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Coevolution of virulence and immunosuppression in multiple infections

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Abstract

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2 This preprint has been reviewed and recommended by Peer Community In Evolutionary Bi-
3 ology (<http://dx.doi.org/10.24072/pci.evolbiol.100043>). Many components
4 of host-parasite interactions have been shown to affect the way virulence (i.e., parasite-induced
5 harm to the host) evolves. However, coevolution of multiple parasite traits is often neglected. We
6 explore how an immunosuppressive mechanism of parasites affects and coevolves with virulence
7 through multiple infections. Applying the adaptive dynamics framework to epidemiological mod-
8 els with coinfection, we show that immunosuppression is a double-edged-sword for the evolution
9 of virulence. On one hand, it amplifies the adaptive benefit of virulence by increasing the abun-
10 dance of coinfections through epidemiological feedbacks. On the other hand, immunosuppres-
11 sion hinders host recovery, prolonging the duration of infection and elevating the cost of killing
12 the host. The balance between the cost and benefit of immunosuppression varies across different
13 background mortality rates of hosts. In addition, we find that immunosuppression evolution is
14 influenced considerably by the precise trade-off shape determining the effect of immunosuppres-
15 sion on host recovery and susceptibility to further infection. These results demonstrate that the
16 evolution of virulence is shaped by immunosuppression while highlighting that the evolution of
17 immune evasion mechanisms deserves further research attention.

18 **Introduction**

19 The fundamental question of virulence evolution, ‘Why do some parasite strains harm their hosts
20 more than others?’, has been a central focus of evolutionary epidemiology for both its conceptual
21 and applied significance (Ewald, 1994, Read, 1994, Schmid-Hempel, 2011, Méthot, 2012, Alizon
22 and Michalakis, 2015). The adaptive explanation of virulence is typically centred around trade-offs
23 involving virulence and other parasite fitness components, such as transmission and competitiveness
24 in multiple infections (Anderson and May, 1982, Ewald, 1983, van Baalen and Sabelis, 1995, Alizon
25 et al., 2009, 2013). While these trade-off theories explain the evolution of finite non-zero optimal
26 virulence, exactly how much virulence a parasite should evolve depends on a variety of processes
27 (Cressler et al., 2016). For example, host traits (e.g. host immune responses) and their interactions
28 with coevolving parasite adaptations (e.g. parasite immune evasion strategies; Frank and Schmid-
29 Hempel, 2008, Alizon, 2008b, Cressler et al., 2016) are likely to influence the trade-offs. The present
30 theoretical study explores how a parasite immunosuppression strategy, namely the ability of parasites
31 to hinder host recovery, coevolves with virulence.

32 The ability of parasites to suppress host immunity is ubiquitous in nature (Schmid-Hempel, 2009)
33 and frequently helps maintain chronic infections (Virgin et al., 2009). In humans, for instance, in-
34 fections by human papillomaviruses (HPVs) and human immunodeficiency virus (HIV) offer two
35 contrasting immune suppression strategies: the former interferes with the cellular machinery to re-
36 duce the presentation of viral antigens or impede the interferon response (Doorbar et al., 2012), while
37 the latter infects and lyses T lymphocytes (Levy, 1998). In plant parasites, as well, a variety of mecha-
38 nisms exist to suppress host defensive responses (Burgyán and Havelda, 2011, Sarmiento et al., 2011).
39 Regardless of the specific host-parasite interaction, or mechanism involved, the adaptive benefit for
40 the parasite is realised through prolonged infection duration (Schmid-Hempel, 2009). For the scope
41 of our study, we generalise any parasite adaptation against host immunity that results in lowered host

42 recovery rate as immunosuppression.

43 In the absence of constraints, it is in the parasite's best interest to evolve maximal immunosup-
44 pression, when immunity serves only to kill parasites. However, lowered host immunity is likely to
45 impose at least one cost to the parasite: an immunocompromised host may be more vulnerable to fur-
46 ther infection by conspecific and heterospecific parasites. A meta-analysis by [Graham \(2008\)](#) shows
47 that lowered immune responses, due to the presence of an immunosuppressive helminth, increase
48 microparasite population density within hosts. Furthermore, experimental evidence suggests that im-
49 munosuppression could lead to increased host mortality through additional infections by opportunistic
50 parasites ([Cornet and Sorci, 2010](#)). Therefore, multiple infections — which are so prevalent that they
51 could be argued to be the rule rather than the exception ([Petney and Andrews, 1998](#), [Cox, 2001](#), [Read
52 and Taylor, 2001](#), [Juliano et al., 2010](#), [Balmer and Tanner, 2011](#)) — are likely a key driver of the
53 coevolution between virulence and immunosuppression.

54 If immunosuppression leads to more multiple infections, one might predict that this should lead
55 to increased virulence. Many theoretical, and some empirical, studies support the notion that within-
56 host competition leads to the evolution of higher virulence (reviewed in [Mideo, 2009](#)). Therefore,
57 at the epidemiological level, as the density of coinfecting hosts increases, so does the optimal level
58 of virulence ([van Baalen and Sabelis, 1995](#), [Choisy and de Roode, 2010](#)). However, given that the
59 benefit of immunosuppression is assumed to be a longer duration of infection, increasing virulence
60 would counteract this effect. Therefore, without a formal model, intuition fails to predict the direction
61 in which virulence evolves when immunosuppression is considered.

62 To elucidate the coevolutionary dynamics of virulence and immunosuppression, we develop math-
63 ematical epidemiology models, in which we assume that the two parasite traits are carried by the same
64 parasite species (as in [van Baalen and Sabelis, 1995](#)). Furthermore, we also investigate how the co-
65 evolved optimal strategy is affected by host background mortality and trade-off concavity determining
66 the effect of immunosuppression on host recovery and susceptibility to further infection.

