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Balanced Oscillatory Coupling Improves Information Flow

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Abstract

All animals are able to rapidly change their behavior. The neural basis of such flexibility requires that groups of distant neural ensembles rapidly alter communications with selectivity and fidelity. Low frequency oscillations are a strong candidate for how neurons coordinate communication via the dynamic instantiation of functional networks. These dynamic networks are argued to rapidly guide the flow of information, with the presumption that stronger oscillations more strongly influence information flow. Surprisingly, there is scant evidence or theoretical support for how oscillatory activity might enhance information flow. Here we introduce a novel computational model for oscillatory neural communication and show that, rather than the strength of the oscillation, it is the balance between excitatory and inhibitory neuronal activity that has the largest effect on information flow. When coupling between an oscillation and spiking has balanced excitatory-inhibitory inputs, information flow is enhanced via improved discriminability between signal and noise. In contrast, when coupling is unbalanced, driven either by excessive excitation or inhibition, information flow is obstructed, regardless of the strength of the oscillation. A multitude of neuropathologies, including Parkinson's disease, schizophrenia, and autism, are associated with oscillatory disruptions and excitation-inhibition imbalances. Our results show that understanding the distinction between balanced and unbalanced oscillatory coupling offers a unifying mechanistic framework for understanding effective neural communication and its disruption in neuropathology.

Introduction

In a loud, crowded room, determining who is saying what to whom and when can be a daunting task. This communication problem pales in comparison to the communication problem between neural ensembles in the brain. Brains have countless possible overlapping anatomical networks of varying sizes and strengths. One dominant theory for how neurons dynamically route information within and between these networks with fidelity, depending on behavioral demands, relies on neural oscillations [Fries, 2005].

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Neural oscillations are self-organized phenomenon that play an important role in cognition and neural communication [Buzsáki, 2006]. They track perception [Spaak et al., 2014], attention [Engel et al., 2001, Fries et al., 2001, Saalmann et al., 2012, Szczepanski et al., 2014], learning [Schaefer et al., 2006, Litwin-Kumar and Doiron, 2014, Ainsworth et al., 2012, Tort et al., 2009], memory [Jensen et al., 1996, Fell and Axmacher, 2011, Voytek and Knight, 2010, Voytek et al., 2013, Lisman and Jensen, 2013], and cognitive control [Cooper et al., 2015, Voytek et al., 2015], among many other behaviors and cognitive states [Wang, 2010, Womelsdorf et al., 2007a, Buschman et al., 2012]. Mechanistically, oscillations bias neuronal spiking [Womelsdorf et al., 2007b, Jia et al., 2013, Sohal et al., 2009] and are thought to aid in information flow between brain regions [Siegel et al., 2015, Buehlmann and Deco, 2010, von Nicolai et al., 2014, Voytek and Knight, 2015]. Furthermore, they have been implicated in nearly every major neurological and psychiatric disorder [Herrmann and Demiralp, 2005, Uhlhaas and Singer, 2006, Voytek and Knight, 2015, de Hemptinne et al., 2015, Allen et al., 2011, Khan et al., 2013].

The nature of excitatory (E) and inhibitory (I) neuronal interactions induce oscillations naturally and spontaneously [Buzsáki, 2006, Wang, 2010]. Balanced excitatory (E) and inhibitory (I) activity have been shown to be crucial components in the studies of effective neural communication [Vreeswijk and Sompolinsky, 1998, Ostojic, 2014], assembly formation [Litwin-Kumar and Doiron, 2012], working memory [Lim and Goldman, 2013], and neural computation [Murphy and Miller, 2009, Litwin-Kumar et al., 2011, Abbott and Chance, 2005]. By 'balanced E-I interactions' we mean that increases in excitatory firing are rapidly and exactly countered by equivalent increases in inhibition [Atallah and Scanziani, 2009], leaving the network in a fluctuation driven state [Renart et al., 2007].

While oscillations have been shown to have a facilitative role in cognition; they are also known to obstruct behavioral functioning [de Hemptinne et al., 2015]. We argue that both their facilitative and obstructive roles can be understood as a consequence of their biophysical origin. In order to understand the functional *and* pathological role that oscillations play in information flow, we need to first create a simple, generalizeable neural framework for linking oscillations and information.

