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Spike-timing pattern operates as gamma-distribution across cell types, regions and animal species and is essential for naturally-occurring cognitive states

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Abstract

Spike-timing patterns - crucial for synaptic plasticity and neural computation - are often modeled as Poisson-like random processes, log-normal distribution or gamma-distribution patterns, each with different underlying assumptions that may or may not be biologically true. However, it is not entirely clear whether (and how well) these different models would or would not capture spike-timing statistical patterns across different neurons, regions, animal species and cognitive states. Here, we examine statistical patterns of spike-timing irregularity in 13 different cortical and subcortical regions from mouse, hamster, cat and monkey brains. In contrast to the widely-assumed Poisson or log-normal distribution patterns, we show that spike-timing patterns of various projection neurons - including cortical excitatory principal cells, hippocampal pyramidal cells, inhibitory striatal medium spiny neurons and dopaminergic neurons, as well as fast-spiking interneurons – all invariantly conform to the gamma-distribution model. While higher regularity in spike-timing patterns are observed in a few cases, such as mouse DA neurons and monkey motor cortical neurons, there is no clear tendency in increased firing regularity from the sensory and subcortical neurons to prefrontal or motor cortices, as previously entertained. Moreover, gamma shapes of spike-timing patterns remain robust over various natural cognitive states, such as sleep, awake periods, or during fearful episodic experiences. Interestingly, ketamine-induced general anesthesia or unconsciousness is associated with the breakdown of forebrain spike patterns from a singular gamma distribution into two distinct subtypes of gamma distributions, suggesting the importance of this spike-timing pattern in supporting natural cognitive states. These results suggest that gamma-distribution patterns of spike timing reflect not only a fundamental property conserved across different neurons, regions and animal species, but also an operation crucial for supporting natural cognitive states. Such gamma-distribution-based spike-timing patterns can also have important implications for real-time neural coding and realistic neuromorphic computing.

Keywords: spike-timing patterns, gamma distribution, monkey, cat, mouse, spike regularity, ketamine-induced anesthesia.

Introduction

Spike-timing patterns play important roles in synaptic plasticity and neural computation (Gerstner et al., 1996;Markram et al., 1997;deCharms and Zador, 2000;Song et al., 2000;Sjostrom et al., 2001;Lisman and Spruston, 2005). During cognitions and behaviors, neurons discharge their spikes *in vivo* with tremendous variability in both the "control" resting states and across trials within the same experiments in response to identical stimuli (Shadlen and Newsome, 1994;Brown et al., 2004;Faisal et al., 2008). The irregularity of inter-spike intervals has long been suggested to be a fundamental process of cortical communication (Shadlen and Newsome, 1998;deCharms and Zador, 2000;Mazurek and Shadlen, 2002;Ma et al., 2006;Caporale and Dan, 2008;Gilson et al., 2011), and it was often modeled as a Poisson-like random process (Amarasingham et al., 2006;Beck et al., 2008), log-normal distribution (Hromadka et al., 2008;Mizuseki and Buzsaki, 2013a) or gamma distribution (Kuffler et al., 1957;Averbeck, 2009;Maimon and Assad, 2009;Mochizuki et al., 2016), each with a set of assumptions that may or may not be biologically true. A growing number of observations has shown that the neuronal spike pattern in many cortical areas seems to be inconsistent with the Poisson process, indicating that the Poisson process can either underestimate or overestimate the variabilities of neuronal spike patterns (Kara et al., 2000;DeWeese et al., 2003;Lindner, 2006;Heil et al., 2007;Kang et al., 2010;Berkes et al., 2011;Li et al., 2015;Moezzi et al., 2016).

More recently, log-normal distribution has been proposed to account for the variables of synaptic weights, the firing rates of individual neurons, the synchronous discharge of neural populations, the number of synaptic contacts between neurons and the size of dendritic boutons (Buzsaki and Mizuseki, 2014). Given the fact that statistical-

distribution patterns of spike activity play important roles in determining the functions of

neural circuits, it is necessary to determine what actual statistical distributions spike-timing

patterns exhibit across various cell types, circuits and brain states across the evolutionary

spectrum.

In the present study, we set out to investigate whether and how well log-normal

distribution, gamma distribution, and/or Poisson model(s) would capture statistical features

of spike-timing patterns. To maximally ensure that any variation in spike timing was not

due to technical differences in terms of recording methods and/or spike-sorting qualities,

we employed a large-scale *in vivo* tetrode recording in freely-behaving mice and hamsters

to collect neural spike datasets, under similar experimental protocols, from 11 brain regions

(10 mouse brain regions and one hamster brain region), spanning from the prefrontal cortex,

primary visual cortex, somatosensory cortex and auditory cortex to the motor cortex and

limbic systems - such as the hippocampus and amygdala, as well as midbrain dopaminergic

neurons in the ventral tegmental area (VTA). To further expand the brain regions and

animal species, we also analyzed the previously published datasets from the parietal cortex

(parietal 5d) of the monkey brain and the primary visual cortex (V1) of the cat brain as a

way to assess cross-species variability in spike-timing patterns.

Given the existence of distinct cell types in the brain and their possible differences

in spike-timing dynamics, we separated the recorded single units into distinct cell subtypes

- including excitatory cortical cells, CA1 pyramidal cells, inhibitory medium spiny neurons

in the striatum, VTA dopaminergic (DA) neurons and fast-spiking interneurons - before

performing statistical analyses. Finally, we investigated whether such dynamic spike-

timing patterns are varied over different *natural cognitive states*, including sleep, awake-

resting state and during fearful stimulation, as well as pharmacologically-manipulated

unnatural states, such as ketamine-induced general anesthesia – an unconscious state

which differs from the natural unconscious state, namely, sleep.

By systematically comparing three different models (namely, log-normal

distribution, gamma distribution and Poisson) using the datasets collected from the 13 brain

regions surveyed in four different animal species and under multiple different natural or

unnatural brain states, we found that the spike-timing patterns of individual neurons all

invariantly conformed to gamma distribution. This fundamental property is conserved

across different neurons, brain regions and animal species despite large local heterogeneity.

This finding will be valuable to the better examinations of real-time neural code and

modeling of neuromorphic computing.

Results

Statistical properties of neural spike-timing patterns

Spike-timing patterns, as measured by inter-spike-interval (ISI distribution

probability plot), are known to be highly variable across all stages of cognitive states,

including the quiet-awake resting state (for examples, see Figure 1A, Upper Subpanel).   It

is well known that ISI patterns did not follow random Gaussian distribution, but exhibited

a skewed distribution with heavy tails (Figure 1A, Lower Subpanel).   Given that Poisson

model is known to underestimate or overestimate the variabilities of neuronal spike

patterns and belongs to a special case of the gamma-distribution (when shape parameter k

equals to 1), we preceded the assessment of log-normal distribution and gamma distribution

in the term of their effectiveness in capturing the spike-timing dynamics across all spike

datasets. Accordingly, we conducted a two-step analysis on individual neurons' activity patterns by asking two basic questions:

Step 1: Do the neural spike-timing patterns follow a positive-skewed or negative-skewed distribution (Figure 1B)? We characterized the distribution of inter-spike intervals (ISIs) for neural spike patterns by using two well-defined statistics - namely, nonparametric-skew (S) and skewness (γ) (see Materials and Methods). In statistics, these two parameters are measurements of the skewness (or long-tailedness) of a random variable's distribution – that is, the distribution's tendency to lean to one side or the other of the mean (Figure 1B). A positive-skewed distribution (red curve in Figure 1B) has $S > 0$ and $\gamma > 0$, a negative-skewed distribution (blue curve in Figure 1B) has $S < 0$ and $\gamma < 0$, while a symmetric distribution (gray dotted curves in Figure 1B) has $S = 0$ and $\gamma = 0$.

Step 2: Which statistical distribution model is the best to fit the (positive) skewed distribution? As two widely-used distributions for modeling and analyzing non-negative skewed data - namely, the gamma-distribution model and the log-normal distribution model – these models were considered as alternatives for comparison (see Materials and Methods). The gamma distribution and log-normal distribution have been previously applied for modeling firing patterns of neuron population (Mizuseki and Buzsaki, 2013b) and spike patterns of single neurons (Maimon and Assad, 2009;Pipa et al., 2013).

In Figure 1C, the ISI distribution shown in Figure 1A was analyzed here as an illustrative example. It is evident that the gamma-distribution model provided more accurate-fitting results than the log-normal distribution model. It should be noted that, the

parameters of both gamma and log-normal distributions in all datasets were directly

estimated from the raw ISIs of neuronal spike activities by using the maximum likelihood

estimates (MLE) method, which guaranteed that the analyses of ISI distributions were

independent of the bin sizes used for the illustrations of ISI histograms.

We then conducted goodness-of-fit analyses to quantitatively discriminate between

the gamma-distribution model and log-normal distribution model. The ratio of maximized

likelihoods (RML), which is a statistical test used for comparing the goodness-of-fit of two

models (Cox, 1961;1962;2013), was employed for discriminating the gamma-distribution

model and the log-normal distribution model. The natural logarithm of RML, denoted as

D, was calculated as the measurement of the goodness-of-fit (see Materials and Methods).

That is, the gamma-distribution model precedes the log-normal distribution model if $D > 0$;

otherwise, choose the log-normal distribution as the preferred model. The larger the

absolute value of D, the more accurate fitting the result of the chosen model over the other

model.

In the following sections, we conducted this two-step analyses on *in vivo* datasets

of neuronal spike activity recorded from a wide range of cortical and subcortical areas

under one or multiple brain states or experimental conditions in mice, hamsters, cats and

monkeys.

