

1 **Title:** The relative fitness of drug resistant *Mycobacterium tuberculosis*: a modelling study of
2 household transmission in Peru

3

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25

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27

28 **Abstract**

29

30 The relative fitness of drug resistant versus susceptible bacteria in an environment dictates resistance
31 prevalence. Estimates for the relative fitness of resistant *Mycobacterium tuberculosis* (*Mtb*) strains are
32 highly heterogeneous and mostly derived from *in-vitro* experiments. Measuring fitness in the field
33 allows us to determine how the environment influences resistance spread.

34 We designed a household structured, stochastic mathematical model to estimate the fitness
35 costs associated with multi-drug resistance (MDR) carriage in *Mtb* in Lima, Peru between 2010-2013.
36 By fitting the model to data from a large prospective cohort study of TB disease in household contacts
37 we estimated the fitness, relative to susceptible strains with a fitness of 1, of MDR-*Mtb* to be 0.33
38 (95% credible interval: 0.17-0.54) or 0.39 (0.26-0.58), if only transmission or progression to disease,
39 respectively, was affected. The relative fitness of MDR-*Mtb* increased to 0.57 (0.43-0.73) when the
40 fitness cost influenced both transmission and progression to disease equally.

41 We found the average relative fitness of MDR-*Mtb* circulating within households in Lima,
42 Peru between 2010-2013 to be significantly lower than concurrent susceptible-*Mtb*. If these fitness
43 levels do not change, then existing TB control programmes are likely to keep MDR-TB prevalence at
44 current levels in Lima, Peru.

45

46 **Background**

47

48 *Mycobacterium tuberculosis* (*Mtb*) is a highly prevalent bacterium, thought to infect just under a
49 quarter of the world's population [1]. Treatment of tuberculosis (TB) disease is not simple and drug-
50 susceptible tuberculosis (DS-TB) requires a multiple drug regimen taken for at least 6 months [2].
51 Multidrug-resistant tuberculosis (MDR-TB) treatment regimens are significantly longer, cause serious
52 side effects and are very expensive [3]. Whilst currently 5% of all TB cases globally are estimated to
53 be MDR-TB [2], predicting the future burden of DS- and MDR-TB is essential for TB control
54 programmes.

55 One key parameter that determines the future prevalence of drug resistant TB is the relative
56 fitness of drug resistant *Mtb* strains as compared to drug susceptible *Mtb* strains [4-7]. Fitness is a
57 complex, environment-dependent trait that can be defined as the ability of a pathogen to survive,
58 reproduce, be transmitted and cause secondary cases of disease. These abilities are affected by
59 multiple environmental factors such as a host's genetics, the current TB treatment regimen and other
60 risk factors for transmission, which are all time-varying. The importance of this parameter has been
61 highlighted by several mathematical models which show how even small changes in its value can
62 predict widely varying future levels of MDR-TB burden [4-6, 8, 9]. Thus, gaining environment
63 dependent, accurate estimates of fitness is of critical importance.

64 Within *Mtb*, it has been shown that the appearance of drug resistance mutations affects fitness
65 [10-12]. These previous studies have shown that resistant *Mtb* is, usually, less fit than susceptible *Mtb*
66 under a range of fitness definitions: either by demonstrating a lower growth rate *in vitro* (e.g. [13]),
67 less progression to disease after inoculation in guinea pigs (e.g. [14]) or a lower chance of causing
68 secondary cases of disease (e.g. [12, 15]). The latter definition is important for epidemiological
69 predictions of burden, whilst the first provides the potential underlying biological cause. The
70 epidemiological fitness of a *Mtb* strain can be split into an ability to (1) cause secondary infections
71 (transmission) and (2) cause subsequent active disease (progression). For example, resistant *Mtb* may
72 be transmitted equally as well, but subsequent disease rates in those infected may be lower or less

73 severe. For *Mtb* this split is especially pertinent due to the importance of the latent, non-infectious,
74 stage of disease.

75 Also highly important for *Mtb* is the spatial location of transmission [16]. Few studies have
76 considered the critical influence of household structure on transmission of *Mtb*. To our knowledge, no
77 studies have considered the spread of drug-resistant tuberculosis in the context of a household-
78 structured stochastic mathematical model.

79 The difference in definitions of fitness and corresponding experimental data makes translation from
80 data analysis to predictive mathematical modelling difficult. Here, we tackle this problem by fitting a
81 mathematical model to a detailed data set on the transmission of *Mtb* strains collected in a large
82 cohort study of households undertaken in Lima, Peru between 2010 and 2013 [17]. We derive
83 estimates of fitness in this specific setting with different fitness definitions (either effects on
84 transmission and/or progression to disease) and test the robustness of these estimates under a range of
85 assumptions. These parameters will allow for better predictions of future MDR-TB levels and an
86 improved understanding of MDR-TB spread.