We begin with a form of oscillatory entrainment or modulation of neural activity known as phase-amplitude coupling (PAC). Generally, PAC is thought to reflect rhythmic changes in neural excitability [Canolty and Knight, 2010]. When phase modulates firing rate directly, as opposed to entraining another oscillator, PAC becomes analogous to spike-field coupling and is often known as "high-gamma PAC". PAC between theta oscillations (6-12 Hz) and the high gamma frequency range (80-300 Hz) has been argued to enhance neural information flow [Siegel et al., 2015, Buehlmann and Deco, 2010, von Nicolai et al., 2014, Voytek and Knight, 2015], facilitate long-term potentiation [Hölscher et al., 1997], and improve behavioral performance [Tort et al., 2009]. Seemingly paradoxically, the presence of PAC has also been linked to clinical outcomes such as Parkinson's disease [de Hemptinne et al., 2013], schizophrenia [Allen et al., 2011], and autism [Khan et al., 2013], with clinical deep brain stimulation in Parkinson's disease associated with a reduction in Parkinsonian

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symptoms and a concomitant reduction in (presumably) pathological PAC [de Hemptinne et al., 2015].

In this simulation study, we model PAC as periodic modulation of an asynchronous, rate-based, population code. Simplified rate models of Poissonic firing have proved to be pivotal in isolating key principles of neural function [Heeger et al., 1996, Reynolds and Heeger, 2009, Mazurek and Shadlen, 2002, Bays, 2014]. This simplified approach also allows our model to encapsulate a broad class of ways in which excitatory or inhibitory oscillations might modulate firing rates [Silver, 2010]. We then use information theory to separate models that facilitate communication from those that obstruct it. We find that only models based on multiplicative gain control–a class of models that implicitly require strong and balanced E-I inputs [Chance et al., 2002, Vreeswijk and Sompolinsky, 1998, Brunel, 2000, Abbott and Chance, 2005, Womelsdorf et al., 2014]–facilitate information flow. Importantly, we identify a plausible mechanism by which this information enhancement occurs, whereby E-I balanced oscillations improve the ability of downstream neural populations to discriminate between input signal and noise.

Methods

Neural architecture

Our formalization of PAC is well characterized by an expanded version of the E-I driver-modulator framework (see [Abbott and Chance, 2005]). Our driver population is direct excitatory stimulation (population s, (Figure 1A)), which exhibits asynchronous naturalistic firing patterns (explained below). Modulation takes the form of slow (6 Hz) endogenous oscillatory activity. While previous models used balanced E-I input to implement gain control [Abbott and Chance, 2005]–*i.e.*, multiplicative scaling (modulation) of s–our model also considers modulation by strong excitation and strong inhibition (Figure 1B). Including all three forms of modulation corresponds to a complete implementation of "neural arithmetic", a well-established, perhaps canonical, view of neural computation [Silver, 2010]. In this view, changes to excitatory conductance (generically labeled with a g in the equations below) leads to a rightward shift of the neurons' tuning curves, akin to "addition" (Figure 1B, middle). Increases in inhibitory conductance lead to a leftward shift synonymous with neural "subtraction" (Figure 1B, bottom). Finally we simulate gain control as a multiplicative process characterized by a leftward and upward warping of each neurons' response function (Figure 1B, top).

Spiking in all neural populations is treated statistically, where each neuron acts as an independent time varying, *i.e.*, non-homogeneous, Poisson process. Each population has 100 neurons, though explored values between 50 and 500 do not alter the qualitative results. Beyond 500 neurons the results do change, and the advantage of gain to information flow rapidly declines, and begins to become obstructive. This size dependence suggests PAC is effective when applied only to small assemblies of neurons. Experimentally, it has been shown that assemblies in the 100-500

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size range form the basis of neural computation [MacLeod and Laurent, 1996, Litwin-Kumar and Doiron, 2014, Buzsáki, 2010].

