

# The Opposing Effects of Hedonic and Eudaimonic Happiness on Gene Expression is Correlated Noise

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## Abstract

**Background** This paper re-analyzes the gene set data from [1] and [2] which purportedly showed opposing effects of hedonic and eudaimonic happiness on the expression levels of a set of genes that have been correlated with social adversity.

**Methods** Four non-parametric methods were used to test the two null hypotheses addressed in the original studies ( $H_0 : \bar{\beta}_{hedonia} = 0$  and  $H_0 : \bar{\beta}_{eudaimonia} = 0$ ) as well as the null hypothesis of no difference in effect between hedonic and eudaimonic happiness ( $H_0 : \bar{\beta}_{hedonia} - \bar{\beta}_{eudaimonia} = 0$ ).

**Results** Standardized effects (mean partial regression coefficients) of *Hedonia* and *Eudaimonia* on gene expression levels are very small in both the 2013 and 2015 data, as well as the combined data. The  $p$ -values from all four tests are similar in magnitude and fail to reject any of the null models.

**Discussion** The results unambiguously fail to support opposing effects, or any detectable effect, of hedonic and eudaimonic happiness on the pattern of gene expression. The apparently replicated pattern of gene expression is simply “correlated noise” due to the geometry of multiple regression given the strongly correlated measures of hedonic and eudaimonic happiness.

## Background

In a highly visible gene set analysis, Fredrickson *et al.* 2013 [1] claimed that a measure of eudaimonic happiness was associated with a decreased “conserved transcriptional response to adversity” (CTRA) while a measure of hedonic happiness was associated with increased CTRA. This transcriptional response includes the up-regulation of pro-inflammatory signals and the down-regulation of antiviral and antibody synthesis signals. Brown *et al.* [3] criticized multiple components of the methodology and interpretation of Fredrickson *et al.* 2013 [1], including importantly here, the one-sample  $t$ -tests of the set of regression coefficients of the CTRA genes on hedonic and eudaimonic scores. Fredrickson *et al.* 2015 [2] followed up

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23 the criticism of [3] with a replicate study but using a marginal model with a specified correlated errors  
24 matrix, to estimate the associations between CTRA gene expression and happiness scores. In this follow-  
25 up study, Fredrickson *et al.* 2015 [2] showed that the pattern of mean CTRA gene expression replicated  
26 that of Fredrickson *et al.* 2013 [1] but that only eudaimonic happiness had a statistically significant effect  
27 on CTRA gene expression.

28 Here, I present the results of a re-analysis of the Fredrickson *et al.* 2013 [1] and Fredrickson *et al.*  
29 2015 [2] data. Not being a social psychologist, I limit my analysis to addressing the question “what  
30 is the evidence for effects of hedonic and eudaimonic happiness scores on CTRA gene expression” and  
31 give here only the necessary background to understand my analysis. The CTRA gene set includes 19  
32 pro-inflammatory, 31 anti-viral, and 3 antibody-stimulating genes. The Fredrickson *et al.* 2013 [1] data  
33 included all 53 genes but the Fredrickson *et al.* 2015 [2] data is missing IL-6 from the pro-inflammatory  
34 subset.

35 Fredrickson *et al.* 2013 [1] used 53 univariate multiple regressions to estimate the effects (the regression  
36 coefficient) of each happiness (hedonic and eudaimonic) score on  $\log_2$ (normalized gene expression) for each  
37 gene. The regression model included both happiness scores, seven covariates to adjust for demographic  
38 and general health confounding (sex, age, ethnicity, BMI, a measure of alcohol consumption, a measure of  
39 smoking, and a measure of recent illness), and eight covariates to adjust for immune status confounding  
40 (expression level of T-lymphocyte markers). Hedonic and eudaimonic scores were transformed to z-scores  
41 prior to the analysis. The 53 multiple regressions (one for each gene) yielded 53 coefficients for hedonic  
42 score and 53 coefficients for eudaimonic score. The coefficients of the 31 anti-viral and 3 antibody genes  
43 were multiplied by -1 to make the direction of the effect consistent with the CTRA response. Fredrickson  
44 *et al.* 2013 [1] used a simple one-sample *t*-test of the 53 coefficients to test for a mean effect of hedonic  
45 or eudaimonic score on CTRA expression. A mean coefficient greater than zero reflects a positive CTRA  
46 response (increased pro-inflammatory and decreased anti-viral and antibody-stimulating genes).

47 The fundamental problem with the Fredrickson *et al.* 2013 [1] *t*-test is that the coefficients are not  
48 independent of each other because of the correlated expression levels among genes. As a consequence of  
49 the correlated error, a one-sample *t*-test of the coefficients violates the test’s assumption of independent  
50 error. One way to think about the consequence of this violation is to consider a null model of no effect of  
51 happiness score on any of the 53 genes. The mean absolute correlation in the  $53 \times 53$  correlation matrix  
52 of Fredrickson *et al.* 2013 [1] gene expression levels is 0.25. The maximum is 0.92. Because of the high  
53 correlations among the expression levels, a set of 53 coefficients computed with the hypothetical null data  
54 will tend to have either more positive or more negative signs than expected. Consequently, the error of  
55 the mean coefficient (the standard error) is much larger than if the coefficients were independent. And,  
56 as a consequence, there will be an inflated Type-I error in a one-sample *t*-test of the mean. Brown *et al.*  
57 [3] discovered this inflated Type-I error in their exploration of the Fredrickson *et al.* 2013 [1] data.

