

1 The theoretical molecular weight of 2 NaYF₄:RE upconversion nanoparticles

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10 Abstract

11 Upconversion nanoparticles (UCNPs) are utilized extensively for biomedical imaging, sensing, and
12 therapeutic applications, yet the molecular weight of UCNPs has not previously been reported. We
13 present a theory based upon the crystal structure of UCNPs to estimate the molecular weight of
14 UCNPs: enabling insight into UCNP molecular weight for the first time. We estimate the theoretical
15 molecular weight of various UCNPs reported in the literature, predicting that spherical NaYF₄
16 UCNPs ~ 10 nm in diameter will be ~1 MDa (i.e. 10⁶ g/mol), whereas UCNPs ~ 45 nm in diameter
17 will be ~100 MDa (i.e. 10⁸ g/mol). We also predict that hexagonal crystal phase UCNPs will be of
18 greater molecular weight than cubic crystal phase UCNPs. Additionally we find that a Gaussian
19 UCNP diameter distribution will correspond to a lognormal UCNP molecular weight distribution.
20 Our approach could potentially be generalised to predict the molecular weight of other arbitrary
21 crystalline nanoparticles: as such, we provide standalone graphic user interfaces to calculate the
22 molecular weight both UCNPs and arbitrary crystalline nanoparticles. We expect knowledge of
23 UCNP molecular weight to be of wide utility in biomedical applications where reporting UCNP
24 quantity in absolute numbers or molarity will be beneficial for inter-study comparison and
25 repeatability.

26 Introduction

27 Photonic upconversion nanoparticles (UCNPs) have garnered widespread scientific interest due
28 to their unique near infra-red (NIR) excitation and visible luminescence properties; a process
29 known as photonic upconversion. UCNPs are inorganic crystalline nanostructures (typically NaYF₄)
30 co-doped with rare-earth (RE) ions, (e.g. Yb³⁺, Er³⁺, Gd³⁺); hereby referred to in general terms as
31 NaYF₄:RE UCNPs. The RE ions act as sensitizers and emitters for photonic upconversion of multiple
32 infra-red photons, resulting in visible luminescence emission. UCNP emission is highly stable,¹ with
33 no photo bleaching, and a relatively long luminescence emission lifetime ranging from hundreds of
34 microseconds to a few milliseconds.^{2,3} NIR excitation via upconversion is highly advantageous for
35 biomedical applications, where ultraviolet or visible excitation of fluorophores (e.g. dyes, proteins,
36 or quantum dots) is normally required, with the associated challenges of photo-bleaching and
37 photo-toxicity. Interactions between nearby molecules and the UCNPs crystal structure enables
38 molecular biosensing via luminescence resonance energy transfer (LRET) between UCNPs and
39 molecules in proximity to them.⁴⁻¹⁰ As such, UCNPs have found wide utility in biomedical
40 applications, including as imaging contrast labels *in cellulo*, *in vivo*, and *ex vivo*^{5,11-19}; as biosensors
41 for detection of antibiotics²⁰ and toxins in food²¹⁻²³; as biosensors to measure biomarkers in
42 biological fluids (e.g. whole blood, serum, urine),^{6-8,24-26} and as therapeutic agents, against targets
43 such as cancer cells.^{27,28} Additionally UCNPs have been applied to nanoscale thermometry^{29,30} and
44 photovoltaic applications.^{31,32} However, to date, the molecular weight of UCNPs has not been
45 reported: as such, both the molarity of UCNPs in solution, and the absolute number of UCNPs in a
46 sample has been unknown.

47 The lack of molecular weight information for UCNPs is a considerable shortcoming in biomedical
48 applications of UCNPs, where precise quantification of UCNP concentration would be highly
49 beneficial for informing of dosage of UCNPs studies, as well as aiding inter-study comparison.
50 Additionally, quantification of UCNP molarity and absolute number of UCNPs would be highly
51 beneficial when constructing biosensors where the ratio of UCNPs compared to other molecules,
52 e.g. antibodies^{6-8,25} or oligonucleotides,³³ is important for informing biosensor design.

53 The lack of information on UCNP molecular weight is likely due to lack of experimental
54 techniques capable of measuring the molecular weight of large macromolecules such as UCNPs.
55 Using the theory we present in this paper, we predict that the molecular weight of NaYF₄:RE UCNPs
56 will range from a few mega Daltons (MDa) (i.e. 10⁶ g/mol) for exceptionally small UCNPs (~10 nm in
57 diameter), to > 100 MDa (for UCNPs with a more typical diameter of ~45 nm). This large molecular
58 weight range is well beyond the measurement limits both mass spectrometry and sedimentation

59 velocity analytical ultracentrifugation (svUAC), which are limited to < 40 kDa and < 5 MDa
60 respectively.³⁴ Despite this limitation, we attempted to employ svAUC to estimate the molecular
61 weight of UCNPs ~30 nm in diameter (corresponding to a molecular weight of ~40 MDa), but
62 reliable results were not obtained (see the Discussion section and supplementary material).

63 In this study, we present a theoretical method, based upon the extensively studied and
64 empirically proven theory of crystallography and UCNP structure, to calculate the molecular weight
65 UCNPs, accounting for UCNP composition and morphology. In brief, the crystalline structure of
66 UCNPs is quantified by transmission electron microscopy (TEM), and x-ray diffraction (XRD)
67 experiments. From this information, the total atomic weight within a single NaYF₄:RE unit cell, and
68 the total number of unit cells within a UCNP can be calculated. Thus, the theoretical molecular
69 weight of UCNPs can be calculated by summing up the total molecular weight contained within all
70 unit cells in a UCNP.

71 We anticipate that this theoretical framework could be extended to crystalline nanoparticles of
72 arbitrary morphology and composition, provided that the crystalline structure of such
73 nanoparticles are known. As such, we also provide two stand-alone graphical user interfaces (GUIs)
74 for simple calculation of the molecular weight of both NaYF₄:RE UCNPs and arbitrary crystalline
75 nanoparticles. Knowledge of UCNP molecular weight will likely be highly beneficial for
76 quantification of UCNP concentration in biomedical applications.

