

Bounds to Parapatric Speciation: A Dobzhansky-Muller incompatibility model involving autosomes, X chromosomes and mitochondria

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Abstract

1
2 We investigate the conditions for the origin and maintenance of postzygotic
3 isolation barriers, so called (Bateson-)Dobzhansky-Muller incompatibilities or
4 DMIs, among populations that are connected by gene flow. Specifically, we
5 compare the relative stability of pairwise DMIs among autosomes, X chromosomes,
6 and mitochondrial genes. In an analytical approach based on a continent-island
7 framework, we determine how the maximum permissible migration rates depend
8 on the genomic architecture of the DMI, on sex bias in migration rates, and on
9 sex-dependence of allelic and epistatic effects, such as dosage compensation.
10 Our results show that X-linkage of DMIs can enlarge the migration bounds
11 relative to autosomal DMIs or autosome-mitochondrial DMIs, in particular in
12 the presence of dosage compensation. The effect is further strengthened with
13 male-biased migration. This mechanism might contribute to a higher density
14 of DMIs on the X chromosome (large X-effect) that has been observed in
15 several species clades. Furthermore, our results agree with empirical findings
16 of higher introgression rates of autosomal compared to X-linked loci.

17 **1 Introduction**

18 Historically, speciation research has mostly focused on two idealized scenarios: allopatric
19 speciation (complete geographic isolation of incipient species) and sympatric speciation
20 (divergence of subpopulations in a common habitat) (Orr and Turelli, 2001; Coyne
21 and Orr, 2004; Via and West, 2008). Both scenarios are simplifications of biological
22 reality. While strict sympatry of incipient species seems to be an exception, there is
23 abundant evidence for hybridization even among “good species” with viable and not
24 completely sterile hybrid offspring (reviewed *e.g.* in Coyne and Orr, 2004; Mallet,
25 2008). Population genetic theory shows that even low levels of gene flow can strongly
26 interfere with population differentiation (Felsenstein, 1981; Slatkin, 1987). This
27 makes it inevitable to assess the impact of limited gene flow at various stages of the
28 speciation process, a scenario commonly referred to as parapatric speciation.

29 The classical model for the evolution of postzygotic isolation barriers in allopatry
30 is the (Bateson-)Dobzhansky-Muller model (DMM) (Bateson, 1909; Dobzhansky,
31 1936; Muller, 1942). The DMM assumes that new substitutions occur on different
32 genetic backgrounds. When brought into secondary contact, these previously untested
33 alleles might be mutually incompatible and form Dobzhansky-Muller incompatibilities
34 (DMIs), thus reducing hybrid fitness and decreasing gene flow at linked sites. The
35 emergence of species boundaries due to accumulation of DMIs in allopatry is well
36 understood (Coyne and Orr, 1989; Orr and Turelli, 2001; Coyne and Orr, 2004).
37 More recently, several studies have considered this process in parapatry (Gavrilets,
38 1997; Feder and Nosil, 2009; Agrawal et al., 2011; Bank et al., 2012; Wang, 2013;
39 Lindtke and Buerkle, 2015). All support that the DMM provides a viable mechanism
40 for the evolution of postzygotic isolation even in the presence of gene flow, although
41 the bounds for maximum permissible migration rates can be quite stringent.

42 Empirically, there is widespread evidence for DMIs not only among recently
43 diverged sister species (Maheshwari and Barbash, 2011; Presgraves, 2010; Sweigart

44 and Flagel, 2014), but also segregating within species (Corbett-Detig et al., 2013).
45 Hence, these authors argue that the genetic basis of reproductive isolation is continuously
46 present within natural populations, rendering the independent allopatric evolution
47 of newly incompatible substitutions obsolete.

48 While most theoretical studies focus on autosomal DMIs, empirical evidence
49 points to a major role of sex chromosomes in speciation. Haldane's rule (Haldane,
50 1922, reviewed in Coyne and Orr, 2004), states that in species with sex specific
51 reduced hybrid fitness the affected sex is generally heterogametic. The *large X-effect*
52 (Coyne and Orr, 1989, reviewed in Presgraves, 2008) expresses the disproportional
53 density of X-linked incompatibility genes in postzygotic isolation. For example
54 Masly and Presgraves (2007) report a higher density of incompatibilities causing
55 hybrid male sterility on the X chromosome relative to autosomes in *Drosophila*.
56 Equivalent findings exist of a *large Z-effect* in WZ-systems, such as birds, where
57 WZ-females are heterogametic (Ellegren, 2009). Also cytoplasmic incompatibilities
58 have been described (Ellison and Burton, 2008; Lee et al., 2008; Burton and Barreto,
59 2012; Barnard-Kubow et al., 2016).

60 A recent study by Bank et al. (2012) determined stability conditions and maximum
61 permissible migration rates of autosomal two-locus DMIs in a continent-island framework.
62 They distinguished two main mechanisms shaping the evolution of DMIs: selection
63 against (maladapted) immigrants and selection against (unfit) hybrids, which lead
64 to different dependence of maximum migration rates on the model parameters.

65 Prompted by the empirical observations described above, we extend the model by
66 Bank et al. (2012) to general two-locus DMIs in diploids involving X chromosomes,
67 autosomes, or mitochondria. We include sex-specific fitness effects, in particular,
68 to account for the effect of dosage compensation of hemizygous X-linked genes in
69 males. We also allow for sex-specific migration, as many species display differences
70 in migration patterns for males and females Greenwood (1980).

71 Following Bank et al. (2012) we derive maximum migration bounds where DMIs

72 can still originate in parapatry, or resist continental gene flow. In contrast to
73 the autosomal case, we find that sex specific fitness- and sex-biased migration
74 cause substantial differences in the maximum permissible rates and hence influence
75 the prevalence of autosomal DMIs relative to X-linked and mitochondrial DMIs.
76 Especially, we find that X-linkage of (nuclear or cytonuclear) DMIs together with
77 dosage compensation and/or male-biased migration boosts migration bounds and
78 thus enhances the evolution of X-linked DMIs, possibly contributing to a *large*
79 *X-effect* and to reduced introgression probabilities of X-linked DMI loci.

80 2 Model and Methods

81 We consider a diploid, dioecious population with separate sexes (at 1:1 ratio) that
82 is divided into two panmictic subpopulations, continent and island. (See Figure 1
83 and Figure B.1 in the Supporting Information (SI)). Both demes are sufficiently
84 large that drift can be ignored (drift effects are discussed in SI Section A.3). They
85 are connected by unidirectional sex-dependent migration at rate $m^{\text{♀}}$ and $m^{\text{♂}}$ from
86 the continent to the island. We fix the average migration rate per individual, $m =$
87 $\frac{m^{\text{♀}} + m^{\text{♂}}}{2}$, and define

$$R := \frac{m^{\text{♀}} - m^{\text{♂}}}{m^{\text{♀}} + m^{\text{♂}}} \in [-1, 1] \quad (1)$$

88 as a measure of sex-bias in migration. Sex-specific migration gives rise to distinct
89 migration rates per allele for autosomes, X chromosomes, and mitochondria, $m_{\mathcal{A}}$,
90 $m_{\mathcal{X}}$, and $m_{\mathcal{O}}$ (Eqs. (B.13)-(B.15)). For $-1 \leq R < 0$ migration is male-biased and
91 we obtain $m_{\mathcal{A}} > m_{\mathcal{X}} > m_{\mathcal{O}}$. In contrast, for $0 < R \leq 1$ migration is female-biased,
92 resulting in $m_{\mathcal{A}} < m_{\mathcal{X}} < m_{\mathcal{O}}$.

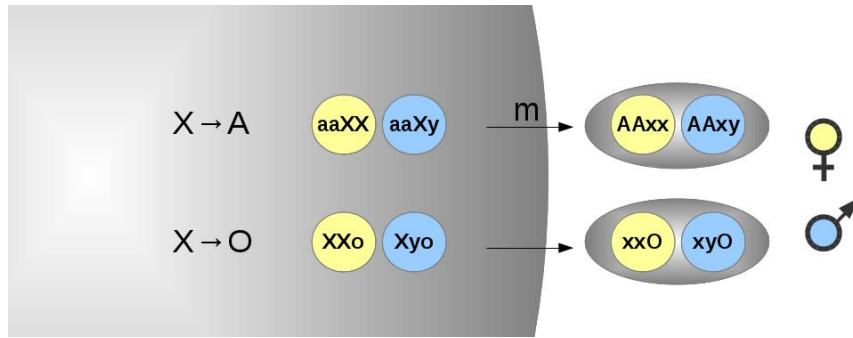


Figure 1: **Schematic model.** The population inhabits a continent (left) and an island (right), which are connected by unidirectional migration at rate m . The figure shows two out of eight genomic architectures investigated: an X-autosome DMI (upper line) and a cytoplasmic DMI between X and mitochondrion (lower line). Genotypes of female residents are depicted by yellow circles and males by blue circles, respectively. The capital letters denote incompatible alleles, which reduce hybrid fitness.