58 In response to criticism from Brown *et al.* [3], Fredrickson *et al.* 2015 [2] used a generalized least  
59 squares (GLS) model with a heterogenous compound symmetry error matrix, effectively treating each of  
60 the 52 gene expression levels as repeated measures of a common effect [2]. I am not aware of any criticism  
61 or re-analysis of Fredrickson *et al.* 2015 [2]. While a GLS estimate of marginal effects is consistent even  
62 if the error correlation is misspecified, the variance of the estimates will be biased. Compound symmetry  
63 assumes equal correlation (conditional on the set of predictors) among all expression levels. This is not  
64 likely to approximate the true error structure for a set of expression levels for different genes, as these  
65 expression levels will share different sets of underlying regulatory factors. A second and perhaps more  
66 fundamental problem with the Fredrickson *et al.* 2015 [2] analysis is the small sample size ( $n = 122$   
67 or  $n = 198$  in the combined data) relative to the number of regression coefficients (69) and variance  
68 parameters (53) that must be estimated. This small sample per parameter ratio is likely to result in  
69 overfit models, which, in turn, will result in unstable and inflated coefficients [4]. Typically, when only  
70 the fixed effects are of interest (as here), the fixed effects and their errors are estimated using Generalized  
71 Estimating Equations instead of GLS to avoid issues resulting from estimating the correlated error matrix  
72 [5, 6]. Finally, and most importantly, the GLS model gains power by assuming that the estimated  
73 regression coefficient is a common effect for all genes (and each univariate estimate is merely an estimate  
74 of this common effect), an assumption that is more appropriate for longitudinal or repeated measures  
75 than for multiple outcomes such as gene expression levels.

76 The general question addressed by Fredrickson *et al.* 2013 [1] and Fredrickson *et al.* 2015 [2], that is,  
77 is there a mean response different from zero for a set of multiple outcomes, has a long and rich history  
78 in applied statistics [7], including in association studies of gene sets[8, 9]. Bull [10] is an especially clear  
79 exposition of the different null hypotheses that one might test. Wu *et al.* [11] clearly outline some of  
80 these hypotheses in the context of gene set associations.

81 Here, I reanalyze the Fredrickson *et al.* 2013 [1] data (hereafter, FRED13), the Fredrickson *et al.*  
82 2015 [2] data (FRED15), and the combined data (FRED13+15) using both bootstrap resampling to  
83 obtain standard errors of effects that account for the correlated expression levels and permutation tests  
84 to test the null hypotheses of zero mean effects for *Hedonia* and *Eudaimonia*. The re-analysis includes  
85 a permutation version of the O'Brien OLS test [7] and a randomization procedure implemented for gene  
86 set analysis [11]. The results from all analyses for each datasets are consistent in that they all fail to  
87 provide evidence against the nulls. Additionally, I show that the high correlation (.79 and .73 in the  
88 two datasets) between the two focal predictors (*Hedonia* and *Eudaimonia*) results in coefficients with  
89 negatively correlated errors that may be misinterpreted as a "replicable" pattern instead of correlated  
90 noise reflecting the geometry of multiple regression.

## 91 **Methods**

92 Data were downloaded as .txt Series Matrix Files from <http://www.ncbi.nlm.nih.gov/geo/> using accession  
93 numbers GSE45330 and GSE55762. The CTRA (response) expression data were log2 transformed. The  
94 T-lymphocyte expression data that formed part of the set of covariates were log2 transformed in the  
95 downloaded data. The downloaded hedonic and eudaimonic scores in FRED13 had means and variances  
96 close but not equal to that expected of z-scores, which suggests that the public data slightly differs from  
97 that analyzed by Fredrickson *et al.* 2013 [1]. Three rows of FRED13 had missing covariate data (two rows  
98 were completely missing) and were excluded; the number of rows (cases) in the cleaned matrix was 76.  
99 The downloaded hedonic and eudaimonic scores in FRED15 were the raw values and were transformed  
100 to z-scores. There was no missing data in FRED15 and the number of cases was 122.

101 Prior to all analyses, the expression levels of the 31 anti-viral and 3 antibody genes were multiplied  
102 by -1 to make the direction of the effect consistent with the CTRA response [1, 2].

