Goodman and Feldman

RESEARCH

Evolution of Hierarchy in Bacterial Metabolic Networks

Aaron Goodman and Marcus Feldman*

1

*Correspondence:

mfeldman@stanford.edu Department of Biology, Stanford University, Stanford, CA, 94305, USA

Full list of author information is available at the end of the article

Abstract

Background: In self-organized systems, the concept of flow hierarchy is a useful way to characterize the movement of information throughout a network. Hierarchical network organizations are shown to arise when there is a cost of maintaining links in the network. A similar constraint exists in metabolic networks, where costs come from reduced efficiency of nonspecific enzymes or from producing unnecessary enzymes. Previous analyses of bacterial metabolic networks have been used to predict the minimal nutrients that a bacterium needs to grow, its mutualistic relationships with other bacteria, and its major ecological niche. Using flow hierarchy, we can also infer the tradeoffs between growth rate and metabolic efficiency that bacteria make given their environmental constraints.

Results: Using a comparative approach on 2,935 bacterial metabolic networks, we show that flow hierarchy in bacterial metabolic networks tracks a fundamental tradeoff between growth rate and biomass production, and reflects a bacterium's realized ecological strategy. Additionally, by inferring the ancestral metabolic networks, we find that hierarchy decreases with distance from the root of the tree, suggesting the important pressure of increased growth rate relative to efficiency in the face of competition.

Conclusions: Just as hierarchical character is an important structural property in efficiently engineered systems, it also evolves in self-organized bacterial metabolic networks, reflects the life-history strategies of those bacteria, and plays an important role in network organization and efficiency.

Keywords: modularity; hierarchy; metabolism; bacteria; reverse ecology

Goodman and Feldman

Page 2 of 15

Background

In characterizing bacteria, we seek to understand both their internal processes and how they interact with other species and their environments. Techniques in cell and molecular biology have been very helpful in revealing the inner workings of bacteria, but do not address the ecological context in which bacteria develop and live.
Increasingly, metagenomic techniques are being used to simultaneously sequence all of the bacteria present in a given environment. However, these techniques can only provide limited information about particular species, where they are found, their relative abundances, and co-occurrence patterns.

By studying the structure and evolution of a bacterium's metabolic network, we 12 can move beyond correlational profiles to understand both the underlying pressures 13 that have driven its evolution as well as the ecological role it occupies. A bacterium's 14 ability to reproduce depends on the efficiency of its metabolism, which we can 15 study as a network of metabolites linked together by the enzymes that transform 16 one metabolite into another [1]. The structure of these networks varies across the 17 bacterial kingdom and reflects the environmental pressures that guide bacterial 18 evolution. Thus, a bacterium's metabolic network can be used to predict the minimal 19 nutrients that it needs to grow, its mutualistic relationships with other bacteria, and 20 its major ecological niche [2][3][4]. In describing metabolic networks, two types of 21 hierarchies can be helpful: flow hierarchy and containment hierarchy. 22

Previous study of the hierarchical nature of metabolic networks has tended to 23 focus on containment hierarchy, which represents the nodes in a network as being 24 contained within modules, which themselves are contained within other modules, 25 and so on, in a recursive fashion. For example, a containment hierarchy may be used 26 to represent the organization of a firm, with divisions, departments, teams and in-27 dividual employees. Applied to metabolic networks, such modules correspond to 28 known pathways [11][12], and modular hierarchy has been hypothesized to increase 29 evolvability of metabolism [13]. Simulations of Boolean logic networks have sug-30 gested that modularity evolves in changing environments, and it has been hypothe-31 sized that this would be reflected in bacterial metabolic networks [14][15]. However 32 this has not been borne out [16]; differences in modularity of metabolic networks 33 have been found to be moderately correlated with the phylogenetic divergence of 34

Goodman and Feldman

Page 3 of 15

³⁵ the organisms, and there is a general trend of loss of modularity over evolutionary

 $_{36}$ time due to the addition of peripheral pathways during niche specialization [17].

In this work, we focus on the heretofore neglected type of hierarchy: flow hierarchy. 37 While containment hierarchy represents the organization of a network as a series 38 of modules, flow hierarchy characterizes the way information moves throughout the 30 network. Information is acquired at the lowest level of the hierarchy and transmitted 40 to higher levels, where it is aggregated and passed upward; at the same time orders 41 come from the top of the hierarchical network and are passed down to lower levels. 42 Flow hierarchy is used to describe networks in many fields, particularly in the 43 study of information accrual networks. In engineering, information accrual networks 44 are used in the design of control systems, and in the social sciences, they are used to 45 study the organization of firms [5][6]. To use the example of the firm, flow hierarchy could be used to represent the movement of orders and responsibilities throughout 47 the firm, as low-level employees report upwards to supervisors who aggregate reports 48 for department heads and so on, while orders flow downward from decision makers 49 to executors. As bacteria synthesize the complex molecules needed for survival, they 50 reduce the overall entropy within the cell. Given the thermodynamic equivalence of 51 entropy reduction and information accrual, this reduction can also be viewed as an 52 increase of information. Thus we can use the metabolic network graph to study the 53 flow of information through the cell. 54