93 The DMI

94 The incompatibility is formed by two unlinked biallelic loci, situated on autosomes
 95 \mathcal{A} , X chromosomes \mathcal{X} , or in the mitochondrial genome (cytoplasmic organelle) \mathcal{O} ,
 96 (cf. Table 1). Both sexes are diploid for autosomes and haploid for the mitochondrial
 97 locus. Males are hemizygous for the X chromosomes, whereas females are diploid.
 98 The continent is monomorphic for the continental (geno-)type and only acts as source
 99 of migrants for the island. Our analysis focuses on the evolutionary dynamics on
 100 the island. A stable DMI corresponds to a stable equilibrium on the island where
 101 all four alleles are maintained (a two-locus polymorphism), including the pair of
 102 incompatible alleles (indicated by capital letters in Table 1).

103 We model genotypic fitness as the sum of direct allelic fitness and epistasis. Hence
 104 any given allele contributes directly to genotype fitness, where it can be locally or
 105 globally adapted, and additionally via epistasis if it is incompatible with other alleles
 106 in the same genotype. We set the (Malthusian) fitness of genotypes containing no
 107 incompatible alleles (only lower case letters) in both sexes to 0. For simplicity, we
 108 assume no dominance of the single-locus effects, but we allow for dominance or

Different genomic architectures of DMIs.

Model	DMI	continental type ($\varphi, \sigma^{\varphi}$)	island type ($\varphi, \sigma^{\varphi}$)
A→A	$\mathcal{A}-\mathcal{A}$	aaBB	AAbb
X→A	$\mathcal{A}-\mathcal{X}$	aaXX, aaXy	AAxx, AAxy
A→X	$\mathcal{A}-\mathcal{X}$	AAxx, AAxy	aaXX, aaXy
X→X	$\mathcal{X}-\mathcal{X}$	$X_1X_1x_2x_2, X_1x_2y$	$x_1x_1X_2X_2, x_1X_2y$
A→O	$\mathcal{A}-\mathcal{O}$	AAo	aaO
O→A	$\mathcal{A}-\mathcal{O}$	aaO	AAo
X→O	$\mathcal{X}-\mathcal{O}$	XXo, Xyo	xxO, xyO
O→X	$\mathcal{X}-\mathcal{O}$	xxO, xyO	XXo, Xyo

Table 1: Each genomic architecture is defined by a continental (geno-)type (third column) and an island (geno-)type (fourth column). Mutually incompatible pairs of DMI-alleles are denoted by capital letters. We call the immigrating DMI-allele *continental allele* and its resident incompatible partner *island allele*. The name of each model in the first column is constituted by “the continental allele → the island allele”. The A→A-model corresponds to the model by Bank et al. (2012).

109 recessitivity of the incompatibility.

110 We define the fitness of an arbitrary female genotype as

$$\omega(G^{\varphi}) = \underbrace{n_C \cdot \sigma_C^{\varphi} + n_I \cdot \sigma_I^{\varphi}}_{\text{allelic fitness}} - \underbrace{\Gamma_*(G^{\varphi})}_{\text{epistasis}} \quad (2)$$

111 or for a male genotype as

$$\omega(G^{\sigma}) = n_C \cdot \sigma_C^{\sigma} + n_I \cdot \sigma_I^{\sigma} - \Gamma_*(G^{\sigma}). \quad (3)$$

112 The allelic fitness is captured by the selection coefficient $\sigma^{\varphi}, \sigma^{\sigma}$ (for females and
 113 males) and weighted with the respective number of incompatible alleles, $n_{C,I} \in$
 114 $\{0, 1, 2\}$ in a given genotype. To match the locus effects of haploid mitochondrial
 115 genes to autosomes, we set $n_{C,I} \in \{0, 2\}$ for the absence or presence of the single
 116 incompatible allele in this case.

117 We assume $\sigma^{\sigma} = \sigma^{\varphi}$ for autosomes and organelles, but for X-linked alleles the fitness
 118 effect may be enhanced in males, $\sigma^{\sigma} = (1 + D)\sigma^{\varphi}$, where $D \in \{0, 1\}$ measures
 119 dosage compensation (see below). The contribution of epistasis to hybrid genotype
 120 fitness can be summarized by an epistasis vector Γ_* , for each model (*), detailed in
 Table 2

Strength of the incompatibility: The epistasis vector

DMI	hybrids: φ, σ	epistasis vector Γ_*
$\mathcal{A}-\mathcal{A}$	φ : AaBb, AaBB, AABb, AABB σ : AaBb, AaBB, AABb, AABB	$\Gamma_{\mathcal{A}\mathcal{A}} = (\underbrace{\gamma_1, \gamma, \gamma, 2\gamma}_{\varphi}, \underbrace{\gamma_1, \gamma, \gamma, 2\gamma}_{\sigma})$
$\mathcal{A}-\mathcal{X}$	φ : AaXx, AaXX, AAXx, AAXX, σ : AaXy, AAXy	$\Gamma_{\mathcal{A}\mathcal{X}} = (\gamma_1, \gamma, \gamma, 2\gamma, (1 + D)\frac{\gamma}{2}, (1 + D)\gamma)$
$\mathcal{X}-\mathcal{X}$	φ : $X_1x_1X_2x_2, X_1x_1X_2X_2$ $X_1X_1X_2x_2, X_1X_1X_2X_2$, σ : X_1X_2y	$\Gamma_{\mathcal{X}\mathcal{X}} = (\gamma_1, \gamma, \gamma, 2\gamma, (1 + 3D)\frac{\gamma}{2})$
$\mathcal{A}-\mathcal{O}$	φ : AaO, AAO, σ : AaO, AAO	$\Gamma_{\mathcal{A}\mathcal{O}} = (\gamma, 2\gamma, \gamma, 2\gamma)$
$\mathcal{X}-\mathcal{O}$	φ : XxO, XXO, σ : XyO	$\Gamma_{\mathcal{X}\mathcal{O}} = (\gamma, 2\gamma, (1 + D)\gamma)$

Table 2: The table shows all possible hybrid genotypes with DMIs (second column) and corresponding fitness cost, parametrized by the entries of the epistasis vector (third column). The strength of the incompatibility depends on the number of incompatible alleles in the genotype. Plausibly, the strength increases with the number of incompatible pairs, which can be 1, 2, or 4 (Turelli and Orr, 2000). We focus on two particular epistasis schemes, one with a codominant DMI ($\gamma_1 = \frac{\gamma}{2}$) with fitness cost proportional to the number of incompatible pairs and one with a recessive DMI ($\gamma_1 = 0$) where the fitness cost is zero if there is still a pair of compatible alleles in the genotype. The strength of X-linked incompatibilities in males depends on dosage compensation, captured by $D \in \{0, 1\}$.

121

122 Dosage compensation

123 Dosage compensation can be related to different mechanisms. For example, in the
 124 model organism *Drosophila melanogaster* the expression of the X chromosome is
 125 doubled in males. An alternative mechanism has evolved in mammals, where one X
 126 chromosome is randomly inactivated in females (Payer and Lee, 2008). Finally, in
 127 birds dosage compensation seems to be incomplete, as some genes show elevated
 128 expression levels in homogametic ZZ-males compared to heterogametic females,

129 whereas other genes are dosage compensated (Ellegren et al., 2007; Graves et al.,
130 2007).

131 Our model allows for arbitrary sex-dependence of allelic and epistatic effects, but
132 we focus on dosage compensation of the hemizygous X chromosome in males as a
133 key biological mechanism. We model fitness for any X-linked allele in hemizygous
134 males in two ways (Charlesworth et al., 1987):

- 135 • *No dosage compensation, $D = 0$* : A single copy of an X-linked allele has the
136 same allelic ($\sigma^{\sigma^{\text{♂}}} = \sigma^{\sigma^{\text{♀}}}$) and epistatic effects in hemizygous males as in females.
- 137 • *Full dosage compensation, $D = 1$* : Hemizyosity of the X chromosome is
138 compensated in males, and a single X-linked allele has the same effect as a
139 homozygous pair of X chromosomes in females (allelic selection coefficient:
140 $\sigma^{\sigma^{\text{♂}}} = 2\sigma^{\sigma^{\text{♀}}}$).

141 With random deactivation of X in females we naturally obtain a codominant
142 DMI in our model since (average) heterozygous fitness is equal to the mean of the
143 homozygous fitnesses in this case.