## 103 **Null hypothesis tests**

104 The overall effect of *Hedonia* or *Eudaimonia* on expression levels of the CTRA gene set is simply the  
105 averaged effect over all genes,  $\bar{\beta}$ . Two of the focal null hypotheses that are tested here, which were  
106 also the focus of Fredrickson *et al.* 2013 [1] and Fredrickson *et al.* 2015 [2] are  $H_0 : \bar{\beta}_{hedonia} = 0$   
107 and  $H_0 : \bar{\beta}_{eudaimonia} = 0$ . Fredrickson *et al.* 2013 [1] and Fredrickson *et al.* 2015 [2] also discussed  
108 the differential effect of *Hedonia* and *Eudaimonia* on CTRA gene expression but inferred this from  
109 differences in  $p$ -values. Here I explicitly test the null hypothesis of no difference in effect between the two  
110 types of happiness using the null hypothesis  $H_0 : \delta = \bar{\beta}_{hedonia} - \bar{\beta}_{eudaimonia} = 0$ . I refer to these three  
111 null hypotheses as  $H_{hedonia=0}$ ,  $H_{eudaimonia=0}$ , and  $H_{\delta=0}$ .

112 All three hypotheses are directional, that is, the mean effect differs from zero. This differs from the  
113 general multivariate test that at least one of the coefficients differs from zero, but the mean response may  
114 be zero. While the hypotheses are directional, the tests are two-tailed, that is, the mean response may  
115 be up or down regulation of the CTRA gene set.

## 116 **Inferential tests**

117 The effects of *Hedonia* and *Eudaimonia* on the mean of the  $m$  gene expression levels are estimated with  
118 the multivariate linear model

$$\mathbf{Y} = \mathbf{XB} + \mathbf{E} \quad (1)$$

119 where  $\mathbf{Y}$  is the  $n \times m$  matrix of gene expression levels for the  $n$  subjects,  $\mathbf{X}$  is the model matrix of dummy  
120 variables and covariates,  $\mathbf{E}$  is the matrix of residual error, and  $\mathbf{B}$  is the  $p \times m$  matrix of partial regression  
121 coefficients. The coefficients of the  $j$ th column of  $\mathbf{B}$  are precisely equal to univariate multiple regression

122 of the  $j$ th gene on  $\mathbf{X}$  (and why the model is sometimes called a multivariate multiple regression). In R,  
123 estimating the  $m$  effects of *Hedonia* and *Eudaimonia* is much faster using this multivariate model than  
124 looping through  $m$  univariate multiple regressions. I refer to the mean of the  $m$  coefficients as the OLS  
125 estimates.

126 Four tests were used to test the null hypotheses. In all four tests, the happiness scores for *Hedonia* and  
127 *Eudaimonia* and the  $m$  expression levels were mean-centered and variance-standardized. Consequently,  
128 the reported OLS estimates are the mean standard partial regression coefficients (averaged over the  $m$   
129 genes).

### 130 Procedural bootstrap $t$ -test

131 Fredrickson *et al.* 2013 [1] used a bootstrap resampling method to compute a  $p$ -value. In their bootstrap,  
132 the 53 partial regression coefficients were re-sampled with replacement 200 times. Each iteration, a mean  
133 regression coefficient was computed. The standard deviation of the 200 means was used as the estimate of  
134 the standard error to compute a  $t$ -statistic and associated  $p$ -value. Resampling the regression coefficients  
135 fails to address the lack of independence among the coefficients. To estimate the sampling error that  
136 accounts for correlated error among the regression coefficients, the entire estimation procedure needs  
137 to be included within the bootstrap by resampling the data and re-estimating the coefficients. In each  
138 iteration of this procedural bootstrap, entire rows of the data were re-sampled with replacement, the  $m$   
139 coefficients were estimated by equation 1, and the re-sampled mean coefficients ( $\bar{\beta}_{hedonia}$  and  $\bar{\beta}_{eudaimonia}$ )  
140 were saved each iteration. 1999 bootstrap iterations were run. The  $t$ -statistic for each hypothesis is the  
141 observed mean coefficient ( $\bar{\beta}_{obs}$ , or  $\delta_{obs}$  for the difference in means) divided by its standard error, which  
142 was estimated as the standard deviation of the 2000 saved mean coefficients.

### 143 Permutation $t$ -test

144 As an alternative to the bootstrap  $t$ -test, I used permutation to generate null distributions of  $t$ -statistics  
145 for each null hypothesis and then computed  $p$ -values from these null distributions. To comply with the  
146 assumption of exchangeable error, I followed Anderson and Robinson [12] and used the permutation  
147 method of Freedman and Lane[13]. For this procedure, the predictor variables were divided into main  
148 effects  $\mathbf{Z}$  (hedonic and eudaimonic scores) and covariates  $\mathbf{X}$  (the demographic and immune variables).  
149 Using the non-permuted data, the observed residuals ( $\mathbf{E}_Y$ ) and predicted values ( $\hat{\mathbf{Y}}$ ) of  $\mathbf{Y}|\mathbf{X}$  were es-  
150 timated using equation 1. For each of the permuted iterations, rows of  $\mathbf{E}_Y$  were permuted and added  
151 to the non-permuted  $\hat{\mathbf{Y}}$  to generate a permuted response  $\mathbf{Y}^\pi = \hat{\mathbf{Y}} + \mathbf{E}_Y^\pi$ , where  $\pi$  indicates a permuted  
152 value. Prior to fitting the permuted data, *Hedonia* and *Eudaimonia* and the  $m$  expression levels were  
153 re-centered and variance-standardized. The  $m$  coefficients for both *Hedonia* and *Eudaimonia* were then  
154 computed from the model  $\mathbf{Y}^\pi|\mathbf{X} + \mathbf{Z}$  and  $\bar{\beta}$  was computed from the  $m$  coefficients for each of the three