77 **Theory**

78 **Crystalline structure and photonic upconversion properties of UCNPs**

79 The key to understanding both the optical properties of UCNPs and their molecular weight lies
80 in the crystalline structure of UCNPs. UCNPs are a crystal lattice made up of repeating crystal unit
81 cells of NaYF₄, with a fraction of Y³⁺ ions selectively replaced by RE dopants (see Figure 1). In
82 UCNPs, photonic upconversion is enabled by the absorption of two or more near-infrared photons,
83 which, via excitation of several long-lived metastable electron states, and subsequent non-radiative
84 multi-phonon and radiative relaxation, produces luminescence emission at visible wavelengths (see
85 Figure 2). Efficient upconversion requires a crystalline host lattice, which is doped with multiple
86 different lanthanide ions (typically Yb³⁺ and Er³⁺), where one lanthanide ion acts as a photo-
87 sensitizer (typically Yb³⁺) and acts as a photonic emitter (typically Er³⁺).³⁵ Although many different
88 combinations of lattice and RE dopants have been explored,³⁶ the combination of Yb³⁺ and Er³⁺ ions
89 in a NaYF₄ host lattice has been found to provide high upconversion efficiency, and as such is
90 commonly used for UCNPs.^{37,38} Figure 2 shows an exemplar upconversion emission spectrum of

91 NaYF₄:Yb,Er cubic UCNPs (20% Yb³⁺, 2% Er³⁺) and the corresponding Jablonski diagram for
 92 upconversion.³⁹

93

94 NaYF₄:RE unit cells are either a cubic or a hexagonal crystal lattice arrangement (see Figure 1).
 95 In the face-centred cubic lattice arrangement (Na₂Y₂F₈), high-symmetry cation sites are formed, and
 96 are randomly occupied by either Na⁺ or RE³⁺ ions (see Figure 1a), and Y³⁺ ions are substituted for
 97 other RE³⁺ ions, enabling photonic upconversion. In hexagonal unit cells (Na_{1.5}Y_{1.5}F₆), there are two
 98 relatively low-symmetry cation sites, which contain either Na⁺ or RE³⁺ ions (see Figure 1b).⁴⁰
 99 Characterisation of UCNP unit cells is typically conducted by XRD measurements. Several studies
 100 have reported the crystal lattice parameters associated with cubic and hexagonal NaYF₄:RE UCNPs:
 101 these are summarised in Table 1. Wang et al., (2010)⁴⁰ report unit cell parameters for cubic (α
 102 phase) and hexagonal (β phase) unit NaYF₄:RE unit cell configurations (see Figure 1). The
 103 arrangement of ions within unit cells influences the crystal lattice parameters, consequently
 104 changing photonic properties, such as upconversion quantum efficiency.⁴⁰

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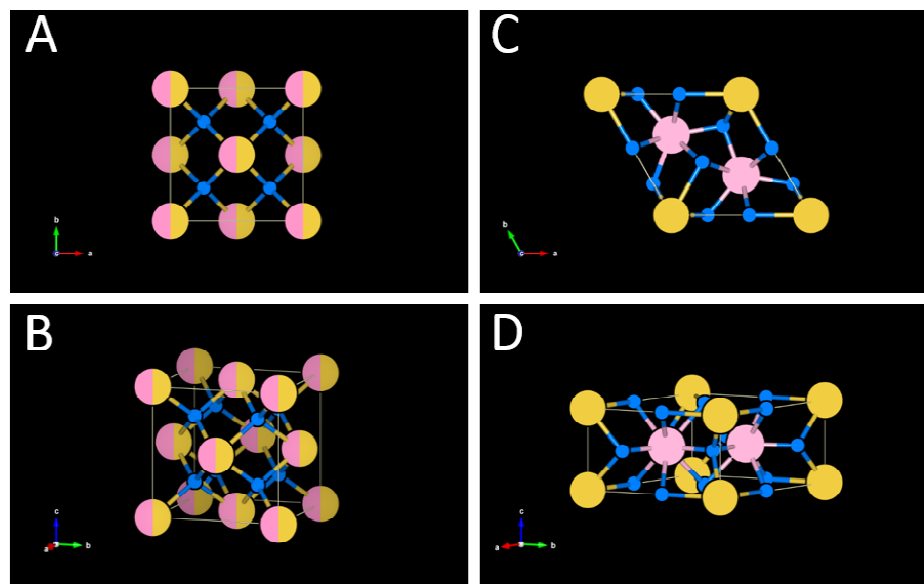
106 Synthesis of NaYF₄:RE UCNPs typically creates pseudo-spherical UCNPs with a range of
 107 diameters. For example, Sikora et al., (2013) report a Gaussian diameter distribution of UCNPs,
 108 ranging between 15 – 70 nm.¹⁴ and Haro-González et al. (2013)⁴¹ report a Gaussian diameter
 109 distribution of UCNPs UCNPs ranging from ~10 – 50 nm in diameter (see Table 1).

110

111 **Table 1.** Crystal lattice parameters of NaYF₄:RE UCNPs reported in the literature.

