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BIAS IN COMMUNITY-WEIGHTED MEAN ANALYSIS RELATING SPECIES ATTRIBUTES

TO SAMPLE ATTRIBUTES: JUSTIFICATION AND REMEDY

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Abstract

A common way to analyse relationship between matrix of species attributes (like functional traits

of indicator values) and sample attributes (e.g. environmental variables) via the matrix of species

composition is by calculating community-weighted mean of species attributes (CWM) and

relating it to sample attributes by correlation, regression, ANOVA or other method. This

weighted-mean approach is used in number of ecological fields (e.g. functional and vegetation

ecology, biogeography, hydrobiology or paleolimnology), and represents an alternative to other

methods relating species and sample attributes via species composition matrix (like the fourth-

corner problem and RLQ analysis).

Here, I point out two important problems of weighted-mean approach: 1) in certain cases,

which I discuss in detail, the method yields highly biased results in terms of both effect size and

significance of the relationship between CWM and sample attributes, and 2) this bias is

contingent upon beta diversity of species composition matrix. CWM values calculated from

samples of communities sharing some species are not independent from each other and this lack

of independence influences the number of effective degrees of freedom. This is usually lower

than actual number of samples entering the analysis, and the difference further increases with

decreasing compositional heterogeneity of the dataset. Discrepancy between number of effective

degrees of freedom and number of samples in analysis turns into biased effect sizes and inflated

Type I error rate in case that significance of the relationship is tested by standard tests, a problem

which is analogous to analysis of two spatially autocorrelated variables.

Consequences of the bias is that reported results of studies using rather homogeneous

(although not necessarily small) compositional datasets may be overly optimistic, and results of

studies based on datasets differing by their compositional heterogeneity are not directly

comparable. I describe the reason for this bias and suggest guidelines how to decide in which

situations the bias is actually a problem for interpretation of results. I also introduce analytical

solution accounting for the bias, test its validity on simulated data and compare it with an

alternative approach based on the *fourth-corner* approach.

Introduction

Weighted-mean approach is a method to analyse link between species attributes and sample

attributes by calculating community-weighted means of species attributes (CWM), which can be

directly related to sample attributes by correlation, regression, ANOVA or other methods (Fig. 1).

Species attributes are species properties (traits), behaviour (species ecological optima) or

phylogenetic age, while *sample attributes* are characteristics of community samples measured in

the field (environmental variables) or derived from matrix of species composition (species

richness or positions of samples in ordination diagrams).

Weighted-mean approach is used in wide range of ecological fields. In functional ecology,

testing the effect of environmental variables on changes in CWM is one of the approaches

demonstrating the effect of environmental filtering on trait-mediated community assembly (Diaz

et al. 1998; Shipley 2010; Laliberté *et al.* 2012). Similarly, CWM are used to predict changes in

ecosystem properties, such as biomass production or nutrient cycling (Garnier *et al.* 2004; Vile *et*

al. 2006), or ecosystem services like fodder production or maintenance of soil fertility (Diaz et al.

2007). In biogeography, grid-based means of species properties (like animal body size, range

size or evolutionary age) are linked to macroclimate or diversity (Blackburn & Hawkins 2004,

Hawkins & Diniz-Filho 2006, Hawkins et al. 2014). Vegetation ecologists use species indicator

values (e.g. those of Ellenberg et al. 1992 or Landolt 1977) to estimate habitat conditions from

calculated mean species indicator values of vegetation samples and relate them to soil, light or

climatic variables (Schaffers & Sýkora 2000, Wamelink et al. 2002, 2005). In hydrobiology,

reliability of saprobic index of Sládeček (1973) based on weighted mean of diatom indicator

values, or similar indices (e.g. trophic diatom index, Kelly & Whitton 1995) is evaluated by

relating them to measured water quality parameters. Similarly, in paleoecology the method used

to reconstruct acidification of lakes from fossil diatom assemblages preserved in lake sediments

is based on weighted means of diatom optima along pH gradient (ter Braak & Barendregt 1986)

and as one of the transfer functions, (e.g. Birks *et al.* 1990) is considered to be a tool which have

"revolutionised paleolimnology" (Juggins 2013). Other, more specific examples include relating

community specialization index (mean of species specialization values weighted by their

dominance in community) to environmental variables (Clavero & Brotons 2010, Fajmonová et al.

2013), or attempts to verify whether plant biomass can be estimated from tabulated plant heights

and species composition as mean of species heights weighted by their cover in a plot (Axmanová

et al. 2012).

Important thing to note is that although weighted-mean approach is technically relating

two sets of variables (CWM and sample attributes), three matrices are in fact involved in the

computation background (notation here follows RLQ analysis of Dolédec *et al.* 1996): matrix of

sample attributes **R** with m sample attributes of n samples ($n \times m$), matrix of *species composition*

L with abundances (or presences-absences) of p species in n samples ($n \times p$) and matrix of

species attributes **Q** with s species attributes for p species ($s \times p$). Weighted-mean approach is

just one of possible options how to tackle the problem of relating species attributes (**Q**) with

sample attributes (**R**) via matrix of species composition (**L**): it combines **Q** with **L** into matrix of

weighted-means **M** and relates it to **R** (Fig. 1). Alternative solution is to combine matrix of

sample attributes **R** with species composition **L** by calculating weighted-mean of sample

attributes (optima of individual species along given sample attribute or species centroids) and

relate these values to species attributes **Q** (e.g. ter Braak & Looman 1986). Third option is to use

methods suitable for simultaneously handling all three matrices (**R**, **L** and **Q**), such as the *fourth-*

corner approach (Legendre *et al.* 1997), related ordination method called RLQ analysis

(Dolédec *et al.* 1996) and other alternatives (Jamil et al. 2013, Brown et al. 2014).

In weighted-mean approach, relationship between CWM and sample attributes is in most

cases tested by standard parametric or permutation test. However, not all types of ecological

questions, which are usually solved by weighted-mean approach, should actually be tested by

standard tests. In certain situations and types of null hypotheses, weighted-mean approach

combined with standard tests generates biased results, which are more optimistic than would be

actually warranted by analysed data. This bias includes unreliable estimates of effect size (e.g.

correlation coefficients in case of correlation or r^2 in case of linear regression) and inflated Type

I error rate, leading to more frequent rejection of the null hypothesis than would be expected.