Although flow hierarchy (hereafter referred to as hierarchy) has not been well stud-55 ied in metabolic networks, it has been identified in a variety of other self-organized 56 networks, including food webs, neural networks, and the transcription factor net-57 work in *D. melanogaster*, where the degrees of hierarchy were significantly higher 58 than would be expected in a random network with the same degree distribution [7]. 59 In studying hierarchy in metabolic networks, we are able not only to learn that 60 hierarchy appears higher than would be expected by a random configuration, but 61 also to assess adaptive benefits that hierarchy provides. 62

These findings show that hierarchy is common among self-organized networks, but they do not explain when hierarchical network organization would provide a selective advantage. A number of comparative approaches have been used to make inferences about the forces guiding the development of networks in other disciplines, and from them we can deduce some of the adaptive benefits that hierarchy

Goodman and Feldman

Page 4 of 15

provides. Simulated evolution experiments of Boolean logic networks have shown 68 that the cost of maintaining links between nodes is the driving force in the emer-69 gence of hierarchy [19]. Hierarchical characteristics have also been shown to predict 70 the costs of maintaining information-sharing relationships in emergent social net-71 works and reflect the degree of market variability that supply chains may be able to 72 withstand [21]. We know that bacterial metabolic networks face similar constraints. 73 Maintaining catalytic abilities between metabolites incurs a cost either as a trade-74 off between specificity and efficiency, or from production and replication of unused 75 enzymes [20][22]. We show that the strength of these constraints is correlated with 76 degree of hierarchy in metabolic networks. 77

To measure flow hierarchy quantitatively, researchers commonly use the global 78 reaching centrality (GRC), defined as the average difference between the maximum 79 local reaching centrality (i.e. fraction of nodes in the network accessible by each node 80 of the network) and the local reaching centrality [23]. In essence, GRC is a measure 81 of heterogeneity in the flow of information throughout a network. For example, a 82 dictatorial firm where the boss exerts great influence over the entire company while 83 individual employees have little sway would have a higher GRC than a consulting 84 firm run by a group of partners, each of whom oversees a small group of highly 85 collaborative employees. Other, less widely used measures of flow hierarchy are an 86 eigenvector centrality based method, the fraction of edges participating in cycles, 87 or by decomposition into treeness, feedfowardness, and orderability [7][8][9]. 88

Studying the evolution of containment hierarchy can tell us about the environ-89 mental contingencies that inform the evolution of metabolic networks (e.g. resource 90 availability, temperature, environmental variation, etc). However, by studying flow 91 hierarchy we can also infer the different growth strategies a bacterium may pursue, 92 furthering our understanding of how it fills its ecological niche [13]. We employ 93 the reverse ecology principle to understand how the hierarchical character of a 94 metabolic network reflects the life-history strategy of a bacterium in relationship to 95 the growth-yield tradeoff, as well as its environmental niche. As bacteria first adapt 96 to new habitats they may develop novel metabolic functions, leading to an increase 97 in hierarchy, since the new metabolic functions are added to the periphery of the 98 network.

Goodman and Feldman

Page 5 of 15

As those ecosystems evolve, however, some bacteria may adopt higher-growth 100 rate strategies in response to increased competition, at the expense of efficiency 101 and consequently metabolic network hierarchy. Since only some bacteria adopt such 102 high-growth rate strategies, while others maintain higher degrees of hierarchy and 103 efficiency, variance in hierarchy increases overall. Though both hierarchy and mod-104 ularity correlate with bacterial specialization, we find that, contrary to the Boolean 105 network simulations, there is little evolutionary relationship between the two, and 106 that there is more conservation of hierarchy than modularity over time. 107

108

Results and Discussion

110 Networks

Networks were reconstructed from 2,935 bacteria species in the KEGG database. These networks were robust to misannotation of enzymes. In random perturbations of the metabolic network for *E. coli* with 10% of the reactions removed, 95% the networks had hierarchy scores within 12% of the true network, and with 10% of reactions reversed, within 6% of the true network.

Network sizes ranged from 76 to 1496 metabolites, with a mean of 848. The
smallest was the obligate insect parasite Nasuia deltocephalinicola and the largest
was the soil bacterium Burkholderia lata.

119 Hierarchy

Hierarchy scores for the metabolic networks were calculated using the GRC hierar-120 chy score [23]. The mean degree of hierarchy was 0.279, and ranged from 0.065, for 121 the insect symbiote Candidatus Nasuia deltocephalinicola, to 0.385 for a Blattabac-122 terium endosymbiont of Nauphoeta cinerea, an insect endosymbiote. The hierarchy 123 score for *E. coli* strains was 0.269 (Figure 1). For comparison with a random net-124 work and real world networks, GRC hierarchy scores for an Erdős-Rényi random 125 graph is 0.058, a scale-free network 0.127, and a tree 0.997, an estuary food web 126 0.814, and the neuronal network of C. elegans [23]. 127

¹²⁸ Relationship to environment and growth rate

¹²⁹ There is a fundamental ecological trade off between growth rate and yield, which is a

¹³⁰ result of the underlying efficiencies of the reactions. Bacteria that have a metabolism

Goodman and Feldman

Page 6 of 15

that produces the maximal growth rate per amount of carbon taken up will have

¹³² suboptimal biomass production, and vice versa.