155 hypotheses. Additionally, a  $t$ -statistic was computed for each hypothesis each iteration using

$$t_{perm} = \frac{\bar{\beta}}{s_{\beta}/\sqrt{m}} \quad (2)$$

156 where  $s_{\beta}$  is the standard deviation of the  $m$  coefficients. 2000 iterations were run, including an iteration of  
157 non-permuted data. The two-sided  $p$ -value of each hypothesis was computed as the fraction of  $|t_{perm}| \geq$   
158 the observed  $|t_{perm}|$ .

### 159 **Permutation O'Brien's OLS $t$ -test**

160 Neither the bootstrap  $t$ -test nor permutation test explicitly accounts for the correlation among the regres-  
161 sion coefficients (although both implicitly account for this in the resampled distributions). To explicitly  
162 account for this correlation, I used a modification of O'Brien's OLS test [7]. After standardizing the  
163 covariates and all gene expression levels to unit variance, O'Brien's test statistic is

$$t_{O'Brien} = \frac{\mathbf{j}^T \mathbf{t}}{\mathbf{j}^T \mathbf{R} \mathbf{j}} \quad (3)$$

164 where  $\mathbf{j}$  is a  $m$  vector of 1s,  $\mathbf{t}$  contains the  $t$ -statistic associated with each of the  $m$  partial regression  
165 coefficients, and  $\mathbf{R}$  is the correlation matrix of the  $m$  coefficients. More simply, the numerator is the  
166 sum of the  $t$ -statistics for each gene and the denominator is the sum of all of the elements of  $\mathbf{R}$ .  $\mathbf{R}$   
167 was estimated using a bootstrap resampling procedure. The null distribution of  $t_{O'Brien}$  was constructed  
168 using the observed value and 1999 permutations of the data. The permutation procedure was exactly  
169 that for the permutation  $t$ -test above except that each iteration of the permutation, the permuted data  
170 was resampled and refit (using Equation 1) 1000 times in order to estimate  $\mathbf{R}$  as the correlation matrix  
171 of the  $1000 \times m$  set of coefficients. The inner and outer loops make this a computationally intensive test.

### 172 **Rotation gene set test (ROAST)**

173 The final test of  $\bar{\beta}$  is the rotation-test described in Wu *et al.* [11] and implemented in the function `roast`  
174 from the `limma` package [14]. The test statistic,  $z_{rot}$ , is a mean  $z$ -score computed from the set of  $m$   
175 moderated  $t$ -statistics computed for each gene. Using a hierarchical model, the moderated  $t$ -statistic uses  
176 information on the error of all genes in the set to estimate the gene specific standard error. A  $p$ -value for  
177 the test statistic is evaluated in a very similar manner to that described above in "Permutation test" but  
178 with some key differences. First, in the rotation-test, the observed residuals ( $\mathbf{E}_Y$ ) are from  $\mathbf{Y}|\mathbf{X}$  where  
179  $\mathbf{X}$  includes not only the covariates but also the non-focal happiness score (for example, *Eudaimonia*  
180 is included in  $\mathbf{X}$  for the test of *Hedonia*). Second, instead of permutation, the  $n$ -vector of residuals is  
181 rotated by a random vector  $r$ , which is constant for all genes within each iteration but variable among  
182 iterations. And third, the rotated residuals ( $\mathbf{E}_Y^r$ ) are used to directly compute the new  $t$ -statistics and

183  $z$ -scores without fitting the new model  $\mathbf{E}_{\mathbf{y}}^{\pi}|\mathbf{X} + \mathbf{Z}$  (where  $\pi$  indicates rotated residuals). The observed  
184 and rotated  $z$ -scores from 1999 rotations were used to generate the null distribution. The  $p$ -value for the  
185 “UpOrDown” test was used as this is the test of the two-tailed directional hypothesis.

