Title:
Chemical map–based prediction of nucleosome positioning using the Bioconductor package nuCpos

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Abstract

Background:
Methods for predicting nucleosome positioning include bioinformatics, biophysical, and combined approaches. An advantage of bioinformatics methods, which are based on in vivo nucleosome maps, is the use of natural sequences that may contain previously unknown elements involved in nucleosome positioning in vivo. The accuracy of such prediction attempts reflects the genomic coordinate resolution of the nucleosome maps applied. Thus, nucleosome maps constructed using Micrococcus nuclease (MNase), which has a strong preference for A/T-rich sequences, may not be appropriate for this purpose. In addition to MNase seq–based maps, base pair–resolution chemical maps of in vivo nucleosomes from three different species (budding and
fission yeasts, and mouse) are currently available. However, these maps have yet to be integrated into publicly available computational methods.

**Results:**

We developed a Bioconductor package (named nuCpos) that uses chemical maps to train duration hidden Markov models (dHMMs) to predict nucleosome positioning. The accuracy of chemical map–based prediction was higher than that of the previously developed MNase seq–based approach. With our method, predicted nucleosome occupancy reasonably matched in vivo observations and was not affected by A/T nucleotide frequency. Effects of genetic alterations on nucleosome positioning that had been observed in living yeast could also be predicted. In addition to dHMM-based prediction, nuCpos can calculate individual histone binding affinity (HBA) scores for given 147-bp sequences to examine their suitability for nucleosome formation. Local HBA scores for 13 overlapping nucleosomal DNA subsegments can also be calculated. HBA and local HBA scores for various sequences agreed well with previous in vitro and in vivo studies. Furthermore, our results suggest that nucleosomal subsegments that are disfavored in different rotational settings contribute to the defined positioning of nucleosomes.

**Conclusions:**

Our results demonstrate that chemical map–based statistical models are beneficial for studying nucleosomal DNA features. Studies employing nuCpos software can enhance understanding of chromatin regulation and the interpretation of genetic alterations and facilitate the design of artificial sequences. nuCpos is freely available from Bioconductor under the GPL-2 license.

**Keywords:**

nucleosome, prediction of nucleosome positions, dHMM, HBA, local HBA, translational and rotational settings, nucleosomal DNA subsegments

**Background:**
The nucleosome is a structure in which a ~147-base pair (bp) double-stranded DNA forms a left-handed super-helix to wrap a histone octamer consisting of two copies of histones H2A, H2B, H3, and H4 [1-3]. The positioning of nucleosomes along genomic DNA sequences affects various biological events, including transcription, DNA replication and repair, and chromosome segregation [4]. The importance of nucleosome positioning has prompted the development of computational methods to predict nucleosome positions along a given DNA sequence [5]. These methods are classified into three groups: biophysical, bioinformatics, and combined [5, 6]. Most biophysical methods are based on the structures of reconstituted nucleosome core particles (NCPs) such as NCP147, which contains a palindromic 147-bp sequence with intrinsic positional stability [3, 7, 8]. The use of palindromic sequence optimized for homogeneous nucleosome reconstitution and the highest resolution of the structure contributed greatly to the development of prediction algorithms. However, relying on the representative structure itself could also be a potential weakness, as there could be unrecognized natural intra-nucleosomal DNA elements that mediate specific physiologic functions in cells.

Studies using reconstituted nucleosomes other than NCP147 have provided many insights into nucleosome organization. In particular, studies using derivatives of the Widom 601 sequence [7] demonstrated the importance of intra-nucleosomal DNA elements from a physiologic context. When a nucleosome with this sequence is placed before elongating RNA polymerase II, the nucleosome acts as a polar barrier to transcription [9]. In this scenario, the polymerase coming from the right side of the sequence pauses in a manner dependent on an element called R3, which is found at the superhelical location (SHL) –2.5 to the left and strongly contacts the histone core [10, 11]. Structural studies demonstrated that a palindromic sequence consisting of two copies of the left-half of the Widom sequence yields a high-resolution X-ray structure, whereas the nucleosome with a right-half palindrome is less stable and yields poor crystals [12, 13]. Efficient reconstitution with the left-half sequence was confirmed in another study [14]. Indeed, the positioning power of the left-half sequence is exploited in reconstitution studies that require nucleosomes at targeted positions [15, 16]. However, why the left- and right-half sequences...
behave differently and how the left-half sequence determines the rotational and
translational settings remain to be fully elucidated.

