP and RFP images while the dishes were maintained at 32°C for 10 to 12 hours.

Measurements of growth, differentiation and lysis rates

Individual strains were initialized to the consumer state or altruist state (lysis-deficient control only) by inoculating individual colonies from a restreaked LB agar plate. The colonies were forced to the consumer state via IPTG induction (1 mM) or the altruist state via aTc induction (100 ng/mL) and grown at 37°C for 16 hours on LB agar media supplemented with ampicillin and kanamycin. Cultures were washed to remove inducer, inoculated 2000:1 into a well of a deep-well plate with 500 µL M9 minimal 0.4% cellobiose media supplemented with biotin and antibiotics as above, and grown at 37°C. To maintain exponential growth and low cell density, each culture was sampled every 12 hours and transferred to the cytometer (C6 with CSampler, Accuri) to measure culture density and the fluorescence distribution to determine the fraction of altruists. Growth rates between measurements were measured as a simple exponential fit using the initial cell density, the final cell density, and the number of hours between measurements. Each culture was diluted into fresh broth with a dilution factor defined by the culture density and the estimated growth rate. The dilution factors ranged from 5:1 to 50:1 every 12 hours. Growth rates and population fractions of consumers and altruists were calculated as described in Supplementary Notes 3 and 4, respectively.

Cell growth in PASC media

Cultures grown in PASC were initially inoculated into LB liquid culture with ampicillin and kanamycin from individual colonies restreaked on LB agar plates with the same antibiotics and IPTG to force the consumer state. Saturated cultures were transferred at 100:1 dilutions into M9 minimal PASC media and viable cell counts were periodically quantified by serial dilution and plating.

Measurements of carbon to biomass conversion efficiency

Carbon to biomass yield for cellobiose and PASC were measured using strains grown in M9 minimal media supplemented with increasing levels of each carbon source, up to 4 g L⁻¹. Cellobiose growth was quantified after 36 hours with cellulase and lysis deficient DL146 by serial dilution, plating and counting colonies. PASC growth was quantified after 72 hours with DL110 by the same method. All cultures were inoculated according to the PASC growth assay protocol and colony forming units were quantified for at least three replicates on LB plates supplemented with ampicillin and kanamycin. The estimate for cellobiose was fit only to the linear, carbon-limited regime observed at concentrations less than 1g L⁻¹ (see Supplementary Figure XX and Supplementary Note 6)

Measurements of cellulose degradation

Cellulase production strains for individual cellulases and cellulase cocktails were initialized by restreaking on LB agar plates supplemented with kanamycin (50 µg/mL), ampicillin (20 µg/mL) and aTc (100 ng/mL). Single colonies were transferred to 3 mL LB supplemented with kanamycin and ampicillin and grown to saturation overnight. Turbid 1 mL cultures were sonicated on ice (Ultrasonic Cell Disruptor, SharperTek) to release intracellular cellulase. The sonicator settings were 15 minutes with 95% power, and 75% duty cycle of 20 seconds on and 10 seconds off. Viable cell counts were measured before and after sonication using serial dilution and CFU plating to measure cell lysis efficiency (ρ). Cell lysates were filtered (0.4 micron filter, Company) to generate sterile supernatant. 10 µL cellulase lysate was transferred to 1 mL of 0.4% M9 minimal PASC + biotin media and incubated at 37°C for 72 hours, periodically measuring cellulose degradation by Congo Red absorbance or nutrient release. Uniprot identifiers for cellulases are Q45430 (CelD04), P10475 (BsCel5) and A9KT90 (CpCel9).

Congo Red absorbance measurements were taken by sampling 100 µL of the PASC growth media with cellulase at 0, 6, 12, 24, 48 and 72 hours post-inoculation, adding 100µL 0.15% (w/v) aqueous Congo red. After staining for 30 minutes, samples were centrifuged at 5000 rpm (Legend XR1) and 100 µL of PASC

supernatant was transferred to a clear, flat-bottom microwell plate (Corning 2595). Absorbance readings were measured by plate reader (Biotek) at a wavelength of 480 nm.

Cellulolytic release of digestible nutrients was estimated by measuring DL146 growth on PASC supernatant after lysate incubation. 10 µL aliquots of sterile cell lysates, prepared as above, were inoculated in 1 mL M9 minimal 0.4% PASC media, prepared in parallel for each time measurement. At each time point, 1 mL PASC samples were centrifuged in triplicate to pellet the PASC and collect the supernatant. DL146 cultures were grown for 36 hours in the supernatant media and culture densities were measured by serial dilution and plating.