Principal cells exhibited gamma-distribution patterns during the quiet-awake state

We used 128-channel tetrode arrays (Xie et al., 2016) to record neurons from 10

cortical and subcortical regions - namely, anterior cingulate cortex (ACC), retrosplenial

cortex (RSC), somatosensory cortex, ventral tegmental area (VTA), primary visual cortex

(V1), secondary auditory cortex (2nd AuV), dorsal striatum (STR), hippocampal CA1, and

the basolateral amygdala (BLA) - in freely-behaving mice as well as the prelimbic cortex

(PrL), a subdivision of the prefrontal cortex, of freely behaving hamsters. The qualities of

recorded neurons were quantitatively measured by "Isolation Distance" (Schmitzer-

Torbert et al., 2005); neurons whose "Isolation Distance" >15 were selected for the present

analysis. To facilitate direct comparison, we separated putative principal cells from

putative fast-spiking interneurons (see Materials and Methods). In addition, to examine

the state-dependent influence on neuronal variability, we used the spike datasets collected

from the quiet-awake state as animals rested in their home-cage environments. In several

cases, we also collected the datasets in a set of mice when they were subjected to fearful

experiences, such as earthquakes, foot shocks, and free-fall drops.

We first calculated nonparametric-skew (S) and skewness (γ) on putative

principal excitatory cells, illustrated by showing datasets from the following four brain

regions - namely, the ACC (neuron number n=197), the RSC (n=321), the hippocampal

CA1 (n=511) and the BLA (n=451). Our results showed that all the principal cells in these

regions exhibited similar positive-skewed distributions (Figures 2A-D). Skewness (γ) had

a range of 1-10 (ACC = 3.82±0.11, RSC = 2.98±0.07, CA1 = 3.92±0.08, and BLA =

3.55±0.09, data were shown as mean ± SEM). Nonparametric-skew (S) were all in a

range of 0.2-0.5 (ACC = 0.346±0.003, RSC = 0.335±0.001, CA1 = 0.335±0.002 and BLA

= 0.358±0.003, data were shown as mean ± SEM). These results nicely demonstrated that

the neuronal spike patterns in these four brain regions of mice indeed followed positive-

skewed, long-tailed distributions.

We then fitted the spike patterns of each principal cell in these four brain regions

during the quiet-awake state, and estimated their parameters for gamma and log-normal

distributions. To avoid the under sampled error due to few data points, units with <250

ISIs were excluded in the present analysis. The left subpanels of Figures 3A-D showed

fitted gamma and log-normal distributions of example principal cells for these four regions.

D (the natural logarithm of RML) was calculated for the fitted gamma and log-normal

distributions for each of the principal cells in the four brain regions. As shown in the right

subpanels of Figures 3A-D, $D > 0$ was observed for all these principal excitatory cells in

the four regions, demonstrating that the gamma distribution consistently outperformed on

fitting neuronal spike ISIs over the log-normal distribution. We noted that the mean firing

rates and D were highly correlated in all four regions (the correlation coefficients were:

0.80 of the ACC, 0.89 of the RSC, 0.83 of the CA1 and 0.70 of the BLA).

Principal cells exhibited gamma-distribution spike-timing patterns during sleep

Since firing patterns could vary significantly under different brain states, we asked

whether the gamma-distribution model can still capture spike-timing patterns in a robust

manner. As such, we compared the gamma distribution and the log-normal distribution in

modeling neuronal activities of principal cells recorded from the same four mice's brain

regions during the animals' sleep. As shown in Figure 4, the gamma-distribution model

outperformed the log-normal distribution model for fitting the putative principal cells

during the animals' sleep ($D > 0$ for all four brain regions). Again, the firing rates of

principal cells in these four regions were also linearly correlated with D under the sleep

state (the correlation coefficients between firing rates and D were: 0.93 of the ACC, 0.71

of the RSC, 0.86 of the CA1, and 0.62 of the BLA).

All of these analyses supported the notion that the positive-skewed distribution of

neuronal spike patterns can be statistically described by the gamma-distribution model in

different cortical and subcortical regions of mice under distinct brain states.

Preserved gamma-distribution patterns across the quiet-awake and sleep states

Since the positive-skewed distribution is the intrinsic characteristic of a neuronal

spike pattern, we asked whether there existed any invariant feature about this positive-

skewed distribution across distinct brain states. Two parameters of the gamma-distribution

model, shape parameter k and scale parameter θ, were measured under two distinct brain

states (the quiet-awake vs. sleep). In the gamma-distribution model, the shape parameter

k describes the overall envelope of an ISI distribution, while the scale parameter θ is

related to the mean firing rate within the uncertain state (the reciprocal of the scale

parameter, $r = 1/\theta$, is known as the rate parameter). The shape parameter k provides

useful measurements for spike dynamics under different cognitive states, with a higher k

indicating more regular spiking discharge patterns and a lower k indicating more irregular

spike activities.

Analyses were compared the patterns of putative principal cell activities in the four

brain regions under both the quiet-awake state and the animals' sleep (34 cells from the

ACC, 102 cells from the RSC, 43 cells from the CA1, and 182 cells from the BLA). The

results showed that the two parameters of the gamma-distribution model were correlated

between awake and sleep states in all four regions (Figure 5, correlation coefficient R

between k_{awake} and k_{sleep} : ACC, R=0.89; RSC, R=0.91; CA1, R=0.94; BLA, R=0.77.

Correlation coefficient R between θ_{awake} and θ_{sleep} : ACC, R=0.81; RSC, R=0.71; CA1,

R=0.79; BLA, R=0.48. Ps <0.0001, t-test).

We further fitted these two parameters with linear functions for visually displaying

the changing trends by the slope of fitted linear dependencies (shown as the red lines and

red numbers in Figure 5). We observed that the transformations of the scale parameter θ

(related to neuron's mean firing rate) between awake and sleep states were varied among

these brain regions. Specifically, the mean firing rates of the principal cells in the ACC

remained unchanged between the two states (in the right subpanel of Figure 5A, the slopes

of fitted linear dependencies was 1.003). The principal cells in the RSC exhibited increased

mean firing rates in the sleep state (in the right subpanel of Figure 5B, the slopes of fitted

linear dependencies was 0.835). On the contrary, as shown in the right subpanels of Figures

5C and D, the slopes of fitted linear dependences of the CA1 and BLA regions were 1.138

and 1.512, respectively, indicating that the mean firing rates of the principal cells in these

two regions decreased in sleep states as compared to awake states.

Comparing the diverse transformations of θ, our analyses showed that the shape

parameter k of the principal cells in all of these four brain regions was tightly correlated

and highly preserved between the two states (the left subpanels of Figures 5A-D, as denoted

by the slopes of fitted linear dependences of k : ACC, 1.056; RSC, 1.045; CA1, 1.010 and

BLA, 1.027). Given the fact that the shape parameter k is the parameter for characterizing

the overall shape of ISI distribution, our results provided strong evidence for the notion

that the overall shapes of positive-skewed distributions of neuronal firing patterns were

preserved across distinct brain states (sleep vs. awake), which is independent of the changes

in firing rates under different cognitive states.

Striatal medium spiny neurons exhibited gamma distribution in spike timing

Next, we investigated whether the gamma-like spike patterns reflect a general property that would remain true for GABAergic projection neurons. Thus, we employed 128-channel recording techniques and monitored activity patterns from the dorsal striatum of freely-behaving mice in the quiet-awake state. We conducted the same statistical analysis on a dataset of 294 medium spiny projection neurons (see Materials and Methods). Being the principal projection neurons of the striatum, medium spiny projection neuron is a special type of GABAergic inhibitory cells distinct from many other types of local interneurons (Preston et al., 1980;Surmeier et al., 2007).

Figure 6A showed the fitted gamma and log-normal distributions of a sample medium spiny neuron, it was evident that the gamma-distribution model produced a better result for the peak of the ISI distribution. As shown in Figure 6B, skewness $\gamma = 3.77 \pm 0.10$ and nonparametric-skew $S = 0.357 \pm 0.003$ (data were shown as mean ± SEM). These results show that the neuronal spike patterns of medium spiny projection neurons also exhibited positive-skewed, long-tailed distributions. Furthermore, the gamma-distribution model achieved superior performance on fitting neuronal spike patterns of medium spiny projection neurons over the log-normal distribution model ($D > 0$ for all medium spiny projection neurons, Figure 6C).

Spike-timing patterns of fast-spiking interneurons conformed to gamma distribution

To further verify that the gamma-like spike-timing patterns were a universal characteristic of neuronal spike activity, we set out to examine if the neuronal spike patterns of fast-spiking interneurons also followed a gamma distribution. A total of 136 putative fast-spiking interneurons recorded from four mice brain regions (36 from the ACC, 31 from

the BLA, 32 from the hippocampal CA1, and 37 from the RSC) were analyzed. As shown

in Figures 7A and B, the neuronal spike patterns of interneurons also exhibited positive-

skewed, long-tailed distributions ($\gamma = 4.68 \pm 0.24$, $S = 0.327 \pm 0.004$, mean ± SEM). The

goodness-of-fit analysis showed that the spike patterns of all these interneurons followed

the gamma-distribution models (Figure 7C, $D > 0$ for all these interneurons, the

correlation coefficient between D and mean firing rates was 0.75).

Dopaminergic neurons exhibited gamma-distribution spike-timing patterns

To further evaluate the general utility of the gamma-distribution model for different

cell types, we then analyzed dopaminergic (DA) neurons from the mouse VTA region. The

DA neuron dataset was collected from freely-behaving mice during the awake period using

32- or 64-channel tetrodes as we have previously described (Wang and Tsien, 2011;Li et

al., 2015). DA neurons, which project over long distances to various cortical and

subcortical sites (Swanson, 1982;Lammel et al., 2011;Beier et al., 2015), are well-known

to subserve a wide range of biological functions, such as motivation and reward (Wise,

2004;Everitt and Robbins, 2005;Bromberg-Martin et al., 2010;Schultz, 2013), addiction

(Grace, 2000;Berridge et al., 2009), fear memory and behaviors (Pezze and Feldon,

2004;Fadok et al., 2009;Wang and Tsien, 2011;Abraham et al., 2014).

