Phototaxis as a Collective Phenomenon in Cyanobacterial Colonies

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Abstract

Cyanobacteria are a widely distributed, diverse group of photosynthetic bacteria that exhibit 14 phototaxis, or motion in response to light. Cyanobacteria such as Synechocystis sp. secrete 15 a mixture of complex polysaccharides that facilitate cell motion, while their type 4 pili allow 16 them to physically attach to each other. Even though cells can respond individually to light, 17 colonies of such bacteria are observed to move collectively towards the light source in dense 18 finger-like projections. Agent-based models are especially useful in connecting individual cell 19 behaviour with the emergent collective phenomena that arise out of their interactions. We 20 present an agent-based model for cyanobacterial phototaxis that accounts for slime deposition 21 as well as for direct physical links between bacteria, mediated through their type 4 pili. 22 We reproduce the experimentally observed aggregation of cells at the colony boundary as a 23 precursor to finger formation. Our model also describes the changes in colony morphology 24 that occur when the location of the light source is abruptly changed. We find that the overall 25 motion of cells toward light remains relatively unimpaired even if a fraction of them do 26 not sense light, allowing heterogeneous populations to continue to mount a robust collective 27 response to stimuli. Our work suggests that in addition to bio-chemical signalling via diffusible 28 molecules in the context of bacterial quorum-sensing, short-ranged physical interactions may 29 also contribute to collective effects in bacterial motility. 30

Key words

Cyanobacteria, phototaxis, quorum-sensing, active matter, T4P motility

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Introduction

A complex set of sensory and regulatory pathways drive decision-making by micro-organisms. For motile micro-organisms, such processes can result in an overall motion towards or away from a host of stimuli. The most well-examined among these behaviours is chemotaxis, studied extensively in flagellated *Escherichia coli* which swim up (or down) chemical gradients [1]. While chemotaxis is relatively well understood, the mechanisms by which various microorganisms respond similarly to many other types of stimuli [2] including pH changes [3], oxygen [4], osmolarity [5], light [6] and magnetic fields [7] are an area of active research.

Phototaxis, or motion in response to a light stimulus, was first reported over a century ago 41 in eukaryotic photoautotrophs [8–11]. Recent studies on this phenomenon have focused on 42 cyanobacteria or 'blue-green algae', which are a widely distributed, diverse group of oxygenic 43 photosynthetic gram-negative bacteria. The model cyanobacterium Synechocystis sp. PCC 44 6803 displays robust positive phototaxis in which dense finger-like projections of cells emanate 45 from a colony over a period of 1-3 days, and move toward a source of white light. Specific 46 wavelengths of light elicit responses that range from slower moving colony fronts for red and 47 far-red light [12] to negative phototaxis under blue, UV and high light conditions [13]. A 48 wide range of wavelength and intensity-dependent tactic responses to light stimuli have been 49 observed in other cyanobacterial species [12, 14]. 50

A specific set of genes, involved in the production and extrusion of complex polysaccharides 51 ('slime'), are essential for Synechocystis motility [15]. Synechocystis possess multifunctional 52 type 4 pili (T4P) that allow them to attach to substrates as well as other cells. These 53 bacteria exhibit "twitching" or "gliding" motility, involving slime secretion. Gliding motility 54 is slow, with speeds ranging from 0.03 to 0.07 $\mu m/s$ [16]. Such speeds are far slower than 55 typical flagella-mediated motion which occurs at speeds of 20 to 50 μ m/s [17]. Phototaxis in 56 Synechocystis colonies occurs in two distinct phases. Initially, individual cells move toward the 57 edge of the colony closest to the light source, forming a crescent of cells. In a subsequent step, 58 cells move towards the light source in regular, dense finger-like projections (see Fig. 1 of [18]). 59 Studies that track the motion of individual *Synechocystis* cells following the application of 60 a directional light source have shown that such cells initially move towards the light source 61 individually [19]. Subsequently, their motion becomes density-dependent [16]. Cell motion at 62 early times is similar to a random walk motion biased in the direction of the light source. This 63 bias increases as cells aggregate into smaller motile groups, eventually leading to the formation 64 of finger-like projections in which the directional bias is most pronounced. When these fingers 65 intersect with the path of a previously formed finger, the cell speed increases, likely a result of 66 encountering the slime that normally accompanies T4P-mediated motility. That even small 67 aggregations of cells (5-8) exhibit an increased bias in the direction of the light source [16] 68 suggests that the "social" aspect to phototaxis might be mediated by physical connections 69 between cells. Similar social phenomena have been documented in other T4P systems such 70 as Myxococcus xanthus [20, 21]. 71