144 **Dynamics of the general model**

145 For our analytical treatment, we assume weak evolutionary forces, such that linkage
146 equilibrium among both loci and Hardy-Weinberg-proportions can be assumed. It
147 is then sufficient to track the frequencies of the continental allele p_C and the island
148 allele p_I on the island. We test this approximation for stronger selection by numerical
149 simulations in SI Section A.2.

150 For each genomic architecture (Table 1) we derive a pair of differential equations
151 in continuous time (see **Box 1**). For the case of an X→A DMI, in particular,
152 p_C measures the frequency of the incompatible X allele that immigrates from the
153 continent and p_I the frequency of the incompatible autosomal allele on the island.

154 We obtain:

$$\begin{aligned}
 \dot{p}_C &= p_C(1 - p_C) \left(\frac{3+D}{3} \sigma_C^{\ominus} + \frac{2}{3} p_I \left((2p_C(1 - p_I) + p_I)(2\gamma_1 - \gamma) - 2\gamma_1 - \frac{\gamma}{2}(1 + D) \right) \right) \\
 &\quad + (1 - p_C) \left(1 + \frac{R}{3} \right) m \\
 \dot{p}_I &= p_I(1 - p_I) \left(\sigma_I^{\ominus} + \frac{1}{2} p_C \left((2p_I(1 - p_C) + p_C)(2\gamma_1 - \gamma) - 2\gamma_1 - \frac{\gamma}{2}(1 + D) \right) \right) \\
 &\quad - p_I m
 \end{aligned} \tag{4}$$

155 We see that with dosage compensation ($D = 1$), the X-linked allelic fitness is
 156 increased ($\frac{4}{3} \sigma_C^{\ominus}$), because a single X-allele in males now acts as strongly as two
 157 X-alleles in females. Similarly, dosage compensation increases the term due to
 158 epistasis in males ($\frac{\gamma}{2}(1 + D)$) affecting both the X-linked allele and the autosomal
 159 allele. Sex-biased migration, quantified by R (see Eq. 1), affects only the X-linked
 160 allele, as males are hemizygous X carriers. Parameterizations for all other cases are
 161 provided in the SI Section B.1.2.

Box 1:

Dynamics of the continental allele frequencies p_C :

$$\dot{p}_C = \begin{cases} \text{for } \mathcal{A} : & p_C \left(\frac{\omega_C^{*\varnothing} + \omega_C^{*\sigma}}{2} - \frac{\bar{\omega}^{\varnothing} + \bar{\omega}^{\sigma}}{2} \right) & +(1 - p_C)m \\ \text{for } \mathcal{X} : & p_C \left(\frac{2\omega_C^{*\varnothing} + \omega_C^{*\sigma}}{3} - \frac{2\bar{\omega}^{\varnothing} + \bar{\omega}^{\sigma}}{3} \right) & +(1 - p_C) \left(1 + \frac{R}{3} \right) \cdot m \\ \text{for } \mathcal{O} : & p_C (\omega_C^{*\varnothing} - \bar{\omega}^{\varnothing}) & +(1 - p_C)(1 + R) \cdot m \end{cases}$$

Dynamics of the island allele p_I :

$$\dot{p}_I = \begin{cases} \text{for } \mathcal{A} : & p_I \left(\frac{\omega_I^{*\varnothing} + \omega_I^{*\sigma}}{2} - \frac{\bar{\omega}^{\varnothing} + \bar{\omega}^{\sigma}}{2} \right) & -p_I m \\ \text{for } \mathcal{X} : & p_I \left(\frac{2\omega_I^{*\varnothing} + \omega_I^{*\sigma}}{3} - \frac{2\bar{\omega}^{\varnothing} + \bar{\omega}^{\sigma}}{3} \right) & -p_I \left(1 + \frac{R}{3} \right) \cdot m \\ \text{for } \mathcal{O} : & p_I (\omega_I^{*\varnothing} - \bar{\omega}^{\varnothing}) & -p_I (1 + R) \cdot m \end{cases}$$

Marginal fitness $\omega_{C/I}^{*\varnothing/\sigma}$ and mean fitness $\bar{\omega}^{\varnothing/\sigma}$ for each sex are functions of genotype fitness (consult SI Eqs.(B.9),(B.10) for explicit expressions). Sex-bias in migration m is measured by R (Eq.(1)).

162

163 **The codominant model**

164 If the effect of the incompatibility is additive, such that it is proportional to the
 165 number of incompatible pairs in a genotype ($\gamma_1 = \frac{\gamma}{2}$ in Table 2), the model simplifies
 166 greatly. For the X→A model, in particular,

$$\begin{aligned}\dot{p}_C &= (1 - p_C)\left(\frac{3+D}{3}p_C(\sigma_C^{\circlearrowleft} - \gamma p_I) + \left(1 + \frac{R}{3}\right)m\right) \\ \dot{p}_I &= p_I\left((1 - p_I)\left(\sigma_I^{\circlearrowleft} - \frac{(3+D)}{4}\gamma p_C\right) - m\right)\end{aligned}\tag{5}$$

167 see SI Eqs. (B.34) for the other models.

168 Evolutionary histories

169 A parapatric DMI can evolve via different routes, depending on the timing and
170 geographic location of the origin of the two mutations. Following Bank et al. (2012),
171 we distinguish five histories: For *secondary contact*, both substitutions occur during
172 an allopatric phase and can originate in any order. In contrast, if the substitutions
173 originate in the presence of gene flow, the timing matters and we obtain four further
174 scenarios: for a *continent-island* DMI we have the first substitution originating on
175 the continent and the second on the island. Analogously, there are *island-continent*,
176 *island-island*, and *continent-continent* scenarios. Note that the first two scenarios
177 lead to *derived-derived DMIs*, with one substitution in each deme, whereas the
178 last two lead to *derived-ancestral DMIs*, where both substitutions occur in the
179 same deme. In all cases we refer to the immigrating incompatible allele as the
180 *continental allele* and to the resident, incompatible allele as the *island allele*. All
181 five evolutionary histories lead to the same dynamics (as given in **Box 1**) upon
182 appropriate relabeling of genotypes, where different histories correspond to different
183 initial conditions (see SI Section B.2.5 and "Mapping of evolutionary histories"
184 below).

185 3 Results

186 Our analytical analysis of the dynamical system in **Box 1** is presented in comprehensive
187 form in SI B. It comprises on the following steps. For the general model ($0 \leq \gamma_1 < \gamma$),

188 we determine all boundary equilibria and conditions for their stability. Instability
189 of all boundary equilibria implies a protected polymorphism at both loci. Excluding
190 cycling behavior, this is a sufficient condition for a globally stable DMI that will
191 be reached from all starting conditions (all evolutionary histories). An internal
192 stable equilibrium (DMI) can also coexist with a stable boundary equilibrium. In
193 this case, the DMI is only locally stable and will only be reached from favorable
194 starting conditions. Necessary and sufficient conditions for the existence of (locally
195 or globally) stable DMIs can be derived for weak migration by means of perturbation
196 analysis: A stable DMI results if the monomorphic boundary equilibrium ($p_I = 1$,
197 $p_C = 0$) is stable for $m = 0$ and is dragged inside the state space for small $m > 0$.
198 For codominant DMIs, also the internal equilibria can be assessed analytically and
199 conditions for stable DMIs follow from a bifurcation analysis. For the recessive
200 DMIs, we complement our analytical results by numerical work to derive stability
201 conditions for locally stable DMIs under stronger migration.

202 Below, we summarize the key results for the general model. This is followed by a
203 detailed analysis of the codominant model. In the supplement we added continuative
204 results, first for the recessive model in SI Section A.1. Second, SI Section A.2
205 contains simulation results to assess the effects of linkage disequilibrium (LD), which
206 is relevant for very strong incompatibilities. Third, we present simulations for finite
207 populations and analyze how migration limits are affected by genetic drift in SI
208 Section A.3. Finally, in SI Section A.4 we calculate adaptive substitution rates for
209 autosomes and X chromosomes with gene flow and derive conditions on dominance
210 favoring the *faster X-effect*, described by Charlesworth et al. (1987).

