Dynamical Model of Drug Accumulation in Bacteria: Sensitivity Analysis and

Experimentally Testable Predictions

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Abstract. We present a dynamical model of drug accumulation in bacteria. The

model captures key features in experimental time courses on ofloxacin

accumulation: initial uptake; two-phase response; and long-term acclimation. In

combination with experimental data, the model provides estimates of import and

export rates in each phase, the time of entry into the second phase, and the decrease

of internal drug during acclimation. Global sensitivity analysis, local sensitivity

analysis, and Bayesian sensitivity analysis of the model provide information about

the robustness of these estimates, and about the relative importance of different

parameters in determining the features of the accumulation time courses in three

different bacterial species: *Escherichia coli*, *Staphylococcus aureus*, and *Pseudomonas*

aeruginosa. The results lead to experimentally testable predictions of the effects of

membrane permeability, drug efflux and trapping (e.g., by DNA binding) on drug

accumulation. A key prediction is that a sudden increase in ofloxacin accumulation

in both *E. coli* and *S. aureus* is accompanied by a decrease in membrane permeability.

Author Summary. Bacteria live or die depending on how much antibiotic gets

inside them. Using a simple mathematical model, detailed information about drug

import and export can be teased out of time courses of internal drug levels after a

sudden exposure. The results suggest that membrane permeability can suddenly

decrease during exposure to drug, accompanied by an increase, rather than a

decrease, in the internal drug level.

Introduction

Drug resistance in bacteria can be increased by efflux pump systems [1], and pump

inhibition has emerged as a strategy for overcoming drug resistance [2]. Many

details of how efflux pumps work are still unclear, however. In particular,

quantitative information about how efflux influences drug accumulation in bacteria

is still scarce [3].

Drug accumulation is a key factor in obtaining a quantitative understanding of

resistance. For example, predictions of minimum inhibitory concentrations (MICs)

of β-lactams in *Escherichia coli* were obtained by equating the steady state

periplasmic drug concentration with a periplasmic binding protein inhibitory

concentration [4]. A predicted MIC was calculated as the *external* concentration that

would yield the accumulated *internal* inhibitory concentration in steady state,

considering flux terms from membrane permeation and β-lactamase degradation.

MIC predictions also have been made considering the action of efflux pumps on

cephalosporins [5] and β-lactams [6] in *E. coli*. These predictions were accompanied

by estimates of efflux pump kinetic constants (*i.e.*, K_m and V_{max} values), providing an

explicit connection between efflux and resistance.

Time-dependent drug accumulation studies also have yielded insight into drug

transport [7-9]. Diver et al. [8] found exposure of *E. coli* to five different quinolones

induced a rapid ~10 sec uptake followed by a ~30 min phase of more gradual

accumulation. Similar two phase behavior was seen by Asuquo and Piddock [7] in

accumulation of fifteen different quinolones in *E. coli*, *Pseudomonas aeruginosa*, and

Staphylococcus aureus [7]. The experiments of Asuquo and Piddock [7] highlighted

exposure to ofloxacin, which exhibited apparently different accumulation behavior

in each species (Fig. 1). Whereas drug levels appeared to plateau in *E. coli* (Fig. 1A)

and *S. aureus* (Fig. 1C) levels in *P. aeruginosa* gradually decreased at longer times

(Fig. 1B), suggesting an acclimation process.

Mathematical modeling has provided substantial insights into accumulation of β-

lactams [4,6], cephalosporins [5], and tetracycline [9] in *E. coli*. Quinolone

accumulation, however, has not yet been analyzed in the context of a mathematical

model. Here we present a mathematical model of drug accumulation and use it to

analyze experimental data on accumulation of the quinolone ofloxacin in *E. coli*, *S.*

aureus, and *P. aeruginosa* [7]. The analysis yields estimates of permeation and efflux

rates, the time of entry into the second phase of the response, and the rate of

decrease of drug during acclimation. We also perform global sensitivity analysis,

local sensitivity analysis, and Bayesian sensitivity analysis of the model. The

sensitivity analyses provide information about the robustness of parameter

estimates and enable assessment of the relative importance of the short-term

response and long-term acclimation in different bacterial species.

The results lead to experimentally testable predictions of membrane permeability

and drug efflux, which influence drug resistance. A key prediction is that an increase

in *E. coli* and *S. aureus* drug accumulation is accompanied by a decrease in

membrane permeability. Overall the results indicate the utility of mathematical

modeling and sensitivity analysis in obtaining new insights into drug accumulation

in bacteria.

Results

Model behavior

Both the *E. coli* (Fig. 1A) and *P. aeruginosa* (Fig. 1B) behavior clearly show two

phases of drug accumulation dynamics, which is captured by our model of drug

accumulation (Methods). The model also allows for the possibility of acclimation in

the second phase; this was initially added to capture the longer-time ($\sim$10-60 min)

behavior of *P. aeruginosa* (Fig. 1b). Although *S. aureus* data initially appeared to

involve only one phase (Fig. 1C), the modeling and sensitivity analysis later revealed

a significant two-phase behavior, with acclimation.

The relationship between the model parameters and the model behavior is

illustrated in Fig. 2. After exposure at $t = 0$, the first phase begins, where cellular

antibiotic levels rise and relax toward an asymptotic value a_1. The relaxation in this

phase is exponential with rate β_1. At time $t = \tau$, the second phase begins, where

antibiotic levels may either rise or fall towards a new asymptotic value a_2. The

relaxation in this phase is initially dominated by exponential relaxation with rate β_2.

Later, acclimation can dominate the dynamics, specified by modulation of β_2 by the

factor $[1+ \delta(t- \tau)]$ (or, equivalently, modulation of α_2 by $[1+ \delta(t- \tau)]^{-1}$; see

Discussion). Together these features capture the full set of salient behaviors

exhibited by the experimental data on ofloxacin accumulation [7] (Fig. 2).