Congo Red clearing assay

Individual colonies were generated on LB agar containing cellulose and the plates were stained with Congo Red dye to observe clearings. Strains were incubated for 14 hours on LB Miller agar supplemented with kanamycin, ampicillin and 0.1% carboxymethylcellulose. Colonies were removed from plates by washing with 70% ethanol. Plates were stained with 0.1% Congo Red for 20 minutes and destained with 1 M NaCl in two rinse steps, destaining for 5 minutes and 30 minutes, respectively. Clearing diameter for each colony was quantified from bright-field images of the stained plates by measuring clearing diameter using ImageJ software. Clearing diameter was converted from pixels to millimeters by normalizing to known plate diameter.

Sequencing SDAc switching or lysis cheaters

Bright, monochromatic red or green fluorescent colonies isolated from six replicate cultures of $(T)_{18}/(A)_{10}$ grown in M9 minimal 0.4% PASC media for 72 hours were identified via blue light transillumination. Each colony was replated separately on an LB agar plate and an LB agar plate supplemented with kanamycin and ampicillin to test for plasmid loss. Sequencing was performed on individual colonies by Genewiz, Inc. Differentiation plasmids were sequenced at the dual promoter region (BSSregSeq_2809) and the *lacI* C-terminal sequence (lacI rptSeq_2810). Payload plasmids were sequenced across the payload transcription unit (oligos Vf2 & Vr). Sequencing oligos are listed in Supplementary Table 13.

Materials and Methods References

1. Zhang, Y. H. P., Cui, J., Lynd, L. R. & Kuang, L. R. A transition from cellulose swelling to cellulose dissolution by o-phosphoric acid: evidence from enzymatic hydrolysis and supramolecular structure. *Biomacromolecules* **7**, 644–648 (2006).
2. Wang, H. H. et al. Programming cells by multiplex genome engineering and accelerated evolution. *Nature* **460**, 894–898 (2009).
3. Egbert, R. G. & Klavins, E. Fine-tuning gene networks using simple sequence repeats. *Proc Natl Acad Sci USA* **109**, 16817–16822 (2012).
4. Hoover, D. M. & Lubkowski, J. DNAWorks: an automated method for designing oligonucleotides for PCR-based gene synthesis. *Nucleic Acids Res* **30**, e43 (2002).

Supplementary Table 3. Cellobiose growth rates for SDAc strains

Strain ID	Switch variant	Cellulase	Lysis	Induction state*	Growth rate (hr ⁻¹)	StDev
DL146	(T) ₁₂ /(A) ₁₀	None	None	Consumer	0.463	0.019
DL146	(T) ₁₂ /(A) ₁₀	None	None	Altruist	0.391	0.019
DL147	(T) ₁₂ /(A) ₁₀	CelD04	None	Consumer	0.459	0.007
DL147	(T) ₁₂ /(A) ₁₀	CelD04	None	Altruist	0.413	0.023
DL046	(T) ₁₂ /(A) ₁₀	CelD04	colE3	Consumer	0.438	0.018
DL112	(T) ₁₄ /(A) ₁₀	CelD04	colE3	Consumer	0.420	0.017
DL183	(T) ₁₄ /(A) ₁₀	None	None	Consumer	0.430	0.012
DL110	(T) ₁₆ /(A) ₁₀	CelD04	colE3	Consumer	0.389	0.018
DL182	(T) ₁₆ /(A) ₁₀	None	None	Consumer	0.423	0.019
DL108	(T) ₁₈ /(A) ₁₀	CelD04	colE3	Consumer	0.266	0.041
DL188	(T) ₁₈ /(A) ₁₀	None	None	Consumer	0.395	0.003

* Induction to consumer state implies IPTG induction (1 mM). Induction to altruist state implies aTc induction (100 ng/mL).

Supplementary Table 4. Differentiation rates for lysis-deficient SDAc switch variants

Strain ID	Switch variant	σ (h ⁻¹)	StDev	τ (h)	StDev
DL146	(T) ₁₂ /(A) ₁₀	0.027	0.009	26.8	4.56
DL183	(T) ₁₄ /(A) ₁₀	0.081	0.018	21.1	0.97
DL182	(T) ₁₆ /(A) ₁₀	0.116	0.019	18.6	0.78
DL188	(T) ₁₈ /(A) ₁₀	0.211	0.015	13.9	0.03