Recent mathematical models of phototaxis assume that cells move via a random walk ⁷² biased in the direction of a light source. In order to investigate the role that slime plays in ⁷³ phototaxis, these models assume that cells prefer to move on regions of the substrate that ⁷⁴ have already been traversed by other cells, based on observations that fingers break up on ⁷⁵ entering an area with pre-existing slime [16]. This framework has been extended to include ⁷⁶ density-dependent interactions between neighbouring cells [16, 22]. It was shown in a cellular ⁷⁷ automaton model that cell aggregates move collectively towards the light source in finger-like ⁷⁸

projections, a result verified using a stochastic model with similar rules [23]. Other models representation of physical attachments between cells [22, 24, 25]. These models show that allowing frequent detachment and reattachment to neighbouring cells leads to increased aggregation. Varying the range across which cells interact modulates the dynamics of taxis patterns. A recent approach uses a reaction-diffusion model to obtain finger-like projections from the cell colonies extended in the direction of light [26]. Here, slime was modelled in terms of a variation of surface properties, influenced by local cell concentrations.

While these models help to elucidate aspects of the collective motion of cyanobacterial cell 86 colonies in response to light, several important questions remain. For instance, the physical 87 interactions between cells appear to be significant in both the initial stages of aggregation as 88 well as in finger formation. Furthermore, previous agent-based models of phototaxis typically 89 assume cells to be point-like particles, thus preventing an investigation into the effects of 90 density and crowding. A natural background for investigating the collective dynamics of 91 phototaxis is provided by the theoretical framework of active matter systems. Ever since 92 the seminal model of Vicsek *et al.* [27], there have been numerous attempts to describe 93 the motion of large aggregations of self-propelled particles, i.e. units whose movement is 94 driven by an internal energy source [28-30]. This framework has been applied to the study 95 of flocking dynamics, although its simplicity allows it to be utilized across a wide range 96 of systems [31]. With regards to the collective motion of cells arising through taxis, most 97 active matter descriptions have been limited to the context of bacterial swimming. These 98 encompass both run and tumble [32] and active Brownian [33] models: two classes of active 99 particle systems that exhibit similar macroscopic dynamics [34, 35]. However, we know of no 100 comparable description in the context of phototaxis. 101

In this paper, we present an agent-based model for the collective motion of a cyanobacterial 102 colony in the presence of a light source. As detailed in the Methods section, we describe 103 the movement of individual cells, modelled as particles of finite extent, that are initially 104 located within a slime-filled colony. We explicitly consider the role of T4P, as well as of 105 slime deposition, on the resulting dynamics. We assume that cells move randomly with a 106 bias in the direction of a light source, governed by a fixed probability. We investigate how 107 variations in this probability affect the collective dynamics. In addition, we study how the 108 colony behaviour changes upon increasing the fraction of cells that are unable to sense the 109 light source. Such cells effectively act as "freeloaders" that can only move in a directed 110 manner by latching onto cells that can sense light. Our model captures a number of reported 111 observations of cyanobacterial colony behaviour. In addition, its flexibility implies that it 112 can be used to provide predictions for several experimental contexts that have not yet been 113 probed systematically. 114

Methods

Our model simulates a colony of cells, each of which are capable of motion, that reside on ¹¹⁶ a flat substrate. The simulation proceeds by describing how the positions of all cells are to ¹¹⁷ be updated at successive time steps. The motion of cells is biased in the direction of a light ¹¹⁸ source, if it is present, while they move randomly in its absence. As cells move, they secrete ¹¹⁹ slime. The presence of slime reduces the friction encountered by cells as they move across the ¹²⁰ substrate, thus facilitating the motion of other cells across that region. We also assume that ¹²¹ cells experience forces from other cells in their vicinity. These inter-cellular forces account for ¹²²

the collective aspects of phototactic motion.