87 **Methods**

88

89 *Data*

90 The details of the study and participants can be found in [17]. Briefly, 213 and 487 households were
91 recruited with an index case of diagnosed MDR- or DS-TB respectively during 2010 to 2013.
92 Households were followed up for variable periods of time up to a maximum of 3 years (Figure S1).
93 During the study households were visited every 6 months, and household contacts were monitored for
94 TB disease. It was found that 35/1055 (3.32%, 95% CI [2.32, 4.58]), of the MDR-TB contacts, and
95 114/2356 (4.84%, 95% CI [4.01, 5.78]), of the DS-TB contacts developed TB disease, suggesting that
96 DS-TB has higher fitness. There were no significant differences between cohorts by HIV status, age,
97 gender or household size [17].

98 The specific data used to calibrate the model was 1) the incidence of MDR-TB and 2) DS-TB
99 in households with an index DS-TB case and 3) the incidence of MDR-TB and 4) DS-TB in
100 households with an index MDR-TB case (Table 1). The percentages of incident cases with resistance
101 profiles matching the index was used to multiply the incidence levels accordingly.

102

103 *Model structure*

104 The mathematical model was a standard two-strain dynamic TB model (Figure 1), with transmission
105 modelled at the level of the household. A Gillespie stochastic simulation algorithm in R [18] was
106 developed using the R package “GillespieSSA” [19]. Using a stochastic transmission model was
107 important as the model was implemented independently in households where the small populations
108 mean stochastic effects are highly important. We assumed that saturation of transmission could occur
109 and hence scaled our transmission rate by the size of the household (number of people), assuming
110 households have the same ventilation level (or at least that this did not vary by index case *Mtb*
111 resistance status) and within-household homogeneous mixing [20]. This assumption of frequency-
112 dependent transmission means that in households with more people, household members are assumed
113 to have lower individual chance of infection from an active disease case than in smaller households,
114 due to decreased exposure. This has been observed for another airborne pathogen, influenza [21] and

115 was explored in sensitivity analysis where we also considered density-dependent transmission. All
116 natural history parameters were taken from the literature, are listed in Table 2 and the dynamics
117 explained in the legend to Figure 1.

118 Four parameters were estimated from the data (Table 1, Figure 1): (1) the per capita
119 transmission rate of DS-TB within households (β_s), (2) the relative fitness of MDR-*Mtb* strains vs.
120 DS-*Mtb* strains (f) expressed as an effect on transmission or progression or both, and the external (to
121 households) force of infection (foi) of (3) DS-TB foi_s , and (4) MDR-TB foi_r .

122 Our main outcome was the impact of resistance on transmission rates, but we also explored
123 the impact on an approximate effective reproduction number (see S1 text).

124

125 *Three model formulations*

126 Resistant strains were allowed to have an equal or lower fitness relative to susceptible strains. The
127 mechanisms behind this reduction were estimated to affect two different rates: the transmission rate,
128 the rate of progression to disease, or both (Figure 1). We assumed that the fitness of the resistant
129 strains could not rise above that of susceptible strains due to the data from the household cohort [17].

130 Model 1 (transmission fitness cost model) assumed that fitness costs directly affected the number of
131 secondary infections by reducing the transmission parameter for MDR-*Mtb* ($0 < f_1 < 1, f_2 = 1$, Figure
132 1). This is the standard assumption for the effect of resistance on fitness for transmission dynamic
133 models of *Mtb* [6, 9, 22] and other pathogens [23]. Model 2 (progression fitness cost model) assumed
134 that although MDR-TB transmission occurred at the same rate as DS-TB, there is a fitness cost to
135 progression to disease ($f_1 = 1, 0 < f_2 < 1$, Figure 1). Model 3 assumed that there was a fitness cost to
136 both transmission and progression, and that the cost was the same for both processes ($0 < f_1 = f_2 < 1$,
137 Figure 1). We could not explore a Model with fitness affecting both processes at differing levels as we
138 did not have data on levels of infection. Without this data, a model with high transmission fitness cost
139 but low progression cost would be equally as likely as a model with a low transmission fitness cost
140 but a high progression cost and hence would be uninformative. Note that fixing either f_1 or f_2 equal to
141 one is the same as ignoring this parameter altogether and leaving the multiplied rate at its background
142 level as they are both scalar constant parameters with no units.

143

144 *Model simulation*

145 The model initially sampled 700 household sizes (with replacement) from the exact distribution of
146 household sizes in the trial [24]. Initial number with latent infection were sampled from a normal
147 distribution generated by data from the literature [2, 25] (S1 text). The model was then simulated for
148 10 years with a MCMC sampled set of the four unknown parameters (pre-study period), capturing
149 transmission within the household prior to enrolment in the household study. A random time point
150 from over this 10-year period in which there was at least one active case with the same sensitivity as
151 the initial case in the household (i.e. DS-TB or MDR-TB) was taken to be the time the household
152 entered the study and the active index case was detected. This allows for simulation of changes in
153 latency in the household and provides initial conditions dependent upon each parameter sample.