In contrast to the biophysical prediction methods, bioinformatics
methods are based on maps of \textit{in vivo} nucleosomes determined using
high-throughput sequencing techniques. \textit{In vivo} nucleosomes contain various
DNA elements that should not necessarily be appropriate for nucleosome
formation (e.g., protein-coding sequences and recognition motifs for
transcription factors). In addition, various types of \textit{trans}-acting factors (e.g.,
transcription factors, histone chaperones, and chromatin remodeling factors) are
known to regulate nucleosome positioning in cells, as reviewed elsewhere
[17-19]. Furthermore, similarity in the usage of dinucleotides at each
superhelical turn in the nucleosome may help nucleosomes position redundantly
along the genomic coordinates with a periodicity of approximately 10 bp [20-23].
Indeed, \textit{in vivo}, most nucleosomes exhibit redundant positions on the genome
[24-26]. The use of complex, natural nucleosomal sequences may cause
difficulty in the interpretation of prediction results; however, use of these
sequences may also lead to unexpected findings that enhance understanding of
nucleosome-based regulation.

A weakness of currently available bioinformatics methods is that the
statistical models are constructed based on \textit{in vivo} nucleosome maps generated
using \textit{Micrococcus} nuclease (MNase) digestion followed by high-throughput
sequencing (MNase-seq). MNase digests linker DNA that connects NCPs,
allowing researchers to obtain nucleosomal DNA that has been protected from
enzymatic digestion. In MNase-seq experiments, DNA fragments of
mono-nucleosome size (~150 bp) are sequenced and mapped to the reference
genome. However, as MNase strongly prefers A/T-rich sequences, unwanted
digestion of A/T-rich nucleosomal sequences and less-effective digestion of
G/C-rich linkers may occur, leading to variation in nucleosome fragment size [19,
27]. Because of this enzymatic bias, precise determination of the genomic
coordinates of \textit{in vivo} nucleosomes using MNase-seq (i.e., dyad base calling) is
challenging.

One bioinformatics method considered successful in a thorough
comparative study [6] is NuPoP, which is built upon a duration hidden Markov
model (dHMM) that considers information regarding both the nucleosome and linker DNA [28]. NuPoP enables the prediction of nucleosome positioning in nine different species by rescaling the base composition of both the nucleosome and linker models for the budding yeast *Saccharomyces cerevisiae* with those of target organisms. The budding yeast models are generated using an MNase-seq–based nucleosome map by considering the central base of each nucleosomal fragment of varying length the dyad base [28]. This may particularly affect construction of the time-dependent statistical model for the nucleosome state, which ideally requires that the dyad bases be determined at bp resolution. The construction of the linker model, which requires extraction of linker sequences as genomic sequences not covered by nucleosomes, may also be affected. Thus, although selecting the MNase-seq–based map was the best practice at the time of the software’s development, the prediction results output provided by NuPoP can be biased by both the enzymatic preference of MNase and the difficulty of dyad base calling.

In order to examine the suitability of a given 147-bp sequence for nucleosome formation using the NuPoP algorithm, a histone binding affinity (HBA) score, also referred to as a ‘nucleosome affinity score’, is calculated [28]. According to the authors’ definition, this score should ideally predict the rotational setting of nucleosomes along the genome. However, this capability would only be expected when the *in vivo* nucleosome map used for construction of the statistical model is at bp resolution. This means that the low coordinate resolution of the MNase-seq–based map could cause ambiguity in the prediction. Indeed, at the implementation level, NuPoP smooths raw HBA scores using a moving average of a 55-bp window and standardizes the scores on a per sequence basis before outputting the processed HBA scores. This prevents software users from examining the actual HBA score for each genomic coordinate to see if the 147-bp sequence of interest is suitable for nucleosome formation.