Supplementary Table 5. Lysis rates for SDAc switch and lysis variants

Strain ID	Switch variant	Lysis variant	σ (h ⁻¹)	ρ (h ⁻¹)	StDev
DL046	(T) ₁₂ /(A) ₁₀	(AT) ₈	0.027	0.180	0.080
DL112	(T) ₁₄ /(A) ₁₀	(AT) ₈	0.081	0.159	0.052
DL108	(T) ₁₈ /(A) ₁₀	(AT) ₈	0.211	0.256	0.036
DL268	(T) ₁₆ /(A) ₁₀	(AT) ₅	0.116	0.130	0.035
DL269	(T) ₁₆ /(A) ₁₀	(AT) ₆	0.116	0.165	0.040
DL270	(T) ₁₆ /(A) ₁₀	(AT) ₇	0.116	0.134	0.042
DL110	(T) ₁₆ /(A) ₁₀	(AT) ₈	0.116	0.192	0.048
DL271	(T) ₁₆ /(A) ₁₀	(AT) ₉	0.116	0.173	0.080
DL272	(T) ₁₆ /(A) ₁₀	(AT) ₁₀	0.116	0.072	0.032
DL273	(T) ₁₆ /(A) ₁₀	(AT) ₁₁	0.116	0.073	0.032

Supplementary Table 6. Carbon to biomass yields for cellobiose and PASC

Media	Linear range	γ (CFU g ⁻¹)	StDev	R ²
Cellobiose	0 – 1 g L ⁻¹	1.279e+12	3.344e+10	0.9919
PASC	0 – 4 g L ⁻¹	1.795e+11	8.475e+09	0.9825

Supplementary Table 7. Cellulase activity measurements for cellulase production strains

Strain ID	Cellulase	ω (hydrolysis)	StDev	ω (biomass)	StDev
DL292	CpCel9	4.6e-12	2.4e-13	3.6e-13	3.9e-13
DL147	CelD04	5.7e-12	6.8e-13	1.6e-12	5.3e-13
DL294	CelD04 + CpCel9	6.8e-12	9.5e-13	1.8e-12	5.6e-13
DL307	BsCel5	6.1e-12	9.8e-13	1.2e-12	2.9e-13
DL294	BsCel5 + CpCel9	7.4e-12	4.3e-13	1.9e-12	3.0e-13

Note: units for ω are CFU⁻¹ mL⁻¹**Supplementary Table 8.** Half-maximal rate constants for growth and differentiation

Parameter	Fit	StDev
k_C, k_A	0.00112	0.00045
k_σ	0.09999	0.00019

Supplementary Table 9. Cheater rates for expanded SDAc model

Cheater type(s)	χ_c (h ⁻¹)	Std Error	χ_A (h ⁻¹)	Std Error
Differentiation	2.473e-07	5.857e-08	n/a	n/a
Differentiation and lysis	1.775e-06	6.279e-07	1.908e-05	8.207e-06

Supplementary Table 10. Genotypes for differentiation cheaters

Plate Replicate	Isolation condition	Promoter mutation	<i>lacI</i> mutation
2	LB	None	None
2	LB kan/amp	None	(CTGG) ₂
2	LB kan/amp	None	None
3	LB kan/amp	None	IS2 insertion at base 15 of <i>lacI</i>
3	LB kan/amp	None	IS2 insertion at base 15 of <i>lacI</i>
3	LB kan/amp	None	IS2 insertion at base 34 of <i>lacI</i>
4	LB	None	(CTTG) ₄
4	LB	None	148 bp <i>lacI</i> deletion (A351)
4	LB kan/amp	None	None
4	LB kan/amp	None	(CTTG) ₄
5	LB kan/amp	None	(CTTG) ₄
5	LB kan/amp	None	(CTGG) ₂
5	LB kan/amp	None	(CTTG) ₄
5	LB kan/amp	None	20 bp <i>lacI</i> deletion (A303)
6	LB kan/amp	Δ(T) ₅	None
6	LB kan/amp	None	(CTGG) ₂
6	LB kan/amp	Δ(T) ₅	None
6	LB kan/amp	Δ(T) ₅	None

Sequencing results of differentiation plasmid mutations from monochromatic RFP-positive (T)₁₈/(A)₁₀ escape colonies (six replicate plates). The first replicate plate had no mutations at the sequenced loci for the differentiation plasmid.

Supplementary Table 11. Genotypes for lysis cheaters

Plate	Replicate	Isolation condition	Payload plasmid mutations
1		LB	None
1		LB Kan/Amp	None
2		LB	None
2		LB	None
2		LB	None
2		LB Kan/Amp	None
2		LB Kan/Amp	None
2		LB Kan/Amp	None
2		LB Kan/Amp	None
3		LB	None
4		LB	IS1 insertion at A514 in celD04
4		LB	IS1 insertion at A514 in celD04
4		LB Kan/Amp	IS1 insertion at A514 in celD04
4		LB Kan/Amp	IS1 insertion at A514 in celD04
5		LB	None
6		LB	None
6		LB	None
6		LB Kan/Amp	None

Sequencing results of payload plasmid mutations from monochromatic GFP-positive $(T)_{18}/(A)_{10}$ escape colonies (six replicate plates).