154 The above randomly chosen time point of entry to the study was taken to be the initial
155 conditions for the simulation of the model that was fitted to the household study [17] (study period).
156 The same values of the four unknown parameters was used as in the pre-study period and the
157 simulation time for each household was randomly sampled (with replacement) from the exact
158 distribution of follow-up times in the study (Figure S1). The only parameter that changed, to match
159 the altered patient care in the study, was the case detection rate which increased for the study period
160 from the WHO estimates to a screen occurring every 6 months (Table 2).

161 The TB incidence from the model was calculated by determining the total number of new
162 cases of active TB in all 700 households over the follow-up time, and dividing this by the total
163 number of follow-up years in these households. The total number of follow-up years was a product of
164 the number of household members and the follow-up time for the household taking into account any
165 deaths over this time. We assumed that no-one left the households other than by death (natural or due
166 to TB). For a detailed overview of the process see Figure S2.

167

168 *Model fitting*

169 Approximate Bayesian Computation (ABC) was paired with Markov chain Monte Carlo (MCMC)
170 methods to estimate the four unknown parameters [26]. All other parameters were kept fixed at their

171 baseline value (Table 2). The summary statistic used was the TB incidence from the model falling
172 within the 95% CI for all four TB incidence measures from the data. Uniform priors were assumed for
173 all four parameters (Table 1).

174 To estimate the standard deviation required for the MCMC for the four unknown parameters,
175 Latin Hypercube Sampling (LHS) from the prior ranges was initially used (Stage A, S1 text). The
176 empirical standard deviation from the accepted fits was then used as proposal distribution of a
177 Metropolis-Hastings MCMC sampler (Stage B), used to estimate posterior probabilities of the
178 parameters.

179 We used the generated trajectories to consider the probability of remaining free of
180 tuberculosis from the model output and compare the general trends to the data (Figure 2 from [17]).

181

182 *Scenario analysis*

183 A scenario analysis was used to explore the sensitivity of Model 1 results to key natural history
184 parameters. Firstly, we changed the initial proportion of the population latently infected with MDR-
185 *Mtb* from 2% to 10%.

186 A full sensitivity analysis of the parameters kept fixed in the model fits was not possible due
187 to limitations imposed by computation time. Instead, to determine which further scenarios to explore,
188 we determined the parameters most correlated with TB incidence in our model, and hence likely to
189 have the biggest impact on our model fit and parameter estimates. To determine these parameters, we
190 used LHS to choose 10,000 parameter sets from (uniform) prior distributions for all parameters (Table
191 2). We then ran Model 1 with these 10,000 parameter sets and determined the parameters that were
192 statistically significantly correlated with any of the four TB incidence outputs (Kendall correlation, p
193 < 0.01). These parameters were then used to design two scenarios - one with a combination of these
194 parameters at their prior values which gave highest TB incidence and the combination which gave the
195 lowest TB incidence.

196 We also increased our 10-year initial run-in period for the population to 30 years and explore
197 the impact on the estimates. Furthermore, we explored removing the assumption of saturating

198 household transmission (per capita transmission rate was then not dependent on household size, i.e.
199 density-dependent transmission).
200 All code is available online [27].

201 **Results**

202

203 *Fit to the data*

204 Model structures 1-3 could all replicate the data from the household study (Figure 2). The MCMC
205 trace and density plots of the posterior distributions are shown in S1 Text.

206

207 *Parameter estimates*

208 The estimates of the external force of infection for DS- and MDR-TB were similar across the three
209 models (Table 3, Figure 3). The per capita transmission rate of DS-TB within households was also
210 similar across the three models. The relative fitness of MDR-*Mtb* was similar for Model 1 and 2, but
211 increased in Model 3, as might be expected as in this third model the reduction in fitness is applied to
212 two rates. For Model 1, that is assuming a resistance phenotype affects transmission, the relative
213 fitness of MDR-*Mtb* was estimated to be 0.33 (median, 95% CI: 0.17-0.54) vs. DS-*Mtb* with a fitness
214 of 1. In Model 2, where a resistance phenotype affected disease progression, a similar relative fitness
215 was estimated: 0.39 (0.26-0.58). If both rates were affected, then the relative fitness of MDR-*Mtb* was
216 estimated to be 0.57 (0.43-0.73) (Table 3, Figure 3).