This tradeoff is representative of fundamentally divergent ecological strategies that 133 bacteria use [24]. Furthermore, the tradeoffs between growth and yield are repre-134 sented in the constraints on the metabolic network, such that high-yield strategies 135 lead to more hierarchical networks. There is a tradeoff between enzyme specificity 136 and efficiency, so when yield is favored there will be higher costs of maintaining 137 edges in the network, which leads to hierarchy [25] [20]. Rapidly growing bacte-138 ria have more metabolic cycles which allow for metabolic flexibility at the cost of 139 wasted energy, and these cycles decrease hierarchy [26]. The cost of maintaining 140 unused enzymes in the genome is higher when efficiency is paramount [22]. 141

Using a dataset of 111 bacteria with known growth rates, we see that the hier-142 archical character of the network correlates inversely with growth rate, Spearman 143 $\rho = -0.31$, p < 0.0007, fig 2. Furthermore, there is evidence that carbon efficiency 144 constraints on bacteria differs greatly by environment, and that the evolutionary dy-145 namics of carbon usage niche specialization are stronger within populations [27][28]. 146 When we control for the bacterial environment, we see a correlation of $\rho = -0.41$, 147 which is significantly greater than 0 (p < 0.0001, and significantly greater than the 148 correlation when not controlling for the environment p < 0.003). Bacteria with hier-149 archy score greater than the median hierarchy score grow at a rate of 0.64 doublings 150 per hour, compared to 1.44 doublings per hour for bacteria with hierarchy score less 151 than the median, *i.e.* bacteria with the less hierarchical metabolic networks grow 152 2.25 times faster than those with more hierarchical networks (p < 0.0002). 153

Thus the hierarchical character of the metabolic networks reflects the growth rate of the organisms and their environmental niche. These constraints of edge weight and tradeoffs between hierachical and ahierachical networks in metabolism are similar to those made in social networks and supply chains [20] [21].

¹⁵⁸ Relationship to other network properties

In addition to measuring hierarchy, we evaluated a number of other network statistics. We computed node count, edge count, modularity (as evaluated by the Girvan-Newman algorithm [29]), clustering coefficient, full diameter, effective diameter, number of strongly connected components, proportion of the nodes in the largest

Goodman and Feldman

Page 7 of 15

strongly connected component, and Luo Hierarchy score, an alternative metric of 163 hierarchy that measures the proportion of edges that do not participate in any cy-164 cles. Edge and node count correlated most strongly with genetic distance. However, 165 after these basic structural properties, the statistics that correlated most highly 166 with genetic distance were the Girvan-Newman modularity score and the GRC hi-167 erarchy score (Table 1). We also computed the partial correlation for each variable 168 with genetic distance, controlling for the others, and found that the GRC metric 169 had the highest partial correlation. 170

¹⁷¹ Hierarchy Over Time

The hierarchy of the KEGG bacteria and reconstructed ancestors seems to first increase, and then decrease with distance from the root of the tree (Figure 3). Interestingly, with the dataset of 2,935 from the latest KEGG database, the correlation of modularity and distance from the root of the tree found by Kreimer *et al.* [17] is actually reversed. Modularity appears to increase rather than decrease with distance from the root, (Figure 4). This correlation remains positive when restricting analysis to the species used by Kreimer *et al.*.

As bacteria specialize to niches in a given ecosystem, they take on different 179 metabolic strategies, which are reflected in the hierarchical profile of the metabolic 180 network. This difference in strategies is consistent with the rise and fall of hierarchy 181 over the evolutionary trajectory. As microbes first adapt to new environments or 182 habitats (niche sensu Grinnell) they must gain novel metabolic functions, which are 183 added as pathways in the periphery in the network and which increases the hier-184 archical character [30]. As complex relationships develop within the habitats, and 185 bacteria adapt to different resource use profiles and competitive strategies (niche 186 sensu Elton), the hierarchical profile of the metabolic network diversifies. Thus, the 187 decrease in hierarchy over evolutionary time is caused by more bacteria specializing 188 in a rapid-growth strategy, but the increasing variance in hierarchy reflects the fact 189 that not all bacteria adopt this strategy. In studying the adaptive strategies chosen 190 by different bacteria, we may be able to make inferences about the bacteria and 191 their environments, as well as the interplay between evolutionary and ecological 192 dynamics. 193

Goodman and Feldman

Page 8 of 15

¹⁹⁴ Correlation of Modularity and Hierarchy

Hierarchy and modularity are global properties of metabolic networks. Both cor-195 relate with bacterial specialization and both change with distance from the root 196 of the phylogenetic tree. Using the method of phylogenetic independent contrasts 197 to look for correlation independent of phylogenetic structure, we found a mod-198 erate inverse correlation between modularity and hierarchy (Pearson correlation 199 $r = -0.18, p < 10^{-15}$), suggesting little evolutionary relationship between modu-200 larity and hierarchy [31]. Interestingly, simulated Boolean networks demonstrate a 201 positive correlation between modularity and hierarchy [19]. 202