Supplementary Table 12. Oligonucleotides used to modify *chb* operon and for cheater sequencing

Oligo name	Sequence
pChb<>pConst	CTTCCATGCTCTGGGTAACTTGCAGAACACATGATGAATCTATTATAAAAAAAAAAAAAAA AAGTCATAACTCTATCGAACTCAGGCCAAAAAAACCGCGCAATGGCCGGTTTC
chbR_del	ggacataaataatccagcaacaggacagatgtgaattgtcaggtataacgacttactgcac actcccttatgccttcagtttcatgaagctcaattaattcagaatcaggtaatcgttcac
chbA_A15	agctcttcagttccgttgcgtatcggaaatgttatcgagatccatcatTTTTTTTTTTTT CCTCCTCtttcttaccggcacattaccgtaccggcatcgattaaaattcag
chbC_T15	actgcaaaaggaggagtacctttcaagcgatgcaataacattactcatAAAAAAAAAAAAAA CCTCCTaaaaaccgcaatttaatattgcgttattgatttataactcttt
chbB_A15	gaggttagacatgcccgcagaacaaaacagataatgtgtttctttccatTTTTTTTTTTTT ACCTCCTGATatcgacgattatctgtcagccagacactccgcaagcctaaccctg
chbF_A5	gtatagctgtccccccaccaatagtgacgactttaatattctggctcatTTTTACCTCCTag acagaataactgatatactggcatatctgccccccggacataaata
chbF_A15	gtatagctgtccccccaccaatagtgacgactttaatattctggctcatTTTTTTTTTTTT ACCTCCTagtacagaataactgatatactggcatatctgccccccggacataaata
chbG_T15	ccttgcttaagccaaatcatggcattaacaatcagtaagcgccatAAAAAAAAAAAAAA CCTCCttaatgtgttttaagctctgcgtgcagttggcagcc
BSSregSeq_2809	GGCTGCTCTACACCTAGCTTCTGG
lacI rptSeq_2810	GGTTTGTTGAAAACCGGACATGG
Vf2	TGCCACCTGACGTCTAAGAA
Vr	ATTACCGCCTTGAGTGAGC

Supplementary Note 1. Model assumptions for SDAc population dynamics

The model for synthetic self-destructive altruism dynamics relies on multiple assumptions to minimize the number of parameters. First, intracellular enzyme accumulation is considered independent of the lysis rate, resulting in a fixed payload size per altruist. Second, cellulase dynamics were removed from the system of equations based on an assumption that cellulase enzymatic activity occurs much faster than its degradation, allowing parameters to be consolidated. Cellulase activity ω is normalized to the altruist population through the product ρA . Third, while we assume nutrient-dependent rates for growth and switching, altruist commitment to lysis is considered to be nutrient independent.

Supplementary Note 2. Parameter bootstrapping for SDAc models

Bootstrapping based on Monte Carlo simulations was used to generate many parameter estimates for SDAc models. Uncertainty in the parameter estimates depend both on experimental measurement error and independently measured experimental parameters. Parameter estimates should reflect both the fit to the experimental data and uncertainty propagated from parameters used to constrain the fit. Thousands of parameter fits were generated to propagate the uncertainty measures, randomly sampling from a normal distribution of the existing parameters for each fit². We calculated the mean and standard deviation of the ensemble of fits to generate the parameter estimate.

Supplementary Note 3. Estimating growth rates from cytometry data

As described in the methods section, the growth rates for consumer cells and altruist cells were estimated by applying an exponential fit to cell densities measured via cytometry at 12 hour intervals in periodically diluted samples. The growth rate for each strain over three passage intervals (36, 48, 60 h) was measured in triplicate to obtain mean and standard error measurements for each strain (Supplementary Table 2).

For each strain, growth rate $\nu = \alpha/\ln(2)$ was estimated from time $t1$ to time $t2$ using equations

$$P_{t2} = P_{t1} \left(\frac{V_{tx}}{V_{tx} + V_w} \right) e^{\alpha(t2-t1)}, \quad (\text{S1})$$

$$\alpha = \ln \left(\frac{P_{t2}}{P_{t1}} \left(\frac{V_{tx} + V_w}{V_{tx}} \right) \right) (t_2 - t_1)^{-1}, \quad (\text{S2})$$

for which P_{t1} and P_{t2} are the cell densities measured in gated events per second at times $t1$ and $t2$, respectively, V_{tx} is the transfer volume in μL between passages and V_w is the media volume in μL .