The cell

We describe each cell as a disc of radius R. Each cell *i* is specified by a two dimensional 125 vector, \mathbf{X}_i , described through the coordinates (x_i, y_i) . At every time step t, each cell can 126 either move via phototaxis in the direction, θ_i^t , of an external light source with probability 127 $p_{\rm photo}$, or in a random direction in the interval $[0, 2\pi]$ with probability $1 - p_{\rm photo}$. Time steps 128 are separated by Δt , which we set to 1. The maximum distance that a cell in a slime-rich 129 background can move in a single time step is a tenth of its radius. In slime-poor backgrounds, 130 the reduced mobility of the cell implies that it moves a smaller distance in the same time. 131

Slime Deposition

We model the secretion of slime by considering a regular square lattice that underlies the cells. The lattice point at row r and column c is specified by (r, c). At each time step, every cell deposits slime. The slime content S^t of the lattice point closest to the cell's centre is thus incremented by an amount S_{rate} :

$$S^{t+1}(r,c) = S^t(r,c) + S_{rate}$$

where S_{rate} is the rate of deposition of slime. $S^t(r,c)$ can increase up to S_{max} , the maximum 133 amount of slime that a grid point can contain. We assume that (i) slime once deposited at a 134 lattice point remains there permanently, i.e. it does not decay, and (ii) slime does not diffuse 135 to neighbouring lattice points. This latter is a valid assumption for a dense gel, given the time 136 scales over which our simulation proceeds. Furthermore this assumption allows, in principle, 137 for the creation of steep gradients in slime content. 138

Cell-cell interactions

The presence of neighbouring cells modulates the direction of motion of a cell. Each cell has 140 a fixed number a of T4P. These pili can attach to other cells lying within a certain distance 141 A of the cell edge (see Fig. 1). We assume that these T4P links are temporary - they break 142 and re-form at each new time step of the simulation - and that each cell can have at most a143 links with other cells. For the duration that a cell pair (i, j) remains attached, cell j exerts a 144 force \mathbf{f}_{ji} on *i* with magnitude K_{ij} that depends on the distance between cell *i* and *j*, D_{ij} , in 145 the following way: 146

$$K_{ij} = (1 + k_1 (\tanh(k_2(D_{ij} - 2R)) - 1)) / a$$

In order to discourage overlaps between cells, we use a sigmoidal form for K_{ij} that is neg-147 ative at short distances, implying a repulsive force. The magnitude of the force is determined 148 by the parameter k_1 , and the division by the parameter a accounts for the fact that each 149 cell distributes its energy across their a pili to exert forces. The parameter k_2 controls the 150 slope of the sigmoidal function, and hence determines how sharply the magnitude of force 151 reduces as inter-cell distance increases. Note that when $D_{ij} < 2R$, i.e. the cells overlap, this 152 functional form results in a repulsive force, which is to be expected. In other words, the force 153 term incorporates soft-core repulsion between cells. The values of k_1 and k_2 were chosen by 154 scanning through the parameter space for finger-like projections (see Fig. S1). 155

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The cell experiences an external force, $\mathbf{F}_i = \sum_j K_{ij} \mathbf{f}_{ij}$ from other cells j in its neighbourhood. In addition, the tendency of the cell to move in the direction θ_i^t is modelled through an additional force $\mathbf{G}_i^t = f_i (\cos \theta_i^t, \sin \theta_i^t)$, where $f_i = 1$. Thus, the force acting on a cell at each time step t is $\mathbf{G}_i^t + \mathbf{F}_i^t$.

Cell movement

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As cell motion is facilitated by the presence of slime, we assume that the motility of a cell ¹⁶¹ at any instant in time depends on the amount of slime at the grid point closest to the cell ¹⁶² centre. The position of each cell is updated at the end of each time step through the equation ¹⁶³ of motion. Hence, the net result of external forces on a cell *i*, over a time interval Δt is a ¹⁶⁴ change in the position of the cell, computed through the expression: ¹⁶⁵

$$\mathbf{X}_{i}^{t+1} = \mathbf{X}_{i}^{t} + \left(\mathbf{G}_{i}^{t} + \mathbf{F}_{i}^{t}\right) / \gamma_{i}^{t},$$

where γ_i^t is a friction factor that is associated with the presence of slime lying below a cell. We assume that:

$$\gamma_i^t = \gamma_0 \, \frac{S_0}{S^t(r,c)} \, .$$

Here, S_0 is the initial slime concentration within the colony while $S^t(r, c)$ is the slime content associated with site (r, c) at time t.

