Title: Environmental anchoring of grid-like representations minimizes spatial uncertainty during navigation

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17 Summary

Minimizing spatial uncertainty is essential for navigation, but the neural mechanisms remain 18 elusive. Here we combine predictions of a simulated grid cell system with behavioural and 19 20 fMRI measures in humans during virtual navigation. First, we showed that polarising cues produce anisotropy in motion parallax. Secondly, we simulated entorhinal grid cells in an 21 22 environment with anisotropic information and found that self-location is decoded best when grid-patterns are aligned with the axis of greatest information. Thirdly, when exposing human 23 24 participants to polarised virtual reality environments, we found that navigation performance is 25 anisotropic, in line with the use of parallax. Eye movements showed that participants 26 preferentially viewed polarising cues, which correlated with navigation performance. Finally, 27 using fMRI we found that the orientation of grid-cell-like representations in entorhinal cortex anchored to the environmental axis of greatest parallax information, orthogonal to the 28 polarisation axis. In sum, we demonstrate a crucial role of the entorhinal grid system in 29 30 reducing uncertainty in representations of self-location and find evidence for adaptive spatial 31 computations underlying entorhinal representations in service of optimal navigation. 32 33 Keywords: spatial navigation; grid cells; computational modeling; virtual reality; fMRI; eye-

- 34 tracking.
- 35

36 INTRODUCTION

Accurate navigation is a daily challenge for humans and other animals alike. In order to self-37 localise an agent must integrate incomplete and uncertain information regarding its position 38 39 and motion. In the brain, entorhinal grid cells are thought to play a central role in this process^{1–6} – appearing to provide an efficient representation of self-location updated on the 40 41 basis of self-motion and the proximity to salient cues. However, while sensory 42 representations - such as those found in the visual cortex - are known to adapt in response to varying levels of uncertainty^{7,8}, it is unknown whether spatial representations in the medial 43 44 temporal lobes respond similarly. 45 In rodents, the regular triangular firing-patterns of grid cells can be heavily distorted by 46 environmental geometry - tending to align to walls of rectangular enclosures^{9,10}. It becomes 47 fragmented in hair-pin mazes and distorted in trapezoidal environments^{10,11}, which translates 48 into systematic memory distortions in humans¹². Human entorhinal fMRI- and iEEG activity 49 50 during virtual navigation is modulated by movement direction. This modulation shows six-fold rotational (hexadirectional) symmetry that has been proposed as a population signal of grid 51 cells (i.e. grid-cell-like representations)^{13–20}. These grid-cell-like representations are present 52 also during visual exploration and anchor to square boundaries^{16,17}. Similar activity patterns 53 have been observed in monkeys during visual tasks²¹. 54

55

Currently, it is unclear whether these distortions are maladaptive - a failed attempt to 56 generate a regular grid, which might conceivably result in navigational errors²². However, an 57 58 alternative explanation could be that the irregularities confer an advantage, supporting more accurate self-localisation than regular grid-patterns would. Indeed, theoretical considerations 59 suggest that the transient expansion in grid scale observed when animals are exposed to 60 novel enclosures²³ may be a strategy to minimise decoding errors in unfamiliar and hence 61 uncertain environments². Plausibly similar adaptive processes would generate altered grid-62 patterns in response to asymmetries or local variability in the availability of reliable spatial 63 64 cues.

65

Here, we test if polarised spatial cues – providing anisotropic motion parallax information during self-motion - systematically alter the configuration of grid-like representations in a way that is consistent with the minimisation of decoding errors. To this end, we employed a simulated grid cell system to make specific predictions about the optimal orientation of gridpatterns under conditions of asymmetric spatial information. In turn, we tested these predictions against the orientation of human grid-cell-like representations monitored while human subjects performed a virtual navigation task. Eye-tracking data and behavioural

performance measures were used to assess the participants' use of spatial cues and their
 ability to navigate accurately within the VR.

75

76 **RESULTS**

77 Impact of environmental geometry on grid pattern may be adaptive

Computational simulations suggest that grid cell firing patterns can partially mitigate the 78 effects of increased spatial uncertainty by increasing in scale² – an effect observed 79 empirically in novel environments ²³. We build on this existing framework ^{2,4}, inquiring how 80 position decoding using a population of grid cells with coherent orientation is affected by 81 anisotropy in spatial uncertainty (random displacement of each grid pattern along a cardinal 82 axis). Grid cell ensembles with an orientation offset at 0 to 30° relative to the axis of greater 83 uncertainty were simulated (in a six-fold rotational system 30° is the greatest possible 84 85 offset). 86 The simulations (see Materials and Methods) demonstrated a substantial difference in the 87 accuracy with which self-location can be decoded depending on the orientation of the grid 88

89 pattern relative to the axis of greatest uncertainty. Specifically, the most accurate

representation of position was obtained when the grid population was oriented at 30° to the

91 axis - equivalent to being fully misaligned to the axis defined by the spatial cues; Figure 1C,

92 Figure 1 – figure supplement 1-3). Decreasing the anisotropy in spatial uncertainty

93 diminished this effect, until no directional benefit was apparent for isotropic uncertainty – a

spherical noise distributions (Figure 1 and Figure 1 – figure supplement 1). In further control

95 experiments, we varied grid scale, firing rate, and the number of grid modules – the optimal

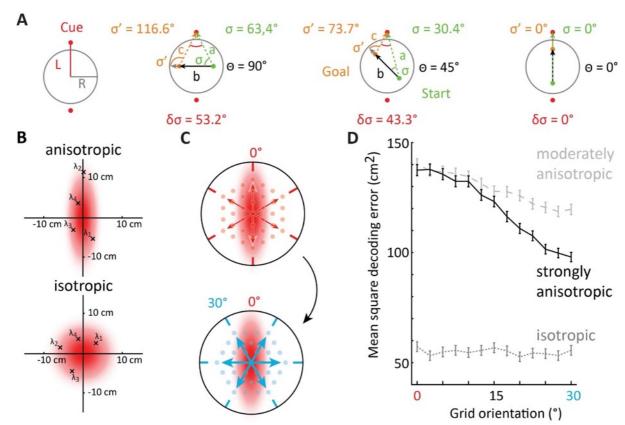
96 grid orientation relative to an axis of uncertainty remained consistent (Figure 1 – figure

supplement 2). Similarly, in the case of less plausible, higher-order noise distributions with

98 multiple peaks, an optimal grid orientation was only present if the alignment of the grid

99 pattern and the noise distribution could be reduced through rotation. This was the case for a

six-leaf distribution, but not for a four-leaf distribution (Figure 1 – figure supplement 3).





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104 Figure 1. Spatial information is anisotropic and affects optimal self-localisation using grid cells. A Spatial 105 information during movement in polarised environments is anisotropic. Left: schematic of arena with radius R, 106 and polarising cues at distance L. Right: three example paths in different directions and through the centre are 107 shown (black arrows at angle θ ; Path lengths are equal to distance of the cue to the centre). The change in cue 108 direction from the observer's heading ($\delta\sigma$) is maximal on paths perpendicular to the polarisation axis (note: this is 109 also the case on average if paths are not centred on the middle but distributed evenly throughout the 110 environment). B-D We simulated decoding of position estimates from the activity of grid cell ensembles with 111 patterns oriented at different angles relative to the axis of lowest spatial certainty. Note that the axis of lowest 112 spatial certainty in A is the polarisation axis formed by the two cues, because angular change is smallest and 113 triangulation errors are largest along it. Uncertainty in spatial information for the simulations of position decoding 114 using grid cells was introduced by adding Gaussian errors to the true position input. These errors were generated 115 independently for each module of grid cells. Anisotropy was created by separately varying the standard 116 deviations of the error in two orthogonal axes. B illustrates an example: the subject's actual location is at the 117 origin; red shading indicates a two-dimensional probability density distribution for error generation, with either 118 different or equal standard deviations in each axis (anisotropic and isotropic, respectively); and crosses indicate 119 four independently generated noisy position estimates, drawn from this distribution and be input to each of the 120 grid cell system's four modules. C Schematic illustration of two grid orientations either aligned with the 121 uncertainty axis (left panel, arrows indicate hexadirectional orientations associated with a grid), or rotated 30° 122 (right panel). The number of depicted grid fields differ only for illustration purpose. D Position decoding error, 123 defined as the mean maximum-likelihood estimate square error (MMLE; cm²), was largest when one grid axis 124 was aligned at 0° relative to the axis of lowest spatial certainty (as shown in panel B, top). No optimal grid 125 orientation was present in the isotropic condition. Solid black line: 'strongly anisotropic', errors with s.d. 5cm and 126 0cm; dashed light grey line: 'moderately anisotropic', 5cm and 1.67cm; dotted medium grey line: 'isotropic',

3.33cm in all directions. Grid orientation is defined as the minimal angular offset of a grid axis from the axis of
 greater uncertainty (this is analogous to hexadirectional offset of entorhinal fMRI activity described below). Error
 bars indicate 95% confidence interval (n=150,000).

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131 Motion parallax is maximal during movement perpendicular to polarising cues

To investigate the effects of uncertainty on grid cells and navigation, we first sought to
generate a virtual environment characterised by anisotropic spatial information. Because
motion parallax - the apparent change in bearing to stationary points - is a major source of

- spatial information during movement²⁴, we reasoned that an enclosure with cues distributed
- along a single axis would exhibit the desired asymmetry. Below we characterise an
- anisotropy of such angular change in polarised environments.
- 138

Suppose we have a circular arena of radius *R* centred on the origin, with a polarising cue at distance *L* (Figure 1A). As an agent moves on a straight path b, we are interested in the angle σ from the agent's heading to the cue, and how it changes when the agent moves. If the cue is within the arena (L<R), then the maximal change in angle (π radians) occurs when the agent moves towards and through the cue. If the cue is outside the arena (L>R), and the length of the path is very short (i.e. in the limit b \rightarrow 0) we can calculate the change in angle $\delta\sigma$ to the cue (see Figure 1A, middle panel for example illustration with a longer path):

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147

$$\frac{\delta\sigma}{b} = \frac{\sin\sigma}{a} \tag{1}$$

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149 If the agent is on the x axis (i.e. y = 0) then we see that $\delta \sigma$ is proportional to $\sin \sigma$ which is 150 maximal for paths at $\theta = \frac{\pi}{2}$, i.e. movements perpendicular (90°) to the cue.

Hence, spatial information during movement is not isotropic across directions (this
conclusion holds on average for the entire arena). Specifically, angular change is maximal
during movement perpendicular to polarising cues. Spatial computations, such as Euclidean
triangulation, benefit from this parallax information and become more noise resilient (Figure
1 – figure supplement 4-6).

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To corroborate this analysis, we conducted biologically inspired simulations of Euclidean
triangulation in polarised environments (see Methods). As expected, the impact of spatial
uncertainty was minimised for movement perpendicular to the polarisation axis (Figure 1 –
figure supplement 4-6; two-sided Wilcoxon signed-rank test: Z= 1026.42, p<0.001). Results
were robust within a plausible range of parameters.