211 **Stable equilibria: global and local stability of DMIs**

212 The model has three boundary equilibria: A monomorphic state, where the continental
213 genotype swamps the island, which is always reached for strong migration. Furthermore,
214 two single locus polymorphisms (SLPs) where one locus is swamped, but the other is

215 maintained polymorphic. There is at most one stable internal equilibrium, corresponding
216 to a DMI. It can either be globally or locally stable. In the latter case, one of
217 the boundary equilibria is also locally stable and it depends on the evolutionary
218 history which equilibrium is reached. We therefore obtain two migration thresholds
219 $0 \leq m_{\max}^- \leq m_{\max}^+$:

- 220 • For migration rates $0 \leq m < m_{\max}^-$, a globally stable DMI, that is reached for
221 all evolutionary histories.
- 222 • For migration rates $0 \leq m_{\max}^- \leq m < m_{\max}^+$, the dynamics are bistable and
223 yield a locally stable DMI. Hence, only certain evolutionary histories permit
224 its evolution, but any existing DMI will be maintained.
- 225 • For migration rate $m_{\max}^+ \leq m$ no stable DMI exists.

226 Mapping of evolutionary histories

227 Every evolutionary history maps to a distinct initial condition (SI Section B.2.5 for
228 results and proofs). As in Bank et al. (2012), we find three permissive histories that
229 always result in the evolution of a stable DMI for $m < m_{\max}^+$: *secondary contact*,
230 *island-continent*, and *continent-continent*. In all these cases, the second substitution
231 occurs in a deme where the incompatible first substitution is not (yet) present.
232 In contrast, the evolution of a stable DMI in parapatry is more difficult for an
233 *island-island* or *continent-island* substitution history. Here, the second substitution
234 needs to invade on the island despite of competition of the incompatible allele. We
235 need $m < m_{\max}^-$ for a DMI to originate under these circumstances.

236 Necessary conditions for the existence of a stable DMI

237 Based on previous results for the model without migration (Rutschman, 1994) or
238 without epistasis (Bürger and Akerman, 2011), and in accordance to Bank et al.
239 (2012), we find that with epistasis and increasing migration a stable DMI can only

240 exist if the island allele is beneficial and its sex-averaged selection coefficient exceeds
241 migration. Furthermore, any averaged selective advantage of the continental allele
242 must be outweighed by averaged epistasis. For example for $X \rightarrow A$, we obtain $m < \sigma_I^{\ominus}$
243 and $\frac{\sigma_C^{\oplus}}{3} < \frac{\gamma}{2}$. Consult Eqs. B.29, B.31 and Table B.3 for different terms for each model
244 and the SI Sections B.1.3, B.1.6 for proofs.

245 **3.1 Nuclear codominant DMIs**

246 We obtain full analytical solutions for the maximum migration bounds m_{\max}^{\pm} (B.2.4).
247 Below, we discuss how these rates depend on the various genetic architectures, sex
248 dependence of fitness and migration, and on dosage compensation. Figures 2 and
249 3 compare the m_{\max}^{\pm} for the different types incompatibilities among nuclear genes:
250 DMIs among autosomal genes ($A \rightarrow A$), DMIs among X and autosomes, with either
251 the incompatible X allele immigrating from the continent ($X \rightarrow A$) or the autosomal
252 locus ($A \rightarrow X$), and DMIs among two X-linked loci ($X \rightarrow X$). Figure 2 assumes full
253 dosage compensation of X-linked alleles in males, Figure 3 treats the case without
254 dosage compensation.

255 **Selection against hybrids and against immigrants**

256 Following Bank et al. (2012), we can distinguish two main selective forces maintaining
257 a DMI in the face of gene flow. If the continental allele is beneficial on the island
258 (first column of Fig. 2 and 3), a polymorphism at the respective locus can only be
259 maintained by hybrid formation and selection against the immigrating allele is due
260 to hybrid inferiority (“selection against hybrids”). This type of selection will only be
261 effective as long as the immigrating allele is rare. Once the migration pressure is so
262 high that the immigrating continental allele is in a majority, incompatibility selection
263 rather works against the resident allele on the island. Consequently, we expect a
264 large bistable regime with $m_{\max}^+ \gg m_{\max}^-$ and a small region with global stability,
265 as can indeed be seen for all types of DMIs with a beneficial continental allele. Note

266 also that m_{\max}^+ increases with γ , as should be expected if hybrid incompatibility, *i.e.*
267 epistasis, is the sole cause of (local) stability.

268 In contrast, with a deleterious immigrating allele (third column of Fig. 2 and 3),
269 a DMI can also be maintained by “selection against immigrants” for small values
270 of epistasis, or via a combination of the two selective forces (selection against
271 hybrids and immigrants) with stronger epistasis. If selection against immigrants
272 predominates, maintenance of the DMI is driven by local adaptation. The fitness
273 advantage of the resident allele depends on its direct effect and the dynamics will
274 usually be frequency independent. Therefore we obtain no or only a small bistable
275 regime, with $m_{\max}^+ \approx m_{\max}^-$. For stronger epistasis, selection against hybrids becomes
276 more important, leading to a relative increase of the bistable regime. The main effect
277 of epistasis now is that it promotes swamping of the island allele: $m_{\max}^{+/-}$ decreases
278 with epistasis. In the case of a neutral immigrating allele, the observed migration
279 bounds exhibit an intermediate pattern.

280 Sex-biased migration

281 To understand the differences among the DMI architectures, we take the case of
282 full dosage compensation and strict female-biased migration ($R = 1$) as a starting
283 point (Fig. 2(a)-(c)). In this case, all curves for m_{\max}^{\pm} for the different models
284 collapse onto a single one. Indeed, if only females migrate, the number of migrating
285 X chromosomes and autosomes is equal. Full dosage compensation balances any
286 direct and epistatic effects of loci with different ploidy levels. Consequently, the
287 corresponding Eqs. (B.34) differ only by a constant factor.

288 If also males migrate (Fig. 2(d)-(i)) genomic architectures involving an X chromosomes
289 experience effectively lower migration rates of the X and hence increasing m_{\max}^{\pm} .
290 Male-biased migration boosts m_{\max}^{\pm} most effectively for X→X, as both loci experience
291 reduced migration pressure. For unbiased migration, m_{\max}^+ of X→X relative to A→A
292 DMIs increases by $\frac{4}{3}$ (the autosome-X ratio), and doubles for pure male migration