Supplementary Note 4. Estimating differentiation rates from cytometry data

As described in Box 1 and the methods section, the differentiation rate σ for individual strains was estimated by applying parameter bootstrapping for growth rate estimates to fit Equations (5-6) to the fraction of lysis-deficient altruists. Cytometry samples were processed using custom Matlab scripts as previously reported³. Briefly, samples were filtered using a fixed gate for forward scatter values between 16,000 and 100,000 and side scatter values between 10 and 7,000. The altruist subpopulation was determined by using a fixed threshold in the GFP channel (488 nm excitation with 533 nm bandpass emission filter) of 600, which captures less than 0.1% of the population for a non-fluorescent strain.

An analytical solution to consumer and lysis-deficient altruist populations that accounts for a temporal delay observed in differentiation experiments was generated from Equations (5-6) of Box 1:

$$C(t) = e^{(v_C - \sigma)(t-\tau)}, \quad (S3)$$

$$A(t) = \frac{\sigma(e^{v_A(t-\tau)} - e^{(v_C - \sigma)(t-\tau)})}{v_A - v_C + \sigma}. \quad (S4)$$

Differentiation rate σ and corresponding delay τ were estimated from measurements of $\frac{A(t)}{A(t)+C(t)}$ fit to Equations (S3, S4) for the cellulase and lysis deficient SDAc strains shown in Figure 2c (see Supplementary Table 3 for values). Fits were generated using the Levenberg-Marquardt nonlinear least squares algorithm (nlsLM) in R. Differentiation delay was observed to be inversely proportional to the differentiation rate (see Supplementary Figure 4). Parameter bootstrapping was performed to create 10,000 fits for each of three biological replicates, randomly sampling a normal distribution ($n=10,000$) of v_C and v_A from control strain DL146. The mean and standard deviation of the fit ensemble were calculated as the mean and standard deviation differentiation and delay measures for each strain.

Supplementary Note 5. Estimating lysis rates from cytometry data

As described in Box 1 and the methods section, the lysis rate ρ for individual strains was estimated by applying parameter bootstrapping for growth rate, differentiation and delay estimates to fit Equation Module I to the fraction of GFP-expressing altruists. Cytometry samples were processed as described in Supplementary Note 4.

An analytical solution to consumer and altruist populations that includes a lysis term and accounts for delayed differentiation as in Supplemental Equations S3 and S4 was generated from Equation Module II of Box 1:

$$C(t) = e^{(v_C - \sigma)(t-\tau)}, \quad (S3)$$

$$A(t) = \frac{\sigma(e^{(v_A - \rho)(t-\tau)} - e^{(v_C - \sigma)(t-\tau)})}{v_A - v_C - \rho + \sigma}. \quad (S5)$$

Lysis rate ρ was estimated from measurements of $\frac{A(t)}{A(t)+C(t)}$ fit to Equations (S3, S5) for the SDAc strains shown in Figure 2f (see Supplementary Table 4 for values). Fits and parameter bootstrapping were performed as described for differentiation rate estimates in Supplementary Note 4. Random growth rate estimates for bootstrapping were sampled from cellulase production variant DL147 and differentiation rates estimates were sampled from rates of the appropriate switch variant.

Supplementary Note 6. Estimating biomass yield for cellobiose and PASC

The Monod model of bacterial growth assumes a linear relationship between the saturated density of cells and the limiting nutrient and states that the slope of the line is the yield coefficient for the nutrient⁴. Here, we depict that relationship as

$$Y(n) = \gamma n + b, \quad (S6)$$

with Y as the biomass yield, γ as the yield coefficient, n as the nutrient level and b as an inoculation-dependent y . DL146 cultures grown in cellobiose appeared to be carbon limited only at concentrations below 1 g L^{-1} (Supplementary Figure 7a). When all cellobiose concentrations are included in the fit, carbon utilization matches an exponential saturation model,

$$Y(n) = S(1 - e^{\alpha n}), \quad (S7)$$

with S as the maximum biomass yield afforded by the limiting nutrient. No saturation was observed for PASC (Supplementary Figure 7b), suggesting the media remains carbon limited up to 4 g L^{-1} . Comparison of the slopes for each carbon source ($\gamma_{\text{PASC}}/\gamma_{\text{cellobiose}}$) suggests approximately 14% of available carbon in the cellulose is released in a digestible form for cellulase CelD04. Estimates for γ are summarized in Supplementary Table 6.

Supplementary Note 7. Estimating cellulase activity rates

Culture densities before and after sonication were used to estimate altruist concentration A and lysis efficiency ρ from the feedstock equation of Module I in Box 1. As mentioned in the Methods section, two approaches were used to estimate cellulose hydrolysis: Congo Red staining of residual cellulose and biomass conversion from released nutrients. Congo Red absorbance measurements consistently suggested higher cellulose degradation rates than the nutrient release assay, suggesting some hydrolysis products, including oligomers larger than cellobiose, might not be digestible by SDAC strains.