A breakthrough in nucleosome mapping occurred with the development of a method for site-directed chemical cleavage of nucleosomal DNA followed by high-throughput sequencing [24, 29]. This technique, called chemical mapping, was first applied to budding yeast and then to the fission yeast
Schizosaccharomyces pombe and embryonic stem cells of the house mouse, Mus musculus [24-26, 30, 31]. In cells expressing histone H4 with an S47C amino acid substitution located near the nucleosome center, nucleosomal DNA is specifically cleaved. By examining the cleavage sites, previous studies determined the dyad positions of in vivo nucleosomes in the three species at bp resolution [24-26]. In addition to the histone H4-S47C approach, chemical mapping of nucleosomes using a histone H3 mutation (Q85C) determined the precise positions of −1 and +1 nucleosomes for protein-coding genes [27]. Molye-Hyerman and colleagues demonstrated that dHMMs trained with chemical maps can roughly predict the phasing pattern of nucleosome occupancy in budding and fission yeasts [25]. For an unknown reason, they used a uniform distribution as the linker length distribution in the calculation. In order to predict the relative positions of nucleosomes using the dHMM as it was originally proposed, a non-uniform, experimentally obtained distribution of linker lengths should be used. Most importantly, the bp-resolution chemical maps have not yet been implemented in publicly available software for prediction of nucleosome positioning.

One goal of nucleosome positioning prediction is in silico reproduction of in vivo observations, preferably at the locus level. If this goal is achieved, predicting the effects of genetic alterations on nucleosome positioning and prediction-based engineering of nucleosome-forming and -depleted sequences would also be practical. In this regard, budding and fission yeasts would serve as preferable model organisms, because nucleosomes formed on native and modified sequences in vivo have been precisely mapped [32-37]. These nucleosomes are suitable for in silico reproduction of in vivo observations. Importantly, for the currently available bioinformatics method NuPoP, the reliability of locus-level nucleosome prediction has seldom been demonstrated, despite its wide use in previous studies [38-47].

In this study, we developed a nucleosome positioning prediction method that utilizes available chemical maps of three species for construction of dHMMs. We show that the prediction accuracy of chemical map–based models is higher than that of MNase-seq–based models. The chemical map–based models appear to recognize appropriate sides of DNA strings as histone-DNA
contact surfaces. The effects of genetic alterations on nucleosome positioning previously observed in living yeast cells were reasonably reproduced in silico, suggesting that this software is useful for chromatin engineering and interpretations of mutation effects. We found that the prediction accuracy for mice was lower than that for yeasts, which should be acknowledged by software users. Our software, nuCpos, is available at the Bioconductor website (https://doi.org/doi:10.18129/B9.bioc.nuCpos).

Results:
Chemical map–based prediction of nucleosome positioning in yeasts
In order to determine whether the bp-resolution chemical maps are suitable for predicting nucleosome positioning, we trained dHMMs with the nucleosome maps determined with H4-S47C–dependent DNA cleavage (see Methods). Linker length distributions derived from the chemical maps, which were implemented in our method (nuCpos), exhibited a 10-bp periodicity, as previously reported [24-27, 48] (Additional file 1: Figure S1). In contrast, linker length distributions of the MNase-seq–based method, NuPoP, did not exhibit such periodicity, reflecting the difficulty of mapping nucleosomes at bp resolution using MNase digestion.

First, we predicted nucleosome positioning in the genomes of budding and fission yeasts (denoted ‘Sc’ and ‘Sp’, respectively, in Figure 1) with models that were constructed with in vivo nucleosome maps of target species (hereafter referred to as “matched-species prediction”). Based on the prediction results, we drew receiver operating characteristic (ROC) curves (Figure 1A, upper panels) and calculated area under the curve (AUC) scores (Additional file 1: Table S1). Here, only the predicted nucleosomes for which the dyad bases matched those of in vivo nucleosomes at a resolution of 1 bp were considered to be correctly predicted (see Methods). The prediction performance of the MNase-seq–based model for unique (representative) budding yeast nucleosomes as determined by AUC was 0.532, and it was 0.526 for redundant nucleosomes (Figure 1A, Target: Sc, Model: Sc, blue). Prediction for the fission yeast genome resulted in similar results (Figure 1A, Target: Sp, Model: Sp, blue). In contrast, better prediction performance was observed with the chemical map–based model
In both yeasts, AUC scores for unique nucleosomes (budding yeast, 0.751; fission yeast, 0.743) were more than 0.07 points higher than those for redundant nucleosomes (Additional file 1: Table S1). These results suggest that the chemical map–based models better predict the suitability of a given sequence for nucleosome formation, as unique nucleosomes are known to have sequences preferred for nucleosome formation [24, 25].