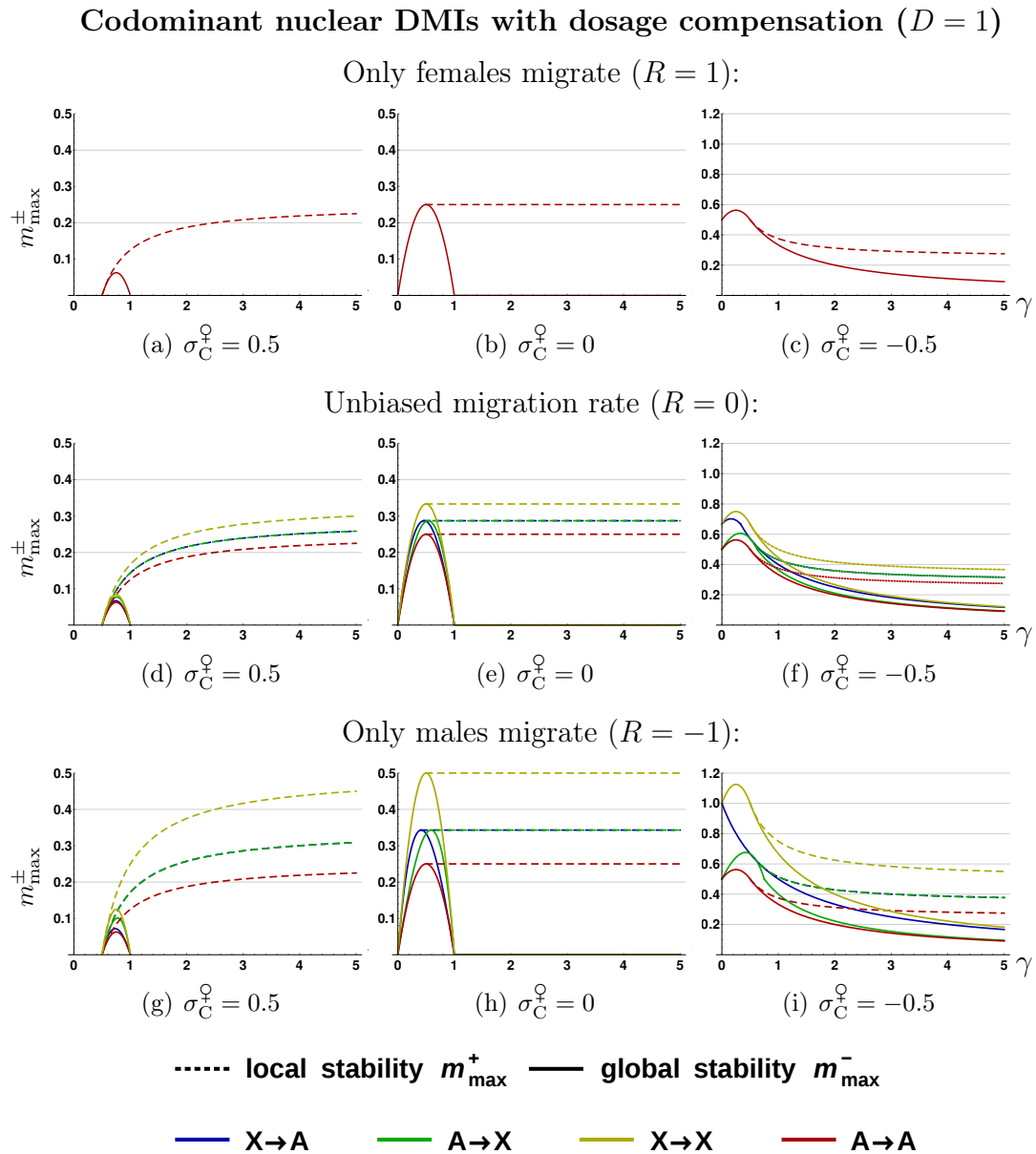


Figure 2: **Codominant nuclear DMIs with dosage compensation, $D = 1$.** The columns show m_{\max}^{\pm} as a function of the strength of epistasis γ for beneficial ($\sigma_C^{\circ} = 0.5$), neutral ($\sigma_C^{\circ} = 0$), and deleterious ($\sigma_C^{\circ} = -0.5$) effect of the immigrating allele. All quantities in the figure (σ_C° , γ , m_{\max}^{\pm}) are measured relative to the fitness effect of the island allele, which is normalized to $\sigma_I^{\circ} = 1$. Note the different scaling of the y-axis in the third column. Strong differences between m_{\max}^{\pm} in the various models occur if migration rates are sex-biased. For female-biased migration m_{\max}^{\pm} coincide for all four models. With increasing proportion of male migrants (top to bottom), migration pressure on the X chromosome is reduced and differences among the models appear. All bounds m_{\max}^{\pm} are derived analytically, see Eqs.(B.40),(B.42).

293 (corresponding to the 1:2 X-autosome ratio among migrants in this case).

294 The migration bounds m_{\max}^{\pm} for the A→X and X→A DMIs are intermediate
295 between the A→A and X→X DMIs. Our analytical results (see B.2) show that the
296 upper limit of the bistable regime (*i.e.*, the value of m_{\max}^+) is identical for the A→X
297 and the X→A models with dosage compensation. However, the limits for global
298 stability, m_{\max}^- , can differ, which can be understood as follows:

299 For pure selection against migrants (no epistasis $\gamma \rightarrow 0$, and $\sigma_C < 0$, right column
300 in Fig. 2), increased male migration reduces the effective migration pressure on the
301 X chromosome. This leads to a corresponding increase in the migration bound m_{\max}^-
302 ($= m_{\max}^+$ in this case) for all DMIs that are lost for $m > m_{\max}^{\pm}$ because of swamping
303 at an X-locus. This is clearly always the case for X→X DMIs, but also for the
304 X→A model, as long as $|\sigma_C| < |\sigma_I|$ (as in our example: X fixes before A is lost).
305 In contrast, for the A→A and the A→X model (if $|\sigma_C| < |\sigma_I|$) the DMI is lost due
306 to swamping at the autosomal locus (continental locus in these cases). Increased
307 male bias in migration therefore does not change the migration bound m_{\max}^{\pm} in these
308 cases.

309 For strong epistasis (with a deleterious immigrating allele), where the direct locus
310 effects are less important, it is always the incompatible island allele that cannot
311 invade on the island for migration rates $m > m_{\max}^-$. Here, any incompatible island
312 allele that interacts with an X allele has an advantage from male-biased migration
313 since it feels less gene flow from the competing X. This can be seen for the m_{\max}^-
314 lines in Figure 2(f),(i): While the migration bound is increased for the X→A model
315 (and the X→X model) over the whole range of epistasis, it converges to the value
316 of the autosomal DMI for the A→X model.

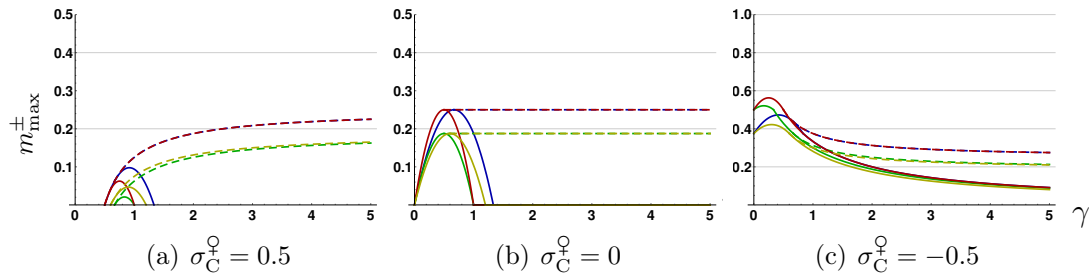
317 **No dosage compensation**

318 In Figure 3 we investigate migration bounds without dosage compensation, such
319 that the differences in ploidy between autosomes and X chromosomes are no longer

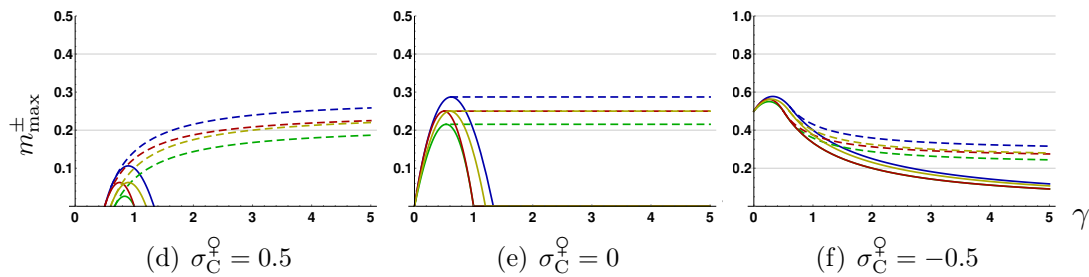
320 masked. Relative to the model with dosage compensation, we have weaker allelic
 321 and epistatic effects of the X chromosome. Hence, incompatible island X alleles
 322 are easier go get swamped and also have a more difficult time to keep incompatible
 323 continental (A or X) alleles from swamping.

Codominant nuclear DMIs without dosage compensation ($D = 0$)

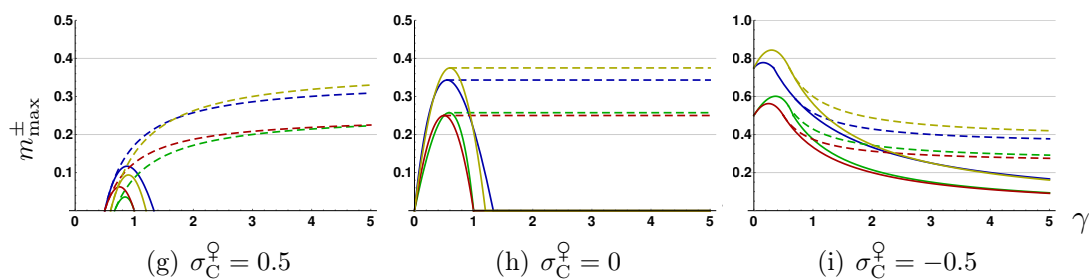
Only females migrate ($R = 1$):



Unbiased migration rate ($R = 0$):



Only males migrate ($R = -1$):



----- local stability m_{\max}^+ ——— global stability m_{\max}^-
 ——— $X \rightarrow A$ ——— $A \rightarrow X$ ——— $X \rightarrow X$ ——— $A \rightarrow A$

Figure 3: **Codominant nuclear DMIs without dosage compensation, $D = 0$.** Without dosage compensation the ploidy differences between the autosomes and the X chromosome are unmasked, inducing strong asymmetry between the \mathcal{A} - \mathcal{X} -models. this leads to a larger effect per allele. All bounds m_{\max}^{\pm} are derived analytically, see Eqs.(B.40),(B.42). See also Figure 2 for further explanations. Note the different scaling of the y-axis in the third column.

324 The consequences can most easily be seen in the first row of Figure 3(a)-(c)
325 with pure female migration, where, in contrast to dosage compensation, differences
326 between the various genomic architectures are not compensated anymore. We
327 observe a strong asymmetry between m_{\max}^{\pm} of X→A and A→X-models for all levels
328 of male migration relative to the corresponding results with dosage compensation.
329 Here migration bounds for X→A always exceed those obtained for A→X-models.
330 Intuitively, one can understand this as follows: In the X→A model, three immigrating
331 X chromosomes “fight” against four resident autosomes, whereas in A→X the odds
332 are in favor of the immigrating autosomes. Thus the island is swamped more easily
333 in the latter case.