163 Hence, in a circular environment polarised by two cues, the axis of greatest uncertainty

164 corresponds to movement parallel to the axis defined by the cues. Thus, we would expect to

- 165 observer larger errors in spatial memory responses in this direction than perpendicular to it.
- 166 Conversely, to minimise positional errors, grid-patterns should orient to lie perpendicular to
- 167 the polarisation axis.
- 168

169 Effects of motion parallax on behavioural distance estimation

170 To test if participants can use anisotropic parallax information to improve distance estimates,

171 we conducted a behavioural distance estimation task (N=20). In a sparse environment

172 (Figure 2A, Figure 2 – figure supplement 1) polarised by two cues defining an axis,

173 participants freely navigated to a start location. There they could initiate forward teleportation

along one of three directions (- 30° , 0° and + 30° relative to the polarisation axis; Angles < 90°

were chosen to allow testing of many distances with limited field-of-view, see Materials and

176 Methods; Figure 2B; Figure 2 – figure supplement 1). At the goal location they gave an

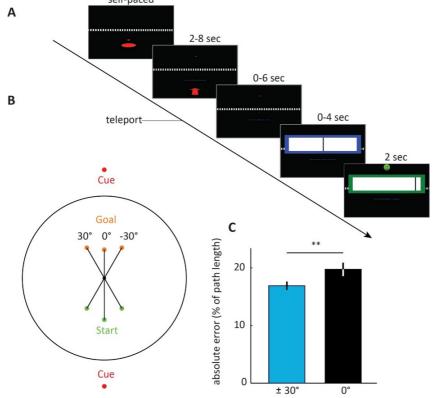
177 estimate of the traversed distance (Figure 2A, see Materials and Methods). As predicted,

178 performance was most accurate when motion parallax was present. That is, when

participants moved ±30° oblique to the polarisation axis, as opposed to along it. Figure 2C,

absolute error, paired, two-sided t-test N=20, T (19) = 2.7, p=0.007; Figure 2 – figure







183 Figure 2. Behavioural experiment - distance estimation is most accurate on oblique paths. A Trial event

184 sequence. Following a familiarisation phase, participants navigated to a start location (indicated by the red circle

and arrow) and initiated teleportation in a given direction, either along a polarisation axis or at ±30° offset, see B

185 186 and Figure 2- figure supplement 1. Teleportation distance was experimentally manipulated, and participants 187 gave a distance estimate at the goal location by sliding a response bar (black slider in blue box). The cue was 188 visible both at the start and the goal location (small red dot at eye height, in this example trial shown at the 189 direction the arrow is pointing). Subsequently, participants received feedback. B Schematic of the three possible 190 path angles shown at the same distance. Path distance varied from trial to trial (see Materials and Methods). 191 Note that no boundary was present. The black circle only illustrates an analogy to the arena environments used 192 in the fMRI experiments. Start and goal positions are illustrated by green and orange dots, respectively. C 193 Distance estimation was most accurate on oblique paths, consistent with anisotropy of spatial information. Error

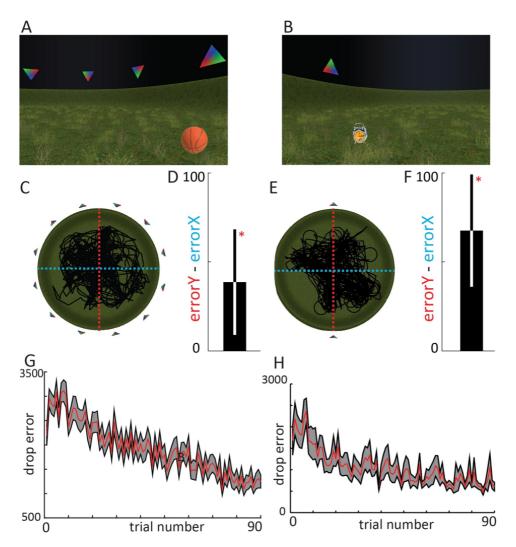
- 194 bars show S.E.M. over participants.
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Polarised environments affect spatial navigation error 196

197 In order to test the effects of polarising cues in more naturalistic settings, we conducted

navigation tasks in two distinct virtual environments (environment 1: N=50: environment 2) 198

- 199 N=24). Both environments contained a grassy plain bounded by a cylindrical cliff,
- surrounded by polarising extra-maze cues (Figure 3). In environment 1, highly similar extra 200
- 201 maze cues were visible in all direction (12 in total), but these changed orientation at two
- 202 opposing points. These inversion points constituted a polarisation axis. A subset of
- 203 participants that navigated in environment 1 underwent concurrent fMRI scanning (fMRI
- 204 experiment 1; N=26), while another subset underwent concurrent eye tracking (eye tracking
- 205 experiment: N=34). Environment 2 was more clearly polarised by a single cue on either side
- (see Figure 3 and Materials and Methods), with participants undergoing concurrent fMRI 206
- scanning (fMRI experiment 2; N=24). In each environment, participants performed a 207
- continuous object-location memory task^{13,19} with 6 or 4 object-location associations (see 208
- Materials and Methods). Each trial comprised navigating to a target location participants 209
- were able to move forward and rotate but not move backward giving a response, and 210
- receiving feedback. This task was interrupted by occasional inter-trial-intervals when a 211
- fixation cross was presented on a grey screen for 2 seconds (on average after every third 212
- trial; range: 2-4). Object identity and location was randomised across participants (see 213
- 214 Materials and Methods).
- 215
- 216



218 Figure 3. Spatial memory performance is anisotropic. Top First-person view A environment 1 (used in fMRI 219 experiment 1, and the eve-tracking experiment), B environment 2 (used in fMRI experiment 2). C, E aerial view. 220 Human participants performed a free-navigation, object-location memory task (one example object shown on 221 grassy plane, see Materials and Methods). In environment 1 an implicit polarisation axis was defined through the 222 configuration of cues, i.e. the switch between upright and downward triangles. environment 2, an explicit 223 polarisation axis was defined with two triangular cues alone. Black lines in aerial view show the paths of 224 exemplary participants. Red dashed line indicates the polarisation axis (Y dimension), whereas the cyan dashed 225 line indicates the orthogonal X dimension. D, F Bars show the median difference in spatial memory performance 226 on the Y axis (i.e. the polarisation axis) versus the X axis. To avoid potential bias, we matched the number of 227 trials in which participants faced (or moved) parallel and perpendicular to the polarisation axis (±45°). Spatial 228 memory performance was anisotropic, with larger errors along the polarisation axis in both environments, which 229 corroborates the theoretical predictions of an anisotropy in spatial information (Equation 1, Figure 1 and Figure 1 230 - figure supplement 4). Bottom Error bars show S.E.M. over participants.

231

- 232 Despite a relatively sparse environment, participants successfully learnt the object locations
- 233 (Figure 3 figure supplement 1). To avoid potential bias of the anisotropy measure due to
- the limitation of navigating using only three buttons, we matched the number of trials in
- which participants faced (or moved) parallel (y-axis) and perpendicular (x-axis) to the

polarisation axis ±45° at the time of the spatial response (median difference in number of 236 trials facing Y - number of trials facing X: environment 1 = 2; environment 2 = 16). We tested 237 if participants' spatial responses were more accurate when given perpendicular to the 238 239 polarisation axes than in parallel with it, as predicted by the anisotropy in angular change information (Figure 3). To this end, for environment 1, we employed a linear mixed-effects 240 regression model using the Imer function from the Ime4 statistics package²⁵ implemented in 241 R 3.5.1 (R Core Team, 2018). As fixed effects, we tested the intercept of the effect of the 242 median X error on the median Y error. As random effects, we used intercepts for the factor 243 experiment with two levels (fMRI experiment 1 and eye tracking experiment; One-sided test; 244 $T_{(57)} = 1.812$, p=0.0376; Median percentage of X error relative to Y error = 3.8 %). 245

246

For environment 2, we employed a paired one-sided t-test (T₍₂₃₎=2.1441: p=0.02141;

248 Median percentage of X error relative to Y error = -15.2%). Participants' spatial memory

249 performance in both environments hence indicated that movement directions parallel to the

250 polarisation axes were associated with low spatial certainty. Next, we asked if participants'

viewing behaviour would reflect increased exploration of more informative cues.

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253 Polarising cues are viewed for longer

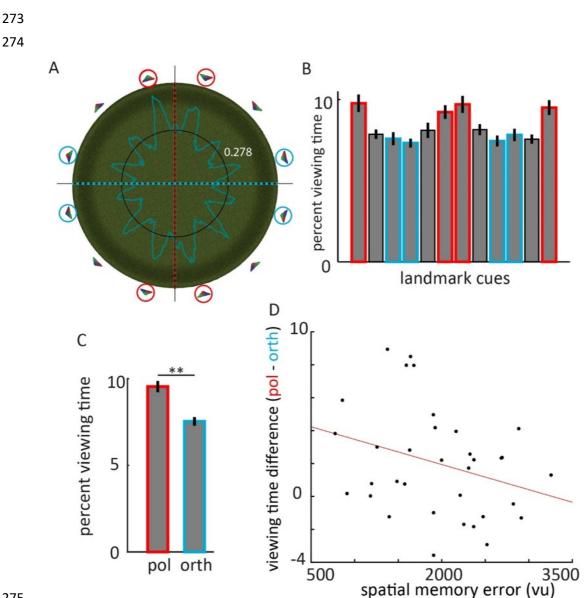
We asked next if participant's viewing behaviour would reflect the use of the polarisation 254 axis. Notably, the visual appearance of all cues was matched and cannot explain any 255 potential viewing time differences. We examined these potential differences in viewing times 256 257 between cues using a repeated-measures ANOVA. Indeed, average percent viewing time 258 differed between cues (Figure 4; F (11) = 4.98, p<0.0001, n=34). However, our specific hypothesis was that the configural cues forming the polarisation axis (i.e. two pairs of cues of 259 260 opposite orientation) were the ones most viewed and informative for navigation behaviour. A one-tailed paired t-test revealed that the configural landmarks were indeed viewed longer 261 than the ones orthogonal to the polarisation axis ($T_{(33)}$ = 3.60, p=0.0005). This reliance on 262

- 263 polarising cues correlated with spatial memory performance across participants. In
- 264 particular, the difference in viewing time of polarising cues versus orthogonal cues correlated
- negatively with participant's mean spatial memory error (Figure 4D. Pearson correlation, one sided, R = -0.2997, P = 0.0425).
- 267 The longer viewing times of the polarising cues and the correlation with spatial memory

strongly suggests that they were key elements for. If hexadirectional activity as an index of

269 grid-cell-like representations would exhibit a preferred orientation orthogonal to the

- 270 polarisation axis, this would provide evidence for an adaptive nature of the impact of
- environmental geometry on the grid pattern.
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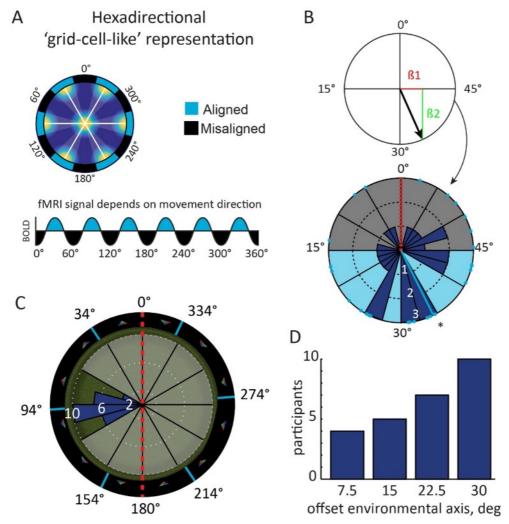


276 Figure 4. Eye tracking experiment - Participant's behaviour in the '12 cue' environment (used in fMRI 277 experiment 1 and the eye tracking experiment) reflects stronger reliance on the polarising cues. A Percent 278 viewing time is plotted for fixations of 360 evenly spaced points on the boundary of the arena defined by the 279 surface of the cues. Black circle: chance level of even distribution of viewing time across all points. Cues marked 280 with red circles constitute the polarisation axis, cues marked with cyan are perpendicular to the polarisation axis. 281 B Bars show average percent viewing time in 30° wide bins that were centered on each of the 12 cues. C 282 Participants viewed the cues that form the polarisation axis longer than those perpendicular. D Spatial memory 283 error correlated with the difference in viewing time of polarising cues versus orthogonal cues. Error bars show 284 S.E.M. over participants.

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Grid-cell-like representation orient to misalign with an axis of high spatial uncertainty
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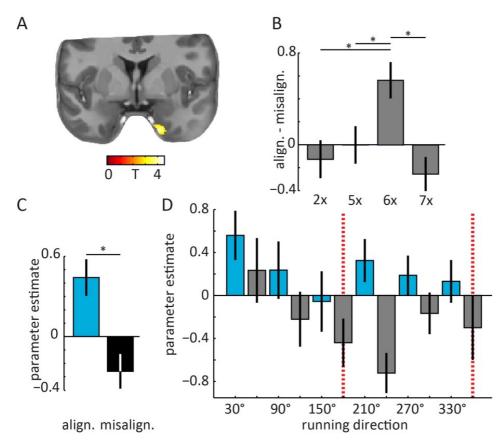
- To examine how grid-cell-like representations orient in simple polarised environments, we 287
- estimated hexadirectional entorhinal activity ^{13,15,19} for each participant. In brief, the method 288
- takes advantage of a six-fold periodic directional modulation of fMRI activity in entorhinal 289
- 290 cortex during virtual movement (see Materials and Methods). First, we estimated individual

orientations of hexadirectional entorhinal activity on the first half of the data. These 291 292 orientations were not randomly distributed, but clustered approximately perpendicular to an axis defined by the configural cues (fMRI experiment 1, Figure 5). The absolute angle to the 293 294 nearest 'grid axis' was approximately 30°, corresponding to maximum mis-alignment. Circular mean = 34°; Figure 5C-D; N=26, circular V test for deviation from homogeneity 295 perpendicular to the polarisation axis: V=6.68, p=0.032). Note that low-level visual features 296 297 were equal in all viewing directions. Second, we performed a whole-brain analysis on the second half of the data. This confirmed that activity in right entorhinal cortex was increased 298 for runs at periods of 60° aligned with the orientation identified from the first half of that data 299 300 (Figure 6A-D, peak voxel t-test, T₍₂₅₎ =4.44, p=0.034, small-volume FWE-corrected). Consistent with the presence of grid-cell-like representations, runs aligned versus misaligned 301 302 show largest activity increase for 6-fold rotational symmetry but not for biologically implausible control models of 5- or 7-fold rotational symmetry (repeated-measures ANOVA: 303 304 F(3,25) = 8.3, p < 0.001; Post-hoc, paired t-tests with Holm-Bonferroni correction, * p<0.05). 305 No other peaks remained across the cerebrum even at more liberal thresholds (p<0.001 uncorrected; T>3.45) and neither was there a notable circular clustering of hexadirectional 306 307 activity in 2 control regions (mammillary bodies, which are close to the hippocampal formation: V test: V=3.33, p=0.822; right, primary visual cortex: V test: V=0.10, p=0.489; See 308 309 Materials and Methods). 310