Parameter estimates

Optimal parameter values were estimated by fitting the model to data on ofloxacin

accumulation in *E. coli*, *P. aeruginosa*, and *S. aureus*. The fits were performed

assuming the same measurement error for each data point within the same curve

(Methods). Reasonable fits were obtained for all datasets (Fig. 1), with an optimal

value of the goodness of fit χ^2/NDF of 0.98, 1.5, and 0.74 for *E. coli*, *P. aeruginosa*,

and *S. aureus*, respectively. Values of β_1, β_2, and τ for *E. coli* and *S. aureus* were

surprisingly similar (Table 1) given the visible differences between the two datasets

(Fig. 1); the parameter values for *P. aeruginosa* differed from the other two cases

(Table 1). *E. coli* exhibits two phases of accumulation with little apparent long-term

acclimation, consistent with the low value of δ. *P. aeruginosa* shows a stronger

acclimation response, corresponding to the higher value of δ. *S. aureus* exhibits a

degree of acclimation (δ) that is intermediate between *E. coli* and *P. aeruginosa*.

Sensitivity analysis results

We applied three types of sensitivity analysis to the model: global sensitivity

analysis (GSA), local sensitivity analysis (LSA), and Bayesian sensitivity analysis

(BSA). The GSA yielded a fine-grained assessment of the importance of each

parameter in determining the model behavior at each time point. The LSA indicated

parameters that are responsible for the principal variations in the immediate

neighborhood of the optimal values. The BSA provided a detailed picture of the

shapes of probability distributions of parameters in a more extended range about

the optimum than for the LSA, including correlations that arise due to the nature of

the model equations. Semi-quantitative sensitivity rankings of parameters for each

case are presented in Supplementary Table S1; the detailed results are described

below.

Global Sensitivity Analysis (GSA)

GSA results were obtained using log-uniform prior distributions over the ranges in

Table 2. The results for *E. coli* (Fig. 3A,B) and *S. aureus* (Fig. 3E,F) are similar, due to

the identical priors (Table 2) and the similarity in the optimal parameter values for

these cases (Table 1). The "main effect" index (a.k.a. the first-order sensitivity index)

quantifies the contribution to the variance of the model of each parameter alone,

while averaging over variations in other parameters, whereas the "total effect" index

quantifies the change in the variance of the model caused by the investigated

parameter and its interactions with any of the other parameters (Methods). Both the

main effect and total effect are measured on a scale from 0 to 1 for each parameter.

As a reference for the following paragraphs, a_1 and a_2 correspond to the initial

steady-state level of antibiotic in the first and second phase; β_1 and β_2 correspond to

the relaxation rates at the entry into the first and second phase; τ is the time of entry

into phase 2; and δ is the rate constant associated with acclimation.

For *E. coli* and *S. aureus*, the main effect of a_1, a_2, and β_1 is high, and the main effect

of β_2, τ, and δ is low (Figs. 3A, 3E). The total effect of a_1, β_1, a_2, and τ is high, and the

total effect is low for β_2 (especially at later times) and δ (Figs. 3B, 3F). The total

effect of a_1 remains high at long times, despite being associated with the first phase;

this is because the prior for τ spans the entire range 0-3600 s, enabling the first

phase to extend to long times in the analysis.

For *P. aeruginosa*, the main effect of a_1, a_2, and δ is high, and the main effect of β_1, β_2,

and τ is low (Fig. 3C). The total effect of a_1, a_2, τ, and δ is high, and the total effect of

β_1 and β_2 is low (Fig. 3D). The increased importance of δ for *P. aeruginosa* compared

to *E. coli* and *S. aureus* is consistent with the more pronounced acclimation response

(Fig. 1). The low importance of β_1 and β_2 is consistent with the unbounded upper

limit due to the step-like transitions in *P. aeruginosa*; in comparison, the behavior of

E. coli and *S. aureus* shows more gradual relaxations with improved sampling (Fig.

1), leading to increased importance of β_1 and β_2 .

Local sensitivity analysis (LSA)

The LSA results are presented using the eigenvectors and eigenvalues of the

covariance matrix of model parameters (Methods). The eigenvectors are visualized

in columns of colored squares in Fig. 4, ordered in importance from left to right

using the eigenvalues (Table 3; sensitivity values correspond to -$\text{Log}_{10}(\lambda)$, where λ

is the eigenvalue). For all cases, the first two eigenvectors are dominated by a_1 and

a_2, indicating that these are the most sensitive parameters. For *E. coli*, the third

eigenvalue is more than 10-fold larger than the first eigenvalue (corresponding to a

lower sensitivity), with an eigenvector that is dominated by τ. The lowest

sensitivities correspond to combinations of β_1, β_2, and δ. For *P. aeruginosa*, the third

eigenvalue is 50-fold larger than the first, and corresponds to δ. The lowest

sensitivities correspond to β_1, β_2, and τ. For *S. aureus*, the third eigenvalue is 100-

fold larger than the first, and corresponds to β_1. The lowest sensitivities correspond

to combinations of β_1, δ, and τ. The relatively low sensitivity of τ in the LSA is

consistent with the very sharp transition between the two phases, as the precise

value of τ is ill-determined between the discretely sampled time points. The higher

sensitivity of τ for *E. coli* is consistent with the extrapolation of the phase 2

relaxation curve to a more precise value of τ.

Bayesian sensitivity analysis (BSA)

We used BSA with Markov Chain Monte Carlo (MCMC) sampling (Methods) to obtain

insight into probability distribution functions (PDFs) of parameter values (Figs. 5-7).

Because the measurement errors were not available for individual data points, we

used an arbitrary error of 1 ng/mg for each data point (Methods). The resulting

PDFs therefore should not be interpreted as actual posterior PDFs, but only as

indicators of: (1) the overall shape of the distributions; (2) the relative degree to

which different parameters are constrained; and (3) the relative degree and nature

in which different parameters are correlated.

The parameters β_1, β_2, and τ in *P. aeruginosa* have relatively flat PDFs that deviate

substantially from a normal distribution (Fig. 6). Sharpening the likelihood function

by decreasing the errors 10-fold led to sharper PDFs for peaked distributions

(Supplementary Figs. S1-S3) while maintaining similarly flat distributions for these

parameters (Fig. S2), providing evidence that the flat distributions are not an

artifact of the sampling.

