Cell-to-cell variability in the yeast pheromone response: Cytoplasmic microtubule function stabilizes signal generation and promotes accurate fate choice


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Abstract

In a companion paper, we carried out a high-throughput screen to identify genes that suppressed cell-to-cell variability in signaling in yeast. Two genes affected cytoplasmic microtubules that can connect the nucleus to a signaling site on the membrane. Here, we show that microtubule perturbations that affected polymerization and depolymerization, membrane attachment, and force generation increased variability. For some perturbations, "outlier" cells drove the increased variability. Bypass experiments that activated the PRS ectopically at downstream points indicated that microtubule-dependent processes might stabilize the membrane-recruited scaffold protein Ste5. The variability caused by microtubule perturbations required the MAP kinase Fus3. Microtubule perturbations hindered stable scaffold formation and decreased the accuracy of a polarity-dependent fate choice. Our experiments suggest that membrane-attached microtubules stabilize signaling by scaffold-bound Fus3, and are consistent with a model in which signaling irregularities from changes in microtubule function are amplified by cross-stimulatory feedbacks among PRS proteins. The fact that microtubule perturbations also cause aberrant fate and polarity decisions during embryonic development and cancer initiation suggests that similar variation-reducing processes might also operate in metazoans.

Introduction

In metazoan tissues, populations of cells must determine extracellular ligand concentrations, and, frequently must determine the ligand gradient vector. Cells then must make appropriate fate decisions (including induction of gene expression, cell cycle arrest, differentiation, and polarity determination) in response to those determinations. Maintaining coherence (i.e. limiting cell-to-cell variation) in population responses is critical for the organized sequence of cell and tissue interactions during embryonic development, and for the regulation of cell division and differentiation that defines tissue maintenance in the adult.

In Saccharomyces cerevisiae, the apparatus (the pheromone response system, or PRS) that allows the response to one such extracellular ligand, the mating pheromone α-factor, is well understood. Sensing of pheromone concentration and induction of genes at appropriate levels in response to pheromone depends on a set of proteins and events that here we called the signaling arm of the PRS (Figure 1a). Determination of gradient vector and growth toward mating partner depends on a second set of proteins and events, here called the polarity determination arm of the PRS (Figure 1b). The two arms share protein components localized to the same site on the inner plasma membrane (called, respectively, the signaling site or polarity patch). For example, formation of both the signaling site and the polarity patch depends on the βγ (Ste4-Ste18) subunits of the G protein, which dissociate from the α subunit (Gpa1) after pheromone binds the Ste2 receptor. Moreover, each arm stimulates the other's activity (Figure 1e shows an example of S to P stimulation).

Cell-to-cell variation (quantified as $\eta^2 = (\sigma/\mu)^2$, the square of the ratio between the standard deviation and the mean) in signal, $P$, transmitted through the PRS signaling arm is
under active control (Colman-Lerner et al. 2005, Yu et al. 2008). P is negatively correlated with global gene expression capacity G. The MAPK Kss1 increases $\eta_2(P)$ at low pheromone inputs and the MAPK Fus3 decreases $\eta_2(P)$ at high inputs (Colman-Lerner et al., 2005). The PRS shows an important "systems level" quantitative behavior, DoRA (Dose-Response Alignment) which aligns downstream output with percent receptor occupied (Yu et al. 2008). DoRA can improve the fidelity of information transmission by making downstream responses more distinguishable, and reduce amplification of stochastic noise during signal transmission (Yu et al., 2008, Andrews et al. 2016). The existence of variation suppression mechanisms suggests that, during evolution, accuracy of information transmission by cell signaling systems may have been under selection.

In the companion paper, in order to reveal additional processes that affected variation, we constructed a collection of more than 4,000 yeast strains, each of which carried a deletion of a single nonessential gene. These strains also carried the reporter genes needed to quantify cumulative system output (O), cumulative transmitted signal (P), and variation in these quantities $\eta_2(O)$ and $\eta_2(P)$ and output of control promoters in individual cells. We then carried out a large, technically complex, high-throughput (more than 1000 strains with different deletions) flow cytometric and microscope-based screen to find genes that affected cell-to-cell variability in signal transmission and gene induction. From this screen, we identified 50 "variation genes" required for normal cell-to-cell variability in signal and response. Some genes affected variability in system output, $\eta_2(O)$, or in transmitted signal $\eta_2(P)$, but not the mean in these parameters, O or P. Thus, those two variability phenotypes define independent “axes” of system behavior, and the wild type genes as "canalizing" (Schmalhausen (1949) and Waddington (1942)) the variation (e.g. Jimenez-Gomez et al. 2011, Makumburage and Stapleton 2011) in these traits. Some of these genes that affected $\eta_2(P)$ also affected microtubule function. These included GIM4 and PAC10/GIM2, whose products form part of a six-protein prefoldin complex needed for tubulin supply, and BIM1, whose product mediates attachment of cytoplasmic microtubule plus-ends to the signaling site. We selected BIM1 and one of the two prefoldin genes, GIM4, as candidates to explore the relationship between microtubule function and signaling variation.

During yeast mating, cytoplasmic microtubules are critical for nuclear fusion (Molk and Bloom, 2006). Early in the pheromone response, Gpa1, the Gα subunit of the heterotrimeric G-protein, associates with the pheromone receptor Ste2, binds the microtubule motor Kar3/Cik1, and recruits it to the signaling site (Zaichick et al. 2009). Kar3/Cik1 subsequently captures plus ends of astral microtubules, which begin growing (by plus end polymerization and depolymerization) from the SPB in the nuclear membrane. The plus ends randomly explore the inner plasma membrane until they are caught by Gpa1. At least during bud formation, other microtubule plus ends reach the signaling site when complexed with Bim1 and its anchoring partner Kar9 (Maddox et al. 2009). When those plus ends are bound by Bim1 and Kar9, Kar9 can contact the motor protein Myo2 (ten Hoopen et al. 2012), suggesting that Myo2 can then walk the Bim1/Kar9-complexed plus ends down the actin cables emanating from the signaling site until they reach the cell membrane. Once at the signaling site, the microtubules alternately bind
Bim1 and Kar3/Cik1. Bim1 acts passively: it only binds to polymerizing microtubules. Therefore, Bim1 bound microtubules become progressively longer. By contrast, when fixed in the membrane, Kar3/Cik1 hydrolyzes GTP and depolymerizes microtubule plus ends. Membrane bound microtubules therefore alternate between growth and shrinkage (Maddox et al., 2009). Later in the pheromone response, once the cell fusion stage of mating is completed, microtubules from both partners associate across the fusion site and pull both nuclei towards each other, in a process called “nuclear congression”, which culminates with the fusion of the two nuclei into a diploid nucleus (Molk et al. 2006, Molk and Bloom, 2006).

Given the above picture of microtubule function during the pheromone response, we considered how BIM1 and prefoldin might be required to diminish variability in the transmitted signals. One idea was inspired by two observations. The first were reports (Maeder et al. 2007, and very recently, Conlon et al. 2016) showing that, in cells exposed to saturating isotropic pheromone, the concentration of active system MAP kinase (phosphorylated Fus3), occurs in a gradient that has its highest value at the shmoo tip, in which the signaling site is located. The other observation was the opposing actions of Kar3/Cik1 and Bim1 described above. The alternation in forces pulling the nucleus towards the shmoo tip (Kar3/Cik1) and pushing it away (Bim1) causes the nucleus to maintain a “fixed” position at the base of the mating protrusion (Maddox et al., 1999, see BOX and Figure 1c). No role had been assigned to this maintenance or homeostasis of nuclear position; the position of the nucleus would not seem to be relevant to the later processes of nuclear congression and fusion. We therefore hypothesized that the precise control of nuclear position within a Fus3 gradient might reduce variability in the strength of the signal transmitted to the nucleus.

A second idea for how normal microtubule function might reduce signaling variability was based on the vulnerability of signaling to positive regulatory interactions at the signaling site/polarity patch. We wondered if the presence of multiple microtubule plus ends at the signaling site might, perhaps because of their sheer size (the outer diameter of each microtubule is 24 nm) affect delivery of new proteins and mRNAs to the site via actin cables (Botstein et al. 1997), or that the polymerization and depolymerization of plus ends might perturb the operation of some other proteins, for example by affecting the local GTP concentration. We realized that any small fluctuation might be amplified by a complex set of direct and indirect positive feedbacks at this membrane site. Activated Cdc42 exerts direct positive feedback on its own recruitment and activation (Butty et al., 2002, Irazoqui et al., 2003) (Figure 1d). In addition, during polarity determination, Cdc42, whose localization is stimulated by actin cables originating from the polarity patch, also recruits and activates Ste20 (Moskow et al., 2000), the PRS MAPKKKK, which in turn leads to the activation of the MAP Kinase Fus3 in the signaling arm (here, called P to S stimulation) (Figure 1a). Moreover, during signaling, the MAPK Fus3, after activation while bound to the Ste5 scaffold, binds Gpa1 and activates the formin Bni1, stimulating actin cable formation and causing transport of additional Cdc42 to the site (S to P stimulation, Figure 1e). Moreover, activated Gpa1 activates an mRNA binding protein Scp160, which transports mRNAs including those encoding Fus3 to the site. Due to these
complex cross-stimulatory interactions, each arm of the PRS should exert positive feedback on its own induction and operation. Positive feedbacks can improve the performance of controlled systems (for example water wheels (Molinié, 1837) servo systems, Hazen, 1934, and electronic amplifiers, Armstrong, 1913, Meissner, 1914, and Franklin, 1913). However, without damping or negative feedback, systems with positive feedbacks are prone to instability (Bennett, 1979). In the PRS, cross stimulation and positive feedback are likely constrained by the fact that both arms compete for components in limited supply. For example, both the S and P arms require the Gβ subunit, Ste4, for their operation, but each cell contains only ~2000 molecules of the Gβ complex even when all ~7500 molecules of the receptor (Thomson et al., 2011) are bound. We thus hypothesized that in normal cells, the attachment, polymerization and depolymerization of microtubule plus ends might be concerted with other activities at the signaling site, so that self-amplifying fluctuations might be minimized.

Here, we undertook experiments to test these ideas. Our results did not support the idea that nuclear positioning might control signaling variation. Our experiments did show that an attached microtubule bridge reduced variation in signaling and in polarity decisions, that interference with attachment of the bridge impaired the formation and stability of the signaling site, leading to erratic signaling in the PRS. They were thus consistent with the idea that the increased variation in signaling and polarity decisions might be due to instabilities in signaling introduced by microtubule perturbations further amplified by positive feedbacks at the signaling/polarity site.

Results

Mutants altered in different variation genes showed distinct differences in signal transmission

From a genetic screen in a companion paper, we found genes that affected cell-to-cell variability in transmitted signal, η^2(P). Some of these affected microtubule function. These included GIM4 and PAC10/GIM2, whose products are needed for tubulin subunit supply, and BIM1, whose product is needed for attachment of plus ends to the signaling site and their subsequent polymerization.

To better characterize signaling in ∆bim1 and ∆gim4 mutants and to test the idea that increased η^2(P) was due to their failure to position the nucleus correctly within a cytoplasmic gradient of activated Fus3, we constructed strains (SI and Table S1) that carried the fluorescent protein reporter for the pheromone response subsystem (P_{PRM1} promoter driving mCherry), a constitutive control reporter to allow measurement of activity of the gene expression subsystem, common to all genes (P_{ACT1} promoter driving CFP), as well as a histone Htb2-YFP chimera to allow precise measurement of nuclear position (see below).

We used time-lapse microscopy in single cells of these strains to measure total system output (O, the accumulated mCherry), transmitted signal (P, the ratio between the accumulated mCherry and CFP), and variability in these values. Figure 2 shows plots of P in single cells over time ("trajectories") after stimulation with 20 nM pheromone. We first analyzed how these
trajectories were grouped. The reference strain ("wild-type") cell trajectories were clustered relatively tightly: The most extreme cells deviated from the average P by less than 50%, while in \( \Delta bim1 \) and \( \Delta gim4 \) populations, the most extreme cells deviated from the mean by substantially more than 50%. The \( \Delta bim1 \) and \( \Delta gim4 \) cells differed strikingly in terms of how common such extremely high or low Ps were. \( \Delta gim4 \) cell populations presented a broader distribution of trajectories around the mean. In contrast, in \( \Delta bim1 \) populations, most cells had trajectories like the reference strain, but a number of "outlier" cells showed P very far from the mean.

To quantify these differences and test their significance, the standard deviation or similar statistics are not well suited, since many distinct distributions may have the same standard deviation, and kurtosis is too sensitive to outliers (see Discussion). Thus, we developed a distribution, the progressive spread distribution (PSD), whose median (MPS) is an appropriate measure of the way a distribution is shaped. The MPS value conveys the dispersion observed in the better-behaved half of the cell population. The higher the MPS, the broader the distribution (see Methods). For the cells in Figure 2, the MPS for the reference population was 0.22 (95% CI 0.19 - 0.23), for \( \Delta bim1 \) cells it was 0.24 (95% CI 0.17 - 0.31, not distinguishable from reference), while for \( \Delta gim4 \) cells it was 0.36 (95% CI 0.32 - 0.37). Restated, these results show that the distribution of trajectories in \( \Delta gim4 \) cells is significantly broader overall than WT, while, for \( \Delta bim1 \) cells, population behavior differs because of outlier cells, while the majority of cells behave normally. We consider the possible significance of these metrics and of outlier cells later (see discussion).

We then analyzed the stability of the trajectories over time. In all populations, the trajectories of most individual cells were stable, while a few cells showed unstable increases in P (evidenced as erratic or "crooked" trajectories (red traces in Figure 2)). For reference cells, stable and crooked trajectories occurred throughout the range of values of P. For \( \Delta bim1 \) cells, cells with crooked trajectories occurred at the same frequency above and below the mean P, and accounted for almost all the cells with extreme values of P. By contrast, \( \Delta gim4 \) cells showed crooked trajectories only for values of P below the mean. Since \( \Delta gim4 \) cells also showed a reduction in system output (O), this result suggested that the increased variation in P (\( \eta^2(P) \)) in \( \Delta gim4 \) populations might be linked to reduced signal, with some cells with low signal exhibiting unstable trajectories. We take crooked trajectories as evidence of erratic operation of the signaling machinery during the course of the experiment (see discussion).