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313 Figure 5. Hexadirectional activity in entorhinal cortex aligns perpendicular to the polarisation axis. A Hypothesis: movement parallel with the axes of grid cells is associated with increased fMRI BOLD signal ^{16,19}; B 314 315 Top: Analysis procedure: the preferred orientation of hexadirectional fMRI activity in the entorhinal cortex was 316 estimated by first fitting a general linear model (GLM) to the data with 60°-periodic sine and cosine regressors. 317 This yields the associated parameter estimates ß1 and ß2, respectively. The preferred orientation in 60°-space 318 (black arrow) can be derived from ß1 and ß2 (see Materials and Methods). The corresponding preferred orientation of hexadirectional activity in 360°-space can then be deduced. Here, this corresponds to multiples of 319 320 60° centered on 34° (light blue lines in C) relative to the polarisation axis (red dashed line) at 0°. B Bottom: 321 Individual, preferred orientations in 60°-space (light blue dots) in right entorhinal cortex clustered at roughly 30° 322 offset relative to the polarisation axis (red dashed line); mean orientation = 34° (light blue line). C Histogram of 323 preferred hexadirectional activity plotted in full circular space (360°). Note that one of the hexadirectional axes 324 (light blue lines) is roughly orthogonal to the polarisation axis (red dashed line), in line with optimal angles for self-325 localisation (Figure 1D) D Absolute angle between nearest axis of hexadirectional activity shown in B and the 326 polarisation axis illustrate a tendency towards maximal misalignment. Note that the maximum offset is 30° due to 327 the 60° periodicity of hexadirectional activity. 328 329 330



332 Figure 6 Cross-validation of hexadirectional activity in entorhinal cortex and control models. A A whole-333 brain cross-validation confirmed that entorhinal activity was increased on runs aligned with the predicted grid (i.e. 334 runs in 30°-wide bins centred on 30°, 90°, 150° etc. indicated by light blue arrows in C and D; see Materials and 335 Methods for details). Peak voxel t-test, T(25)=4.44, p=0.034, small-volume FWE-corrected). Image is thresholded 336 at p<0.001 uncorrected for display purpose. Across the cerebrum no other peaks were observed at this 337 threshold. The T statistic (colour bar) is overlaid on the structural template. B In agreement with grid-cell-like 338 representations, runs aligned versus misaligned show largest activity increase for 6-fold (6x) rotational symmetry 339 but not for biologically implausible control models. Next to 5- and 7-fold rotational symmetry, 2-fold symmetry was 340 tested to rule out a direct effect of running parallel to the polarisation axis or not. For all analyses the aligned 341 condition was centered at an angle equivalent to 90° from the polarisation axis (e.g. 30° for 6-fold symmetry). C 342 Parameter estimates of runs aligned (light blue, see schematic grid in Figure 1C right panel) and misaligned 343 (black) with the predicted hexadirectional orientation extracted from the peak voxel in A. D To examine the 344 influence of different running directions, we plotted the parameter estimates for separate regressors of 12 345 directional across the entire time-series of fMRI data from the peak-voxel in A. Note the alternating pattern of 346 activity aligned and misaligned. Red dashed lines indicates the polarisation axis. Bars show means and S. E. M. 347 across participants. 348

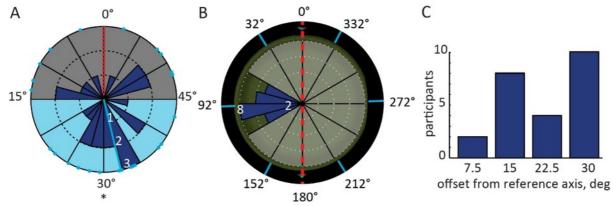
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To test if the environmental anchoring depends on the configural cues, we scanned another group of participants in an environment with a non-configural, polarisation axis consisting of only two extra-maze cues (fMRI experiment 2). We estimated individual orientations of hexadirectional activity, and again found that they clustered perpendicular to the polarisation axis (circular mean = 32.28°; Figure 7) replicating the findings from the first experiment

(N=24, circular V test: V = 5.95, p=0.043; Figure 7). Sampling of running directions could not 355 explain these effects in either experiment (Figure 3 – figure supplement 1). In sum, the 356 results from fMRI experiment 1 and the replication in fMRI experiment 2 provide converging 357 358 evidence that the preferred orientation of hexadirectional activity in entorhinal cortex depends on navigation-relevant, polarising cues, independent of the specific type of cue 359 (configural or non-configural). The orthogonal arrangement of hexadirectional activity, as an 360 index of grid-cell-like representations, is in agreement with optimal activity patterns of 361 simulated grid cells for self-localisation, suggesting that the impact of environmental 362 geometry on grid cells may be adaptive. 363 364

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366 367 Figure 7. Environmental effects on hexadirectional activity in fMRI experiment 2. A Preferred 368 hexadirectional activity in 60°-space (light blue dots) in right entorhinal cortex clustered at roughly 30° offset 369 relative to the polarisation axis (mean orientation = 32.28°; light blue line), in line with optimal angles for self-370 localisation (Figure 1D) B Histogram of preferred hexadirectional orientations plotted in full circular space (360°) 371 onto a top-down view of the arena. Note that one of the putative grid axes (light blue lines) is roughly orthogonal 372 to the polarisation axis (red dashed line). C Absolute angle between nearest axis of hexadirectional activity 373 shown in B and the polarisation axis. Note that the maximum offset is 30° due to the 60° periodicity of 374 hexadirectional activity. 375

376 **DISCUSSION**

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We examined the effects of polarising cues on spatial navigation behaviour and grid-cell-like representations. We found that estimation of movement distance in a virtual environment was least accurate when participants moved along a polarisation axis and no motion parallax was present. Likewise, spatial memory performance in free-navigation, object-location memory tasks in polarised environments showed relatively larger errors parallel to the polarisation axes (i.e. anisotropy). Eye-tracking recordings indicated that participants viewed polarising cues for longer than other cues, which correlated with their spatial memory

385 performance.

To test the theoretical implications of anisotropic spatial information on a system of grid cells, 386 387 we used biologically inspired simulations. We demonstrate that the representation of selflocation is most accurate when grid-patterns align with the axis of highest spatial information. 388 Motion induced parallax is a source of navigation-relevant information^{24,26} and lies at the 389 heart of surveying unknown terrain for the creation of spatial maps. With respect to parallax, 390 the optimal grid-pattern alignment corresponds to grid angles 30° offset from the polarisation 391 axis. fMRI-based estimates of grid-cell-like representations^{13,14,16–19} showed consistent 392 orientations across participants in two independent experiments, yielding the optimal grid 393 orientation for decoding self-location. Taken together, our results provide evidence that the 394 grid system aligns to axes of high spatial information, which suggests that effects of 395 environmental geometry on the grid system are adaptive responses in service of flexible 396 397 navigation. Furthermore, angular change to stationary cues during self-motion may play a central role in the computations underlying the grid system. 398

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Could grid-cell-like representations simply follow extra maze cues or object locations? Note that the peaks of hexadirectional activity (grid-cell-like representations) did not correspond to movement directions directly facing a cue in either fMRI experiment. This speaks against a simple sensory 'anchoring' of grid-cell-like representations to landmarks in the environment. Importantly, the coherent orientations of grid-cell-like representations can also not be attributed to the presence of objects in each trial, since their locations were randomised across participants and the two fMRI experiments had different numbers of objects.

408 Our findings are in agreement with reports showing that entorhinal fMRI activity correlates with Euclidean distance to a goal location ²⁷ and the proposal that grid cells might enable 409 goal-directed vector navigation ^{1,2,5,28–32}. Interestingly, both angular and distance information 410 that is needed for triangulation can be derived from either visual or proprioceptive and 411 vestibular cues. For example, visually modulated cells in the rat posterior-parietal cortex 412 signal the egocentric cue direction ³³ and head-direction cells in the entorhinal cortex and 413 other regions realign to visible cues, but also function without vision and rely on vestibular 414 information ³⁴. On the other hand, distance information can be inferred visually from the 415 relative size of objects and cues ²⁴ or is based on proprioceptive and timing information 416 during movement, both of which modulate grid cell activity ³⁵. Hence, triangulation for 417 navigation could bridge different sensory modalities. Furthermore, it combines egocentric 418 419 cue directions and distance information to infer map-like, survey representations of the 420 environment, thereby naturally integrating egocentric and allocentric reference frames, which are not mutually exclusive and can work in parallel and across brain regions ^{33,36,37}. 421 422

A potential avenue for future studies is to examine the effect of anisotropic spatial 423 424 uncertainty on rodent grid-cell firing, albeit many animals may be needed to detect such a stochastic effect. It is known that grid cell firing exhibits plasticity, regularising and reorienting 425 426 incrementally with continued experience of an enclosure (Barry et al., 2007; Barry, Heys, & Hasselmo, 2012; Carpenter et al., 2015; Stensola et al., 2015). Our results suggest that 427 these changes likely optimise the grid-code, allowing for an increasingly accurate 428 representation of self-location. However, the physiological and circuit mechanisms that 429 facilitate and direct this process are currently unknown. Theoretically, a number of authors 430 have considered the impact of noise in grid cell coding of self-location and its implications for 431 the capacity and error-tolerance of the entorhinal spatial representation ^{5,41,42}. However, to 432 the best of our knowledge, we have provided the first theoretical and practical account of 433 434 anisotropic spatial uncertainty on the grid system. It remains to be seen if such asymmetries, which are likely a common feature of the environment ⁴³, exert more wide-ranging influences 435 436 on grid-firing; distorting the grid-pattern or changing the relative scales of different grid 437 modules; or might also impact grid-like coding of non-spatial information. In conclusion, we combined biologically inspired computational models, behavioural tests, eye-tracking and 438 fMRI-based proxy measures of grid-cell-like population activity to test the effects of 439 environmental geometry on the entorhinal grid system. Our results are consistent with an 440 adaptive and flexible role of grid cells in self-localisation and navigation. This opens up the 441 exciting possibility for a deeper understanding of fundamental neural building blocks of 442 cognition and behaviour. 443

445

446 Materials and Methods

447

448 Simulation of Euclidean triangulation

449 To test the impact of stochastic fluctuations or noise on triangulation accuracy, we

450 implemented the following simulation in Matlab (2012b, The MathWorks Inc.,

451 Massachusetts). Triangles were formed by two points representing start and end points of a

452 straight path in the horizontal plane (e.g. observer locations at time point 0 and time point 1)

and one of two polarising, stationary cues. Triangulation was based on the sine ruleaccording to:

455

$$c = b * \sin(\sigma) / \sin(\delta\sigma)$$
⁽²⁾

456 where *c* is the unknown side (distance to the cue at the end point; Figure 1 -figure

457 supplement 4), *b* the known side (distance travelled), σ the angle to the cue at the start point 458 and $\delta\sigma$ the angular change to the cue between start and end point.