Simulation details

We simulate the dynamics of a cyanobacterial colony containing 500 cells. The cells are 169 initially distributed randomly in space over the extent of a circular or rectangular domain. 170 We assume that the colony has an initially uniform slime distribution, with the slime content 171 set at S_0 for every grid point contained within the domain. We specify the initial positions 172 (x_i^0, y_i^0) of each cell, their initial speeds, $1/\gamma_0$, and the angles θ_i^0 that they would move in if 173 other cells were absent. Unless otherwise indicated, the parameters used are those listed in 174 Table 1.

The length parameters used in these simulations were scaled to the size of a *Synechocystis* 176 cell. These cells are about $1\mu m$ in radius [36], which is assumed to be one length unit in 177 these simulations. Observations of cells under a SEM suggest that the T4Ps can be about 178 four times times the cell radius and that they number about four [37]. The time parameters 179 were scaled to the reported cell speed [38]. We have assumed that the highest cell speeds 180 are obtained under maximum slime conditions. To our knowledge, there have not been any 181 quantitative measurements of slime deposition or a detailed explanation of the mechanism 182 through which slime affects cell speeds. Also, barring a few studies (e.g. [39]) the forces that 183 cells can apply on each other through T4P have not been systematically measured. Hence, 184 our choice of values for the associated parameters (k_1, k_2) was based on an exploration of the 185 parameter space (see Fig. S1). 186

At each iteration of our simulation, we begin by updating the angles θ_i^t of all cells *i*, based on the probability of moving in the direction of light, p_{photo} . We then find the set of all pairs of cells that are within tugging distance and determine which "tugs" occur. Next, we compute the distances between the *x* and *y* projections of all cells to determine the total force exerted by neighbouring cells on each other. The position of each cell is then updated using the equations of motion. At the end of each iteration, cells secrete a unit of slime in the grid point closest to their centre, and we update the slime matrix accordingly. ¹⁹³

Results

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In Fig. 2, the left column displays the positions of cells in an initially circular colony at ¹⁹⁵ different times after the application of light, as indicated in the figure caption. The right ¹⁹⁶ column shows the trajectories of an individual cell, shown in purple against the background ¹⁹⁷ of trajectories of all other cells, shown in grey. ¹⁹⁸

Fig. 2(a) shows the positions of individual cells at a time just after the application of light 199 from a source at the right of the colony. Fig. 2(b) shows the trajectory of a labelled cell for 200 10^3 time steps starting from this initial time. The overall bias of this trajectory towards the 201 light source is obvious, although cells in the bulk feel forces that are largely isotropic from 202 the cells in their vicinity. As Fig. 2(c) shows, cells concentrate into denser circular regions at 203 later times. These cells move collectively towards the light source. The trajectory shown in 204 Fig. 2(d) is now largely straight and directed toward the source. At a still later time, shown 205 in Fig. 2(e), these dense accumulations of cells split off from the main colony although they 206 remain connected to it through a trail of slime. A few isolated cells may remain in the bulk of 207 the finger. The trajectory in Fig. 2(f) illustrates the far more directed motion of a cell within 208 the finger-like protrusion, since it is now confined to a narrow strip of slime (See Movie S1). 209

Fig. 3 depicts properties of the trajectories of individual cells, initiated from a semi-210 infinite aggregate out of which cells move perpendicular to the surface upon application of 211 light. Fig. 3(a) provides a snapshot of a configuration of an initially flat colony of cells moving 212 in response to a light source at infinity, placed to the right of the colony. This is shown for a 213 value of $p_{\rm photo} = 0.1$, with a snapshot at $t = 10^5$ time steps. Fig. 3(b) shows a rose plot of the 214 direction of motion of individual cells obtained in the following way: each cell is tracked across 215 a moving window and the net direction of displacement over five time steps is calculated. The 216 angle this makes with respect to the x-axis is histogrammed and plotted. As can be seen, 217 the anisotropy of the rose plot is indicative of the anisotropy of cellular motion induced by 218 phototaxis towards the light source. 219