**Microtubule perturbations have distinct effects on the position and movement of the nucleus relative to the signaling site**

To pursue the question of whether variation in nuclear position caused variation in transmitted signal, we determined the relation between P and the distance to the nucleus from the signaling site in single cells. In \( \Delta bim1 \) cells, Bloom and collaborators had measured this distance under saturating pheromone stimulation (Maddox et al. 1999). Based on this and other work (Maddox et al. 2003, Zaichick et al., 2009, Box) we expected that \( \Delta bim1 \) cells would not be able to properly position their nuclei during pheromone stimulation. However, there was no
published work on the effects of the Δgim4 mutation or other prefoldin mutants on nuclear positioning. Thus, as a next step we sought to learn the effects of microtubule perturbations on nuclear positioning.

We thus measured the position of the nucleus in the same cells in which we analyzed trajectories. To do so, we used the signal from Htb2-YFP, which labeled the nucleus, to measure the shortest distance between the base of the mating protrusion (starting with the site on the cell perimeter at which the protrusion starts forming) and the nuclear edge. We first plotted time courses of nuclear distance from the shmoo base in these cells, stimulated with a saturating dose of pheromone. Figure 3a shows the results. As expected and described (Maddox et al, 1999), in the reference cells nuclei moved synchronously and rapidly from various initial locations to 0-1 µm away from the base of the mating protrusion. In Δbim1 populations some nuclei moved towards the base of the mating protrusion, while other nuclei seemed to wander in the cytosol. In Δbim1 cells, both sorts of nuclear movement were characterized by sudden changes in position, more frequent and drastic than in reference cells. In contrast, in Δgim4 populations nuclear position was as coherent as in reference cells. However, in Δgim4 cells, nuclei took longer to initiate their movement towards the shmoo base, with the majority remaining at the same distance for two hours or more.

To better measure the position of the nucleus, we made another set of strains (SI and Table S1). In this set, we expressed an Spc42-GFP fusion, which labels the SPB (Spindle Pole Body, the yeast MTOC, MicroTubule Organizing Center), and a Sec8-mCherry fusion, which labels the signaling site/polarity patch. We then stimulated these cells with pheromone. The use of these two labels allowed us to obtain precise measures of the distance between the SPB and the signaling site at all pheromone doses (Figure 3aii and iv). However, because the signals were weak and we needed to acquire several images in the z-axis to find them, photobleaching of the fluorophores prevented us from taking time-courses in individual cells. Figure 3ai shows the results. In these strains at saturating pheromone doses, the Spc42-GFP signal appeared as a single dot in the cytosol of each cell, and the Sec8-mCherry signal formed a small crescent at the shmoo tip (Figure 3Ai). At concentrations near the receptor EC50, Sec8-mCherry localized to one of the two otherwise indistinguishable ends of the enlarged arrested cells (Figure 3aiii). In reference cells stimulated for two hours at saturating pheromone doses, the nuclei were between 1 to 3 µm from the signaling site (Figure 3aii), in agreement with the work of Maddox et al. (1999). In Δbim1 cells the mean SPB-to-signaling site was larger, and the distance ranged from between 2 to 7 µm. In Δgim4 cells, the mean SPB-to-site distance was unchanged relative to the reference cells, but the distribution of distances was broader. In reference cells at the EC50 pheromone dose, which causes cell cycle arrest but not shmooing (Figure 3A iii), we observed an even shorter distance between the nucleus and the signaling site, 0 (too close to resolve) - 2 µm, including a striking ~30% of cells in which we could not measure any distance between the nucleus and signaling site (Figure 3A iv). At the EC50 dose, effects of the Δgim4 and Δbim1 mutations on nuclear distance were qualitatively similar to those at saturating
pheromone, with the exception that the $\Delta gim4$ cells showed larger SPB to nuclei distances, in the 1-3 µm range.

Taken together, these results were consistent with the idea that microtubules comprise a force-generating tether connecting the signaling site and the nucleus. They also demonstrated that the $\Delta bim1$ and $\Delta gim4$ mutations partially disrupt its function. They confirmed previous observations about Bim1’s role in positioning the nucleus during the pheromone response and showed that prefoldin activity is also required for this process. Thus, both mutations we had identified as causing increases in $\eta^2(P)$ also caused changes in one or more aspects of the position of the nucleus relative to the signaling site, including average distance, variation in distance, and tempo of positioning.

**Microtubule-perturbation-induced changes in nuclear position do not correlate with changes in pathway output**

We next sought to test the hypothesis that the amount of transmitted signal depended on nuclear position. If so, $P$ in single cells might be a negative (or positive) function of the nucleus-to-signaling-site distances. We examined this correlation in populations of reference and mutant cells. Figure 3c shows the results. Neither mutant ($\Delta gim4$ or $\Delta bim1$) nor reference cells show a correlation between instantaneous or average nucleus to site distance and the rate of change of output $O$ (here, a proxy for $P$). The most straightforward interpretation of these results is that the distance between the signaling site and nucleus does not affect the strength of the transmitted signal, $P$.

These results did not exclude the idea that the lack of relation between $P$ and the nucleus-signaling site distance might be because the nucleus is constantly moving, especially in the mutant strains, and as a result of that movement, the observed $P$ is actually an average of higher and lower $Ps$ (when the nucleus is closer or farther from the signaling site, respectively). To test this possibility, we generated a $kar3\text{-}1$ (rigor mutation) Htb2-YFP strain in which the microtubule bridge was stable and did not change in length. The Kar3-1 protein binds microtubules plus-ends, but can neither actively depolymerize nor release them. $kar3\text{-}1$ strains therefore maintain cytoplasmic microtubules attached both the shmoo tip and nucleus, and these microtubules do not change in length (Maddox et al., 2003; Meluh and Rose, 1990). In our $kar3\text{-}1$ strain, the nucleus did not move to the shmoo base, its distance from the signaling site varied significantly from cell to cell (1.5 to 6 µ,Figure 3d), but it did not change over time in each cell. Figure 3D shows that, in $kar3\text{-}1$ cells, there was no correlation between nucleus to signaling site distance and output $O$, a proxy for $P$. This result confirmed that $P$ is not a function of the distance between the nucleus and the signaling site, and showed that the MAPK signal can reach the nucleus even when the nucleus is not in line with the signaling site.

**Inhibition of microtubule polymerization and depolymerization increased signaling variation**

The above results showed that increased signaling variation in $\Delta bim1$ and $\Delta gim4$ strains were not related to the position of the nucleus relative to the signaling site, and were consistent
with the idea that their effects were due to alteration of some other aspect(s) of microtubule function. To explore how altered microtubule function might increase variation, we examined the effect of perturbations that disrupted different aspects of microtubule function.

We first tested chemical treatments that cause the depolymerization of dynamic microtubules. We used the microtubule-polymerization inhibitors benomyl and nocodazole at concentrations reported to induce breakdown of cytoplasmic microtubules (Palframm et al. 2006). Figure 4 (lower left) shows that chemical disruption of microtubules caused a decrease in $P$ at doses of pheromone higher than the EC50, consistent with the decrease in $P$ in $\Delta bim1$ and $\Delta gim4$ strains. However, unlike the effects of $\Delta bim1$ and $\Delta gim4$, these microtubule poisons did not affect $\eta^2(P)$ (Figure 4, upper left). This result was again consistent with the idea that the effect of $\Delta bim1$ and $\Delta gim4$ on $\eta^2(P)$ could be due to these mutants perturbing specific aspects of microtubule function. In this view, microtubules are present and functional in both deletion strains, but, are either impaired in their ability to attach to the site of polarized growth ($\Delta bim1$) or less abundant ($\Delta gim4$). However, these results again do not exclude the idea that the effects of $\Delta bim1$ and $\Delta gim4$ on $\eta^2(P)$ could be unrelated to their effects on microtubule function. To distinguish between these possibilities, we used additional genetic perturbations that affected other aspects of microtubule function.

**Microtubule perturbations affecting membrane attachment, polymerization and depolymerization increased signaling variation**

We next disrupted microtubule polymerization and depolymerization by a targeted genetic perturbation: expression of a dominant negative variant of $\alpha$-tubulin, encoded by the $TUB1$-$828$ allele. When expressed at low levels in cells containing wild type $\alpha$-tubulin, Tub1-$828$ is incorporated into the growing microtubule tip, where it blocks polymerization and depolymerization (Anders and Botstein, 2001). Since high levels of Tub1-$828$ block further cell division (Anders and Botstein, 2001), we used the $GAL1$ promoter, expressed at low levels in cells grown in glucose medium (Guarente et al., 1982, Yocum et al. 1984), to drive Tub1-$828$ expression (SI and Table S1). Figure 4 shows that, in glucose medium, Tub1-$828$ expression increased variation in transmitted signal, $\eta^2(P)$ at all pheromone doses tested. In galactose medium, at higher levels of Tub1-$828$ expression where cells were blocked from further division, we also observed increased $\eta^2(P)$ (not shown). We also observed increased $\eta^2(P)$ in cells in which higher levels of Tub1-$828$ were expressed in an inducible system in which estradiol activates $P_{GAL}$ (see below and (Louvion et al. 1993)). These results strongly supported the idea that altering microtubule function increases variation in transmitted signal.

We next blocked microtubule pulling by constructing (SI and Table S1) otherwise-isogenic $\Delta kar3$ and $\Delta cik1$ strains and measured the effect of these genetic alterations on signal. Kar3 and Cik1 proteins are needed for active, ATP-dependent depolymerization of membrane-attached microtubule plus ends. Figure 5 shows the results. Compared to the reference strain, cells of the $\Delta kar3$ strain showed the same level of output $O$, while $\Delta cik1$ strains showed a reduction in $O$, i.e., the measured data cover a smaller horizontal range for $\Delta cik1$ than for the
For comparable values of $O$, both perturbations significantly increased variation in transmitted signal, $\eta^2(P)$. These results show that two independent mutations that, like $\Delta bim1$, reduce the ability of microtubules to bind to the site of polarized growth, also increase $\eta^2(P)$. Because both $\Delta bim1$ and $\Delta kar3$ also substantially reduced the fraction of cells with a microtubule bridge attached to the signaling site (Maddox et al., Bloom 1999), we hypothesized that the reason $BIM1^+$ and $KAR3^+$ cells maintain low variability might be that in these cells the microtubule bridge between nucleus and the signaling site was intact. In this view, the additional microtubule functions of pulling in ($KAR3$) and pushing out ($BIM1$) the nucleus might not be not required for the control of $\eta^2(P)$. To test this hypothesis, we again made otherwise-isogenic strains that carried $kar3^{-1}$, the rigor variant of Kar3 in which the microtubule bridge is intact but in which microtubules cannot change in length. Figure 5 shows the results. The rigor mutation slightly lowered $O$, but increased $\eta^2(P)$ by at least a factor of three, as much as the full $\Delta kar3$ lesion. These results show that attachment of the microtubule bridge was not sufficient to control $\eta^2(P)$. They suggest that, to lower $\eta^2(P)$, microtubules not only have to be attached, but must also be able to alternatively push and pull on the nucleus and exert force.

Finally, we tested the effects of preventing the attachment of microtubules to the SPB. To do that, we replaced $KAR1$ with the $kar1^{-15}$ allele (SI and Table S1). $KAR1$ encodes a component of the SPB. The $kar1^{-15}$ allele expresses a C-terminally truncated variant of Kar1. In pheromone treated cells, the Kar1 C terminus is the main site of minus-end microtubule anchoring to the MTOC (Pereira et al., 1999), and its absence leads to detachment of cytoplasmic microtubules from the nucleus and from the signaling site (Erlehman et al. 2012). Relative to the reference cells, populations of $kar1^{-15}$ cells showed decreased $O$ but no change in $\eta^2(P)$ (Figure 5), similar to the effect of microtubule depolymerizing drugs (Figure 4). These results support the idea that complete loss of the microtubule bridge reduces $P$ but does not increase $\eta^2(P)$.

Taken together, these results suggested that a) an intact microtubule bridge was needed for the full signal transmission ($P$) by the PRS; b) normal cell-to-cell variability in PRS signaling required correct operation at the plus ends (perhaps the ability to generate force), where the microtubules attach to the signaling site, but not at the minus ends, where they attach to the nucleus. Thus, one or more steps that take place at the signaling site might be affected when microtubules operation is not normal. In the next section, we sought to find the affected steps.

**Genetic bypass of Ste5 recruitment restored coherent population responses**

To better understand possible mechanisms by which normal operation of cytoplasmic microtubules might control variation in the pheromone response, we used artificial “bypass” activators to identify pathway step(s) at which microtubule action affected signaling.
variation. Bypass activators activate systems "ectopically", that is at different steps along the causal chain of signal transmission in the PRS. (Beadle and Ephrussi, 1936, 1937, Botstein and Maurer, 1982, Cairns et al. 1992, Takahashi and Pryciak 2008). In a linear pathway, a result showing that a bypass activator is not affected by a perturbation is considered evidence that a perturbation such as a mutation acts upstream or at the ectopically activated step. In systems with feedback and feedforward loops such experiments by themselves cannot preclude other interpretations (Avery and Wasserman, 1992), for example that a downstream perturbation might transmit via feedback its effects upstream of the ectopic activator.