Path orientation (azimuth) was varied in steps of 1°, path length remained constant and each 459 path was centred on the origin of the coordinate system. Hence, the start and endpoints of 460 different paths mapped onto a circle. This ensured that the mean distance of different paths 461 462 to one or multiple cues remained constant. Before the triangulation iterations, random noise was added to the known side and the two distance angles. The error in side length had a 463 mean absolute deviation of roughly 5% the original length (based on typical human distance 464 errors during walking ⁴⁴) and was drawn from a Gaussian distribution with mean 0 and a 465 sigma of path length of 15.95. The absolute angular error for a single angle was 5° on 466 average (drawn from a von Mises distribution with mean 0 and a sigma of 6.26) and 15° on 467 average for the absolute cumulative error across all three angles of a triangle. This error rate 468 was based on the mean, absolute angular error observed in humans performing a triangle 469 470 completion task in virtual reality, which involved pointing to a start location after an outward path with two turns ⁴⁵. 471

472

Triangulation measurements: noise resilience. Triangulation was repeated for all sides of a 473 triangle using the known base a. If the inferred side was the base (the path), triangulation 474 was repeated with both remaining sides serving as the known side and the two results were 475 then averaged. Dual triangulation for the base was done to avoid biased results due to the 476 477 selection of any one of the remaining sides. Note that the length of the remaining sides was not constant and changed in opposite directions for different path angles, potentially 478 affecting the noise resilience measure at different path angles. This was not a problem in the 479 reverse case, because the base (side a) had constant length. The triangulation error for the 480 481 3 sides was computed as the absolute difference in the original side length and the length

based on triangulation with noisy input parameters. The 3 error rates were then averaged for 482 483 further computations and the assessment of noise resilience across paths (Figure 1 – figure supplement 4-6). Furthermore, the distance between the most proximal cue to the centre of 484 485 each path (the middle of the base of a triangle) was always equal to the length of the path, with the exception of Figure 1 – figure supplement 6 that shows the effects of different path 486 lengths and different noise levels. In other words, usually the path length was half the length 487 of the polarisation axis. Triangulation to additional cues was performed for a given path 488 angle if these were within $\pm 90^{\circ}$ (determined from the centre of a path) to emulate a limited 489 field-of-view. This meant that cues in only that half of the environment were used for 490 491 triangulation that was faced on a given path (1 point in Figure 1 – figure supplement 4). 492

493 *Triangulation measurements: triangle quality.* The quality measure for triangle shape

(triangle area divided by the sum of squares of side lengths; Figure 1 – figure supplement 4
 light blue curve) was modified from ⁴⁶ who describe optimization of finite element

- 496 triangulations in the generation of meshes.
- 497

498 Computational models of grid cell systems

499

500 Grid cell system model

Spiking activity of a population of grid cells, organised into 4 (except where otherwise 501 specified) discrete modules by spatial period size, was modelled in a two-dimensional 502 503 circular environment of radius 50cm using Matlab v.8 (Mathworks). Spatial periods or grid 504 scales, λ_i , were determined as a geometric sequence beginning with λ_1 = 25cm and increasing with a scale factor of 1.4 (except where otherwise specified). Tuning curves for 505 each grid scale λ_i were generated with locations of grid nodes specified as a regular 506 triangular grid and expected firing rate at each location determined by a Gaussian 507 distribution centred on the nearest node: 508

509
$$\alpha_{i,j}(x,y) = f_{max}e^{-\frac{d^2}{2\sigma_i^2}}$$

where *j* specifies a particular cell, *d* is the distance from (x,y) to the nearest grid node, f_{max} the maximum firing rate (constant across the population; 10Hz except where otherwise specified), σ_i the tuning width of the grid fields ($\sigma_i = 3\lambda_i/(20\sqrt{\log_e 100})$ following ⁴.

514 Within each of the 4 modules, M = 195 offset tuning curves were distributed in a 13 × 15 515 rectangular grid via translations of this original tuning curve, as well as adding a random 516 translation common to all grids in the module. This resulted in a total of 1560 grid cells in a 517 system. Grid tuning curves could also be rotated to specified orientations; all grid tuning

curves always shared a common orientation. All these transformations were performed usingcubic interpolation.

520

521 In each iteration of the model, the true position (x, y) was specified as the centre of the

- 522 circular environment (0, 0). To model uncertainty, Gaussian noise, with standard deviation
- 523 varied independently in x and y, was generated separately for each module and added to (x,
- 524 y), to yield a noisy position estimate (x + $\varepsilon_{x,i}$, y+ $\varepsilon_{y,i}$). Anisotropic uncertainty was produced by
- independently varying the standard deviations of $\varepsilon_{x,i}$ and $\varepsilon_{y,i}$ between 0 and 5. All cells within
- a module therefore received the same noisy position input, but cells in different modules
- 527 received different input. Thus cell firing rate was now modulated according to $\alpha_i (x + \epsilon_{x,i}, y +$
- 528 ε_{y,i}).
- 529

530 Higher-order "four-leaf" and "six-leaf" noise distributions were created for control

531 experiments (Figure 1 – figure supplement 3). In polar coordinates, the width (s.d.) of the

532 Gaussian noise distribution along the ray was modulated by a cosine function of the angular 533 coordinate.

534

535 The signal extracted from the grid cell system was the number of spikes, *k*, generated by

each neuron during a finite read-out period, T = 0.1s (the approximate length of a theta cycle) – i.e. a population response $K = (k_1, ..., k_N)$. We assume the decoding cannot take the added noise into account in any way, so that given a position *x* the probability of observing the response *K* in time T, following ⁴, is taken to be:

540
$$P(\mathbf{K}|x,y) = \prod Poisson\left(k_{i,j}, T\alpha_{i,j}(x,y)\right) = \prod \frac{\left(T \times \alpha_{i,j}(x,y)\right)^k}{k!} \times e^{-T\alpha_{i,j}(x,y)}$$

541

where $\alpha_{i,j}(x,y)$ is calculated by cubic interpolation from the tuning curve. From the population response *K*, we can decode position as the maximum likelihood estimate of (x, y), that is x, \hat{y} (*K*). Given the initial assumption that all positions within the environment are uniformly likely,

- 546
- 547

$$\hat{x}, \hat{y}(\boldsymbol{K}) = \max P(x, y | \boldsymbol{K}) = \max P(\boldsymbol{K} | x, y)$$

548

Thus x, y, \tilde{K} may be closely approximated by calculating P(K|x,y) for a sufficiently finely spaced uniform sample of *x* and *y* values across the environment, and selecting the values of x and y which yield the greatest P(K|x,y). We used a spatial bin size of 0.5 cm. Where two or more solutions yielded the same maximal P(K|x,y) (i.e. decoding was ambiguous), one was randomly selected ^{2,4}.

554

555 Assessing grid system performance

For each combination of levels of uncertainty in x and in y, we assessed the performance of 556 557 grid systems whose patterns were orientations to these x-y axes from 0° to 30° at intervals of 2.5°. For each case, five experiments each consisting of 15,000 iterations of this 558 procedure were performed. In each of these five experiments, the square grid across which 559 the environment was sampled to produce tuning curves was set at a different orientation to 560 the environment's Cartesian axes, in order to control for any effect of uneven sampling (the 561 orientations were 0° and 4 orientations randomly selected and then used across all 562 563 conditions). The results of equivalent pairs of uncertainty levels (e.g. standard deviation respectively in x and y of 0 and 5 cm, and 5 and 0 cm) were combined to total 2 × 5 × 75.000 564 565 = 150,000 iterations. Using these, accuracy of decoding was assessed via the approximated maximum-likelihood estimate square error, or MMLE, based on the square errors of position 566 567 decodina:

$$MMLE \approx \frac{1}{75000} \sum_{c=1}^{75000} \left(0 - \hat{x}(\mathbf{K}_c) \right)^2 + \left(0 - \hat{y}(\mathbf{K}_c) \right)^2$$

569

568

570 Neuroimaging, behavioural- and eye-tracking experiments

571

572 Participants

FMRI experiment 1. 26 participants took part in the study (12 females, age range: 19–36,
mean age: 23 years). Materials and Methods were approved by the local research ethics
committee (ethics committee University Duisburg-Essen, Germany and CMO region

576 Arnhem-Nijmegen, NL). Written informed consent was obtained from each participant.

577

578 FMRI experiment 2. 25 participants took part in this study (11 females, age range: 18-32,

579 mean age: 24 years). One participant was excluded from the analysis due to poor

580 performance (i.e. 55 trials with no location response within 30 seconds of the respective trial,

- 581 more than a standard deviation above the mean). Materials and Methods were approved by
- the local research ethics committee (CMO region Arnhem-Nijmegen, NL). Written informed
- 583 consent was obtained from each participant.
- 584

585 *Behavioural experiment.* 20 participants (11 females, age range: 18-24, mean age: 20 years)

586 participated in the behavioural experiment. Materials and Methods were approved by the

587 local research ethics committee (CMO region Arnhem-Nijmegen, NL). Written informed

588 consent was obtained from each participant.

589

Eye tracking experiment: 36 participants (15 females, age range: 18-63, mean age: 26)
participated in the experiment. Two participants aborted the experiment early, because of
VR-induced nausea, and their data was excluded from all analyses. Materials and Methods
were approved by the local research ethics committee (CMO region Arnhem-Nijmegen, NL).

- 594 Written informed consent was obtained from each participant.
- 595
- 596

597 **FMRI acquisition**.

598 FMRI experiment 1. Blood-oxygenation-level-dependent (BOLD) T2*-weighted functional images were acquired on a 7T Siemens MAGNETOM scanner (Siemens Healthcare, 599 600 Erlangen, Germany) using a three dimensional echo-planar imaging (3D EPI) pulse sequence 47 with a 32-channel surface coil with the following parameters: TR = 2.7 s, TE = 601 20 ms, flip angle = 14° , voxel size $0.9 \times 0.9 \times 0.9$ mm, field of view (FoV) = 210 mm in each 602 603 direction, 96 slices, phase encoding acceleration factor = 4, 3D acceleration factor = 2. The scanning session was subdivided into EPI acquisition blocks of 210 volumes each. The 604 605 majority of participants performed 5 blocks over the course of approximately 55 minutes. 606 Deviations from the 5 blocks in a few participants were due to technical problems or interruptions on behalf of the participants (3 participants had 4 blocks, 2 participants 6 607 blocks). In addition, T1-weighted structural images (MP2RAGE; voxel size: 0.63 mm 608 isotropic) and a field map (gradient echo; voxel size: 1.8 x 1.8 x 2.2 mm³) were acquired. 609 Results of an entirely unrelated, task-independent whole-brain connectivity analysis of data 610 611 from experiment 1 have been described in a previous report ⁴⁸.

612

FMRI experiment 2. BOLD T2*-weighted functional images were acquired on a 3T Siemens 613 Trio scanner (Siemens Healthcare, Erlangen, Germany) using a three dimensional echo-614 planar imaging (3D EPI) pulse sequence ⁴⁷ with a 32-channel surface coil with the following 615 parameters: TR = 1.8 s, TE = 25 ms, flip angle = 15°, voxel size 2 × 2 × 2 mm, field of view 616 (FoV) = 224 mm in each direction, 64 slices, phase encoding acceleration factor = 2, 3D 617 acceleration factor = 2. Each scanning session consisted of an EPI acquisition block of 1031 618 619 volumes on average (range: 661-1200), amounting to roughly 31 minutes of scan time. In addition, T1-weighted structural images (MPRAGE; voxel size, 1 mm isotropic; TR, 2.3 s) 620 621 and a field map (gradient echo; voxel size, $3.5 \times 3.5 \times 2 \text{ mm}^3$) were acquired. 622

623 Experimental tasks

FMRI experiment 1. Participants freely navigated a 3D virtual reality environment with a

modified version of the arena from the studies by Doeller and colleagues ^{13,19} (Figure 3A)

using a 4-button controller. UnrealEngine2 Runtime software (Epic Games) was used to 626 627 generate the virtual reality task. Instead of two orthogonal axes that are formed by the walls of square enclosures (as in (Krupic et al., 2015; Stensola et al., 2015)) we opted for the 628 629 simplest case of a single axis, which was determined by extra-maze cues in a circular arena. We hypothesized that the orientation of grid representations would be coherent across 630 631 participants, as shown in rats moving through square environments, and that this orientation 632 would be determined by the amount of spatial information obtained on movement paths of 633 such orientation. The environment consisted of a circular arena with 12 extra-maze cues, 6 upright and 6 inverted triangles. Two pairs of neighbouring triangles of different orientation 634 comprised the two configural cues on opposite sides of the arena that defined a polarisation 635 axis. To control for possible visual effects on our direction-related analysis, we designed the 636 637 colour textures for the extra-maze cues in such a way, that the low-level visual features 638 remained equal across cues. Each triangle had a red, green and blue corner, arranged in 1 639 of 6 possible constellations. The arrangement of textures was randomised across 640 participants. Counting one's steps was not possible, because no body parts were visible, and the virtual pitch direction was fixed. Self-motion information such as optic flow induced 641 by the grassy plane was present but did not yield directional information. Participants 642 performed a self-paced object-location memory task that involved collecting and replacing 643 six everyday objects to locations that were randomised across participants. Participants 644 collected each object from its associated location once during an initial phase, by running 645 over it. Navigation was not interrupted during the transitions between trials to enable more 646 natural (ecologically valid) continuous navigation. In each subsequent trial they saw an 647 648 image (cue) of one of the objects in the upper part of the screen and had to move to the object's associated location and press a button (replace phase). After this response, the 649 object appeared in its associated position and participants collected it again (feedback 650 phase). After an average of 3 trials (range 2-4 trials), a fixation cross on a grey background 651 652 was presented for 4 seconds (inter-trial-interval, ITI). Object locations were randomised 653 across participants. Since the task was self-paced, the number of trials varied across participants (range: 94-253; mean: 179). Prior to the fMRI experiment, participants 654 performed a similar object-location task with different objects in a different virtual 655 656 environment outside the scanner to familiarise themselves with the task demands. 657

FMRI experiment 2. Participants freely navigated the same virtual environment as used in
fMRI experiment 1, but with only two extra-maze cues on opposite sides of the arena that
defined a polarisation axis (Figure 3A). Participants performed the same object-location
memory task described above, except that 4 objects were used instead of 6. Participants
performed an average of 117 trials (range: 63-179). Prior to the fMRI experiment,

participants performed a similar object-location task with different objects and a different
 virtual environment outside the scanner to familiarise themselves with the task demands.

