2 EMERGING TREND IN VISION SCIENCE

3 Deep learning: Using machine learning

4 to study biological vision

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ABSTRACT

Today most vision-science presentations mention machine learning. Many neuroscientists use

machine learning to decode neural responses. Many perception scientists try to understand

recognition by living organisms. To them, machine learning offers a reference of attainable

performance based on learned stimuli. This brief overview of the use of machine learning in

biological vision touches on its strengths, weaknesses, milestones, controversies, and current

directions.

INTRODUCTION

What does machine learning offer to biological-vision

scientists? We suppose that most of our readers have

heard of machine learning but are wondering how to

interpret machine-learning results and whether it would

be useful in their own research. We begin by naming

some of its pluses and minuses.

PLUSES: WHAT IT'S GOOD FOR

Deep learning is the latest phase of machine learning,

and is becoming very popular (Fig. 1). Is it just a fad? At

the very least, machine learning is a powerful tool for

interpreting biological data. For computer vision, the old

paradigm was: feature detection, segmentation, and

grouping (Marr, 1982). The new paradigm defines just

the task and a feature set, and machine learning builds

the classifier from a training set. Unlike the handcrafted

pattern recognition (including segmentation and

grouping) popular in the 70's and 80's, machine-learning

algorithms are generic, with little domain-specificity. They

replace hand-engineered feature detectors with filters

that can be learned from the data. Advances in the mid

90's in machine learning made statistical learning theory

useful for practical classification, e.g. handwriting

recognition (Vapnik, 1999).

GLOSSARY

Machine learning is a computer algorithm that uses data from the environment to improve performance of a task.

Deep learning is the latest version of machine learning, distinguished by having more than three layers. It is ubiquitous in the internet.

Supervised learning refers to any algorithm that accepts a set of labeled stimuli — a training set — and returns a classifier that can label stimuli similar to those in the training set.

Unsupervised learning works without labels. It is less popular, but of great interest because labeled data are scarce while unlabeled data are plentiful. Without labels, the algorithm discovers structure and redundancy in the data.

Cost function. A function that assigns a real number representing cost to a candidate solution. Solving by optimization means minimizing cost.

Gradient descent: An algorithm that minimizes cost by incrementally changing the parameters in the direction of steepest descent of the cost function.

Convexity: A problem is convex if there are no local minima competing with the global minimum. In optimization, a convex cost function guarantees that gradient descent will always find the global minimum.

Figure 1. Top: The frequency of appearance of each of five terms — "linear classifier", "perceptron", "support vector machine", "neural net" and "backprop" — in books indexed by Google in each year of publication. Frequency is reported as a fraction of all instances of that number of words (1,2, or 3) normalized by the number of books published that year (ngram/year/books published). The figure was created using Google's n-gram viewer (https://books.google.com/ngrams), which contains a yearly count of n-grams found in sources printed between 1500 and 2008. **Bottom:** Numbers represent worldwide search interest relative to the highest point on the chart for the given year for the term "deep learning" (as reported by https://trends.google.com/trends/).

Machine learning allows a neurophysiologist to decode

neural activity without knowing the receptive fields

(Seung & Sompolinsky,1993; Hung et al., 2005).

Machine learning shifts the emphasis from how the cells

encode to what they encode, i.e. from how they encode

the stimulus to what that code tells us about the stimulus.

Mapping a receptive field is the foundation of

neuroscience (beginning with Weber's 1834/1996

mapping of tactile "sensory circles"), but many young

scientists are impatient with the limitations of single-cell recording: looking for minutes or hours

at how one cell responds to each of perhaps a hundred different stimuli. New neuroscientists

Cross validation assesses how well a classifier generalizes. Usually the training and test stimuli are chosen to be identically-distributed independent samples.

Backprop, short for "backward propagation of errors", is widely used to apply gradient-descent learning to multi-layer networks. It uses the chain rule from calculus to iteratively compute the gradient of the cost function for each layer.

Hebbian learning and spike-timing dependent plasticity (*STDP*). According to Hebb's rule, the efficiency of a synapse increases after correlated pre- and post-synaptic activity. In other words, neurons that fire together, wire together (Löwel & Singer, 1992).

Support Vector Machine (SVM) is a learning machine for classification. SVMs generalize well. An SVM can quickly learn to perform a nonlinear classification using what is called the "kernel trick", mapping its input into a high-dimensional feature space (Cortes & Vapnik, 1999).