To perform the bypass analysis, we generated a set of strains that conditionally expressed, in the absence of pheromone, one of four different proteins that activated the PRS at different steps, (Takahashi and Pryciak, 2008, SI and Table S1). Expression of each PRS activator protein was driven by $P_{\text{GAL1}}$, whose activity was controlled in turn by an estrogen-responsive Gal4 derivative, originally developed by Picard and collaborators (Picard 1994). In the order of their function in the pathway, the activator proteins were a) native Ste4, whose expression mimics dissociated (i.e., active) Gβγ dimers (Pryciak and Huntress, 1998); b) Ste5-CTM, a fusion of the Ste5 scaffold with a transmembrane domain, whose expression mimics membrane-recruited (i.e. activated) Ste5 (Pryciak and Huntress, 1998); c) a Ste11-4-Ste7 chimera, a fusion of the Ste11-4 mutant protein, a constitutively active form of Ste11, to the MAPKK Ste7, whose expression mimics activated Ste7 (Harris et al., 2001); and finally d) native Ste12, whose overexpression mimics activated Ste12 (perhaps due to titration of inhibitory factors (Dolan and Fields, 1990; Takahashi and Pryciak, 2008; Tedford et al., 1997)). To prevent interference from basal activation of the native PRS, strains expressing activators b), c) and d) also carried a Δste5 mutation. Finally, strains in this set also carried both PRS responsive ($P_{\text{PRM1-mCherry}}$) and constitutive ($P_{\text{BMH2-YFP}}$) reporters. From each bypass activator strain, we generated four strains which were either unperturbed, carried the Δbim1 or Δgim4, or expressed the Tub1-828 protein.

Figure 6A shows the results. Each plot shows $\eta^2(P)$ as a function of $P$ at different estradiol doses for the unperturbed strain (gray curves) and the strains with three microtubule perturbations (blue curves). Each row of plots corresponds to one of the four bypass activators (Ste4, Ste5-CTM, Ste11-4-Ste7 and Ste12), while each column of plots corresponds to one of the microtubule perturbations (Δbim1, Δgim4, and Tub1-828-expression). If the site(s) of action for the microtubule perturbations were downstream of the Ste4 activation step, then the perturbations would still show their effects in the Ste4 activator strains. This was so. All three perturbations Δbim1, Δgim4 and Tub1-828 expression caused increases in $\eta^2(P)$ , the same effects they had when we stimulated the PRS with pheromone (data not shown). The increase in $\eta^2(P)$ in Δbim1 was similar in both systems, while for Δgim4 it was less pronounced in the artificial activator system. For Tub1-828 expression the increase in $\eta^2(P)$ was also similar in both systems, although we could only assess it at low values of $P$, because Tub1-828 expression had an unexpectedly strong inhibitory effect on $P$ (see below).
In the Δbim1 and Δgim4 strains, the higher-than-reference $\eta^2(P)$ phenotype was suppressed by all activators downstream of Ste4 (compare plots in Figure 6A columns 1 - Δbim1- and 2 - Δgim4). The suppression was clearest for Δbim1, for which the increase in $\eta^2(P)$ was present in the Ste4 activator strain and completely suppressed in all downstream activators. The suppression was less conclusive for Δgim4 because the increase in $\eta^2(P)$ in the Ste4 activator strain was smaller and the suppression by the downstream activators was not complete. By contrast, the increase in $\eta^2(P)$ caused by Tub1-828 expression was not suppressed by any of the bypass activators. These results suggested that the microtubule-dependent process(es) perturbed by the Δbim1 mutation, and possibly also by Δgim4, increased signaling variation the PRS at or upstream of the recruitment of Ste5 to the membrane.

We also sought to map the steps in the PRS at which perturbations to microtubule function affected total transmitted signal, P. Figure 6B plots P vs dose. Δbim1, Δgim4 and Tub1-828 expression caused decreases in P. For Δbim1 and Δgim4, the effects on P in the artificial activator system were qualitatively similar to their effects on P in the normal PRS. (see companion paper). The magnitude of the decrease in P due to Δbim1 in the artificial activator system was similar to that in the PRS. For Δgim4 the decrease in P in the artificial system was less pronounced. By contrast, in the artificial system, Tub1-828 expression a strong inhibitory effect on P, which it did not have in the PRS (Figure 4 and data not shown), perhaps due to very high expression of the Tub1-828 protein at high estradiol doses driven by the Gal4-ER-VP16 fusion.

The reduction in P caused by Tub1-828 expression was completely suppressed by the artificial recruitment of Ste5 in the STE5-CTM strain. That is, the reduction in P caused by Tub1-828 expression mapped to the Ste5 recruitment step. By contrast, the reduction in P caused by the Δbim1 and Δgim4 mutations was present in the Ste5-CTM strain but bypassed in the strains with downstream activators.

These results showed that, with one exception (very high levels of Tub1-828 expression), the effects of all the perturbations on $\eta^2(P)$ and P can be bypassed. They thus established that the microtubule perturbations directly affected the pheromone response by interfering with specific steps in signaling rather than acting indirectly by causing unrelated changes in the cell. They also suggested that microtubule perturbations affected output P and pathway variation $\eta^2(P)$ by two different mechanisms, one at or upstream of Ste5 recruitment and the other upstream of the MAPK activation step, and that BIM1 and GIM4 are involved in both of them.

**Induced signaling variation by microtubule perturbations requires Fus3**

The above bypass experiments suggested that both the function of the microtubule bridge in normal pathway output and the involvement of Bim1 and Gim4 in maintaining low variability depended on Ste5 recruitment. Ste5 is a cytosolic protein that, upon pheromone stimulation, is recruited to the membrane, primarily by binding to activated Ste4 and secondarily by binding to phospholipids in the membrane. At the membrane, Ste5 localizes the
MAPK Ste11 MAPK and the MAPKK Ste7. We showed in previous work that a negative feedback
requiring the downstream MAPK Fus3 diminishes retention of Ste5 at the membrane (Yu et al.
2008, Bush and Colman-Lerner 2013). Here we tested whether low variability and normal
pathway output mediated by Bim1, Gim4, and the microtubule bridge depended on the action
of membrane-localized Ste5 and the partially redundant Fus3 and Kss1 MAPK kinases.

To do so, we generated four strains (S1 and Table S1) with a normal PRS, but each
bearing deletions of GIM4 or BIM1 and also deletions of FUS3 or KSS1, and measured $\eta^2(P)$ as a
function of $P$. Figure 7 shows the results. Notably, in $\Delta$bim1 and $\Delta$gim4 strains, the $\Delta$fus3
deletion suppressed completely the increased $\eta^2(P)$ observed in the single deletion strains, at all
doses (Figure 7). That is, Fus3 protein was required for these microtubule perturbations to
increase $\eta^2(P)$ (Figure 7).

The fact that the $\Delta$fus3 deletion eliminated the increases in signaling variation caused by
the $\Delta$gim4 and $\Delta$bim1 mutations again shows that the increased variation is not a secondary
consequence of a generalized increase in variability in cells with disrupted microtubule function,
but rather reflects an effect of these mutations on operation of the PRS.

Perturbation of microtubule function increases variation in establishment and maintenance
of the initial signaling site

The above experiments indicated that Ste5 membrane recruitment/retention and the
action of membrane bound Fus3 was the point at which $\Delta$bim1 and $\Delta$gim4 deletions introduced
variation into signaling. We thus sought to validate these results by directly observing Ste5
membrane localization in the natural PRS and in the perturbed strains. We constructed
otherwise-isogenic strains that expressed Ste5 fused in frame to three copies of YFP (Ste5-YFP-
YFP-YFP, here called Ste5-YFP). In previous work, we used this construct to show that, in cells in
the G1 phase of the cell cycle, cytosolic Ste5-YFP translocates to the plasma membrane
isotropically within 2-3 minutes of exposure to isotropic pheromone, followed after 2 to 30
minutes by clustering of the Ste5-YFP signal into the signaling site, a single patch in the plasma
membrane that coincides with the site of future shmoo growth (Figure 8A) (Ventura et al.,
2014). In addition to the reference strain, this strain set was also comprised of strains that had
the $\Delta$bim1, $\Delta$gim4 or the $\text{tub1-828 expression}$ perturbations. We exposed these cells to a high
pheromone dose and monitored them by fluorescence microscopy for up to three hours.

In cells of the reference strain, for the first 45-120 min, the Ste5-YFP patch was visible as
a crescent at the tip of the growing shmoo. In most cells the shmoo tip ceased growing after 45-
120 min. In these cells a second site of polarized growth appeared later in a different location.
Before the second site of growth was morphologically visible, a second Ste5-YFP patch appeared
at the site that would become the second site of growth. Progressively, the second site became
brighter while the first site faded (Figure 8A). Compared with cells of the reference strain, cells
bearing microtubule perturbations showed several common differences. First, in the perturbed
strains, a greater number of cells failed to form a signaling site (Figure 8B). This result is in
agreement with our earlier observation that in Δbim1 and Δgim4 populations about 5% of the cells did not induce a $P_{PRM1}$-mCherry reporter after pheromone treatment (Pesce et al., companion paper). Second, in perturbed cells that formed a signaling site, the mean time to site formation was longer and more variable. Third, in perturbed cells, the first site on average lasted a shorter and more variable time. Fourth, in perturbed cells, the time from initiation of the first patch until appearance of the second was on average shorter and more variable. By contrast, compared with the reference strain, the perturbed strains showed no differences in the average and variability of duration of the second patch. Restated, these observations showed that cells with microtubule perturbations had difficulties establishing and maintaining their first signaling sites, but not their second. Some cells failed to form sites, others showed delays of variable length in formation of the first site, and all showed shorter times (also of variable length) to its dissolution. The fact that formation and maintenance of the second site in these cells was normal shows that these three microtubule perturbations do not cause a generalized cellular malaise that indirectly impacts signaling site formation, but that rather they affected the formation of the first signaling site. The results also suggest that the formation and stability of the second site do not require the microtubule functions we assessed above, and thus suggesting that it did not require the microtubule bridge.

**Perturbation of microtubule function decreases accuracy of polarity decisions in speed mating experiments**

Our results pointed to a role for the microtubule bridge in promoting the rapid establishment and sustained maintenance of the signaling site. Haploid *S. cerevisiae* prefer to mate with partners expressing wild type levels of mating pheromone than with partners expressing lower levels (Jackson and Hartwell, 1990). In mixed species mating experiments, haploid *S. cerevisiae* prefer to mate with one another, but also out compete cells from other related species (Murphy and Zeyl, 2010, 2012), in part by mating more quickly (Murphy et al. 2006). For *cerevisiae*, one part of mating more quickly would be rapid establishment of a stable signaling site oriented toward the correct, high expressing suitor. To test the importance of initial site establishment in mating partner choice, we modified a technique first developed by Hartwell and collaborators (Jackson et al. 1990). In both the original and our methods, mating occurs in mixtures in which MATa cells from the strain being tested are combined with equal numbers of two strains of MATα partners that i) secrete different amounts of pheromone and ii) carry a marker than can be measured in the resulting diploids. In the variant we used here, one of the MATα partner strains (MATα Δade2 MFALPHA1) secreted normal levels of pheromone while the other (MATα ADE2+ Δmfalpha1) lacked one of the two genes encoding pheromone and thus produced an estimated 5% of WT levels of pheromone. Mating of MATa Δade2 cells with low-producing suitors produces Δade2/ADE2+ diploids, which form white colonies on low-adenine medium, while mating of MATa Δade2 partners with the high-producing suitors produces Δade2/Δade2 diploids, which form red colonies on the same medium. We mated MATa cells with a 10-fold excess of a 1:1 mix of high-producing and low-producing MATα partners for different lengths of time, resuspended cells in starvation medium, sonicated the
mating mixtures, spread the cells onto selection plates, and scored the color of the resulting diploid colonies.

Figure 9 shows the outcome. In these assays the reference MATa cells showed significant preference for mating with the high-pheromone producing partner (65% of the diploid colonies were red, 35% were white.) Among the mutant strains, only Δgim4 mated with the same discrimination efficiency as wild-type, with Δbim1, Δbim1 Δgim4, and Tub1-828-expressing strains all showing at least marginally significant large reductions in frequency of choosing the normal-pheromone partner, relative to wild-type. We made this comparison via the two-sample t-test; p-values were 0.064, 0.67, 0.025, and 0.034, for the Δbim1, Δgim4, Δbim1Δgim4, and Tub1-828-expressing strains, respectively, for the data shown in Figure 9B.)

In the control matings, done for 1 hour (not shown), the Δbim1, Δgim4 and Tub1-828-expressing strains were as able as the reference strain to mate efficiently and preferentially with high expressing partners, confirming that these perturbations did not disrupt those aspects of mating. In contrast, in 5-minute mating reactions, the Δbim1 and Tub1-828-expressing strains showed 35% and 50% reductions, respectively, in their ability to choose "correct" high expressing partners (Figure 9B). The Δgim4 mutation did not affect discrimination on its own, nor did it affect discrimination when combined with the Δbim1 mutation (Figure 9B). Restated, in mating assays dependent on the rapid establishment of a signaling site, loss of Bim1 protein and Tub1-828-expression increased variability in transmitted signal η²(P) (where P is the ratio PPRM1-XFP/ PAT1-YFP, as usual) and impair mating partner choice, while loss of Gim4 only increased variation in η²(P).

Discussion

Although much is known about how cell signaling systems operate, little is known about cell-to-cell variation in their operation. Here we investigated a possible microtubule-dependent process, identified by a genetic screen, that reduces variation. Our results showed that disruptions of microtubule function that affect the nucleus-to-signaling-site bridge increased variation in signal transmission, decreased coherence in population signaling and gene expression, and decreased accuracy of polarity decisions. The loss of coherence in signal and response was entirely suppressed by bypassing the natural means of recruitment of the MAPK scaffold Ste5 to the plasma membrane. Genetic epistasis experiments and direct observation suggested that the microtubule perturbations affected membrane residence of the scaffold protein Ste5.

We first discuss genetic implications of these results and then discuss what they might tell us about mechanism. To test the effects of perturbations on microtubule function, our overall approach (used for some time) (Brent and Ptashne, 1984, 1985, Colman-Lerner et al., 2005) was to compare quantitative behaviors in different clonal populations of cells of otherwise-isogenic strains with defined genetic differences. We found that reduction of variation required the genes BIM1 and GIM4, which affect cytoplasmic microtubule function,
and that it also required other functions, including plus-end attachment to the signaling site, and the ability of the microtubule plus ends to exert force by polymerizing and depolymerizing while attached to the signaling site. Perturbations affecting these functions increased variability in transmitted signal among cells in the population. Moreover, a number of them caused signaling within individual cells to become erratic.