The individual PDFs for the parameters of both *E. coli* (Fig. 5) and *S. aureus* (Fig. 7)

all show peaks, which is justification for the providing the estimates for all

parameters in Table 1 (the distribution of β_2 for *S. aureus* is truncated at low values

due to the restricted range of the prior; however, the peak clearly falls within the

range of the prior when the likelihood function is sharpened (Supplementary Figure

S3)). The range of the values of β_2 and δ among the MCMC sampled points (an

indicator of the width of the PDFs) is greater than for other parameters (Table 4),

indicating that estimates of β_2 and δ are less reliable (there is a noticeable tail in the

a_2 distribution for *E. coli*, but the range of 0.14 Log_{10} units is still sufficiently narrow

to provide an estimate). The pairwise scatter plots indicate relatively strong

correlations between a_2 and both β_2 and δ. These correlations follow from Eq. (4), in

which both β_2 and δ appear in factors that multiply a_2; a weaker correlation

between δ and β_2 is explained by the same term. The correlations involving δ are

only substantial when δ is sufficiently large; this is because the effect of δ is

negligible when it is smaller than about 10^{-5} s^{-1} (Eq. 4, considering the experiment

duration of 3600 s). In addition, β_1 appears in the term modulating a_1 in Eq. (4),

explaining a weak correlation between these two.

Like for *E. coli* and *S. aureus*, the PDFs of a_1, a_2, and δ for *P. aeruginosa* show peaks

(Fig. 6), justifying the entry of estimates in Table 1. In addition the PDF for τ,

although flat, is confined to a very narrow range, leading to an estimate in Table 1.

The lack of a peak for τ can be understood by the sharp, step-like increase (Fig. 1B)

combined with the discrete sampling in time; i.e., the step can be located anywhere

between the time points that mark the increase, with approximately equal

probability. Step-like increases in accumulation also lead to high uncertainty in both

β_1 and β_2 (Table 4); these parameters can assume essentially any value that is large

enough to enable the antibiotic to rise between the time points that mark the

increase, with equal probability. Like for *E. coli* and *S. aureus*, a_2 and δ are correlated

for *P. aeruginosa*; however, compared to *E. coli* and *S. aureus*, increased uncertainty

masks any underlying correlations involving β_1 and β_2.

Predictions of permeability, net efflux rate, and accumulation factor

We used Eqs. (5)-(7) to predict the values of parameters that directly characterize

permeation, net efflux, and the degree of drug accumulation. The predictions are

quantified in the form of the permeability α_i in each phase i, the net efflux rate ε_i,

which is defined as the portion of the specific export rate not associated with

permeation, and the accumulation factor, ϕ_i, which is the fold-increase of antibiotic

concentration inside the cell compared to the external concentration. A positive

value of ε is associated with a net efflux and a value $\phi<1$, while a negative value is

associated with a net trapping of drug and a value $\phi>1$. The total value of ε can be

determined by a combination of individual positive or negative fluxes, potentially

involving multiple mechanisms including efflux pumps and drug binding to DNA

(Discussion).

The resulting predictions of α_i, ε_i, and ϕ_i are shown in Table 5. Predictions of α_i and

ε_i for *P. aeruginosa* are provided as lower bounds, following from the entries for β_i in

Table 1. The true reliability of the predictions of ϕ_i depends both on the robustness

of the estimation of a_i (Sensitivity analysis results) and the uncertainty in the factor

used to convert a_0 to ng/mg dry weight units (Methods). The reliability of the

predictions of α_i, ε_i additionally depends on the robustness of the estimation of β_i.

The predictions of permeability behavior are strikingly similar for *E. coli* and *S.*

aureus. At early times, the permeability is high, corresponding to about a 5.5 s half-

equilibration time for *E. coli*, and a 1.5 s half-equilibration time for *S. aureus* (α_1

from Table 5). The permeability then decreases dramatically after about 12.5

minutes (τ from Table 1): by a factor of ~50 for E. coli and a factor of ~100 for S.

aureus (α_2/α_1 from Table 5). In addition, the value of ε at both early and late times is

negative for both *E. coli* and *S. aureus*, and the values of ϕ are greater than one,

indicating a net trapping of antibiotic.

In contrast to *E. coli* and *S. aureus*, the values of ϕ are less than one for *P. aeruginosa*,

indicating a net efflux of antibiotic. The lower bound of α_1 for *P. aeruginosa* is

consistent with *E. coli* and *S. aureus* but the lower bound of α_2 is higher by a factor

O(10). The upper bounds of ε for *P. aeruginosa* are consistent with the estimates for

E. coli and *S. aureus.*

Discussion

The present modeling and analysis of ofloxacin accumulation time courses indicates

that *E. coli* and *S. aureus* exhibit a similar two-phase ofloxacin accumulation

behavior. Whereas the two-phase behavior for *E. coli* was easily visible in the data,

for *S. aureus* it was only detected as a result of the BSA. Even though the change in

antibiotic level entering phase 2 is small for *S. aureus*, the BSA indicates a clear peak

in the posterior distributions of all of the influx and outflux parameters, increasing

confidence in the two-phase model for this case (Fig. 7).

The contribution of sensitivity analysis to the present study was substantial. The

BSA enabled us to identify a significant two-phase model for *S. aureus* that we were

unable to detect in the data by eye. In addition, the BSA enabled us to identify

correlations in the data that are consistent with the way the parameters work

together in the model. We also note that the lack of individual error estimates for

each data point in the present study prevented calculation of true posterior PDFs;

the availability of error estimates for future datasets will enable a substantial

increase in the information provided by the BSA. The sensitivity analysis also

enables a quantitative means of distinguishing of important from unimportant

parameter values in the modeling. This further enables a degree of confidence to be

associated with results based on the quantitative analysis, which can be used to

assess which predictions are more or less likely. Some aspects of the sensitivity

analysis confirm what is already apparent in just looking at the data, such as the

increased importance of δ for *P. aeruginosa* compared to *E. coli*; however, even in

this case, it provides quantitative measures that can enable obvious results to be

obtained automatically. Automation will become increasingly important as we

increase the number of data sets being analyzed. In addition, future data sets might

not be as straightforward to interpret by eye, and the present study serves as an

example that demonstrates the consistency of the sensitivity analysis with the

interpretation of a relatively clear-cut case, so that the methods can be applied with

increased confidence to cases where the interpretation might not be so obvious.