Prediction performance was also evaluated using cross-species models; nucleosome positioning in the target genomes was predicted using models constructed with nucleosome maps of different species. Using the budding yeast chemical model for prediction of nucleosome positioning in the fission yeast genome (Figure 1A, Target: Sp, Model: Sc, red) resulted in lower AUC scores for unique and redundant nucleosomes (0.667 and 0.626, respectively) in comparison with the matched-species scores (Additional file 1: Table S1). A reciprocal prediction with the budding yeast genome and the fission yeast chemical model resulted in similar scores (Figure 1A, Target: Sc, Model: Sp, red). These results indicate that the species of the nucleosome map from which the model is constructed must be matched to the prediction target species for optimal prediction results. For MNase-seq–based predictions, matched-species and cross-species predictions performed similarly (Additional file 1: Table S1 and Figure 1A, compare blue lines in upper and bottom panels). Interestingly, these MNase-seq–based scores were much lower than those obtained from chemical map–based cross-species predictions. These results thus highlight the usefulness of chemical map–based models and indicate that nucleosome-forming sequences exhibit similar properties in both types of yeast, as previously reported [25].

Ideally, prediction results should be evaluated at a 1-bp resolution, as done above, because if nucleosomes can be predicted at such a high resolution, it might be possible to discern the rotational settings of given nucleosomes. As the resolution of the chemical maps that we used for model construction could be 1-2 bp or lower, the resolution of the prediction results would be expected to be at a similar level. Indeed, the distance between chemically predicted nucleosomes and the nearest in vivo nucleosomes was generally 0 bp (located
at the same position) or 1 bp (located at the juxtaposed nucleotide positions) (Figure 1B, left panel). In order to determine the appropriate resolution for examining prediction results, we calculated the matching rate between predicted and \textit{in vivo} nucleosomes with stepwise widening of the matching window (Additional file 1: Figure S2). Here, we defined the matching window as the allowable distance between nucleosomes regarded as matched. In chemical map–based predictions (nuCpos), the matching rate doubled to over 50% when the matching window was widened from 0 bp (1-bp resolution) to 1 bp (2-bp resolution) (Additional file 1: Figure S2, red lines). However, the rate did not markedly increase upon further widening of the matching window, suggesting that the chemical models distinguish the histone-facing side of the DNA string.

In MNase-seq–based predictions (NuPoP), by contrast, the matching rate increased gradually as the matching window was widened from 0 to 9 bp (Additional file 1: Figure S2, blue lines). The matching rate drew a very loose anti-S shape, suggesting that the MNase-seq–based model still recognized the histone-facing side of the DNA string, but only to a small extent. We also noticed that a substantial population of nucleosomes predicted with the MNase-seq–based model was positioned approximately 5 nucleotides away from the \textit{in vivo} nucleosomes (Figure 1B, right panel, marked with a blue horizontal bar). These observations suggest that the MNase-seq–based model has difficulty in discriminating rotationally mispredicted nucleosomes. Considering these results, we concluded that prediction results should be evaluated at 2-bp resolution, as further widening of the matching window would increase the misprediction rate.