We analyzed a total of 84 well-identified DA neurons, as illustrated in Figure 8A.

We found that the ISI distribution of VTA DA neurons can be better characterized by the

gamma distribution. Skewness ($\gamma = 2.57 \pm 0.21$, mean ± SEM) and nonparametric-skew

($S = 0.263 \pm 0.010$, mean ± SEM) demonstrated that the neuronal spike patterns of VTA

DA neurons followed positive-skewed distributions with heavy tails (Figure 8B). Again,

the gamma-distribution model outperformed the log-normal distribution model for fitting

the neuronal spike patterns of VTA DA neurons ($D > 0$ for all VTA DA neurons, as shown

in Figure 8C). And the firing rates were linearly correlated with D (the correlation

coefficients between firing rates and D was 0.33).

Principal cells in the hamster prelimbic region also conformed to gamma distribution

To examine the generality of gamma distribution patterns across the evolutionary

spectrum, we asked whether the excitatory units in the prelimbic region (PrL) of Golden

Syrian hamsters would follow the gamma-distribution spike patterns. As described in our

previous study (Xie et al., 2016a), we implanted 64-channel tetrode arrays bilaterally into

the PrL region and recorded neural-activity patterns when animals were in their quiet-

awake states. A total of 200 putative excitatory principal cells recorded from 13 hamsters

were identified as stable and well-isolated units for the analyses.

The gamma and log-normal models of a sample PrL principal cell were shown in

Figure 9A. The spike patterns of these cells exhibited clearly positive-skewed, heavy-

tailed distributions (Figure 9B, $\gamma = 3.78 \pm 0.12$, $S = 0.341 \pm 0.003$, mean ± SEM). The

goodness-of-fit analysis showed that all PrL excitatory principal cells can be better

described by using the gamma-distribution models (Figure 9C, $D > 0$ for all PrL

excitatory principal cells), and D was linearly correlated with the mean firing rates

(correlation coefficient is 0.79). Together, we showed that these putative principal cells in

the hamster PrL cortex also followed the gamma-distribution spiking patterns.

Spike-timing patterns in the monkey posterior parietal cortex area 5d exhibited gamma distribution

Next, we asked whether spike-timing patterns in primate species also followed the gamma distribution. We analyzed the datasets collected from rhesus monkeys (Li and Cui, 2013). In this study, the single-neuron activities were recorded from the parietal cortex dorsal area 5 (area 5d) on the gyral surface adjacent to the medial bank of the intraparietal sulcus, which is closely linked to movement kinematics (Hamel-Pâquet et al., 2006) and movement preparation (Cui and Andersen, 2011). Briefly, the monkeys were required to touch the fixation center at the trial beginning. Then, the first- and second- reaching goals were simultaneously displayed for 400 ms with a green square and triangle (shifted by 135° counterclockwise from the square), respectively. After a 600 ms delay, the central green dot turned off (GO signal), and the monkeys were allowed to initiate the reaching sequence to touch the locations previously cued by the square and triangle in the correct order. Throughout the trial, the monkeys were either required to maintain eye fixation (fixation condition) at the center or allowed to move their eyes freely (free-view condition). Single-reach trials were pseudo-randomly interleaved with the double-reach trials for control. Here, we analyzed a total of 211 single units and observed that the spike patterns of monkey area 5d neurons also exhibited obvious positive-skewed distributions (Figures 10A and B, $\gamma = 17.81 \pm 1.37$, $S = 0.219 \pm 0.007$, mean ± SEM), and can be best modeled by gamma-distribution (Figure 10C, $D > 0$ for all area 5d neurons, the correlation coefficient between D and mean firing rates was 0.42).

Spike-timing patterns in cat primary visual cortex conformed to gamma distribution

To further investigate the generality of gamma distribution patterns in different

animal species, we analyzed a dataset of extracellular recordings from the primary visual

cortex of anesthetized adult cats that were deposited in the public domain (Dan et al., 2009).

This dataset was originally performed for measuring the spatiotemporal receptive fields of

cortical cells (Touryan et al., 2002;Felsen et al., 2005;Touryan et al., 2005;Dan et al., 2009).

One of two different visual stimuli, either 1-D white noise [473 neurons, 1-D white noise

(random bars) aligned to the preferred orientation of each cell] or 2-D stimuli (202 neurons,

natural images, natural phase and random phase), were delivered to the anesthetized cats.

Thus, this dataset was not only ideal for verifying the gamma-distribution model, but it

also afforded us an opportunity to examine if the gamma-distribution model was robust

under two different types of stimulus conditions.

First, we observed that the spike patterns of the neurons in the primary visual cortex

of cats all followed positive-skewed distribution under 1-D white noise (cat V1: 1-D)

(Figures 11A and C, $\gamma = 2.80 \pm 0.04$, $S = 0.421 \pm 0.004$, mean ± SEM) and 2-D stimuli (cat

V1: 2-D) (Figures 11B and D, $\gamma = 2.81 \pm 0.05$, $S = 0.392 \pm 0.006$, mean ± SEM).

Furthermore, the distributions of γ and S showed no significant differences under these

two distinct types of stimuli ($p > 0.94$, t-test). Second, the goodness-of-fit analysis

demonstrated that the gamma distribution outperformed the log-normal distribution for

characterizing the spike patterns of the primary visual cortex neurons under both 1-D white

noise and 2-D stimuli (Figures 11E and F, the correlation coefficients between D and

mean firing rates were 0.44 for 1-D white noise and 0.41 for 2-D stimuli). These results

demonstrated that spike-timing patterns in the primary visual cortex of cats also followed

the gamma-distribution model. Moreover, overall gamma distribution remained robust

over different stimulus types.

Preserved gamma-distribution spike patterns under fearful episodes

To further examine whether and how well gamma-distribution patterns capture

spike-timing patterns across different brain states, we performed additional set of

experiments under which mice were subjected to fearful stimulation. Specifically, two

datasets were recorded from the ACC and RSC regions when mice experienced three

fearful episodic events, namely, earthquakes, foot shocks and free-fall drops (see Materials

and Methods) as well as during the quiet-awake and sleep states. A total of 95 and 120

principal cells were recorded from the ACC (three mice) and RSC (four mice), respectively.

As shown in Figure 12, the goodness-of-fit analysis confirmed that the spike-timing

patterns followed gamma distribution under these three brain states ($D > 0$).

Furthermore, the firing rates and D were highly linearly correlated in all three

brain states (left subpanels of Figures 12A and B) with D increasing with higher firing

rates (the correlation coefficients between firing rates and D were: 0.94 of the ACC and

0.71 of the RSC for the quiet-awake state; 0.93 of the ACC and 0.71 of the RSC during

sleep; and 0.91 of the ACC and 0.84 of the RSC during the fearful-event experiment).

Interestingly, compared with the quiet-awake state and sleep, the gamma-distribution

model provided even more accurate-fitting results from the stimulated states (as shown by

the gradients of the fitted, linear relationships between firing rates and D, left subpanels

of Figures 12A and B).

We also examined the robustness of the shape parameter k by calculating the

correlations between these three distinct brain states, revealing that the shape parameter k

was preserved not only between the quiet-awake state and sleep but also in behaving

animals experiencing fearful events (right subpanels of Figures 12A and B, the correlation

coefficients were: ACC, 0.83 between the quiet-awake state and sleep, 0.75 between sleep

and the behaving state, and 0.71 between the quiet-awake state and behaving state; RSC,

0.96 between the quiet-awake state and sleep, 0.95 between sleep and the behaving state,

and 0.94 between the quiet-awake state and behaving state).   Thus, our analysis

demonstrated that the spike-timing patterns conformed to gamma distribution with

preserved shape parameter k under both resting states (the quiet-awake and sleep states)

and emotionally activated states (in which fearful experiences were represented).

Regularities of spike-timing patterns across different cells and brain regions

Given the critical roles of regularity or irregularity of spike-timing patterns in

synaptic plasticity and neural computations, we further asked how spike dynamics vary

over a wide range of different brain regions. Therefore, we systematically recorded and

compared the regularities of neuronal spike patterns in a wide range of mouse brain regions.

This includes a total of 10 mouse brain regions as follows: **1)** 84 DA neurons from the

VTA; **2)** 85 excitatory principal cells from the somatosensory cortex; **3)** 615 excitatory

principal cells from the RSC; **4)** 342 excitatory principal cells in the primary visual cortex

(V1); **5)** 325 CA1 pyramidal cells; **6)** 41 excitatory principal cells recorded from the 2nd

AuV, **7)** 56 neurons from the primary motor cortex (M1); **8)** 195 excitatory principal cells

from the ACC; **9)** 263 pyramidal cells in the BLA, and **10)** 221 medium spiny neurons in

the STR. The datasets collected from these 10 mouse brain regions offered a unique

opportunity for cross-region comparisons, because the tetrode recording techniques and

criteria used for spike sorting were from the same laboratory.

Moreover, we analyzed 182 excitatory principal cells from the hamster PrL

obtained in the laboratory; In addition, 475 units in the cat V1 during 1-D white noise and

207 excitatory principal cells from the cat V1 area during 2-D stimuli (from Dan

laboratory), as well as 206 excitatory cells in the monkey brain area 5d (from Cui

laboratory). In addition, GABAergic interneurons recorded from four mouse brain region

(36 interneurons in mouse ACC region, 37 interneurons in mouse RSC region, 32

interneurons in mouse hippocampal CA1 region, and 31 interneurons in mouse BLA region)

were also included in our analysis for systematically comparison of spike-timing

regularities across distinct brain regions as well as different cell types. As a result, the

datasets consisted of a total of 3,378 neurons obtained from 13 brain regions of the four

species (mice, hamsters, cats and monkeys).