A spectrophotometric calibration curve was established to estimate residual cellulose by measuring absorbance at 480 nm for PASC supernatant stained with 0.15% Congo Red. The calibration curve was generated for PASC concentrations from 2.68 g L^{-1} to 4 g L^{-1} . Absorbance readings were converted to cellulose concentrations using a linear fit to the calibration curve ($R^2 = 0.8869$).

$$[\text{Cellulose}] = -(0.595 \pm 0.0125) \times \text{ABS}_{480} + (4.7 \pm 0.03) \quad (S8)$$

Cellulose concentrations were estimated from released nutrients by measuring viable cell counts of cultures grown in PASC supernatant and converting cell counts to nutrients using the γ parameter and Supplementary Equation S6.

$$F = F_0 - n_i = F_0 - \frac{CFU(n_i) - b}{\gamma} = 0.004 - \frac{CFU(n_i) - (5.1e07 \pm 1.68e07)}{(1.28e12 \pm 3.34e10)} \quad (S9)$$

Parameter bootstrapping was used to estimate feedstock degradation for measurements using each method by generating mean and standard deviation statistics for 10,000 fits, each randomly sampling from a normal distribution of the error for the appropriate calibration curve.

An analytical solution to feedstock levels was generated from feedstock equation of Module I in Box 1 to estimate cellulase activity rates from Congo Red absorbance or nutrient release measurements,

$$F = Pe^{-\alpha\rho At} + f, \quad (S10)$$

with parameters P , α , and f . By the rules of derivation, the cellulase activity rate ω is the product of P and α . Fits were generated using initial altruist concentrations (A) and lysis efficiency (ρ) measured for each strain (Supplementary Table 7).

Supplementary Note 8. Estimating half-maximal rate constants for growth and differentiation

Nutrient-specific half-maximal rate constants for consumer and altruist growth – (k_C and k_A , respectively) and differentiation (k_σ) were fit to the growth curve for strain DL110. 10,000 fits were generated using parameter distributions with the mean and standard deviation for σ , ρ and ω associated with switch variant (T)₁₆/ (A)₁₀, lysis rbSSR variant (AT)₈ and CelD04 payload variant from Supplementary Tables 4, 5 and 7, respectively. Parameter bootstrapping distributions for growth rates (v_C, v_A) were generated from DL147 (Supplementary Table 3):

$$\begin{aligned}v_C &= 0.459 \pm 0.004 \\v_A &= 0.413 \pm 0.012 \\\sigma &= 0.116 \pm 0.009 \\\rho &= 0.191 \pm 0.025 \\\gamma &= 1.279 * 10^{12} \pm 3.344 * 10^{10} \\\omega &= 1.6 * 10^{-12} \pm 5.3 * 10^{-13}\end{aligned}$$

The half maximal constants for C and A are assumed to be the same and were fit as one parameter. The resulting parameter fits are shown in Supplementary Table 8. These half-maximal rate constants were adopted for use as necessary in models for SDAc strains.

Supplementary Note 9. Initial conditions for nutrients and population size in full dynamics model

SDAc system dynamics, both in the model and the physical implementation, were sensitive to initial conditions. For example, PASC growth media was inoculated with SDAc cultures directly from a saturated culture in rich media. Thus, the initial concentration of viable cells was dependent on differentiation rate (cultures with high differentiation rates likely generate more altruists, reducing the concentration of viable cells) and the inoculum included cellulase payload to begin converting PASC to nutrients. To account for these details, initial nutrients (with a concomitant reduction in initial feedstock) and initial population size were estimated as a function of the differentiation rate σ . Nutrients levels were estimated by fitting a logarithmic curve to the growth yield of DL146 in PASC media with filtered supernatant from SDAc strains DL046, DL112, DL110 and DL108, applying the biomass conversion equation from Module IV of Box 1 to convert CFUs to nutrients. Parameter bootstrapping from uncertainty in the γ parameter (Supplementary Equation S6) was applied to the fit (10,000 samples), which produced an estimate for initial nutrients as a function of differentiation rate (see Supplementary Figure 11): $n_0 = (1.952 * 10^{-4} \pm 2.952 * 10^{-5}) \log(\sigma) + (8.529 * 10^{-4} \pm 9.463 * 10^{-5})$.

A linear curve fit was used to map differentiation rate to initial population size. Viable cell count mean and standard deviation measurements from the same SDAc strains above were used to map differentiation rate σ to initial cell concentration x_0 : $x_0 = -(1.7 \times 10^8 \pm 4.14 \times 10^7) \sigma + (3.66 \times 10^7 \pm 5.43 \times 10^6)$. Initial population estimates were distributed among consumers and altruists by applying the steady state solutions to the equations of Module II from Box 1 for DL147 growth rates and strain-specific differentiation rates.