The basic Poisson rate model is given by $\frac{r^k}{k!}e^{-r}$ where r is the firing rate (traditionally designated λ) and k is the number of spikes per time step (1 ms for all models). Diffusion processes have been suggested as a reasonable approximation to the "naturalistic" firing patterns observed in early visual areas during passive movie viewing [Mazzoni et al., 2011, Barbieri et al., 2014]. As such, firing in the stimulus population was given by, $r_s^t = r_s^{t-1} + N(0, \sigma_s)$ where $N(0, \sigma_s)$ is the normal distribution with $\sigma_s = 0.01 r_s$ and constrained so $r_s \geq 0$. Oscillatory firing was sinusoidal, where, $r_o^t = r_o^{t-1} + (\frac{r_o^{t-1}}{2}) * sin(2\pi f t)$ where f is 6 Hz. r_o was fixed at 2 Hz. To constrain the firing models closer to biological reality, an absolute refractory period of 2 ms was enforced. Note that while rate terms are explicitly functions of time (*i.e.*, $r(t)$), we use the superscript notation r^t.

The oscillation rate r_o^t modulates the stimulus r_s^t with coupling strength g. To better simplify the initial presentation, the overall model is depicted with independent E and I modulation terms, g_e and g_i (Figure 1A). However g_e and g_i can be replaced with a single term g. In the gain condition, $g_e = g_i$. In the excitatory and inhibitory conditions each term is varied independently but over the same range (Figure 1A). This new common g term then defines the coupling strength for all models (see below). Values of g were bound between 1-8, consistent with previous modeling efforts [Brunel, 2000].

Our simplified "arithmetic networks" (Figure 1) simulate changes to excitatory or inhibitory conductance by direct linear manipulation of the PAC population's rate, r_m. In EI, gain modulation was defined by $r_m^t = g * r_s^t * r_o^t$ whereas E and I modulation were defined by $r_m^t = r_s^t + g * r_o^t$ and $r_m^t = r_s^t - g * r_o^t$ respectively (see Figure 1A for a graphical depiction). Results in the figures are averages of 100 random simulation runs, each defined with its own unique but randomly initialized stimulus pattern and Poissonic neural realizations.

Information estimation

Information content was estimated from the PAC and stimulus s populations using summed population activity at every time-step (*i.e.*, in 1 ms intervals). To allow for reliable calculation of the conditional probabilities necessary for information theoretic calculations, the summed rates were discretized into 8 integer levels. Integer levels between 4 and 30 were considered, but did not alter the patterns of results we report here. Using this new activity "alphabet", entropy and mutual information (MI) were subsequently calculated with the pyentropy library [Ince et al., 2009], using the Panzeri–Treves method [Panzeri and Treves, 1996] of correcting for downward bias in estimating entropy H introduced by finite sampling of each time window.

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The definition of facilitative and obstructive PAC

In line with the conceptualization of PAC as enhancing neural communications, we offer a definition of facilitative and obstructive PAC based on a set of information theoretic inequalities. The precept is simple. Beneficial PAC should improve information flow while obstructive PAC should hinder flow. We then use the level of (Poissonic) noise present in the stimulus s itself as the baseline to compare against. We estimate this baseline by calculating the mutual information of two Poisson instantiations of the same inhomogeneous stimulus rate process, giving two spike trains s and s' (for more on the origin of s see above). Facilitative PAC, by definition, has higher MI than the baseline reference, *i.e.*, Eq 1. In contrast, obstructive PAC is defined to have decreased information flow compared the baseline 2.

$$MI(PAC, s) >= MI(s', s) \tag{1}$$

$$MI(PAC, s) < MI(s', s) \tag{2}$$

PAC-mediated changes to signal strength were assessed using d-prime $d' = (r_2 - r_1)/\sqrt{(r_1 + r_2)/2}$ where r_1 and r_2 represent firing rates. As out underlying statistical model is Poisson the divisor in our d' estimate replace uses average rate in place of the traditional variance.

PAC estimation.

The degree of phase-amplitude coupling in our models was assessed using the direct PAC estimator (see [Özkurt and Schnitzler, 2011]), a normalized version of the common modulation index [Canolty et al., 2006]. In brief, this method uses the summed product of instantaneous estimates of phase and amplitude to estimate degree of coupling. Instantaneous estimates are provided by the Hilbert transform [N. E. Huang et al., 1998]. All spectral estimation used simulated local field potentials (LFP; next section).