217 Comparing the external force of infection for DS- vs. MDR-TB we found that the ratio of the
218 two was around 0.5 (median estimate 0.42 / 0.54 / 0.55 from the three models). This single value for
219 the external force of infection (f_{oi}) represents a complex set of processes (contact patterns, length of
220 infectiousness etc.) and so cannot be used to determine relative fitness. However, the ratio is in the
221 range that supports our estimates of the relative fitness from the internal household model. The ratio
222 of an approximate effective reproduction number for MDR- and DS-TB also supported our main
223 results (see S1 Text).

224

225 *Probability of remaining free from tuberculosis*

226 We explored the probability of remaining free from tuberculosis as was presented from the original
227 study (Figure 2 in [17]). By comparison we had highly similar dynamics to the study (Figure 4a vs.
228 (b-d)).

229

230 *Scenario analysis*

231 Our five scenarios gave very similar estimates for the relative fitness of MDR-*Mtb* (a range of
232 medians from 0.22 – 0.41, S1 text). This suggests that the estimates of relative fitness are robust to:
233 increasing the initial proportion of households that were initially infected with latent MDR-*Mtb* from
234 2% to 10% (in the pre-study), setting TB incidence to high or low levels (see S1 text for parameter
235 details), extending the initial run-in period from 10 to 30 years or removing the saturation of
236 transmission within households.

237

238 **Discussion**

239

240 Our results suggest that the average relative fitness of MDR-*Mtb* strains circulating in households in
241 Lima, Peru in 2010-2013 was substantially lower than that of drug susceptible strains (~40-70%
242 reduction). When a resistance phenotype was assumed to affect both transmission and progression to
243 disease rates, then the relative fitness of MDR-TB strains was ~60%.

244 The strengths of this study are that we were able to fit a stochastic household-level model to
245 detailed location-specific data, accounting for accurate distributions of both household size and study
246 follow-up time. We were also able to differentiate between internal and external transmission,
247 matching the resistance typing data from the household study [17]. Moreover, our transmission rate
248 estimates account for the longer infectiousness of MDR-TB cases (due to delays in diagnosis and
249 treatment initiation etc.). This model and its MCMC fitting algorithm can be applied to other settings
250 and then used as the basis for predictions of future levels of DS- and MDR-TB. In particular, this
251 novel way of estimating fitness costs, by fitting dynamic transmission models to resistance-specific
252 incidence data could be used for other TB prevalent settings or for other bacteria. Furthermore, the
253 estimates given can be directly translated into dynamic transmission models for prediction whilst
254 previous estimates, for example of differences in growth rates have less clear epidemiological
255 translations.

256 Our modelling analysis is limited by the assumption of homogeneity - of both hosts and
257 strains. The characteristics of the DS- and MDR-TB contacts under consideration in the underlying
258 household study were highly similar [17]. Thus, as our estimate is of a relative fitness we believe that
259 including host differences in our model may have had little effect on our relative results. Strain
260 heterogeneities however, mean that our result is (potentially) an average across many different drug
261 resistant strains. It is known that differences in resistance and compensatory mutation combinations
262 result in a diversity in fitness across strains [13]. This diversity is highly important for predictions of
263 MDR-TB levels in the future [28]. Our estimate must therefore be taken as a population average in
264 Lima, at a certain time and indicative of the mean fitness rather than an indicator of the range of
265 potential fitness in the population. If one highly fit MDR-TB strain were to emerge (or were already

266 present), then future prevalence predictions based on our (mean) estimate could be an underestimate.
267 We fitted the model to data with confidence intervals that were derived without fully accounting for
268 the dependency of infection between household members. Improving methods for robust
269 approximation of parameters from mechanistic models that take full account of such dependencies is
270 an important active area of research [29], and will improve future studies of this kind.

271 Our Model 1, where a transmission effect is assumed, is the most similar to previous models
272 of MDR-TB transmission [6, 9, 22]. Reductions in transmission could arise from many factors
273 including differences in location of infection (pulmonary vs. non-pulmonary), a different interaction
274 with the basic immune system or different aerosolization levels. However, our MDR-TB fitness
275 predictions are at the lower end of the range seen previously [10]. This may reflect the situation in
276 Peru where there is a strong tuberculosis control infrastructure with a well-developed MDR-TB
277 treatment program and a growing economy. These two factors may have combined to limit the spread
278 of MDR-TB and hence prevent the adaptation of MDR-TB to a higher fitness. At the bacterial level,
279 compensatory fitness mutations that could influence the ability of drug resistant *Mtb* strains to spread
280 may not have emerged or not been allowed to spread. Calibrating the model to other settings would
281 help clarify this issue. Alternatively, it may be that our estimates are providing, for the first time, a
282 better direct translation of fitness from epidemiological data to a transmission model parameterisation.