203 Conclusion

Characterizing the hierarchical structure of metabolic networks is useful in un-204 derstanding the constraints under which these networks evolve. Hierarchy corre-205 lates with phylogenetic divergence, as would be expected for a trait subject to 206 natural selection. This correlation is similar to the correlation of phylogenetic dis-207 tance and modularity, suggesting that the hierarchical organization of networks, 208 like modular organization, is important for function. However, modularity should 209 be viewed as complementary to, rather than supplanted by, hierarchy when analyz-210 ing the global organization of metabolic networks. Both structural properties are 211 conserved across phylogenies and evolve together. A better understanding of the 212 character of metabolic networks is valuable in the growing field of 'reverse ecol-213 ogy,' in which the observed networks can be used to make inferences on possible 214 environments [2][32][33]. 215

By algorithmically reconstructing the metabolic networks, we are able to perform a larger-scale analysis than has previously been reported. Although the reaction annotations in KEGG may be prone to errors or omissions, we find that the GRC hierarchy metric is robust to small amounts of reaction omissions or reversals. By expanding the scope of the analysis, we find that modularity is actually inversely correlated with distance from the root of the tree, contrary to what has been found in previous studies of a more limited set of bacteria.

From reconstructed ancestral metabolic networks, we are able to infer how hierarchy evolves in networks over time, and understand the interplay between evolutionary and ecological dynamics. Hierarchy shows an increase followed by a decrease

Goodman and Feldman

Page 9 of 15

- across the phylogenetic tree, which is reflective of the adaptive process of bacteria,
- ²²⁷ first to novel fundamental niches, and then to a realized niche. The net trend in
- decreasing hierarchy reflects a dominance of fast-growth, low-efficiency strategy.

229 Methods

230 Hierarchy Metric

Hierarchy scores were calculated using the global reaching centrality metric devel-231 oped by Mones *et al.*, which is based on the local reaching centrality [23]. The 232 local reaching centrality (LRC) of a node in a network is the fraction of the nodes 233 of the network that can be reached starting at the focal node. More precisely, if 234 the metabolic network is represented as a graph, G = (V, E) it can be said that v 235 reaches v' if there exists a series of edges $(v, v_i), (v_i, v_j)...(v_j, v') \in E$. Let R(v) be 236 the set of nodes $v' \in V$ where v' is reachable from v. Then the LRC of v is $\frac{|R(v)|-1}{|V|-1}$. 237 The GRC is then $\frac{1}{|V|-1} \sum_{v \in V} \max_{v' \in V} \operatorname{LRC}(v') - LRC(v)$ 238

239 Modularity Metric

The modularity metric was calculated using the SNAP package [34]. The modularity 240 of a network is the optimal partitioning of the nodes into clusters to maximize 24 $Q = \frac{1}{4m} \sum_{ij} \left(A_{ij} - \frac{k_i k_j}{2m} I_{ij} \right)$. Where *m* is the number of edges in the network, A_{ij} 242 is the adjacency matrix, i.e. A_{ij} is 1 if there is an enzyme that converts metabolite 243 i into metabolite j. k_i is the number of reactions that metabolite i participates in, 244 and $I_{ij} = 1$ if i and j are in the same module, and -1 otherwise. Since finding the 245 global optimal of Q is an NP-hard problem, we use the method developed by Girvan 246 and Newman, which partitions the network by iteratively removing the edge with 247 the highest betweenness centrality [29]. 248

249 Robustness of Reconstruction

The KEGG database is large, with heavy manual curation; however, this does not mean that the data are always perfect. A reaction may be favorable in one direction in a model organism in laboratory conditions, but might proceed in the opposite direction or become bidirectional in different environments or species. It is also possible that reactions are missing from the database, or that an enzyme placed in an orthology group based on the study of one species may catalyze a different reaction in other species. To evaluate robustness to errors in the KEGG database,

Goodman and Feldman

Page 10 of 15

- ²⁵⁷ we examined the network for the well-studied bacterium, *E. coli*. We performed 100
- $_{258}$ replicates dropping or reversing 10% of the reactions, evaluated the hierarchy scores
- ²⁵⁹ of these networks, and calculated the spread of the central 95% of hierarchy scores.

260 Reconstruction of Genetic Distance

Following the methods often used in bacterial comparative genomics [35][3][36], for each of the 2,935 species, the 16s ribosomal sequence from KEGG was aligned to the Greenegenes database using PyNast, resulting in multiple sequence alignments for the 2,935 species [37][38]. The genetic distances between all pairs of bacterial species were computed using the Kimura distance metric [39].