LFP simulation

Simulated LFPs were constructed by convolving the population firing rate summed at each time-step with a double exponential kernel tuned to match fast AMPA channel kinetics. Changes to firing rate along with an exponential post-synaptic are a reasonable, albeit simple, approximation of an LFP recording [Buzsáki et al., 2012, Barbieri et al., 2014]. Simulated LFPs were used only in spectral analyses (Figure 2).

Results

Information and oscillatory modulation

Because E-I balance has been shown to be critical for effective neural communication, considering phase-amplitude coupling under a balanced E-I framework, specifically as a gain control process [Murphy and Miller,

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2009, Abbott and Chance, 2005], would therefore be a fairly natural extension of past work. However empirical and simulation studies suggest populations of only excitatory [Cellulaire, 1992, Hansel et al., 1995] or only inhibitory neurons [MacLeod and Laurent, 1996, Wang and Buzsaki, 1996], as well as populations of both excitatory and inhibitory ensembles [Brunel and Wang, 2003, Geisler et al., 2005, Brunel, 2000, Börgers and Kopell, 2003, Tiesinga and Sejnowski, 2009], all can sustain robust oscillations across a range of frequencies (for a review see [Wang, 2010]). This suggests the oscillatory drive in PAC may come from E or I cells (middle, right panels in Figure 1a.), or from balanced E-I interaction synonymous with multiplicative gain (left panel in Figure 1a.). Therefore, we report here how each kind of entrainment, E, or I, or EI, altered information flow as function of entrainment degree (g, see *Methods*) and stimulus strength (r_s).

Balanced inputs (EI) led to an increase in information flow (see ΔMI in EI, Figure 1**d**). In contrast, information flow declined when PAC was based on excitatory firing, modeled as a linear additive increase in rate, or as an inhibitory process, *i.e.*, a subtractive decrease (see E and I, Figure 1**d**). Both the strength of coupling (g, blue) and the firing rate of the stimulus population (r_s) monotonically enhanced each model's effect on information flow. As g and r_s increased in the EI model, so too did information flow. Again, in contrast E and I saw increasing declines (Figure 1**e**).

Spectral measurement and mutual information.

Phase-amplitude coupling between slow theta and high gamma in humans was first identified in recordings of cortical tissue [Canolty et al., 2006], and continues to be assessed with a range of largely equivalent spectral methods [Tort et al., 2010]. We applied one of these methods, the direct PAC estimator (see *Methods* and [Özkurt and Schnitzler, 2011]), to an LFP estimate derived from our simulated neural population. Partially confirming the validity of our model definition, we find that all models had a degree of spectral PAC (referred to as "SC" for spectral coupling PAC) above that present in the stimulus alone (compare all models to S in Figure 2**a**).

In the E and I models, SC positively correlates with degree of coupling g ($\rho_E = 0.32$, $\rho_I = 0.51$, $p < 2 \times 10^{-16}$). Interestingly, the strongest spectral PAC was driven by inhibition (I in Figure 2**a**), which has important implications regarding the nature and interpretations of experimentally measured PAC. In contrast, for the EI model there is a negative correlation between g and SC ($\rho_{EI} = -0.39$, $p < 2 \times 10^{-16}$). These results suggest that under EI balance, increasing conductance actually reduces PAC. Notably, in all models the firing rate r_s negatively correlates with SC ($\rho_{EI} = -0.48$, $\rho_E = -0.60$, $\rho_I = -0.50$, with $p < 2 \times 10^{-16}$ all models). This relation is to be expected. The stronger the stimulus–the larger its firing rate–the the more oscillatory modulation is needed to effect it.