Study	NaYF ₄ RE dopant composition (%)	UCNP lattice structure	a (Å)	c (Å)	Mean UCNP diameter (nm)	UCNP diameter range (nm)
Sikora et al., (2013). ¹⁴	30% Yb ³⁺ , 2% Er ³⁺	Cubic	5.51	-	~ 30	15 -70
Cao et al., 2010. ¹⁵	20% Yb ³⁺ , 2% Er ³⁺	Hexagonal	5.960	3.510	33 ± 1 nm	32 - 34 nm
Wang et al., 2010. ⁴⁰	18% Yb ³⁺ , 2% Er ³⁺	Hexagonal	5.96	3.53	Not reported	Not reported
Wang et al., 2010. ⁴⁰	18% Yb ³⁺ , 2% Er ³⁺ , 60% Gd ³⁺	Hexagonal	6.02	3.60	Not reported	Not reported

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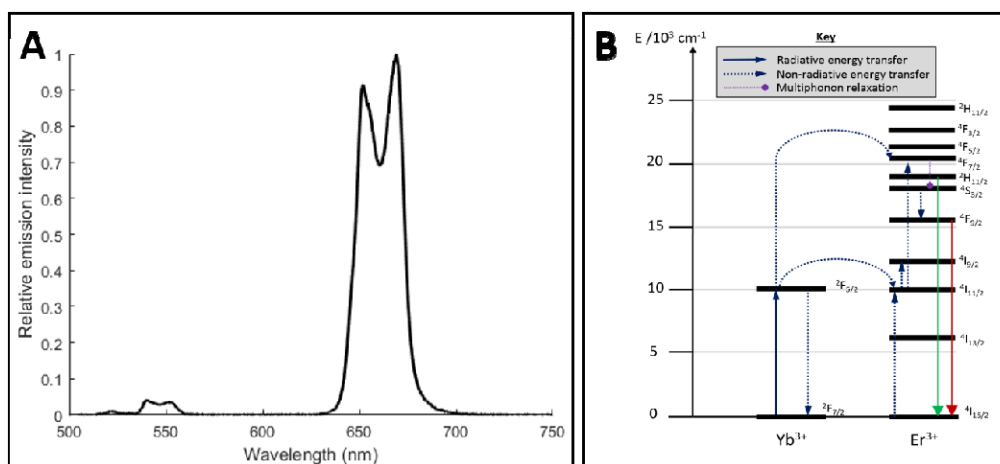
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Figure 1. NaYF₄:RE UCNPs unit cell structures. Colour key: Na⁺ ions are yellow; Y³⁺ and RE³⁺ dopant ions are pink; F⁻ ions are smaller and blue. **(A, B)** Cubic lattice unit cell structure. Sites that are randomly occupied by both Na⁺ and RE³⁺ are depicted as both pink and yellow. **(C, D)** Hexagonal lattice unit cell structure. This Figure is based upon data from Kramer et al., (2004)⁴² and Wang et al., (2010).⁴⁰ Diagrams created with the open-source software package VESTA.⁴³



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Figure 2. The upconversion emission of UCNPs. **(A)** Emission of a 1 mg/mL of NaYF₄:Yb,Er UCNPs (20% Yb and 2% Er) suspended in ultra-pure water (see supplementary material for UCNP synthesis details). **(B)** Corresponding Jablonski diagram depicting the upconversion process (based upon Heer et al., (2004)).³⁹

125 Estimating the number of unit cells in a UCNP

126 For the purposes of this study, we assume UCNPs to be spherical, with volume (V_{UCNP})

127 described by:

$$V_{UCNP} = \frac{4}{3} \pi r^3, \quad (1)$$

128 where r is the radius of the UCNP. Note that non-spherical UCNP morphologies can be
129 incorporated by modifying Equation 1 appropriately. If the UCNP consists of cubic unit cells, then
130 the volume of an individual cubic unit cell (uV_{cubic}) is given by:

$$uV_{cubic} = a_c^3. \quad (2)$$

131 If the UCNP consists of hexagonal unit cells, volume of a hexagonal unit cell ($uV_{hexagonal}$) is given
132 by:

$$uV_{hexagonal} = \frac{2\sqrt{3}}{4} a_h^2 c_h. \quad (3)$$

133 Where a_h and c_h are lattice parameters describing hexagonal unit cells. Thus, the number of unit
134 cells in a UCNP (i.e. uN_{cubic} or $uN_{hexagonal}$) can be estimated by:

$$uN_{cubic} = V_{UCNP} / uV_{cubic}, \quad (4)$$

$$uN_{hexagonal} = V_{UCNP} / uV_{hexagonal}. \quad (5)$$

135 This calculation assumes the effects of crystal dislocations and rounding error in the total number
136 of unit cells to be negligible. Further, we assume that UCNPs are composed of 100% cubic or
137 hexagonal unit cells because, to the best of our knowledge, hybrid crystal phase UCNPs have not
138 been reported.

139

140 Estimating the total atomic weight within a single unit cell

141 Assuming no RE dopants, the atomic weight of a single cubic NaYF₄ (uAW_{cubic}) or hexagonal
142 NaYF₄ unit cell (uW_{hex}) is described by:

$$uAW_{cubic} = (2 \times AW_{Na}) + (2 \times AW_Y) + (8 \times AW_F); \quad (6)$$

$$uAW_{hex} = (1.5 \times AW_{Na}) + (1.5 \times AW_Y) + (6 \times AW_F); \quad (7)$$

143 where AW_{Na} , AW_Y , and AW_F are the atomic weight (Da or g/mol) of Sodium, Yttrium, and
144 Fluorine respectively (see Table S1). We assume any mass difference due to loss of electrons due to
145 ionisation to be negligible. If RE dopant ions are added during UCNP synthesis, then a fraction of Y³⁺
146 ions are substituted for RE³⁺ dopant ions, altering the average atomic weight of unit cells within
147 UCNPs. This RE doping can be accounted for by defining a total additive factor (af):

148

$$af = fRE_{d1} + fRE_{d2} \dots + fRE_{dn}, \quad (8)$$

149 where RE_{d1} , fRE_{d2} , ... fRE_{dn} is the fractional percentage of an arbitrary number of RE dopants.
 150 The total additive factor is a numeric value ranging between 0 and 1, representing the theoretical
 151 extremes of 0% and 100% Y substitution respectively. Thus, total the atomic mass contained within
 152 a single cubic or hexagonal unit cell with RE dopants is be calculated by:

153

$$uAW_{cubic RE_{Doped}} = (2 \times AW_{Na}) + (8 \times AW_F) + (2(1 - af) \times AW_Y) + \quad (9)$$

$$(2 \times fRE_{d1} \times AW_{RE_{d1}}) + (2 \times fRE_{d2} \times AW_{RE_{d2}}) + \dots + (2 \times$$

$$fRE_{dn} \times AW_{RE_{dn}});$$

$$uAW_{hexagonal RE_{Doped}} = (1.5 \times AW_{Na}) + (6 \times AW_F) + (1.5(1 - af) \times \quad (10)$$

$$W) + (1.5 \times fRE_{d1} \times AW_{RE_{d1}}) + (1.5 \times fRE_{d2} \times AW_{RE_{d2}}) + \dots +$$

$$(1.5 \times fRE_{dn} \times AW_{RE_{dn}});$$

154 where $uAW_{cubic RE_{Doped}}$ and $uAW_{hexagonal RE_{Doped}}$ are the average atomic weight of RE doped
 155 cubic and hexagonal unit cells, respectively.

156

157 Estimating the theoretical molecular weight of a UCNP

158 Once the total number of unit cells within a UCNP (uN) and the total atomic weight (uAW)
 159 within each individual unit cell are estimated, the theoretical molecular weight of a cubic lattice
 160 UCNP (MW_{cubic}) can be estimated by summing the atomic weight contributions from all unit
 161 cells:

$$MW_{cubic} = uAW_{cubic RE_{Doped}} \times uN_{cubic}, \quad (11)$$

$$MW_{hexagonal} = uAW_{hexagonal RE_{Doped}} \times uN_{hexagonal}. \quad (12)$$

162 From Equations 4, 5, 11, and 12, it can be seen that the molecular weight of UCNP scales
 163 proportionally to volume, thus spherical UCNP's molecular weight will scale proportionally to the
 164 cube of UCNP radius.

165

166

167 **Methods**

168 **Molecular weight predictions for cubic and hexagonal NaYF₄:RE UCNPs**

169 Using the theory presented in Sections 2.4 – 2.6, the theoretical molecular weight of hexagonal
170 and cubic lattice NaYF₄ UCNPs were calculated, assuming the following typical unit cell lattice
171 parameters: cubic: $a = 5.51 \text{ \AA}$; hexagonal: $a = 5.91 \text{ \AA}$, $c = 3.53 \text{ \AA}$; (see Table 1).

172

173 **The effect of RE doping on theoretical molecular weight**

174 The effect of RE doping was investigated by using the theory presented in Sections 2.4 – 2.6 to
175 calculate the theoretical molecular weight of NaYF₄:RE UCNPs incorporating various concentrations
176 of Yb³⁺ and Er³⁺ dopant ions. We assume that UCNP lattice parameters will remain constant,
177 neglecting the unit cell contraction effect demonstrated by Wang et al. (2010),⁴⁰ where UCNP unit
178 cell lattice parameters are altered when the concentration of RE dopants is increased.⁴⁰

179

180 **The theoretical molecular weight of UCNPs reported in the literature**

181 The theoretical molecular weight of various NaYF₄:RE UCNPs reported in the literature was
182 calculated by incorporating various lattice parameters and mol% of RE dopants from the literature
183 into the theory presented in Sections 2.4 – 2.6.

184

185 **UCNP diameter distribution vs. theoretical molecular weight distribution**

186 UCNP synthesis typically produces a Gaussian distribution of UCNPs diameters. To investigate
187 how such a distribution of UCNP diameters affects the distribution of theoretical UCNP molecular
188 weights, the Gaussian diameter distribution data for a single batch of NaYF₄:Yb,Er UCNPs was
189 reproduced from data presented in Sikora et al (2013).¹⁴ The theoretical molecular weight for each
190 UCNP diameter in this distribution was calculated by the theory presented in Sections 2.4 – 2.6.
191 Gaussian fits to the data were calculated by using non-linear least squares fitting in MATLAB
192 (MATLAB 2016a, MathWorks).

193

194 **Stand-alone GUIs for calculation of nanoparticle theoretical molecular weight**

195 Two stand-alone executable graphic user interfaces (GUIs) were created in MATLAB to enable
196 rapid calculation of UCNP theoretical molecular weight. Each GUI incorporates different features
197 and assumptions. The first, more simple, GUI was developed to enable other researchers to
198 calculate the theoretical molecular weight of spherical NaYF₄:RE UCNPs for a user-defined
199 nanoparticle size range. The second, more powerful, GUI was designed to enable users to estimate
200 the theoretical molecular weight of crystalline nanoparticles with arbitrary nanoparticle geometry;

201 arbitrary lattice parameters; and arbitrary elemental composition, across a user-defined range of
202 characteristic nanoparticle sizes. Additional technical information for both GUIs is provided in the
203 supplementary material section. The stand-alone GUIs developed are shown in supplemental
204 Figures S1 and S2. These GUIs are freely available from the University of Leeds Research Data
205 Depository and are attributed with their own citable DOI (<https://doi.org/10.5518/173>).⁴⁴

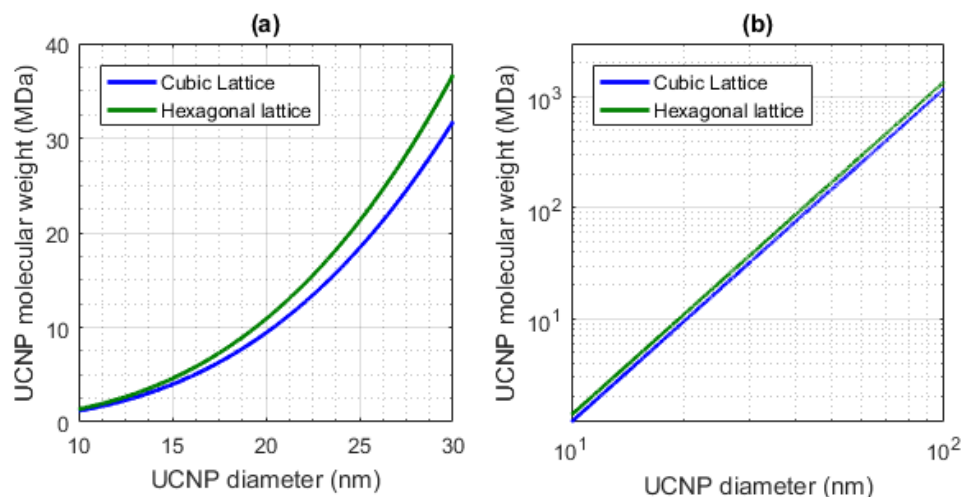
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207 Results