266 Reconstruction of Networks

For each bacterial species, a network of metabolites was inferred based on the en-267 zymes present in the genome, the reactions known to be catalyzed by the enzymes 268 present or orthologous enzymes, and a database of reaction substrates and prod-269 ucts. The KEGG database of the genomic content of the 2,935 bacterial genomes 270 was used to identify which enzyme classes were present in each genome and which re-271 actions were present [40]. The reaction information from KEGG was supplemented 272 by a the bioreaction database from Stelzer *et al.* which excludes currency metabo-273 lites, improves on predictions of directionality of reactions, and, for reactions with 274 multiple substrates and products, provides carbon tracking of which substrates are 275 converted to which products [41]. Using this reaction information, networks were 276 constructed with metabolites as nodes, and a directed edge was placed between 277 metabolites if there was a reaction that converted one metabolite to another. If re-278 actions were reversible, then bi-directional edges were added between the substrates 279 and products. 280

281 Ancestral Networks

To construct the ancestral networks, a phylogenetic tree was reconstructed using RAxML 8.2.9 and the 16-state GTR nucleotide substitution model with gamma rate heterogeneity [42]. The branch-length weighted average bootstrap support of the partitions over 300 trees was 85.4. Using the maximum likelihood estimate of the best tree, at each interior node of the phylogenetic tree, a genome was constructed using the Fitch small parsimony algorithm. In cases where the presence or absence

Goodman and Feldman

Page 11 of 15

- of a gene was equally parsimonious, the gene was randomly selected to be included.
- ²⁸⁹ These ancestral genomes were then used to reconstruct ancestral networks, just as
- ²⁹⁰ the networks were constructed on the leaves of the tree.

²⁹¹ Niche strategies

Growth rate data for 113 bacterial species and environmental annotations for those 292 bacteria, which for 68 species were gathered from NCBI, and manual curation fol-293 lowing literature review was used for the remaining $45 \ [43][4]$. Due to their low 294 number, the two aquatic species in the data set were excluded from further anal-295 ysis. Correlations were calculated as Spearman's ρ . To calculate correlation con-296 trolling for environment, ρ was calculated within each environment, and a species 29 weighted-average across environments was computed. Due to several bacteria hav-298 ing the same growth rates, p-values were calculated using permutation tests rather 299 than the Student's t-distribution approximation. Significance tests were performed 300 with 100,000 permutations each. For the overall ρ , permutations were done across 301 all bacteria. To test the strength of the habitat-controlled correlation, growth rates 302 were permuted within habitat classes and the species-weighted ρ was computed for 303 each permutation. To test the effect of controlling for the environment, habitat la-304 bels were permuted and the difference between the species weighted ρ and overall 305 ρ was computed. 306

307 Consent to Publish

308 All authors have approved this manuscript for submission. This work has not been published or submitted elsewhere.

- 309 Competing interests
- 310 The authors declare that they have no competing interests.

311 Author Contributions

- 312 AG designed the experiment, carried out the analysis, and wrote the paper. MF provided critical guidence on the
- 313 direction of the work, and revision of the manuscript.

314 Availability of the Data

- The dataset supporting the conclusions of this article, specifically the reconstructed metabolic network
- 316 (Supplementary File 1) and topological statistics (Supplementary File 2) of these networks, are included within the
- 317 article (and its additional files)

318 Acknowledgments

- 319 We are grateful to B Callahan, E Borenstein and J Leskovec for helpful feedback with this work, and to editor Richard
- 320 Goldstein and two anonymous reviewers for there insightful comments