We compared the regularities of neuronal spike patterns in these brain regions by

examining the shape parameters k of their gamma distribution patterns. Based on its

definition, k provides an effective way to measure neuronal spike patterns' regularities. A

gamma distribution with $k=1$ is the mathematical equivalent to an exponential distribution,

the corresponding neuronal spike pattern fits a Poisson process (shown as the gray

horizontal line in Figure 13). Neuronal spike patterns with $k<1$ indicate that the neuron

discharges more frequently in short and long intervals than the exponential distribution –

namely, irregular spiking. When $k>1$, the peaks of ISI distributions shift away from zero,

and the neuron discharges more regular spiking than the Poisson process. Gamma

distribution with $k = \infty$ is the distribution of no variance, and the corresponding neuronal

spike pattern is perfectly regular.

We grouped these neurons according to their general anatomical locations and cell

types, namely, seneory cortices (mouse V1, cat V1, mouse RSC, mouse somatosensory,

and mouse 2nd AuV), prefrontal cortices (mouse ACC and hamster PrL), motor cortices

(mouse M1 and monkey 5d), limbic regions (mouse BLA and mouse CA1), DA neurons

(mouse VTA), and GABAergic neurons (mouse STR, interneurons in mouse ACC, BLA,

CA1 and RSC).

As shown in Figure 13, we observed that the neuronal spike patterns in most brain

regions exhibited more irregular spiking than the Poisson process (k : 0.844±0.015 in

mouse V1, 0.530±0.007 in Cat V1: 1-D, 0.636±0.013 in Cat V1: 2-D, 0.921±0.008 in

mouse RSC, 0.719±0.040 in mouse 2nd AuV, 0.689±0.015 in mouse ACC, 0.793±0.018 in

hamster PrL, 0.791±0.033 in mouse M1, 0.632±0.013 in mouse BLA, 0.825±0.010 in

mouse CA1, 0.601±0.014 in mouse STR, 0.921±0.032 of interneurons in mouse ACC,

0.749±0.061 of interneurons in mouse BLA, and 0.804±0.029 of interneurons in mouse

hippocampal CA1, data were shown as mean ± SEM).

We also noted that neurons in the other three brain regions seemed to discharge

more regular spikes than the Poisson process (k : 1.240±0.039 in the mouse somatosensory

cortex, 1.610±0.055 in the monkey brain motor area 5d, and 1.806±0.104 by DA neurons

from the mouse VTA, data were shown as mean ± SEM). There were significant

differences between three regular-spiking regions in comparison to 15 regions which

showed irregular-spiking ($p < 0.0001$, One-way ANOVA coupled with Tukey's posthoc

test). Overall, there is no obvious tendency in increased firing regularity from the sensory

and subcortical neurons to prefrontal or motor cortices.

Gamma-distribution spike patterns were dramatically altered under anesthesia

If the gamma-distribution spike-timing patterns reflect a fundamental and

conserved property for natural cognitions produced by naturally occurring internal states

and external inputs, we hypothesized that such gamma-distribution spike-timing patterns

would be altered if naturally occurring cognitions were pharmacologically shut down (*i.e.*,

upon anesthesia). Accordingly, we used ketamine/domitor to induce general anesthesia

and compared neuronal spike activities from the BLA, CA1 and RSC regions with those in

the awake states from the same set of mice. We found that ketamine induced rhythmic

spike discharge patterns as well as synchronized local field potential (LFP) oscillation In

all these three brain regions (Figures 14A-C). Most notably, ketamine-induced general

anesthesia produced profound delta band in LFP (Figures 14A-C, middle subpanels). while

the frequencies of the rhythmic spike patterns were different in these brain regions -

specifically, BLA > CA1> RSC, the spike patterns of pyramidal cells in these three regions

during awake periods conformed to the gamma-distribution model (Figures 14A-C).

However, the spike patterns of these pyramidal cells during anesthesia were broken down

from a single gamma distribution (p<1E-5, one-sample Kolmogorov-Smirnov test) into

two distinct subtypes of gamma distributions - as shown in the right subpanels of Figures

14A-C. The gamma shapes of the two subtypes of the distributions revealed that the

Subtype-1 is highly irregular, reflecting bursting firing, whereas the second gamma

distribution subtype showed highly regular, rhythmic spike-timing patterns in the range of

delta frequency. This pharmacologically-based manipulation experiment demonstrated that

the naturally-occurring and ongoing external and internal processes are essential for

generating a singular gamma-distribution spike pattern for various neurons, whereas

ketamine-induced general anesthesia were associated with the breakdown of this singular

distribution pattern into two distinct subtypes of gamma-distribution spiking patterns.

Discussion

Given the critical roles of spiking-timing patterns in synaptic plasticity and neural

coding, it is important to understand the statistical patterns in spike-discharge dynamics in

a brain-wide manner, as well as across multiple mammalian species. Although researchers

have extensively modeled spike-timing patterns over decades of research, only several

studies have compared spike regularity or irregularity over multiple brain subregions

and/or animal species (Maimon and Assad, 2009;Mochizuki et al., 2016). One major

caveat of any comparative experiment is that datasets were collected using rather different

recording methods and with or without stringent spike-sorting criteria, leading to variations

that may affect the outcome.   To circumvent or minimize such technical variability, we

have employed large-scale tetrode recording techniques and recorded from a total of 10

brain regions from mice and one region from hamsters using the same procedures and

similar experimental protocols. These datasets were further compared with additional

datasets from two brain regions of cats and monkeys that were collected by other

laboratories. This systematic analysis of a wider range of brain regions, behavioral states,

cell types and animal species has produced several important insights that are revealing to

us.

First, the gamma distribution consistently outperforms Poisson distribution or log-

normal distribution models across all datasets. Throughout the literature, spike patterns

were often modeled with three different methods - namely, gamma distribution (Kuffler et

al., 1957;Averbeck, 2009;Maimon and Assad, 2009;Mochizuki et al., 2016), log-normal

distribution (Hromadka et al., 2008;Mizuseki and Buzsaki, 2013a) and Poisson-distribution

process (Amarasingham et al., 2006;Beck et al., 2008), respectively. Because three

statistical models have made different assumptions with underlying biological meaning

that may or may not be true, it would be important to assess the statistical patterns over a

wide range of cell types, regions, brain states and animal species, which have not been

performed until now. We found that the neuronal spike-timing patterns have all conformed

to gamma distributions.

In our analyses, we showed that Poisson process can only account for very small

numbers of cells (when shape parameter $k=1$) (see Figure 13), a special case of the gamma-

distribution. This is consistent with the notion that the Poisson model can either

underestimate or overestimate the variabilities of neuronal spike patterns (Kara et al., 2000;

DeWeese et al., 2003; Lindner, 2006; Heil et al., 2007; Kang et al., 2010; Berkes et al.,

2011; Li et al., 2015; Moezzi et al., 2016). According to the independent spike hypothesis

that the generation of each spike is independent of all the other spikes, the neuronal spike

train would be completely described as a particular kind of random process called the

Poisson process. If the Poisson process holds true for neuronal spike-activity patterns, ISI

distribution would be statistically described by the exponential-distribution model.

However, there are certain important features of neuronal firing that may render this

simplistic assumption unsatisfactory or inaccurate for capturing spike-time patterns. In

fact, burst-firing and the refractory periods after the generation of spikes can make neuronal

spike patterns deviate away from a Poisson process (exponential-distribution model). We

showed that the neuronal spike-timing patterns were best captured by gamma distributions.

Recently, log-normal distribution has been proposed to account for many variables

of brain parameters (e.g., firing-rate distributions of neurons, the number of synaptic

contacts between neurons, and the size of dendritic boutons), which had a positive-skewed,

long-tailed distribution (Mizuseki and Buzsaki, 2013; Buzsaki and Mizuseki, 2014).

Quantifications of cortical principal neurons have shown that the mean firing rates of

individual neurons can span at least four orders of magnitude and that the firing-rate

distribution of both stimulus-evoked and spontaneous activity in cortical neurons fit well

with the log-normal distribution model. While our results support the notion that spike-

timing patterns of single neurons followed a positive-skewed distribution, we found that

the gamma-distribution model has consistently offered more precise fitting to the spike-

timing patterns from all these brain regions, cell types, animal species and brain states.

Second, assessing from 13 different brain regions, we noted that there is the lack of

a clear trend in increased regularity from primary sensory to higher cortical or motor

cortical areas, as two previous studies had indicated (Maimon and Assad, 2009;Mochizuki

et al., 2016). While our analysis of the parietal cortex dorsal area 5 (area 5d) in the monkey

brain indeed found these motor-related neurons exhibited higher regularity, we showed that

the mouse M1 cortex seemed to have similar irregular firing patterns in comparison to the

mouse V1, auditory cortex, and RSC - as well as the prefrontal cortices, such as the PrL

and ACC. The fact that we confirmed more regular firing in monkey 5d datasets from Cui

laboratory argue against the idea that the discrepancy was simply due to different recording

and analysis techniques. One possible explanation for this discrepancy between monkey

parietal cortex area 5d and mouse M1 cortex is the difference in how the datasets were

collected under different training conditions. In monkey, spike datasets were typically

collected after monkeys were subjected to extensive behavioral training over many weeks

and months, whereas our M1 datasets from mice were collected from naïve mice which

were not subjected to any particular motor tasks. In fact, past studies have reported that

cortical neurons, including M1 neurons, can generate spike trains with high irregularity

(bursting) (Mountcastle et al., 1969;Bair and Koch, 1996;Buracas et al., 1998;Masse and

Cook, 2008). Thus, trial conditions (such as oscillatory stimulus presentation or rhythmic

motor actions) and extensive training of animals (over weeks and months) on motor tasks

may influence spiking dynamics via experience-dependent plasticity and learning

experience.