Changes in PAC, however, does not predict changes to information flow in any model (Figure 2**b**). Binning data by coupling strength g or firing rate r_s does not alter this null result (not shown). This is somewhat

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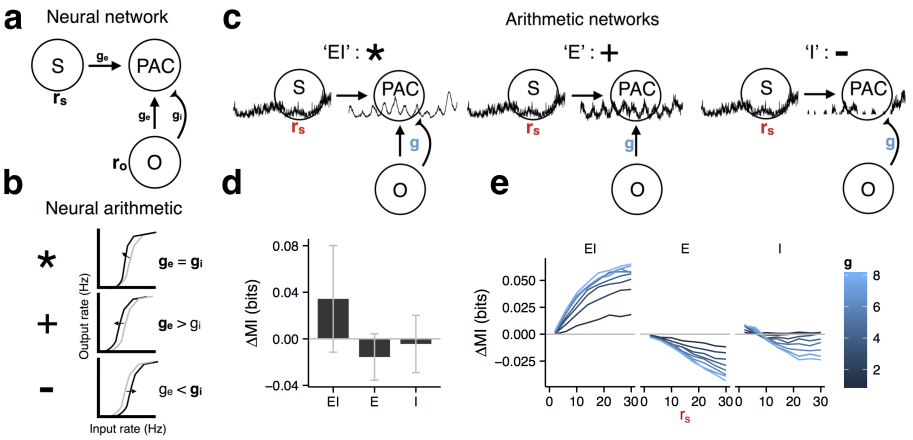

Figure 1: Phase-amplitude coupling (PAC), excitatory-inhibitory interactions, and their mutual effect on information flow in a simplified neural circuit. **a)** Diagram of a simple neural model capable of generating PAC. This model contains an excitatory stimulus population (s), which functions as a strong driver of the downstream populatio, as well as a modulatory oscillatory population (o), both of which synapse onto a third target population, PAC. All connections are completely characterized by a synaptic strength of g, and the population firing rate is given by r. **b)** Diagram of "neural arithmetic", characterized as a single neuron's input-output firing rate curve (*i.e.*, F-I curve). The top panel depicts balanced increases to both excitation and inhibition, which lead to a multiplicative increase in firing, *i.e.*, gain control ($ge = gi$). Increasing only excitation ($g_e > g_i$) leads to leftward shift of the input-output firing curve and is synonymous with addition (middle). Increasing only inhibition ($g_i > g_e$) is equivalent to a rightward shift, or subtraction (bottom). **c)** Illustration of each PAC in "arithmetic network" form. Each model is an implementation of a subset of the full model outlined in **(a)** but replacing traditional synaptic dynamics with linear changes to firing rate based on neural arithmetic operations – multiplicative (EI), addition (E), subtraction (I). Example simulated LFP time courses, of both s and PAC, are shown. **d)** Overall change in mutual information (ΔMI) for all three PAC models (see Methods). Error bars are standard deviations. **e)** Change in mutual information (ΔMI) plotted as a function of stimulus firing rate r_s and synaptic strength g (blue).

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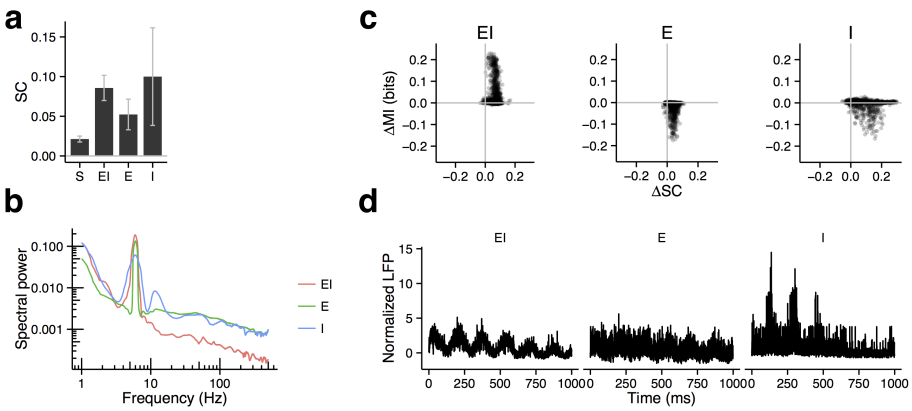