666 Behavioural experiment. Participants freely navigated a virtual reality environment (Figure 2A, Figure 2 – figure supplement 1) by using four buttons on a keyboard to move in the four 667 668 cardinal directions and the mouse to change horizontal viewing direction. The virtual environment was displayed at 1680x1050 pixel resolution and 60 Hz refresh rate 669 approximately 40cm in front of the participants' eyes. They were teleported between varying 670 start and end locations at one of three possible angles and performed a distance estimation 671 672 task. The environment was a 'pitch black' space with otherwise only three distinguishable elements. First, it included a background consisting of a white dashed line oriented 673 674 horizontally and projected at infinity. This background provided minimal visual information to 675 perceive rotational movements as well as motion parallax of a cue viewed from different 676 angles. Second, a cue, consisting of a red circle, was displayed vertically on a fixed location. 677 Third, a red circle indicated the start location of each path with an arrow pointing in the direction of the goal location. The rationale behind using a visually sparse environment and 678 teleportation to the goal location was to prevent the use of other distance cues, such as cue 679 size (e.g. patches of grass or a boundary) or an estimate of 'time-of-flight', respectively. This 680 ensured that the change in size of the cue and the change in angle and motion parallax to 681 the cue from start to the end of a path was the sole means by which the distance estimation 682 task could be performed correctly. Prior to the experiment, participants performed a similar 683 distance estimation task in a different virtual environment to familiarise themselves with the 684 685 task demands. At the beginning of the behavioural experiment, participants were instructed to approach the cue in order to familiarise themselves with its location and distance. 686

687

The trial structure was as follows: Participants were instructed to navigate to the starting 688 689 point. Once they reached the starting point, their movement was restricted to rotations and 690 the message 'click right mouse button to teleport ahead' was displayed (orientation phase one). Participants could self-initiate teleportation to the goal location by a mouse-click and 691 692 orienting towards the pointing direction of the arrow, at which point the view was frozen and 693 teleportation commenced 2 seconds later. After teleportation to the goal location, the start location became invisible (the red circle with arrow disappeared), movement remained 694 restricted and only rotations were possible and the message 'click right mouse button to give 695 response' was displayed (orientation phase two). Participants could self-initiate the response 696 697 phase. Then, a horizontally oriented window was displayed together with the message 'indicate distance (left = minimum, right = maximum)' and participants could move the mouse 698 to slide a bar inside the window to indicate how far they thought they were being teleported. 699

The range of possible responses was 0 virtual units (vu) to 6000 vu. For comparison, the 700 701 arena diameter used in the fMRI studies was 9500 vu for the inner boundary and the length 702 of the polarisation axis (i.e. the distance between opposing, extra-maze cues) was 12064 vu. 703 The range of teleportation distances was 500 vu to 5500 vu (mean = 2742 vu). The response was finalised by another mouse click and subsequently, feedback in the form of 704 smiley faces was given for 2 seconds. The color of a smiley for a response error < 2% of the 705 correct distance was green, light green for an error < 4 %, yellow for an error < 8 %, orange 706 for an error < 16% and red otherwise. During this feedback phase, participants could still 707 move the response bar to see other response-to-feedback mappings (i.e. the smiley 708 709 associated with a given horizontal pixel location). Once the feedback disappeared, 710 participants were able to freely navigate again. At the beginning of about 50% of trials 711 (determined pseudo-randomly), participants were placed to a point in front of the start location to speed up the experimental procedure (i.e. to reduce navigation time from a goal 712 713 location to the start location of the subsequent trial) and thereby increase the number of 714 trials. In addition, the orientation phase 1 and 2 were restricted to 6 seconds and the response phase to 4 seconds indicated through the display of a timer. If the time limit was 715 716 reached, 'Time is up! This trial is invalid' was displayed on a red background and no 717 response was recorded. Teleportation distances and teleportation directions were pseudorandomly determined on each trial. Teleportation directions were either 0° (approaching the 718 cue on a straight line), -30° or $+30^{\circ}$. The location of the cue was at (x = 0 vu, y = 8500 vu) 719 720 and following the approach of the simulations, all paths were centered on the origin of the 721 coordinate system. However, this would provide a relative advantage to the parallel 722 condition. The size of the cue directly reflects its distance to the observer, which becomes 723 particularly apparent at close proximity. In the -30° and the +30° conditions, the goal location 724 is always further away from the cue compared to the 0° condition at equal teleportation distances. Furthermore, the independent measure (teleportation distance) is linearly 725 associated with goal-to-cue distance only in the 0° condition. To avoid bias due to unequal 726 727 goal-to-cue distance, we equalized this measure by subtracting the difference across conditions (at equal teleportation distances). In effect, this shifted the teleportation paths in 728 the 0° condition backwards by a given amount (Figure 2B). Due to a limited field-of-view of 729 730 85°, testing of large path offsets of e.g. 90° was not feasible. The task duration was limited to 30 minutes in which participants performed an average of 129 self-paced trials (range: 52-731 238). Prior to the main task, participants performed a training version of the task in a richer 732 733 virtual environment with a comparable trial structure where the length of the path was not 734 traversed by teleportation but rather through guided movement.

Eye tracking experiment: During a magnetoencephalography study (MEG; data are subject
of an independent report), participants performed the same task in the same virtual
environment as in fMRI experiment 1 (i.e. the environment with 12 cues). However, they had

to learn the locations of 8, instead of 6 objects. Simultaneously, gaze position and pupil area

- of the left eye were monitored with an infrared-based Eylink 1000 eye tracking system at
- 741 1200 hz.
- 742

743 Analysis of eye tracking data

The eye tracking data were converted to screen coordinates. Blinks were removed from the 744 745 time series based on deviations in pupil area of more than one standard deviation from the mean including 25ms around the blink on- and offsets. After smoothing with a running 746 747 average kernel of 10 ms and linearly detrending, gaze positions were transformed to 748 velocities expressed as degree visual angle per second. Since gaze velocity profiles differed 749 between translations and rotations during navigation, saccades were detected individually 750 during head rotations and static or translational navigation. During head rotations, saccades were detected using a threshold of 12 times the median-based standard deviation of 751 752 velocity, during static or translational periods with 6 times the median-based standard 753 deviation of velocity. Saccades shorter than 12 ms were excluded ⁴⁹.

754

To examine which cues were looked at most during the experiment, we transformed 755 horizontal gaze positions to degrees visual angle and scaled them linearly to match the 756 physical field of view (36 degrees visual angle) to the virtual field of view (85 degrees virtual 757 758 visual angle). The resulting virtual degrees visual angles were then combined with the virtual head direction to reconstruct the allocentric viewing direction at each point in time. Since all 759 760 twelve spatial cues were visible exclusively in the upper visual field, we limited our analysis to gaze positions on the upper half of the screen. Moreover, to account for any potential 761 influence of initial viewing angle on this analysis, we excluded all samples recorded before 762 763 participants rotated at least 90 virtual degrees away from the starting viewing angle (average time excluded at start of experiment: 15.2 seconds). We then computed the intersection 764 765 between allocentric gaze and a surface at the radius of the extra-maze cues from the centre 766 of the arena for each point in time as follows. We first generated 360 equally spaced vertices at the radius of the extra-maze cues and computing the vectors between the participant's 767 768 location and all of these vertices. We then selected the respective vertex with the minimal 769 angular distance to the current allocentric viewing direction. This way, we obtained the 770 position of gaze on the arena border or cues at each given point in time. For each vertex we computed the respective viewing time expressed as percent of all samples obtained for each 771 772 respective participant to account for differences in experiment duration across participants

- (Figure 3 figure supplement 2). To examine whether there were differences in viewing
- times between cues, we then binned vertices into 30-degree bins centred on the cues and
- compared average viewing time using a repeated-measures ANOVA. However, our specific
- hypothesis was that especially the cues forming the polarisation axis should be most
- informative for the task. To test whether these cues were the ones most viewed, we
- averaged viewing times for the configural landmarks that comprised the polarisation axis (i.e.
- two pairs of cues of opposite orientation) and compared it to the average of the four cues
- 780 orthogonal to the polarisation axis using a one-tailed paired t-test.
- 781

782 FMRI data pre-processing

- 783 Image pre-processing and analysis were performed with the Automatic Analysis Toolbox
- 784 (https://github.com/rhodricusack/automaticanalysis). This involved using custom scripts
- combined with core functions from FSL 5.0.4 (http://fsl.fmrib.ox.ac.uk/fsl/) and SPM8
- 786 (http://www.fil.ion.ucl.ac.uk/spm). SPM was used for an iterative functional image
- realignment and unwarping procedure to estimate movement parameters (three for rotation,
- three for translation) and to correct images with respect to gradient-field inhomogeneities
- caused by motion. To improve co-registration and the creation of a group-specific structural
- and functional template using the Advanced Neuroimaging Toolbox (ANTS;
- 791 <u>http://www.picsl.upenn.edu/ANTS/</u>) structural images were de-noised using an optimised
- non-local means filter ⁵⁰ and mean EPI images were corrected for gradual changes in signal
- intensity (bias correction) using SPM. Next, structural images were co-registered (based on
- mutual information) to the functional images using SPM and brain-extraction was performed
- using FSL. The resulting skull-stripped structural image was segmented into grey matter
- (GM), white matter (WM) and cerebro-spinal fluid (CSF) voxel masks. Finally, functional
- 797 images were spatially smoothed with an isotropic 8-mm full-width-half-maximum Gaussian
- kernel and high-pass filtering with a 128-s cut-off to reduce low-frequency drift.
- 799

800 Physiological artefact correction.

- 801 During the 7T-fMRI acquisition of fMRI experiment 1, we recorded the cardiac pulse signal
- and respiration of participants by means of an MRI compatible pulse oximeter and
- 803 pneumatic belt (Siemens Healthcare, Erlangen, Germany) at a sampling rate of 50 Hz. In
- addition, scanner pulses were recorded in an analogue input for synchronisation of fMRI and
- 805 physiological data at 200 Hz. Due to technical problems, these data were not available for all
- scanning blocks and participants (average of 2.7 blocks, range 0 to 5 blocks per participant).
- 807 Physiological artefact correction was performed for fMRI data with available concurrent
- 808 physiological data. This involved band-pass filtering the pulse data between 20 and 150 bpm
- 809 (0.3 and 2.5 Hz, respectively) to improve peak detection. Subsequently, RETROICOR was

- used to create regressors that were fed into the subject-specific fMRI analyses (GLMs) as
- 811 confound regressors to remove spurious fluctuations. Fluctuations due to cardiac and
- 812 respiratory phase were each modeled by 6 regressors for sine and cosine Fourier series
- 813 components extending to the 3rd harmonic. Two additional regressors modeled lower
- 814 frequency changes in respiration and heart rate with a sliding window analysis following ⁵¹.
- 815

816 Region-of-interest (ROI) definition

- 817 Based on our a priori hypothesis ^{13,19}, ROI analyses were performed for the right entorhinal
- cortex (EC). Right EC ROIs were created on the Montreal Neurological Institute (MNI152) T1
- template using a probabilistic atlas based on cytoarchitectonic mapping of ten human post-
- 820 mortem brains ⁵² with FSL 5.0.4 (http://fsl.fmrib.ox.ac.uk/fsl/). The probability threshold was
- conservative (95%) for the estimation of hexadirectional orientations and liberal (0%, i.e.
- including all voxels with non-zero probability) for the small volume correction of the mask.
- Thresholded masks were binarised and converted to NiFTI file format and then normalised
- to the space of the individual functional images via the group-specific EPI template (Figure 5
- 825 figure supplement 1) using the Advanced Neuroimaging Toolbox (ANTS;
- 826 <u>http://www.picsl.upenn.edu/ANTS/</u>). SPM was used to reslice the ROI mask dimensions to
- the EPI dimension, which was again followed by binarisation of the masks. Through the
- same procedure, a right, primary visual cortex ⁵³ mask (95% threshold) and a mamillary
- body ⁵⁴ mask (25% threshold) were created for control analyses.
- 830