67 **The model**

68 We use an evolutionary epidemiology approach based on adaptive dynamics theory (Geritz et al.,
69 1998, Dieckmann et al., 2002, Otto and Day, 2007). We first present the epidemiological model
70 itself, then the evolutionary trade-offs that constrain evolution and finally we show how the (co-
71)evolutionary analyses are conducted.

72 **Epidemiological dynamics**

73 We employ a coinfection framework, which allows for coexistence of two parasite strains within a
74 host. Existing coinfection models track either two different resident strains belonging to different
75 species (Choisy and de Roode, 2010) (Fig. 1a), or more simply, a single resident species (van Baalen
76 and Sabelis, 1995) (Fig. 1b). While the two models differ in biological motivations, conceptually, the
77 latter is a special case of the former: the two models are identical if the within-host interactions are the
78 same between the two species (Alizon et al., 2013). Here, we employ the single species model (Fig.
79 1b) which allows us to study the coevolution of virulence and immunosuppression without making
80 assumptions about how two parasite species are different; thereby requiring fewer parameters. In
81 this model, hosts are divided into three classes: susceptible, singly infected and doubly infected,
82 occurring at densities S , I and D respectively. Following the notation of Table 1, we derive the
83 following system of ordinary differential equations (ODEs) to describe the changes of the resident
84 system over continuous time:

$$\frac{dS}{dt} = \rho - \mu S - \lambda_r S + \gamma(\theta) I_r \quad (1a)$$

$$\frac{dI_r}{dt} = \lambda_r S - (\mu + \alpha(x)) I_r - \sigma(\theta) \lambda_r I_r - \gamma(\theta) I_r + 2 \gamma(\theta) D_{rr} \quad (1b)$$

$$\frac{dD_{rr}}{dt} = \sigma(\theta) \lambda_r I_r - (\mu + \alpha(x)) D_{rr} - 2 \gamma(\theta) D_{rr} \quad (1c)$$

85 where the subscript r denotes the resident parasite strain. In this formulation, there is a constant

86 input of susceptible hosts into the population at the rate ρ . Susceptible hosts exit the system through
87 background mortality at the rate μ , while infected hosts, both singly and doubly infected individuals,
88 experience additional mortality caused by parasites (i.e., virulence α). Susceptible and singly infected
89 hosts acquire infection according to the force of infection $\lambda_r = \beta I_r + \beta D_{rr}$, where β corresponds to
90 the parasite transmission rate. The host class for double infection by the same strain, D_{rr} is included
91 in the system for a technical motivation: it is necessary for an unbiased invasion analysis because the
92 mutant strain would gain a frequency-dependent advantage in its absence (discussed in [Alizon, 2008a](#),
93 [Lipsitch et al., 2009](#)). We assume that the rate of recovery, $\gamma(\theta)$, and susceptibility to coinfection,
94 $\sigma(\theta)$, are functions of immunosuppression, θ . Within the existing epidemiological framework, the
95 effect of host immunity can be implicitly accounted for as the rate of recovery (equivalent to the
96 rate of parasite clearance). We assume that hosts recover from infection at a rate $\gamma(\theta)$, in a stepwise
97 fashion, i.e., doubly infected hosts (D) only lose one infection at a time). The key feature of our
98 model is that we assume that singly infected hosts (I) suffer an increased risk of contracting a further
99 infection at a rate proportional to a coefficient $\sigma(\theta)$. We treat the host class D_{rr} similarly to singly
100 infected hosts I_r , except for the fact that the doubly infected hosts cannot be infected any further.

101 **Within-host processes and resulting trade-offs**

102 It is commonly assumed that virulence (i.e., parasite-induced host mortality) correlates with the extent
103 of parasite resource exploitation. Adaptive benefits of resource exploitation include the positive cor-
104 relation with transmission ([Fraser et al., 2007](#), [de Roode et al., 2008](#), [Råberg, 2012](#)), and a within-host
105 competitive advantage in coinfection ([de Roode et al., 2005](#), [Bell et al., 2006](#), [Ben-Ami et al., 2008](#),
106 [Zwart et al., 2009](#)). Here, we focus on the latter adaptive benefit to study the evolution of virulence
107 and immunosuppression. We assume that virulence (α) increases linearly with the level of resource
108 exploitation by a parasite (x), such that $\alpha(x) = a x$, where a is a proportionality constant (we explore
109 a transmission-virulence trade-off in the Supplementary Information 2). We then assume that finding

110 themselves in a doubly infected host is inherently costly for parasites due to exploitation competition
111 between coinfecting strains (Mideo, 2009, Schmid-Hempel, 2011), and that more virulent strains are
112 more competitive in multiple infections:

$$\beta_{rm}(x_r, x_m) = \left(\frac{x_r}{x_r + x_m} \right) \beta \quad (2a)$$

$$\beta_{mr}(x_r, x_m) = \left(\frac{x_m}{x_r + x_m} \right) \beta. \quad (2b)$$

113 There is ample empirical evidence that immunosuppression benefits the parasites by prolonging
114 infections (reviewed in Schmid-Hempel, 2008), and lowered host immunity would increase the sus-
115 ceptibility to multiple infections (Palefsky and Holly, 2003, Rockstroh and Spengler, 2004, Cornet
116 and Sorci, 2010). Thus, the key trade-off in our model is between infection duration and susceptibil-
117 ity to coinfections (both being mediated by immunosuppression). We, therefore, assume a trade-off
118 between the rate of recovery, $\gamma(\theta)$, and additional susceptibility of infected hosts to coinfection, $\sigma(\theta)$,
119 by making them both functions of immunosuppression intensity, θ . It is conceivable for the decline
120 of recovery rate and the increase of additional susceptibility to either accelerate or decelerate with
121 increasing immunosuppression. Because the trade-off shape typically matters for evolutionary dy-
122 namics (Bowers et al., 2005, Kisdi, 2006) and little is known from empirical data, we explore the
123 trade-offs involving recovery and susceptibility as both accelerating and decelerating functions of
124 immunosuppression. The parameters δ_γ and δ_σ control the degree of concavity of the effect of im-
125 munosuppression on recovery and increased susceptibility, respectively (eq. 3; Fig. S1).