Among cells exhibiting higher firing regularity, we noted that DA neurons in the

VTA and excitatory principal cells from the somatosensory cortex of the mouse brain

belonged to this list. Tonic firing of DA neurons with their unique synaptic and cellular

machinery can contribute to this unique pattern. We and other laboratories have reported

different subtypes of DA neurons (Wang and Tsien, 2011), it will be interesting to further

analyze how subtype DA neurons differ in their spike-timing patterns in future experiments.

We found that principal neurons in the mouse and cat V1 cortex – such as principal

excitatory cells from the mouse retrosplenial cortex, secondary auditory cortex, anterior

cingulate cortex, basolateral amygdala and hippocampal CA1 pyramidal cells – as well as

inhibitory projection cells of striatum and fast-spike putative local interneurons, all tend to

exhibit greater irregularity, a property likely due to different burst-firing dynamics of these

neurons. It is noteworthy that current classification of cell types were based on waveforms and/or firing rates. More sophisticated classification will be necessary for future analyses. It is known that even within CA1 pyramidal cells, they may contain distinct subtype cells with a different burst index (Mizuseki et al., 2011; Li et al., 2015), a feature that can affect spike-time irregularity.

Third, by taking advantage of recorded spike datasets collected from the same animals under different cognitive states, we have examined the question of how different brain states influence the overall statistical patterns of spike-timing dynamics. Accordingly, we have verified that the spike-timing patterns conformed to gamma distribution under the quiet-awake and sleep states. One may argue that the spike-timing patterns during these brain states could be represented or dominated by "noise." Therefore, it would be important to exclude such a possibility by using spike datasets from animals during more active states. By performing fearful stimulation experiments, we showed that gamma-distribution spike patterns not only continued to remain robust, but also the gamma-distribution model provided even more accurate-fitting results in comparison to awake resting or sleep states.

It should be noted that despite neurons' mean firing rates varied between distinct natural states (i.e., sleep vs. awake resting period) (shown by the scale parameter θ in the right subpanels of Figures 5A-D), the overall shapes of the neuronal spike patterns are preserved across different states (shown by the scale parameter k in the left subpanels of Figures 5A-D). This supports the notion that while distinct brain activity states or inputs may boost or lessen the mean firing rates, the statistical characteristics of spike-timing patterns are able to remain robust and likely reflect preconfigured, skewed synaptic

connections and/or intrinsic electrical/chemical attributes of a neuron. Similarly, the

datasets from the anaesthetized cat V1 under two different visual stimulation conditions

also showed the conserved gamma-distribution patterns. This conserved characteristic

may be useful in term of offering a potential way of estimating a neuron's spike pattern

among distinct states. For example, instead of recording a single neuron's spike train for

a long period to get the statistical distribution of its spike pattern in the awake resting state,

one may predict it by using the shape parameter k calculated under the sleep state and/or

a mean firing rate within a shorter period in the stimulated state, or vice versa.

Fourth, given the widely conserved gamma-distribution spike-timing patterns

across cell types, brain regions and naturally-occurring cognitive states, one may ask how

important this pattern would be. In other words, does the disruption of this conserved

gamma distribution pattern alter brain state and/or cognition? To address this question, we

used ketamine-induced general anesthesia as a way to examine the relationship between

gamma-distribution patterns and cognitions. The main action of ketamine is the blockade

of the NMDA receptors, which is traditionally believed to reduce activation in the thalamo-

cortical structures via blocking the inputs of afferent stimuli and information integration to

the conscious mind (Alkire et al., 2008;Sinner and Graf, 2008). Interestingly, we found

that ketamine turned a singular gamma distribution of spike-time patterns in the BLA, CA1

and RSC cells into two distinct subtypes of gamma distributions (see gamma distributions

1 and 2 in Figure 14). Most notably, subtype-2 gamma distribution showed highly regular

firing patterns, which seem to be associated with the emergence of the delta band

oscillation in simultaneously recorded LFP. Therefore, ketamine-induced unconsciousness

is different from natural unconscious (sleep) states in term of dynamic spike-timing

patterns.

In conclusion, we systematically investigated the statistical patterns of spike-timing

irregularity in 13 different cortical and subcortical regions of mouse, hamster, cat and

monkey brains. By comparing the effectiveness of different models, we show that spike-

timing patterns of various projection neurons - including cortical excitatory principal cells,

hippocampal pyramidal cells, inhibitory striatal medium spiny neurons and dopaminergic

neurons, as well as fast-spiking interneurons – all invariantly conform to the gamma-

distribution model. While higher regularity in spike-timing patterns is observed in a few

cases, such as mouse DA neurons and monkey motor cortical neurons, there is no clear

tendency in increased firing regularity from the sensory and subcortical neurons to

prefrontal or motor cortices. Moreover, gamma shapes of spike-timing patterns remain

robust over various natural brain states - such as sleep, awake resting periods, as well as

during fearful experiences. However, ketamine-induced general anesthesia led to the

breakdown of spike patterns from a singular gamma distribution into two distinct subtypes

of gamma distributions. Taken together, the above results suggest that gamma-distribution

patterns of spike timing reflect not only a fundamental property (Song et al., 2000;Lisman

and Spruston, 2005) conserved across different neurons, regions and animal species, but

also an operation crucial for supporting naturally-occurring cognitive states. Such gamma-

distribution-based, spike-timing patterns may also have important implications for

investigating real-time neural coding (Buzsaki, 2010;Gupta et al., 2010;Xie et al., 2016a)

and perhaps better modeling of neuromorphic computing.

Materials and Methods

Ethics Statement

All animal work described in the study was carried out in accordance with the guidelines laid down by the National Institutes of Health in the United States, regarding the care and use of animals for experimental procedures, and was approved by the Institutional Animal Care and Use Committee of Augusta University (Approval AUP number: BR07-11-001).

Construction of tetrode headstages and animal surgery of the datasets of mouse BLA, CA1, ACC, RSC, STR, V1, 2nd AuV, M1, and somatosensory cortex, and hamster PrL.

Tetrodes and headstages were constructed using the procedures as we have previously described (Lin et al., 2006;Xie et al., 2016a;Xie et al., 2016b). To construct tetrodes, a folded piece consisting of four wires (90% platinum, 10% iridium, 13 μm, California Fine Wire Company, Grover Beach, CA, USA) was twisted together using a manual turning device and soldered with a low-intensity heat source (variable temperature heat gun 8977020, Milwaukee, Brookfield, WI, USA) for six seconds. The impedances of the tetrodes were measured with an electrode impedance tester (Model IMP-1, Bak Electronics, Umatilla, FL, USA) to detect any faulty connections, and our tetrodes were typically between 0.7 MΩ and 1 MΩ. The insulation was removed by moving the tips of the free ends of the tetrodes over an open flame for approximately three seconds. The tetrodes were then placed into appropriate polyimide tubes. The recording ends of the tetrodes were cut differentially (Vannas spring scissors −3 mm cutting edge, Fine Science Tools, Foster City, CA, USA) according to the different depths of the recording sites. This

ensures that only tetrodes, but not the surrounding polyimide tubes, were inserted into the

brain tissue, thereby minimizing the tissue damage.

We employed adjustable 128-channel tetrode microdrives to target the basolateral

amygdala (BLA; n = 8 WT mice), hippocampal CA1 (n = 9 WT mice), anterior cingulate

cortex (ACC; n = 7 WT mice), the retrosplenial cortex (RSC; n = 20 WT mice), dorsal

striatum (STR; n = 7 WT mice), primary visual cortex (V1; n = 14 WT mice), 2nd auditory

cortex (2nd AuV; n = 9 WT mice), somatosensory cortex (n = 11 WT mice), and hamster

prelimbic region (PrL; n = 13 WT Golden Syrian hamsters) bilaterally with 64 channels

per hemisphere (Lin et al., 2006). Stereotaxic coordinates were as follows: for BLA, 1.7

mm posterior to bregma, 3.5 mm lateral, −4.0 mm ventral to the brain surface; for ACC,

+0.5 mm AP, 0.5 mm ML, −1.75 mm DV; or CA1, 2.0 mm lateral to the bregma and 2.3

posteriors to the bregma; for RSC, −2.5 mm AP, 0.5 mm ML, −0.8 mm DV; for STR, +0.62

mm AP, 1.35 mm ML, −2.0 mm DV; for V1, -3.08 mm AP, 2.5 mm ML, −0.5 mm DV;

for 2nd AuV, -1.94 mm AP, 4.75 mm ML; for somatosensory cortex, -1.1 mm AP, 1.5 mm

ML; and for recording in the prelimbic cortex (PrL) of the Golden Syrian hamster, the

stereotaxic coordinate was +3.50 mm AP, ± 0.7 mm ML, −4.0 mm DV (Paxinos and

Franklin, 2004).