Our work defines \textit{BIM1} and \textit{GIM4} as canalizing genes, affecting stochastic variation around the mean values of measures of signal transmission, independently from their effects on the mean itself. Recent studies have identified a number of genes and alleles that affect variation, rather than mean, in quantitative traits as varied as plant height, flowering and leaf number, intracellular abundances of particular proteins and mRNAs, and the number of somatic cells present in fresh cow milk (Ansel et al., 2008; Fraser and Schadt, 2010; Hall et al., 2007; Jimenez-Gomez et al., 2011; Landers and Stapleton, 2014; Makumburage and Stapleton, 2011; Ordas et al., 2008) (Mulder et al., 2013). 20th century population genetic formalisms (e.g., Hartl (1980)) attributed variation in quantitative traits either to differences in genetic background or to differences in "environment", and a good deal of initial work focused on genetic and other mechanisms by which organisms canalize (or suppress) (Schmalhausen (1949), and by Waddington (1942)) variation due to these two causes. Researchers later recognized a third source of variation, attributed to stochastic events (Ansel et al., 2008; Jimenez-Gomez et al., 2011; Makumburage and Stapleton, 2011) or to unknowable differences in the "microenvironment" (Fraser and Schadt, 2010; Mulder et al., 2013), for example during development (Waddington, 1957), defined operationally by differences in quantitative phenotype among genetically identical organisms (animals) raised in homogeneous environments (Gärtn er, 1990). Some theoretical arguments suggest that genes that canalize traits in the face of genetic and environmental differences (Meiklejohn and Hartl, 2002), and in the face of stochastic differences (Lehner, 2010) might be the same. However, we note that loci that canalize variation in quantitative phenotype caused by differences in environment in other organisms were found by mapping of QTL (Quantitative Trait Loci), so the fact that those loci also reduce variation due to differences in genetic background is not surprising. Moreover, because canalizing loci found by QTL mapping suppressed variation among organisms grown in the same environments, they by definition diminished variation due to “microenvironmental” and stochastic differences. Thus, the fact that \textit{BIM1}, \textit{GIM4}, and some canalizing genes affect variation due to all three causes is not unexpected.

Our identification of \textit{BIM1} and \textit{GIM4} as canalizing genes illustrates the frailty of generalizations advanced about such genes based only on population-genetic arguments. These canalizing genes do not operate in some genetic backgrounds (for example, in cells with mutations in proteins that attach microtubules to the signaling site) and would not operate in some environments (for example, those containing chemical inhibitors of microtubule formation). Moreover, in our own previous work, we identified other processes and molecular mechanisms, depending on specific negative feedbacks and specific protein kinases (Colman-Lerner et al., 2005; Yu et al., 2008) that reduced variation in isogenic populations in the same
environment, that would not operate in genetic backgrounds deficient in these components. Similarly, recent studies in mice, Arabidopsis, and maize reveal canalizing loci, that suppress stochastic variation around mean values, that operate in some environments but not others (Fraser and Schadt, 2010; Jimenez-Gomez et al., 2011; Makumburage and Stapleton, 2011). Thus, taken with previous work, our results establish that genes that reduce variation in specific traits caused by differences in genetic background, differences in environment, and by stochastic causes are not always the same.

In this work, standard deviation, and the related CV and normalized variation used in our previous work (Colman-Lerner 2005, Yu 2008, Pesce 1), provided limited descriptions of variation phenotypes. By eye, measurements of signal transmission over time revealed that clonal populations with some microtubule perturbations had more cells with near average behaviors and a few outliers, while behaviors of cells with other microtubule perturbations were more broadly distributed. Such differences are probably consequential, for example, during metazoan embryonic development and adult tissue maintenance when malfunctioning canalizing processes that increased the number of rare cells that divide or divide out of plane lead to defects and dysplasias. And yet, these sorts of differences in distribution shape were also not well captured by kurtosis, a standard measure of distribution shape that works best with large samples of outlier-free data. We therefore devised a robust and hypotheses-free measure we called "Median Progressive Spread" or MPS, and used it to quantify differences in the distributions of single cell behaviors in mutant populations. This measure worked well for our purposes, and reinforced the point that measures of "deviations from normality" may in some circumstances provide more biological insight into variation than the standard deviation and CV commonly used by population geneticists (Lewontin, 1966).

To understand the mechanism by which microtubule function suppressed variation in signal, we first considered studies by (Maeder et al., 2007, Colon et al. 2016) which reported a gradient of the Fus3 protein kinase originating at the signaling site. We tested a mechanical model in which the microtubule bridge regulates signal strength by precisely positioning the nucleus within the gradient of Fus3, and for which perturbations to microtubule function resulted in a more variable position of the nucleus within the gradient. The underlying assumption in this model was that the strength of the signal that reaches the nucleus is stronger when the nucleus is closer to the signaling site. We found no correlation between nuclear distance from signaling site and O, which we used as a proxy for P (masking of correlations between nuclear position and P would require a very specific and unlikely relationship between O and nuclear distance, hence O is a good proxy for P). Our results did not support this simple "motion-in-a-gradient" model, although they do not exclude more complex possibilities, for example that the amount of Fus3 along the gradient is not proportional to signal strength, or that the Fus3 gradient varies so much among individual cells that the distance of nucleus from signaling site is not a good measure of signal level.

We therefore pursued a general approach to learn where in the signaling pathway microtubule-dependent processes reduced variation in signal. To do so, we treated variability in
transmitted signal $\eta^2(P)$, as a simple (albeit difficult to measure) quantitative trait. We then used the estrogen-inducible synthesis of proteins that activated the PRS ectopically at different steps downstream of the receptor to bypass the pathway steps at which the microtubule perturbations acted to produce the trait. These "suppression by epistasis" (Hodgkin, 2005) experiments showed that the tested microtubule perturbations introduced variation into the signal at steps between Ste5 recruitment and activation of the MAP kinase cascade. They suggested that microtubule function(s) stabilized signaling by membrane-localized Fus3 MAP kinase. We confirmed by direct experiment that enhancement of the variation in signal by microtubule plus-end perturbations at these steps required the Fus3 MAP Kinase. This series of experiments thus extends and generalizes the scope of a classical genetic method first used in the 1930s (Beadle and Ephrussi 1936), and subsequently used extensively in analysis of regulatory pathways in C. elegans and Drosophila (Avery and Wasserman 1992).

Our epistasis suppression results were consistent with the idea that the microtubule perturbations might interfere with signaling by the MAP kinase Fus3 when localized to the membrane via the membrane-recruited Ste5 scaffold. Ste5 signaling complexes form at the signaling site, which is co-territorial on the membrane with the polarity patch, which defines the site of future polarized growth. We showed that, in some cells in the population, microtubule perturbations slowed the initial establishment and shortened the lifetime of the Ste5 signaling site. We next showed that plus-end microtubule perturbations interfered with a fate decision that depends on correct polarity determination; they interfered with the ability to choose high pheromone-expressing partners in "speed mating" experiments, but not with the ability to choose correct partners given more time. Restated, these experiments showed that perturbations to microtubule function destabilized the signaling site and interfered with rapid polarity decisions.

Taken together, our results suggest a possible explanation for how perturbations to cytoplasmic microtubule function could increase signaling variation and interfere with polarity determination. This idea is based on the fact that the signaling site and the polarity patch both stimulate one another’s activity and compete for a limited supply of shared protein components (see Introduction). In this view, unattached microtubule plus-ends disrupt movement and membrane recruitment of proteins, including Cdc42, Cdc20, and Ste5, in their neighborhood. Variable recruitment of Ste5 causes variability in Ste5-dependent signaling, which is then subsequently amplified by the complex positive feedbacks that affect recruitment, trafficking, accumulation, and activation of the numerous proteins and mRNAs, including Ste5 itself, to the signaling site and polarity patch. Moreover, if any of the proteins needed for signaling and polarity determination are transported along microtubules, the fact that the untethered plus-ends cannot hand off cargo to actin cables growing from the signaling site would result in further variability in accretion of signaling and polarity proteins. It is interesting in this context that another protein identified in the high throughput screen, Erv46, is a component of COPII transport vesicles. Restated, in this view, increased variability in Ste5 recruitment to the signaling site causes variability in the amount of signal the site sends via Fus3, and the positive
feedbacks amplify this variability. This picture is consistent with our finding that Fus3 is needed for signal variability, and of course with If so, this picture is consistent with conclusions from control theory, in which control of servomechanisms and electronics by positive feedback alone is prone to instabilities.

The complexity of the above model drives home the point that our current means for approaches to perturbing the system and monitoring its operation are not sufficient to elucidate the process under study: how the normal operation of cytoplasmic microtubules helps the cell transmit a signal of constant strength. Too much remains unknown. At the signaling site, there are too many different proteins operating, too many positive cross-regulatory interactions, too many simultaneously occurring mechanical processes like cargo delivery and membrane fusion that are now insufficiently understood. It is as if we had learned to monitor frequency and timing of sounds given off by an electric motor that was operating abnormally because we had disrupted the operation of particular bearings, bushings, and shafts. In this light, our analysis of signal control has explored an "inverse problem", for which inferences from doable experiments are insufficient to describe the system under investigation (Brenner, 2010). But the sort of genetics-powered quantitative physiology we have employed here does have utility. Certainly, it can of course identify important proteins. Moreover, in some cases, it can establish important physical and regulatory processes for which the theory of how human-built machines (eg, Meiksen, 1959, Bennett, 1979) are controlled (here, how positive feedbacks lead to instabilities) can provide small additional insights. Moreover, consider the motor analogy above. In it, different bands of frequencies of noises coming from the partly-malfunctioning machinery will reflect different aspects of motor function. In the same way, here and in the companion paper, we assert that attention to different kinds of system malfunction will lay groundwork for future insight by identifying different aspects or axes of system function dependent on different subsets of system proteins and molecular events.

Reduction of variation by cytoplasmic microtubule function may also be important in metazoans, for coherent population fate decisions (eg proliferation, apoptosis, and differentiation) and polarity decisions needed to form and maintain correct tissue architecture. Cytoplasmic microtubule function in vertebrates is even more complex than that in budding yeast. At the plus-end, mammalian orthologs of yeast Bim1, MAPRE1-3/EB1-3 (Su and Qi, 2001), interact with +TIP proteins, many of which are involved in cell polarity decisions (Sayas and Avila, 2014). These include APC (Adenoma Polyposis Coli), required for radial glial cells to polarize in response to extracellular cues, and for them to support birth and migration of the neurons that make up the cell layers of the cortex (Yokota et al., 2009). Microtubule-end-dependent polarity decisions during adult cell growth and proliferation are important for maintenance of a cancer free soma. APC is a tumor suppressor, frequently inactivated in colorectal cancers (Kinzler and Vogelstein, 1996) and other epithelial tumors (Vogelstein et al., 2013). APC is a negative regulator of the Wnt/β-catenin signaling pathway (Bienz and Clevers, 2000). But APC also carries out other functions suggested by its protein interaction partners (Brent and Finley, 1997), which include plus-end-associating kinesins, formins and actins found...
at sites of polarized growth (Lesko et al., 2014). At the minus end, lesions in proteins that connect microtubules to the MTOC in the nuclear membrane (in particular the Nesprin-1 and Nesprin-2 isoforms encoded by SYNE1 and SYNE2 (reviewed by Gundersen and Worman (Gundersen and Worman, 2013)) contribute to formation of some solid tumors (e.g. squamous cell carcinomas of the head and neck (Stranksy et al., 2011)) in which tumor development requires incorrect polarity decisions that allow cells to divide out of an epithelial plane. Human exome sequencing reveals considerable coding sequence polymorphism in genes encoding MAPRE/EB1, APC, and other microtubule-end-interacting proteins in the human population (Fu et al., 2013), suggesting that different allelic forms of these proteins might have quantitative effects on cell polarity decisions in response to signals and so affect cancer incidence (Britain and Brent, unpublished).

Box

Methods
General methods, yeast strains and plasmid construction are detailed in Supplementary Information.

**Analysis of cell-to-cell variation in signal and response.** We obtained cell images and fluorescent signals as described previously (Colman-Lerner et al., 2005; Gordon et al., 2007). We sonicated cell cultures in microfuge tubes and incubated for 3 hours at 30 °C in medium with 10 μM 1-NM-PP1 and 0, 0.6 nM or 20 nM α-factor. We manually curated timecourses to eliminate cell outlines showing segmentation mistakes, overlapping cells and other imaging artifacts. In these assays, cell densities were in the OD₆₀₀ 0.02 – 0.1 range.

To analyze the data, as in Colman-Lerner et al. 2005, we bounded the system and defined total system output by the total accumulated signal from a fluorescence protein reporter gene driven by a pheromone-induced promoter \( PRM1 \). We then divided the PRS into a “pathway subsystem”, which included all the events leading to activation of transcription, and an “expression subsystem”, which includes all the events from transcription initiation through accumulation of expressed protein. In this framework, the system output for any given cell \( O_i \) was the product of the average pathway subsystem output per unit time \( P \) which varies with input pheromone dose, the expression subsystem output \( E \), and the duration of stimulation \( \Delta T \) (Colman-Lerner et al., 2005), as follows:

\[
O_i = P \times E \times \Delta T
\]

We considered output of each subsystem to be the sum of the capacity of the subsystem in each cell (i.e., “capacity”) plus stochastic fluctuations in the operation of that subsystem during the course of an experiment (“noise”): \( L \) and \( \lambda \), respectively, for the pathway subsystem, and \( G \) and \( \gamma \) for the expression subsystem. Thus,

\[
O_i = \left( L_i \times \alpha F + \lambda_i \right) \times (G_i + \gamma_i) \times \Delta T
\]

We defined the variation in system output as the normalized variance of in \( O \), \( \eta^2(O) \) decomposable into the sum of individual sources and a correlation term (Colman-Lerner et al., 2005), as follows:

\[
\eta^2(O) = \eta^2(L) + \eta^2(\lambda) + \eta^2(G) + \eta^2(\gamma) + 2\rho(L,G)\eta(L)\eta(G)
\]

In the WT, in the deletion strains, and mutants used in the manuscript, we measured output of each reporter; as well as \( \eta^2(P) \) (i.e. \( \eta^2(L) + \eta^2(\lambda) \)), pathway variation, for the pheromone response system. We estimated \( \eta^2(P) \) as the variance in the difference of the normalized abundances of the two fluorescent proteins, one driven by the \( PRM1 \) promoter and the other driven by the constitutive, pheromone-independent promoter \( PA1 \) or \( BMH2 \) depending on the strain). This variance is actually equal to \( \eta^2(P) + \eta^2(\gamma) \) (see supplement), but we have previously shown that \( \eta^2(\gamma) \) is small enough (Colman-Lerner et al., 2005) to make our estimate a good approximation for \( \eta^2(P) \).
To quantify the perception that in microscopic time course measurements, the spread of trajectories for cells of some strains differed in both magnitude and quality from the corresponding spread for other strains, we developed a statistical measure we called the progressive spread distribution (PSD). For each strain, we computed the PSD by first computing the absolute deviation from the median of each cell’s final pathway output. We then sorted these deviations from smallest to largest. We found the first value of the PSD by starting with the two trajectories with smallest absolute deviations and finding the difference between the corresponding pathway output values. We computed the next value of progressive spread by including the value of pathway output corresponding to the cell trajectory with the third smallest deviation, and again finding the range of corresponding outputs, and so on until we had included trajectories for all the cells in each tested population of each strain. For a given set of pathway output measurements, the last value of the PSD was simply the full range of the pathway output values. For symmetric distributions, the median of the PSD, which we call Median Progressive Spread (or MPS), is equivalent to the interquartile range.