Figs. 3(c-d) depict the kymographs of the trajectories of individual cells. The cells at ²²⁰ the boundary of the colony initially move slower than those in the bulk due to the lack of ²²¹ slime in their proximity. As the fingers form and cells in the bulk move towards the surface ²²² their velocities slow to match the cells at the boundary. We see substantial accumulation of ²²³ cells at the boundary before fingers form and extend out of the colony, an indication of the ²²⁴ importance of collective effects triggering finger formation. ²²⁵

Fig. 4 shows the evolution of fingers from an initial flat colony when the probability of 226 moving towards light changes across nearly two orders of magnitude. Surprisingly, even a 227 relatively small bias (Fig. 4(a), $p_{\text{photo}} = 0.01$) produces fingers, although these tend to appear 228 somewhat more disordered than fingers obtained at higher bias (Fig. 4(c), $p_{\text{photo}} = 0.10$ and 229 Fig. 4(e), $p_{\rm photo} = 0.50$). A larger $p_{\rm photo}$ leads to longer, better-defined fingers with a large 230 cell density at the tip. Fig. 4(b,d,f) show the corresponding rose plots of the direction in 231 which cells move. As seen in Fig. 4(f), at large $p_{\rm photo}$, cells mostly move in the direction of 232 the light alone, leading to far more elliptical rose plots compared to the case of small $p_{\rm photo}$. 233 These results suggest that very small p_{photo} can lead to robust phototaxis. 234

It has been observed that cells increase their speed when they encounter regions in which 235

slime has already been laid down. To simulate this, we initiate fingers from a colony allowing 236 them to grow in the direction of light placed towards the right of the colony. After the fingers 237 grow to a certain length, they encounter a band of slime placed normal to the direction of 238 their growth. As seen in Fig. 5(a), after crossing the slime finger growth continues for those 239 fingers that manage to reach the band. In Fig. 5(b) we show kymographs of the trajectories 240 themselves. These show that cells that encounter the band of slime speed up within it before 241 emerging and then move with the same velocity that they had before encountering the slime 242 band (See Movie S2). 243

Fig. 6 shows the evolution of fingers from an initial flat colony that contains a fraction of 244 "freeloaders" mixed with ordinary cells. These freeloaders do not sense light although, they 245 can move and lay down slime. Their net motion towards light can thus only come from being 246 dragged along by cells that do sense light. Our results show that these freeloaders can in fact 247 entrain with cells that sense and move towards light, but the precise details of finger formation 248 and evolution depend both on $p_{\rm photo}$ and the initial concentration of freeloaders $\phi_{\rm ch}$. At small 249 p_{photo} (Fig. 6 (a,d,g)) one finds small and disordered fingers, whereas at intermediate values of 250 $p_{\rm photo} = 0.10$ (Fig. 6(b,e,h)), well developed fingers are observed even at somewhat larger $\phi_{\rm ch}$. 251 If p_{photo} is large (Fig. 6(c,f,i)), entrainment is less successful and we find that the freeloaders 252 can be left behind in the colony, even as normal cells move toward light in fingers. When 253 the tip of a finger comprises both types of cells, we observe that freeloaders tend to cluster 254 towards the back of such tips. 255

The advantage of a simple model is that it provides predictions for more complex cases 256 in which the position of the light source changes over the course of the experiment. We are 257 able to replicate observations of fingers that turn when the source of light is moved [26]. 258 In Fig. 7(a), we show how fingers extend from the colony towards the direction of a source 259 of light, initially placed towards the right of the colony. After these fingers have developed 260 substantially, the position of the light source is changed instantaneously so that light now 261 emanates from a point rotated 90° clockwise from the original position. As can be seen in 262 Fig. 7(b), there is a sharp kink that develops in the fingers as the cells at the tip change their 263 direction of motion so as to follow the light. The fingers now develop and extend in the new 264 direction of light (See Movie S3). 265

Discussion

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Our agent-based model for the phototaxis of *Synechocystis* reproduces prior observations 267 concerning the finger-like projections that form and extend in colonies of motile cells as a 268 phototactic response. The fundamental unit in our model is a single cell which interacts with 269 its environment by sensing light. Two central features of our model are the ability of motile 270 cells to lay down slime, thereby facilitating the motion of cells that subsequently traverse 271 that region, as well as the ability of T4P to mediate the direct physical interaction of cells. 272 These interactions lead to collective behaviour in the form of aggregation and subsequent 273 finger formation, as cells migrate in the direction of light. We suggest that this interaction is 274 central to collective phototaxis. 275