1. Ma, H., Zeng, A.-p.: Reconstruction of metabolic networks from genome data and analysis of their global

Goodman and Feldman

322

Page 12 of 15

321	References
321	References

323		structure for various organisms. Bioinformatics 19(2), 270–277 (2003)
324	2.	Borenstein, E., Kupiec, M., Feldman, M.W., Ruppin, E.: Large-scale reconstruction and phylogenetic analysis of
325		metabolic environments. Proceedings of the National Academy of Sciences of the United States of America
326		105(38), 14482-7 (2008). doi:10.1073/pnas.0806162105
327	3.	Levy, R., Borenstein, E.: Metabolic modeling of species interaction in the human microbiome elucidates
328		community-level assembly rules. Proceedings of the National Academy of Sciences 110(31), 12804–12809
329		(2013). doi:10.1073/pnas.1300926110
330	4.	Freilich, S., Kreimer, A., Borenstein, E., Yosef, N., Sharan, R., Gophna, U., Ruppin, E.:
331		Metabolic-network-driven analysis of bacterial ecological strategies. Genome biology $10(6)$, 61 (2009).
332		doi:10.1186/gb-2009-10-6-r61
333	5.	Brooks, R.: A robust layered control system for a mobile robot. IEEE Journal on Robotics and Automation
334		2(1), 14-23 (1986). doi:10.1109/JRA.1986.1087032. 1010.0034
335	6.	Teece, D.J.: Firm organization, industrial structure, and technological innovation. Journal of Economic
336		Behavior & Organization 31 (2), 193–224 (1996). doi:10.1016/S0167-2681(96)00895-5
337	7.	Luo, J., Magee, C.: Detecting evolving patterns of selforganizing networks by flow hierarchy measurement.
338		Complexity (2011)
339	8.	Czégel, D., Palla, G.: Random walk hierarchy measure: What is more hierarchical, a chain, a tree or a star?
340		Scientific Reports 5(December), 17994 (2015). doi:10.1038/srep17994. arXiv:1508.07732v1
341	9.	Corominas-Murtra, B., Goñi, J., Solé, R.V., Rodríguez-Caso, C.: On the origins of hierarchy in complex
342		networks. Proceedings of the National Academy of Sciences of the United States of America $110(33)$,
343		13316–21 (2013). doi:10.1073/pnas.1300832110. 1303.2503
344	10.	Lorenz, D.M., Jeng, A., Deem, M.W.: The emergence of modularity in biological systems. Physics of Life
345		Reviews 8(2), 129–160 (2011). doi:10.1016/j.plrev.2011.02.003. 1204.5999
346	11.	Ravasz, E., Somera, A.L., Mongru, D.A., Oltvai, Z.N.: Hierarchical Organization of Modularity in Metabolic
347		Networks 297 (August), 1551–1555 (2002)
348	12.	Sales-Pardo, M., Guimerà, R., Moreira, A.A., Amaral, L.A.N.: Extracting the hierarchical organization of
349		complex systems. Proceedings of the National Academy of Sciences of the United States of America $104(39)$,
350		15224–15229 (2007). doi:10.1073/pnas.0703740104. 0705.1679
351	13.	Braakman, R., Smith, E.: The compositional and evolutionary logic of metabolism. Physical biology ${f 10}(1),$
352		011001 (2013). doi:10.1088/1478-3975/10/1/011001. 1207.5532
353	14.	Kashtan, N., Alon, U.: Spontaneous evolution of modularity and network motifs. Proceedings of the National
354		Academy of Sciences of the United States of America 102(39), 13773-13778 (2005).
355		doi:10.1073/pnas.0503610102
356	15.	Parter, M., Kashtan, N., Alon, U.: Environmental variability and modularity of bacterial metabolic networks.
357		BMC evolutionary biology 7, 169 (2007). doi:10.1186/1471-2148-7-169
358	16.	Takemoto, K.: Does Habitat Variability Really Promote Metabolic Network Modularity? PLoS ONE 8(4), 2–10
359		(2013). doi:10.1371/journal.pone.0061348
360	17.	Kreimer, A., Borenstein, E., Gophna, U., Ruppin, E.: The evolution of modularity in bacterial metabolic
361		networks. Proceedings of the National Academy of Sciences of the United States of America $105(19)$, 6976–81
362		(2008). doi:10.1073/pnas.0712149105
363	18.	Muchnik, L., Itzhack, R., Solomon, S., Louzoun, Y.: Self-emergence of knowledge trees: Extraction of the
364		Wikipedia hierarchies. Physical Review E 76(1), 016106 (2007). doi:10.1103/PhysRevE.76.016106
365	19.	Clune, J., Mouret, JB., Lipson, H.: The Evolutionary Origins of Hierarchy. PLOS Computational Biology
366		280 (1755), 20122863 (2016). doi:10.1098/rspb.2012.2863. 1207.2743v1
367	20.	Nepusz, T., Vicsek, T.: Hierarchical self-organization of non-cooperating individuals. PLoS ONE 8(12) (2013).
368		doi:10.1371/journal.pone.0081449. 1308.0029
369	21.	Hu, F., Zhao, S., Bing, T., Chang, Y.: Hierarchy in industrial structure: The cases of China and the USA.
370		Physica A: Statistical Mechanics and its Applications 469, 871–882 (2016). doi:10.1016/j.physa.2016.11.083