**Chemical inhibition of microtubule function.** For every experiment in every strain, we grew cells in medium with microtubule-polymerization inhibitors for 3 hours, then counted % cells arrested in metaphase. If the proportion of arrested cells was >95%, we declared that the treatment had worked. For the experiments in the GPY4000 reference strain, we also made a derivative that expressed GFP-Tub1 instead of Tub1 and observed disappearance of visible microtubule bundles after chemical inhibition.

**Analysis of nuclear movements.** We defined nuclear position in two ways. One was by the position of the SPB, which attaches microtubules to the nucleus. To do so we used otherwise-isogenic cells that expressed an SPB component, Spc42, tagged with Green Fluorescent Protein. We defined the signaling site using RFP-tagged Sec8, verifying its localization to the shmoo tip by inspection of brightfield images (not shown). We divided cells into two aliquots. We treated one with 50 nM pheromone, a concentration at which most receptors are occupied, cells shmoo, and there is low cell-to-cell variation in transmitted signal (low $\eta^2(P)$) (Colman-Lerner et al. 2005). We treated the other aliquot with 1 nM pheromone (the EC 50 dose), a concentration that half-saturates receptor and arrests progression through the cell cycle. At this concentration cells do not shmoo, but form a broad mating projection known as a peanut (Figure 3A iii) and show high cell-to-cell variation in transmitted signal ($\eta^2(P)$). The other means to track nuclear position was to mark the nuclear volume with a fluorescent signal. To do so, we used strains expressing HTB2-YFP, a histone subunit, and used the $P_{\text{PRMI-}}$mCherry and $P_{\text{ACT1}}$-CFP reporters to measure pathway output in the same cells.

**Analysis of Ste5 membrane localization.** Ste5 protein is present at very low numbers. There are ~500 molecules per cell on average (Thomson et al., 2011), and due to significant YFP fluorophore maturation times, when Ste5 is tagged with YFP only ~350 of 500 YFP-Ste5 are fluorescent in exponentially growing cells (Gordon et al.). In these cells, the fluorescence signal from YFP-Ste5 molecules is barely above background autofluorescence. To increase the signal-to-background ratio, we used strain MW003 (Ventura et al., 2014), a strain that expresses three
copies of chromosomally integrated \( \text{STE5-YFP(x3)} \), in which three copies of YFP are fused to 3’ end of the \( \text{STE5} \), expressed from native promoter sequences. For this fusion protein, tripling the gene dosage increases the signal-to-noise ratio while only modestly perturbing levels of Ste5 and system activity, as reflected by the amount of reporter gene output (about 1.5 times wild-type cells, data not shown). We stimulated this strain’s cells with 1 \( \mu \text{M} \) pheromone (high pheromone) collected scanning confocal fluorescent microscope images every 10 minutes over 4 hours (see Supplement).

To quantify Ste5 patches, we created image montages of each cell automatically using Rcell’s function \textit{cimage}. These montages included all Z slices for every time point in an ordered layout. We identified Ste5 patches manually and tagged them using ImageJ’s plugin Cell Counter on the image montages. Cells were presented in random order (with no identifying label) to avoid any bias in the manual quantification. The tag data created with Cell Counter was then mapped to the corresponding cell in the Cell-ID dataset (Bush et al., 2012; Gordon et al., 2007) for further analysis in R.

We assessed the significance of differences in quantitative variables (e.g. time to 1st pol, 1st pol duration, etc.) using permutation tests (Good, 2004), which gave results consistent with traditional parametric tests (e.g. t-test, F-test of variance, etc). We assessed the significance of differences in the fraction of cells with a given phenotype (cells with coexisting polarizations for more than 60 min, cells with no polarizations, etc.) using Fisher’s exact test for count data. We calculated standard errors for all variables using bootstrap resampling (Efron, 1979).

**Partner choice mating assays.** The rapid mating protocol is derived from a previously published method (Jackson and Hartwell, 1990). We grew MATa and MATalpha cells overnight to exponential phase. In the morning we counted the number of cells/ml in each culture with a hemocytometer. Next, we made a 50:50 mixture of GPY4077 (Reference or “WT” MATalpha \( \Delta \text{ade2} \)) and GPY1551 (MATalpha \( \Delta \text{alpha1 ADE2}+ \)) cells. We added approximately \( 10^7 \) cells of this mixture (about 1 ml) to 15ml BD Falcon tubes. To supplement the concentrations calculated from the hemocytometer, we counted plated dilution series from the MAT alpha mixture on YPD plates in quadruplicate. On these plates, each viable GPY4077 cell (or cell clump) will form a pink colony and each viable GPY1551 cell (or cell clump) will form a beige colony. We sonicated the cultures of reference MATa cells (GPY4078) and otherwise-isogenic \( \Delta \text{bim1} \), \( \Delta \text{gim4} \), \( \Delta \text{bim} \Delta \text{gim4} \), and \textit{Tub1-128-expressing} perturbed cells to be tested, counted them in a hemocytometer, and plated out dilutions as above.

We performed all mating experiments in triplicate. To carry out the mating, we added \( 10^6 \) MATa cells (about 0.1ml) to the \( 10^7 \) cells in the MATalpha mix Falcon tube, vortexed, and vacuum filtered the cells onto a 0.2 \( \mu \text{m} \) Millipore nitrocellulose filter. We placed the filter face up on uracil-deficient agar medium and incubated at 30ºC for 5 minutes. We transferred the filters to 5 ml of SD-N (nitrogen deficient medium; \( \text{H}_2\text{O}, 2\% \text{ glucose, and 1X YNB with no ammonium sulfate or amino acids} \) and vortexed for 30 seconds at maximum power with a Fisher Vortex Genie 2. We sonicated these mating mixtures for three minutes at power 3, and
plated ~200 cells from the mating mixtures (having diluted cells to densities estimated from previous hemocytometer counts) onto SD deficient in lysine, methionine, and adenine using 3mm glass beads. On this medium, only diploids grow. On this medium, diploids resulting from mating of MATα GPY4078 cells with "correct" MATα wild type GPY 4077 cells form pink colonies, diploids resulting from mating with lower-pheromone-expressing GPY1551 strain form white colonies. We scored the plates by hand after two days of incubation at 30°C. In control experiments against GPY4007 cells, under these conditions 3-5% of reference MATα cells and Δbim1 and Tub1-828-expressing cells mated and formed diploids.

**Author contributions**

GP and SZ performed the microtubule perturbation and epistasis suppression experiments. WP showed the Fus3 dependence of the introduced variation and analyzed, plotted, and determined statistical significance of quantitative results. AB and VR quantified effects of microtubule perturbations on the Ste5 patch at the signaling site. RCY contributed to experimental design, data analysis and earlier versions of the manuscript. RB, GP and AC-L directed the work and its interpretation, wrote the paper, and guarantee the integrity of its results.

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**References**


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**Figures and legends**

**Figure 1.**

**a. The signaling arm of the pheromone response system (PRS).** After Ste2 binds the α-factor ligand, the following events lead to the expression of pheromone responsive genes (PRGs). (1) The trimeric G-protein Gpa1/Ste4/Ste18 dissociates and thus becomes active. (2) Ste20 is recruited to the membrane by a complex containing Cdc42 and Cdc24 (This is an example of positive regulation of the signaling arm by the polarity determination arm, or P to S stimulation) Ste20 makes independent contacts with the membrane (not shown here). (3) The Ste20/Cdc42/Cdc24 complex binds to the dissociated G-protein Ste4/Ste18. (4) The Ste20/Cdc24/Cdc24/Ste4/Ste18 complex recruits the scaffold protein Ste5 to the cell membrane. (5) Thus recruited, Ste5 enables Ste20 activation of the MAP kinase cascade from MAPKKK Ste11 through MAPKK Ste7 and MAPK Fus3. (6) Some phosphorylated Fus3 then enters the nucleus to phosphorylate Ste12, Dig1, and Dig2 (not shown), thereby inducing the expression of PRGs, which here include fusions of $P_{PRM1}$ to fluorescent proteins. Ste7 can also phosphorylate Kss1 which can enter the nucleus and activate PRGs (not shown). Events (1) and (2) are independent and may occur concurrently.
b. Membrane-bound components of the polarity determination arm of the PRS. Many of these proteins (but not Far1 and Bni1) are shared with the signaling arm. Bni1, a formin, stimulates actin cable formation when phosphorylated by Fus3 (Matheos et al. 2004). Actin cables nucleated at Bni1 in turn provides a route for delivery of vesicles and cargo to the membrane and transport and attachment of cytoplasmic microtubules (S to P stimulation, Figure 1e) (Karpova et al. 2000).
c. Microtubule bridge connecting the signaling site and the nucleus. Schematic of a shmooing cell showing the signaling site (for simplicity, only Ste2 and Ste5 are shown), with Bim1 and Cik1/Kar3 anchors respectively polymerizing (pushing) and depolymerizing (pulling) cytoplasmic microtubules at their plus ends. Cytoplasmic microtubule minus ends attach to the microtubule organizing center/spindle pole body (MTOC/SPB) in a process that requires Kar1. The gradient of grey in the cytoplasm represents a gradient of activated MAPK Fus3 (Maeder et al. (2007), Conlon et al (2016)). Inside the nucleus, the pheromone-induced genes concentrate on the proximal side, closest to the signaling site (Casolari et al., 2005).
**d. Self-stimulation of Cdc42 membrane recruitment and activation.**  
(1) The small G protein Cdc42 is activated (converted to GTP-bound form) at some basal stochastic rate. **(2) Activated Cdc42 recruits a complex containing Bem1, Ste20 and Cdc24. (3) Membrane associated Cdc24 (a guanine exchange factor or GEF) activates additional membrane-bound Cdc42. (4) As in (2), activated Cdc42 recruits additional Bem1/Cdc24/Cdc42 complexes, completing the positive feedback loop (Kozubkowski et al 2008, Johnson et al. 2011)**
e. Stimulation of polarity patch formation by activity of Fus3 (S to P stimulation). (1) Fus3 is phosphorylated and activated due to the operation of the PRS signaling arm. Some phosphorylated Fus3 binds to the Gpa1 subunit of the dissociated G-protein. (2) Gpa1-bound Fus3 activates Bni1, which nucleates formation of actin cables. (3) Additional proteins involved in signaling, cell polarization, and cell fusion, including Cdc42 and Fus2 (Paterson et al., 2008, not shown) are then trafficked to the membrane as cargo carried along the actin cables. (4) Microtubule plus ends are captured by Kar3/Cik1 associated with Gpa1 (not shown) and Kar9/Bim1-complexed plus ends can be walked down the actin cables to the polarity patch by motor proteins including Myo2 (not shown). Microtubules, actin cables and cargo proteins are larger than the approximate scale used here would indicate. Also not shown is a second, more complex instance of stimulation involving Fus3. In this process, activated GPA1 allows the RNA binding protein Scp160 to complex with mRNAs encoding polarity and signaling proteins (called POLs), including Fus3 (Gelin-Licht et al. 2012). These mRNAs are trafficked down actin cables to the site, and, when translated, increase the amounts of proteins such as Fus3 at the site (S to S) stimulation. Activated Fus3 protein stimulates the formation of more actin cables (S to S and S to P stimulation).
**Figure 2.** Accumulated signal $P$ vs time in reference and microtubule perturbed cells. y axis shows $P$ measured in individual cells of the reference (GPY4143, "wild type"), $\Delta bim1$ (GPY4144) and $\Delta gim4$ (GPY4150) strains. We induced the PRS by addition of 20nM pheromone to the medium and imaged cells every 30 minutes as in (Colman-Lerner et al. 2005 and Gordon et al., 2007). In all populations, about 5% of the cells do not respond to pheromone induction. Traces correspond to pathway output (inducible $P_{PRM1}$-mCherry signal/ constitutive $P_{ACT1}$-CFP signal) from individual cells followed over time. For each strain, variation in the inducible $P_{PRM1}$-mCherry signal was larger than variation in the constitutive $P_{ACT1}$-CFP signal (not shown). For each strain, we colored the 10 most stable trajectories green, and the 10 least stable (crooked) trajectories red. The black bar shows the full range of WT responses, for comparison.
Figure 3. Distance and change in distance between nucleus and signaling site in microtubule perturbed cells. (A) Images of cells expressing Spc42-GFP, which marks the MTOC, and Sec8-RFP, which marks the signaling site. On the left, images show reference (“WT”) and Δbim1 cells.
(GPY1752 and GPY1709)-- cells of the Δgim4 strain (GPY1759) were visually indistinguishable from images of WT cells and thus were not shown. Images were recorded after 90 min of exposure to high (20 nM, i-ii) or intermediate (2 nM, iii-iv) pheromone doses. On the right, histograms show distances in μm between the MTOC and the signaling site (the shmoo tip) for reference (WT, blue), Δbim1 (orange) and Δgim4 (green) cells. (B) Time courses of the distance between base of the shmoo (where the cell wall is before the protrusion starts growing) and the nuclear edge (visualized by Htb2-Venus) after stimulation with 20 nM pheromone, for reference, Δbim1, and Δgim4 cells as in A, with the same color-coding. At each time point, we computed the 0.25 and 0.75 quantiles, and used these to shade the middle two quartiles. The white dashed line marks the mean, and we drew a dashed black reference line to indicate 1 μm distance. (C) Signaling strength (P) in kar3-1 (rigor mutant) strains. We stimulated kar3-1 cells (SGA150, expressing Htb2-Venus to mark the nucleus and bearing P_{PRM1}-mCherry and P_{ACT1}-CFP reporters to monitor P) with 20 nM pheromone for 180 min. Panel shows the P vs distance between the site of polarization and the nucleus for kar3-1 cells, with each dot representing a single individual cell from this clonal population. We estimated Pathway output P from the ratio between the output of the P_{PRM1} and P_{BMH2} reporters. At this pheromone concentration, these kar3-1 populations showed three-fold higher signal variation (not shown).
Figure 4.