The rapid initial accumulation of ofloxacin in *E. coli*, *P. aeruginosa*, and *S. aureas* has

been cited as evidence that these bacteria lack a substantial permeability barrier for

fluoroquinolones [7]. Our modeling supports the high permeability at early times in

the accumulation dynamics. The permeation rates in Table 5 lead to a half-

equilibration time for ofloxacin permeation of 5.5 s into *E. coli*, <18 s into *P.*

aeruginosa, and 1.5 s for *S. aureus*. These values are similar to the expected 5 s half-

equilibration time for permeation of norfloxacin across a lipid bilayer [10]; as

measured in Ref. [7], the apparent partition coefficient of ofloxacin is 4-fold greater

than that of norfloxacin, so their permeabilities across the cytoplasmic membrane

are expected to be within a similar range.

In contrast with the early time behavior, after about 12.5 mins, both *E. coli* and *S.*

aureus show a predicted 50-to-100-fold decrease in permeability (Table 5). This

sudden decrease in permeability only was detected using the modeling and was not

detected in the prior qualitative analysis of the data [7]. One way to test this

prediction is to shift the cells to a medium with radiolabeled drug, looking for a

difference in labeled drug accumulation in phase 1 versus phase 2. At this point we

can only speculate about the mechanism. *E. coli* is gram negative, whereas *S. aureus*

is gram positive, suggesting the common decrease in permeability does not involve

the outer membrane. That the permeability rates are consistent with diffusion

across the cytoplasmic membrane indicates that the decrease in permeability is not

necessarily be associated with transporters. It is possible that the sacculus, a mesh

structure common to both *E. coli* and *S. aureus*, might be involved in a decrease in

permeability. The ability of the sacculus to allow translocation of proteins as large as

25 kDa [11] or 100 kDa [12] would seem to rule out a role for the sacculus by itself,

as ofloxacin has a molecular weight of 361 Da, and should ordinarily freely diffuse

across the mesh. However, the sacculus is associated with a comparable mass of

other biomolecules in both gram negative and positive bacteria [13] [14]. If ~98%

of the mesh were to become blocked somehow, it could explain the ~50-fold

decrease in permeability for *E. coli.*

For *E. coli* and *S. aureus*, the values of the accumulation factor $\phi>1$ indicate net

trapping of antibiotic. The trapping is weak for *E. coli* in phase 1 (ϕ_1=1.09) and

becomes stronger in phase 2 (ϕ_2=2.29). Compared to *E. coli*, the trapping is stronger

in *S. aureus* for both phases: ϕ_1=2.93 and ϕ_2=3.75. For *P. aeruginosa*, the values of

$\phi<1$ indicate a net efflux of antibiotic that is stronger in phase 1 (ϕ_1=0.39) than in

phase 2 (ϕ_2=0.72).

Several individual effects can combine to determine whether there is a net trapping

or efflux of antibiotic. Targeted experiments will be required to determine the role

of specific mechanisms, but we can gain some insights by assuming that an

important effect favoring trapping is the immobilization of antibiotic on DNA. This

effect can be estimated using the dissociation constant K_D = 633 µM reported by

Shen et al. [15] for nonspecific binding to DNA of norfloxacin at high concentrations

(10-1000 µM). Assuming roughly 2.1 genome equivalents per cell [16], a volume of

1.25 fL, and 4.7 x 10^6 bp per chromosome yields an estimated DNA bp concentration

in *E. coli* [D] = 1.3 x 10^4 µM. Then, assuming the K_D for norfloxacin applies to

ofloxacin and that each bp can bind one drug molecule yields a fraction of DNA-

bound drug of $1/(1+K_D/[D])$ = 0.95, or a mobile fraction of just 0.05. In this case, the

contribution of permeability to the outflow would be only 5% of that assumed in Eq.

(6), leading to an increase in efflux by 0.95α. This translates into an increase in the

specific efflux rate by 0.12 s^{-1} for *E. coli* in phase 1.

Based on the above estimates, despite the small negative value of the net efflux

parameter ε_1 (= -0.011 s^{-1}) in Table 5, due to the effect of trapping by DNA binding,

we expect the underlying rate of efflux in *E. coli* to be 0.11 s^{-1} (= 0.12 s^{-1} - 0.011 s^{-1}),

which is comparable to the rate of permeation. To assess the importance of efflux in

S. aureus, we use similar reasoning as for *E. coli*, noting that the net efflux parameter

ε_1 is -0.326 s^{-1} and the effective permeability α is 0.495 s^{-1} (Table 5). Assuming the

same degree of trapping in *S. aureus* as in *E. coli* yields a contribution 0.48 s^{-1} and an

estimated specific efflux rate of roughly 0.15 s^{-1} (= 0.48 s^{-1} - 0.326 s^{-1}) in phase 1,

which is close to the value for *E. coli*. In contrast to *E. coli*, however, where the efflux

rate is comparable to the inflow rate, in *S. aureus* the efflux rate is less than 1/3 of

the inflow rate.

The estimated specific efflux rates in phase 1 of 0.11 s^{-1} for *E. coli* and 0.15 s^{-1} for *S.*

aureus can be used to estimate the rate of outflow of drug due to efflux. Multiplying

by a_1 yields an outflow of 3.5 ng/mg/s (= 0.11 s^{-1} x 32 ng/mg) for *E. coli*, and 10

ng/mg/s (= 0.15 s^{-1} x 66.6 ng/mg) for *S. aureus*. Dividing by the molecular weight of

ofloxacin (361.368 g/mol) yields 0.0097 nmol/mg/s for *E. coli* and 0.028

nmol/mg/s for *S. aureus*. These values are similar to the V_{max} value of 0.0235 ± 0.003

nmol/mg/s found by Lim and Nikaido [6] for efflux of nitrocefin from *E. coli*, and are

much lower than the value of 1.82 ± 0.85 nmol/mg/s found for cephaloridine efflux

from *E. coli* in the same study. Therefore our predictions are consistent with the V_{max}

for efflux of ofloxacin in *E. coli* and *S. aureus* being similar to the V_{max} for efflux of

nitrocefin in *E. coli*.