Supplementary Note 10. Estimating SDAc cheater rates

Cooperation escape rates for consumers and for altruists were estimated by applying parameter bootstrapping for growth, differentiation and lysis rates to fit the equations of Module V from Box 1 to the fluorescence distribution and overall growth rate data from SDAc hyperdifferentiator strain DL108. The model was fit to the fluorescence distribution data (collected as described in Supplementary Note 4) separately with different assumptions: no cheaters ($\chi_C = \chi_A = 0$, simplifies to Equations 5-6), switch-deficient cheaters only ($\chi_A = 0$) and both switch and lysis-deficient cheaters. Cheater rate estimates for the latter two assumptions are shown in Supplementary Table 9. The fits were generated using the

Levenberg-Marquardt nonlinear least squares algorithm (nlsLM) in R. The standard error represents residuals error reported by the algorithm.

Supplementary Note 11. Modeling cheater dynamics

Consumers and altruists only

Steady-state analysis of the mutagenesis-naïve model of SDAc dynamics cannot account for the observed altruist fraction dynamics. The initial model for SDAc dynamics included cell states for only consumers (C) and altruists (A). Examination of the altruist fraction dynamics with differentiation and lysis for hyperdifferentiator $(T)_{18}/(A)_{10}$ grown in cellobiose (Supplementary Figure 5) clearly shows that the initial models do not track the measured data. While the population appears to reach an initial steady-state fraction around 40 hours, the altruist fraction subsequently decreases to settle at a new, non-zero steady state at 120 hours.

For this model, the fraction of cells expressing RFP (f_{red}) and GFP (f_{green}) represent the fraction of consumers and altruists, respectively. We can derive the rate of change of each relative fraction from the ODEs of Module II in Box 1 of the main text by applying the quotient rule:

$$f_{red} = f_C = \frac{C}{C + A}, \quad f_{green} = f_A = \frac{A}{C + A}.$$

$$\dot{f}_C = \frac{\dot{C}(C + A) - C(\dot{C} + \dot{A})}{(C + A)^2} = \frac{\nu C - \sigma C}{C + A} - \frac{f_C(\nu C - \sigma C + \nu A - \rho A + \sigma C)}{C + A} = f_C(\rho f_A - \sigma)$$

$$f_C^*: f_C(\rho f_A - \sigma) = 0$$

$$f_C^* = 0$$

$$f_A = (1 - f_C), \quad f_C(\rho(1 - f_C) - \sigma) = 0$$

$$f_C^* = 1 - \frac{\sigma}{\rho}$$

$$\dot{f}_A = \frac{\dot{A}(C + A) - A(\dot{C} + \dot{A})}{(C + A)^2} = \frac{\nu A - \rho A + \sigma C}{C + A} - \frac{f_A(\nu C - \sigma C + \nu A - \rho A + \sigma C)}{C + A} = \sigma f_C - \rho f_A(1 - f_A)$$

$$f_A^*(f_C^* = 0): 0 - \rho f_A(1 - f_A) = 0$$

$$f_A^*(f_C^* = 0) = 0, 1$$

$$f_A^*\left(f_C^* = 1 - \frac{\sigma}{\rho}\right): f_C = 1 - f_A, \quad 1 - f_A = 1 - \frac{\sigma}{\rho}$$

$$f_A^*\left(f_C^* = 1 - \frac{\sigma}{\rho}\right) = \frac{\sigma}{\rho}$$

$$(f_C^*, f_A^*) = \begin{cases} (0,0) & \text{stable} \\ \left(1 - \frac{\sigma}{\rho}, \frac{\sigma}{\rho}\right) & \text{saddle for } \sigma < \rho, \text{unstable for } \sigma > \rho \\ (0,1) & \text{unstable for } \sigma < \rho, \text{saddle for } \sigma > \rho \end{cases}$$

Steady state analysis of this model constrains the consumer and altruist fractions to simple, saturating dynamics from the initial condition $f_A = 0$, as used in experiments. For this model, the fractions stabilize at

$\left(1 - \frac{\sigma}{\rho}, \frac{\sigma}{\rho}\right)$ if σ is less than ρ , or $(0,1)$ if σ is greater than or equal to ρ . The steady state with both population fractions at zero is trivial.