283 There is a paucity of evidence for whether differences in TB disease prevalence in general are
284 due to infection or progression to disease [30]. In particular, for resistant strains it is unclear where the
285 effect of becoming resistant should be applied in the natural history of tuberculosis infection. Both
286 Snider and Teixeira [31, 32] demonstrated similar levels of tuberculin skin test (TST) conversion
287 among MDR- and DS-TB household contacts but lower levels of disease in contacts of those with
288 MDR-TB. This was also seen in a recent study in children [33], whilst a higher prevalence of TST
289 positivity was found in household contacts of MDR-TB patients than contacts of newly diagnosed TB
290 patients in Viet Nam [34]. This evidence combines to suggest that the fitness cost to resistance, if any,
291 was to be observed on the progression to disease. We make this assumption in our Model 2, where the
292 hypothesis is that those with active TB disease, whether due to resistant or susceptible bacteria, have a
293 similar bacterial load and hence ability to transmit successfully. However, once successfully

294 established in a new host, resistant bacteria may be less able to combat the immune system and
295 establish a disease state. This has been assumed in a previous model of HIV and MDR-TB interaction
296 [35].

297 Previous models have assumed that resistant strains could become more fit (i.e. have a
298 relative fitness greater than 1), whilst we capped the relative fitness of the resistant strains at 1, due to
299 the data from previous studies and the literature [13, 36]. Our posterior parameter distributions for the
300 estimated relative fitness parameter (reflected in the 95% CI for f , see S1 text) suggest that this is a
301 valid assumption for the resistant strains circulating at this time in Lima. Importantly, all our
302 estimates are of “relative” fitness, and therefore should be robust to changes in natural history
303 assumptions as these would affect both drug susceptible and resistant strain transmission.

304 Future work will include adding in detail on host and strain heterogeneity to the model. Data
305 collection of strain heterogeneity along with active contact tracing and an understanding of where and
306 from whom transmission occurs would drastically improve our understanding of fitness and hence
307 improve estimates of future MDR-TB levels. Exploring the external infection methods and potential
308 changes in this force of infection over time (i.e. making it dynamic as in [37].) would allow for
309 models that can predict levels of MDR-TB in Lima. Future predictive transmission modelling using
310 our relative fitness estimates are likely to suggest that if treatment objectives are maintained and this
311 fitness measure remains constant, that MDR-TB prevalence will remain under control in Lima in the
312 short term.

313 In conclusion, we find the fitness cost of drug resistance in *Mtb* in Lima Peru to be
314 substantial. Importantly this paper provides direct transmission model estimates, using a novel
315 method, of the relative fitness levels of drug resistant *Mtb* strains. If these fitness levels do not change,
316 then the existing TB control programmes are likely to keep MDR-TB prevalence at their current
317 levels in Lima, Peru. These estimates now need to be gained for *Mtb* in other settings and the values
318 used in models to explore future global burden.

319

320 **Competing interests**

321 We have no competing interests.

322

323 **Author's contributions**

324 GMK and LG conceived of, and designed the study, with support from MZ, RHG and JF; GMK
325 performed the mathematical modelling, with calibration support from SF. All authors contributed to
326 analysis and interpretation. The manuscript was drafted by GMK, MZ, SF and LG, with support from
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328

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485

486 **Figure Legends**

487

488 Figure 1: A standard natural history, transmission model for two strains (susceptible and resistant) of
489 *Mtb* was used (diagram on the left). Uninfected people become infected at a rate dependent on the
490 number of active cases (dynamic transmission). Once infected, the majority of people (85%) are
491 assumed to enter a Latent slow (LS / LR) state. The remainder enter a rapid progression (Latent fast,
492 LFS / LFR) state which has a higher rate of progression to active disease (AS / AR). Resistance
493 mutations are acquired during active disease. Those with active disease recover to the Latent slow
494 state via treatment or natural cure. The fitness cost to resistance is assumed to affect the rate of
495 transmission (f_1) or the rate at which those latently infected with MDR-TB progress to active disease
496 (f_2). Only the effect on primary transmission of f_1 is highlighted here, but reinfection is also decreased.
497 f_1 and f_2 are set at 1 or allowed to vary between 0 and 1 in the three separate models: f_1 in Model 1, f_2
498 in Model 2 and both f_1 and f_2 in Model 3. The four estimated parameters (shown in the diagram on the
499 right) were rates of internal transmission (β_s, f) and the external forces of infection ($foi_s + foi_r$).

500

501 Figure 2: Model fits. Black dots represent Model 1 output that matches to data shown in ranges for
502 each type of household (HH). See SI text Figures S3&S4 for equivalent plots for Model 2&3.

503

504 Figure 3: Fitted parameters from each Model. The units for the y-axis of the corresponding plots are:
505 for the external forces of infection ($'foi_s'$ and $'foi_r'$) proportion infected per year, for the relative
506 fitness (f) there are no units and for the per capita transmission rate ('beta') the units are effective
507 contact rate per year. Model 1 assumes a transmission cost to resistance, Model 2 a disease
508 progression cost and Model 3 assumes an effect on both.