Cell-cell interactions and the ability of cells to self-propel are essential aspects of active 276 matter descriptions of collective cell migration. Our model can be viewed as an extension of 277 studies in which net motion depends on an externally imposed cue, rather than arising from a 278 spontaneous breaking of symmetry. The presence of slime is an ingredient of our model, which 279

appears to have no direct precedent in active matter models. (A possible exception are models 280 for ant trails, which rely on signalling through pheromones laid down by ants that sample 281 multiple paths [40].) The advantage of these and similar mathematical and computational 282 models is that, once benchmarked, they allow us to query aspects of experimental systems 283 that can also be separately examined in targeted experiments (as in [41]). In addition, they 284 allow us to estimate ranges of e.g., force parameters (k_1, k_2) and the slime deposition rate 285 $(S_{\rm rate})$ that can generate fingers reminiscent of ones observed in experiments. Interestingly, 286 relatively small values of $p_{\rm photo}$ appear to be sufficient to generate well-developed fingers; a 287 result that is in agreement with experimental observations [42]. 288

Chemotaxis-like gene clusters in bacteria such as *Synechocystis* have several photorecep-289 tors [12, 43, 44]. These clusters also contain genes involved in signal transduction, including 290 genes that code for signal receptors, response regulators and motility regulators [44, 45]. A 291 number of motility-related genes involved in the biosynthesis and function of pili are required 292 for phototaxis [36, 37, 46]. Genes involved in cAMP regulation have also been shown to be 293 important in phototaxis [47]. Specifically, phototaxis was found to be impaired in colonies 294 of mutants in *cya1* (an adenylate cyclase) and *sycrp1* (a cAMP receptor-like protein), which 295 accumulate near the colony edge closest to a light source but do not extrude outwards in fin-296 gers [18]. We model such mutants as "freeloaders", since they cannot, on their own, exhibit 297 the directional motion characteristic of phototaxis. However, provided the cell-cell interac-298 tions are intact, one can expect that combining a small density of freeloaders with other 299 cells capable of sustained phototaxis might be sufficient to sustain motion of the collective. 300 We have shown that the role of freeloaders, as well as the consequences of a change in light 301 direction, can be examined systematically. 302

Other scenarios can be tested in models and then later investigated through experiments. 303 These include effects of multiple light sources and wavelengths, as well as finger formation in 304 mutants that cannot either move or produce slime. Whether such taxis mutants might lead 305 to different architectures of colonies remains to be fully explored. In principle, expanding this 306 model further to include a quantification of fitness might also allow us to address evolutionary 307 questions, such as whether a fraction of freeloaders can persist in mixed populations over 308 several generations. Finally, we note that the term quorum-sensing is conventionally applied 309 to a situation where a commonly sensed biochemical signal crosses an activation threshold. 310 Thus, quorum-sensing is at its core a collective process. Phototaxis as discussed here also 311 embodies a collective effect in the TFP-mediated cell-to-cell interaction as well as slime-312 mediated interactions. For this reason it may be worth exploring other contexts for quorum-313 sensing that emphasize its origins in collective, especially physical interactions, and nonlinear 314 response. 315

In conclusion, we have developed a model for phototaxis in *Synechocystis* colonies which 316 incorporates several features that underlie collective motion in systems of this nature. Our 317 model describes the movement of individual cells, each having a finite volume and capable of 318 detecting light. Cell motion is accompanied by the deposition of slime that serves to reduces 319 friction. The role of T4P is captured in our model by allowing cells to attach to neighbours, 320 and exert forces on them. We observe that the collective behaviour is characterized by cells 321 aggregating into small clusters that first accumulate at the edge of the colony. These clusters 322 then extrude towards the light source in finger-like projections, reminiscent of recent exper-323 imental observations. We find that these projections occur even when the bias of individual 324 cell motion towards light is very small, and also in situations where some fraction of the 325 colony consists of freeloaders that do not sense the direction of the light source. Further 326

improvements of our model would involve the coupling of the systems biology of light-sensing with our physical model for cyanobacterial motility. 328