334 As seen for dosage compensation before, for weak epistasis ($\gamma \approx 0$, pure “selection
335 against immigrants”), it is always the locus with weaker direct effect that is swamped
336 first. In our example this is always the “continental” locus, because we have stronger
337 selection on the island locus. For unbiased migration (Fig. 3(f)) all models converge
338 to the same bound. However, introducing sex-biased migration leads to relative
339 higher gene flow on the X for a female bias (and therefore lower bounds for models
340 with immigrating X), as can be seen in Figure 3(c). Similarly, male-biased migration
341 leads to weaker X-linked gene flow and a higher bounds in these models, *i.e.* X→A
342 and X→X, (Fig. 3(i)).

343 If we compare migration bounds of Figure 2 and 3, we can see that dosage
344 compensation outbalances most of the differences in m_{\max}^{\pm} between A→X and X→A,
345 especially for local stability. While dosage compensation strengthens the fitness
346 effect of the island allele in A→X, the increased epistatic pressure on the continental
347 allele in X→A is outbalanced by its increased fitness effect.

348 3.2 Cytonuclear (mitochondrial) codominant DMIs

349 Finally, we investigate cytonuclear DMIs in Figure 4, where a gene in the haploid
350 mitochondrial genome (termed o/O for organelle) is incompatible with a nuclear

351 locus. Dosage compensation of the X chromosome again means that the male
352 XyO-hybrids suffer as much as the female XXO-hybrids while they suffer only as
353 much as XxO hybrids without dosage compensation. Relative to nuclear DMIs,
354 three main effects lead to changes in m_{\max}^{\pm} :

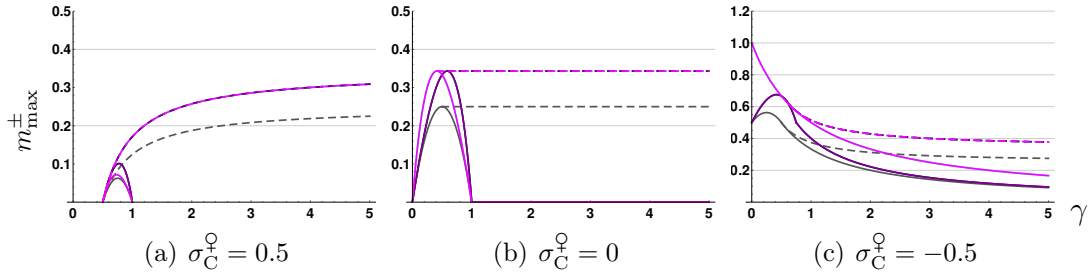
355 First, the cytoplasmic locus experiences effectively stronger direct and epistatic
356 selection (factor two in Eqs. (B.34c)), because we maintain the per locus effect
357 identical to nuclear loci. Since a single allele already accounts for the full mitochondrial
358 locus effect this leads to a larger effect per allele. As a consequence, m_{\max}^{\pm} without
359 sex-bias in migration is elevated relative to A→A model (gray lines in Fig. 4(a)-(c)).

360 Second, sex-biased migration has an even stronger effect in cytonuclear DMIs
361 than in the X-linked nuclear DMIs: Since mitochondria are maternally inherited, the
362 effective gene flow for mitochondrial loci is reduced to zero with pure male migration.
363 Consequently, all migration bounds with immigrating incompatible mitochondrial
364 genes diverge to infinity. In Figure 4 (last two rows), we study the case of strong,
365 but not complete male bias ($R = -0.9$). Since the migration pressure on the
366 mitochondrial locus and the X chromosome is reduced, migration bounds m_{\max}^{\pm}
367 increase for all cytonuclear DMIs, especially for those also involving X chromosomes.
368 This increase in m_{\max}^{\pm} is even further promoted by dosage compensation, strengthening
369 the effect of X.

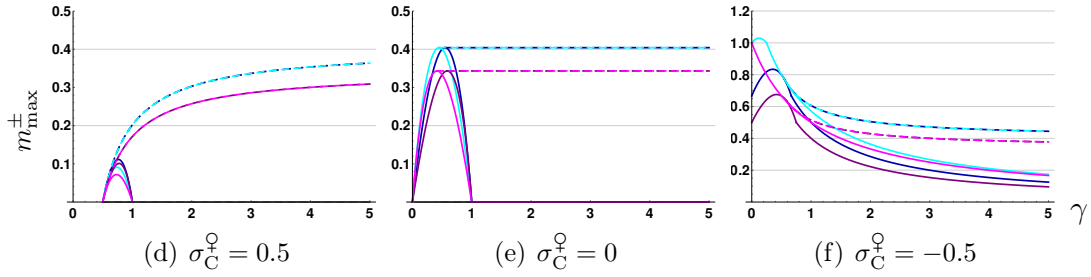
370 Finally, because of strict maternal inheritance, the dynamics of the mitochondrial
371 locus is not influenced by any fitness effects in males. In $\mathcal{X}\text{-}\mathcal{O}$ models this also entails
372 that dosage compensation only affects the dynamics of the X-locus - in contrast
373 to nuclear DMIs, where also autosomal loci are affected if they interact with a
374 hemizygous X locus. As a consequence, the boosting effect of dosage compensation
375 on m_{\max}^{\pm} is symmetric for O→X and X→O, in stark contrast to nuclear DMIs, where
376 dosage compensation does not change much for X→A while it strongly increases
377 A→X.

Codominant cytonuclear (mitochondrial) DMIs

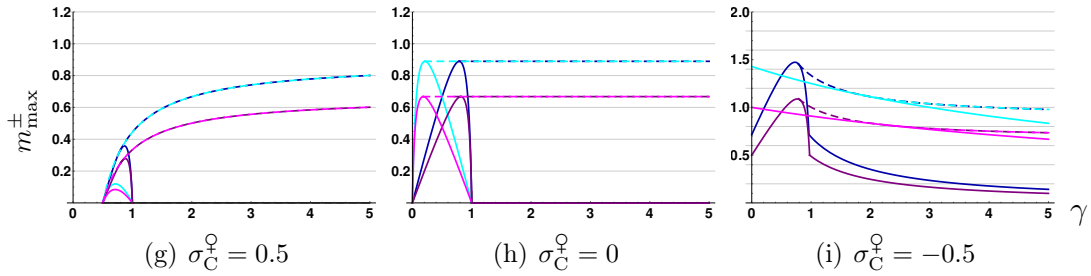
Unbiased migration ($R = 0$) without dosage compensation ($D = 0$):



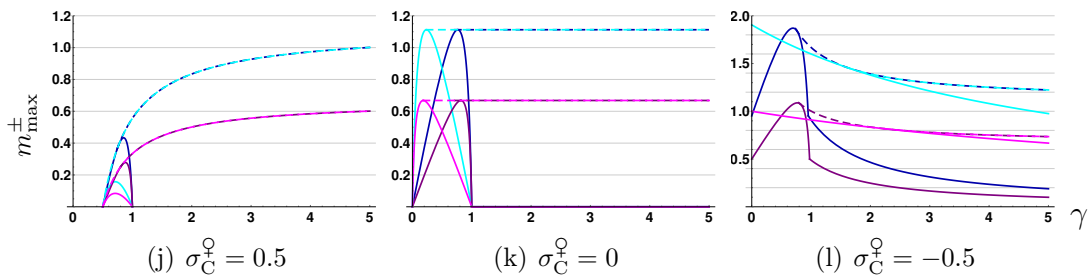
Unbiased migration ($R = 0$) with dosage compensation ($D = 1$):



Male dominated migration ($R = -0.9$) without dosage compensation ($D = 0$):



Male dominated migration ($R = -0.9$) with dosage compensation ($D = 1$):



----- local stability m_{\max}^+ ——— global stability m_{\max}^-
— X→O — O→X — A→O — O→A

Figure 4: **Codominant cytonuclear DMIs.** Maximum permissible migration rates for local stability either coincide for all models (a)-(c), or just for X→O and O→X as well as for O→A and A→O in all other cases. Migration bounds for global stability only coincide without dosage compensation or sex-biased migration between O→X and O→A, as well as for X→O and A→O. The A→A model is given in panel (a)-(c) in gray as a reference. All bounds m_{\max}^{\pm} are derived analytically, see Eqs.(B.40),(B.42). See Figure 2 for further explanations. Note the different scaling of the y-axis in third column.