$$\gamma(\theta) = \gamma_{\max} \begin{cases} \left(1 - \frac{\theta}{\theta_{\max}}\right)^{\delta_{\gamma}}, & \text{if accelerating} \\ 1 - \left(\frac{\theta}{\theta_{\max}}\right)^{\delta_{\gamma}}, & \text{if decelerating} \end{cases} \quad (3a)$$

$$\sigma(\theta) = 1 + \sigma_{\text{range}} \begin{cases} 1 - \left(1 - \frac{\theta}{\theta_{\max}}\right)^{\delta_{\sigma}}, & \text{if accelerating} \\ \left(\frac{\theta}{\theta_{\max}}\right)^{\delta_{\sigma}}, & \text{if decelerating} \end{cases} \quad (3b)$$

126 With these functions, we assume that the realised recovery rate, $\gamma(\theta)$, decreases as a function
 127 of immunosuppression such that it equals the intensity of host immunity, γ_{\max} , in the absence of
 128 immunosuppression and approaches 0 as immunosuppression approaches θ_{\max} . We also assume that
 129 the proportional gain in susceptibility to a further infection, $\sigma(\theta)$, elevates the force of infection
 130 experienced by an immunosuppressed singly infected host by up to $1 + \sigma_{\text{range}}$ fold at the upper limit of
 131 immunosuppression (when $\theta = \theta_{\max}$). Because it is commonly assumed that the pay-off of a beneficial
 132 trait saturates, we set the recovery trade-off as decelerating at default. We set the default susceptibility
 133 trade-off as accelerating to further emphasise the difference between beneficial and costly traits.

134 Evolutionary analyses

135 The mutant systems

136 We carry out an invasion analysis investigating perturbation of the resident state by adding a rare mu-
 137 tant strain, the densities and traits of which are denoted with subscript m (Fig. 1b). For the evolution
 138 of immunosuppression, the dynamics of the mutant strain are summarised in the following system of
 139 ODEs:

$$\frac{dI_m}{dt} = \lambda_m S - (\mu + \alpha) I_m - \sigma(\theta_m) \lambda_r I_m - \gamma(\theta_m) I_m + \gamma(\theta_{rm}) D_{rm} \quad (4a)$$

$$\frac{dD_{rm}}{dt} = \sigma(\theta_r) \lambda_m I_r + \sigma(\theta_m) \lambda_r I_m - (\mu + \alpha) D_{rm} - 2 \gamma(\theta_{rm}) D_{rm} \quad (4b)$$

Table 1: Parameter notation, description and default values. Parameter values chosen to sustain non-zero and non-complex equilibria for the resident system and relevant evolutionarily singular strategies. Parameters that are functions of others are indicated with the dependent parameters (or variables) inside parentheses. When we allow only immunosuppression to evolve, virulence, α , is a constant; otherwise, α evolves as a function of a and x . Rates are in units of per day.

Symbol	Description	Value (or range)
ρ	Susceptible host birth rate	100
μ	Background mortality rate	[0.001, 0.1]
β	Transmission rate	0.001
λ	Force of infection	$\lambda(\beta, I, D)$
α	Virulence: parasite-induced mortality	[0, 0.5] or $\alpha(a, x)$
γ	Realised recovery rate	$\gamma(\theta)$
σ	Increased susceptibility of infected hosts	$\sigma(\theta)$
θ	Immunosuppression	[0, 100]
θ_{\max}	Maximum immunosuppression	100
γ_{\max}	Maximum host recovery rate	0.5
$1 + \sigma_{\text{range}}$	Maximum susceptibility coefficient	[1, 5]
$\{\delta_{\gamma}, \delta_{\sigma}\}$	Recovery-coinfection susceptibility trade-off curve shape	{0.05, 0.25}
a	Virulence scaling parameter	0.1
x	Resource exploitation rate	[0.001, 5]

140 where $\lambda_r = \beta I_r + \beta D_{rr} + \beta_{rm} D_{rm}$ and $\lambda_m = \beta I_m + \beta_{mr} D_{rm}$. For simplicity we assume that the
141 order of infection does not matter so that D_{rm} is identical to D_{mr} . We neglect hosts infected twice by
142 the mutant strain (which would be D_{mm}) because it is unlikely that the same host gets infected twice
143 by a rare mutant. Recovery from D_{rm} can be achieved through either clearing a resident or a mutant
144 parasite. Other aspects of demographic changes of the mutant system are identical to the resident
145 system described above.

146 We assume that the level of immunosuppression in coinfection is the average between the resident
147 and mutant strain, i.e., $\theta_{rm} = \frac{\theta_r + \theta_m}{2}$. For virulence evolution, we assume that the only within-host
148 interaction between coinfecting parasites is competition for the shared host resources. Therefore, we
149 also calculate the overall virulence of coinfection as the average of the two strains, i.e. $\alpha_{rm} = \frac{\alpha_r + \alpha_m}{2}$.