The left panel of Figure 1C presents the evaluation of matched-species predictions at 2-bp resolution. When the budding yeast MNase-seq–based model (NuPoP) was applied to the prediction of nucleosome positioning in the budding yeast genome (Target: Sc, Model: Sc), only 3.2% and 12.6% of the nucleosomes on the most probable (Viterbi) path matched \textit{in vivo} unique (red) and redundant (orange) nucleosomes, respectively. When the fission yeast model was applied to the prediction of nucleosome positioning in the fission yeast genome (Target: Sp, Model: Sp), the MNase-seq–based model scored 2.7% and 11.0%, respectively. In contrast, when the budding yeast chemical
map–based model (nuCpos) was used for predictions (Target: Sc, Model: Sc), 23.5% and 50.9% of the nucleosomes on the Viterbi path matched unique and redundant nucleosomes, respectively. For the fission yeast (Target: Sp, Model: Sp), the corresponding scores were 25.5% and 54.2%, respectively. Thus, with the chemical map–based models, over half of the nucleosomes predicted as being on the Viterbi path are present in living cells at exactly the same positions or at the juxtaposed nucleotide positions. In the chemical maps of budding and fission yeasts, in vivo unique nucleosomes accounted for 19.6% and 17.8%, respectively, of all redundant nucleosomes [24, 25]. Thus, in the MNase-seq–based predictions, enrichment of unique nucleosomes on the Viterbi paths was only 1.3- and 1.4-fold, respectively. In contrast, the chemical map–based predictions exhibited 2.4- and 2.6-fold enrichment, respectively. The higher enrichments suggest that chemical map–based models better distinguish sequences favorable for nucleosome formation, compared with MNase-seq–based models [24, 25].

The right panel of Figure 1C presents the evaluation of cross-species predictions at 2-bp resolution. When the fission yeast MNase-seq–based model (NuPoP) was used to predict nucleosome positioning in the budding yeast genome (Target: Sc, Model: Sp), 12.7% of the nucleosomes on the Viterbi path matched in vivo redundant nucleosomes. Prediction in the fission yeast genome with the budding yeast model (Target: Sp, Model: Sc) scored 10.8%. When the chemical map–based model (nuCpos) was used for cross-species predictions, greater proportions of predicted nucleosomes matched in vivo redundant nucleosomes: 36.7% (Target: Sc, Model: Sp) and 37.1% (Target: Sp, Model: Sc). Thus, although the prediction accuracy tends to decrease, cross-species predictions using chemical map–based models appear to produce better results than MNase-seq–based models.

**Prediction of in vitro reconstituted nucleosome positions**

The evaluations described above suggested that chemical models perform better in the prediction of rotational settings. To confirm this observation, we compared HBA scores calculated along the original 282-bp Widom 601 sequence [7] with the chemical map–based and MNase-seq–based models.
(Figure 2A). As mentioned in the Introduction section, non-smoothed HBA scores are expected to predict the rotational setting of nucleosomes if the resolution of the nucleosome map used for model construction is sufficiently high. The original 282-bp Widom 601 sequence contained primer sequences for the SELEX study at both ends and additional sequences flanking the nucleosome-forming 147-bp sequence centered at nucleotide position 154 [7]. When analyzed using the chemical map–based model, discrete HBA peaks with an interval of approximately 10 bp were observed at positions 124, 135, 143, 154, 164, and 175 (asterisks). This periodicity indicated that nearly the same surface of the DNA string was predicted to be in contact with the histone core in these potential translational positions. Among these positions, the one with the highest HBA score corresponds to the translational position of the in vitro stable nucleosome (position 154, orange vertical lines). In contrast, the MNase-seq–based HBA score was relatively low at position 154, and the peaks did not exhibit the apparent 10-bp periodicity. Thus, the chemical map–based model performed better for the prediction of rotational settings, at least when the Widom 601 sequence was tested.