831 Analysis of fMRI time series

832 Following pre-processing, fMRI time series were modeled with general linear models (GLMs). The different trial phases of the object-location memory task were modeled with two 833 regressors. One regressor was used for the retrieval phase (replacement of an object) and 834 one for the encoding phase (following the location response, when the object was shown at 835 the correct location and could be collected), both of which were associated with a parametric 836 837 modulator for spatial memory performance to discount large-error trials. Inter-trial-intervals (presentation of a fixation cross on a grey background) were not explicitly modeled and 838 served as an implicit baseline. The presentation of the object cues and the feedback was 839 840 modeled with two additional regressors. Furthermore, all GLMs included nuisance regressors, comprising at least 6 movement parameters, 2 regressors for signal fluctuations 841 842 across white and grey matter voxels and 1 regressor to model time points with frame-wise 843 displacements ⁵⁵ larger than 0.5 mm. In addition, physiological signals have been recorded 844 for a sub-set of participants (see section below for details) which was used to correct for cardiac and respiratory artefacts by means of 14 additional regressors. The main regressors 845 of interest modeled virtual movement periods with two associated parametric modulators 846

847 (see 'Analysis of hexadirectional activity' below for details). Coefficients for each regressor

- 848 were estimated for each participant using maximum likelihood estimates to account for serial
- correlations. All parametric modulators were normalized to have zero mean and thus be
- orthogonal to the un-modulated regressor. Prior to the second-level random effects analysis,
- 851 the linear contrast images of the regression coefficients underwent nonlinear normalization
- to the group-specific template brain using ANTS.
- 853

854 Analysis of grid-cell-like representations

The orientation of 6-fold rotational symmetry of entorhinal activity (referred to as 855 'hexadirectional activity' and consistent with grid-cell representations in humans¹⁹) was 856 estimated in participant's right EC using a quadrature-filter approach on fMRI data during 857 858 fast movements in all trial phases. Participant's virtual-navigation fMRI data entered a general linear model (GLM) with two parametric modulators of a movement regressor. These 859 860 modelled the sine and cosine of running direction $\theta(t)$ in periods of 60° (i.e. $\sin(6^{\circ}\theta(t))$ and 861 $\cos(6^{*}\theta(t)))$ for participant's 50% fastest movement time points, where grid-cell-like representations can be reliably detected ^{13,19}. Multiplication by 6 transformed running 862 direction into 60° periodic space to create regressors sensitive to activation showing a six-863 fold rotational symmetry in running direction. Activations with six evenly spaced peaks as a 864 function of running direction will produce parameter estimates β_1 and β_2 for the two 865 regressors with large amplitude sqrt ($\beta_1^2 + \beta_2^2$). To this end, running direction $\theta(t)$ was 866 arbitrarily aligned to 0° of the coordinate system underlying the virtual reality engine. 867 Participants were not aware of the environmental coordinate system. The relationship 868 869 between the underlying coordinate system and the polarisation axes (defined by extra-maze cues) differed between fMRI experiment 1 and fMRI experiment 2. The orientation of the 870 polarisation axis (i.e. 0°) had an angular offset from the underlying coordinate system of 15° 871 in fMRI experiment 1 and 90° in fMRI experiment 2. This made it unlikely that an anchoring 872 of grid-cell representations to polarisation axes were due to other factors, such as viewing 873 direction during the start of the experiment, which was -15° in fMRI experiment 1 and -90° in 874 fMRI experiment 2, relative to the visible polarisation axes. Next, the parameter estimates of 875 the two parametric modulators (β_1 and β_2) were extracted from the right EC ROI and used to 876 877 calculate preferred orientation in 60° space (varying between 0° and 59°). A participant's 878 mean orientation of hexadirectional activity was defined as $\phi_{60^\circ} = \arctan(\beta_1/\beta_2)$, where β_1 is 879 the averaged beta value for $sin[6^*\theta(t)]$ and β_2 is the averaged beta value for $cos[6^*\theta(t)]$ 880 across voxels of the right EC. Dividing by six transformed the mean orientation φ_{60° back into 881 standard circular space of 360° for one of the three putative grid axes (the remaining two being 60° and 120° relative to the first). 882 883

Our main research question was if environmental geometry affects the orientation of putative 884 grid-cell representations (see below for a description of the statistical test procedure). To 885 additionally cross-validate effects of entorhinal hexadirectional activity ^{13,14,19}, we tested the 886 887 temporal stability of preferred orientations and their regional specificity in a split-half procedure (Experiment 1). This was done only for experiment 1, because data acquisition 888 was roughly twice as long, participants completed more trials (179 versus 117, on average; 889 890 two-sample t-test, $T_{(48)}$ =5.25, p<0.001) and SNR likely higher due to high-field scanning compared to experiment 2, which warranted a sacrifice in sensitivity for the main research 891 892 question.

- 893 The procedure involved testing activation differences in the second half of the data with sixfold rotational symmetry that was aligned with the (potentially environmentally determined) 894 895 hexadirectional activity estimated from the first half of the data. More specifically, the second 896 GLM contained regressors for both 'aligned' and 'misaligned' runs relative to the estimated 897 hexadirectional activity (respectively, this means running directions were either less than ± 898 15° or more than ± 15° oriented relative to the nearest axis of hexadirectional activity). As for the estimation procedure, regressors modeling six-fold rotational symmetry captured 899 900 participant's 50% fastest movement time points. Participants' contrast values (aligned > 901 misaligned) then entered a second level random-effects analysis to test for hexadirectional activity in the entire brain volume acquired. Supra-threshold activation in the right EC would 902 indicate temporal stability and regional specificity of putative grid orientation. 903 904 Having evaluated temporal stability and regional specificity of the quadrature-filter approach 905 for investigation of grid-cell-like representations in fMRI experiment 1, we decided to 906 maximise statistical power addressing the main research question of environmental effects
- 907 on hexadirectional activity in fMRI experiment 2.
- 908

909 Analysis of environmental anchoring of hexadirectional activity

We tested environmental anchoring of the hexadirectional activity relative to the polarisation 910 axes by using a V test for circular homogeneity ⁵⁶. The V test for circular homogeneity is 911 similar to the Rayleigh test for circular homogeneity and can be used if an a-priori hypothesis 912 913 of a certain mean direction in a sample of angles is being tested. Due to our hypothesis of a 914 relationship between the orientation of the grid-system and anisotropy in spatial information derived from angular changes to polarising cues, we tested participant's putative grid 915 orientations in 0°-60° space (Figure 5B and Figure 7A) for the presence of a mean direction 916 917 aligned 30° off the polarisation axis. 918

- 919
- 920

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935 SUPPLEMENTAL INFORMATION

936

937 Supplemental Figures :

938

Uncertainty standard deviation x & y axis, respectively

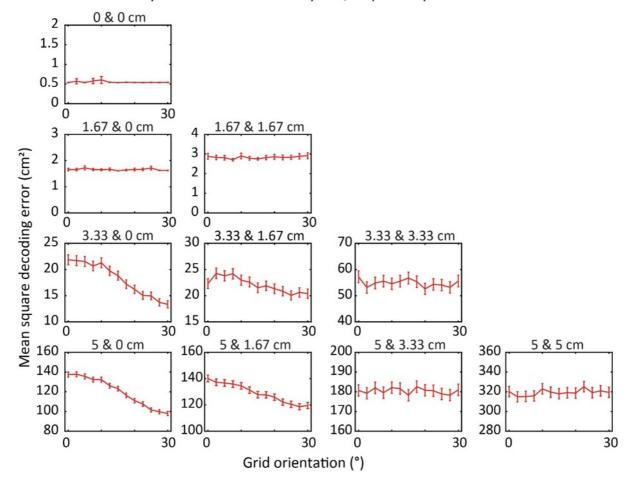




Figure 1 – figure supplement 1. More extreme anisotropy in spatial uncertainty results
in a more pronounced dependency of self-localisation accuracy on grid orientation.

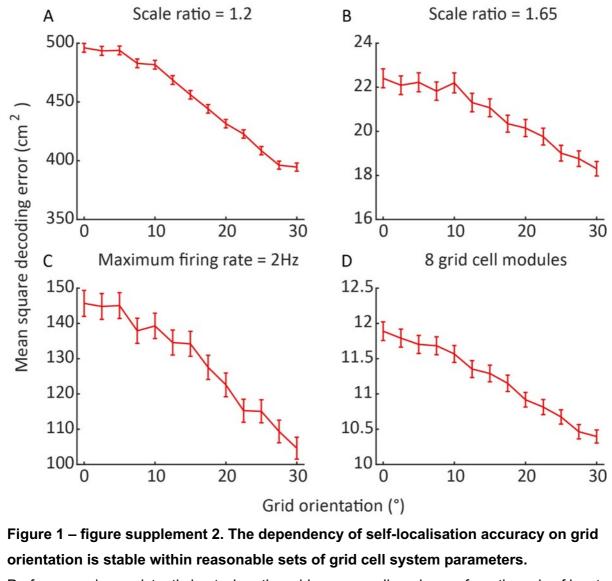
942 The performance of grid cell systems was assessed while independently varying the

943 degrees of spatial uncertainty in two orthogonal axes. When uncertainty is equal in both

axes performance does not depend on the orientation of the grid pattern. As uncertainty

945 becomes more anisotropic, self-localisation is more accurate in grid cell systems in which

946 the grid pattern axes are aligned away from the axis of greatest spatial uncertainty.



Performance is consistently best when the grid axes are aligned away from the axis of least spatial uncertainty, across variations in the parameters of the grid cell system. Error bars

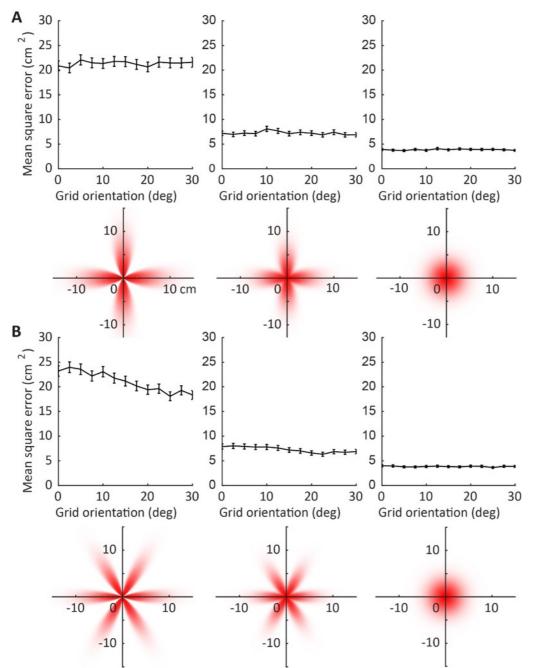
indicate 95% confidence interval, n = 150,000. A Grid period scaling factor reduced to 1.2. B

Grid period scaling factor increased to 1.65. C Grid cell maximum firing rate reduced to 2Hz.

(In order to compensate for increased effects of noise in this system, the number of cells per

module was quadrupled. Due to the high computational intensity of this simulation n =

75,000.) D Four further grid cell modules added, with scales continuing to increase geometrically.