208 Theoretical molecular weight of cubic and hexagonal NaYF₄:RE UCNPs

209 Hexagonal lattice UCNPs have a greater theoretical molecular weight than cubic lattice UCNPs
210 (see Figure 3); this is due to the lower volume of hexagonal unit cells, and correspondingly higher
211 density of hexagonal lattice UCNPs. Additionally, because molecular weight scales to UCNP volume,
212 relatively small changes in UCNP diameter increased molecular weight considerably: e.g. a 20 nm
213 cubic UCNP has a molecular weight of ~10 MDa, whereas a 30 nm UCNP has a molecular weight of
214 > 30 MDa (an increase of 20 MDa for a 5 nm change in UCNP diameter).

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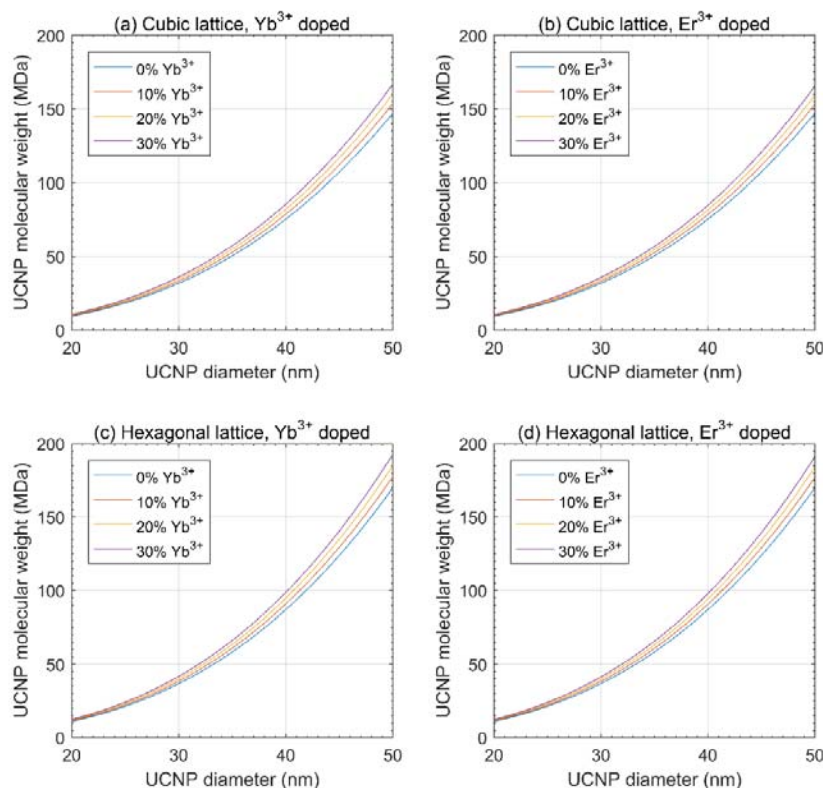
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218 **Figure 3. Diameter versus theoretical molecular weight for hexagonal and cubic**
219 **NaYF₄ UCNPs (green and blue respectively). (a) UCNP diameter vs. molecular**
220 **weight on a standard x-axis. (b) The same data plotted with a logarithmic scale.**
221 Lattice parameters were assumed to be: $a = 5.51 \text{ \AA}$ for cubic UCNPs; $a, c = 5.91 \text{ \AA}$
222 and 3.53 \AA for hexagonal UCNPs.

223

224 The effect of RE doping on UCNP molecular weight

225 Increasing Yb^{3+} or Er^{3+} dopant % increased the theoretical molecular weight of UCNPs (see
226 Figure 4) because Yb^{3+} and Er^{3+} have a greater atomic mass than Y^{3+} . However, the difference in
227 theoretical molecular weight between UCNPs doped with Yb^{3+} and Er^{3+} was relatively small to the
228 small difference between the atomic weight of Yb^{3+} and Er^{3+} (173.054 and 167.259 g/mol
229 respectively, see Table S1). Hexagonal lattice UCNPs show a slightly higher increase in theoretical
230 molecular weight for a given dopant concentration than cubic lattice UCNPs because hexagonal
231 lattice UCNPs have a greater unit cell density compared to their cubic counterparts.



232

233 **Figure 4. The effect of RE doping on theoretical UCNP molecular weight. (a, b)**

234 theoretical molecular weight vs. RE dopant mol% for cubic lattice UCNPs. (c, d)

235 theoretical molecular weight vs. RE dopant mol% for hexagonal lattice UCNPs.

236 Calculations assume that lattice parameters are $a = 5.51 \text{ \AA}$ for cubic lattice UCNPs,

237 $a = 5.91 \text{ \AA}$; $c = 3.53 \text{ \AA}$ for hexagonal lattice UCNPs, and that lattice parameters are

238 independent of dopant mol%.