Cell-to-cell variability in transmitted signal, $\eta^2(P)$, and in cumulative transmitted signal, $P$, in strains treated with chemical and genetic inhibitors of microtubule polymerization and depolymerization. Top row shows $\eta^2(P)$ as a function of $P$ (top row), Bottom row shows $P$ as a function of dose. The Tub1-828-expressing strain (GPY1873) was a derivative of GPY4000. Strains in left column were treated with nocadazole/benomyl, strains in right column were and perturbed by Tub1-828 expression (right column).
Figure 5. Cell-to-cell variability in signal transmission in cells with mutations affecting microtubule end function. Left panel shows $\eta^2(P)$ versus output O in $\Delta kar3$ (SGA2015), $kar3$-1 (SGA108, the "rigor mutant"), and reference cells (SGA103). Right panel shows $\eta^2(P)$ versus O in $kar3$-$\Delta 15$ (SGA109) cells, $\Delta cik1$ (GPY4123) cells, and reference cells (SGA103).
Figure 6A. Microtubule perturbations affect cell-to-cell variation in cell signaling at the Ste5 recruitment and MAP kinase steps.

We exposed reference ("WT"), Tub1-828 expressing, Δbim1 and Δgim4 derivatives of GPY1810 (bearing the chimeric genes P_{PPRM1-mCherry}, P_{BMY2-YFP}, and a gene constitutively expressing the chimeric transcription factor P_{BMY2-GAL4BD-hER-VP16}), to the indicated concentrations of estradiol to induce expression of the ectopic activators of the pheromone response system Ste4 (A), Ste5-CTM (B), Ste11-4-Ste7 (C) and Ste12 (D) for 180 min. Cartoons show the proteins of the PRS signaling arm (most shown in Figure 1a) with the ectopic activator highlighted in red. We quantified η^2(P) from measurements of the two reporter signals in flow cytometry as described. y axis shows cell-to-cell variation in P, uncorrected for η^2(γ) (η^2(P)+η^2(γ)), and x axis
shows signal strength $P$, normalized by the maximum $P$ observed for each reference strain, for cells in three replicate cultures of each mutant and reference strain.
**Figure 6B. Microtubule perturbations affect transmitted signal P.** These are the x-axis values of Figure 6A, plotted here vs. pheromone dose. Reductions in these values are thus also reflected in ranges of P which are reduced relative to reference, for data from mutant strains in the plots of Figure 6A.
Figure 7. Fus3 is required for microtubule perturbations to increase signal variation. y axis in each panel shows $\eta^2(P)$ as a function of $P$. **Top left.** $\Delta$ fus3 $\Delta$ bim1, $\Delta$ bim1, $\Delta$ fus3, and reference strain (wt). **Top right.** $\Delta$ fus3 $\Delta$ gim4, $\Delta$ gim4, $\Delta$ fus3, and reference (wt). **Bottom left.** $\Delta$ kss1 $\Delta$ bim1, $\Delta$ bim1, $\Delta$ kss1, and reference (wt). **Bottom right.** $\Delta$ kss1 $\Delta$ gim4, $\Delta$ gim4, $\Delta$ kss1 and reference strain (wt). $\Delta$ bim1 and $\Delta$ gim4 strains show increased $\eta^2(P)$ relative to WT (p-values are both less than $10^{-5}$). However, $\Delta$ bim1 $\Delta$ kss1 and $\Delta$ gim4 $\Delta$ kss1 cells show higher $\eta^2(P)$ relative to WT (p-values are both less than $10^{-5}$). The double mutant $\Delta$ bim1 $\Delta$ kss1 had significantly higher $\eta^2(P)$ than either $\Delta$ kss1 or $\Delta$ bim1 alone (p-values are both $10^{-5}$ or less), while the double mutant $\Delta$ gim4 $\Delta$ kss1 had essentially the same $\eta^2(P)$ as either $\Delta$ kss1 or $\Delta$ gim4 alone (p-values are 0.341 and 0.106, respectively). This shows that Fus3 protein is required for increased $\eta^2(P)$. 
Figure 8. Microtubule perturbations cause Ste5 patches to form less reliably, delay patch formation, and cause patches to persist for less time. We stimulated reference ("WT"), Tub1-828-expressing, Δbim1 and Δgim4 derivatives of MW003 (bearing 3 copies of P_{STE5-STE5-3xYFP}, Ventura et al. 2014) with 1μM pheromone and imaged them over time for up to 3.5 hours.
A. Example of a cell with two co-existing Ste5 patches (top) and a cell with an interval without detectable Ste5 patches between the first and second patch (bottom), marking the dynamic features we quantified: time to 1st patch (polarization), duration of 1st and 2nd polarization, interval in which 1st and 2nd polarization overlap, or gap between them, and time from 1st to 2nd polarization. B. Bar graph plots show qualitative defects observed: cells with no polarization, cells with gaps between 1st and 2nd polarizations and cells with overlapping (coexisting) polarizations. Table shows quantitative defects. Data corresponds to the mean +/- SEM, the standard deviation +/- SE and the coefficient of variation (mean divided by the standard deviation) +/- SE. Values for the probability p of the observed data under the null hypothesis that each mutant strain is no different from WT are shown by asterisks: * = p<0.05; ** = p<0.01; *** = p<0.001.
Figure 9. Disrupting microtubule plus end function impairs mating partner choice.  

A. Schematic of discrimination assay, in which MATa cells choose between potential MATα mating partners producing normal levels of α-factor and potential Δmatalpha1 partners that expressed about 5% as much α-factor.  

B. We performed rapid mating discrimination assays as described in Methods for reference (GPY4078, Δade2, and also expressing PACT1-YFP, here called w.t), and for Δbim1, Δgim4, Δbim1 Δgim4, and Tub1-828-expressing GPY4078 derivatives. We allowed mating to proceed for 5 minutes and then halted it by transferring the cells to medium without nitrogen. Graph shows the discrimination efficiency for three biological replicates of each strain (circles) and the corresponding average (bars). For each strain, we calculated this value as (1-((Δmatalpha1/total) diploids / (Δmatalpha1/total) haploids)) expressed relative to the value for GPY4078. Loss of Bim1 protein and Tub1-828-expression increase variability in transmitted signal η²(P), and impair mating partner choice, while loss of Gim4 only increases variation in η²(P). In all cases, P is PPRM1-XFP/ PACT1-YFP.
Supplementary Information for

Cell-to-cell variability in the yeast pheromone response: Cytoplasmic microtubule function stabilizes signal generation and promotes accurate fate choice


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1. General methods

We performed DNA manipulations including PCR and subcloning as described (Ausubel et al., 1987-2016). We cultured and manipulated yeast as described (Ausubel et al., 1987-2016; Guthrie and Fink, 1991). Unless otherwise noted, we grew cells in synthetic dextrose complete (SDC) media consisting of Brent Supplemental Media (MP Biomedicals, Solon, OH), yeast nitrogen base without amino acids and ammonium sulfate (BD, Franklin Lakes, NJ), and dextrose (Sigma-Aldrich, St Louis, MO).

2. Yeast strains

2.1 Base strains

2.1.1 Construction of GPY1802, a strain derived from BY4741

We first generated GPY1802, a BY4741 derivative with markerless Δbar1 and cdc28-as2 loci. To do this we first deleted BAR1 in BY4741 using a PCR product containing the pRS406 URA3 gene flanked by 50 nt of homology the BAR1 promoter and terminator. We confirmed proper insertion was confirmed by PCR and a phenotypic test of BAR1 status. We named the resulting Δbar1::URA3 strain GPY8190.

We then deleted the URA3 marker by transforming GPY8190 with a 100-bp double stranded oligonucleotide composed of two “arms” of 50 nt of homology to the sequences flanking the URA3 marker. We selected for Δura3 transformants in 5-FOA plates and confirmed proper deletion by PCR. We named the resulting strain GPY1800 and annotated this locus in the strain table as Δbar1 (Table S4).
Next we introduced the \textit{cdc28-as2} allele. We used linearized pCDC28-as2-406 to “loop in” the allele, generating strain GPY1801, and then we “looped it out” as described earlier (Colman-Lerner et al., 2005). We confirmed proper recombination by PCR and confirmed it by testing for 1-NM-PP1 sensitivity. We named the resulting strain GPY1802 and annotated this marker in the strain table as \textit{cdc28-F88A} (Table S4).

\textit{Construction of GPY1804, as GPY1802 but without a constitutive reporter}

We used GPY1802 to generate the \textit{TUB1-828-expressing} strain and its cognate reference strain (see below). To do so, we added a \textit{P}_{\text{PRM1}}-\text{mCherry} reporter to GPY1802 by replacing the \textit{PRM1} ORF with the \text{mCherry} coding sequence followed by a terminator and a marker. We used an approach identical to the one above for \textit{P}_{\text{PRM1}}-\text{YFP} and \text{mRFP}, except that in this case we used an \text{mCherry-TADH1---G418 r} template described before (Yu et al., 2008). We confirmed integration by PCR and checked the presence of a pheromone-inducible \text{mCherry} reporter. We named the resulting strain GPY1804 and annotated this locus as \textit{PRM1pr-mCherry-\text{G418(MX6)}} in the strain table (Table S4).

\textit{Construction of GPY 4000-derived strains to validate and further analyze Δbim1 and Δgim4 phenotypes}

In other experiments, we had learned that \textit{P}_{\text{ACT1}} was mildly induced by pheromone. For GPY4000 and related strains, we therefore chose to use \textit{P}_{\text{BM180}}-\text{YFP} as a constitutive promoter to ensure that the changes in η²\text{(P)} observed in the deletion mutants did not arise from a change in variation in the pathway controlling the constitutive control reporter.

We introduced all gene deletions in the GPY4000 strain by a PCR approach. We first obtained strains carrying the gene deletion of interest marked with G418 resistance from the haploid deletion collection. We then changed the G418 resistance to either NAT resistance or hygromycin B resistance by transforming the deletion strain with a PCR product of the resistance cassettes and selecting for the marker carried in the PCR product. Since all three drug resistance markers contain the same 300-400 bp promoter and terminator, those flanking sequences directed a double homologous recombination gene replacement. Proper recombination was confirmed by the loss of the original G418 resistance. Subsequently, we amplified the gene deletion locus by PCR, including 300-500 bp of 5’ and 3’ gene-specific flanking sequences in the amplicon. We transformed this PCR product into GPY4000, selected for the appropriate drug resistance and confirmed proper gene deletion by PCR. The resulting strains are listed in Table S1.
Construction of SGA101, a clean background for testing additional genes that might affect microtubule function

SGA85 was is the haploid MATa reporter strain used in the companion paper (Pesce et al. 2016) as a reference in our screen to find otherwise isogenic deletion strains with alterations in variation in signal transmission. In this study, we used this strain to introduce different alleles possibly affecting microtubule function by loop in/loop out replacement with URA3-marked plasmids and for the three-color FP live cell time courses (see below). Starting with the reference strain SGA85, we derived a Δura3 strain by transforming SGA85 with a PCR product spanning the entire LYP1 locus from promoter to terminator, amplified from BY4741 genomic DNA. We selected for loss of the URA3 marker in 5-FOA plates and confirmed restoration of the LYP1 ORF by verifying the loss of YFP fluorescence from P_{ACT1}-YFP-T_{ADH1} and by diagnostic PCR. The resulting strain was a URA3 LYP1 derivative of SGA85. We named it SGA101.

2.2 Construction of strains with genetic alterations in KAR1, KAR3, and CIK1

kar1-Δ15 (SGA109).

We obtained plasmid pMR1593 as a gift from Mark Rose and used it as described (Vallen et al., 1992) to replace KAR1 for kar1-Δ15 in parent strain SGA101. Briefly, we linearized pMR1593 with Bgl II, transformed it into SGA101, selected for uracil prototrophy and in a second step selected for loss of the URA3 marker in 5-FOA plates. We screened the resulting colonies by PCR to identify a kar1-Δ15 strain, which was named SGA107. For this strain and the kar3-1 (SGA108) strains and the Δkar3 (GPY4003) strain, the reference strain is SGA103.

We then transformed SGA107 with pTC-PBMH2-YFP-TADH1-URA3 linearized with StuI as above. We identified transformants with a single PBMH2-YFP copy using fluorescence microscopy. The resulting strain was named SGA109.

kar3-1 (SGA108)

We obtained the plasmid pMR1510 from Mark Rose and used it as described to replace KAR3 with kar3-1. Briefly, we linearized pMR1510 with MluI, transformed it into SGA101, selected for uracil prototrophy and in a second step selected for loss of the URA3 marker in 5-FOA plates. We screened the resulting colonies by PCR to identify a kar3-1 strain, which was named SGA106. As above, we transformed SGA107 with linearized pTC-PBMH2-YFP-TADH1-URA3 and identified transformants with a single PBMH2-YFP copy using fluorescence microscopy. The resulting strain was named SGA108.