150 The mutant dynamics for virulence evolution are governed by

$$\frac{dI_m}{dt} = \lambda_m S - (\mu + \alpha(x_m))I_m - \lambda_r \sigma(\theta)I_m - \gamma(\theta)I_m + \gamma(\theta)D_{rm} \quad (5a)$$

$$\frac{dD_{rm}}{dt} = \lambda_m \sigma(\theta)I_r + \lambda_r \sigma(\theta)I_m - (\mu + \alpha_{rm})D_{rm} - 2\gamma(\theta)D_{rm} \quad (5b)$$

151 where λ_r and λ_m are the force of infection for the resident and mutant, respectively, defined here
152 as $\beta I_r + \beta D_{rr} + \beta_{rm} D_{rm}$ and $\beta I_m + \beta_{mr} D_{rm}$. We again assume the trade-offs between recovery and
153 coinfection susceptibility as functions of immunosuppression in this model.

154 Adaptive dynamics

155 The fate of a rare mutant strain is determined by its fitness function (here denoted R_{θ_m} and R_{α_m} ,
156 respectively), that is, the ability to spread through a host population already infected with a resident
157 parasite (Geritz et al., 1998, Dieckmann et al., 2002). In the continuous time scale, the mutant parasite
158 invades and replaces the resident if the mutant fitness, calculated as the dominant eigenvalue of the
159 Jacobian matrix of the mutant system, is positive (Otto and Day, 2007). The expressions for the

160 invasion fitness of a rare mutant — with respect to immunosuppression and virulence (R_{θ_m} and R_{α_m} ,
 161 respectively) — emerging in a population infected by a resident strain are:

$$R_{\theta_m} = \frac{\beta(1 + \frac{1}{2} \frac{1}{\mu + \alpha + \gamma \frac{\theta_r + \theta_m}{2}} \sigma(\theta_m) \lambda_r)}{\mu + \alpha + \gamma(\theta_m) + \sigma(\theta_m) \lambda_r} \tilde{S} + \sigma(\theta_r) \frac{\frac{\beta}{2}}{\mu + \alpha + \gamma \frac{\theta_r + \theta_m}{2}} \tilde{I}_r \quad (6a)$$

$$R_{\alpha_m} = \frac{\beta(1 + \frac{\frac{x_m}{x_r + x_m}}{\mu + 2\gamma(\theta) + \frac{\alpha(x_r) + \alpha(x_m)}{2}} \sigma(\theta) \lambda_r)}{\mu + \alpha(x_m) + \gamma(\theta) + \sigma(\theta) \lambda_r} \tilde{S} + \sigma(\theta) \frac{\beta \frac{x_m}{x_r + x_m}}{\mu + 2\gamma(\theta) + \frac{\alpha(x_r) + \alpha(x_m)}{2}} \tilde{I}_r \quad (6b)$$

162 Consequently, an evolutionarily singular strategy can be found where the change of the invasion
 163 fitness ceases with respect to the evolving trait. For example, an evolutionarily singular strategy of
 164 immunosuppression (denoted θ^*) can be found when θ^* is an extremum of R_{θ_m} :

$$\left. \frac{\partial R_{\theta_m}}{\partial \theta_m} \right|_{\theta_m = \theta_r = \theta^*} = 0. \quad (7)$$

165 The properties of a singular strategy can then be assessed by the second derivatives of R_{θ_m} . Fol-
 166 lowing the notations used by Geritz et al. (1998), here we denote the second derivatives of R_{θ_m} with
 167 respect to the resident and mutant strain with a and b :

$$a = \left. \frac{\partial^2 R_{\theta_m}}{\partial \theta_r^2} \right|_{\theta_m = \theta_r = \theta^*}, \quad b = \left. \frac{\partial^2 R_{\theta_m}}{\partial \theta_m^2} \right|_{\theta_m = \theta_r = \theta^*} \quad (8)$$

168 The convergence stable ES (i.e. the strategy towards which selection drives the population and that
 169 is also non-invasible by mutants; i.e., evolutionarily stable and convergence stable, or the continuously
 170 stable strategy, CSS *sensu* Eshel (1983)) condition is satisfied when $b < 0$ and $a - b > 0$. The first
 171 condition states that the mutant fitness is at a local maximum and hence evolutionarily stable and
 172 the second condition implies no mutant invasion is possible at the point, meaning convergence stable
 173 (Geritz et al., 1998). Various other possible configurations of evolutionarily and convergence stability
 174 are discussed in Geritz et al. (1998).

175 **Coevolution of virulence and immunosuppression**

176 We graphically identified the coevolutionarily singular state as the intersection between the singular
177 state of immunosuppression and virulence (Choisy and de Roode, 2010, Alizon, 2013). When this
178 intersection is both convergence and evolutionarily stable, it can be interpreted as the coevolutionarily
179 stable strategy (Maynard Smith, 1982, Marrow et al., 1996, Dieckmann et al., 2002). The conditions
180 for coevolutionary stability are given in detail by (Abrams et al., 1993, Marrow et al., 1996). In brief,
181 the stability of each co-evolving trait is neither sufficient nor necessary, and there is no simple set of
182 criteria that guarantees local asymptotic stability. We explore the coevolution of the two traits across
183 different extrinsic mortality conditions and immunosuppression trade-off concavity.

184 **Results**

185 **Virulence evolution**

186 We first assume that the level of immunosuppression is constant and infer the virulence level towards
187 which the parasite population evolves, that is the evolutionarily stable virulence (ESV). We find that
188 the higher the immunosuppression, the higher the ESV (grey curve in Fig. 2a). Because immuno-
189 suppression renders infected hosts more susceptible to further infections, it consequently increases
190 the relative abundance of doubly infected hosts (Fig. 2e). This favours more virulent parasites due to
191 within-host competition (see equation 2).