The key point before applying the weighted-mean approach is to explicitly decide, based on

critical inspection of the context of the study question and tested null hypothesis, what is actually

the relationship between species attributes or sample attributes and species composition, and

which of these relationships is actually fixed and which is random (more on the terms "fixed"

and "random" below). Inspiration for this issue can be seen in application of the fourth-corner

approach (Legendre et al. 1997), for which Dray & Legendre (2008) demonstrated the problem

of deciding the right permutation test (from five permutation models) to test the actual question

in hand, with a risk of inflated Type I error rate in situation of wrong choice. For *weighted-mean*

approach, this issue was shown by Zelený & Schaffers (2012) in a specific context of relating

mean Ellenberg indicator values (species attributes) to sample attributes derived from species

composition matrix (like ordination scores or species richness), and also by Peres-Neto et al.

(2012) in the context of metacommunity phylogenetics. Both studies proposed numerical

solutions: Zelený & Schaffers (2012) introduced modified permutation test, based on permuting

species instead of sample attributes, and Peres-Neto et al. (2012) suggested to use *sequential test*

(ter Braak et al. 2012) using the *fourth-corner* statistic (Legendre et al. 1997). Additionally,

Šmilauer & Lepš (2014) touched on this issue in the context of CWM-RDA method (Kleyer et al.

2012).

In this study, first I review categories of questions and null hypotheses which are

commonly analysed by weighted-mean approach. Using simulated data, I show for which

category there is a risk of biased results if tested by standard tests, and describe in detail what

exactly causes this bias. Namely, I argue that the bias is caused by mismatch between number of

samples in weighted-mean analysis and actual number of effective degrees of freedom, since

community samples sharing some of the species with other samples do not count for the full

degree of freedom in this analysis. I will also demonstrate that the amount of bias depends on the

compositional heterogeneity (beta diversity) of the species composition matrix in a way that with

increasing heterogeneity the bias decreases, which makes comparison of results between datasets

of different compositional heterogeneity difficult. Note that for numerical simplicity, I ignore

intraspecific variation in species attributes. Finally, I will review methods available for solving

the problem of inflated Type I error rate in weighted mean approach (namely *modified*

permutation test of Zelený & Schaffers 2012 and solution based on combining *fourth-corner*

statistic and *sequential permutation test* in weighted regression as introduced by Peres-Neto et al.

2012) and introduce novel solution, here called *two-step permutation test*. Although the

examples, ecological interpretations and reasoning used here are focused on relationship of

species functional traits or species indicator values with sample attributes analysed by weighted-

mean approach, the general context is valid also for other types of species and sample attributes

linked by weighted-mean approach.

Types of species and sample attributes

When thinking about possible alternative types of questions which are commonly being analysed

using weighted-mean approach, it proves as useful to distinguish whether species and sample

attributes are fixed or random. Terminology behind distinction into fixed and random is diverse

(Gelman 2005); here I don't use this terms in the sense of ANOVA (fixed vs random terms),

neither in the sense inferring their importance (fixed factors are important while random are

nuisance factors). As *fixed attributes* I consider those which are specific for given dataset and

related to given species or samples, and this specificity is acknowledged by the

question/hypothesis being tested in a way that this link is deemed as given, and not further

questioned or tested. *Random attributes* represent a subset of some larger pool of values, and

their link to species composition is not acknowledged by the question being tested. In the narrow

sense of permutation tests, fixed attributes should not be permuted among each other, while

random attributes can. For interpretation, effect of fixed attributes is limited only for given set of

attribute values and in the context of community datasets included in the analysis and is not

likely to be generalized beyond, while in case of random attributes interpretation is focused on

the general effect of given attribute, not only the subset of attribute values used in the study.

Species traits measured on individuals from plots of given community datasets can be considered

as fixed, while species traits taken from large trait databases and measured often in completely

different context should more likely be considered as random. Similarly, species richness or

sample ordination scores derived from community matrix are more likely fixed sample attribute,

while environmental variables measured in the field or derived from GIS layers may be

considered as random. Indeed, this distinction is often dependent on author's view of the

problem and on the theoretical context of the study, and the same variables can be seen as fixed

or random in different context.

In the original description of the fourth-corner problem (Legendre et al. 1997), focused

on linking fish behavioral and biological characteristics to environmental variables, both species

and sample attributes have been considered as fixed, and random was matrix of species

composition. Alternative permutation models were then used to test alternative hypotheses about

the mechanisms assembling the community (like environmental control over individual species

or species assemblages, lottery or random species attributes). In weighted-mean approach,

decision about fixed or random nature of attributes directly influences the decision for

meaningful way to test the relationship, and is therefore crucial for selecting correct statistical

test. Important is to note that all hypotheses tested by weighted-mean approach make (implicit or

explicit) assumption that either species or sample attributes are fixed, and their link to species

composition is *a priori* acknowledged and therefore not questioned (and not tested). In some

cases, whether the species or sample attributes are better considered as fixed or random depends

also on the need to generalize the results of the study. If the results should be used e.g. for local

application (e.g. whether CWM of species height in given agricultural system can predict well

the harvested biomass), species attributes can be seen as fixed, since the results will be used

solely in the context of the studied system – if the same values are measured again for the same

community, the results should be similar, but not applicable generally to other communities. If

the aim is to generalize the results (e.g. to assess whether the species height itself, as tabulated in

the floras, can be used as a tool to predict biomass yield), it is more reasonable to treat the

species attributes as random and modify the analysis accordingly, so as even local study can

contribute to more general description of such pattern.

Another useful distinction of attribute types is whether the sample or species attributes

are internal or external. The main difference is that internal attributes are numerically derived

from matrix of species composition, while external attributes are typically measured or estimated

variables, not directly derived from species composition matrix. Internal species attributes are

species optima calculated as weighted-means of sample attributes or as species scores on

ordination axes, and similarly internal sample attributes are e.g. sample scores on ordination axes,

species richness of individual samples or assignment of samples into groups based on

compositional similarity (e.g. by numerical classification). External species attributes, in contrary,

are measured traits or tabulated species indicator values, external sample attributes are measured

or estimated environmental variables or experimental treatments. While the link of external

species or sample attributes to species composition may be fixed or random and depends on the

context, internal attributes should always be considered as fixed, since they refer only to the

context of the dataset from which they have been derived.