Male wild-type mice (6–8 months old) or adult male hamsters (3–4 months old)

were moved from home cages housed in the LAS facility to the holding area next to the

chronic recording rooms in the laboratory and stayed in a large plastic bucket (20 inches in

diameter and 16 inches in height – per mouse, Walmart) with access to water and food for

a week prior to surgery. During this period, the animals were also handled daily to

minimize the potential stress from human interaction. On the day of the surgery, the animal

was given an intraperitoneal injection of 60 mg/kg Ketamine (Bedford Laboratories, Bedford, OH, USA) and 4 mg/kg Domitor (Pfizer, New York, NY, USA) prior to the surgery. The head of the animal was secured in a stereotaxic apparatus, and an ocular lubricant was used to cover the eyes. The hair above the surgery sites was removed, and Betadine solution was applied to the surface of the scalp. An incision was then made along the midline of the skull. Hydrogen peroxide (3% solution, Fisher Scientific) was placed onto the surface of the skull so that bregma could be visualized. The correct positions for implantation were then measured and marked. For fixing the microdrive headstage, four holes for screws (B002SG89S4, Amazon, Seattle, WA, USA) were drilled on the opposing side of the skull and, subsequently, the screws were placed in these holes with reference wires being secured to two of the head screws. Craniotomies for the tetrode arrays were then drilled, and the dura mater was carefully removed. After the electrodes were inserted and tetrodes were secured to the fiberglass base, the reference wires from the connector-pin arrays were soldered such that there would be a continuous circuit between the ground wires from the head screws and those from the connector-pin arrays. Finally, the connector-pin arrays were coated with epoxy. Aluminum foil was used to surround the entire headstage to aid in the protection and to reduce noise during recordings. The animals were then awoken with an injection of 2.5 mg/kg Antisedan. The animals were allowed to recover post-surgery for at least 3–5 days before recording began. Then, the electrode bundles targeting the BLA, STR and hippocampal CA1 region were slowly advanced over several days in small daily increments. For the cortical sites, tetrodes were advanced usually only once or twice in a small increment. At the end of the experiments, the mice were anesthetized, and a small amount of current was applied to the recording electrodes

in order to mark the positions of the stereotrode bundles. The actual electrode positions

were confirmed by histological Nissl staining using 1% cresyl echt violet. In some

experiments, for facilitating the identification of electrode array position, the electrode tips

were dipped in fluorescent Neuro-Dil (Neuro-Dil, #60016, Red oily solid color, from

Biotium, Inc.), which then reveal the electrode track.

Experimental Design

We recorded mouse (B6BCA/J) STR, V1, 2nd AuV, M1, somatosensory cortex,

and hamster PrL when animals were in the quiet-awake state. The datasets of the mouse

(B6BCA/J) ACC, RSC, CA1 and BLA were recorded under two distinct states: the quiet-

awake state and sleep state.

In vivo **recording of the datasets of the mouse BLA, CA1, ACC, RSC, STR, V1, 2nd**

AuV, M1, somatosensory cortex, and hamster PrL

After surgery, the animals were handled for another 5–10 days while electrodes

were advanced to the recording sites for obtaining the maximum neural units.

For the datasets of the mouse STR, 2nd AuV, M1, somatosensory cortex, and

hamster PrL, recordings were carried out while the animals were in their home cages.

Quiet-awake episodes were manually assigned when the mice were awake and immobile.

Neuronal spike data during the awake state was recorded for at least 15 minutes for each

animal.

For the datasets of the mouse ACC, RSC, CA1 and BLA, we recorded the neuronal

spike activity in both the quiet-awake state and the sleep state. Recordings were first

carried out while the animals were in their home cages. To identify the sleep episodes, local

field potentials were first band-pass filtered in theta band (4–12 Hz) and delta band (1–

4 Hz); then the ratio of the power in theta band to that of delta band was calculated. Two

criteria were applied to extract from the sleep state: (1) Duration of an epoch was longer

than five seconds, and (2) the ratio of the power during an epoch was greater than mean

5SD. For each mouse, the awake and sleep states were recorded for at least 15 minutes.

For the dataset of mouse V1, we set up an experimental configuration modified

from the design of a previous study (Niell and Stryker, 2010). Briefly, a treadmill (five

inches in diameter) was levitated by a stream of pressured air, the tangential force of a

mouse running on the treadmill was calculated to be comparable to the force needed for

free running. There was a lick port in front of the mouse's mouth, dropping sugar water

every minute. A camera with a telescope was set at the right side of the mouse eye (8cm

distance) for monitoring eye movement. The mouse has implanted electrode arrays in the

primary visual cortex of the left hemisphere for chronic recording a week before a head-

fixed visual stimulation experiment. For habituation, the mouse was fixed on the top of a

treadmill two hours every day, by mounting the headstage on a metal holder. An optical

mouse was placed underneath the treadmill to measure the animal's movements. During

the recording, the mouse was to either sit still or run on the treadmill. We found that the

eye movement and animal's movement state were highly synchronized; the eyeball was

almost fixed when the mouse was in a still state.

Visual stimuli were generated in MATLAB and displayed on a Dell 24-inch

monitor placed 27 cm in front of the right eye. Before any recordings, we calibrated the

location of the monitor. Specifically, black and white dots with one - four degrees were

randomly presented on the monitor with a 10 ms duration. The visual responses of the

primary visual cortex were amplified, acquired and streamed to the computer by the Plexon

electrophysiology recording system. The time stamps of the visual stimulations were also

sent to the Plexon simultaneously. The receptive field mapping software was written in

MATLAB, which could tag the receptive field of the recorded neurons on the monitor,

based on the e-Phys data. Then we adjusted the location of the monitor to make sure the

neuron group receptive field would be located in the center of the monitor.

Two different visual stimuli were employed in the formal recording: 1. Full-length

drifting bars [combinations of eight orientations ($\pi/8$, $\pi/4$, $\pi3/8$, $\pi/2$, $\pi5/8$, $\pi3/4$, $\pi7/8$ and

π), four spatial frequencies (0.25, 0.5, 1 and 2 Hz), four temporal frequencies (0.25, 0.5, 1

and 2 Hz) and two directions (drifting either left or right)]; and 2. Two-dimensional stimuli

[we recorded 624 gray-scale images of 78 objects (42 toy animals and 36 toy cars), each

object was recorded from eight different viewing directions in a 45º interval]. For each

recording section, one of these three visual stimuli were delivered. At least 30 minutes of

neuronal spike data were recorded during each recording section. Basically, the mice

stayed on the treadmill without struggling for more than two hours, then they were freed

to the home cages.

Cell-type classification in mouse BLA, ACC, RSC, STR, CA1 and hamster PrL

For the datasets recorded from the mouse BLA, ACC, RSC, STR, CA1 and hamster

PrL, well-isolated units were classified as either putative excitatory principal cells or

inhibitory interneurons based on three characteristic features of their spike activities -

namely, trough-to-peak width, half-width after trough, and the mean firing rates. The k-

means method was employed to achieve automated cell-type clustering. In general,

putative principal cells fire at lower rates and have broader waveforms, whereas

interneurons have higher rates and relatively narrower waveforms.

Animal surgery and *in vivo* recording of mouse VTA dataset

The details have been previously described (Wang and Tsien, 2011). A 32-channel

(a bundle of eight tetrodes) electrode array was constructed. One week before surgery,

mice (3–6 months old) were removed from the standard cages and housed in customized

home cages (40×20×25 cm). On the day of surgery, the mice were anesthetized with

Ketamine/Xylazine (80/12 mg/kg, i.p.); the electrode array was then implanted toward the

VTA in the right hemisphere (3.4 mm posterior to bregma, 0.5 mm lateral and 3.8–4.0 mm

ventral to the brain surface) and secured with dental cement.

Two or three days after surgery, the electrodes were screened daily for neural

activity. If no dopamine neurons were detected, the electrode array was advanced 40~100

μm daily, until we could record from a putative dopamine neuron. In brief, spikes (filtered

at 250–8000 Hz; digitized at 40 kHz) were recorded during the entire experimental process

using the Plexon multichannel acquisition processor system (Plexon Inc.). Mice behaviors

were simultaneously recorded using the Plexon CinePlex tracking system. Recorded

spikes were isolated using Plexon Offline Sorter software. Dopamine neurons were

distinguished from other neurons in the region by the characteristics of their extracellularly

recorded impulses - including long, multiphasic waveforms and low basal firing rates.

Fearful-event experiment

Mice were subjected to three fearful episodic events, earthquakes, foot shocks, and

free-fall drops. For the earthquake-like shake, the mouse was placed in a small chamber

(4" x 4" x 6"H circular chamber) fixed on top of a vortex mixer and shaken at 300 rpm for

400ms six times with 1~3-minute time intervals between each shake. For fearful foot shock,

the foot-shock chamber was a square chamber ($10" \times 10" \times 15"H$) with a 24-bar shock grid

floor. The mouse was placed into the shock chamber for three minutes and received the

foot-shock stimulus (a continuous 300-ms foot shock at 0.75 mA) for a total of six times

with inter-trial time interval between 1~3 minutes. For free-fall in the elevator, the animal

was placed inside a small box (3" x 3" x 5"H) and dropped from a 13-cm height (a cushion

which made from a crumbled tablecloth was used to dampen the fall and to stop the

bouncing effect). After 1~2 minutes, the elevator was raised gently back to the 13-cm

height and dropped again after 1~2 minutes (this process was also repeated six times).

These episodic stimuli are fearful as evidenced from physiological indications including a

rapid increase in heart rates as well as reduced heart rate variability (Liu et al., 2013;Liu et

al., 2014). To maintain the consistency of stimulation timing (minimizing the possible

prediction of upcoming stimuli), the stimuli were triggered by a computer and delivered at

randomized intervals within 1-3 minutes. After the completion of all fearful event sessions,

the mouse was placed back into the home cage.

Dataset recorded from the quiet-awake state and anesthesia

Three datasets were recorded from the BLA, hippocampal CA1, and RSC under

two distinct states - namely the quiet-awake state and anesthesia. Recordings were first

carried out when animals were awake and immobile in their home cages. Minimum 40-

minute neural activities were recorded in the quiet-awake state. To produce ketamine-

induced anesthesia, the animals were injected with a 60 mg/kg Ketamine and 0.5 mg/kg

Domitor cocktail mixture via *i.p.*; the animals lost the righting reflex in a few minutes.

Neural spike activities were recorded for 50 minutes under the anesthetized state. Forty-

minute neural spike data recorded from the fully anesthetized state starting from 10 minutes

after the Ketamine/Domitor injections were selected for the present analysis. The dataset

for neuronal variability analyses of awake state vs. anesthesia (Figure 14) contained 92

BLA putative principal cells from two mice, 59 CA1 putative principal cells from three

mice, and 59 RSC putative principal cells from three mice.