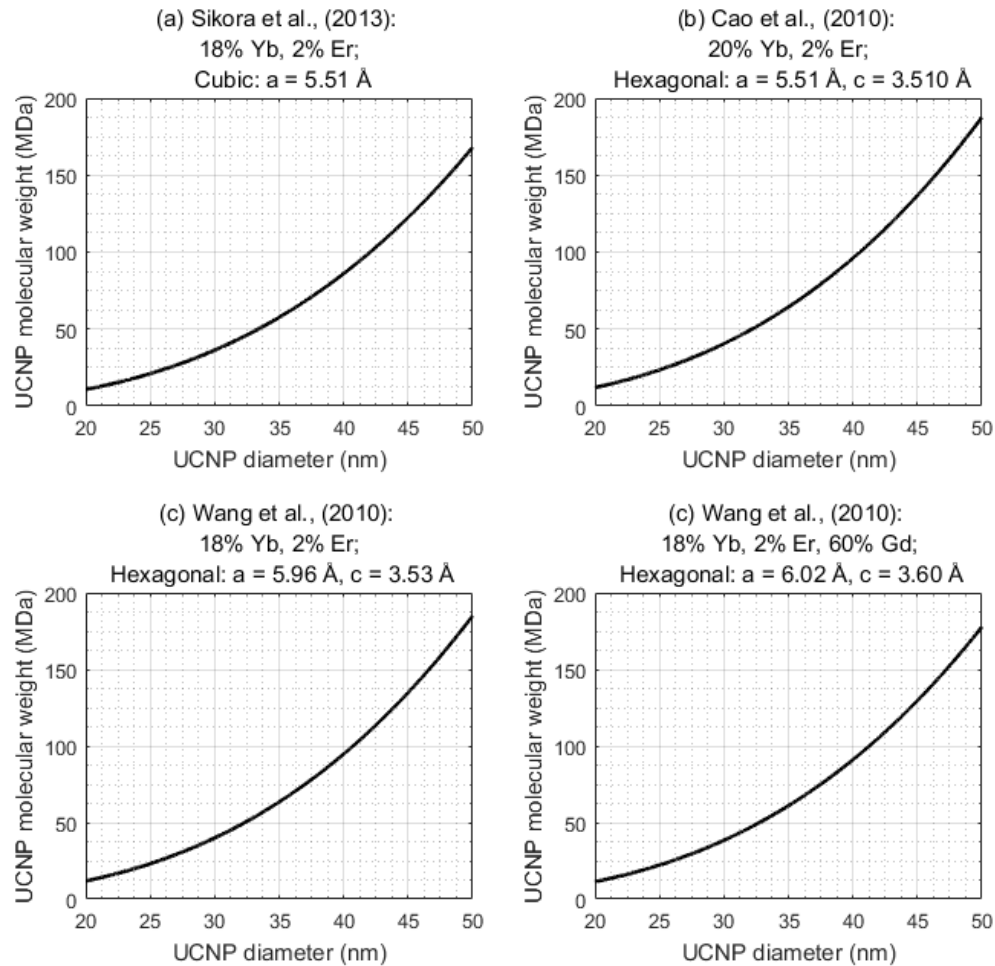
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241 **The theoretical molecular weight of NaYF₄:RE UCNPs reported in the literature**

242 The theoretical molecular weight of various NaYF₄:RE UCNPs reported in the literature are
243 shown in Figure 5.

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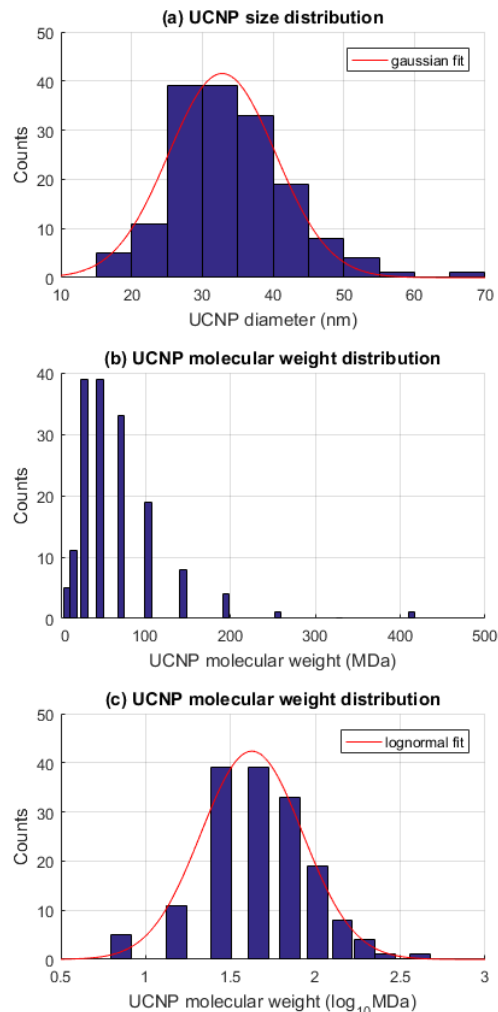
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246 **Figure 5. Theoretical molecular weight of various UCNPs reported in the**
247 **literature. (a) Sikora et al., (2013).¹⁴ (b) Cao et al., (2010).¹⁵ (c, d) Wang et al.,**
248 **(2010).⁴⁰**

249

250 UCNP diameter distribution vs. theoretical molecular weight distribution

251 The UCNP diameter distribution data from Sikora et al., (2013)¹⁴ was well-fitted by a Gaussian
252 distribution ($R^2 = 0.96$) (see Figure 6a). The corresponding theoretical molecular weight distribution
253 (shown in Figure 6b), demonstrates the exponential relation between UCNP diameter and UCNP
254 molecular weight distribution. Plotted on a logarithmic x-axis scale (Figure 6c), the resulting
255 molecular weight distribution was well fitted by a Gaussian distribution ($R^2 = 0.98$), indicating that
256 the molecular weight distribution corresponding to a Gaussian diameter distribution is lognormal.