192 **Immunosuppression evolution**

193 We then set the virulence to a constant value and study whether parasite immunosuppression evolves
194 towards an evolutionarily stable strategy (i.e., evolutionarily stable immunosuppression, or ESI; black
195 curve in Fig. 2a). We find that ESI decreases with virulence at first, but it increases again when viru-

196 lence is high enough. The initial decrease can be attributed to two non-mutually exclusive processes.
197 First, the benefits gained by increasing immunosuppression (i.e., slower host recovery) are reduced
198 as virulence increases since the duration of infection decreases. Note that ESI similarly decreases as
199 host mortality increases (Fig. 3a). Second, the decreasing pattern may originate from demographic
200 feedbacks: increasing virulence reduces coinfections, therefore parasites reap the benefit of immuno-
201 suppression in reduced recovery without paying the cost of contracting further infections. Therefore,
202 the initial decrease in ESI with virulence is also likely mediated by the falling fraction of multiple
203 infections (Fig. 2d).

204 We also find that the ESI increases with virulence when virulence is high enough. As the lifespan
205 of an infected host decreases due to high parasite-induced mortality, it becomes unlikely for a host to
206 survive a single infection long enough to get infected again. At this point, coinfections are sufficiently
207 rare (Fig. 2d) that highly immunosuppressive parasites would rarely suffer the cost of immunosup-
208 pression in contracting further infections. Taken together, focusing on the prevalence of coinfections
209 alone is not enough to predict how ESI will evolve.

210 **Coevolution of virulence and immunosuppression**

211 The co-ESS is found at the intersection between the two curves in Figure 2. For our default param-
212 eters, this occurs at intermediate values of immunosuppression and virulence. We now investigate
213 how changes in host mortality and the trade-off shapes determining the effect of immunosuppression
214 on host recovery and susceptibility to further infection affect this co-ESS. We first explore how the
215 co-ESS varies with respect to the rate of host background mortality. We find that co-ES immunosup-
216 pression (co-ESI) always decreases with host background mortality (black line in Fig. 3a), in accord
217 with the intuition that immunosuppression represents a lost investment if the host dies too rapidly.

218 In the absence of immunosuppression, as found in previous models (van Baalen and Sabelis,
219 1995, Gandon et al., 2001), the optimal virulence decreases with host background mortality because

220 the higher the mortality, the lesser the chance of coinfection from which the benefit of virulence is
221 realised (dashed grey line in Fig. 3a & purple area in b). In contrast, we find that virulence coe-
222 volving with immunosuppression (co-ESV), peaks at an intermediate value of background mortality
223 (solid grey line in Fig. 3a). Considering an extreme case in which the host never dies through back-
224 ground mortality (i.e., $\mu = 0$), the best strategy for the parasite is to evolve avirulence and maximise
225 immunosuppression so that the host remains infected forever (Fig. 3a). This scenario can be inter-
226 preted as an alignment of interest between resident and mutant strains as the benefit of keeping the
227 host alive longer appears to outweigh the adaptive advantage of being competitively dominant. With
228 zero mortality and maximum immunosuppression, a parasite's fitness is infinite: any mutant with
229 some virulence will have a finite fitness (because it will kill its host in single and double infections).
230 Intuitively, this avirulent strategy can also invade because in absence of the virulent strain, the fitness
231 is always maximised and the advantage reaped by the virulent one in coinfection is not enough to
232 overcome the cost of killing its singly-infected hosts. This cost of killing the host in single infection
233 relaxes as mortality increases, leading to a steep increase in virulence. The eventual decrease in viru-
234 lence is consistent with the evolution of virulence in the absence of immunosuppression (dashed grey
235 line in Fig. 3a)(van Baalen and Sabelis, 1995, Gandon et al., 2001).

236 Little is known about how immunosuppression impacts host recovery and susceptibility to further
237 infection. Therefore, we also explored the sensitivity of our co-ESS results to the qualitative shape
238 of the immunosuppression trade-off and the extent of its concavity using parameters, δ_σ and δ_γ . We
239 find that evolution moves away from the singular strategy when the recovery concavity is highly
240 accelerating (Fig. 4a) meaning that in this case immunosuppression is either maximised or minimised
241 depending on the initial conditions. Furthermore, we find that immunosuppression is maximised for
242 a large area of the near-linear and decelerating recovery trade-off space, δ_γ . Intermediate ESI levels
243 are observed for highly decelerating recovery, δ_γ . Overall, this suggests that there is a tendency
244 for parasites to specialise in immunosuppressing their host or to completely avoid doing so, and

245 knowledge of the recovery function appears particularly important for predicting immunosuppression
246 evolution. For virulence, the concavity of the susceptibility function (δ_σ) has the strongest quantitative
247 effect, with decelerating trade-offs leading generally to higher co-ESV. As in the rest of this model,
248 since the only benefit associated with virulence is increased competitiveness in a coinfecting host, the
249 co-ESV is an indicator of the importance of this competition in the parasite's life cycle.

250 Discussion

251 Host immune responses present a major challenge for parasites and, so, establishing a successful in-
252 fection often depends upon a parasite's ability to evade host immunity (Schmid-Hempel and Frank,
253 2007, Kerr et al., 2017). Despite its ubiquity among all major groups of parasitic organisms (Schmid-
254 Hempel, 2009), the effect of immunosuppression on virulence evolution has largely been overlooked
255 (but see Koella and Boete, 2003, Hurford and Day, 2013). We modelled immunosuppression through
256 its joint effect on host recovery and susceptibility to coinfection in an attempt to understand epidemi-
257 ological forces driving the coevolution of virulence and immunosuppression.