## 186 Permutation generalized least-squares

187 If we assume the separate coefficients for each of the  $m$  genes is an estimate of a common effect  $\beta$ , then the  
188 tests described above lose power due to effectively discarding the  $m$  within subject estimates of  $\beta$ . A fixed-  
189 effects marginal model potentially gains power by using all  $nm$  responses but avoids pseudoreplication  
190 [15] (or inflated Type I error) by weighting the standard error of the estimate by the within subject error  
191 covariance matrix. To implement this model, the data matrix is stacked into long format by combining  
192 the  $m$  expression levels into a single variable *expression* and the variable *Gene* is created to identify the  
193 gene associated with a specific expression value. The fixed-effects marginal model is

$$\mathbf{y}_i = \mathbf{X}_i\beta + \varepsilon_i \quad (4)$$

194 where  $\mathbf{y}_i$  is the vector of  $m$  responses for subject  $i$ ,  $\mathbf{X}_i$  is the model matrix for subject  $i$ , which includes  
195 the main effect *Gene* to identify the  $j$ th element of  $\mathbf{y}_i$ , and  $\beta$  is the vector of coefficients, including the  
196 common effects of each covariate on the response. In this model,  $\varepsilon_i \sim N(\mathbf{0}, \Sigma)$ , where  $\Sigma$  is the within  
197 subject error covariance matrix.

198 While the “common effect” assumption is highly questionable for gene expression data, it is useful to  
199 explore this model in order to learn about the results from Fredrickson *et al.* [2]. Following Fredrickson *et*  
200 *al.* 2015 [2], I used GLS with a heterogenous compound symmetry error matrix to estimate the common  
201 effects  $\beta_{Hedonia}$  and  $\beta_{Eudaimonia}$ . Exploration of the behavior of the GLS suggested very unstable  
202 coefficients and, consequently, I used a bootstrap procedure to show this sensitivity to sampling and a  
203 permutation test to estimate  $p$ -values. Each iteration of either the bootstrap or permutation, the data  
204 was resampled (permuted) in wide format, rescaled, and reshaped to long format. For both bootstrap and  
205 permutation, the coefficients were estimated using the `gls` function from the `nlme` package [16]. In both,  
206 the first iteration used the observed (not resampled or permuted) data. The bootstrap was limited only  
207 to the combined FRED13+15 data because of lack of convergence issues with the smaller datasets. 500  
208 iterations of the bootstrap procedure were run (including the iteration with the observed sample). For  
209 the permutation test, the standard partial regression coefficients and associated  $t$ -statistics for *Hedonia*  
210 and *Eudaimonia* were saved each iteration and used to generate a null distribution of expected values  
211 (using the  $t$ -statistic) given no effect of either on expression level. Due to the time required to fit the  
212 GLS, only 300 permutations were run but this was sufficient to get an approximate  $p$ -value. To estimate  
213 the sensitivity of this  $p$ -value to only 300 permutations, 95% confidence intervals were computed for the

214  $p$ -value using 2000 bootstrap resampled sets of the 300 permutation  $t$ -statistics.

### 215 **Type I error in the GLS method**

216 I used Monte Carlo simulation to explore the inflation of type I errors due to overfitting in the GLS fit  
217 using the parametric estimate of the standard error. In each run of the simulation, a random  $n \times p$  matrix  
218  $\mathbf{X}$  of independent variables ( $n$  samples of  $p$  covariates) and a random  $n \times m$  matrix  $\mathbf{Y}$  of response variables  
219 ( $n$  samples of  $m$  responses) were generated using the function `rmvnorm` from the `mvtnorm` package [17].  
220 All simulated independent variables were modeled as continuous variables sampled from  $\mathcal{N}(\mathbf{0}, \mathbf{S}_X)$ , where  
221  $\mathbf{S}_X$  is the covariance matrix of the 17 regressor variable from FRED15. The 52 response variables were  
222 modeled as continuous variables sampled from  $\mathcal{N}(\mathbf{0}, \mathbf{S}_Y)$ , where  $\mathbf{S}_Y$  is the covariance matrix of the 52  
223 gene expression levels from FRED15. The expected effect of any of the  $X$  on any of the  $Y$  is zero.

224 To reduce the time required for the simulation, subsets of  $m = 10, 20, \text{ or } 30$  of the 52 response  
225 variables were sampled randomly.  $p$  is the number of covariates (17) from FRED15. The sample size  
226 was determined as  $n = 2(m + p)$ . Because the number of regressors is  $m + p$  (again, the data are in long  
227 format), the ratio of samples to regressor was 2 for all runs. This ratio is in-between that for FRED15  
228 and the combined data (1.8 and 2.9, respectively). 200 iterations of each subset were run. The  $p$ -values  
229 associated with the  $t$ -test of the coefficients for the two  $X$  variables simulating *Hedonia* and *Eudaimonia*  
230 (that is, with an expected correlation equal to that in FRED15) were saved each iteration.

231 All analyses were performed using R [18]. All data cleaning and analysis scripts are available at the  
232 public GitHub repository <https://github.com/middleprofessor/happiness>.