257

258 Figure 6. Gaussian UCNP diameter distributions give rise to lognormal

259 distribution of theoretical molecular weights. (a) A Gaussian diameter distribution

260 of UCNPs is well described by a normal distribution ($R^2 = 0.96$). (b) The

261 corresponding theoretical molecular weight distribution of UCNPs on a linear

262 molecular weight scale. (c) The molecular weight distribution on a logarithmic x-axis

263 is well fitted by a lognormal distribution ($R^2 = 0.98$).

264 Discussion

265 We have provided a theory to estimate the molecular weight of UCNPs. Our theory is required
266 because, to the best of our knowledge, there are no experimental techniques measuring the
267 molecular weight of UCNPs, which we predict will be > 5 MDa for UCNPs ~15 nm in diameter, and
268 100 MDa for UCNPs ~45 nm in diameter. Mass spectrometry is limited to molecules < 40 kDa, and
269 svAUC is limited to measurements of macromolecules < 5 MDa.³⁴ Our theory predicts that UCNPs
270 with a molecular weight of < 5 MDa would be < 15 nm in diameter. To the best of our knowledge
271 monodisperse synthesis of such small UCNPs has not been reported in the literature.

272

273 Despite the aforementioned challenges of experimental verification, we attempted svAUC
274 measurements of UCNPs, because successful svAUC studies of other types of nanoparticles (e.g.
275 SiO₂ nanoparticles) with unknown molecular weight have been reported.^{45,46} If accurate svAUC
276 measurements of UCNPs could be made, then UCNP molecular weight could potentially be
277 calculated by the theory described by Carney et al., (2011),³⁴ which is based upon accurate
278 quantification of sedimentation and diffusion coefficients from svAUC measurements, and which
279 has been verified for gold nanoparticles ~2 MDa in molecular weight. The full details of the method
280 of our svAUC experiment are provided in the supplementary information. However, our svAUC
281 experiment studying UCNPs was not successful. In brief, our svAUC results showed that the UCNPs
282 (diameter = 32 ± 5 nm, average theoretical molecular weight of ~ 43 MDa) sedimented very rapidly,
283 even at low centrifuge rotor speeds (3,000 rpm), limiting the amount of useable data. At higher
284 rotor speeds UCNPs sedimented too rapidly for data collection. When the recovered sedimentation
285 coefficient was extrapolated to zero sample concentration, a negative sedimentation coefficient
286 was returned. Additionally, UCNPs were observed to diffuse considerably, further complicating AUC
287 experiments. This unusual behaviour is not typical of the nanoclusters and gold nanoparticles used
288 to demonstrated the molecular weight estimation technique described by Carney et al., (2011),³⁴
289 and as such UCNP molecular weight could not be estimated by svAUC. The challenges associated
290 with svAUC measurement of UCNPs serve to further highlight the need for a method to estimate
291 the molecular weight of UCNPs theoretically.

292

293 Although it has not been possible for us to experimentally validate our estimates of UCNP
294 molecular weight, it may be possible in future to verify some limited predictions of our theory. For
295 example, it may be possible to measure the difference in bulk densities of cubic and hexagonal
296 UCNPs and compare this with predictions from our theory. However, we could not attempt this

297 measurement because we did not have access to the high temperature crucible equipment
298 required for hexagonal UCNP synthesis.⁴⁰

299

300 Despite this lack of current and direct experimental verification, we can be reasonably confident
301 in the accuracy of our theory because it stems directly from the theory of crystallography, which
302 has been a subject of intense study in the past century,⁴⁷ combined with empirical measurements
303 of UCNP crystal structure.

304

305 Our method to calculate the theoretical molecular weight of NaYF₄:RE UCNPs relies on two basic
306 assumptions: 1. that UCNPs are crystals of homogenous elemental composition and unit cell phase,
307 and 2. that the lattice parameters and diameter data utilized is accurate. These assumptions can be
308 verified by TEM and XRD measurements of UCNP crystal structure. Ensuring accurate lattice
309 parameters is particularly important when estimating the molecular weight of UCNPs with
310 arbitrarily large dopant concentrations. For example, Wang et al., (2010)⁴⁰ experimentally
311 demonstrated that by doping a hexagonal phase NaYF₄:Yb,Er UCNP (18% Yb, 2% Er) with increasing
312 concentrations of Gd³⁺ increases the lattice parameters of the UCNP significantly, resulting in an
313 increased unit cell volume. Thus, because of this dependence of lattice parameter on RE dopant
314 percentage, our estimations of UCNP molecular weight in Figure 3 may be an over-estimation on
315 true values if lattice parameters are not independently verified for each RE dopant concentration
316 of interest. UCNP volume/morphology also influences theoretical UCNP molecular weight. We
317 recommend using TEM to directly quantify UCNP morphology with limited assumptions. Other
318 techniques such as such as dynamic light scattering (DLS) and nanoparticle tracking analysis can be
319 used to estimate the equivalent hydrodynamic radius of nanoparticles but incorporate various
320 assumptions into calculations.^{46,48} As such, direct TEM imaging of UCNPs is preferable to ensure
321 theoretical molecular weight is as accurate as possible. In this study we assumed UCNPs are
322 perfectly spherical, but our method could be trivially adapted for arbitrary nanoparticle
323 geometries; e.g. rods,^{40,49} triangular,⁵⁰ or prism-shaped⁵¹ nanoparticles, and for nanoparticles of
324 varying crystalline composition. The extension of our technique to arbitrary geometries, arbitrary
325 crystal lattice parameters, and arbitrary elemental composition is demonstrated by the
326 development and application of an advanced GUI incorporating all of these variables (see Figure
327 S2). Our theory does not account for any dislocations in the regular UCNP crystal structure. Instead
328 we assume the influence of any such dislocations to be negligible compared to the molecular
329 weight of whole UCNPs. Our theory also does not account for any surface functionalisation with
330 amorphous layers or other molecules. Thus the molecular weight of UCNPs modified by addition of

331 a silica^{8,35,52} or calcium fluoride⁵³ shell coating will be greater than the theoretical molecular weight
332 estimated by our technique.