258 We found that immunosuppression increases the optimal parasite exploitation by creating more
259 coinfections, in which more competitive (and hence more virulent) strains are favoured. On the other
260 hand, the evolution of immunosuppression is driven by the balance between the benefit conferred by
261 immunosuppression to evade clearance from the host and the associated cost of contracting further
262 infections, which introduce a competitor for limited host resources. Because virulence simultaneously
263 decreases both the benefit (by killing hosts faster) and the cost (by reducing the risk of coinfection),
264 its effect on the optimal immunosuppression is nuanced — increasing virulence can both increase or
265 decrease the optimal immunosuppression depending on the baseline virulence of the parasite.

266 We then investigated the change in coevolutionarily optimal strategies of the two traits over host
267 background mortality. We find that mortality decreases the coevolutionarily stable level of immuno-

268 suppression, which is a lost investment when hosts die too fast anyway. In the absence of immuno-
269 suppression, we expect the optimal virulence to consistently decrease with host background mortality
270 because, again, investing in competitive ability (with which virulence correlates) is wasted when
271 coinfections are rare (van Baalen and Sabelis, 1995, Gandon et al., 2001). When coevolving with
272 immunosuppression, however, we find that evolutionarily stable virulence peaks for an intermediate
273 level of host mortality. This stems from the fact that for low host mortality, the coevolutionarily
274 optimal parasite strategy is to prolong the duration of infection by simultaneously maximising im-
275 munosuppression and minimising virulence.

276 In light of our theoretical model, we can formulate testable predictions. In *Daphnia*, for example,
277 the rate of host background mortality can be experimentally manipulated and its effect on virulence
278 evolution of microsporidian parasites can be quantified (Ebert and Mangin, 1997). Microsporidians
279 are common eukaryotic parasites of many animals including *Daphnia*, which often harbour multiple
280 infections (Ebert, 2005). In their mosquito host, microsporidians have been suggested to suppress
281 host immunity by manipulating the production pathway of a host immune defence molecule (nitric-
282 oxide, NO), which is part of the innate immune system conserved in all animals (Biron et al., 2005).
283 Conveniently, the production of NO can also be experimentally enhanced and blocked, making it
284 possible to investigate the effects of manipulating host immune intensity (Rivero, 2006). While our
285 model predicts the coevolution of virulence and immunosuppression is likely influenced by the pre-
286 cise shape of the trade-offs determining the cost and benefit of immunosuppression, there is a dearth
287 of empirical data with which to calibrate these curves. The *Daphnia* system may offer an opportunity
288 to characterise immunosuppression trade-offs and advance the understanding of the role of immuno-
289 suppression in virulence evolution.

290 A natural extension to the model of coinfection by the same species (van Baalen and Sabelis,
291 1995) is the model that accommodates two distinct resident parasite species, each of which can be
292 challenged by a mutant (Choisy and de Roode, 2010). Under the different species model, two co-

293 evolving traits (e.g., immunosuppression and virulence) could be carried by two separate parasite
294 species, which better reflect the reality for some immunosuppressing parasites, e.g., the immunosup-
295 pressing capabilities of HIV render the host susceptible to the virulence induced by opportunistic
296 infections. Similarly, in an amphipod system, [Cornet and Sorci \(2010\)](#) show that immunosuppressive
297 parasites elevate host mortality by promoting opportunistic pathogen infections. Furthermore, there
298 is evidence that pathological severity of malaria infection can be amplified through immunosuppres-
299 sion caused by helminths, which are common parasites in malaria prevalent tropical regions ([Graham
300 et al., 2005](#)). That being said, considering multiple species would force us to revisit our assumption
301 that more virulent mutants are more competitive than their resident at the within-host level. Indeed,
302 this assumption has recently been shown to hold for a variety of within-host processes, but only if the
303 mutant traits are close to that of the resident ([Sofonea et al. in prep](#)). Therefore, adding more details
304 about the within-host interactions, e.g., via a nested model ([Mideo et al., 2008](#)), seems necessary to
305 study coinfection by different species.

306 In the present model, we assumed no direct link between immunosuppression and virulence. How-
307 ever, immune evasion strategies of bacteria and viruses have been empirically linked to a range of
308 pathological effects ([Casadevall and Pirofski, 2003](#), [Monack et al., 2004](#), [Stanford et al., 2007](#)). On
309 the other hand, immunosuppression may decrease immunopathology which can, therefore, reduce
310 host mortality, as shown experimentally using rodent malaria infections ([Long et al., 2008](#), [Long and
311 Graham, 2011](#)). In fact, helminth therapy, which involves deliberate ingestion of parasitic worms,
312 takes advantage of the parasite's ability to mediate host immunity and has been successful in coun-
313 tering inflammations caused by immune-mediated diseases ([Day et al., 2007](#), [Elliott and Weinstock,
314 2009](#), [Summers et al., 2003](#)).

315 The only cost of immunosuppression we assumed is indirect (coinfection facilitation), however,
316 the production of immunosuppressive compounds could impose a direct fitness cost to individual par-
317 asites. At the within-host level, immunosuppression would, therefore, be seen as a public good since

318 parasites that do not invest in it can still reap the benefits (Diard et al., 2013, Rundell et al., 2016). In
319 fact, our model predicts that invasive repellers are common while coexistence of two strains with ex-
320 treme immunosuppression strategies (i.e., zero and maximum immunosuppression) is always possible
321 regardless of trade-off concavity (figure not shown). These findings suggest that it may be common
322 for some strains to specialise in immunosuppressing and others in exploiting these immunosuppressed
323 hosts.