Figure 2: Spectral assessment of phase-amplitude coupling, matching the approach unused in past empirical studies, and its relation to mutual information flow. **a)** Average spectral coupling (SC) for all three PAC populations (EI, E, and I), as well as the stimulus population (S). Error bars are standard deviations. **b)** Change in PAC, ΔSC, (comparing PAC population to stimulus population) compared to the change in mutual information, ΔMI, for all simulations and parameters ($N_{total} = 6400$). Despite each condition having noticeable PAC as measured by SC **(a)**, and SC scaling with model parameters (see text), there was no significant correlation between PAC change and information flow change. **c)** Power spectrum of simulated LFPs from all three PAC models ($g = 4$, $r_s = 14$) **d)** Simulated LFPs from **(c)**.

surprising given that increased PAC is often associated with improved behavioral outcomes, except for pathological cases. This result hints at a more complex relationship between PAC and information flow. Spectral PAC methods, which relate band-passed regions of the power spectrum, may be insensitive to the spectral and temporal changes that accompany changes to information flow. SC measures were based on simulated LFPs (see *Methods*).

Information flow in temporal and spectral domains

We showed (above) that changes to information flow, changes to PAC in our models, and changes to spectral coupling are model dependent. Specifically, we find that an increase in spectral coupling is not indicative of an increase in information flow (Figure 3). In fact, the opposite pattern was frequently observed (compare Figure 2 and 3). Notably, however, it is observed from the full spectral and temporal series that facilitative PAC has distinct temporal and spectral features compared to both obstructive models and the original stimulus population (Figure 2**c** and **d**).

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Information flow and signal detection

From the point of view of downstream neuron receiving action potentials, and from the point of an information theoretic framework, reliable information transmission requires a good estimate of conditional probabilities. That is, the system needs to determine if a change in firing rate is the result of a change to the underlying neural encoding, or due to noise-driven fluctuations (Figure 3**a**). When viewing neurons as transmission devices, ideal downstream neurons should only adjust their firing to changes in signal or encoding, and not noise. Likewise, our information theoretic analyses estimate both $p(r)$, the probability of the system having rate r and $p(r|s)$, the probability of r given some input stimulus, s. The more reliable these quantities are, the better our estimate of mutual information.

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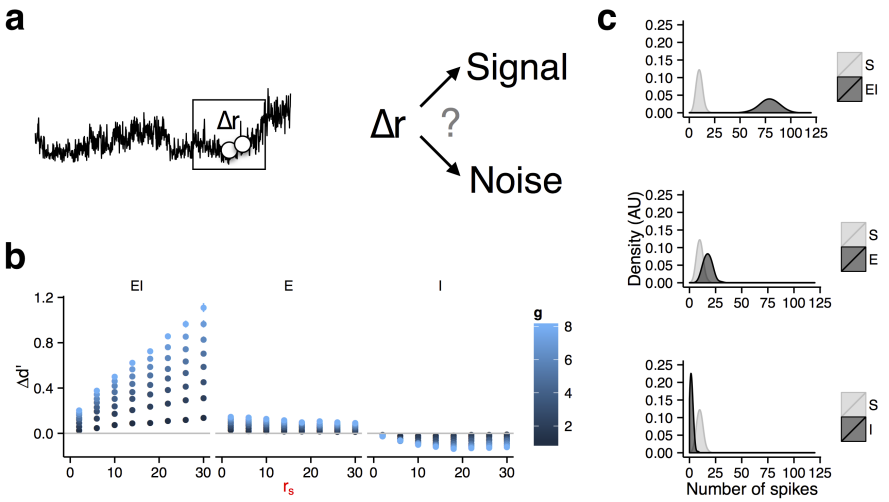

Figure 3: Signal detection theory explains the mutual information changes in our three models of phase-amplitude coupling. **a)** Illustration of rate coding as a signal detection problem. Under the rate-coding model, a critical aspect of decoding a rate-driven population is whether an instantaneous rate change is driven by the input signal, or noise fluctuations. **b)** In a rate-coding regime, we can assess the distinction between signal and noise by comparing moment-to-moment population firing rates using signal detection theory, using d'. We compare d' values between the stimulus population, S, and each PAC-modulated population, giving $\Delta d'$. This is done between each successive time-step to assess average $\Delta d'$. Error bars are standard deviations. **c)** Examples of Poisson-distributed spike rates for the stimulus population S and each PAC-modulated population at a single time point. We compare 100 Poisson draws at (rate = 10), creating distribution S (light grey). S was then transformed into distributions EI, E, or I with each transform mimicking the appropriate neural arithmetic operation (dark grey; see *Methods*). As can be seen, the average firing rate for S is approximate equal to the defined rate of 10 spikes. In the EI/gain population (top), both the firing rate and variance of the downstream population are higher than the input drive, greatly improving the signal-to-noise ratio. In contrast, oscillatory E populations only show modest signal-to-noise improvements (middle), while I populations show small decreases (bottom).