Table 1: Fitted parameters with description, prior distributions, any differences by model structure and data used for fitting. All parameters are fitted to the TB incidence data from the household (HH) study (17). The three models have different assumptions around the effect of decreased fitness, with f varying to be f_1 (affects transmission rate) or f_2 (affects progression to disease rate) (see Figure 1).

Symbol	Parameter description	Prior Distribution	Model 1	Model 2	Model 3	Data
foi_s	External force of infection of DS-TB	Uniform [0; 0.5]	/			DS-TB incidence in MDR-TB index HH: 4264 [3916, 4338]
foi_r	External force of infection of MDR-TB	Uniform [0, 0.3]	/			MDR-TB incidence in DS-TB index HH: 87 [13, 435]
f (f_1, f_2)	Relative fitness of MDR-TB strains compared to DS-TB strains, which have a fitness of 1	Uniform [0, 1]	$0 < f_1 < 1$ $f_2 = 1$	$f_1 = 1$ $0 < f_2 < 1$	$f_1 = f_2$ $0 < f_1 < 1$	MDR-TB incidence in MDR-TB index HH: 2112 [1646, 2358]
β_s	Per capita transmission rate of DS-TB within households	Uniform [90, 140]	/			DS-TB incidence in DS-TB index HH: 4264 [3916, 4338]
β_r	Per capita transmission rate of MDR-TB within households	Calculated from other fitted parameters: $\beta_r = f_1 \beta_s$				

households		
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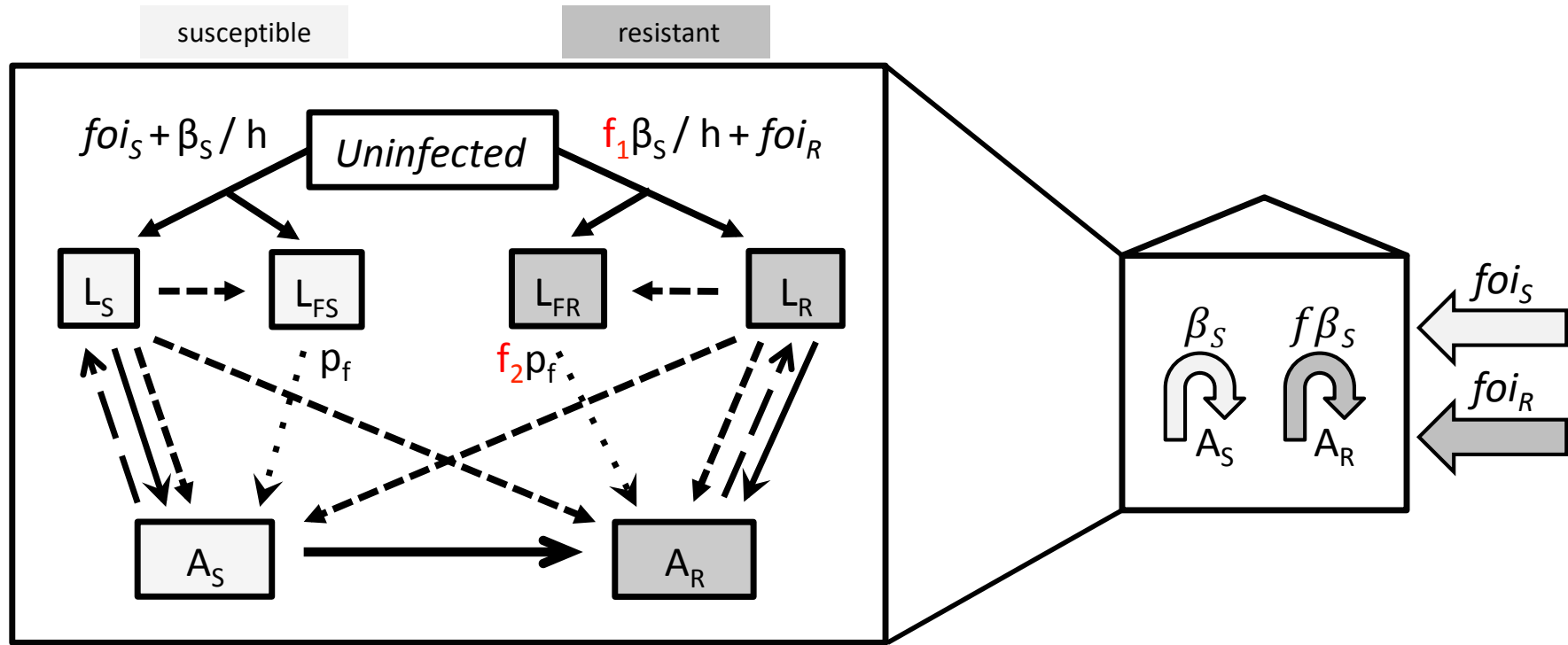
Table 2: Parameter values with description and baseline values. All prior distributions were uniform.