In addition to DNA binding, differential permeability of ionic subspecies of ofloxacin

or Mg2+ chelates of ofloxacin might also influence the balance of inflows and

outflows [10]. These effects can easily lead to two-fold or greater accumulation or

exclusion of antibiotic [10]. In addition to the predicted change in membrane

permeability, therefore, changes in DNA binding, efflux, pH, and the availability of

Mg2+ all might potentially be linked to the two-phase behavior of ofloxacin

accumulation.

Because we predict that the underlying efflux rate is comparable to the inflow rate

in *E. coli*, we also predict that efflux plays an important role in ofloxacin

accumulation. In contrast, for *S. aureus*, we predict efflux plays a less important role

in ofloxacin accumulation, because the efflux rate is predicted to be substantially

lower than the inflow rate. For *P. aeruginosa*, we are unable to make predictions

based on quantitative estimates of rate constants, due to uncertainty in the key

parameter values in Table 1 and Table 5. However, because the internal

concentration of antibiotic is predicted to be less than the external concentration (ϕ

< 1 in Table 5), we predict that efflux is important in *P. aeruginosa* accumulation of

ofloxacin.

Both *P. aeruginosa* and *S. aureus* exhibit a visible slow decrease in accumulated drug

during the second phase (Fig. 1). The model captures this decrease in terms of the

parameter δ which increases β_2 by a factor $[1 + \delta(t - \tau)]$ in Eq. (3). Mechanisms for

increasing β include enhancing efflux (e.g., by increased expression of pumps) or

decreasing trapping (e.g., by chromosome remodeling that results in a decrease in

drug binding to DNA). Importantly, the combination of Eq. (4) and Eq. (5) indicate

that δ can be interpreted alternatively as decreasing α_2 by a factor $[1 + \delta(t - \tau)]^{-1}$.

Thus, in addition to an increase in efflux or a decrease in trapping, the acclimation

behavior can be attributed to a decrease in permeability (e.g., through the

hypothetical mechanisms described above). Additional experiments targeted at the

mechanism of decrease will be required to determine the cause of the acclimation

response.

Ofloxacin is bactericidal at the concentration of 10 mg/L used in the experiments [7],

which might have important implications for the interpretation of the results. If

nonviable cells are excluded from the analyzed pellet after centrifugation (e.g.

because they have been lysed and remain suspended), the accumulation data simply

correspond to viable cells, and the interpretation is straightforward. If nonviable

cells are included in the pellet, the interpretation depends on the relative

populations of viable and nonviable cells. According to Ref. [7], 5 mins after

exposure in phosphate buffer, the viable count of *E. coli* decreased by 0.74 Log_{10}

units, the count of *P. aeruginosa* decreased by 0.45 Log_{10} units, and the count of *S.*

aureus decreased by 0.4 Log_{10} units. These data indicate that in all cases, the number

of viable cells decreases by at least 2.5-fold after 5 mins. At the longest times, 60

mins after exposure, the values were 2.06, 3.75, and 0.54 Log_{10} units, respectively,

indicating that the number of viable cells of *E. coli* and *P. aeruginosa* decreases by at

least 100-fold over the course of the experiment. These results indicate that if

nonviable cells are included in the analyzed pellet, the behavior should be

dominated by the nonviable cells; indeed, trapping of antibiotic in nonviable cells

removes antibiotic from the environment and can increase the chance of survival of

neighboring viable cells, leading to a fitness advantage at the population level.

That the model matches the data well (Fig. 1) is consistent with the interpretation

that the behavior is predominantly due to one type of cell, either viable or nonviable.

However, the killing kinetics do indicate that the number of viable cells is still not

negligible at early times for all cells, and at late times for *S. aureus*. In addition,

including the effect of antibiotic on cell growth and death will be critical to

connecting the present results to drug resistance. Future work should therefore

include investigating an expanded dynamical model that includes subpopulations of

viable and nonviable cells, including the dependence of cell growth (for

bacteriostatic effect) and death (for bactericidal effect) on intracellular antibiotic

concentration. Including the antibiotic effect (e.g., via the target inhibitory

concentration [4-6]) is essential for understanding the relation between the amount

of accumulated drug and antibacterial activity, as they are not necessarily correlated

[7]. In particular, Nagano and Nikaido [5] used mathematical modeling to predict

MIC values of drugs for *E. coli*, and to show how efflux pump deletion or

overexpression might not change the MIC value of drugs that are nevertheless

strong efflux pump substrates.

It is interesting to consider the importance of models of drug accumulation in light

of a recent survey of physical properties of active compounds in a drug screening

collection and their relation to whole cell antibacterial activity [17]. The survey

reported on the difficulties encountered in simultaneously optimizing both

biochemical potency and antibacterial activity, and concluded that "what is clearly

needed is greater insight into medicinal chemistry strategies which optimize

transport through porins and decrease efflux through the prolific efflux pumps."

Together, the findings reported here and elsewhere [5,6] suggest that mathematical

modeling of drug accumulation can provide these insights, and thus can be a key

tool in enabling antibacterial medicinal chemistry.

Materials and Methods

Model

Our dynamical model of drug accumulation lumps together transport across the

inner and outer membranes. This is appropriate as the drug target is in the

cytoplasm, there are no data on drug accumulation in the periplasm, and we wish to

use the same model for gram positive or negative bacteria. We note that this

lumping does not prevent the interpretation of results in light of differences

between the outer and inner membranes (Discussion).

The time dependence of accumulated drug $a(t)$ is modeled using

$$\frac{da(t)}{dt} = \alpha(t)a_o - \beta(t)a(t) \tag{1}$$

where a_o is the environmental antibiotic concentration, $\alpha(t)$ is the specific rate of

increase, and $\beta(t)$ is the specific rate of decrease. The term "specific" is used to

indicate that the rate constant is multiplied by the antibiotic concentration. We

assume $\alpha(t)$ corresponds to the permeability, although it also can include active

transport. We assume $\beta(t)$ corresponds to both active and passive transport,

although it also can include degradation and cell growth. Cell growth in *E. coli* occurs

by a constant cell size extension [18], which is consistent with including cell growth

in β. If included, assuming a 42 min doubling time, cell growth would contribute a

specific rate of 2.75 x 10^{-4} s^{-1}; this is orders of magnitude smaller than the values of

β at early times (Table 1), when growth is expected to be highest, and is at least 4-

fold smaller than the values of β at early times (Table 1), when growth is expected to

be lowest. Ignoring cell growth therefore is a reasonable approximation in the

present study, although it might be necessary to include it in other studies.