Types of hypotheses tested by weighted-mean approach

Considering the distinction between fixed and random (sample or species) attributes, questions

and hypotheses commonly tested by weighted-mean approach fall into one of the three

categories (see Table 1 for summary). *Category 1* assumes that while sample attributes are fixed,

species attributes are random; *category 2* is opposite to the previous, with sample attributes

considered random and species attributes fixed; and, finally, *category 3* assumes that both

species and sample attributes are random. Below, I review in detail individual categories with

examples of ecological questions/hypotheses for each of them.

Category 1 – species attributes are random, sample attributes are fixed

Hypotheses in this category explicitly acknowledge the link between sample attributes and

species composition, or the link is implicit from the context or numerical background of the

study, and they focus on testing the link of species attributes to species composition. The null

hypothesis which is tested states that species attributes are not linked to species composition,

while alternative hypothesis states that they are. Questions focused on relating CWM to internal

sample attributes derived computationally from matrix of species composition fall into this

category (e.g. relating mean Ellenberg indicator values to sample scores on unconstrained

ordination, often used to interpret ecological meaning of ordination axes; Zelený & Schaffers

2012). Also studies with external sample attributes considered to be fixed, like experimental

treatments, fall into this category in case that their effect on species composition is

acknowledged, and the question is about how does species attributes response to it. Additional

level of complexity is added in studies dealing with grid data with both CWM and internal

sample attributes (e.g. species richness derived from community data) spatially autocorrelated

due to spatial coherence of species distribution (B. Hawkins, *pers. comm.*). Zelený & Schaffers

(2012) showed that standard parametric and permutation tests has inflated Type I error rate for

this category, and as an alternative introduced *modified permutation test*, permuting species

attributes instead of sample attributes as further discussed in this study.

Category 2 – species attributes are fixed, sample attributes are random

Hypotheses in the second category assume that the species attributes are linked to species

composition, and the null hypothesis states that sample attributes are not linked to species

composition, while alternative hypothesis states that they are. Example are trait-based studies

asking whether species traits can explain effect of environmental filtering on species abundances

in community; these studies operate with an assumption that species traits (as species attributes)

are functional, i.e. they influences the abundances of species in community, and the question

being evaluated is whether the sample attributes (environmental factor) acts as an environmental

filter on species abundances. Also descriptive studies without ambitions to be more generalized

fall into this category – e.g. relationship between CWM of species indicator values (e.g. mean

Ellenberg indicator values) and measured environmental variables, if the interpretation is

restricted only for the community dataset included in the study. Finally, studies using internal

species attributes (derived from species composition, e.g. as weighted-mean of sample attributes

or as scores on ordination axes) also belong to this category.

Category 3 – both species and sample attributes are random

This category of hypotheses includes mostly observational studies without prior knowledge or

expectations about link between any of matrices. The null hypothesis states that there is no link

between species and sample attributes via the matrix of species composition because either

species attributes or sample attributes (or both) are not linked to species composition. To reject

this null hypothesis means to prove that both species and sample attributes are actually linked to

species composition. Empirical studies describing general relationship between sample attributes

and species attributes without explicitly or implicitly acknowledging some underlying

assumptions or mechanisms belong to this category. Examples are studies relating CWM of

functional traits to environmental variables without clear assumption that traits are functional,

allowing to question whether particular trait are actually linked to species composition or not. In

case of studies with species indicator values, these include relating mean indicator values to

environmental variables with aim to generalize the result also out of the studied dataset (e.g.

answering the question whether Ellenberg indicator values for soil reaction *per se* are good

predictors of measured soil pH, i.e. not only in the context of given community dataset).

Illustration of the bias using simulated community data

In the next section, I will use simulated community data to illustrate performance of standard

parametric test, if this is used to test hypotheses from each category defined above. The benefit

of simulated data is the possibility to keep certain parameters fixed and to manipulate only those

parameters whose effect is studied – in this case fixed are numbers of samples in the dataset, and

manipulated are links between species or sample attributes and species composition, and also

compositional heterogeneity of community data.

Each artificial community dataset includes the set of three matrices (sample attributes **R**,

species composition **L,** and species attributes **Q**), with the link between species or sample

attributes and species composition (or both) broken by permutation of attributes. This creates

four scenarios (Fig. 2, identical with scenarios 1-4 of Dray & Legendre 2008): *scenario 1 -* both

sample and species attributes are linked to species composition, *scenario 2 -* sample attributes

are linked to species composition, but species attributes are not, *scenario 3 -* species attributes

are linked to species composition, but sample attributes are not, and *scenario 4 -* none of species

or sample attributes are linked to species composition. For hypotheses in category 1 defined

above, the scenario 2 represents the null hypothesis, for category 2 scenario 3 is the null

hypothesis, and for category 3 the scenarios 2, 3 and 4 represent alternative states of null

hypothesis (Table 1). Scenario 1 represents the power test for all three categories (i.e. it measures

probability of getting significant results if the alternative hypothesis is true). Additionally, I also

examined how observed bias depends on compositional heterogeneity (beta diversity) of

community matrix, which influences the number of effective degrees of freedom in analysis (as

explained in detail further in the section *Justification of the bias*). Note that all analyses in this

paper were conducted using R-project (v. 3.2.3, R Core Team 2015); complete R scripts are

available in Appendix S5, and all functions have been wrapped into R-packages *weimea*

(abbreviation for *wei*ghted *mea*n; source code for v. 0.58 available as Appendix S6).