Monkey area 5d dataset

The dataset was previously described (Li and Cui, 2013). Data were recorded from

two male rhesus monkeys (Macaca mulatta, 7-10 kg). The animals were trained to perform

visually guided single- and double-arm reaching tasks. All procedures were in accordance

with NIH guidelines and were approved by the Institutional Animal Care and Use

Committee of Augusta University. Recorded spikes were re-sorted using Plexon Offline

Sorter software for obtaining the spike trains of single neurons; multiple spike-sorting

parameters (e.g., principal component analysis, energy analysis) were used for the best

isolation of single-unit spike trains. Because of the absence of the spike waveform

information, we were not able to separate different neuron types (excitatory vs. inhibitory

cells, etc.). However, we observed that the previously-held conclusion that neuronal spike

activities can be best described by the gamma-distribution model still holds true in the

monkey area 5d region.

Cat V1 Datasets

The cat V1 datasets (1-D and 2-D) were downloaded from the Collaborative

Research in Computational Neuroscience (CRCNS) website (data from Yang Dan Lab at

UC-Berkeley,   download   link: http://crcns.org/data-sets/vc/pvc-2).   Experimental

procedures have been previously described (Touryan et al., 2002;Felsen et al.,

2005;Touryan et al., 2005). The data were obtained with extracellular recordings from the

primary visual cortex of anesthetized adult cats. Single-unit recordings were made in area

17 of adult cats (2–6.5 kg) using tungsten electrodes (A-M Systems, Carlsborg, WA).

Animals were initially anesthetized with isoflurane (3%, with O_2) followed by sodium

pentothal (10 mg/kg, i.v., supplemented as needed). During recording, anesthesia was

maintained with sodium pentothal (3 mg $\cdot$ kg^{-1} $\cdot$ hr^{-1}, i.v.), and paralysis was maintained

with pancuronium bromide (0.1–0.2 mg $\cdot$ kg^{-1} $\cdot$ hr^{-1}, i.v.). Because of the absence of the

spike waveform information, we were not able to separate different neuron types

(excitatory vs. inhibitory cells, etc.). However, we observed that the previously-held

conclusion that neuronal spike activities can be best described by the gamma-distribution

model still holds true in the cat V1 region (both 1-D and 2-D stimuli).

Data processing and spike sorting

Neuronal activities from mouse experiments were recorded by the MAP system

(multi-channel acquisition processor system, Plexon Inc., Dallas, TX) in the manner as

previously described (Kuang et al., 2010). Extracellular action potentials and local field

potentials data were recorded simultaneously and digitized at 40 kHz and 1 kHz,

respectively. The artifact waveforms were removed, and the spike waveform minima were

aligned using the Offline Sorter 2.0 software (Plexon Inc., Dallas, TX), which resulted in

more tightly clustered waveforms in principal component space. Spike sortings were done

with the MCLUST 3.3 program with an auto-clustering method (KlustaKwik 1.5). Only

units with clear boundaries and less than 0.5% of spike intervals within a 1 ms refractory

period were selected. The stability of the *in vivo* recordings was judged by waveforms at

the beginning, during and after the experiments. Well-separated neurons were assessed by

"Isolation Distance" (Schmitzer-Torbert et al., 2005). Neurons whose "Isolation

Distance" >15 were selected for the present analysis as previously described (Lin et al.,

2006;Xie et al., 2016a;Xie et al., 2016b).

Statistical Analysis

As shown in Figure 5, a *t*-test was used to assess whether k (or θ) was linearly

correlated between the quiet-awake state and the sleep state. In Figure 11, one-way

ANOVA analysis and Tukey post-hoc tests were conducted for the comparisons of multiple

means of k across different brain regions. Three asterisks denoted the p-value is less than

0.001. Data were represented as mean ± SEM.

Statistical properties of neural spike patterns

A two-step analysis was employed to examine the statistical properties of neural

spike patterns.

Step 1: Positive-skewed vs. negative-skewed distributions. The distribution of ISI

was characterized by two well-defined statistics - namely, nonparametric-skew (S) and

skewness (γ), defined as follows:

873
$$S = \frac{\mu - \upsilon}{\sigma} \tag{1}$$

874
$$\gamma = \mathrm{E}\left[\left(\frac{I - \mu}{\sigma}\right)^3\right] = \frac{\mathrm{E}\left[(I - \mu)^3\right]}{\left(\mathrm{E}\left[(I - \mu)^2\right]\right)^{3/2}} \tag{2}$$

where μ is the mean, υ is the median, σ is the standard deviation, E is the expectation

operator, and I denotes the ISIs of a neuronal spike train.

In probability theory and statistics, nonparametric-skew (S) and skewness

[$\gamma \in (-\infty, +\infty)$] are measurements of the skewness (or long-tailedness) of a random

variable's distribution – that is, the distribution's tendency to lean to one side or the other

of the mean (Figure 1B). A positive-skewed distribution (red curve in Figure 1B) has

$S > 0$ and $\gamma > 0$, a negative-skewed distribution (blue curve in Figure 1B) has $S < 0$ and

$\gamma < 0$, while a symmetric distribution (gray dotted curves in Figure 1B) has $S = 0$ and

$\gamma = 0$.

Step 2: Gamma distribution vs. log-normal distribution. Let $I_1, I_2, \cdots I_n$ denote the

ISIs of a neuron's spike train, the probability density function for a gamma distribution of

I is defined by a shape parameter $k > 0$ and a scale parameter $\theta > 0$:

$$f_{GA}(i; k, \theta) = \frac{1}{\Gamma(k)\theta^k} i^{k-1} e^{-\frac{i}{\theta}} \qquad (3)$$

888 where $\Gamma(k)$ is the gamma function.

889 The probability density function of a log-normal distribution of I is defined by a

890 location parameter $\mu \in (-\infty, +\infty)$ and a scale parameter $\sigma > 0$:

$$f_{LN}(i; \mu, \sigma) = \frac{1}{\sqrt{2\pi} i \sigma} e^{-\frac{(\ln i - \mu)^2}{2\sigma^2}} \qquad (4)$$

In the present analyses, both gamma distribution and log-normal distribution were

estimated using the maximum likelihood estimates (MLE) method, which selected values

of parameters that produced corresponding distributions for the histograms of ISI with

minimal errors. The parameters of both gamma distribution and log-normal distribution

were directly estimated by using the raw ISIs of neuronal spike activities, which ensured

that the analyses of ISI distributions were independent of the bin sizes used.

Goodness-of-fit analyses were then conducted to quantitatively discriminate

between the gamma-distribution and log-normal distribution models. For convenience, we

termed a gamma distribution and a log-normal distribution as $GA(k,\theta)$ and $LN(\mu,\sigma)$,

respectively. Thus, the likelihood functions of data that follow $GA(k,\theta)$ and $LN(\mu,\sigma)$

can be denoted as:

903
$$L_{GA}(k,\theta) = \prod_{j=1}^{n} f_{G}(i;k,\theta) \tag{5}$$

904
$$L_{LN}(\mu,\sigma) = \prod_{j=1}^{n} f_{LN}(i;\mu,\sigma) \tag{6}$$

905   Therefore, the RML between a gamma distribution and a log-normal distribution is

906   defined as:

907
$$RML = \frac{L_{GA}(\hat{k},\hat{\theta})}{L_{LN}(\hat{\mu},\hat{\sigma})} \tag{7}$$

908   where $(\hat{k},\hat{\theta})$ and $(\hat{\mu},\hat{\sigma})$ are the MLEs of (k,θ) and (μ,σ) for I. The natural logarithm

909   of RML can be written as:

910
$$D = n\left[\hat{k}\ln\left(\frac{\tilde{I}}{\hat{\theta}}\right) + \frac{1}{2\hat{\sigma}^2 n}\sum_{j=1}^{n}\left(\ln\left(\frac{I_j}{\hat{\mu}}\right)\right)^2 + \frac{1}{2}\ln(2\pi) - \ln\left(\frac{\Gamma(\hat{k})}{\hat{\sigma}}\right) - \frac{\bar{I}}{\hat{\theta}}\right] \qquad (8)$$

911 where $\bar{I} = \frac{1}{n}\sum_{j=1}^{n}I_j$ and $\tilde{I} = \left(\prod_{j=1}^{n}I_j\right)^{\frac{1}{n}}$ are the arithmetic and geometric means of I ,

912 respectively.

913   The natural logarithm of RML, D , measured the goodness-of-fit between the

914 gamma-distribution model and the log-normal distribution model of ISI. That is, the

915 gamma-distribution model precedes the log-normal distribution model if $D > 0$; otherwise,

916 choose the log-normal distribution as the preferred model of ISI. The larger the absolute

917 value of D , the more accurate-fitting the result of the chosen model over the other model.

918 **Local field potential spectral analysis**

919   To generate the power spectra of LFP in Figure 14, the local field potential power

density was calculated in a range of 0.025–20.0 Hz with 0.025 Hz intervals for the

recording dataset of hippocampal CA1, BLA and RSC regions. The fast Fourier transform

(with Hann windowing function) was applied to the EEG signal, the resulting frequency

resolution was 0.025 Hz, and the frequency bins less than 1 Hz were discarded due to the

sensitivity of these bins to noise.

Author Contributions: J.Z.T. and M.L. conceived and designed the project. J.Z.T.

designed the experiments with M.L., K.X., H.K., G.E.F. and J.L. The research was

performed as follows: K.X. recorded from the ACC and PrL datasets; G.E.F. from the RSC;

Jun Liu from the BLA; D.W. from the striatum, H.K. for the CA1, M.L., F.Z., Z.S., L.C.,

Y.M., and H.K. for data analyses together with J.Z.T. J.Z.T. and M.L. wrote the paper with

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1123

Figure legends

Figure 1. Statistical properties of neural spike patterns.

(**A**) Neuronal spikes are highly variable. The upper subpanel illustrates the spike-activity patterns of 20 neurons within a 10-sec time period recorded from the VTA region of a mouse during the awake state. The lower subpanel shows the ISI distribution of a sample VTA DA neuron.