Consumers, altruists, and switch cheaters

Let us now consider a system in which a subpopulation of consumer cells no longer differentiates. We will refer to this cell state as switch cheaters (S). The resultant three cell states can be described by the following system of equations, with an introduced consumer defection rate χ :

$$\begin{aligned}\dot{C} &= (v - \sigma - \chi)C \\ \dot{A} &= (v - \rho)A + \sigma C \\ \dot{S} &= vS + \chi C\end{aligned}$$

For this model, the red cell fraction includes consumers and switch cheaters:

$$f_{red} = f_C + f_S = \frac{C + S}{C + A + S}, \quad f_{green} = f_A = \frac{A}{C + A + S}.$$

Deriving the fractional dynamics, as above, results in the following system of equations:

$$\begin{aligned}\dot{f}_C &= f_C(\rho f_A - \sigma - \chi) \\ \dot{f}_A &= \sigma f_C - \rho f_A(1 - f_A) \\ \dot{f}_S &= \chi f_C + \rho f_A f_S\end{aligned}$$

The altruist and switch cheater fractions can be rewritten to remove the variable for the consumer fraction by assuming the three fractions sum to 1:

$$\begin{aligned}\dot{f}_A &= \sigma(1 - (f_A + f_S)) - \rho f_A(1 - f_A) \\ \dot{f}_S &= \chi(1 - (f_A + f_S)) + \rho f_A f_S\end{aligned}$$

$$\begin{aligned}f_C^* : f_C(\rho f_A - \sigma - \chi) &= 0 \\ f_C^* &= 0, 1 - f_S - \frac{\sigma + \chi}{\rho}\end{aligned}$$

$$\begin{aligned}f_S^* : \chi(1 - f_A) + f_S(\rho f_A - \chi) &= 0 \\ f_S^* &= \frac{\chi(f_A - 1)}{\rho f_A - \chi}\end{aligned}$$

$$\begin{aligned}f_A^* : \sigma \left(1 - f_A - \left(\frac{\chi(f_A - 1)}{\rho f_A - \chi}\right)\right) - \rho f_A(1 - f_A) &= 0 \\ f_A^* &= 0, \frac{\sigma + \chi}{\rho}, 1\end{aligned}$$

The only equilibrium point for this system is $(f_C^*, f_A^*, f_S^*) = (0, 0, 1)$. In this model, the green cell fraction dynamics peak at $\frac{\sigma + \chi}{\rho}$ or 1 and then decrease to zero. The red cell fraction, however, stabilizes at 1 because of the switch cheater population, which acts as a sink state.

Cheaters, altruists, switch cheaters, lysis cheaters

In the data used to fit lysis rate, f_{green} appears to stabilize at a non-zero value suggesting the presence of an additional cheater subpopulation that differentiate, but cease to lyse; we will refer to these cells as

pseudo-altruists (P). The resultant four cell states can be described by the following system of equations, with consumer defection rate χ_C and altruist defection rate χ_A :

$$\begin{aligned}\dot{C} &= (v - \sigma - \chi_C)C \\ \dot{A} &= (v - \rho - \chi_A)A + \sigma C \\ \dot{S} &= vS + \chi_C C \\ \dot{P} &= vP + \chi_A A\end{aligned}$$

For this model, the green cell fraction now includes the lysis cheaters:

$$f_{red} = f_C + f_S = \frac{C + S}{C + S + A + P}, \quad f_{green} = f_A + f_P = \frac{A + P}{C + S + A + P}.$$

Deriving the fractional dynamics, as above, results in the following relationships:

$$\begin{aligned}\dot{f}_C &= f_C(\rho f_A - \sigma - \chi_C) \\ \dot{f}_A &= \sigma f_C + f_A(\rho f_A - \rho - \chi_A) \\ \dot{f}_S &= \chi_C f_C + \rho f_A f_S \\ \dot{f}_P &= f_A(\chi_A + \rho f_P)\end{aligned}$$

If we substitute the consumer fraction in the altruist fraction dynamics as $f_C = 1 - (f_A + f_S + f_P)$, we see that the altruist fraction has a clear steady state at zero if the combined switch and lysis cheater fractions equal one:

$$\begin{aligned}\dot{f}_A &= \sigma(1 - (f_A + f_S + f_P)) + f_A(\rho f_A - \rho - \chi_A) \\ \dot{f}_A &= \rho f_A^2 - (\sigma + \rho + \chi_A)f_A + \sigma(1 - (f_S + f_P)) \\ f_A^*: \rho f_A^2 - (\sigma + \rho + \chi_A)f_A + \sigma(1 - (f_S + f_P)) &= 0, \\ f_A(\rho f_A - \sigma + \rho + \chi_A) &= -\sigma(1 - (f_S + f_P)) \\ f_A^*(f_S + f_P = 1) &= 0, \frac{\sigma - \rho - \chi_A}{\rho}\end{aligned}$$

Additionally, the switch and lysis cheater fractions only have clear non-negative steady states when the consumer and altruist fractions are zero. Unless the lysis cheater rate is zero, this system will settle on a final non-zero ratio of switch and lysis cheaters. Thus, the dynamics of the green cell fraction follow similar trajectories to the model with only switch cheaters, but with a non-zero steady state.

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