## 233 **Results**

### 234 **Replication of previous analyses**

235 Fredrickson *et al.* 2013 [1] do not report either the partial regression coefficients of each gene expression  
236 level on hedonic and eudaimonic score or the mean coefficient for each score. The back-transformed mean  
237 effects ( $2^{4\bar{\beta}} \times 100$ , where  $\bar{\beta}$  is the mean of the  $m$  coefficients) for all three datasets are given in Table 1.  
238 My values approximate the values inferred from Fig. 3 of Fredrickson *et al.* 2015 [2] with the exception  
239 of that for *Hedonia* from FRED13, which is noticeably smaller than that figured in Fredrickson *et al.*  
240 2015 [2]. This likely reflects small differences between the public data and thta analyzed in Fredrickson  
241 *et al.* 2013 [1] [see also 3]. From the  $p$ -values based on a  $t$ -statistic that assumes independence of the  
242 regression coefficients (Table 1), one might reasonably reject each null hypothesis for each dataset.

243 The variance-standardized effects and  $p$ -values for hedonic and eudaimonic scores estimated from the  
244 GLS for each dataset are given in Table 2. My coefficients for FRED15 are the same as those reported  
245 in Fredrickson *et al.* 2015 [2] to the 3rd decimal place. My coefficients for the combined data are similar



Table 1: Back-transformed mean effect sizes ( $2^{4\bar{\beta}} \times 100$ ) and naive  $p$ -values from the 2013, 2015, and combined data

data	Hedonia	Eudaimonia	$p_{hedonia}$	$p_{eudaimonia}$
FRED13	3.6	-7.3	0.096	0.003
FRED15	7.2	-5.7	<0.001	0.045
FRED13+15	6	-5.3	<0.001	0.048

Table 2: GLS estimates of the variance-standardized coefficients for the 2013, 2015, and combined data. The bootstrap standard error and permutation  $p$ -values are also given

Type	Data	$\beta$	SE	$p$	bootstrap SE	permutation $p$
<i>Hedonia</i>	FRED13	0.525	0.169	0.002		0.29
	FRED15	0.086	0.122	0.48		0.74
	FRED13+15	0.062	0.099	0.53	0.227	0.79
<i>Eudaimonia</i>	FRED13	0.135	0.176	0.44		0.83
	FRED15	-0.511	0.126	<0.001		0.16
	FRED13+15	-0.456	0.101	<0.001	0.272	0.07

246 to my coefficients for the FRED15 data, while Fredrickson *et al.* 2015 [2] report a substantially smaller  
 247 negative effect for *Eudaimonia* for the the combined data. Again, this is likely due to small differences  
 248 between the public FRED13 data and the data actually analyzed in [1].

249 Importantly here, the coefficients for the FRED13 data have the opposite pattern of that for FRED15  
 250 and combined data, that is, with the 2013 data, the effect of *Hedonia* is large and has a very small  
 251  $p$ -value (0.002) while the effect for *Eudaimonia* is small and not statistically significant ( $p = 0.44$ ).

## 252 New results

253 Standardized mean effects ( $\bar{\beta}$ ) are very small and positive for *Hedonia* and very small and negative  
 254 for *Eudaimonia* for all three datasets (Table 3). The bootstrap SE for each mean indicates that a  
 255 95% confidence interval is too large to have any confidence in the direction of either of the effects for  
 256 any dataset. The  $p$ -values computed using the the procedural bootstrap, the permutation  $t$ -test, the  
 257 permutation O'Brien's  $t$ -test, and the rotation  $z$ -test are very consistent and all fail to reject the null.  
 258 The OLS estimates of the difference ( $\Delta$ ) between hedonic and eudaimonic effects are small and positive.  
 259 The bootstrap SE for all  $\Delta$  are too large to have any confidence in the direction of the difference and the  
 260  $p$ -values from each of the four tests fail to reject the null for any of the data sets.

## 261 GLS stability

262 The GLS coefficients were described above (Table 2). The bootstrap standard errors for the FRED13+15  
 263 data for the GLS fit are over twice the parametric estimates (Table 2), which shows that the coefficients  
 264 are very sensitive to sampling. Again, bootstrap errors were not computed for FRED13 or FRED15  
 265 because of too many issues with convergence of the smaller datasets. Despite the large coefficient for

Table 3: OLS estimates of mean *Hedonia* and *Eudaimonia* effects on CTRA gene expression. The estimates are the mean variance-standardized partial regression coefficients from the multivariate regression over the  $m$  responses (genes). The SE was estimated using a bootstrap. The  $p$ -values are from the bootstrap, permutation  $t$ , permutation Obrien's  $t$ , and rotation  $z$  tests.