(**B**) Illustrations of a positive- and negative-skewed distribution. The red and blue curves illustrate a positive-skewed distribution and a negative-skewed distribution, respectively. Gray dashed lines denote symmetric distributions. Skewness (γ) and nonparametric-skew (S) are applied to examine the positive/negative-skewed properties.

(**C**) Illustrations of a gamma-distribution model and a log-normal distribution model. Fitted gamma distribution and log-normal distribution of the ISI in the lower subpanel of (**A**) are plotted as red and blue curves. The goodness-of-fit analysis is conducted to compare the gamma-distribution model with the log-normal distribution model for characterizing neuronal spike patterns.

Figure 2. Putative principal cells in mice's cortical and subcortical regions discharge positive-skewed, heavy-tailed spike patterns.

(**A**) ACC, (**B**) RSC, (**C**) CA1, and (**D**) BLA. The left subpanels of (**A-D**) show the histograms of skewness γ in the corresponding regions, where the gray vertical lines denote the symmetric distributions ($\gamma=0$), positive-skewed distributions have $\gamma>0$, while negative-skewed distributions have $\gamma<0$. The middle subpanels of (**A-D**) show the histograms of nonparametric-skew S in the corresponding regions, the symmetric

1147 distributions have $S = 0$, $S > 0$ for positive-skewed distributions and $S < 0$ for negative-

1148 skewed distributions. The right subpanels of (**A-D**) show their relationships with the

1149 neurons' mean firing rates, where the colors of each dot represent the mean firing rates of

1150 corresponding neurons.

1151

Figure 3. Spike-timing patterns of principal cells conformed gamma distribution

across mice cortical and subcortical regions under the quiet-awake state.

(**A**) ACC, (**B**) RSC, (**C**) CA1, and (**D**) BLA. The left subpanels of (**A-D**) show the spike-

timing patterns of sample neurons recorded from the corresponding brain regions, their

fitted gamma distributions (red curves) and log-normal distributions (blue curves). The

right subpanels of (**A-D**) are the distributions of D (the natural logarithm of RML) vs.

mean firing rates of principal cells under the quiet-awake state. The lines in these plots

illustrate the linear regression between D and mean firing rates of principal cells.

1160

1161 **Figure 4. Spike-timing patterns of principal cells conformed gamma distribution**

1162 **across different mice cortical and subcortical regions during the animals' sleep.**

1163 The distributions of D vs. mean firing rates of principal cells recorded from different

1164 cortical and subcortical regions during the animals' sleep. The lines in these plots illustrate

1165 the linear regression between D and mean firing rates of principal cells.

1166

Figure 5. Preserved shape parameter k across brain states.

Distributions of shape parameter k of principal cells in four brain regions during awake

and sleep states are shown in the left subpanels of (**A-D**), while distributions of scale

parameter θ in these two states are shown in the right subpanels. Red lines denote the

linear regressions of corresponding parameters, red numbers at the upper-left corner of

each subpanel denote the correlation coefficients.

1173

Figure 6. Spike-timing patterns of striatum medium spiny projection neurons

conformed to gamma distribution.

(**A**) The spike-timing pattern of a medium spiny projection neurons recorded from the

dorsal striatum of mice, and its fitted gamma distribution (red curve) and log-normal

distribution (blue curve).

(**B**) Medium spiny projection neurons discharge positive-skewed, heavy-tailed spike

patterns. The upper subpanel: the histogram of γ. The middle subpanel: the histogram of

S. The lower subpanel: the distribution of γ and S, where the dots' colors represent

neurons' mean firing rates.

(**C**) The distribution of D vs. mean firing rates of medium spiny projection neurons. The

line in the plot denotes the linear regression between D and mean firing rates.

1185

Figure 7. Spike-timing patterns of interneurons conformed to gamma distribution.

(**A**) Interneurons recorded from four brain regions (ACC, BLA, hippocampal CA1, and

RSC) discharge positive-skewed, heavy-tailed spike patterns. The left subpanel: the

histogram of γ. The right subpanel: the histogram of S.

(**B**) The distribution of γ and S, where the dots' colors represent neurons' mean firing

rates.

(**C**) The distribution of D vs. mean firing rates. The line in the plot denotes the linear regression between D and mean firing rates.

Figure 8. Spike-timing patterns of VTA DA neurons conformed to gamma distribution.

(**A**) Fitted gamma distribution and log-normal distribution of the spike-timing pattern of a DA neuron recorded from mice VTA region.

(**B**) VTA DA neurons discharge positive-skewed, heavy-tailed spike-timing patterns. The upper subpanel: the histogram of γ. The middle-subpanel: the histogram of S. The lower subpanel: the distribution of γ and S, where the dots' colors represent neurons' mean firing rates.

(**C**) The distribution of D vs. mean firing rates of VTA DA neurons. The line in the plot represents the linear regression between D and mean firing rates.

Figure 9. Spike-timing patterns of principal cells in hamster PrL region conformed to gamma distribution.

(**A**) Fitted gamma distribution and log-normal distribution of a principal cell recorded from hamster PrL region.

(**B**) Principal cells in hamster PrL region discharge positive-skewed, heavy-tailed spike patterns. The upper subpanel: the histogram of γ. The middle subpanel: the histogram of

1213 S. The lower subpanel: the distribution of γ and S, where the dots' colors represent

1214   neurons' mean firing rates.

1215   (**C**) The distribution of D vs. mean firing rates of principal cells in the hamster PrL region.

1216   The line in the plot represents the linear regression between D and mean firing rates.

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Figure 10. Spike-timing patterns in monkey area 5d conformed to gamma

distribution.

(**A**) Fitted gamma distribution and log-normal distribution of a sample neuron recorded

from monkey area 5d.

(**B**) Neurons in area 5d discharge positive-skewed, heavy-tailed spike patterns. The upper

subpanel: the histogram of γ. The middle-subpanel: the histogram of S. The lower

subpanel: the distribution of γ and S, where the dots' colors represent neurons' mean

firing rates.

(**C**) The distribution of D vs. mean firing rates of neurons in area 5d. The line in the plot

denotes the linear regression between D and mean firing rates.

1228

Figure 11. Spike-timing patterns in cat primary visual cortex conformed to gamma

distribution.

(**A** and **B**) Fitted gamma distributions and log-normal distributions of two neurons

recorded from cat primary visual cortex under 1-D white noise (**A**) and 2-D stimuli (**B**).

(**C** and **D**) Neurons in cat primary visual cortex discharge positive-skewed, heavy-tailed

spike patterns under both 1-D white noise (**C**) and 2-D stimuli (**D**). The upper subpanels:

the histograms of γ. The middle subpanels: the histograms of S. The lower subpanels:

the distributions of γ and S, where the dots' colors represent neurons' mean firing rates.

(**E** and **F**) The distributions of D vs. mean firing rates of neurons in the cat primary visual

cortex under 1-D white noise (**E**) and 2-D stimuli (**F**). The line in the plot denotes the

linear regression between D and mean firing rates.

1240

Figure 12. Preserved shape parameter k across resting states and behaving states.

The distributions of D vs. mean firing rates of principal cells recorded from the ACC and

RSC regions during two resting states (the quiet-awake state and sleep) and the behaving

state are shown in the left subpanels of (**A** and **B**). The lines in the left subpanels of (**A** and

B) are the linear regressions between D and mean firing rates. 3D distributions of k

during three states are shown in the right subpanels of (**A** and **B**).

1247

Figure 13. Comparisons of spike-timing regularities and irregularities across

different cell types and brain regions.

The distributions of k in 18 datasets recorded from four mammalian species (mice,

hamster, cat and monkey), it consisted of a total of 3,378 neurons obtained from 13 brain

regions. These neurons were grouped according to their general anatomical locations and

cell types, namely, the sensory cortices (mouse V1, cat V1, mouse RSC, mouse

somatosensory, and mouse 2nd AuV), prefrontal cortices (mouse ACC and hamster PrL),

motor cortices (mouse M1 and monkey 5d), limbic regions (mouse BLA and mouse CA1),

DA neurons (mouse VTA), and GABAergic neurons (mouse STR medial spiny neurons,

and fast-spiking interneurons in mouse ACC, BLA, CA1 and RSC). Each dot represents a

neuron. The gray horizontal line denotes the Poisson process ($k = 1$), regular spiking ($k > 1$)

and irregular spiking ($k < 1$) are shown as a red-arrow line and blue-arrow line,

respectively. Error bars represent mean ± SEM.

1261

Figure 14. Gamma-like spike-timing patterns diminished under anesthesia.

(**A-C**) Left subpanels: spike activities of 15 example principal cells recorded during awake

state and anesthesia from CA1 (**A**), BLA (**B**), and RSC (**C**). Middle subpanels: power

spectra of LFP recorded during awake state and anesthesia from CA1 (**A**), BLA (**B**), and

RSC (**C**). Right subpanels: spike-timing patterns under the quiet awake state conform

single gamma distribution (shown as the plots in red color), spike-timing patterns during

ketamine-induced anesthesia can be described by using two gamma distributions (shown

as the plots in blue color). The subplots show the similarity between the empirical

cumulative probabilities and the cumulative probabilities of corresponding fitted gamma

distributions. The one-sample Kolmogorov-Smirnov test is applied to verify the fitness of

the gamma distribution.

A

Spikes are highly variable

Figure 1

ISI distribution

B

Positive-skewed or **Negative-skewed** ?

Median < Mean

Mean < Median

– – Symmetric distribution

C

Gamma or **Log-Normal** ?

— Fitted Gamma distribution
— Fitted Log-Normal distribution

Figure 2

A. ACC (n = 197)

B. RSC (n = 321)

C. CA1 (n = 511)

D. BLA (n = 451)

Figure 3

Figure 4

Figure 6

Figure 7

Figure 8

Figure 11

A ACC (n=95)

B RSC (n=120)

Figure 12

Figure 13