Convolutional neural networks (ConvNets) have their roots in the Neocognitron (Fukushima 1980) and are inspired by the simple and complex cells described by Hubel and Wiesel (1962). ConvNets apply backprop learning to multilayer neural networks based on convolution and pooling (LeCun et al., 1989; LeCun et al., 1990; LeCun et al., 1998).

are the first generation for whom it is patently clear that characterization of a single neuron's

receptive field, which was invaluable in the retina and V1, fails to characterize how higher visual

areas encode the stimulus. Statistical learning techniques reveal "how neuronal responses can

best be used (combined) to inform perceptual decision-making" (Graf, Kohn, Jazayeri, &

Movshon, 2010).

For psychophysics, Signal Detection Theory (SDT) proved that the optimal classifier for a signal

in noise is a template matcher (Peterson, Birdsall, & Fox, 1954; Tanner & Birdsall, 1958). SDT

has been a very useful reference in interpreting human psychophysical performance (e.g.

Geisler, 1989; Pelli et al., 2006). However, it provides no account of learning. Machine learning

shows promise of guiding today's investigations of human learning and may reveal the

constraints imposed by the training set on learning. It can be hard to tell whether behavioral

performance is limited by the set of stimuli, or the neural representation, or the mismatch

between the neural decision process and the stimulus and task. Implications for classification

performance are not readily apparent from direct inspection of families of stimuli and their neural

responses. SDT specifies optimal performance for classification of known signals, but does not

tell us how to generalize beyond a training set. Machine learning does.

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69   **MINUSES: COMMON COMPLAINTS**
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Some biologists complain that neural nets do not match what we know about neurons (Crick,

1989; Rubinov, 2015). In particular, it is not clear, given what we know about neurons and

neural plasticity, whether a backpropagation network can be implemented using biologically

plausible circuits (but see Mazzoni et al., 1991, and Bengio et al., 2015). With a different,

perspective, engineers and computer scientists, though inspired by biological vision, focus on

what works.

Some biological modelers complain that neural nets have alarmingly many parameters. Deep

neural networks continue to be opaque, especially if the problem is not known to be convex.

Before neural-network modeling, a model was simpler than the data it explained. Deep neural

nets are typically as complex as the data, and the solutions are hard to visualize (but see Zeiler

& Fergus, 2013). However, while the training sets and learned weights are long lists, the

generative rules for the network (the computer programs) are short.

Some cognitive psychologists dismiss deep neural networks as unable to "master some of the

basic things that children do, like learning the past tense of a regular verb" (Marcus et al., 1992).

Some statisticians worry that rigorous statistical tools are being displaced by machine learning,

which lacks rigor (Friedman, 1998; Matloff, 2014, but see Breiman, 2001; Efron & Hastie, 2016).

Assumptions are rarely stated. There are no confidence intervals on the solution. However,

performance is typically cross-validated, showing generalization, and it has been proven that

convex networks can compute posterior probability (Rojas, 1996).

Some of the best classifiers in computer science were inspired by biological principles

(Rosenblatt, 1957; 1958; Rumelhart et al., 1986; LeCun, 1985; LeCun et al. 1989; LeCun et al.

1990; Riesenhuber & Poggio, 1999; and see LeCun, Bengio, Hinton 2015). Those classifiers

are now so good that they occasionally exceed human performance and might serve as models

for how biological systems classify (e.g. Ziskind, Hénaff, LeCun, & Pelli, 2014).

MATHEMATICS VS. ENGINEERING

The history of machine learning has two threads: mathematics and engineering. In the

mathematical thread, two statisticians, Fisher and later Vapnik, developed mathematical

transformations to uncover categories in data, and proved that they give unique answers. They

assumed distributions and proved convergence.

In the *engineering* thread, a loose coalition of psychologists, neuroscientists, and computer

scientists (e.g. Rosenblatt, Minsky, Fukushima, Hinton, Sejnowski, LeCun, Poggio) sought to

reverse-engineer the brain to build a machine that learns. Their algorithms are typically applied

to stimuli with unknown distributions and lack proofs of convergence.