333

334 It should be noted that a simple theory for estimation of the molecular weight of a single
335 homogenous gold nanoparticle based upon bulk density of materials was proposed by Lewis et al.
336 (2006).⁵⁴ However, this simple theory did not account for crystalline unit cell parameters or
337 elemental doping. Further, their theory was not extended to describe the molecular weight
338 distributions of a population of nanoparticles. Our results demonstrate that a Gaussian distribution
339 of UCNP diameters corresponds to a lognormal distribution in molecular weight (as shown in Figure
340 6). Mathematically, it is reasonable to expect similar logarithmic relations between UCNP diameter
341 and molecular weight for arbitrary diameter distributions. Such molecular weight distributions may
342 of consequence when studying behaviour of UCNP populations, because minor outliers in UCNP
343 diameter will be extreme outliers in terms of molecular weight.

344

345 Estimation of molecular weight of NaYF₄:RE UCNPs will likely be of utility in various applications,
346 particularly in biomedical imaging, biosensing, and therapeutics. Knowledge of UCNP molecular
347 weight will likely be of great utility in studies where UCNP surfaces are functionalised with
348 additional molecules, e.g. antibodies^{6-8,25} or oligonucleotides,³³ because if the molecular weight of
349 UCNPs is known, then the molar concentrations of substances in the functionalisation processes
350 can be determined. When combined with estimation of UCNP surface area, this could inform the
351 UCNP functionalisation for biosensing applications. Knowledge of UCNP molecular weight would
352 also be beneficial in the processing of particles for downstream applications. In particular, steps
353 taken to functionalise the nanoparticles may require separation procedures to remove unreacted
354 moieties or unwanted reactants. If the molecular weight of UCNPs were known, then it may be
355 beneficial for the optimisation of conjugation stoichiometry, which can be concentration
356 dependant; the reaction rates of UCNPs will be heavily influenced by their molecular weight; thus a
357 greater understanding of their molecular weight may increase the knowledge of thermodynamic
358 properties of UCNP systems. This is particularly important when considering the use of bio-
359 receptors with UCNPs where the mass of the particle may affect the binding kinetics of the UCNP-
360 receptor construct.

361 The molecular weight of UCNPs will also be of interest in the study of cytotoxicity, bio-
362 distribution, cellular uptake, metabolism, and excretion of UCNPs in biological systems.^{12,14}
363 Currently, it is extremely challenging to compare the results from various imaging and therapeutic
364 studies because UCNP concentration is reported as weight of UCNPs per volume of aqueous media

365 (i.e. mg/mL or similar).¹² This is a crude measure which does not quantify number of UCNPs in a
366 given sample. For example, nanoparticles can induce membrane damage⁵⁵ and initiate apoptosis
367 (programmed cell-death).^{56,57} Reporting the molar concentration of UCNPs would help assessment
368 of UCNP cytotoxic effects. A standardised protocol based on molecular weight of UCNPs would help
369 assessment of accumulation of UCNPs *in vivo* and their clearance time from organs¹³ or tumours.⁵³
370 Reporting the molar concentration of UCNP composites may also help to develop highly-localised
371 targeted delivery of therapeutic drugs to the required sites in the body, leading to better controlled
372 targeted photodynamic therapy,²⁷ and potential improvements in targeted drug delivery.¹⁶

373 Conclusions

374 We have provided a method to estimate the theoretical molecular weight of UCNPs. This theory
375 is based upon UCNP crystal parameters which can be measured for batches of UCNPs by TEM and
376 XRD techniques. The theory presented here is generalizable to other crystalline nanoparticles
377 where the relevant crystalline lattice parameters are known, i.e. nanoparticle unit cell elemental
378 composition, unit cell size parameters, and nanoparticle morphology. To enhance dissemination of
379 our theory we provide two stand-alone GUIs for calculation of the molecular weight of both UCNPs
380 and arbitrary crystalline nanoparticles respectively. We could not, however, experimentally verify
381 our predictions of UCNP molecular weight with mass spectrometry or *svAUC*. We did attempt
382 *svAUC* experiments but could not recover reliable *svAUC* data because UCNPs were observed to
383 sediment and diffuse rapidly. Nevertheless, our theory provides some key predications about the
384 molecular weight of UCNPs. Firstly, that the theoretical molecular weight of UCNPs scales with
385 volume of the nanoparticle. As an example, we predict that a spherical UCNP ~10 nm diameter will
386 have a molecular weight of ~1 MDa (10^6 g/mol), whereas a UCNP ~ 45 nm in diameter will be ~100
387 MDa (10^8 g/mol). From this relation, we find that a Gaussian distribution of nanoparticle diameters
388 corresponds to a lognormal distribution of UCNPs molecular weights, and that a small change in
389 UCNP diameter distribution can potentially represent a large change in overall UCNP molecular
390 weight. We also report that Hexagonal crystal lattice phase UCNPs will be of greater molecular
391 weight than cubic lattice phase UCNPs, and that increasing RE dopant % will increase UCNP
392 molecular weight.

393 We expect that the knowledge of UCNP molecular weight will be of utility in a wide variety of
394 biomedical applications, as UCNP concentrations can now be reported in terms of molarity or
395 absolute number of UCNPs instead of the relatively crude measure of sample weight. This will likely
396 aid inter-study comparison of both UCNP dosage and improve methods for creating UCNP
397 biosensors.

398

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541

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556 **Competing financial interest statement**

557 The authors declare no competing financial interests

558 **Author contributions statement**

- 559 • L.E.M and J.A.G. conceived the research concept and wrote the manuscript.
- 560 • L.E.M. performed all calculations, provided Figures 2, 3, 4, 5, 6, and created the stand-alone
561 GUIs.
- 562 • J.A.G. provided Figure 1.
- 563 • A.V, P.P.N, S.S, G.J., and P.M, contributed to and reviewed the manuscript.