Type	Data	$\bar{\beta}$	SE	$p_{boot}$	$p_{perm}$	$p_{Obrien}$	$p_{rot}$
<i>Hedonia</i>	FRED13	0.026	0.117	0.83	0.75	0.8	0.77
	FRED15	0.062	0.044	0.17	0.22	0.23	0.23
	FRED13+15	0.049	0.04	0.23	0.19	0.27	0.23
<i>Eudaimonia</i>	FRED13	-0.063	0.125	0.62	0.42	0.51	0.5
	FRED15	-0.067	0.048	0.17	0.31	0.21	0.21
	FRED13+15	-0.058	0.039	0.14	0.32	0.17	0.16

Table 4: OLS estimates of the difference in effect ( $\Delta = \bar{\beta}_{hedonia} - \bar{\beta}_{eudaimonia}$ ) for the 2013, 2015, and combined data. The SE was estimated using a bootstrap. The  $p$ -values are from the bootstrap, permutation  $t$ , permutation Obrien's  $t$ , and rotation  $z$  tests

Data	$\Delta$	SE	$p_{boot}$	$p_{perm}$	$p_{Obrien}$	$p_{rot}$
FRED13	0.089	0.235	0.71	0.55	0.62	0.62
FRED15	0.129	0.085	0.13	0.23	0.19	0.19
FRED13+15	0.107	0.075	0.16	0.25	0.19	0.18

266 *Eudaimonia* for FRED13+15, the standard errors are too large to have any confidence in the direction  
 267 of the effect. The  $p$ -values from the permutation test fail to reject any of the nulls.

268 The large bootstrap relative to parametric standard errors for the GLS coefficients suggest an inflated  
 269 Type I error rate with the parametric  $p$ -values. Type I error for the GLS parametric  $p$ -values for simulated  
 270 data modeled on FRED15 is given for different levels of  $\alpha$  in Table 5. The results show highly inflated  
 271 Type I error which increases with smaller  $\alpha$ .

## 272 Discussion

273 The re-analysis of the gene expression data in subjects scored for hedonic and eudaimonic happiness  
 274 unambiguously fails to support either the original conclusion of an opposite relationship of hedonic and  
 275 eudaimonic happiness on the CTRA (conserved transcriptional response to social adversity) gene set [1] or  
 276 the more recent conclusion limiting the relationship to eudaimonic well-being [2]. The consistency among  
 277 the four different tests for each hypothesis and dataset is notable. The  $p$ -values from the permutation

Table 5: Type I error and Inflation factor ( $\frac{Error}{\alpha}$ ) for the GLS test of Fredrickson *et al.* 2015 [2]. The Error is the average of the error computed for the simulated coefficients for *Hedonia* and *Eudaimonia*

$\alpha$	Error	Inflation
.1	0.21	2.1
.05	0.14	2.7
.01	0.06	5.7
.001	0.02	19.2
.0001	0.01	108.3

278 O'Brien's  $t$ -test and rotation  $z$  test are especially close despite the differences in the implementation of  
279 the randomization. That said, the rotation test is very fast relative to the permutation O'Brien test,  
280 which required nested re-sampling.

281 The apparent replication of the sign of the effects between FRED13 and FRED15 [2] is true for the  
282 OLS estimates but strikingly false for the GLS estimates, although this failure of the GLS test to replicate  
283 was not noted by Fredrickson *et al.* [2] because they used the OLS estimate and not the GLS estimate  
284 to show the replicated pattern of expression. Regardless, any replication in the sign of the mean effect  
285 should not be surprising given only two replicates of two coefficients. More importantly, as I show below,  
286 the apparent replication is expected given the high correlation between hedonic and eudaimonic scores.

287 Beyond the fact that a GLS model with 69 predictors and 53 variance estimates was fit with a mere  
288 122 (FRED15) or 198 (FRED13+15) subjects, several features of the results suggest inflated coefficient  
289 estimates resulting from overfitting the model to noise. First, at least one of the GLS coefficients in each  
290 of the datasets is very large relative to what we'd expect from a gene set association given observational  
291 data and the stated hypotheses. Second, the GLS coefficients are very different from the OLS coefficients  
292 (Tables 2 and 3). Third, the opposite pattern of effects estimated in FRED13 and FRED15 suggests that  
293 either something very different biologically is going on between the subjects in FRED13 and FRED15 or  
294 the coefficients are very unstable due to a combination of overfitting and multicollinearity. Fredrickson  
295 *et al.* 2015 [2] did not report re-analyzed results for FRED13 using the GLS model so do not discuss  
296 either interpretation. Fourth, the plot of residuals against the predicted values shows a strong, negative  
297 relationship (not shown). And finally, the Type I error rate of the simulated data modeled on FRED15 is  
298 highly inflated (Table 5). Especially striking about the Type I error rates is the relatively high frequency  
299 of very small  $p$ -values ( $p \leq 0.001$ ).

300 The conclusions of Fredrickson *et al.* 2015 [2], then, are based on  $p$ -values from tests contaminated  
301 by highly inflated Type I errors due to overfitting combined with moderate multicollinearity and a high  
302 correlation between the two focal predictors. The consequences of the highly correlated focal predictors  
303 has not been discussed in detail. Fredrickson *et al.* 2015 [2] emphasized the replicated pattern of a  
304 positive mean coefficient (described in the introduction) for *Hedonia* and a negative mean coefficient  
305 for *Eudaimonia*, where a positive coefficient implies up-regulation of the genes associated with social  
306 adversity. This pattern and apparent replication is almost certainly a function of the multicollinearity  
307 among the predictors in combination with the high positive correlation between hedonic and eudaimonic  
308 scores. It is well known that the partial regression coefficients of two highly correlated predictors are  
309 negatively correlated (one will tend to be positive and the other negative), which is the case with these  
310 data. For example, using FRED13, and disregarding all predictors but hedonic and eudaimonic scores,  
311 the partial regression coefficient of any gene expression level on *Hedonia* ( $X_1$ ) and eudaimonia ( $X_2$ ) are

$$\begin{aligned}\beta_1 &= 2.66\mathbf{x}_1^\top \mathbf{y} - 2.1\mathbf{x}_2^\top \mathbf{y} \\ \beta_2 &= -2.1\mathbf{x}_1^\top \mathbf{y} + 2.66\mathbf{x}_2^\top \mathbf{y}\end{aligned}\tag{5}$$