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Tables

Parameter	Quantity	Value
R	cell radius	1
A	appendage length	4R
a	number of appendages per cell	4
γ_0	inverse of initial cell speed	1/(0.1 R)
(k_1, k_2)	force parameters	(1, 2)
S_0	initial slime within colony	1000
$S_{ m max}$	maximum slime a grid point can contain	1000
S_{rate}	slime deposition rate	0.1
p_{photo}	phototaxis probability	0.1
$\phi_{ m ch}$	proportion of freeloaders	0
ρ	average colony density	0.05

Table 1: Parameters used in simulations (unless mentioned otherwise)

Figures



Figure 1: Schematic of simulation system (a) Cells are represented as green spheres of radius R. The amount of slime is proportional to the intensity of background colour (darker implying more slime). Cells can attach to other cells through TFP, which can extend to length A. (b) In the presence of a distant light source (indicated by a star), the colony morphology gradually changes.

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Figure 2: Finger formation and individual cell paths at different stages The left column displays the position of each cell, indicated by green markers, while the concentration of slime is proportional to the intensity of colour (darker implying more slime). (a) At t = 0, the cells lie within a circular colony. In the presence of a light source placed at infinity (to the right of the colony), the colony morphology gradually changes. (c) At around $t = 8 \times 10^3$ finger like projections begin to form. (e) As seen from this snapshot at $t = 50 \times 10^3$, smaller projections can merge over time to form larger, well-defined projections. The right column displays the path of a representative cell (purple) and those of surrounding cells (gray) over an interval of 10^3 steps. The thick lines represent the spatial scales of each of the panels (which is identical in both x and y directions), and their extent is denoted by the corresponding number on top. The cases shown are for (b) the initial trajectory ($t = 0-10^3$), (d) early finger formation ($t = 8 \times 10^3-9 \times 10^3$), and (f) late finger formation ($t = 5 \times 10^4-5.1 \times 10^4$).



Figure 3: Phototaxis in the direction of light (a) Snapshot of a flat colony of cells that move towards a light source placed at infinity (to the right of the colony) corresponding to a value of $p_{\text{photo}} = 0.1$ at $t = 10^5$. (b) Corresponding rose plots for the net directions of the cells, (calculated over 5 time steps). (c-d) Trajectories of individual cells over time, with two randomly chosen cells coloured distinctly to illustrate characteristic paths. (c) The *x*component of the trajectories, with the edge of the colony indicated by a dashed line. (d) The *y*-component of the trajectories, showing finger formation.



Figure 4: Robust phototaxis can occur even with a small bias for moving in the direction of light The left column displays snapshots of flat colonies at $t = 10^5$ for three different choices of p_{photo} , namely (a) $p_{\text{photo}} = 0$, (c) $p_{\text{photo}} = 0.01$ and (e) $p_{\text{photo}} = 0.5$. We see that fingers can form even for very low p_{photo} . The right column displays the corresponding rose plots for the net directions of the cells, (calculated over 5 time steps) showing that directed motion is enhanced at higher p_{photo} .



Figure 5: **Movement of fingers through a slime band:**(a) Motion of fingers through a slime band after extending from a flat colony. (b) Kymograph of cells indicating how velocities increase when cells in fingers encounter a pre-existing band of slime.



Figure 6: "Freeloaders" that do not sense light can also move toward light through entrainment: Snapshots of the colonies at $t = 10^5$ for a range of p_{photo} and for different ratios of cells that do not sense the direction of light (freeloaders, at a fraction ϕ_{ch} of the total number of cells, represented in red). We consider the cases (a-c) $\phi_{\text{ch}} = 0.1$, (d-f) $\phi_{\text{ch}} = 0.5$, and (g-i) $\phi_{\text{ch}} = 0.9$. For each of these values of ϕ_{ch} , we show snapshots for (a, d, g) $p_{\text{photo}} = 0.01$, (b, e, h) $p_{\text{photo}} = 0.1$ and (c, f, i) $p_{\text{photo}} = 0.5$. Fingers can be observed even for high values of ϕ_{ch} , especially for high values of p_{photo} . We observe that freeloaders cluster towards the back of the tips of fingers.



Figure 7: Changing the direction of light: Cells in a colony of density $\rho = 0.2$ move toward a light source to the right until $t = 2 \times 10^5$ at which time the position of light source is moved 90° clockwise. The cells reorient themselves and start moving toward the new direction of light. (a) Snapshot at $t = 2 \times 10^5$ (b) Snapshot at $t = 2.5 \times 10^5$.