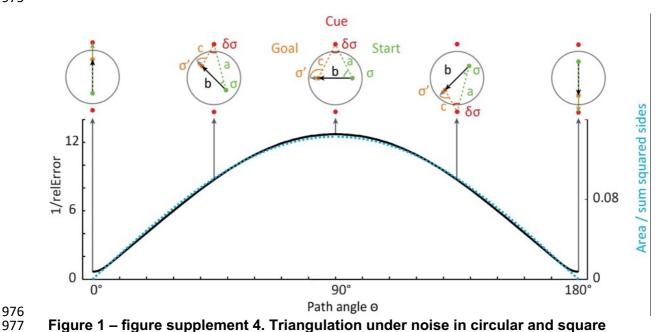


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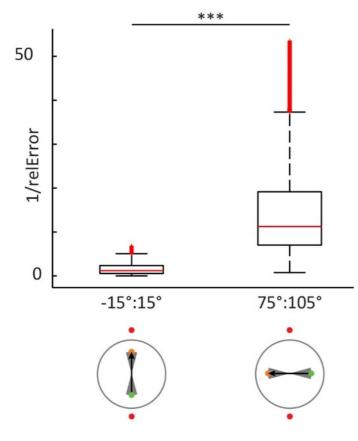
Figure 1 – figure supplement 3. Higher-order uncertainty distributions and self-964 localisation accuracy. A Four-leaf uncertainty distribution. Across different grid orientations 965 the different grid axes are variously aligned and misaligned with the directions of greatest 966 and least certainty. No clear trend for an optimal grid orientation is apparent. B Six-leaf 967 distribution. Across different grid orientations the grid axes are either aligned or misaligned 968 with the high-uncertainty directions, producing the same trend as the simple (two-leaf) 969 970 anisotropic uncertainty distribution. Localisation performance is best when the grid axes are aligned away from the axis of least spatial uncertainty. Error bars indicate 95% confidence 971 interval, n = 150,000. 972



975



977 environments. To test the impact of anisotropic optic flow information on spatial 978 979 computations, we performed a biologically inspired simulation of Euclidean triangulation. For 980 example, an estimate of the distance between start and end points was computed from noisy 981 estimates of the angles and distance to one of the cues using equation 2. All sides (a-c) of a triangle served as both inputs and distance to be estimated, before the results were 982 averaged on one iteration. The median noise resilience (1/relative error [relError]) across 983 iterations is plotted in black. On a given iteration, relErr is determined as the absolute 984 distance error / side length, averaged across the three sides of each triangle. Black arrows 985 indicate example paths between two observer positions (start in green and goal in orange, 986 987 always crossing the centre; see Materials and Methods for details). Red dots show polarising 988 cues. Most accurate triangulation was achieved on paths orthogonal to the polarisation axis (10*10³ repetitions for each triangle, 90° ±15° versus 0° ±15°, two-sided Wilcoxon signed-989 rank test: Z=1026.42, p<0.001). Optimal path angle was well predicted by a quality measure 990 for triangulation (triangle area / sum of squares of the side lengths; R=0.99, p<0.001). This 991 measure increases for more equilateral triangles. 992 993



995

996 Figure 1 – figure supplement 5. Magnitude of noise resilience of directional bin of 997 paths centred on peaks and troughs of Figure S1. The most accurate triangulation was 998 achieved on paths orthogonal to the polarisation axis. 10*10³ repetitions for each triangle, 999 90° ±15° versus 0° ± 15°, two-sided Wilcoxon signed-rank test: Z=1026.42, p<0.001. The 1000 grey shaded area in the bottom panels indicate the range of paths that were tested. The box 1001 1002 edges denote the 25th and 75th percentiles and central red mark the median. The whiskers 1003 extend maximally to $q_3 + 1.5 * (q_3 - q_1)$ and minimally to $q_1 - 1.5 * (q_3 - q_1)$, where q_1 and q_3 1004 are the 25th and 75th percentiles, respectively. A red + denotes points outside this range, 1005 with the exception of the upper 10% of values that were omitted for display purposes. Statistical testing included all data. 1006

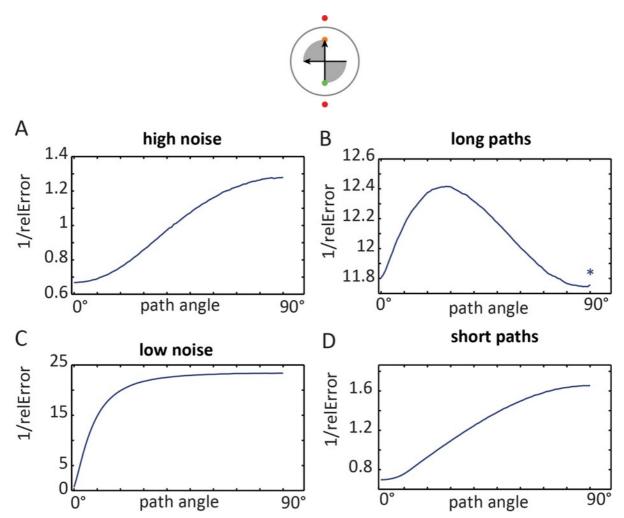


Figure 1 – figure supplement 6. Effects of noise levels and path length on optimal 1009 1010 triangulation paths Environment with a single axis are defined by two cues (analogous to 1011 the two fMRI experiments and the behavioural experiment). All (A, C, D) except the long 1012 path condition (B) yielded an optimum at 90°. However, this extreme case never occurred for 1013 participant's paths in the fMRI experiments due to the limitations of the circular boundary. The average length of straight (+-45°) paths was 11% of the polarisation axis' length in fMRI 1014 1015 experiment 1 (12% in fMRI experiment 2) – See Figure 3 – figure supplement 1E-F. High 1016 noise = randomly sampled from a distribution with a 10 times larger sigma (62.6, instead of 6.26, see Materials and Methods). Low noise = randomly sampled from a distribution with a 1017 10 times smaller sigma (0.626, instead of 6.26). Long paths = simulated path length was 1018 1019 equal to the length of the polarisation axis (instead of 50%, see Materials and Methods). 1020 Short paths = simulated path length was 5% of the length of the polarisation axis (instead of 50%, see Materials and Methods). Asterix = plots have been smoothed with a 5° -wide kernel 1021 1022 for display purposes. The grey shaded area in the top panels indicates the range of paths 1023 that were used. 1024

1008

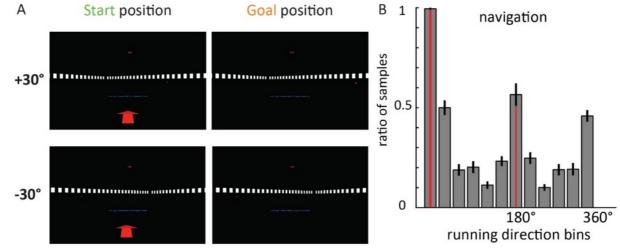
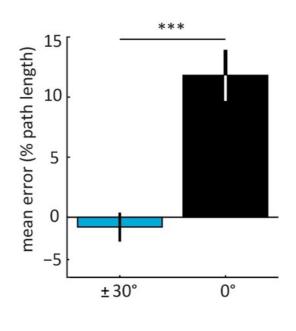




Figure 2 - figure supplement 1. A Additional views of the behavioural experiment at the 1028 beginning (Start) and end (Goal) of a path. Note that the background was rendered at infinity 1029 (see Materials and Methods), such that it did not change during teleportation in the ±30° or 1030 the 0° condition (Figure 2BC). **B** Sampling of movement direction. Participants were not only 1031 exposed to translations in the ±30° and 0° condition, which might force spatial 1032 representations to align with those directions. During free navigation to a start position, all 1033 other directions were sampled, albeit not homogeneously (Friedman test: $\chi^{2}_{(11)}$ =179, 1034 p<0.0001; note that on some trials the start position was on the opposite side of the 1035 1036 environment). 1037





1041 Figure 2 – figure supplement 2. Mean distance estimation error (in percent of correct

1042 **path length) in the behavioural experiment** (Figure 2). Paths along the polarisation axis

1043 (0°) yielded less accurate distance estimation than oblique paths (±30°). Paired, two-sided t-

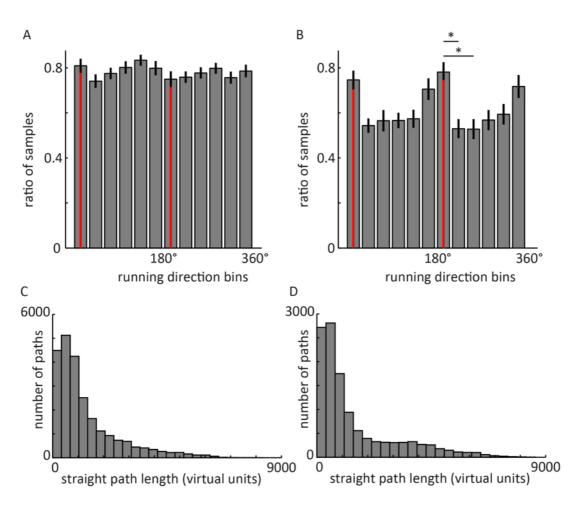
1044 test N=20; $T_{(19)}$ = 5.47, p<0.001. See Figure 2C for an effect in the same direction for

absolute errors. Bars show errors in percent of correct path length averaged across

1046 participants +- S. E. M.; Mean 0° condition = 11.8 %; Mean $\pm 30^{\circ}$ condition = -0.8 %.

1047

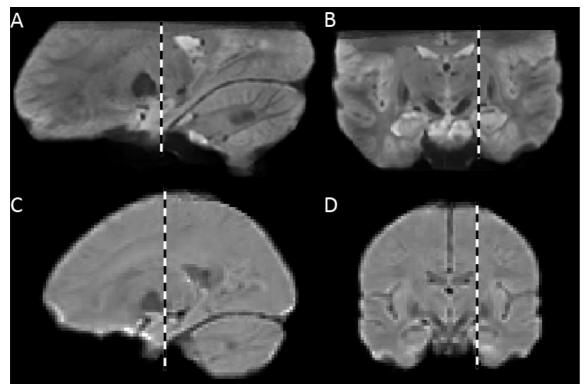
1039 1040



1049 1050

1051 Figure 3 – figure supplement 1. Behavioural analyses of fMRI experiment 1 (A, C, E) 1052 and fMRI Experiment 2 (B, D, F). Spatial memory performance: the decreases in drop error 1053 indicate that participants in both experiments were able to successfully navigate and 1054 remember locations in the sparse virtual environments. Participants learned the locations of 6 objects in fMRI experiment 1 (A) and 4 objects in fMRI experiment 2 (B; See Materials and 1055 1056 Methods). Red line denotes mean drop error (i.e. Euclidean distance in virtual units between 1057 participants' response location and the correct location of a given object on a given trial) across participants. Grey outline denotes standard error of the mean. For display purposes, 1058 results are shown up to trial number 90 for consistency. Variations in the number of trials 1059 1060 across participants were due to differences in self-paced completion of trials. C-D Sampling of running directions. The number of samples of movements in 30° bins of running direction 1061 was normalised within participants for comparability across participants by dividing it by the 1062 1063 maximum number of samples in any of the 12 bins, thereby yielding a maximum value of 1 for a bin. C FMRI experiment 1 (polarisation axis defined by configural cues), N = 26: A non-1064 parametric Friedman test of median differences among repeated measures of directional 1065 sampling was revealed no clear differences ($\chi^2_{(11)}$ =9.5, p=0.57). **D** FMRI experiment 2 1066 1067 (polarisation axis defined by non-configural cues), N = 24: A non-parametric Friedman test of

median differences among repeated measures revealed differences ($\chi^2_{(11)}$ =36.7, p<0.001). Post-Hoc tests with Tukey-Kramer correction for multiple comparisons revealed that particularly runs along the environmental axis at 165° (+-15°) occurred more often than runs oblique at 195° (+-15°) and 125° (+-15°). Asterix: p<0.05 Note that both the absence of a difference in fMRI experiment 1, as well as more frequent runs along the polarisation axis in fMRI experiment 2 speak against the possibility that the environmental effects on hexadirectional activity reported above would be due to biases in navigation behaviour. Error bars show S.E.M. over participants. E-F Distances of running paths. Histograms show the number of straight paths for different distances. Path length was determined as the Euclidean distance between start and end point of a path with continuous movement and rotations of less than +- 45° (i.e. a 90°-wide bin). FMRI experiment 1 (E): mean = 1316.2 vu. FMRI experiment 2 (F): mean = 1493.5 vu.