378 4 Discussion

379 If barriers to gene flow build up among populations in primary or secondary contact,
380 this can have important consequences for their genetic architecture. A lot of recent
381 interest has focused on *islands of speciation (or divergence)* (Wu, 2001; Turner
382 et al., 2005; Butlin et al., 2012; Nosil, 2012; Nosil and Feder, 2012; Via, 2012),
383 yet corresponding empirical findings are equivocal on that matter (Cruickshank
384 and Hahn, 2014; Pennisi, 2014). There are, however, several clear and undisputed
385 genomic patterns of speciation, on which we concentrate here. The most widely
386 known ones are Haldane's rule, (Haldane, 1922), which has motivated much previous
387 speciation research (see reviews and examples in Coyne and Orr (2004); Presgraves
388 (2008); Lachance and True (2010); Presgraves (2010); Oka and Shiroishi (2013)
389 and the *large X-effect* (reviewed in Presgraves, 2008), which both highlight an
390 important role of the X chromosome (or the Z chromosome in birds) in speciation. In
391 addition, hybrid incompatibilities are frequently observed also between nuclear and
392 cytoplasmic markers. Plants show incompatibilities with plastid genomes (Greiner
393 et al., 2011; Snijder et al., 2007) and mitochondria have been reported to be incompatible
394 with nuclear genes across a wide range of species (Ellison and Burton, 2008; Lee
395 et al., 2008; Burton and Barreto, 2012). In insects, cytoplasmic incompatibilities
396 can also be caused by infections with the intracellular bacterium *Wolbachia* (O'Neill
397 et al., 1992; Werren, 1997; Coyne and Orr, 2004).

398 In the current study we investigate how the genetic architecture of an initial
399 hybrid incompatibility between incipient sister species can maintain divergence in
400 the presence of ongoing gene flow. Can (primary or secondary) gene flow favor
401 X-linked or cytonuclear DMIs over autosomal ones, and if so under which conditions?
402 We studied this question about a possible first step towards speciation using a
403 minimal model of a two-locus DMI in a continent-island population that allows
404 for analytical treatment. We derive maximum permissible migration bounds which

405 still permit maintenance of a DMI in the face of gene flow. Conditions that yield
406 increased migration limits facilitate speciation, as they are lost less easily and can
407 subsequently provide more persistent seeds for further ongoing differentiation.

408 **Conditions for parapatric DMIs**

409 Like in the autosomal case (Bank et al., 2012), the origin and maintenance of
410 a two-locus X-linked or cytonuclear DMI requires that at least one of the DMI
411 substitutions (namely: the incompatible variant on the island) is adaptive. If
412 multi-locus barriers to gene flow build up gradually from initial two-locus incompatibilities,
413 this confirms that postzygotic parapatric speciation requires at least some degree
414 of ecological differentiation and local adaptation. Empirically, there is widespread
415 evidence for positive selection on genes involved in DMIs (Macnair and Christie,
416 1983; Ting et al., 1998; Presgraves et al., 2003; Barbash et al., 2004; Dettman et al.,
417 2007).

418 For all types of DMIs, we observe two basic selective forces driving their evolution.
419 Selection against immigrants implies that the new migrants have a fitness deficit
420 relative to island residents, resulting in *ecological speciation* scenarios (Schluter and
421 Conte, 2009; Nosil, 2012). A characteristic of this regime is that evolution of a stable
422 DMI is independent of its evolutionary history.

423 Alternatively, a stable DMI is caused by selection against hybrids, where migrants
424 can even have a positive fitness. If hybrids are unfit, immigrants still suffer an
425 indirect disadvantage as long as they are rare and their genotypes are readily
426 broken down by sex and recombination. This scenario typically leads to a bistable
427 dynamics, where a stable DMI will only evolve from favorable starting conditions
428 or permissive evolutionary histories (such as secondary contact). The scenario has
429 also been referred to as *mutation-order-speciation* (Mani and Clarke, 1990).

430 We measure the strength of a parapatric DMI by means of two migration bounds.
431 The higher one, m_{\max}^+ , is the limit beyond which a DMI can neither evolve nor an

432 existing one can be maintained. The lower bound, m_{\max}^- , is the limit up to which
433 a DMI will always evolve in the face of gene flow, irrespective of the evolutionary
434 history (globally stable DMI). For migration rates between both bounds, a DMI is
435 maintained, but will evolve only under favorable histories, such as secondary contact,
436 or if the second incompatible substitution occurs on the continent.

437 **Contrasting different DMI architectures**

438 We find that the genetic architecture of a DMI (with incompatible genes on autosomes,
439 X chromosomes, or in the mitochondrial genome) can have a strong effect on its
440 stability. However, this effect also crucially depends on other factors, such as, in
441 particular, the level of dosage compensation and the sex-bias in the migration rates.

442 First, without dosage compensation and without sex-biased gene flow, the hemizyosity
443 of the X chromosome in males leads to shifts of m_{\max}^\pm in the presence of epistasis
444 compared to autosome-autosome DMIs. This is due to ploidy differences: “3 X
445 chromosomes fight 4 autosomes”. Therefore, the A→X scenario (where a resident
446 X-linked allele competes with an immigrating incompatible autosomal gene) constitutes
447 a weaker barrier to gene flow than the X→A model. Note that this effect depends
448 crucially on the (negative) epistasis of the DMI and is not observed in a single-locus
449 model of local adaptation. Second, dosage compensation strengthens the X alleles,
450 which leads to higher migration bounds in all X-linked DMIs. In particular, it
451 increases stability of DMIs with an incompatible X locus on the island, compensating
452 the A→X versus X→A asymmetry. Third, sex-biased migration leads to lower/higher
453 limits for DMIs with immigrating X for female/male bias. Fourth, our results in the
454 SI Section A.1 show no large difference between codominant and recessive nuclear
455 DMIs (which lead to Haldane’s rule) concerning the migration bounds. In fact, the
456 difference for X-linked DMIs are even smaller than for autosome-autosome DMIs.
457 Fifth, for cytonuclear DMIs we often observe stronger barriers to gene flow since the
458 haploid cytoplasmic alleles experience the full locus effect. Furthermore, sex-bias

459 in migration yields an especially strong effect, as for pure male migration effective
460 gene flow at the mitochondrial locus ceases completely.

461 Our numerical simulations for the effect of LD in the SI Section A.2 agree with
462 the approximate analytical results for weak and moderately strong DMIs. For very
463 strong DMIs, stronger deviations occur for codominant $A \rightarrow A$ and $X \rightarrow X$ DMIs,
464 which maintain very strong LD once all (male and female) hybrids with incompatible
465 alleles are almost inviable/infertile. As a consequence, gene flow among the continent
466 and island haplotypes is blocked and we obtain higher migration bounds relative
467 to $X \rightarrow A$ and $A \rightarrow X$ DMIs. For the latter two, F1 hybrid males carrying the
468 compatible x allele (genotype $Aaxy$) are viable and can produce ax gametes for
469 the F2 generation. This effect of extreme LD and blocked gene flow does not exist
470 for recessive DMIs (see SI Section A.1 for details). Our numerical simulations also
471 show that the effect of drift is usually small and does not lead to qualitative changes
472 (SI Section A.3). Since DMI alleles can be lost by drift, stochastic migration bounds
473 m_{\max}^N are generally smaller than their deterministic counterparts. In SI Section A.3,
474 we present an analytical approximation to estimate this reduction due to drift.

475 ***The large X-effect***

476 Summarizing all different cases described above, we find that the most stable DMIs
477 are almost always X-linked, where migration bounds are typically enhanced by a
478 factor of $4/3$ to 2 relative to autosomal DMIs (unless migration is strongly female
479 biased). Although this is not a very strong effect, it is very general and applies
480 whenever gene flow plays a role at any stage of the speciation process. This includes,
481 in particular, scenarios of secondary contact and also later stages of the speciation
482 process where additional barriers to gene flow exist in the genomic background.
483 In this latter case, the gene flow at the focal DMI loci needs to be replaced by
484 appropriate effective migration rates (Barton and Bengtsson, 1986). The pattern
485 that follows from a more stable X barrier is consistent with a higher density of

486 X-linked hybrid incompatibilities, the *large X-effect*.

487 Our results show a clear boost of X migration bounds, in particular, if there is
488 dosage compensation and if migration is male biased. Empirical studies show that
489 sex-biased migration is common in nature and report a prevalence for migration
490 of the heterogametic sex in both mammals, where dispersal is on average male
491 biased, (Lawson Handley and Perrin, 2007) and in birds, where female dispersal
492 dominates (Greenwood, 1980). In the context of our results, these trends strengthen
493 the predicted pattern of a *large X-effect* or *large Z-effect*, respectively.