We also calculated HBA scores along the 485-bp mouse mammary tumor virus (MMTV) 3’–long terminal repeat sequence (Figure 2B). The dyad bases of two nucleosomes, designated B and A, were located at nucleotide positions 139 and 335 (−127 and +70 relative to the transcriptional start site), respectively [49]. At these positions, chemical map–based HBA scores were the highest within the 50-bp-wide surrounding regions. For nucleosome B, alternative translational positions with an interval of approximately 10 bp were suggested (asterisks), probably due to the higher dinucleotide periodicity of nucleosome B compared with nucleosome A [49]. Note that the periodicity of the chemical map–based HBA peaks on this natural sequence was not as clear as seen with the in vitro–optimized Widom sequence (Figure 2A). We also noticed that the MNase-seq–based HBA score was highest at position 339, which was quite near nucleosome-forming position 335. However, the 4-base difference suggested that the MNase-seq–based model primarily recognized the opposite side of the DNA string as the histone-contacting surface.
Figure 2C shows the results of HBA calculations for a dinucleosomal DNA fragment derived from the somatic 5S RNA gene of *Xenopus borealis* [50]. As one of the two nucleosomes occupies a 150-bp region spanning nucleotide positions 30 to 179 (−70 to +79 with respect to the +1 nucleotide position of the 5S RNA gene), the dyad base should be around nucleotide positions 103 to 106 [50]. In this tandemly joined duplex sequence, the dyad base of the second nucleosome should be located around positions 300 to 303. The chemical map–based model revealed potential nucleosomes with their dyad bases at positions 105 to 107 and 302 to 304, with relatively high HBA scores. Around these potential dyad positions, 10-bp periodicity of the chemical map–based HBA was observed (asterisks). Selection of *in vitro* nucleosome-forming positions from these candidates could be made by linker histones [50, 51]. In contrast to the prediction with the chemical map–based model, the MNase-seq–based model did not appear to successfully recognize appropriate rotational settings, as in the case of the MMTV sequence.

**Prediction of *in vivo* nucleosome positions**

Next, we calculated HBA scores around budding yeast −1 and +1 nucleosomes (n=5,542 each) mapped by means of histone H3-Q85C–based chemical cleavage [27]. As shown in Figure 3A, mean HBA scores calculated using both models exhibited a periodicity with a 10-bp interval. However, the amplitude of the chemical map–based HBA scores (red) around the tested nucleosomes was larger than that of the MNase-seq–based HBA scores (blue). This suggested that the chemical model could clearly distinguish the surface of the DNA string that interacts with the histone core even when natural genomic sequences were queried. We found that the chemical map–based HBA scores were highest at the −1 and +1 nucleosome positions (0 bp). Chemical map–based HBA scores for the three neighboring translational positions (10, 20, and 30 bp in distance) relative to the nucleosome-depleted regions (marked with asterisks in Figure 3A) remained relatively high despite the gradual increase in the A/T frequency of the tested sequences (Figure 3B). After the A/T frequency reached a plateau (A/T≈0.64), the chemical map–based HBA scores began to decrease. In contrast, MNase-seq–based HBA scores at the −1 and +1 nucleosome positions
were already at moderate levels, and they simply decreased as the A/T frequency increased. Thus, the MNase-seq–based model was adversely influenced by the enzymatic bias of MNase, whereas the chemical map–based model was not.

The higher accuracy of chemical map–based models at the genomic level prompted us to perform a locus-level evaluation of prediction results, using the budding yeast TRP1ARS1 minichromosome [34, 36]. On this well-studied, circular, 1,465-bp DNA, three (numbered I to III) and four (IV to VII) nucleosomes are interspersed with two nucleosome-depleted regions or nuclease-hypersensitive regions designated HSRA and HSRB. HSRA includes the DNA replication origin ARS1, whereas HSRB is located upstream of the TRP1 marker gene. At a glance, the chemical map– and MNase-seq–based model prediction results appeared very different (Figure 3C). Each model suggested eight and seven representative nucleosomes, respectively. Seven of the eight nucleosomes predicted by the chemical map–based model (Figure 3C, nuCpos) reasonably matched the positions of in vivo nucleosomes determined previously [36]. The only exception was a predicted nucleosome located in HSRA, in which functional ARS1 would be occupied by the ARS-binding factor Abf1 and the origin recognition complex instead of the nucleosome to maintain this circular DNA across generations [52]. This prediction was reasonable, as DNA replication origins are known to be covered by nucleosomes when the subunits of the origin recognition complex or Abf1 are perturbed in vivo [52-54].