MILESTONES IN CLASSIFICATION

1936: Linear discriminant analysis

1953: Machine learning

1958: Perceptron

1969: Death of the perceptron

1974: Backprop

1980: Neocognitron

1987: NETtalk

1989: ConvNets

1995: Support Vector Machine (SVM)

2006: Backprop, revived

2012: Deep learning

1936: Linear discriminant analysis*. Fisher (1936) introduced linear discriminant analysis to

classify two species of iris flower based on four measurements per flower. When the distribution

of the measurements is normal and the covariance matrix between the measurements is known,

linear discriminant analysis answers the question: Supposing we use a single-valued function to

classify, what linear function $y = w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4$, of four measurements x_1, x_2, x_3, x_4

made on flowers, with free weights w_1, w_2, w_3, w_4, will maximize the ratio of the difference

between the means to the standard deviations within species?[1] Linear classifiers are great for

simple problems for which the category boundary is a hyperplane in a small number of

dimensions. However, complex problems like object recognition typically require more complex

category boundaries in a large number of dimensions. Furthermore, the distributions of the

features are typically unknown and not necessarily normal.

Cortes & Vapnik (1995) note that the first algorithm for pattern recognition was Fisher's optimal

decision function for classifying vectors from two known distributions. Fisher solved for the

optimal classifier in the presence of gaussian noise and known covariance between elements of

the vector. When the covariances are equal, this reduces to a linear classifier. The ideal

template matcher of signal detection theory is an example of such a linear classifier (Peterson et

al., 1954). This fully specified simple problem can be solved analytically. Of course, many

important problems are not fully specified. In everyday perceptual tasks, we typically know only

a "training" set of samples and labels.

1953: Machine learning. The first developments in machine learning were to play chess and

checkers. "Could one make a machine to play chess, and to improve its play, game by game,

profiting from its experience?" (Turing, 1953). Arthur Samuel defined *machine learning* as the

"Field of study that gives computers the ability to learn without being explicitly programmed."

(Samuel, 1959)

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[1] Linear discriminant analysis is an outgrowth of regression which has a much longer history. Regression is the optimal least-squares linear combination of given functions to fit given data and was applied by Legendre (1805) and Gauss (1809) to astronomical data to determine the orbits of the comets and planets around the sun. The estimates come with confidence intervals and the fraction of variance accounted for, which rates the goodness of the explanation.

1958: Perceptron. Inspired by physiologically measured receptive fields, Rosenblatt (1958)

showed that a very simple neural network, the perceptron, could learn to classify from training

samples. Perceptrons combined several linear classifiers to implement piecewise-linear

separating surfaces. The perceptron learns the weights to use in a linear combination of feature-

detector outputs. The perceptron transforms the stimulus into a feature vector and then applies

a linear classifier to the feature vector. The perceptron is piecewise linear and has the ability to

learn from training examples without knowing the full distribution of the stimuli. Only the final

layer in the perceptron learns.

1969: Death of the perceptron. However, it quickly became apparent that the perceptron and

other single-layer neural networks cannot learn tasks that are not linearly separable, i.e. cannot

solve problems like connectivity (Are all elements connected?) and parity (Is the number of

elements odd or even?); people solve these readily (Minsky & Papert, 1969). On this basis they

announced the death of artificial neural networks.

1974: Backprop. The death of the perceptron showed that learning in a one-layer network was

too limited. This impasse was broken by the introduction of the backprop algorithm, which

allowed learning to propagate through multiple-layer neural networks. The history of backprop is

complicated (see Schmidhuber, 2015). The idea of minimisation of error through a differentiable

multi-stage network was discussed as early as the 1960s (e.g. Bryson, Denham, & Dreyfus,

1963). It was applied to artificial neural networks in the 1970s (e.g. Werbos, 1974). In the 1980s,

efficient backprop first gained recognition, and led to a renaissance in the field of artificial neural

network research (LeCun, 1985; Rumelhart, Hinton, & Williams, 1986). During the 2000s

backprop neural networks fell out of favor, due to four limitations (Vapnik, 1999): **1. *No proof of***

convergence. Backprop uses gradient descent. Gradient descent with a nonconvex error

function with multiple minima is only guaranteed to find a local, not the global of the error

function. This has long been considered a major limitation, but Yann LeCun et al. (2015) claim

that it hardly matters in practice in current implementations of deep learning. **2. *Slow*.**

Convergence to a local minimum can be slow due to the high dimensionality of the weight

space. **3. *Poorly specified*.** Backprop neural networks had a reputation of being ill-specified, an

unconstrained number of units and training examples, and a step size that varied by problem.