Δkar3 (GPY4003)

To make strains with a deletion in the KAR3 coding sequence, we used primers GP800-801 to amplify the hygromycin B resistance cassette hph from pAG32. This PCR was transformed
into GPY4000, which was then plated on non-selective media and replica plated to media containing hygromycin B. Transformants were confirmed to be knockouts of KAR3 using primers GP1397-1044, and the resulting strain was named GPY4003.

Δcik1 (GPY4123)

To make strains with a deletion in the CIK1 coding sequence, primers GP1361-1362 were used on KAN MX4 to generate a PCR product that had the TEFpr-G418-TEFter cassette with homologous tails directly flanking the 5’ and 3’ of the CIK1 ORF. GPY4104 was then transformed with the generated PCR product, plated on non-selective media, and replica plated to media containing geneticin. Transformants were confirmed to be knockouts of CIK1 using primers GP1397-1062, the resulting strain was named GPY4123. The reference strain for this Cik1 strain is GPY4000 4741 MATa Δbar1::Δmarker cdc28-F88A Δprm1::PRM1pr-mCherry--G418(MX6) BMH2::BMH2pr-YFP--MET15

2.3 Construction of strains with nuclear label and gene expression reporters for nuclear movement experiments

HTB2-YFP strains

We based this set of strains was based on SGA85, the reference strain for the modified haploid gene-deletion collection used in our screen for cell to cell variability mutants. To make it, we modified SGA85 by removing the PPRM1-CFP-TADH1 and PACT1-YFP reporters and introducing PACT1-CFP reporter and a YFP label to allow visualization of the nucleus.

In SGA85, the PACT1-YFP reporter had been inserted in the Δlyp1 locus replacing the LYP1 ORF, as part of an inserted plasmid with a URA3 marker. We removed the entire plasmid insertion by transforming SGA85 with a PCR product of the WT LYP1 locus that included 300-500 bp of promoter and terminator sequences. We selected for ura3 mutants in 5-FOA plates and identified the colonies with a restored LYP1 locus by their loss of YFP fluorescence, acquired thialysine sensitivity and by PCR. This LYP1 variant of SGA85 was named SGA101.

In SGA85, the PPRM1-CFP reporter had been inserted in the Δbar1 locus replacing the BAR1 ORF, as part of an inserted plasmid with a HIS3 marker. We removed the entire plasmid insertion by transforming SGA85 with a PCR product of a Δbar1::URA3 locus that included 300 bp of promoter sequences and 700 bp of terminator sequences. We used strain GPY8190 as template for the Δbar1::URA3 PCR. We selected for uracil prototrophs and confirmed appropriate gene replacement by the loss of the pheromone inducible CFP reporter, acquired histidine auxotrophy and by PCR. We named the resulting strain SGA114.

We then introduced a nuclear-localized fluorescent label by fusing the HTB2 ORF to YFP. We used a PCR product containing the YFP- TADH1-KAN(MX4) cassette with ends with homology to sequences upstream and downstream of the HTB2 ORF, that was generated with the YFP-
KAN(MX4) from the Pringle collection (Longtine et al. 1998). We confirmed proper insertion by the appearance of a bright yellow fluorescence label in the nucleus and by PCR. We named the resulting strain SGA118.

We recovered the URA3 marker by transforming SGA118 with a 200 bp double stranded oligonucleotide composed of two 100 bp sequences with homology to the ends of the URA3 marker in the Δbar1::URA3 locus. We plated the transformation in 5-FOA and checked proper deletion of URA3 by PCR. We named the resulting strain SGA123.

We next deleted BIM1 from SGA123. We followed the same protocol described above for deleting BIM1, except that we used HIS3(MX4) as the selective marker. The resulting Δbim1 strain was named SGA125.

SEC8-RFP SPC42-GFP strains

This set of strains was derived from a clonal isolate from the yeast GFP collection (Huh et al., 2003). The members of this collection were derived from a BY4741 parental strain. The clone we used carried a modified allele of $SPC42$ expressing a Spc42 with a C-terminal GFP tag and linked to a $HIS3$ marker (this allele is denoted here as $SPC42$-GFP—$HIS3$).

To make the reference strain for this set, we first deleted the $BAR1$ gene in $SPC42$-GFP—$HIS3$ using the approach we described above for the generation of GPY8190.

This resulted in strain GPY1752: $SPC42$-GFP—$HIS3$ Δbar1::Δmarker.

In a second step, we modified the $SEC8$ gene to express Sec8 with a C-terminal mCherry tag. We used an approach identical to the one above for $PPR1$-YFP and mRFP, except that in this case we added the tag at the end of the gene instead of replacing the gene with it, and used the mCherry-T$_{ADH1}$---G418 r template described before.

This resulted in strain $SPC42$-GFP—$HIS3$ SEC8-mCherry—KanMX6 Δbar1::Δmarker, named GPY1751.

In a final step to construct the base strain for this series, we replaced the $CDC28$ gene by the analog-sensitive $cdc28$-F88A allele. We used linearized pCDC28-as2-406 to “loop in” the allele, and then we “looped it out”, as described earlier (Colman-Lerner et al., 2005). We confirmed proper recombination by PCR and confirmed it by testing for 1-NM-PP1 sensitivity.

This resulted in strain $SPC42$-GFP—$HIS3$ SEC8-mCherry—KanMX6 Δbar1::Δmarker $cdc28$-F88A, named GPY1752. GPY1752 was the base strain for this set.
Starting with GPY1752, we generated GPY1709 (Δbim1--NatMX6). We used GPY1752 and GPY1709 to measure the effect that deleting BIM1 had on nuclear positioning relative to the site of polarized growth (Figure 3).

To measure the effect that deleting GIM4 had on nuclear positioning we used otherwise-isogenic strains that carried GFP-tagged alpha tubulin, in addition to Spc42-GFP and Sec8-mCherry. We to make these, we transformed GPY1752 with plasmid pAFS125C, a construct from Aaron Straight carrying the TUB1 gene, driven by its own promoter and fused in-frame with a gene coding for GFP (Straight et al., 1998). pAFS125C is an integrative plasmid (has no yeast origin of replication) and is marked with the URA3 gene. Before transformation we linearized pAFS125C (a gift of by Julia Kardon, a postdoc in Tania Baker’s lab at MIT), cutting the TUB1 promoter with the Eag I restriction enzyme. This cut site created a strong preference for insertion of the plasmid at the TUB1 promoter in the genome. The resulting TUB1 locus carried two tandem copies of the TUB1 gene. The S’ copy was driven by the endogenous TUB1 promoter and fused with the GFP gene. The 3’ copy was driven by the plasmid-borne TUB1 promoter and is not tagged. We noted this modified TUB1 locus as TUB1::PTUB1-GFP-TUB1---URA3.

We named the resulting strain GPY1756 (a derivative of GPY1752 carrying TUB1::PTUB1-GFP-TUB1---URA3). GPY1756 and GPY152 showed no difference in nuclear positioning (data not shown). Starting with GPY1756, we generated GPY1759 (Δgim4--NatMX6). We used GPY1759 to measure the effect that deleting GIM4 had on nuclear positioning relative to the site of polarized growth (Figure 3).

2.4 Construction of strains expressing human estrogen receptor chimeras

Vectors for homologous recombination with excisable CEN/ARS cassettes

For some cloning steps below we used the pTC41x series of derivatives of the pRS41x shuttle vectors (Gordon et al., 2007). Each pTC41x vector was made by cloning a CEN/ARS containing-fragment flanked by AatII overhangs into the AatII site of each pRS40x vector. As a result all pTC41x vectors can be converted to pRS40x versions (“integrative” vectors that lack a yeast origin of replication) by cutting with AatII and religating.

Plasmid carrying estrogen receptor chimera driven by the ADH1 promoter

Our source of the GAL4 DNA binding domain – human estrogen receptor – VP16 transactivation domain (GEV) chimera was plasmid pp1557, a gift of Peter Pryciak (Takahashi and Pryciak, 2008). We first subcloned a PvuI fragment of pp1557 containing P_{ADH1}–GEV–T_{ADH1} into the Smal site of pTC415. To do this we co-transformed PvuI-cut pp1557 and Smal-cut pTC415 in yeast strain BY4741. We isolated gap-repaired plasmids from leucine prototrophs using a Zymoprep Yeast Plasmid Miniprep I kit. The resulting plasmids were then transformed into Z-competent E.coli to amplify the plasmid, 8 colonies were grown overnight in LB-Amp.
media and miniprepped using Qiagen QIAprep Spin Miniprep Kit, and the plasmid sequences were confirmed by DNA sequencing. This cloning resulted in pSZ100.

We subsequently removed the CEN/ARS in pSZ100 by the AatII process described above, yielding pSZ101. pSZ101 elements are $P_{ADH1}$-GEV-$T_{ADH1}$-LEU2.

**Plasmid carrying estrogen receptor chimera driven by the BMH2 promoter**

In a separate line of research we had found that the $ADH1$ promoter showed unusually high cell-to-cell variability. For this reason, in parallel we constructed an alternative GEV expression vector driven by the $BMH2$ promoter. We amplified the GEV coding sequence by PCR from pp1557, using primers that added to the amplicon ends with homologies to the 3’ end of the $BMH2$ promoter (in the 5’ end of the amplicon) and to the pTC7 backbone (in the 3’ end of the amplicon, pTC7 is the plasmid from which pTC-P$B_{MHH2}$-YFP-URA3 is derived (Colman-Lerner et al., 2005)). We cut pTC-P$B_{MHH2}$-YFP-$T_{ADH1}$-URA3 with EcoRI (partial digest) and XhoI to remove the YFP sequence. We co-transformed this digested plasmid with the GEV PCR product into yeast strain TCY3277, which carried a $PGAL1$-GFP-$T_{ADH1}$-HIS3 reporter. We transferred to *E. coli*, mapped and sequenced plasmids that showed estradiol induction of GFP.

We named the resulting pTC-P$B_{MHH2}$-GEV-$T_{ADH1}$-URA3 construct pSZ110.

Subsequently, we moved the P$B_{MHH2}$-GEV-$T_{ADH1}$ cassette to LEU2 vector pRS305. We cut pSZ110 and pRS305 with BglII and ligated both DNA’s by standard cloning procedures. Recombinant plasmids were screened for those derived from a pRS305 backbone and containing the P$B_{MHH2}$-GEV-$T_{ADH1}$ cassette. The resulting plasmid was named pSZ111.

**Strains carrying single copies of P$B_{MHH2}$-GEV or P$ADH1$-GEV**

Both P$B_{MHH2}$-GEV or P$ADH1$-GEV LEU2 plasmids are designed to be integrated by single recombination in the LEU2 locus, such that one or more copies could be integrated at the LEU2 locus. It was essential for our purposes to ensure that the strains we used had just one copy of either construct.

To obtain strains with single copies of the GEV constructs, we first obtained a set of clones with unknown number of copies for each construct. To determine the number of GEV construct copies integrated in the clones we introduced pp1744 (a gift from Peter Pryciak containing $P_{GAL1}$-GFP-$T_{ADH1}$-His5S. pombe), linearized at the HIS3 locus with Nhe1, into each of them and screened the $P_{GAL1}$-GFP transformants to identify those with just one copy of this GFP reporter. Finally, we stimulated the GEV clones with a gradient of estradiol doses and obtained a GFP vs estradiol dose response. We use the dose responses to identify the clones with just one copy of the GEV constructs. For subsequent applications of these strains, we used the parents of
these clones, because they did not carry the P_{GAL1}-GFP construct. The steps we followed are described below.

We generated 8 clones carrying P_{BMH2}-GEV by transforming pSZ111 linearized with XcmI at the LEU2 locus into GPY1804. 8 leucine prototrophs were saved and named GPY1806 (a-h). Similarly, we obtained 12 clones carrying P_{ADH1}-GEV by linearizing pSZ101 with a PacI cut within P_{ADH1} and transforming GPY1804. 8 leucine prototrophs were saved and named GPY1805(a-h). We then transformed all 16 of GPY1806(a-h) and GPY1805(a-h) with pp1744 linearized with Nhe1.

We determined how many copies of pp1744 were integrated in 2 isolates of each of the 16 transformations by measuring GFP levels after incubating cells for 3 hours in 2% galactose. We selected 1 clone with one copy of pp1744 for each of the 8 clones each of GPY1806 and GPY1805 we had isolated earlier and named them GPY1808 (a-h) and GPY1807 (a-h) respectively. Finally, we did estradiol dose–response curves in all 16 GEV clones carrying P_{GAL1}-GFP. We grew GPY1808 (a-h) and GPY1807 (a-h) in glucose media overnight in exponential phase and stimulated these cells at low density with a gradient of estradiol concentrations (1 to 50 nM range) for 3 hours. After 3 hours we added 200µg/ml cycloheximde, incubated cells 5-9 hours at room temperature and measured GFP levels by flow cytometry. In each group of 8 clones, a majority of 5 to 7 clones showed identical dose responses. The remainder showed higher maximal induction and lower EC50. We judged that the dose responses shown by the majority of the clones corresponded to the single-copy integrants. From this point forward the names GPY1805, GPY1806, GPY1807 and GPY1808 (without the lower case letters sub-ID) were used to designate a single copy GEV integrant of each set.

The GEV locus driven by the BMH2 promoter is annotated as BMH2::BMH2pr-GAL4BD-hER-VP16--LEU2 in the strain table (Table S1).

Comparison of variability of activation dependent on P_{BMH2}-GEV or P_{ADH1}-GEV constructs

We first integrated a housekeeping fluorescent protein reporter in GPY1805 and GPY1806 by integrating pTC-P_{BMH2}-YFP-T_{ADH1}—URA3 linearized with Stul within P_{BMH2}. We identified strain with single-copy integrations and named them GPY1809 (P_{ADH1}) and GPY1810 (P_{BMH2}). Then we performed estradiol dose responses as above and analyzed the results as described earlier (Colman-Lerner et al., 2005). From this analysis we found that the level of cell-to-cell variation in GEV activator function (amount and activity) in GPY1809 (P_{ADH1}) was higher than in GPY1810 (P_{BMH2}).