1093

| 1094 | Figure 5 – figure supplement 1. Mean functional images across participants used as |
|------|---|
| 1095 | template brains. A-B Template for fMRI experiment 1 (7T scanner). C-D Template for fMRI |
| 1096 | experiment 2 (3T scanner). Dashed lines indicate the location of the slice in the |
| 1097 | corresponding orientation in the panel above or below. Template images were created with |
| 1098 | Advanced Neuroimaging Toolbox (ANTS; <u>http://www.picsl.upenn.edu/ANTS/</u>) based on |
| 1099 | individual, mean 3D echo-planar images. Note the relatively high contrast for functional |
| 1100 | images in the 7T data, with clear grey and white matter intensity differences even in the |
| 1101 | medial temporal lobes. |
| 1102 | |

1104 **Competing interest:**

1105 The authors declare no competing interests.

1106

1107 **References**

- Bush, D., Barry, C., Manson, D. & Burgess, N. Using Grid Cells for Navigation.
 Neuron 87, 507–520 (2015).
- Towse, B. W., Barry, C., Bush, D. & Burgess, N. Optimal configurations of spatial
 scale for grid cell firing under noise and uncertainty. *Philos. Trans. R. Soc. Lond. B. Biol. Sci.* 369, 20130290 (2014).
- Hafting, T., Fyhn, M., Molden, S., Moser, M.-B. & Moser, E. I. Microstructure of a
 spatial map in the entorhinal cortex. *Nature* 436, 801–6 (2005).
- Mathis, A., Herz, A. V. M. & Stemmler, M. Optimal Population Codes for Space: Grid
 Cells Outperform Place Cells. *Neural Comput.* 24, 2280–2317 (2012).
- 1117 5. Burak, Y. & Fiete, I. R. Accurate Path Integration in Continuous Attractor Network
 1118 Models of Grid Cells. *PLoS Comput. Biol.* 5, e1000291 (2009).
- Banino, A. *et al.* Vector-based navigation using grid-like representations in artificial
 agents. *Nature* 557, 429–433 (2018).
- 1121 7. Clifford, C. W. G. *et al.* Visual adaptation: Neural, psychological and computational aspects. *Vision Res.* 47, 3125–3131 (2007).
- Sharma, J. *et al.* Spatial attention and temporal expectation under timed uncertainty
 predictably modulate neuronal responses in Monkey V1. *Cereb. Cortex* 25, 2894–
 2906 (2015).
- 1126 9. Stensola, T., Stensola, H., Moser, M.-B. & Moser, E. I. Shearing-induced asymmetry
 1127 in entorhinal grid cells. *Nature* 518, 207–212 (2015).
- 1128 10. Krupic, J., Bauza, M., Burton, S., Barry, C. & O'Keefe, J. Grid cell symmetry is shaped 1129 by environmental geometry. *Nature* **518**, 232–235 (2015).
- 1130 11. Derdikman, D. *et al.* Fragmentation of grid cell maps in a multicompartment
 1131 environment. *Nat. Neurosci.* **12**, 1325–32 (2009).
- 1132 12. Bellmund, J. L. S. *et al.* Deforming the metric of cognitive maps distorts memory. *bioRxiv* 391201 (2019).
- 13. Kunz, L. *et al.* Reduced grid-cell-like representations in adults at genetic risk for
 Alzheimer's disease. *Science (80-.).* **350**, 430–433 (2015).
- 1136 14. Bellmund, J. L. S., Deuker, L., Navarro Schröder, T. & Doeller, C. F. Grid-cell
 1137 representations in mental simulation. *Elife* 1–21 (2016).
- 1138 15. Horner, A. J., Bisby, J. A., Zotow, E., Bush, D. & Burgess, N. Grid-like Processing of
 1139 Imagined Navigation. *Curr. Biol.* 1–6 (2016).
- 1140 16. Nau, M., Navarro Schröder, T., Bellmund, J. L. S. & Doeller, C. F. Hexadirectional

| 1141 | | coding of visual space in human entorhinal cortex. Nat. Neurosci. (2018). |
|------|-----|--|
| 1142 | 17. | Julian, J. B., Keinath, A. T., Frazzetta, G. & Epstein, R. A. Human entorhinal cortex |
| 1143 | | represents visual space using a boundary-anchored grid. Nat. Neurosci. (2018). |
| 1144 | 18. | Stangl, M. et al. Compromised Grid-Cell-like Representations in Old Age as a Key |
| 1145 | | Mechanism to Explain Age-Related Report Compromised Grid-Cell-like |
| 1146 | | Representations in Old Age as a Key Mechanism to Explain Age-Related Navigational |
| 1147 | | Deficits. Curr. Biol. 1–8 (2018). |
| 1148 | 19. | Doeller, C. F., Barry, C. & Burgess, N. Evidence for grid cells in a human memory |
| 1149 | | network. <i>Nature</i> 463 , 657–61 (2010). |
| 1150 | 20. | He, Q. & Brown, T. I. Environmental Barriers Disrupt Grid-like Representations in |
| 1151 | | Humans during Navigation. Curr. Biol. 1–5 (2019). doi:10.1016/j.cub.2019.06.072 |
| 1152 | 21. | Killian, N. J., Jutras, M. J. & Buffalo, E. A. A map of visual space in the primate |
| 1153 | | entorhinal cortex. Nature 5, 3–6 (2012). |
| 1154 | 22. | Carpenter, F. & Barry, C. Distorted Grids as a Spatial Label and Metric. Trends Cogn. |
| 1155 | | Sci. xx , 2–5 (2016). |
| 1156 | 23. | Barry, C., Ginzberg, L. L., O'Keefe, J. & Burgess, N. Grid cell firing patterns signal |
| 1157 | | environmental novelty by expansion. Proc. Natl. Acad. Sci. (2012). |
| 1158 | 24. | Gibson, J. J. Visually controlled locomotion and visual orientation in animals. Br. J. |
| 1159 | | Psychol. 49 , 182–194 (1958). |
| 1160 | 25. | Bates, D., Mächler, M., Bolker, B. & Walker, S. Fitting Linear Mixed-Effects Models |
| 1161 | | Using Ime4. J. Stat. Softw. (2015). |
| 1162 | 26. | Raudies, F. & Hasselmo, M. E. Differences in Visual-Spatial Input May Underlie |
| 1163 | | Different Compression Properties of Firing Fields for Grid Cell Modules in Medial |
| 1164 | | Entorhinal Cortex. PLOS Comput. Biol. 11, e1004596 (2015). |
| 1165 | 27. | Howard, L. R. et al. The Hippocampus and Entorhinal Cortex Encode the Path and |
| 1166 | | Euclidean Distances to Goals during Navigation. Curr. Biol. 1–10 (2014). |
| 1167 | 28. | Sreenivasan, S. & Fiete, I. Grid cells generate an analog error-correcting code for |
| 1168 | | singularly precise neural computation. Nat. Neurosci. 14, 1330–1337 (2011). |
| 1169 | 29. | Stemmler, M. B., Mathis, A. & Herz, A. Connecting Multiple Spatial Scales to Decode |
| 1170 | | the Population Activity of Grid Cells. Sci. Adv. in press, 1–12 (2015). |
| 1171 | 30. | Mathis, A., Herz, A. V. M. & Stemmler, M. B. Multiscale codes in the nervous system: |
| 1172 | | The problem of noise correlations and the ambiguity of periodic scales. Phys. Rev. E - |
| 1173 | | Stat. Nonlinear, Soft Matter Phys. 88, 1–10 (2013). |
| 1174 | 31. | Kubie, J. L. & Fenton, A. a. Linear Look-Ahead in Conjunctive Cells: An Entorhinal |
| 1175 | | Mechanism for Vector-Based Navigation. Front. Neural Circuits 6, 1–15 (2012). |
| 1176 | 32. | Erdem, U. M. & Hasselmo, M. E. A Biologically Inspired Hierarchical Goal Directed |
| 1177 | | Navigation Model. J. Physiol. Paris (2013). |
| | | |

| 1178 | 33. | Wilber, A. A., Clark, B. J., Forster, T. C., Tatsuno, M. & McNaughton, B. L. Interaction |
|------|-----|---|
| 1179 | | of Egocentric and World-Centered Reference Frames in the Rat Posterior Parietal |
| 1180 | | Cortex. <i>J. Neurosci.</i> 34 , 5431–5446 (2014). |
| 1181 | 34. | Taube, J. S. The head direction signal: origins and sensory-motor integration. <i>Annu.</i> |
| 1182 | | <i>Rev. Neurosci.</i> 30 , 181–207 (2007). |
| 1183 | 35. | Kraus, B. J. et al. During Running in Place, Grid Cells Integrate Elapsed Time and |
| 1184 | | Distance Run. <i>Neuron</i> 88, 578–589 (2015). |
| 1185 | 36. | Epstein, R. A. Parahippocampal and retrosplenial contributions to human spatial |
| 1186 | | navigation. Trends Cogn. Sci. 12, 388–96 (2008). |
| 1187 | 37. | Burgess, N. Spatial memory: how egocentric and allocentric combine. Trends Cogn. |
| 1188 | | <i>Sci.</i> 10 , 551–557 (2006). |
| 1189 | 38. | Barry, C., Hayman, R., Burgess, N. & Jeffery, K. J. Experience-dependent rescaling of |
| 1190 | | entorhinal grids. <i>Nat. Neurosci.</i> 10 , 682–684 (2007). |
| 1191 | 39. | Barry, C., Heys, J. G. & Hasselmo, M. E. Possible role of acetylcholine in regulating |
| 1192 | | spatial novelty effects on theta rhythm and grid cells. Front. Neural Circuits 6, 1–13 |
| 1193 | | (2012). |
| 1194 | 40. | Carpenter, F., Manson, D., Jeffery, K., Burgess, N. & Barry, C. Grid Cells Form a |
| 1195 | | Global Representation of Connected Environments. Curr. Biol. 25, 1176–1182 (2015). |
| 1196 | 41. | Navratilova, Z., Giocomo, L. M., Fellous, J. M., Hasselmo, M. E. & McNaughton, B. L. |
| 1197 | | Phase precession and variable spatial scaling in a periodic attractor map model of |
| 1198 | | medial entorhinal grid cells with realistic after-spike dynamics. <i>Hippocampus</i> 22, 772– |
| 1199 | | 789 (2012). |
| 1200 | 42. | Burgess, C. P. & Burgess, N. Controlling Phase Noise in Oscillatory Interference |
| 1201 | | Models of Grid Cell Firing. <i>J. Neurosci.</i> 34 , 6224–6232 (2014). |
| 1202 | 43. | Hardcastle, K., Ganguli, S. & Giocomo, L. M. Environmental Boundaries as an Error |
| 1203 | | Correction Mechanism for Grid Cells. <i>Neuron</i> 1–13 (2015). |
| 1204 | 44. | Elliott, D. The influence of walking speed and prior practice on locomotor distance |
| 1205 | | estimation. <i>J. Mot. Behav.</i> 19 , 476–485 (1987). |
| 1206 | 45. | Wolbers, T., Wiener, J. M., Mallot, H. A. & Büchel, C. Differential recruitment of the |
| 1207 | | hippocampus, medial prefrontal cortex, and the human motion complex during path |
| 1208 | | integration in humans. <i>J. Neurosci.</i> 27, 9408–16 (2007). |
| 1209 | 46. | Bank, R. E. & Smith, R. K. Mesh Smoothing Using A Posteriori Error Estimates. SIAM |
| 1210 | | <i>J. Numer. Anal.</i> 34 , 979–997 (1997). |
| 1211 | 47. | Poser, B. A., Koopmans, P. J., Witzel, T., Wald, L. L. & Barth, M. Three dimensional |
| 1212 | | echo-planar imaging at 7 Tesla. <i>Neuroimage</i> 51 , 261–6 (2010). |
| 1213 | 48. | Navarro Schröder, T., Haak, K. V, Zaragoza Jimenez, N. I., Beckmann, C. F. & |
| 1214 | | Doeller, C. F. Functional topography of the human entorhinal cortex. <i>Elife</i> 4 , 1–17 |
| | | , |

| 1215 | | (2015). |
|------|-----|--|
| 1216 | 49. | Engbert, R. & Kliegl, R. Microsaccades uncover the orientation of covert attention. |
| 1217 | | <i>Vision Res.</i> 43 , 1035–1045 (2003). |
| 1218 | 50. | Manjón, J. V, Coupé, P., Martí-Bonmatí, L., Collins, D. L. & Robles, M. Adaptive non- |
| 1219 | | local means denoising of MR images with spatially varying noise levels. J. Magn. |
| 1220 | | Reson. Imaging 31 , 192–203 (2010). |
| 1221 | 51. | Hutton, C. et al. The impact of physiological noise correction on fMRI at 7T. |
| 1222 | | <i>Neuroimage</i> 57 , 101–112 (2011). |
| 1223 | 52. | Amunts, K. et al. Cytoarchitectonic mapping of the human amygdala, hippocampal |
| 1224 | | region and entorhinal cortex: intersubject variability and probability maps. Anat. |
| 1225 | | Embryol. (Berl). 210 , 343–52 (2005). |
| 1226 | 53. | Amunts, K., Malikovic, a, Mohlberg, H., Schormann, T. & Zilles, K. Brodmann's areas |
| 1227 | | 17 and 18 brought into stereotaxic space-where and how variable? <i>Neuroimage</i> 11 , |
| 1228 | | 66–84 (2000). |
| 1229 | 54. | Bürgel, U. et al. White matter fiber tracts of the human brain: Three-dimensional |
| 1230 | | mapping at microscopic resolution, topography and intersubject variability. |
| 1231 | | <i>Neuroimage</i> 29 , 1092–1105 (2006). |
| 1232 | 55. | Power, J. D., Barnes, K. a, Snyder, A. Z., Schlaggar, B. L. & Petersen, S. E. Spurious |
| 1233 | | but systematic correlations in functional connectivity MRI networks arise from subject |
| 1234 | | motion. <i>Neuroimage</i> 59 , 2142–54 (2012). |
| 1235 | 56. | Berens, P. CircStat: A MATLAB toolbox for circular statistics. J. Stat. Softw. 31, 1–21 |
| 1236 | | (2009). |
| 1237 | | |
| 1238 | | |
| 1239 | | |
| 1240 | | |