"Neural networks came to be painted as slow and fussy to train [,] beset by voodoo parameters

and simply inferior to other approaches." (Cox & Dean, 2014). **4. *Not biological*.** Lastly,

backprop learning may not to be physiological: While there is ample evidence for Hebbian

learning (increase of a synapse's gain after correlated activity of the two cells that it connects),

such changes are never propagated farther back, beyond the one synapse, to a previous layer.

1980: Neocognitron, the first convolutional neural network. Kunihiko Fukushima (1980)

proposed and implemented the Neocognitron, a hierarchical, multilayered artificial neural

network. It recognized stimulus patterns (numbers) despite small changes in position and

shape. It didn'

1987: NETtalk, the first impressive backprop neural network. Sejnowski et al. (1987) reported

the exciting success of NETtalk, a neural network that learned to convert English text to speech:

"*The performance of NETtalk has some similarities with observed human performance. (i) The*

learning follows a power law. (ii) The more words the network learns, the better it is at

generalizing and correctly pronouncing new words. (iii) The performance of the networks

degrades very slowly as connections in the network are damaged: no single link or processing

unit is essential. (iv) Relearning after damage is much faster than learning during the original

training. (v) Distributed or spaced practice is more effective for long-term retention than massed

practice."

1989: ConvNets. Yann LeCun and his colleagues combined convolutional neural networks with

backprop to recognize handwritten characters (LeCun et al., 1989; LeCun et al., 1990). This

network was commercially deployed by AT&T, and today reads millions of checks a day

(LeCun, 1998). Later, adding half-wave rectification and max pooling greatly improved its

accuracy in recognizing objects (Jarrett et al., 2009).

1995: Support Vector Machine (SVM). Cortes & Vapnik (1995) proposed the support vector

network, a learning machine for binary classification problems. SVMs generalize well and are

free of mysterious training parameters. Many versions of the SVM are convex (e.g. Lin, 2001).

2006: Backprop, revived. Hinton & Salakhutdinov (2006) sped up backprop learning by

unsupervised pre-training. This helped to revive interest in backprop. In the same year, a

supervised backprop-trained convolutional neural network set a new record on the famous

MNIST handwritten-digit recognition benchmark (Ranzato et al., 2006).

2012: Deep learning. Geoff Hinton says, "it took 17 years to get deep learning right; one year

thinking and 16 years of progress in computing, praise be to Intel." (Cox & Dean, 2014; LeCun,

Bengio, & Hinton, 2015). It is not clear who coined the term "deep learning".[2] In their book, *Deep*

Learning Methods and Applications, Deng & Yu (2014) cite Hinton et al. (2006) and Bengio

(2009) as the first to use the term. However, the big debut for deep learning was an influential

paper by Krizhevsky et al. (2012) describing AlexNet, a deep convolutional neural network that

classified 1.2 million high-resolution images into 1000 different classes, greatly outperforming

previous state-of-the-art machine learning and classification algorithms.

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[2] The idea of "deep learning" is not exclusive to machine learning and neural networks (e.g. Dechter, 1986)

CONTROVERSIES

Unproven convexity. A problem is convex if there are no local minima other than the global

minimum. This guarantees that gradient-descent will converge to the global minimum. As far as

we know, classifiers that give inconsistent results are not useful. Conservation of a solution

across seeds and algorithms is evidence for convexity. For some combinations of stimuli,

categories, and classifiers, convexity can be proved. For others, empirical tests can provide

qualified assurance that the solution is a global minimum. Many widely used networks are not

convex, but still give mostly consistent answers (LeCun, Bengio, & Hinton, 2015). In machine

learning, kernel methods, including learning by SVMs, have the advantage of easy-to-prove

convexity, at the cost of limited generalization. In the 1990s, SVMs were popular because they

guaranteed fast convergence even with a large number of training samples (Cortes & Vapnik,

1995). Thus, when the problem is convex, the quality of solution is assured and one can rate

implementations by their demands for size of network and training sample. Deep neural

networks, on the other hand, generalize well, but are not convex.

Shallow vs. deep networks. The field's imagination has focused alternately on shallow and

deep networks, beginning with the Perceptron in which only one layer learned, to backprop,

which allowed multiple layers and cleared the hurdles that killed the Perceptron. Then SVM,

with its single layer, sidelined the multilayer backprop, and today the multilayer deep learning

seems to reign. Krizhevsky et al. (2012) attributed the success of their network to its 8-layer

depth; it performed worse with fewer layers.