Symbol	Parameter description	Baseline value	Prior distribution	Notes and references
Nr	Number of households with MDR-TB index case	213	/	[24]
Ns	Number of households with DS-TB index case	487	/	[24]
h	Household size	2 - 15	/	[17]
p	Proportion of (re-)infected individuals which progress to the “latent fast” state	0.15	0.08-0.25	[38-40]
χ	Protection from developing active TB upon re-infection	0.35	0.25-0.45	[38, 41-44]
ϕ	Rate of reactivation among those latently infected per year	1.13×10^{-4}	$1 - 3 \times 10^{-4}$	[38, 41, 42, 44-46]
ε	Probability of acquiring new drug resistance during treatment	0:008	0.005-0.01	[47]
d	Proportion of new active cases which directly become infectious	0.5	0.25-0.75	[38, 44, 48, 49]
μ	Background death rate	$1/77 = 0.013$	0.012-0.014	Inverse of average life expectancy in Peru [50]
μ_A	Additional death rate of those actively infected and infectious per year	0.26	0.2-0.4	[38]
n	Annual rate of natural cure for	0.2	0.15-0.25	[38]

	TB cases (returns to latent state)			
ω_s	Proportion of DS-TB active cases detected and treated per year	0.8; 2	0.5-0.95	For 2012 [2] for prestudy; In study: screen every 6 months
ω_r	Proportion of MDR-TB active cases detected and treated per year	0.64; 2	0.2-0.9	79% of the above 80% (ω_s) found that received DST in 2012 [51]; In study: screen every 6 months
$(1 - k_s)$	Proportion of DS-TB active cases started on treatment that are successfully cured	0.74	0.5-0.9	[51, 52] (for midpoint of study)
$(1 - k_r)$	Proportion of MDR-TB active cases started on treatment that are successfully cured	0.6	0.2-0.9	For 2012 [2]
p_f	Progression rate of latent fast individuals to active disease	0.2	0.1-0.9	Duration of fast latency period of 5 years [42]

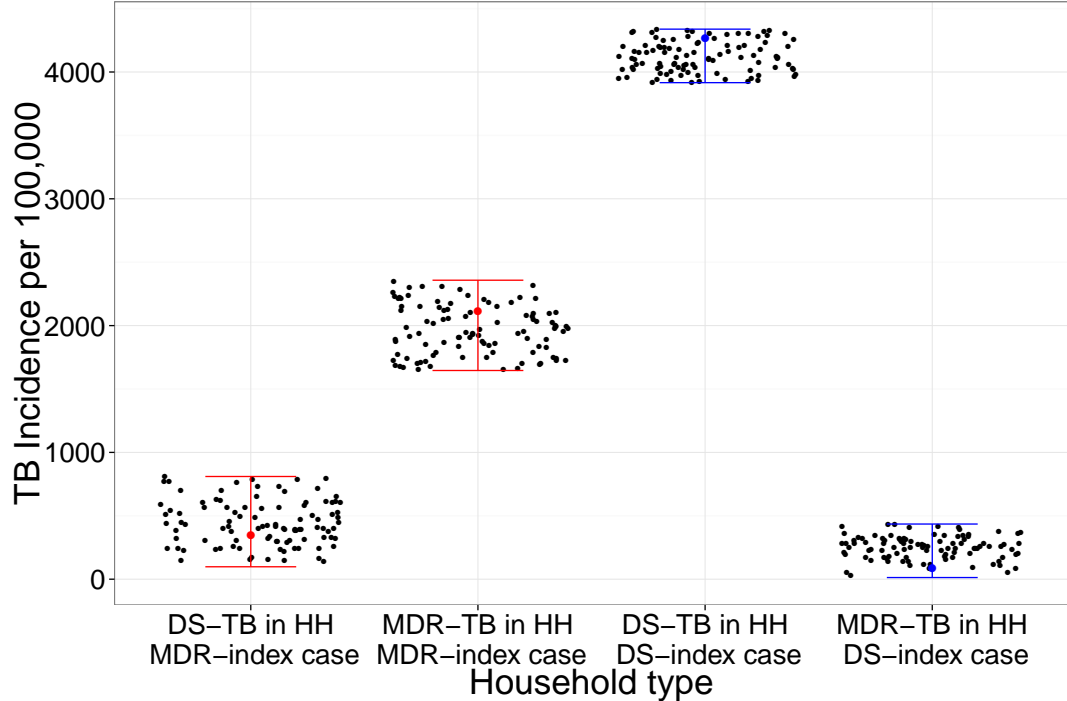
Table 3: Parameter estimates for the median and 95% credible intervals of the four unknown parameters from at least 100 5,000 MCMC runs. The fitness cost to resistance is assumed to affect transmission in Model 1, progression to active disease in Model 2 and both transmission and progression in Model 3.