27. D'Souza, G., Waschina, S., Pande, S., Bohl, K., Kaleta, C., Kost, C.: Less is more: Selective advantages can

Goodman and Feldman

Page 13 of 15

372		explain the prevalent loss of biosynthetic genes in bacteria. Evolution 68 (9), 2559–2570 (2014).
373	00	doi:10.1111/evo.12468
374	23.	Mones, E., Vicsek, L., Vicsek, T.: Hierarchy measure for complex networks. PLoS ONE 7(3), 1–10 (2012).
375	24	doi:10.1371/journal.pone.0033799. 1202.0191
376	24.	Lipson, D.A.: The complex relationship between microbial growth rate and yield and its implications for
377	05	ecosystem processes. Frontiers in Microbiology 6 (JUN), 1–5 (2015). doi:10.3389/fmicb.2015.00615
378	25.	Beardmore, R.E., Gudelj, I., Lipson, D.A., Hurst, L.D.: Metabolic trade-offs and the maintenance of the fittest
379	26	and the flattest. Nature 472 (7343), 342–6 (2011). doi:10.1038/nature09905
380	20.	Russell, J.B., Cook, G.M.: Energetics of bacterial growth: balance of anabolic and catabolic reactions.
381	27	Microbiological reviews 59 (1), 48–62 (1995) Sinsabaugh, R.L., Manzoni, S., Moorhead, D.L., Richter, A.: Carbon use efficiency of microbial communities:
382	21.	
383	20	stoichiometry, methodology and modelling. Ecology Letters 16 (7), 930–939 (2013). doi:10.1111/ele.12113
384	28.	Novak, M., Pfeiffer, T., Lenski, R.E., Sauer, U., Bonhoeffer, S.: Experimental tests for an evolutionary trade-off
385	20	between growth rate and yield in E. coli. The American naturalist 168 (2), 242–51 (2006). doi:10.1086/506527
386	29.	Girvan, M., Newman, M.E.J.: Community structure in social and biological networks. Proceedings of the
387		National Academy of Sciences of the United States of America 99 (12), 7821–7826 (2002).
388	20	doi:10.1073/pnas.122653799.0112110
389	30.	Da Silva, M.R., Ma, H., Zeng, A.P.: Centrality, network capacity, and modularity as parameters to analyze the
390		core-periphery structure in metabolic networks. Proceedings of the IEEE 96 (8), 1411–1420 (2008).
391	21	doi:10.1109/JPROC.2008.925418
392	31.	Felsenstein, J.: Phylogenies and the Comparative Method. The American Naturalist 125 (1), 1–15 (1985).
393	22	doi:10.1086/284325
394	32.	Shapiro, B.J., Polz, M.F.: Ordering microbial diversity into ecologically and genetically cohesive units. Trends in
395	22	Microbiology 22(5), 235–247 (2014). doi:10.1016/j.tim.2014.02.006. NIHMS150003
396	55.	Dekel, E., Mangan, S., Alon, U.: Environmental selection of the feed-forward loop circuit in gene-regulation
397	24	networks. Phys. Biol. Phys. Biol 2(2), 81–81 (2005). doi:10.1088/1478-3975/2/2/001
398	54.	Leskovec, J., Sosič, R.: SNAP: A General-Purpose Network Analysis and Graph-Mining Library. ACM
399	25	Transactions on Intelligent Systems and Technology $8(1)$, 1–20 (2016). doi:10.1145/2898361
400	35.	Chiu, H.C., Levy, R., Borenstein, E.: Emergent Biosynthetic Capacity in Simple Microbial Communities. PLoS
401	26	Computational Biology 10(7) (2014). doi:10.1371/journal.pcbi.1003695
402	50.	Zaneveld, J., Turnbaugh, P.J., Lozupone, C., Ley, R.E., Hamady, M., Gordon, J.I., Knight, R.: Host-bacterial coevolution and the search for new drug targets. Current Opinion in Chemical Biology 12 (1), 109–114 (2008).
403		doi:10.1016/j.cbpa.2008.01.015. NIHMS150003
404 405	37	DeSantis, T.Z., Hugenholtz, P., Larsen, N., Rojas, M., Brodie, E.L., Keller, K., Huber, T., Dalevi, D., Hu, P.,
	51.	Andersen, G.L.: Greengenes, a chimera-checked 16S rRNA gene database and workbench compatible with ARB.
406		Applied and Environmental Microbiology 72 (7), 5069–5072 (2006). doi:10.1128/AEM.03006-05
407	38	Caporaso, J.G., Bittinger, K., Bushman, F.D., Desantis, T.Z., Andersen, G.L., Knight, R.: PyNAST: A flexible
408 409	50.	tool for aligning sequences to a template alignment. Bioinformatics $26(2)$, $266-267$ (2010).
409		doi:10.1093/bioinformatics/btp636
410	30	Kimura, M.: A simple method for estimating evolutionary rates of base substitutions through comparative
412	55.	studies of nucleotide sequences. Journal of Molecular Evolution 16(2), 111–120 (1980).
412		doi:10.1007/BF01731581. arXiv:1011.1669v3
413	40	Ogata, H., Goto, S., Sato, K., Fujibuchi, W., Bono, H., Kanehisa, M.: KEGG: Kyoto encyclopedia of genes and
414	40.	genomes. Nucleic Acids Research 27(1), 29–34 (1999). doi:10.1093/nar/27.1.29
416	41	Stelzer, M., Sun, J., Zeng, AP., Kamphans, T., Fekete, S.P.: An extended bioreaction database that
410	τ1.	significantly improves reconstruction and analysis of genome-scale metabolic networks. Journal of Chemical
417		Information and Modeling 53, 1689–1699 (2013). doi:10.1017/CBO9781107415324.004. arXiv:1011.1669v3
418	42	Stamatakis, A.: RAxML version 8: A tool for phylogenetic analysis and post-analysis of large phylogenies.
419	τ∠.	Bioinformatics 30 (9), 1312–1313 (2014). doi:10.1093/bioinformatics/btu033. bioinformatics/btu033
420	43	Couturier, E., Rocha, E.P.C.: Replication-associated gene dosage effects shape the genomes of fast-growing
421		bacteria but only for transcription and translation genes. Molecular Microbiology 59 (5), 1506–1518 (2006).
744		second second for danserption and dansation genes. Morecular Microbiology 33(3), 1300-1310 (2000).

Goodman and Feldman

Page 14 of 15

423 doi:10.1111/j.1365-2958.2006.05046.x

Goodman and Feldman

Page 15 of 15

	Correlation	Partial Correlation
Node Count	0.26***	0.03***
Edge Count	0.27^{***}	-0.02*
Modularity	0.28^{***}	0.05***
GRC Hierarchy	0.28^{***}	0.17***
Luo Hierarchy	0.22^{***}	-0.06***
Largest SCC Fraction	0.30^{***}	0.12***
Cluster Coefficient	0.13^{***}	0.03***
Full Diameter	0.23^{***}	0.06***
Effective Diameter	0.20^{***}	0.01
SCC Count	0.14^{***}	0.02**
Mean Degree	0.24^{***}	-0.04***

Table 1 Correlation of network statistics with phylogenetic distances, and partial correlation of network statistic with phylogenetic distance, controlling for the other variables. The correlation and partial correlation of GRC Hierarchy metric with genetic distance is higher than all other non-trivial metrics. ***: p value < 0.001, **: p value < 0.01, *: p value < 0.05.