Supervised vs. unsupervised. Learning algorithms for a classifier can be supervised or not,

i.e. need labels for training, or don't. Today most machine learning is *supervised* (LeCun,

Bengio, & Hinton, 2015). The images are labeled (e.g. "car" or "face"), or the network receives

feedback on each trial from a cost function that assesses how well its answer matches the

image's category. In *unsupervised* learning, the network processes images, typically to minimize

error in reconstruction, with no extra information about what is in the (unlabeled) image. A cost

function can also reward decorrelation and sparseness. This allows learning of image statistics

and has been used to train early layers in deep neural networks. Human learning of

categorization is sometimes done with explicitly named objects — "Look at the tree!" — but

more commonly the feedback is implicit. Consider reaching your hand to raise a glass of water.

Contact informs vision.

CURRENT DIRECTIONS

What does deep learning add to the vision-science toolbox? Deep learning is more than

just a souped up regression (Marblestone et al., 2016). Like Signal Detection Theory (SDT), it

allows us to see more in our behavioral and neural data. In the 1940's, Norbert Wiener and

others developed algorithms to automate and optimize signal detection and classification. A lot

of it was engineering. The whole picture changed with the SDT theorems, mainly the proof that

the maximum-likelihood receiver is optimal for a wide range of simple tasks (Peterson et al.,

1954). Later work added prior probability, for a Bayesian approach. Tanner & Birdsall (1958)

noted that, when figuring out how a biological system does a task, it is very helpful to know the

optimal algorithm and to rate observed performance by its *efficiency* relative to the optimum.

SDT solved detection and classification mathematically, as maximum likelihood. It was the

classification math of the sixties. Machine learning is the classification math of today. Both

enable deeper insight into how biological systems classify. In the old days we used to compare

human and ideal classification performance. Today, we can also compare human and machine

learning.

What computer scientists can learn from psychophysics. Computer scientists build

classifiers to recognize objects. Vision scientists, including psychologists and neuroscientists,

study how people and animals classify in order to understand how the brain works. So what do

computer and vision scientists have to say to each other? Machine learning accepts a set of

labelled stimuli to produce a classifier. Much progress has been made in physiology and

psychophysics by characterizing how well biological systems can classify stimuli. The

psychophysical tools (e.g. threshold and signal detection theory) developed to characterize

behavioral classification performance are immediately applicable to characterize classifiers

produced by machine learning (e.g. Ziskind, Hénaff, LeCun, & Pelli, 2014).

Psychophysics. "Adversarial" examples have been presented as a major flaw in deep neural

networks. These slightly doctored images of objects are misclassified by a trained network,

even though the doctoring has little effect on human observers. The same doctored images are

similarly misclassified by several different networks trained with the same stimuli (Szegedy, et

al., 2013). Humans too have adversarial examples. Illusions are robust classification errors. The

blindspot-filling-in illusion is a dramatic adversarial example in human vision. While viewing with

one eye, two finger tips touching in the blindspot are perceived as one long finger. If the image

is shifted a bit so that the fingertips emerge from the blindspot the viewer sees two fingers.

Neural networks lacking the anatomical blindspot of human vision are hardly affected by the

shift. The existence of adversarial examples is intrinsic to classifiers trained with finite data,

whether biological or not. In the absence of information, neural networks interpolate and so do

biological brains. Psychophysics, the scientific study of perception, has achieved its greatest

advances by studying classification errors. Such errors can reveal "blindspots". Stimuli that are

physically different yet indistinguishable are called *metamers*. The systematic understanding of

color metamers revealed the three dimensions of human color vision (Palmer, 1777; Young,

1802; Helmholtz, 1860).

CONCLUSION

Machine learning is here to stay. Deep learning is better than the "neural" networks of the

eighties. Machine learning is useful both as a model for perceptual processing, and as a

decoder of neural processing, to see what information the neurons are carrying. The large size

of the human cortex is a distinctive feature of our species and crucial for learning. It is

anatomically homogenous yet solves diverse sensory, motor, and cognitive problems. Key

biological details of cortical learning remain obscure, and may preclude backprop, but the

performance of current machine learning algorithms is a useful benchmark.

ACKNOWLEDGEMENTS

288   Thanks to Yann LeCun for helpful conversations. Thanks to Aenne Brielmann and Laura Suciu

289   for helpful comments on the manuscript.

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