Description of simulated data

I created an algorithm generating community data which are structured by two virtual ecological

gradients (by extending the original one-gradient algorithm of Fridley et al. 2007 based on

concept of Minchin 1987). The first gradient has *constant* length for all generated datasets and

serves as a surrogate for measured environmental variable; in the analysis, positions of samples

along this gradient are used as *sample attributes*, while the optima of species along this gradient

are used as *species attributes*. The length of the second gradient is *variable* and its increasing

length increases the compositional heterogeneity of species composition matrix. Community

samples based on this simulated community ecospace were created by randomly locating

samples along the first gradient, and species composition for each sample was derived by

random assignment of fixed number of individuals to species identities weighted by relative

abundances of species with non-zero probability of occurrence at given location of the gradient

(see Appendix S1 for further details). With short second gradient, the resulting simulated

community dataset was compositionally relatively homogeneous, with samples located nearby

along the first gradient (with similar value of sample attribute) sharing rather high proportion of

species. Increasing the length of the second gradient increased the compositional heterogeneity

of the dataset, since two nearby samples may have quite different species composition (Fig. S1 in

Appendix S1). Note that although scenarios 1-4 are conceptually analogous to scenarios 1-4 in

Dray & Legendre (2008) used in the context of the *fourth-corner approach*, the model

generating simulated communities is different, since Dray & Legendre (2008) used one-gradient

model, which generates rather homogeneous communities, while I used two-gradients model,

generating set of communities of increasing compositional heterogeneity.

Weighted-mean approach with standard parametric tests applied on simulated data

Using the algorithm described above, for each of the four scenarios (1-4) I created ten levels of

compositional heterogeneity, and for each combination of *scenario × level of heterogeneity* I

created 1000 datasets (4 scenarios × 10 levels of heterogeneity × 1000 replications = 40 000

datasets). For each dataset I calculated CWM of species attributes, related it to sample attributes

using Pearson's *r* correlation and tested its significance using parametric *t*-test (for additional

results for least-square regression and r^2 see Fig. S2 in Appendix S2). For each level of

community heterogeneity in each scenario I counted proportion of correlations significant at $\alpha =$

0.05 (note that this proportion is identical to the proportion of significant regressions).

From the three scenarios with no direct link between species and sample attributes

(scenarios 2, 3 and 4), analysis of data generated by scenario 2 (Fig. 3) reveals the bias – the

correlation coefficient deviates from zero more than in other cases (Fig. 3), and the test of

significance shows inflated Type I error rate (Fig. 4). This bias is decreasing with increasing

heterogeneity of the species composition matrix (Fig. 3 & 4, Scenario 2): for the most

homogeneous dataset (*number of communities* = 1), the range of Pearson's *r* correlation

coefficients (expressed as 2.5% and 97.5% quantiles) is between -0.751 and 0.751 with 60% of

correlations significant, while for the most heterogeneous dataset with high beta diversity

(*number of communities* = 10) the range of Pearson's *r* values is between -0.381 and 0.354 with

15% of correlations significant (compared to 2.5 and 97.5% quantile range values of *r* observed

in scenarios 3 and 4 being in average between -0.278 and 0.281, with expected number of

significant results being close to 5%). Similarly inflated are values of coefficient of

determination (r^2; Fig. S2, Scenario 2) calculated by least-square linear regression.

Dray & Legendre (2008) showed that the *fourth-corner approach*, if tested by the

permutation test based on reshuffling sample attributes (or rows of species composition matrix,

respectively, model 2 in their paper) also reveals inflated Type I error rate in case of scenario 2. I

applied the fourth-corner analysis also on the simulated community data described above.

Results show, in line with Dray & Legendre (2008), biased values of the fourth-corner statistic

and inflated Type I error rate for the model 2 permutation test (Figs. S3 & S4, Appendix S2),

with the bias (and inflated Type I error rate) decreasing with increasing compositional

heterogeneity (Fig S3 & S4 with Scenario 2, Appendix S2).

Justification of the bias

Simulation study above showed that if hypotheses in category 1 or 3, for which scenario 2 is

relevant, are tested by standard parametric or permutation tests, results are prone to biased

estimates of model parameters and inflated Type I error rate, and the bias is contingent upon

compositional heterogeneity of the community dataset. In this section, I explore the reasons for

this bias, which will be used as a theoretical base for solution proposed in the next section, and

also explain the link of bias to compositional heterogeneity. Note that only hypotheses in

category 1 and 3 are influenced by this bias, since for the category 2 with fixed species and

random sample attributes, scenario 2 is not relevant and the bias therefore does not occur.

A peculiar feature of CWM of species attributes is their "numerical burden", namely that

they are calculated from species attributes assigned to individual species and from species

composition of individual samples, and therefore inherit part of information from both sources.

The numerical difference between calculated CWM values of two community samples is indeed

constrained by a difference in species composition of these two samples - if they have identical

species composition (or identical relative species abundances), their calculated weighted-means

do not differ (because they cannot), and if their species composition differs only slightly, the

difference in their weighted-mean values is likely to be small. This property of weighted-mean

values, which are not independent from each other, has notable consequences for analysis with

sample attributes, if these are themselves related to species composition. In fact the situation is

analogous to the analysis of two spatially autocorrelated variables, just the autocorrelation is not

happening in the geographical space, but in the compositional space (more about this analogy in

the next section). Two values of CWM calculated from community samples sharing some

species do not bring two independent degrees of freedom into analysis, because samples used for

their calculation are not independent - difference in their CWM are predictable (to some extent)

from difference in their species composition in a way that the more similar is species

composition of two community samples, the more similar must be also their calculated CWM.

This problem scales up to the dataset level: in case of two compositional datasets with the same

number of samples used in weighted-mean approach, the dataset which is compositionally more

homogeneous has lower number of effective degrees of freedom compared to the more

heterogeneous one.

Although there are many ways how to quantify compositional heterogeneity of the dataset,

promising is to use beta diversity measure based on Whittaker's index of association (Whittaker

1952; in Legendre & Legendre 2012 as D_9). This index can be numerically derived from

differences in species composition between two calculated CWM values, and therefore quantifies

the dissimilarity in species composition which is directly related to weighted-mean approach

analysis (Appendix S3). To obtain single value of beta diversity for given dataset, one may use

beta diversity metric of Legendre & De Cáceres (2013) quantifying the variation in species

composition, which can be calculated also from symmetric matrix of dissimilarities among all

pairs of samples (here using Whittaker's index of association). Advantage of this beta diversity

metric is that it is independent on the size of the dataset, and the underlying dissimilarity

coefficient is directly related to weighted-mean approach.

Below, I will first illustrate what I mean by the differences in *effective number of degrees*

of freedom in analysis. I use a simple example focused on relationship between community-

weighted mean of traits with environmental variables, and compare two contrasting sampling

designs differing substantially by number of effective degrees of freedom they bring to the

analysis. Then, I elaborate in more detail the analogy to analysis of two spatially autocorrelated

variables, since it offers deeper insight to the problem and inspiration for potential solutions.