312 where the 2.66 and -2.1 are the diagonal and off-diagonal elements of the inverse of the correlation  
 313 matrix with .79 in the off-diagonal (the correlation between hedonic and eudaimonic scores in FRED13).  
 314 Because of the high correlation, both  $\beta_1$  and  $\beta_2$  include a large contribution from the covariance of the  
 315 other  $X$  and  $Y$  but the sign of this contribution is negative. Consequently, if the expected  $\mathbf{x}^\top \mathbf{y}$  is zero  
 316 for both predictors, the  $\beta$  coefficients will be negatively correlated. Random noise creates negatively  
 317 correlated error. This negative correlation is easily seen in the scatterplot of  $\beta_{hedonia}$  vs.  $\beta_{eudaimonia}$  for  
 318 the gene IL1A (the choice of gene doesn't matter) from the permutation  $t$ -test (Figure 1A). The negative  
 319 correlation is also seen using the coefficients from GLS model, which estimates a single coefficient for  
 320 the complete set of genes (Figure 1B). In both of these analyses, the expected effects (partial regression  
 321 coefficients) are zero (because of the permutation) yet the estimates are negatively correlated. Note that  
 322 this correlated error arises from the correlation between hedonic and eudaimonic scores (Equation 5)  
 323 and is not the same as the correlated error that arises from the correlation among the gene expression  
 324 levels. Unambiguously, then, the data from Fredrickson *et al.* 2013 [1] and Fredrickson *et al.* 2015 [2] do  
 325 not show a replicated pattern of differentially expressed genes associated with social adversity between  
 326 hedonic and eudaimonic people. Instead, this apparently replicable pattern of differential expression is  
 327 simply correlated noise arising from the geometry of multiple regression.

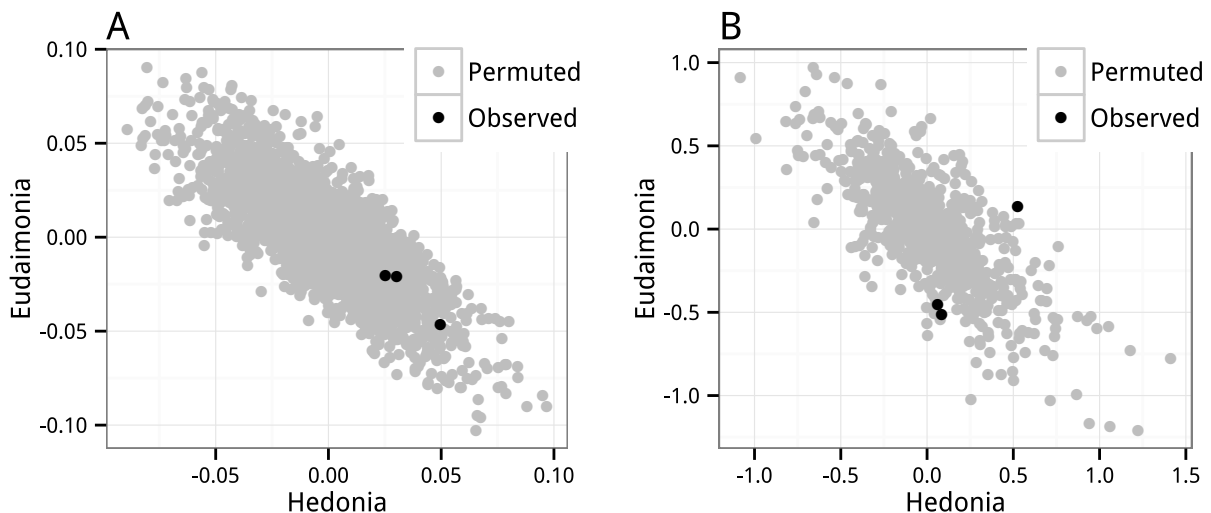


Figure 1: **Correlation between regression coefficients of gene expression levels on *Hedonia* and *Eudaimonia* for permuted data.** Coefficients from permuted runs are in grey. Observed coefficients for all three datasets are in black. The expected effects for the permuted runs is zero. A. Partial regression coefficients of IL1A from the permutation  $t$ -test. B. Partial regression coefficients (accounting for the expression of all genes simultaneously) from the permutation GLS model.

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