Model	foi_s	foi_r	β	f
1	0.19 (0.04 – 0.42)	0.08 (0.00 – 0.22)	69.95 (53.78 – 86.86)	0.33 (0.17 – 0.54)
2	0.24 (0.06 – 0.46)	0.13 (0.01 – 0.28)	69.39 (53.46 – 86.49)	0.39 (0.26 – 0.58)
3	0.20 (0.05 – 0.43)	0.11 (0.01 – 0.27)	70.46 (54.14 – 88.19)	0.57 (0.43 – 0.73)

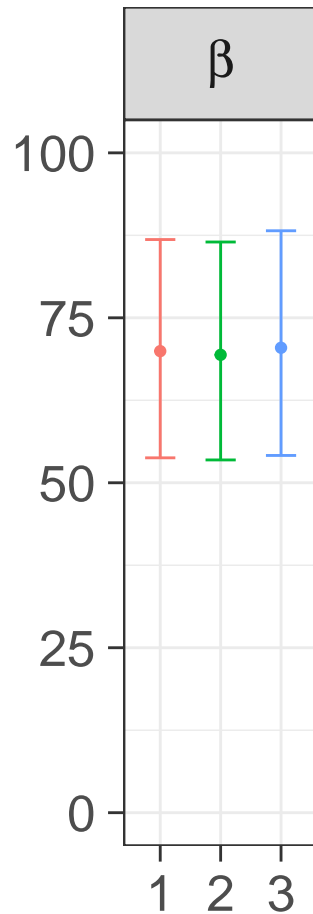
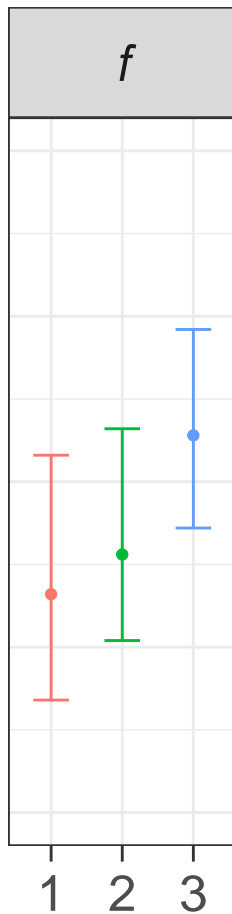
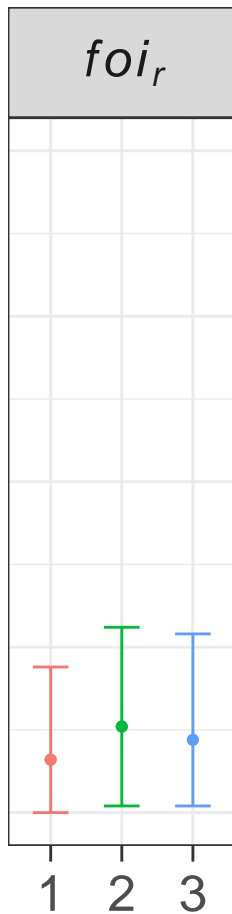
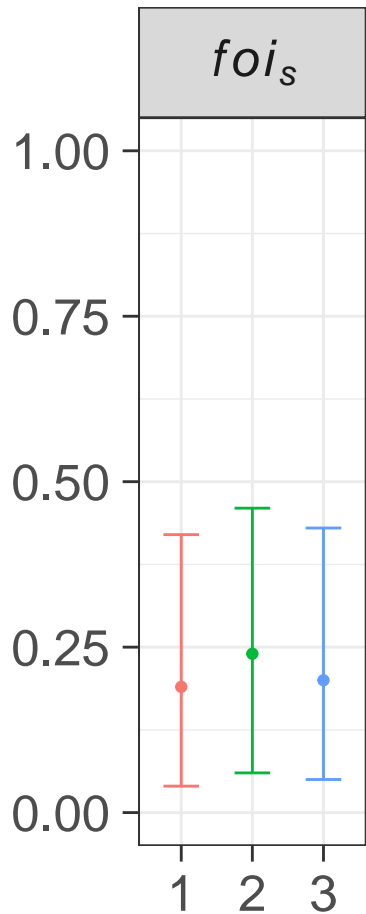


Transmission
 (primary \rightarrow re-infection \dashrightarrow) Progression/Re-activation
 (slow \rightarrow fast $\cdot \dashrightarrow$)

Acquisition of resistance \rightarrow Treatment/Natural cure \rightarrow



Parameter value



Model

Model