Two sampling designs: difference in effective number of degrees of freedom

The following example will illustrate the mismatch between number of effective degrees of

freedom and number of samples in analysis, using species functional traits. The weighted mean

of species functional traits, if combined with environmental variables, is used to investigate

whether the environment filters species into community via their trait properties. Assumption

behind is that the traits are functional, meaning that they directly influence the probability of

species occurrence in community under given environmental conditions, and this hypothesis

therefore classifies into the category 2 described above. For example, plant species specific leaf

area (SLA, Reich et al. 1992) is known to be related to the plant requirements for light, and

shade tolerant species restricted to more shady habitats have larger thinner leafs with higher SLA

values (e.g., Lambers et al. 2008). One may therefore expect that light acts as an environmental

filter for species entering given community, and this filtering is (at least partly) happening

because of species specific SLA. To support this reasoning, let's conduct imaginary experiment:

collect a dataset about composition of understory species in the forest and analyse it by the

weighted-mean approach. Let's keep things simple in this example and assume that we will

compare two forest types, one with open and one with closed canopy, to see whether the closed

canopy filters the understory species with high SLA. When preparing the design of data

collection, we have two options. The first is to choose two vegetation types (e.g. at the level of

association) with contrasting canopy openness, search for them in the study area (this could be

just one forest complex with mosaic of both vegetation types, or a larger region where these

vegetation types occur), sample their species composition and measure the light in the canopy

and SLA of individual species. The second option is to sample open- and closed-canopy forests

without any restrictions about their species composition, possibly in wider area. Following the

first sampling design we get dataset where samples of open-canopy forest are compositionally

similar to each other, as well as samples made in closed-canopy forest (but the composition of

open-canopy forest is different from the close-canopy one). In the second scenario we probably

get samples which all are having rather different species composition.

A simplified example how the species composition of six samples collected by these two

sampling designs would look likes in extreme cases is on Fig. 5. In the case of the first sampling

design, three and three samples have exactly the same species composition, while in the case of

the second design, species composition of each sample is distinctly different from the others (no

species are shared among any pair of samples). In the first case, three and three samples have the

same weighted-mean values since their species composition is identical. In the second case, three

and three samples have also the same weighted-mean values, not because of identical species

composition, but because samples from the same canopy cover category (open or closed) are

made to have similar distribution of trait values (although the species taxonomic identities are

completely different).

Indeed, the real data would fall somewhere in between these two cases, but this example

illustrates well the concept of effective degrees of freedom in weighted-mean analysis. The

relationship of the light availability to weighted-mean of SLA is exactly the same in both cases

(if analysed e.g. by one-way ANOVA in this situation, when environmental variable is

categorical with two levels, open-canopy forest with more light and close-canopy forest with less

light). The difference is in the number of effective samples, which each sampling design offers

for answering our question whether light serves as an environmental filter of species occurrence

in the community via species SLA. Three community samples with completely different species

composition, yet similar CWM of SLA (low for open- and high for closed-canopy forest) offers

considerably better information about interaction between and SLA *per se*, then do the three

samples with identical species composition (and hence also identical low or high CWM of SLA).

Also, what if our assumption is wrong and the SLA is in reality not a functional trait, and hence

belongs to category 3 instead of category 2? Let's replace the real trait values by random one (by

randomizing species attributes among species in table), calculate CWM and test their difference

between open- and closed-canopy stands (and repeat this process 1000 times). In case of the first

sampling design, 87% of tests detect significant difference (874 significant results of one-way

ANOVA at $P < 0.05$), while in case of the second sampling design the probability is near the

expected Type I error rate of 5% (54 significant results out of 1000). This agrees with the result

of weighted-mean approach applied on simulated data saying that inflation of Type I error rate is

high for homogeneous datasets (the case of the first sampling design) and decreases with

increasing compositional heterogeneity (being effectively zero in dataset with all samples

completely dissimilar as in case of the second sampling design).

Analogy to the analysis of spatially autocorrelated variables

The situation when *weighted-mean approach* is based on species composition data, in which

some pairs of samples have the same or similar species composition and sample attributes are

related to species composition, resembles an analysis of two spatially autocorrelated variables. In

case of spatially autocorrelated variables, samples located more close to each other in

geographical space have more similar values than expected if the values are randomly selected

(Legendre & Legendre 2012). In case of weighted means, it is not the proximity in geographical

space, but the proximity in compositional space, which reflects distances between samples

expressed as their compositional dissimilarity.

It has been shown that when analysing two positively *spatially autocorrelated* variables,

spatial autocorrelation biases the results of statistical tests, inflating the type I error rate and thus

resulting into too optimistic results (Legendre 1993). The problem is not with autocorrelation of

individual variables themselves, but with spatially autocorrelated residuals when analysing their

relationship (e.g. by linear regression). From the point of view of the degrees of freedom,

samples located nearby in geographical space are not statistically independent, behaving to a

certain degree as pseudoreplications (Legendre & Legendre 2012). A new observation does not

bring completely new information, because its value can be partly derived from the value of a

nearby site, and the effective number of samples (i.e., effective number of degrees of freedom) is

lower than the real number of samples. Since for standard parametric tests the number of degrees

of freedom is important for choosing the correct statistical distribution, appropriate for a given

sample size, disparity between the real number and effective number of samples leads to

selection of narrower confidence intervals and hence a higher probability of obtaining significant

results (Bivand 1980; Legendre 1993).

The same reasoning applies also for analysis of two *compositionally autocorrelated*

variables. Two weighted-mean values calculated from two samples with similar species

composition do not bring two full degrees of freedom to the analysis, as would be case of two

weighted-mean values calculated from samples with distinctively different species composition.

In a simple example with two sampling designs above, if we want to know whether species SLA

really increases with decreasing light in the understory, we would learn more about this from two

samples in the shaded understory which have different species composition and yet both have

high CWM of SLA, than from two samples which both have similar species composition (and

hence also similar CWM of SLA).