Equation (1) was developed assuming that only viable cells are analyzed. This

corresponds to the case when nonviable cells are disrupted and are excluded from

pellet after centrifugation in Ref. [7]. Even when nonviable cells are not excluded

from analysis (Discussion), Eq. (1) applies to viable cells when the external

antibiotic level is low and there is a negligible fraction of nonviable cells at all times.

If nonviable cells are included in the pellet and there is a negligible fraction of viable

cells at all times, Eq. (1) will still be relevant but will instead describe accumulation

in the nonviable cells. If both viable and nonviable cells are analyzed and there is an

intermediate drug concentration, the model should be extended to include both

viable and nonviable cells, with population dynamics (Discussion).

To model the data in Fig. (1), we assume α(t) and β(t) both switch rapidly from a

constant value in phase 1 to a different constant value in phase 2. The import rate

α(t) is given by

$$\alpha(t) = \begin{cases} \alpha_1, & t < \tau \\ \alpha_2, & t \geq \tau \end{cases}$$ (2)

494   where α_1 applies to the early phase of the accumulation dynamics (t<τ), and α_2

495   applies to the late phase (t ≥ τ).

497   The export rate β(t) is given by

$$\beta(t) = \begin{cases} \beta_1, & t < \tau \\ \beta_2[1 + \delta(t - \tau)], & t \geq \tau \end{cases}$$ (3)

500   where β_1 applies during the early phase (t<τ), β_2 applies during the late phase (t≥τ),

501   and δ is the fractional rate of increase of export during the later phase.

503   Assuming rapid relaxation (β_2) compared to acclimation (δ) in phase 2 yields

$$a(t) = \begin{cases} e^{-\beta_1 t}a(0) + \left(1 - e^{-\beta_1 t}\right)a_1, & t \leq \tau \\ e^{-\beta_2(t-\tau)}a(\tau) + \left[1 - e^{-\beta_2(t-\tau)}\right]\dfrac{a_2}{1 + \delta(t - \tau)}, & t > \tau \end{cases} \quad (4)$$

where $a_1 = \alpha_1\, a_o/\, \beta_1$, and $a_2 = \alpha_2\, a_o/\, \beta_2$.

Given additional assumptions, the α and β parameters can be used to derive

permeation and net efflux rates (see below). The δ parameter models long-term

acclimation by, e.g., gene regulation.

Parameter estimation

Parameter estimation for Eq. (4) was performed using published experimental time

courses of ofloxacin accumulation in *E. coli*, *P. aeruginosa*, and *S. aureus* [7]. Data

points were extracted from Figure 1 in Ref. [7]. Numerical solutions to Eq. (4) were

obtained for each data point using functions defined in Mathematica Version 10

(Wolfram Research, Inc., Champaign, IL). Errors for each individual data point were

not available, and were therefore estimated using the maximum values given for

norfloxacin in Ref. [7]: ±12.5, ±11.6, and ±9.7 ng/mg for *E. coli*, *P. aeruginosa*, and *S.*

aureus, respectively. To obtain error estimates for ofloxacin, these maximal errors

were scaled using the initial rapid phase concentration entries in Tables II, III, and

IV of Ref. [7], and were then divided by two. The following were the resulting

estimated errors for each data point: 2.3 ng/mg for *E. coli*, 0.75 ng/mg for *P.*

aeruginosa; and 4.35 ng/mg for *S. aureus*. We also performed the fits using the

maximal errors as the estimates, without dividing by two; however, we favored

using the half-maximal errors for the following reasons: (1) the maximal values are

very likely overestimates; and (2) the half-maximal values yielded χ^2/NDF values

close to 1, whereas the maximal values yielded values substantially lower than 1.

The choice of errors between these cases merely resulted in a different overall

scaling χ^2 and did not influence the optimal parameter values obtained in the fits.

A standard χ^2/NDF was used as a goodness of fit measure between the model and

the data, using a number of degrees of freedom NDF = number of data points minus

six parameters. The χ^2/NDF was minimized with respect to values of a_1, a_2, β_1, β_2, δ,

and τ using the `FindMinimum` method, assuming a(0)=0. The values of a_1, a_2, β_1, β_2,

δ were varied over twelve decades. For *E. coli* and *P. aeruginosa*, the value of τ was

varied from 0-10,000 s (covering the full span of each 3,600 s time course) to seek

an optimal solution. For *S. aureus*, optimization was initially performed for τ =

10,000 s (a time beyond the last data point), as the behavior appeared to be one

phase. A more thorough investigation of the parameter space using Bayesian

sensitivity analysis (BSA), however, revealed a relatively weak but significant two-

phase response, with a value of τ that is similar to *E. coli*. Therefore the optimization

for *S. aureus* also was performed varying τ from 0-10,000 s. Mathematica

workbooks and experimental data for all cases are available in a compressed

archive in the Supporting Information.

Sensitivity analysis methods

All sensitivity analyses were performed using the open source code Model-Analysis

and Decision Support (MADS), developed at Los Alamos National Laboratory

(http://mads.lanl.gov).

Global Sensitivity Analysis (GSA): We performed variance-based GSA [19], which

decomposes the variance of the output into parts ascribed to different input

parameters using a Fourier Haar decomposition [20,21]. Both the "main effect " and

the "total effect" results presented here for each input parameter were calculated

using the Sobol Monte Carlo algorithm [22] using about 10^6 independent model

evaluations drawn from log-uniform distributions defined by Table 2. We found that

this number of samples was sufficient to achieve convergence for the estimated

quantities. The ranges in Table 2 were chosen arbitrarily to encompass the optima

in Table 1 while exploring a reasonably broad region of parameter space and

satisfying the requirement of rapid relaxation (β_2) compared to acclimation (δ) in

phase 2 for Eq. (4).