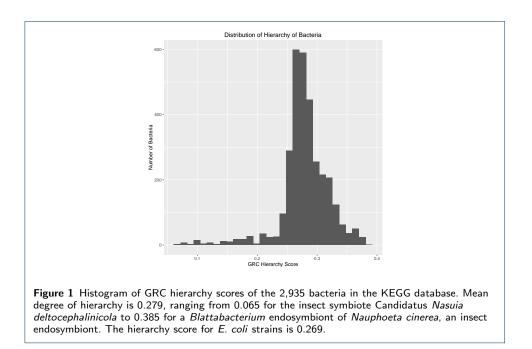
Goodman and Feldman

Page 16 of **15**

424	List o	f Figures	
425	1	Histogram of GRC hierarchy scores of the 2,935 bacteria in the	
426		KEGG database. Mean degree of hierarchy is 0.279, ranging from	
427		0.065 for the insect symbiote Candidatus Nasuia $delto cephalinicola$	
428		to 0.385 for a Blattabacterium endosymbiont of Nauphoeta cinerea,	
429		an insect endosymbiont. The hierarchy score for $E. \ coli$ strains is 0.269.	17
430	2	The relationship between hierarchical character and growth rate re-	
431		flects fundamental tradeoffs between growth and yield and is informa-	
432		tive about the ecological niche the bacteria occupy. Overall, growth	
433		rate is inversely correlated with hierarchy (Spearman's rank correla-	
434		tion, $\rho = -0.31$, $p = 0.00065$). When controlling for bacterial envi-	
435		ronment the trend becomes stronger ($\rho = -0.41, p = 0.0001$). The	
436		outlier in the facultative parasite pane is <i>Borrelia burgdorferi</i> , which	
437		is an obligate parasite that alternates between insect and vertebrate	
438		hosts, and thus is similar to the obligate parasites. The particular	
439		strain also lacks a number of enzymes in its glycolysis pathway that	
440		are present in other <i>B. burgdorferi</i> strains that have hierarchy scores	
441			18
442	3	Hierarchy has a slight overall decrease with phylogenetic distance	
443		(Spearman's rank correlation, $\rho = -0.06, p < 10^{-6}$). Hierarchy ap-	
444		1	19
445	4	Modularity increases with phylogenetic distance (Spearman's rank	•
446		correlation, $\rho = 0.31, p < 10^{-15}$)	20

Goodman and Feldman

Page 17 of 15



Goodman and Feldman

Page 18 of 15

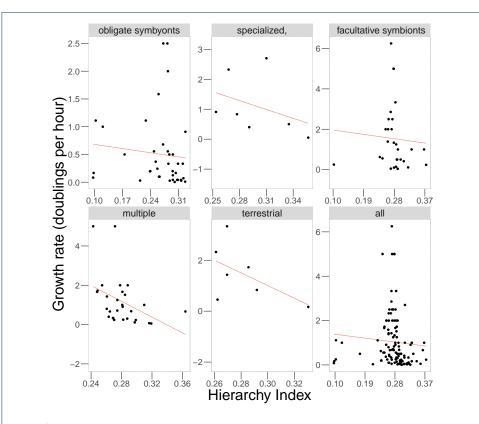
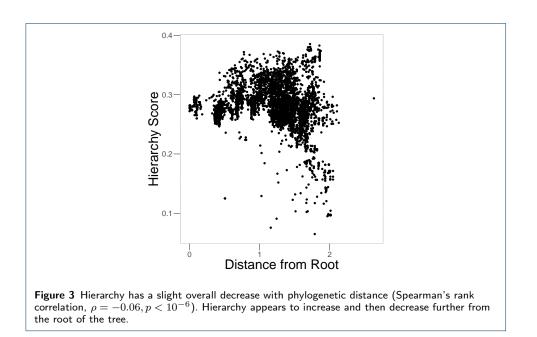


Figure 2 The relationship between hierarchical character and growth rate reflects fundamental tradeoffs between growth and yield and is informative about the ecological niche the bacteria occupy. Overall, growth rate is inversely correlated with hierarchy (Spearman's rank correlation, $\rho = -0.31$, p = 0.00065). When controlling for bacterial environment the trend becomes stronger ($\rho = -0.41$, p = 0.0001). The outlier in the facultative parasite pane is *Borrelia burgdorferi*, which is an obligate parasite that alternates between insect and vertebrate hosts, and thus is similar to the obligate parasites. The particular strain also lacks a number of enzymes in its glycolysis pathway that are present in other *B. burgdorferi* strains that have hierarchy scores of 0.183 ± 0.002 .

Goodman and Feldman



Goodman and Feldman