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The relation between neural arithmetic and signal detection is clearly demonstrated by comparing Poisson distributed data for a single time point, r. We compare 100 Poisson draws at $r = 2$, creating distribution S. S is then transformed into distributions EI, E, or I by the appropriate neural arithmetic operation (see *Methods*). Figure 3**c** demonstrates that multiplicative gain leads to a strong increases in separation from S. In contrast additive and subtractive alterations to to S, akin to those present in models E and I, show no change or worsening separation, respectively (Figure 3**c**).

To quantify signal separation in our neural models we measured d' (*Methods*) between each successive time-step, comparing the observed population rate for S to the three PAC models (Figure 3**b**). As expected, model EI showed consistent increases in d', increasing as a function of stimulus drive (r_s) and modulation strength (g). Model E had a slight increase, while I saw a slight decrease. When comparing trends in $\Delta d'$ to ΔMI (*i.e.*, Figure 3**b** to 1**e**) there are two notable discrepancies. For model EI, the MI effect plateaus as a function of both r_s and g. In contrast, d' scales nearly linearly. This can be explained when considering the signal detection problem in relation to information theory.

We argue that the more reliable the estimate of $p(r)$ and $p(r|s)$, the better our ability to estimate MI. However this effect has a limit. Once the probability estimates of have become sufficiently reliable, further increases to d' are of no benefit, leading ΔMI to plateau. Additionally, ΔMI decreases strongly for both E and I, but the effect on $\Delta d'$ in these models is mild. However, recall that we compared the separation of only successive estimates in rate, but the oscillatory modulation spans multiple time-steps and introduces a very different pattern than that of naturalistic firing. Without the increase in signal separation to compensate, the modulatory oscillatory pattern corrupts our estimate of $p(r)$ and $p(r|s)$, giving the observed decrease in ΔMI.

Discussion

In this modeling study we provide novel evidence that oscillatory modulation of a population of spiking neurons can actually enhance mutual information between an input signal and its neural encoding via improved neural signal detection. This enhancement requires that PAC act as a multiplicative gain modulator, a requirement synonymous with strong *and* balanced excitatory and inhibitory inputs [Chance et al., 2002, Vreeswijk and Sompolinsky, 1998, Brunel, 2000, Abbott and Chance, 2005, Atallah and Scanziani, 2009, Womelsdorf et al., 2014]. When there is an imbalance in either direction–such that PAC is driven by either excitatory or inhibitory inputs–information flow is obstructed. These results have striking implications for the role of neural oscillations in coordinating functional neural assemblies, and make a number of predictions regarding network dysfunction in neurological and psychiatric disease. Importantly, our model makes no *a priori* assumptions about the utility or function of oscillations; rather the results emerge from a purely analytic framework grounded in first principles of neuronal physiology. Our model unifies

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seemingly paradoxical results wherein PAC is related to successful cognitive function across multiple cognitive domains, but is also observed in neuropathological disorders[Voytek and Knight, 2015] including Parkinson's disease [de Hemptinne et al., 2015], autism [Khan et al., 2013], and schizophrenia [Allen et al., 2011].

Prior empirical and modeling work suggests that gain control requires strong, balanced EI connections [Abbott and Chance, 2005, Lim and Goldman, 2013, Renart and Machens, 2014]. Interestingly, in healthy tissue there are momentary fluctuations in EI balance [Knoblich et al., 2010, Chance et al., 2002, Renart et al., 2007], however, under normal conditions homeostatic mechanisms keep these fluctuations from deviating too far. One of the implications of our results is that minor alterations in EI balance may allow for functional networks to switch between subassemblies, perhaps allowing for oscillatory multiplexing of population codes [Akam and Kullmann, 2014].