Local Sensitivity Analysis (LSA): LSA has a rich history of use in assessing the

robustness of biochemical network model behavior to changes in parameter values

[23,24]. In LSA, the local gradients of the model output are calculated with respect

to model parameters at a fixed point (the point with the lowest χ^2). Here we use the

gradients to define a covariance matrix of variations [25]. We used a finite

difference method requiring a limited number of model evaluations (equal to the

number of unknown parameters). As a result, we obtain a gradient matrix **J** (i.e. the

Jacobian) with dimensions $[m \times n]$ where m is the number of model parameters and

n is the number of model inputs (we use logarithmic derivatives, to obtain an

analysis in terms of dimensionless parameters). Each component of the **J** matrix

represents the local sensitivity of each model parameter to each model output [25].

We analyze the covariance matrix **C** of model parameters which is computed as **C** =

$[J^TJ]^{-1}$. The covariance matrix is analyzed using eigenanalysis where eigenvectors

and eigenvalues of the covariance matrix are explored. How dominant (important)

is each eigenvector depends on the respective eigenvalues; the smaller the

eigenvalue, the higher the importance of the eigenvector. The components of each

eigenvector represent the contributions of each model parameter to the

simultaneous variation of multiple parameters: the larger the absolute value of the

components, the larger the contribution. Model parameters with a large

contribution in dominant eigenvectors are important (sensitive) model parameters.

Model parameters with large contribution in non-dominant eigenvectors are

unimportant (insensitive) model parameters. If several model parameters have an

important contribution in a single eigenvector, these model parameters are

correlated. If these contributions have the same sign, the correlation is positive. If

these contributions have opposite signs, the correlation is negative.

Bayesian Sensitivity Analysis (BSA): Posterior probability density functions (PDFs) of

the model parameters given observed data (Figs. 5-7) were obtained following

Bayes' theorem [26,27]. The PDFs were obtained using a log-uniform prior with the

ranges indicated in Table 2, with a likelihood function defined as $e^{-\chi^2/2}$, using an

arbitrary error value of 1 ng/mg for each data point. The error was decreased to 0.1

ng/mg to demonstrate the effect of sharpening the likelihood function in

Supplementary Figs. S1-S3. The BSA was performed using the Robust Adaptive

Metropolis Markov Chain Monte Carlo (MCMC) algorithm [28]. Analysis was

performed using sample sizes of 10^4, 10^5, and 10^6; we found a sample size of 10^6

yielded adequate sampling. The posterior PDF scatter plots (off-diagonal panels in

Figs. 5-7) show an overlay of individual counts; the extent of the plots reflects the

parameter range over which 10^6 random samples can fall. The posterior parameter

ranges in Table 4 were obtained by identifying the minimum and maximum

parameter values among 10^6 points sampled using the MCMC. (The values in Table 4

must be interpreted in light of the fact that the range might increase with increasing

number of samples, and that the precise values can change depending on differences

in sampling, e.g., using different random number seeds.) The histograms (diagonal

panels in Figs. 5-7) indicate the shape of the individual marginalized PDFs using the

number of counts on the y-axis.

Predictions of permeability, net efflux rate, and accumulation factor

Estimation of the model parameters enables prediction of permeability and efflux

rates. Given a_o, the specific import rate α_i in each phase *i* may be calculated as

$$\alpha_i = a_i \beta_i / a_0. \tag{5}$$

617   Assuming the import is due to permeation, α_i is the permeability. Next, assume the

618   specific export rate β is a sum of contributions from permeability, α and other

619   effects. The other effects are then captured by the difference ε between β and α:

$$\varepsilon_i = \beta_i - \alpha_i. \tag{6}$$

622   When $\varepsilon_i > 0$, outward flow is enhanced compared to permeation, and ε_i indicates a net

623   efflux. When $\varepsilon_i < 0$, the outward flow is decreased compared to permeation, and ε_i

624   indicates a net trapping of drug.

626   Finally, the accumulation factor ϕ is used as a measure of the degree to which

627   antibiotic is either accumulated in or expelled from the cell. It is given by

$$\phi_i = a_i / a_o. \tag{7}$$

If $\phi_i < 1$ the internal antibiotic concentration is less than the external antibiotic,

which is associated with net efflux ($\varepsilon_i > 0$). If $\phi_i > 1$ the internal antibiotic exceeds

the external antibiotic, which is associated with net trapping ($\varepsilon_i < 0$).

Eqs. (5)-(7) are only valid under the same assumptions as for Eq. (4). Predictions of

α_i and ε_i are only meaningful using reliable estimates of both a_i and β_i . In contrast,

ϕ_i can be predicted just with estimates of a_i and a_o.

The predictions use the environmental drug concentration a_0 in ng drug/mg dry

weight units. The external ofloxacin concentration in the experiments was 10 mg/L

[7]. To convert to ng/mg dry weight units, following Ref. [29], we used a buoyant

density of 1.1 g/mL and a 31% dry weight for *E. coli*, a buoyant density of 1.2 g/mL

and a 48% dry weight for *P. aeruginosa* (transferred from *P. putida*), and assumed a

buoyant density of 1.1 g/mL and a 40% dry weight for *S. aureus*. This yielded

conversion factors of 0.341 (mg drug/L)/(ng drug/mg dry weight) for *E. coli*, 0.528

for *P. aeruginosa*, and 0.440 for *S. aureus*. The uncertainty in the dry weight fraction

for *S. aureus* should be estimated at about 25%, given the range spanned by *E. coli*

and *P. aeruginosa*. This introduces uncertainty in the predictions beyond those

indicated by the sensitivity analysis alone.

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Figure Captions

Figure 1. Ofloxacin accumulation data (open squares) with model fits (solid lines).

A) *E. coli*. B) *P. aeruginosa*. C) *S. aureus*. Each data point is assumed to have the same

measurement error, estimated from the maximum values reported for norfloxacin

in Ref. [7] (vertical bars)*.* The external drug concentration of 10 mg/L is shown in

each panel in ng/mg units (dashed straight lines), converted using the factors

derived from the buoyant densities and dry fraction (Methods). The x-axis is plotted

using a log scale, reflecting the time sampling of the data.