324 Understanding how host immunity and the corresponding parasite immune evasion strategies af-
325 fect virulence evolution is a key challenge for contemporary evolutionary epidemiology (Frank and
326 Schmid-Hempel, 2008). Our results demonstrate that immune evasion mechanisms are among the
327 major forces shaping virulence evolution at the between-host level. Future theoretical studies may
328 focus on multi-species epidemiological dynamics, direct trade-offs between immunosuppression and
329 virulence and life-history perspectives.

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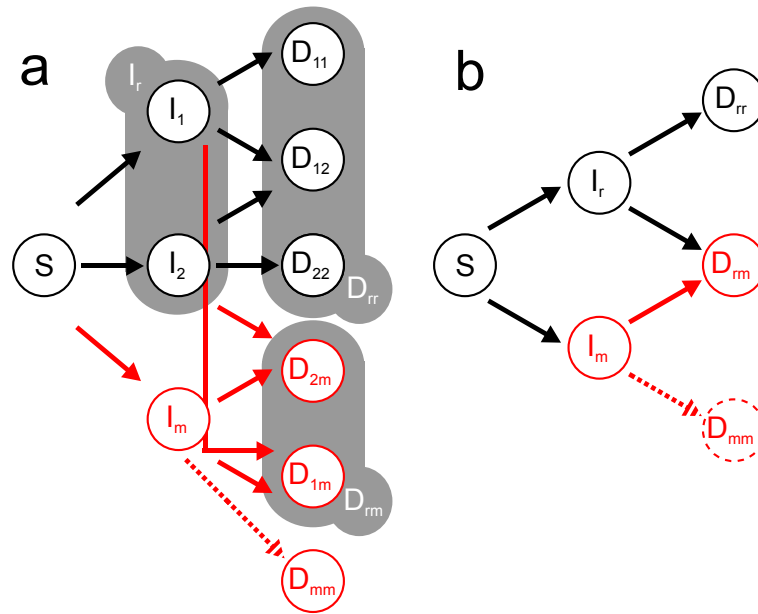


Fig. 1: Evolutionary epidemiology model for (a) coinfections by parasites from different species and (b) from same species. In black is the resident system (two strains, one for each species, in (a; labeled 1 and 2) and one strain in (b; labeled r)) and in red are the host classes related to the rare mutant (labeled m). The one species model (b) is a special case of the two species model (a) because the grey bubbles in (a) can be simplified to formulate the one species model (b) when within-host parameters are identical between the two parasite species.

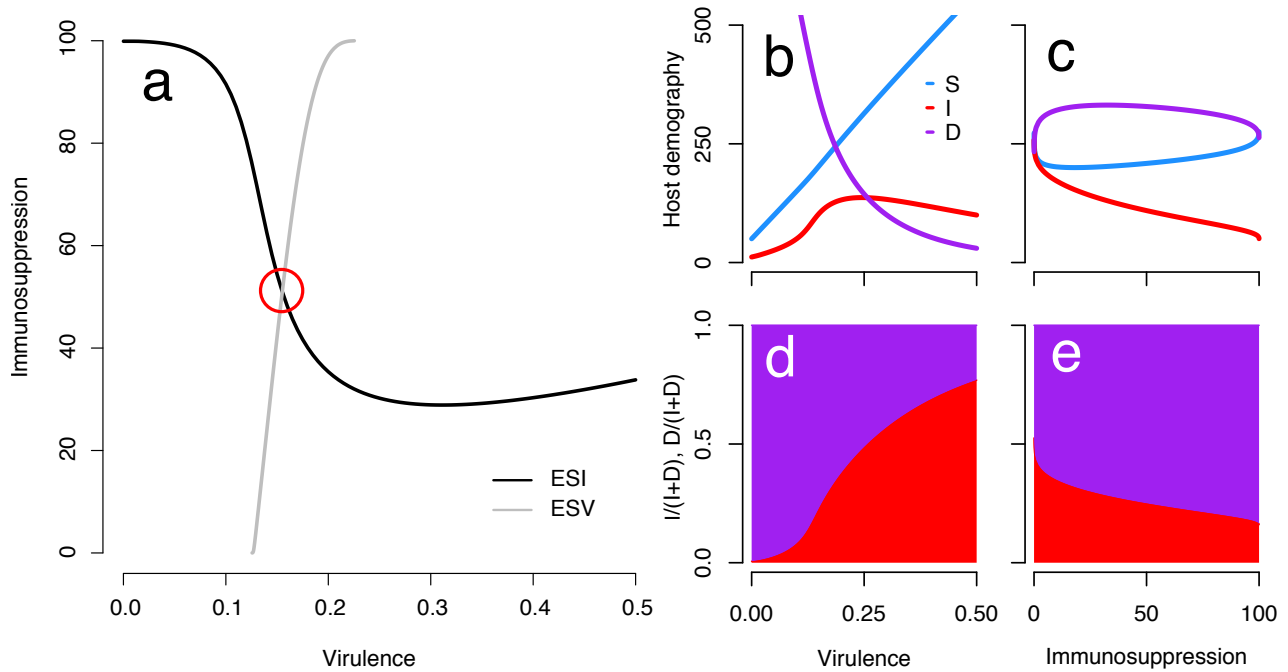


Fig. 2: (a) Evolutionarily stable immunosuppression (ESI; black) and virulence (ESV; grey) against fixed values of the other trait. The co-evolutionarily stable strategy (co-ESS) of the two traits occurs at the intersection of the two lines, indicated by the red circle. The immunosuppression trade-offs for the recovery rate and additional susceptibility were decelerating and accelerating, respectively with shape parameters $\delta_\gamma = 0.05$ and $\delta_\sigma = 0.25$. The equilibrium population size of the three host classes — susceptible (S ; blue), singly infected (I ; red) and doubly infected (D ; purple) — underlying the ESI over a range of of virulence and the ESV over a range of immunosuppression values is presented in (b) and (c). The relative abundances of singly (red) and doubly (purple) infected host are plotted in (d) and (e).