If sample attributes are not related to species composition, than the problem with

effective number of degrees of freedom is not present; although weighted-means are still

compositionally autocorrelated, sample attributes are not – in case of spatially autocorrelated

variables this is analogous to situation when one variable is spatially autocorrelated, but the other

is not, in which case the bias caused by autocorrelation doesn't appear. The situation which

requires attention due to potential bias is therefore limited to cases when sample attributes are

linked to species composition (i.e. they are fixed). This is the case of all internal sample

attributes derived from matrix of species composition, since they are linked to matrix of species

composition (fixed) due to their numerical origin, and also the case of some of external sample

attributes, if these are considered to be fixed (for examples see section *Types of species and*

sample attributes).

Proposed solutions

Analogy between the bias in weighted-mean approach to the bias in analysis of spatially

autocorrelated variables suggests potential toolbox for solving the problem. A simple option

would be to stratify the dataset to reduce redundancy in species composition among samples, i.e.

from pairs of samples with similar species composition remove one of them. Although methods

for stratification based on species composition are available (e.g. Lengyel et al. 2011), it

potentially results into throwing out a large number of expensive data. Alternative option would

be to apply some correction for effective degrees of freedom in analysis, analogously to

Dutiluel's method introduced for estimating effective number of samples in case of

autocorrelated variables (Dutilleul 1993). The option I will further investigate here is based on

comparison of results obtained by weighted-mean approach with those generated by a null model.

Modified permutation test: comparison with the results of a null model

Comparison with results of a null model is an analogy to testing the relationship between

autocorrelated variables using toroidal shift, when one variable is permuted in a way that it

preserves the original degree of spatial autocorrelation (Fortin & Dale 2005). Alternatively, one

can generate random variables with the same degree of spatial autocorrelation as of the original

variable (Deblauwe et al. 2012). In case of compositionally autocorrelated variables used for

weighted-mean analysis, such variables can be generated for weighted-mean values, by

calculating weighted mean from randomized (or randomly generated) species attributes. Such

weighted-mean of randomized species attributes inherits the same level of compositional

autocorrelation as have the weighted-mean values of the real species attributes, because they are

calculated by the same algorithm from the same species composition matrix. One can generate

the null distribution of a test statistic (like t-value for correlation or F-value for regression) for

each weighted-mean of randomized species attributes related to original sample attributes, and

compare the observed statistic (relating the weighted-mean of real species attributes to sample

attributes) to this null distribution. This is identical with the modified permutation test,

introduced to test the relationship between weighted mean of species attributes and sample

attributes by Zelený & Schaffers (2012) in case of relating mean Ellenberg indicator values with

variables derived from ordination/classification based on the same species composition dataset.

To illustrate behaviour of the modified permutation test, I used the set of artificial

community data as above, calculated the correlation between weighted-mean of species attributes

and sample attributes for all four scenarios in communities of increasing heterogeneity, and

tested the significance of this correlation using modified permutation test. Results show that in

contrast to standard permutation test, inflated Type I error rate in case of the scenario 2

disappears (Fig 6b). At the same time, in case of scenario 3 (species composition related to

species attributes, but not to sample attributes) the test is overly conservative for homogeneous

datasets. Additional power analysis (Appendix S4) reveals that the modified permutation test

loses the power with decreasing sample size and mainly with decreasing number of species

which are being permuted (Fig S5 in Appendix S4). Modified permutation test seems therefore

suitable for testing hypotheses in the category 1, which assume that species attributes are random,

while sample attributes are fixed (linked to species composition) and for which scenario 2 is

relevant for testing the null hypothesis. It is, however, not optimal for hypotheses in the category

3, which assume that both species and sample attributes are not fixed (not linked to species

composition), since in scenario 3, which is also relevant as an alternative null hypothesis for this

category, the results are overly conservative (although only for the most homogeneous dataset,

Fig. 6).

Use of the fourth-corner statistic and the sequential test

Dray & Legendre (2008) noted that the fourth-corner statistic *r*, introduced by Legendre et al.

(1997), is "equal to the slope of the linear model, weighted by total species abundances, with the

niche centroids as the response variable and the species trait as the explanatory variable". This

analogy was further elaborated by Peres-Neto et al. (2012, Appendix A), who presented

algorithm how to use the *fourth-corner* statistic in weighted-mean approach. In short, both **R** and

Q matrices are first centred by weighted mean of row sums of **L** (in case of **R**) and column sums

of **L** (in case of **Q**), and rescaled; then, the fourth-corner *r* statistic is the slope of regression

between weighted mean of standardized **Q** and standardized **R**, weighted by row sums of **L**.

Advantage of the fourth-corner statistic is an option to use *sequential permutation test* introduced

by ter Braak et al. (2012), which gives unbiased test of significance for all scenarios (for

application on the simulated community data used above, see Fig. S3 & S4 in Appendix S2).

This sequential permutation test combines results based on permuting sample attributes (model 2)

and species attributes (model 4); if the first one is significant, than the second test is done, and

overall significance of the result is equal to the higher of these two test's *P*-values. Disadvantage,

on the other side, is the fact that the combination of fourth-corner statistic and sequential test

applies only to the regression between standardized (centred and rescaled) species and sample

attributes, weighted by row sums of species composition matrix (**L**), and (to my knowledge) it

cannot be used to test correlation, non-weighted regression or ANOVA between non-centred and

standardized CWM and sample attributes.

Two-step permutation test

As an analogy to the sequential test used together with the fourth-corner statistic, here I introduce

two-step permutation test, which gives unbiased results for relationship between CWM and

sample attributes for range of statistical metrics (*t*-value for correlation and *F*-value for linear

regression tested here). The test is based on combination of standard and modified permutation

test; while both tests give unbiased results for scenario 4, standard test gives unbiased results also

for scenario 3 (in which sample attributes are not related to species composition), while modified

permutation test gives unbiased results for scenario 2 (where sample attributes are related to

species composition). The idea behind the two-step permutation test is to first test whether

sample attributes (**R**) are related to matrix of species composition (**L**), without considering (or

even knowing) the values of species attributes (**Q**). This could be achieved e.g. by constrained

ordination, when sample attributes are used as explanatory variables explaining variation in

species composition. Here I introduce more general solution (called *LR permutation test* within

this paper as a notice that relationship between **R** and **L** matrices is tested), which can be directly