Within the E-I framework, oscillations are robust, with imbalances in either excitation or inhibition favoring their formation. Given their ubiquity, the question becomes how does neural entrainment by oscillations interact with imbalances in E-I? That is, not all oscillations are equal, and under E or I imbalance, EI multiplicative coupling between a stimulus and oscillatory populations is replaced with obstructive coupling.

This model provides a way for oscillations to be re-framed in terms of their informational utility. Thus, a number of neurological and psychiatric disorders that are associated with both EI imbalances at the microscale, and oscillatory abnormalities at the meso- and macro-scales, can now be assessed in terms of disruptions in the information flow within functional networks. Notably, a PAC network is itself an oscillator that can further entrain downstream neural populations. In this sense, EI imbalance may lead to a cascade of reduced neural information exchange. This is further exacerbated by the fact that E-I imbalance itself can favor the formation of oscillatory networks, resulting in the formation of sustained pathological information flow. This is strongly reminiscent of the pathologically strong oscillatory activity and EI imbalances seen in disorders such as Parkinson's disease.

Additionally, our model successfully produces cross-frequency coupling between a low frequency phase and high gamma, a common method for assessing the functional role of oscillations. Importantly, however, cross-frequency coupling strength does not track changes to mutual information; more specifically, it does not track the temporal and spectral characteristics of gain modulation. This suggests a disassociation between spectral and functional changes.

It is notable that the system that yields the largest overall PAC is the inhibitory condition. However, despite this large PAC, there is no improvement in the mutual information between the input and the encoding population. This is likely due to the fact that the inhibitory system introduces a severe oscillation via periods of inhibition-induced silence, which comes at the cost of any possible encoding due to periods with no spiking. In contrast, in the excitatory condition there is an observed minor signal detection improvement, but relatively lower PAC. Here, it may be that relatively weaker inputs are needed to activate the encoding population,

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which, combined with weaker inhibitory modulation makes the population more susceptible to noise. This may yield a slight discrimination improvement, but at the cost of encoding accuracy.

It is common in the literature to relate increases in cross-frequency coupling to increases in communication efficiency. Our modeling suggests that this inference is not without peril. Our results (Figure 2) strongly suggest that, although oscillatory gain modulation has distinct spectral and temporal signatures, these features cannot be fully captured by narrowband cross-frequency coupling methods. Rather, the signatures for facilitative versus obstructive cross-frequency coupling may instead be best captured by studying interrelations of frequency bands in power spectra as part of a unified and temporally-sensitive system.

The time-courses of activity present under EI, E, and I conditions are distinct (Figure 1 and 4). Empirically, oscillatory "shape" (*e.g.*, peakedness and asymmetry) vary by frequency, brain region, and behavioral state. However, there exists little modeling support to guide interpretation of these non-sinusoidal features in cognition, in terms of either biologically or functionally meaningful categories. Our results suggest that time-domain, non-sinusoidal features may be critical for understanding the relationship between PAC and information flow. In other words, the common Fourier-based spectral methods–which by definition have sinusoidal basis functions–may by their sinusoidal nature be masking our ability to detect biologically-relevant changes in neural information flow.

It is important to stress that any computational modeling approach has both strong benefits and limitations. The results presented herein would be difficult to experimentally assess given the biological difficulty in driving excitatory or inhibitory neurons with high specificity. In contrast, building this computational model allows us to explore multiple forms of biologically-plausible oscillations and their effects on information flow. However, any model is limited by its underlying assumptions. Here we conceive of spiking as a statistical (Poisson) process with simplified synaptic interactions. This comes at the cost of more complex neural dynamics such as changes to spike-timing induced by oscillatory activity or caused by the tuning to information flow that can follow from activity-dependent changes to synaptic strength (*i.e.*, spike-time dependent plasticity). Nevertheless, our results offer a parsimonious explanation for a diversity of empirical PAC results in both cognition and disease. In conclusion, our model predicts that in a system of excitatory and inhibitory neurons, PAC will improve mutual information between an input stimulus and its neural encoding *only* when there is a excitation/inhibition balance. In contrast, when excitation or inhibition alone drives PAC, information flow is obstructed.

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