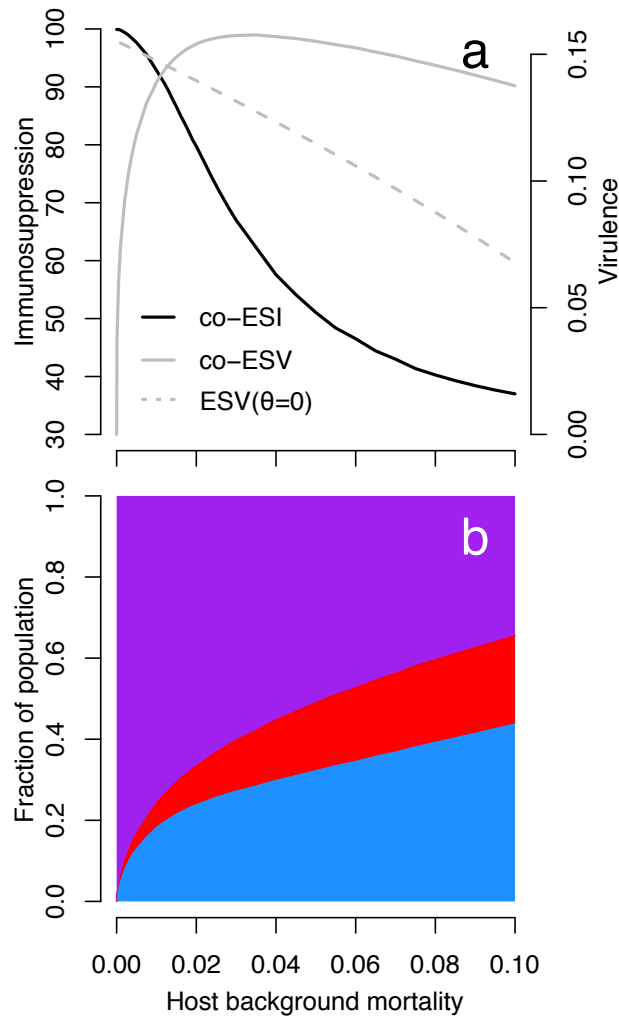


Fig. 3: (a) Coevolutionarily stable immunosuppression (co-ESI; black) and virulence (co-ESV; solid grey) strategies, and evolutionarily stable virulence strategy in the absence of immunosuppression (ESV ($\theta = 0$); dashed grey) against host background mortality and (b) the fraction of population of the three host classes — susceptible (S ; blue), singly infected (I ; red) and doubly infected (D ; purple) at the coevolutionarily stable state.

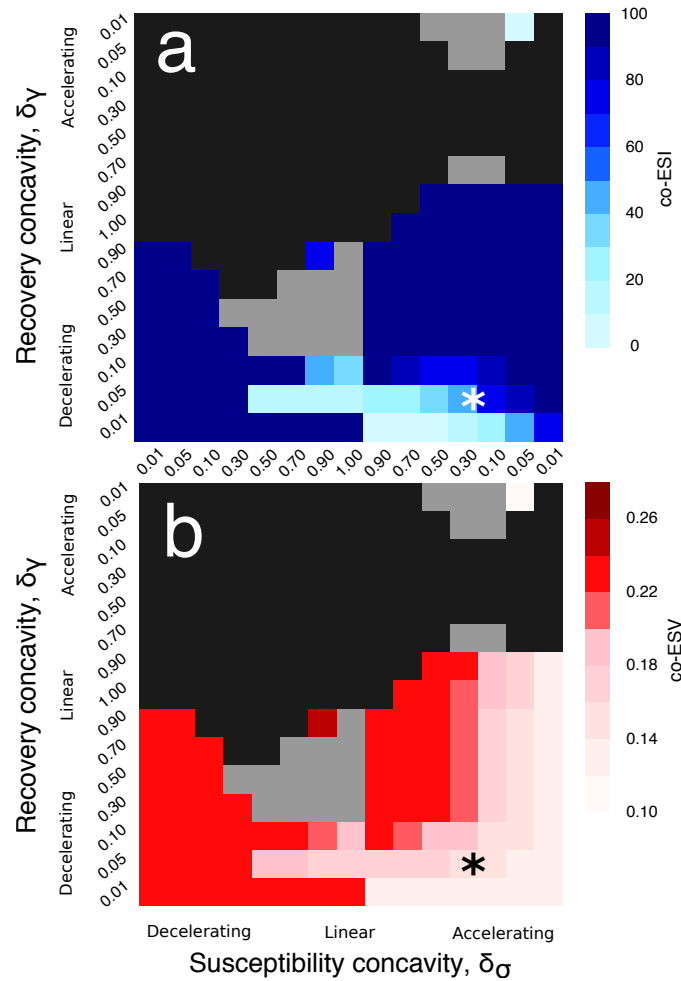


Fig. 4: The trade-off concavity influences the coevolutionary outcome. The shade of blue and red indicates the coevolutionarily stable strategy value of (a) immunosuppression and (b) virulence, respectively. The asterisk (*) indicates the default set of trade-off parameters explored in Figure 2 and 3. The dark grey areas indicate that the coevolutionarily singular strategy is an invasive repeller. The light grey squares indicate that the outcome of coevolutionary stability depends on the details of the rate and variance of mutational inputs of the two coevolving traits.