connected to particular test statistic (e.g. *t*-value for correlation). The LR permutation test

consists of the following steps: (i) generate artificial set of species attributes as species centroids

calculated from real sample attributes, (ii) use these species attributes to calculate CWM, (iii)

calculate observed test statistic for relationship between artificial CWM and real sample

attributes, and (iv) test this relationship. The test is based on comparing observed values of the

test statistic (calculated in step iii) with the null distribution of the test statistic, generated in the

following way: 1) randomize sample attributes, 2) use them to calculate species attributes as

species centroids from weighted-means of sample attributes, 3) use these species attributes to

calculate CWM, and 4) relate these calculated CWM with randomized sample attributes from

step 1) to obtain the expected test statistic; repeat steps 1) to 4) n-times (n = number of

permutations). If this test is significant, it means that the sample attributes are related to matrix of

species composition, and relationship of CWM with sample attributes is consequently tested by

modified permutation test. If the test is not significant, standard permutation test is used. When

applied on the set of artificial communities used above, this sequential test gives unbiased values

of Type I error rate for all three scenarios (2, 3 and 4) and for all levels of compositional

heterogeneity (Fig. 6).

Discussion

Main motivation of this study was to show that results of weighted-mean approach critically

depend on the correct decision about the test used for statistical inference. To help in this

decision process, I suggested that each hypothesis can be classified into one of the three

categories, given the explicit (or implicit) assumptions about the role of species and sample

attributes. For each category, I suggested optimal strategy for testing the significance of

relationship between CWM and sample attributes. The decision about appropriate category is not

always straightforward, although the decision whether species attributes should be considered as

fixed or random changes classification of the hypothesis from category 2 (with recommended

standard parametric or permutation test) into category 3 (with two-step permutation test). For

example, trait studies, which are testing whether environment is filtering the species into

community via their functional traits, routinely assume that such traits are functional, and in

weighted-mean approach are therefore considered as fixed (category 2). However, this

assumption may not always be justified; traits included in these analyses are often those readily

available in databases and/or relatively easy to measure, but these do not necessarily need to be

really the functional ones (Fox 2012, Mlambo 2014). In case of compositionally relatively

homogeneous datasets, even the traits with no ecological meaning may show high and significant

relationship to environmental variables if tested by standard tests. I believe that this calls for

revision of such commonly applied practice.

Differences in effective degrees of freedom among datasets complicate comparison of

results between studies based on datasets of different compositional heterogeneities. Studies

conducted on datasets of relatively low beta diversity may obtain stronger and more likely

significant relationship between weighted-mean of species attributes and sample attributes than

studies on datasets of relatively higher beta diversity, even in case that the real link of species

attributes to species composition is missing (Figs. 3 & 4, Scenario 2). This situation is analogous

to biased estimates of model parameters and inflated Type I error rate in analysis of spatially

autocorrelated variables. An option how to deal with this problem is to routinely report, in each

case-study using weighted-mean approach, some standardized value of compositional

heterogeneity. Although this would not remove bias in results of these studies, it would at least

allow for comparison of the potential for bias among different studies. Good metric for this

purpose should be independent on the sample size, and should pertain dissimilarity in species

composition which is relevant for differences in community-weighted means; here, I suggested

beta diversity measure based on Whittaker's index of association (Appendix S3) following the

approach summarized by Legendre & De Cáceres (2013).

Specific question is how to deal with missing values of species attributes for some of the

species. Should species with missing species attributes remain in the matrix of species attributes

and species composition? And in a case of the modified and two-step permutation tests, should

the missing values be kept and permuted among species? The analogy to spatial autocorrelation

issue offers clear answers for these questions. Species with missing attribute values are not used

for weighted-mean calculation, so they do not contribute to the compositional autocorrelation of

weighted-mean values. The point of the modified (and subsequently also two-step) permutation

test is to generate random variables with the same compositionally autocorrelated structure as the

weighted mean calculated from the original species attributes. For this, matrix of species

composition, which inherits the compositional autocorrelation into weighted-mean values,

should remain the same also for calculation of weighted-means from randomly generated species

attribute values. This would not be the case if the species with missing attribute values remains

in both matrices, because permuting missing values would cause the weighted mean of permuted

species attributes being calculated every time with different species composition matrix (the

species which in given permutation run would be assigned missing values will not be included in

this weighted-mean calculation). The solution is hence to remove species with missing species

attributes from both species attributes and species composition matrix, and in the case of

modified permutation test to permute only existing species attribute values. In case that more

species attributes are analyzed (e.g. three different functional traits, or six different species

indicator values) and species has missing species attribute value for some attributes and not for

the others, the species should be removed from species composition matrix only for the purpose

of calculating and testing weighted mean of that species attributes for which the species value is

missing, and not for the others.

Power test using simulated dataset showed that the power of both two-step as well as

modified permutation test decreases with decreasing number of species in the dataset (and less

strongly also with decreasing number of samples). This makes these tests less suitable for

smaller and relatively homogeneous datasets with few species (e.g. less than 40), since the

probability of Type II error (i.e. not rejecting the null hypothesis which is false) strongly

increases. Similarly, both two-step and modified permutation tests are overly conservative for

scenario 3. For modified permutation test this is not a problem, since for the hypotheses for

which the scenario 3 is null hypothesis (category 2) the modified permutation test is not

recommended method (see Table 1). The two-step permutation test is also overly conservative,

but only only in case of the most homogeneous community dataset, and with increasing

compositional heterogeneity this issue diminishes (Fig. 6 and Table S2).

In this study, I explicitly ignored intraspecific variation in species attributes, focusing

only on use of dataset-wide mean species attribute values. Indeed, intraspecific variation may be

important; e.g. in the context of functional traits, the intra-specific variation gains an increasing

attention (Albert et al. 2012), and relevant question is whether the inclusion of intra-specific

variation (e.g. by including trait values which are sample-specific, not dataset-wide) influences

the potential bias reported in this study or not. This question requires further examination, which

goes beyond this study, but in my opinion including another source of variation (species-level

variation in species attributes) does not remove the problem of the bias itself, but makes the

estimation of the bias and its correction more complex.