Figure 2. Behavior of the model and connection to parameters.

Figure 3. Global sensitivity analysis results for *E. coli* (A, B); *P. aeruginosa* (C, D); and

S. aureus (E, F) models. The left panels (A, C, E) show the main effect results, and the

right panels (B,D,F) show the total effect results. Color code: a_1 (cyan); a_2 (yellow);

β_1 (magenta); β_2 (green); δ (lavender); and τ (red).

Figure 4. Local sensitivity analysis (LSA) results for A) *E. coli*; B) *P. aeruginosa*; and

C) *S. aureus*. Columns correspond to eigenvectors, ordered left to right from the

most to the least sensitive, as in Table 3. Rows correspond to parameters, with

labels indicated at the left. The strength and sign of the coefficient of each parameter

with each eigenvector is indicated using the color code in the legend to the right.

Figure 5. Bayesian sensitivity analysis for $E.\ coli$. Pairwise parameter PDFs are

shown using scatter plots in off-diagonal panels; Monte Carlo sampled points

illustrate the extent of the PDFs in the space of parameter values indicated on the x-

and y-axes. Panels in transposed positions within the grids contain identical

information with the x- and y-axes swapped. PDFs for individual parameters are

shown on the diagonals using histograms, with the number of counts in each bin

(out of 10^6 total samples) indicated on the y-axis.

Figure 6. Bayesian sensitivity analysis for *P. aeruginosa*. Plots of posterior PDFs for

parameter values and pairwise distributions are as in Fig. 5.

770
Figure 7. Bayesian sensitivity analysis for *S. aureus*. Plots of posterior PDFs for

parameter values and pairwise distributions as in Fig. 5.

Figure S1. Bayesian sensitivity analysis for *E. coli* using a sharpened likelihood

function. The analysis and presentation is the same as in Fig. 5, but using a 10-fold

lower error value.

Figure S2. Bayesian sensitivity analysis for *P. aeruginosa* using a sharpened

likelihood function. The analysis and presentation is the same as in Fig. 6, but using

a 10-fold lower error value.

Figure S3. Bayesian sensitivity analysis for *S. aureus* using a sharpened likelihood

function. The analysis and presentation is the same as in Fig. 7, but using a 10-fold

lower error value.

Tables

Table 1. Estimated parameter values obtained after fitting the model to data on

ofloxacin accumulation in different bacteria.

	a_1	a_2	β_1 (1/s)	β_2 (1/s)	δ (1/s)	τ (s)
	(ng/mg)	(ng/mg)				
E. coli	32.0	67.1	0.116	0.00125	0.000048	772
P. aeruginosa	7.43	13.7	>0.1[a]	>0.1[a]	0.000314	44.5
S. aureus	66.6	85.2	0.169	0.0014	0.000091	740

789   [a]Entries using '>' represent lower bounds.

790 Table 2. Parameter ranges used for prior distributions for GSA and BSA (Log_{10}

791 transformed values). Units of parameters are as in Table 1.

	$Log_{10} a_1$	$Log_{10} a_2$	$Log_{10} \beta_1$	$Log_{10} \beta_2$	$Log_{10} \delta$	$Log_{10} \tau$
			E. coli			
min	0	0	-3	-3	-7	0
max	2	2	0	0	-3.5	4
			P. aeruginosa			
min	0	0	-1	-1	-7	0
max	2	2	4	4	-2	4
			S. aureus			
min	0	0	-3	-3	-7	0
max	2	2	0	0	-3.5	4

796   Table 3. Sensitivities calculated from eigenvalues corresponding to each eigenvector

797   from LSA. Sensitivity values are calculated as $-\text{Log}_{10}(\lambda)$, where λ is the eigenvalue.

798   The connection of each eigenvector to the model parameters is visualized in Fig. 4.

Eigenvector #	E. coli	P. aeruginosa	S. aureus
1	3.6	3.7	3.6
2	3.5	2.7	3.1
3	2.4	2.0	1.5
4	1.7	-1.9	1.2
5	1.3	-6.7	0.5
6	-1.0	-11.8	-1.2

807 Table 4. Minimum and maximum values of parameters among 10^6 random samples

808 obtained by BSA MCMC (Log$_{10}$ transformed values). Units for parameters are as in

809 Table 1.

	$\text{Log}_{10}\,a_1$	$\text{Log}_{10}\,a_2$	$\text{Log}_{10}\,\beta_1$	$\text{Log}_{10}\,\beta_2$	$\text{Log}_{10}\,\delta$	$\text{Log}_{10}\,\tau$
			E. coli			
min	1.49	1.75	-1.05	-3.00	-7.00	2.81
max	1.52	1.90	-0.80	-2.57	-3.90	2.94
range	0.03	0.14	0.25	0.43	3.10	0.13
			P. aeruginosa			
min	0.76	1.08	-1.00	-1.00	-3.75	1.53
max	0.97	1.18	4.00	4.00	-3.28	1.69
range	0.21	0.10	5.00	5.00	0.47	0.16
			S. aureus			
min	1.82	1.88	-0.84	-3.00	-4.53	2.76
max	1.83	1.98	-0.69	-0.77	-3.80	2.96
range	0.01	0.10	0.15	2.23	0.73	0.20

813   Table 5. Predicted accumulation factors (ϕ), permeabilities (α), and net efflux (ε)

814   rates.

	ϕ_1	ϕ_2	α_1 (1/s)	α_2 (1/s)	ε_1 (1/s)	ε_2 (1/s)
E. coli	1.09	2.29	0.126	0.0029	-0.011	-0.0016
P. aeruginosa	0.39	0.72	>0.039[a]	>0.072[a]	>0[a]	>0[a]
S. aureus	2.93	3.75	0.495	0.0053	-0.326	-0.0039

817   [a]Entries with a '>' indicate a lower bound.

Figure 1

Figure 2

Figure 3

Figure 4

Figure 5

Figure 6

Figure 7

Figure S1

Figure S2

Figure S3