494 One example stems from the house mouse, *Mus musculus*. There is strong
495 empirical evidence for a *large X-effect* in this species (Tucker et al., 1992; Good
496 et al., 2008; White et al., 2012), such as the major involvement of the X chromosome
497 in hybrid sterility (Oka et al., 2004; Storchova et al., 2004). Mice exhibit rather
498 complete dosage compensation due to X-inactivation in females (Payer and Lee,
499 2008). Furthermore, the house mouse displays male-biased dispersal at breeding
500 age (Greenwood, 1980; Gerlach, 1990).

501 Several alternative mechanisms as potential underlying causes for a *large X-effect*
502 have been discussed in the literature, such as sex ratio meiotic drive, regulation of
503 the X chromosome in the male germ line (Coyne and Orr, 2004; Presgraves, 2008), or
504 faster evolution of the X chromosome (termed *faster-X-effect* Charlesworth et al.,
505 1987). In the panmictic population model by Charlesworth et al. (1987), faster
506 evolution on the X chromosome results if adaptations are, on average, recessive
507 and are thus exposed to stronger selection on the hemizygous X. We note that our
508 model with gene flow predicts an advantage of X-linked genes for island adaptations
509 even if they are not recessive, but codominant (or even slightly dominant, see SI
510 Section A.4 for details and proofs). Since the *faster X-effect* (more adaptations on
511 the X) also favors a *larger X-effect* (more incompatibilities involving the X), this
512 is another way how speciation with gene-flow can contribute to this pattern. In
513 summary a mono-causal explanation for the *large X-effect* seems unlikely, and it

514 remains an open question, to which extent each factor contributes. Our study adds
515 differentiation under gene flow as another element to this mix.

516 Our results relate to Haldane’s rule only in so far as this pattern partially overlaps
517 with the *large X-effect*. Beyond that, we do not obtain a prediction. In particular,
518 the migration bounds for codominant and recessive DMIs are similar (while only the
519 latter lead to Haldane’s rule).

520 **Introgression patterns**

521 A second conclusion from our results that can be related to data is that X-linked
522 alleles in an incompatibility face stronger barriers to introgression than the corresponding
523 autosomal alleles. This effect rests on two basic observations: the tendency for
524 higher migration bounds of all X-linked DMIs with dosage compensation (which
525 also contributes to a large X-effect), and the asymmetry promoting $A \rightarrow X$ over $X \rightarrow A$
526 introgression that we observe for the incompatible allele if dosage compensation is
527 incomplete or absent (the 3 versus 4 chromosomes effect). Our findings agree with
528 the result of a recent simulation study for DMIs on a cline by Wang (2013), who
529 showed that, for an X-autosome DMIs, the incompatible X allele flows less easily
530 across a cline than the autosomal allele.

531 A pattern of reduced X-introgression relative to autosomal introgression has been
532 recognized in many sister-species in nature. In the complex of *Anopheles gambiae*
533 sister clades Fontaine et al. (2015) found “pervasive autosomal introgression” between
534 different species, in contrast to the X chromosome, which contains disproportionately
535 more factors in reproductive isolation.

536 Liu et al. (2015) report three interspecies hybridization events in mice (*Mus*
537 *musculus domesticus* and *M. spretus*), leading to exclusively autosomal, partially
538 adaptive introgression. Similarly, Macholán et al. (2007) showed weaker introgression
539 patterns and lower selection pressure on the X chromosomes compared to the autosomes
540 in the central European mouse hybrid zone of *Mus musculus musculus* and *M.*

541 *m. domesticus*. The authors suppose that the X is shielded more effectively from
542 introgression due to the *large X-effect*.

543 Further examples exist for birds. Sætre et al. (2003) report “rather extensive
544 hybridization and backcrossing in sympatry” between two populations of flycatchers
545 hybridizing in secondary contact. Nevertheless, gene flow was again predominantly
546 found on the autosome. Hooper and Price (2015) report that derived cross-species
547 inversions among sister species of Estrilid finches are strongly enriched on the Z
548 chromosome. The pattern is strongest in continental clades with high level of
549 sympatry and (plausibly) higher levels of gene-flow during the speciation process. If
550 inversions harbor DMIs, this is consistent with our finding that derived incompatibilities
551 on the Z chromosome are more stable to gene flow than autosomal incompatibilities.

552

553 Also other factors, such as recombination, can influence differential introgression
554 on X chromosomes and autosomes. Indeed, there is empirical evidence that recombination
555 can structure autocorrelation patterns among introgressed loci. However, available
556 data also show that recombination cannot be the the sole explanation for differential
557 introgression among genomic regions, e.g. in mice (Payseur et al., 2004) or finches (Hooper
558 and Price, 2015). As for the *large X-effect* our mechanism is one of several possible
559 ones.

560 **Biological assumptions and limitations of the model**

561 Our study has been intended as a minimal model approach that allows for analytical
562 treatment. As such, it rests on several simplifying assumptions concerning the
563 genetics of the DMI and the ecological setting. These limitations suggest possible
564 model extensions for future work.

565 All our results assume a simple DMI between just two loci. This is in line with
566 most previous theoretical work and known empirical cases (Coyne and Orr, 2004;
567 Maheshwari and Barbash, 2011). Nevertheless, complex DMIs involving multiple

568 loci are clearly relevant at later stages of a speciation process and could lead to new
569 effects that are not captured here (*e.g.* Lindtke and Buerkle, 2015).

570 Our fitness scheme for two-locus DMIs comprises codominant and recessive
571 cases. Empirically, the functional form depends on the underlying mechanisms
572 causing hybrid fitness loss, which is still debated. Hybrid incompatibilities can
573 be due to loss-of-function or gain-of-function mutations (reviewed by Maheshwari
574 and Barbash, 2011). While the former tend to act recessively, the latter will likely
575 affect heterozygotes, and may be better captured by a partially dominant DMI.

576 Recessive DMIs, in turn, occur in a number of different types, (*e.g.* Presgraves,
577 2010; Cattani and Presgraves, 2012; Matsubara et al., 2015), which lead to slightly
578 different models. We have briefly studied some of these alternatives analytically, such
579 as a *recessive-A codominant-X*-DMI or a *codominant-A recessive-X*-DMI (data not
580 shown). We did not detect any noteworthy difference in their evolutionary dynamics
581 or for the migration bounds relative to the results reported here. Still, more relevant
582 changes are clearly possible, for example if the single locus effects can lead to over-
583 or underdominance.

584 For the results presented, we assume that dosage compensation enhances not only
585 the single-locus effect, but also the incompatibility. Empirically, hybrid incompatibilities
586 are frequently dosage-sensitive, *e.g.* in a *Arabidopsis thaliana*/*A. arenosa* cross,
587 where a DMI results due to failure in gene silencing Josefsson et al. (2006), or in
588 a *Mus musculus musculus*/*M. m. domesticus* cross, where X-linked hybrid male
589 sterility results from over-expression of X-linked genes in spermatogenesis (Good
590 et al., 2010). Furthermore, in haplo-diploid Nasonian wasps genetically engineered
591 diploid males were less affected by hybrid sterility than haploid male hybrids, pointing
592 to a strong effect of ploidy on hybrid fertility Beukeboom et al. (2015).

593 Nevertheless, we also investigated the effect of dosage compensation only on the
594 single locus effect or only on the incompatibility (results not shown). As expected,
595 we obtain intermediate patterns between no and full dosage compensation.

596 Concerning the ecological assumptions, our model assumes unidirectional gene
597 flow between two panmictic demes. While our results readily extend to weak back
598 migration (which leads only to slight shifts of the equilibria), strong bidirectional
599 migration can lead to qualitatively new effects that are not captured by our framework.
600 For example, polymorphisms at single loci can be maintained for arbitrarily strong
601 gene flow if heterogeneous soft selection leads to a rare-type advantage (Levene,
602 1953). Furthermore, generalist genotypes that are inferior in both demes, but do well
603 on average, can be maintained if (and only if) bidirectional migration is sufficiently
604 strong (see Akerman and Bürger, 2014, for results in a two-locus model without
605 epistasis).

606 Alternative models for the population structure can also lead to substantial
607 differences. In particular, our two-deme model ignores isolation by distance, which
608 can be captured either in a discrete cline model with a chain of demes, or in a
609 continuous-space framework. It is expected that polymorphisms (and DMIs) can
610 be maintained with much larger gene flow (or weaker selection) in these settings
611 (Barton, 2013). Still, several of our key results, such as reduced introgression of
612 X-linked incompatibility alleles, should still hold under these conditions (see Wang,
613 2013, for a discrete cline model).

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