Finally, relevant consideration is whether the weighted-mean approach is actually the best

analytical solution for question which is being explored. In some cases, the question is explicitly

focused on relating community-level values of species attributes, like mean Ellenberg indicator

values (serving as an estimates of ecological conditions for individual sites) or CWM of traits (as

one of the functional-diversity metrics and as a community-level trait value), and use of

weighted-mean approach is fully justified. Yet, in other cases, when the question is focused on

relating individual species-attributes to sample attributes, weighted-mean approach may not be

the best analytical choice. Use of alternative options, like fourth-corner or RLQ analysis, for

which the problem of inflated Type I error rate and choice of suitable permutation test have been

already solved, can be a better solution.

Conclusions

In this study, I attempted to draw attention to the problem in weighted-mean approach which I

believe is largely overlooked and generally not acknowledged, although it represents a source of

potentially serious misinterpretations. Since in certain fields the weighted-mean approach gains

increasing momentum (e.g. in functional ecology with CWM of species functional traits as one

of the functional-diversity indices), I suggest that time is ripe to critically asses in which

situations and for which types of hypotheses the commonly used standard parametric or

permutation tests are not appropriate, since they yield results which may be overly optimistic. I

offer simple guidelines how to decide whether in given context of a study the standard

methodology gives correct or biased results, and suggest solutions available in case that it does

not.

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Supplementary materials

Appendix S1. Description of an algorithm generating artificial community data along two

environmental gradients.

Appendix S2. Weighted-mean approach applied on simulated data: additional results.

Appendix S3. Dissimilarity index between two CWM values and beta diversity assessment.

Appendix S4. Evaluation of permutation tests using simulated data from Dray & Legendre

(2008).

Appendix S5. R-code for all analyses.

Appendix S6. Source code for the R library *weimea*, version v. 0.58 (actual version can be found

on https://github.com/zdealveindy/weimea/).

Table 1

Overview of the characteristics for the three categories of hypotheses tested by *weighted-mean*

approach. For each situation, corresponding assumption about link between sample attributes (**R**)

or species attributes (**Q**) to species composition (**L**) is given, as well as null vs alternative

hypothesis, scenario relevant in the context of given category (see Fig. 2), and recommended test.

Category	Assumption	Null hypothesis	Alternative hypothesis	Relevant scenario	Recommended test
1	sample attributes fixed (**R** <--> **L**)	**Q** <-//-> **L**	**Q** <--> **L**	Scenario 2	modified permutation test
2	species attributes fixed (**Q** <--> **L**)	**R** <-//-> **L**	**R** <--> **L**	Scenario 3	standard parametric or permutation test
3	no assumptions	**R** <-//-> **Q**, i.e. **R** <-//-> **L** and/or **Q** <-//-> **L**	**R** <--> **Q**, i.e. **R** <--> **L** and **Q** <--> **L**	Scenarios 2, 3 and 4	two-step permutation test

    Figure captions

Figure 1. Computational schema of the weighted-mean approach to analyse relationship between

species attributes and sample attributes via matrix of species composition. **R** - matrix of sample

attributes (e.g. environmental variables), **L** - matrix of species composition ($\mathbf{L_s}$ – **L** standardized

by sample totals to simplify the equation), **Q** - matrix of species attributes (e.g. traits, species

indicator values), **M** - matrix of weighted means of species attributes (e.g. CWM). The colour

gradient within the matrix M (weighted mean of species attributes) from dark to light grey

illustrates that this matrix includes information from both matrix of species composition (dark

grey) and matrix of species attributes (light grey).

Figure 2. Schema showing conceptual differences between scenarios 1-4 in weighted-mean

approach. In scenario 1, both sample attributes (**R**) and species attributes (**Q**) are fixed, linked to

matrix of species composition (**L**), while in the other three scenarios one (or both) of attributes

are considered random, without the link to species composition. In simulated data example, the

link of attributes to species composition is cancelled by permuting the values of species attributes

(scenario 2), sample attributes (scenario 3) or both (scenario 4). In the schema, matrix of species

attributes is transposed (**Q'**) to match the dimension of matrix of species composition (**L**).

Figure 3. Pearson's *r* correlation coefficients among CWM and sample attributes for each of the

four scenarios and ten levels of compositional heterogeneity of species matrix (1000 correlations

for each combination have been conducted). Grey horizontal bars are outliers.

Figure 4. Proportion of significant correlations ($P < 0.05$) between CWM and sample attributes,

tested by standard parametric *t*-test. For each of the four scenarios and ten levels of

compositional heterogeneity of species matrix, 1000 tests have been conducted.

Figure 5. Simplified example of two community datasets (each with six samples) collected in

plots of two different environmental conditions (A and B, e.g. open- vs closed-canopy forest).

First sampling design (a) restricts choice into only two vegetation types (one open- and one

closed-canopy forest), and results into three and three plots with identical species composition.

Second sampling design (b) does not restrict the sampling by choice of community type (any

forest with open- or closed-canopy can be sampled), resulting in situation when none of six

samples share any species in common. For each dataset, three matrices are presented:

sample $\times$ species compositional matrix, matrix of sample attributes (in this case with two-level

categorical variable) and matrix of species attributes (quantitative variable in range 1 to 5). x -

presence of species in the sample.

Figure 6. Proportion of significant correlations ($P < 0.05$) between CWM and sample attributes,

tested by three different permutation tests: standard, modified and two-step. For each of the four

scenarios and ten levels of compositional heterogeneity of species matrix, 1000 tests have been

conducted.

 Figure 1

853   *Figure 2*

856 *Figure 3*

859   *Figure 4*

862 *Figure 5*

(a)

```
            species
                1111:
            12345678901234  env

sample_1    xxxxxx           A
sample_2    xxxxxx           A
sample_3    xxxxxx           A
sample_4          xxxxxxx    B
sample_5          xxxxxxx    B
sample_6          xxxxxxx    B

spec.attr. 11122233344455
```

(b)

```
                          species
                1111:11111222222222223333333333444
            12345678901234567890:23456789012345678901012 env

sample_1    xxxxxxx                                        A
sample_2          xxxxxxx                                  A
sample_3                xxxxxxx                            A
sample_4                      xxxxxxx                      D
sample_5                            xxxxxxx                B
sample_6                                  xxxxxxx B

spec.attr. 11122231112223111222333444553344455334 44455
```

865   *Figure 6*