Based on these studies we decided to use GPY1810 (P_{BMH2}) for subsequent constructions. At this point we decided to free the URA3 marker to allow the introduction of the TUB1-828 construct (see below). We thus replaced the pTC-P_{BMH2}-YFP-T_{ADH1}—URA3 integrant
with a pTC-\(P_{\text{BMH}2}\)-YFP-\(T_{\text{ADH}1}\)–MET15 integrant by loop out using 5-FOA selection followed by transformation with the MET15 plasmid linearized by cutting within \(P_{\text{BMH}2}\). We screened the transformants by fluorescence microscopy to identify single-copy \(P_{\text{BMH}2}\)-YFP integrants. We called the resulting strain GPY1858. The locus is annotated as \(BMH2::BMH2pr-YFP--MET15\) in the strain table.

### 2.5 Construction of an estradiol inducible TUB1-828-expressing strain (GPY1873)

We used an inducible \(TUB1-828\) construct that we received from Kirk Anders (Anders and Botstein, 2001). This plasmid, pRB2949, is a CEN/ARS URA3 yeast episome carrying a \(P_{\text{GAL}1}--TUB1-828\) cassette. Expression of \(TUB1-828\) from this construct is induced by galactose and repressed by glucose.

In our experimental system, incubation in media without glucose with galactose alters many aspects of system behavior, including a substantial increase in pathway variation (data not shown). We therefore induced \(TUB1-828\) expression using the estradiol responsive Gal4-ER-VP16 chimeric transcription factor (described above, Louvion et al., 1993).

We transformed GPY1858 with plasmid pRB2949 (Anders and Botstein, 2001). We tested several colonies for growth in the presence of estradiol. All of them failed to grow, the expected consequence of the induction of \(TUB1-828\). We selected one clone for \(TUB1-828\) expression experiments and named it GPY1873.

After constructing GPY1873 and testing its effect on the PRS response to pheromone we found that basal \(TUB1-828\) expression conferred by the estrogen-responsive chimeric transcription factor was enough to give the maximum response observed, shown in Figure 7B.

### 2.6 Construction of strains expressing ectopic PRS activating proteins for bypass experiments

If strains that contain artificial activator plasmids are grown on media that is depleted of glucose, the artificial activator induces the pheromone pathway and stops growth. For that reason, when using antibiotic selection to knock out genes, we first re-suspended these strains in 15ml of SDC medium for 6 hours, spun down, re-suspended in 100\(\mu\)l, and plated directly onto antibiotic. This transformation protocol ensured that the cell cycle was not inhibited by expression of the ectopic activators prior to antibiotic selection.

In order to screen for single copy integration of activator plasmids, we used frozen stocks of 6 isolates to inoculate cultures in selective SDC media. These cultures were allowed to grow for 6-8 hours and were then diluted to grow in log phase overnight. The following morning the 6 isolates were induced cultures that contained serial dilutions of \(\beta\)-Estradiol in SDC with .04mg/ml casein and 10\(\mu\)M 1-NM-PP1. These cultures were then fixed in 200\(\mu\)g/ml
cycloheximde and taken to the flow cytometer for fluorescence measurements. Out of 6 isolates tested, the 4-5 that typically had the same dynamic range and maximum induction were scored as single integrations and given strain numbers.

**STE4 activator strains**

GPY1810 was transformed with pp1610 linearized with BsmI to target the plasmid to the HIS3 locus and plated onto histidine deficient media. 6 isolates were then streaked to single colonies, patched, and immediately frozen to prevent unwanted activation of the pheromone pathway. One of the isolates that was determined to have 1 copy of GAL1pr-STE4 was named GPY1816 and used as base strain in this set. We noted this locus his3-Δ1::GAL1pr-STE4--HIS3. This strain was then transformed with the PCR product generated from primers GP1046 and GP1047, mentioned above, to knock out BIM1. 8 isolates were then screened for successful BIM1 removal using primers GP1246 and GP1397, the positive isolate was named GPY1818. Later, upon deciding to incorporate TUB1-828 into our studies, we needed to free up URA3 from these strains. To do so, we plated, GPY1816 and GPY1818 onto 5-FOA and collected singles, 4 of which were screened to verify the successful loop-out of the BMH2pr-YFP::URA3 plasmid. The resulting strains were named GPY1828 (STE4) and GPY1830 (STE4Δbim1) and transformed with a plasmid containing BMH2pr-YFP::MET15 linearized at the BMH2 promoter with Stu1. 6 transformants of each were streaked to singles and single copy integrations were determined by microscopy, the resulting strains were named GPY1855 and GPY1862. GPY1855 was then transformed with the PCR product generated using primers GP1153 and GP1155, mentioned above, to knock out GIM4, transformants were then PCR verified for the knock out using primers GP1175 and GP1397. GPY1855 was also transformed with a TUB1-828 CEN/ARS plasmid pRB2948, received from Kirk Anders (Anders and Botstein, 2001), and plated directly onto URA3 selective plates. Positive transformants were identified by cell cycle arrest in response to 50nM β-Estradiol and named GPY1879.

**STE5-CTM Δste5 strains**

GPY1810 was transformed with pp1611 linearized with BssH1 to target the plasmid to the HIS3 locus and plated on histidine deficient media. 6 isolates were then streaked to singles, patched, and immediately frozen to prevent unwanted activation of the pheromone pathway. The isolate that was determined to have 1 copy was named GPY1817. This strain was then transformed with the PCR product generated from primers GP1046 and GP1047, mentioned above, to knock out BIM1. 8 isolates were then screened for successful BIM1 removal using GP1246 and GP1397, the positive isolate was named GPY1820. The same protocol was followed as for STE4 to free up the URA3 marker for the incorporation of TUB1-828 into GPY1817 and GPY1820. The resulting strains that contained BMH2pr-YFP::MET15 instead of BMH2pr-YFP::URA3 were named GPY1856 (STE5-CTM) and GPY1864 (STE5-CTM Δbim1). GPY1856 and GPY1864 were then transformed with PCR DNA with tails homologous to the STE5 promoter and terminator generated using primers GP1098 and GP1099 on the NAT MX4 plasmid to knock out
From the genome. Transformations were grown for 6 hrs in SDC and plated directly to proper selection plates. Transformants were streaked out on selective plates to singles and PCR verified for the deletions using GP1101 and GP1397, positive isolates were named GPY1915 (STE5-CTM ∆ste5) and GPY1916 (STE5-CTM ∆bim1 ∆ste5). GPY1915 was then used to incorporate the ∆gim4 and TUB1-828 mutations as described for the STE4 activator to generate GPY1997 and GPY1986 respectively.

**STE11-4-STE7 ∆ste5 strains**

GPY1806 was first transformed with a ds PCR product that had tails homologous to the STE5 promoter and terminator, generated using primers GP1098 and GP1099 on the NAT MX4 plasmid. We used this PCR product to knock out STE5 from the genome. The transformation was first plated on leucine deficient plates, allowed to grow to a lawn overnight, and then replicated to leucine deficient plates with containing NAT. Transformants were streaked out on selective plates to singles and PCR verified for the deletions using primers GP1101 and GP1397. We named one positive isolate GPY1861. GPY1861 was then transformed with BMH2p-YFP::MET15 and single copy isolates were identified as described for the STE4 activator to generate GPY1874. GPY1874 was then transformed with pp1609 linearized Bsm1 (partial digest) to target the plasmid to the HIS3 locus. Single copy transformants were isolated as described above to generate GPY1890. The BIM1 and GIM4 gene knockouts and TUB1-828-expressing cassette were then incorporated into GPY1890, as described above, to generate GPY1932 (∆bim1) GPY1996 (∆gim4) and GPY1935 (TUB1-828).

**STE12 ∆ste5 strains**

To generate these we first needed to construct a plasmid that carried DNA _P_GAL1_ reading STE12 (GAL1pr-STE12). To do this, we linearized pp1611 with NotI, co-transformed 5ng of the digested plasmid with 20ng of a PCR product that contained the CEN/ARS sequence into BY4741, and plated the transformations on plates deficient in histidine. We prepped 8 isolates using the Zymoprep Yeast Plasmid Miniprep I kit, then transformed into Z-competent _E.coli_ to amplify the plasmid, grew single colonies overnight in LB-Amp media and mini-prepped using Qiagen QIAprep Spin Miniprep Kit. Purified plasmids were digested with ApaI to confirm that the CEN/ARS sequence was inserted. We named one such plasmid pSZ99. pSZ99 was then cut with a double digest of ApaI and NcoI to remove the STE5-CTM sequence. Next, 5ng of digested pSZ99 and 20ng of STE12 PCR product (generated using primers GP1110 and GP1111, on BY4741) were co-transformed into BY4741, and transformation mixes plated on histidine deficient media. We isolated DNA from 8 isolates using a Zymoprep Yeast Plasmid Miniprep I kit, then transformed the mix into Z-competent _E.coli_ , grew His+ Amp’ colonies overnight in LB-Amp media and mini-prepped using Qiagen QIAprep Spin Miniprep Kit. The purified plasmids were then cut with XbaI to verify loss of STE5-CTM and insertion of STE12, positive isolates were named pSZ98. pSZ98 was then cut with AatII to remove the CEN/ARS, ligated with Rapid T4 DNA Ligase Kit from Roche Diagnostics, transformed into Z-competent _E.coli_, and plated on LB-Amp
media. 8 colonies were then grown overnight in LB-Amp media and miniprepped using Qiagen QIAprep Spin Miniprep Kit. Purified plasmids were confirmed for CEN/ARS removal by ApaLI digestion, the resulting plasmid was named pSZ97.

GPY1874 was then transformed with pSZ97 linearized with Nsil to target the plasmid to the HIS3 locus. Single copy transformants were isolated as described above to generate GPY1958. The BIM1 and GIM4 gene knockouts and TUB1-828 were then incorporated into GPY1890, as described above, to generate GPY1976 (∆bim1), GPY1998 (∆gim4) and GPY1978 (∆TUB1-828).

2.7 Construction of strains to quantify Ste5 membrane localization

YPP3662 (Ventura et al.), which carries instead of Ste5 three copies of a Ste5-YFP-YFP-YFP fusion gene, was the parental strain for these experiments. From it, we generated ∆bim1, ∆gim4, and tub1-828-expressing derivatives. We generated GPY4112 (∆bim1) and GPY4113 (∆gim4), via the same Pringle cassette approach using the URA3(MX4 plasmid) we used to make the GPY4000 series strains. We generated the tub1-828-expressing YGP3858 by the same steps we used to generate the strains used in the bypass experiments: transformation by linearized pSZ111 followed by isolation a PBHM2-Gal4-hER-VP16 construct integrated at BMH2. We introduced into 8 transformed strains those strains a PGal1-mCherry construct, and picked one strain from the majority of strains that showed low expression consistent with single copy insertion of the PBHM2-Gal4-hER-VP16. We called this strain ACL-GP-001. We then introduced into it pRB2949 (Anders and Botstein, 2001) which carries a PGAL1-TUB1-828 construct, to create ACL-GP-003.

3. Pheromone dose-response experiments

For follow up studies on the gene deletions of interest and/or all other perturbation experiments, we adapted the high throughput protocol flow cytometry we used for the screen. The only modification was in how we cultured the cells. Instead of culturing them in deep-well 96-well plates, we used the test tube protocol described above for the fluorescence microscopy secondary screen. We did the pheromone stimulation step exactly as in the assays we used in the screen, in shallow-well 96-well plates, with the only difference being the addition of pheromone, which in this case was done using a pipette from a serial dilution of pheromone stocks instead of the slotted-pin tool we used for the screen. All dose response experiments were measured by flow cytometry as described above.

4. Chemical disruption of microtubule polymerization

We used media with high concentrations of nocodazole (10 µg/ml) and benomyl (30 µg/ml), two chemically distinct but functionally equivalent inhibitors of microtubule
polymerization. To prepare the media with these drugs we first heated to 100 °C media containing all ingredients for SDC except glucose and buffered with low-strength PBS (0.15 times the standard concentration). We then added 30 µg/ml benomyl from a 10 mg/ml stock in DMSO made daily. We added the same volume of DMSO to a control medium. We then allowed both media to cool to 50 °C, at which point we added 20 g/L glucose and 40 µg/ml casein. Finally we added 10 µg/ml nocodazole from a 10 mg/ml DMSO stock stored in small aliquots at -20 °C. We added the same volume of DMSO to the control media. When indicated, 1-NMPP1 was added to both media to a final concentration of 10 µM.

We tested every batch of nocodazole/benomyl media for its effectiveness at inducing cell cycle arrest in a reference strain. To do so we grew a culture of BY4741 to log phase, spun the cells and resuspended the pellet in the nocodazole/benomyl media. After a 3 hour incubation we counted the number of cells arrested in metaphase, judged by their large budded appearance. The media was considered effective if the fraction of arrested cells was equal or larger than 0.95.

5. Consideration of morphology of Δbim1 and Δgim4 strains

As we initiated close study in this work of increases in transmitted signal caused by Δbim1 and Δgim4 deletions, but before we had carried out the other genetic and chemical perturbation experiments that pointed toward effects on membrane localized, Fus3-dependent signaling, we wished to get a sense of whether the effects of these mutations were on processes at least somewhat specific to signal generation, rather than more general effects due for example to overall disorganization of cell cytoskeletal organization. To this end, we verified by light microscopic observation (not shown) that, compared with reference cells, cells with these lesions showed no great morphological differences during normal growth or after treatment with stimulating pheromone concentrations. Later in this study, we performed, the experiments in Figure 8 to quantify subtle differences in Ste5 signaling patch formation and shmoo formation in Δbim1 and Δgim4 cells. In performing those, we again verified by eye that those strains showed no other morphological differences that the ones quantified. Finally, at the suggestion of a reviewer, we subsequently confirmed from published work (Ohya et al., 2005, http://yeast.gi.k.u-tokyo.ac.jp) that Δbim1 and Δgim4 cells from the original deletion collection did not show morphological differences from the reference B4741 strain.

References


Supplementary Table S1 legend.

Strains used in this work.