In this native sequence, the chemical map–based HBA scores exhibited a periodicity of an approximately 10-bp interval (Figure 3C, nuCpos, and Additional file 1: Figure S3). Some nucleotide positions with high HBA scores were selected by the chemical map–based dHMM as representative nucleosome positions. As the dHMM considers the linker length distribution as a major factor affecting nucleosome-linker state transition and does not allow nucleosomes with shorter DNAs (<147 bp), nucleosome positions tend to be selected in a limited manner. Although there were many high-HBA positions, only a few were clearly selected by the dHMM. Thus, although the predicted occupancy provides a rough image of chromatin state, it should be cautiously
considered. Instead, it should be kept in mind that periodic HBA scores may contribute to redundant nucleosome positioning in vivo.

In contrast to the chemical map–based model, most of the nucleosomes predicted by the MNase-seq–based model were mislocated (Figure 3C, NuPoP); most of the in vivo nucleosome centers (inverted triangles in figure) were located in predicted linkers or nucleosome ends. This tendency to mislocate nucleosomes may explain the lower genome-wide prediction accuracy (Figure 1). Importantly, MNase-seq–based HBA scores for this sequence appeared to mirror the A/T-content over the X-axis (Figure 3C, A/T); high-HBA positions were generally A/T-poor, and low-HBA positions were A/T-rich. In addition, the local amplitude of MNase-seq–based HBA scores was apparently lower compared with the chemical map–based model (Additional file 1: Figure S3). These observations also demonstrated that MNase-seq–based model prediction results are influenced by the A/T preference of MNase. A/T-content exhibited a similar effect in the MNase-seq–based nucleosome positioning prediction around the fission yeast ura4+ gene (Additional file 1: Figure S4) [55]. Given these results, we concluded that the chemical map–based models output better genome-wide and locus-level prediction results.

Prediction of effects of genetic alterations on nucleosome positioning

Next, we examined whether the effects of genetic alterations on nucleosome positioning could be predicted. In α cells of budding yeast, expression of the a-specific gene BAR1 is repressed by a2-operator–dependent positioning of the nucleosome at its promoter, which masks the gene’s TATA box [32, 35]. The chemical map–based model perfectly predicted the positioning of this repressive nucleosome (Figure 4, WT). The HBA score for this translational position (0 bp), which is 82 bp away from the a2-operator, was very high (HBA=8.47), suggesting that repression of the BAR1 gene is assisted by the intrinsic suitability of the promoter DNA for nucleosome formation. When a 36-bp sequence consisting of 12 repeats of CTG is inserted at the center of this nucleosome, repression of BAR1 and nucleosome positioning are not affected in vivo [35]. Prediction results agreed that this insertion should not cause nucleosome depletion (Figure 4, [CTG]_{12}). Other repeat sequences causing no
transcriptional derepression \textit{in vivo} \cite{35} were also predicted to not cause nucleosome depletion (\textbf{Figure 4}, Sac$_5$ and Sac$_6$). It is also known that insertion of a 30-bp A-stretch or a 10-bp CG (i.e., CpG) repeat sequence inhibits \textit{in vivo} nucleosome formation and causes derepression of \textit{BAR1} \cite{35}. Interestingly, the effect of these genetic alterations on nucleosome positioning was reproduced \textit{in silico} with the chemical map–based model (\textbf{Figure 4}, A$_{30}$ and CG$_5$). We noted that the disruptive effect of fragment insertion on nucleosome positioning was more pronounced in predictions than \textit{in vivo} observations. Insertion of a 20-bp A-stretch, which does not cause complete nucleosome depletion \textit{in vivo}, was clearly predicted to inhibit nucleosome formation (\textbf{Figure 4}, A$_{30}$). However, in the case of CG repeat insertion, shortening of the repeat to 8 bp, which satisfies \textit{in vivo} nucleosome formation \cite{35}, was predicted to preserve the capability to form nucleosomes (\textbf{Figure 4}, CG$_4$). Thus, despite some exceptions, the effects of genetic alterations on nucleosome positioning can be predicted with the chemical map–based model.

We also confirmed that the inhibition of nucleosome formation by telomeric DNA insertion demonstrated in a previous study \cite{56} was also largely predictable (\textbf{Additional file 1: Figure S5}). In budding yeast cells, the fourth nucleosome of a derivative of the \textit{TRP1ARS1} minichromosome called \textit{TALS} is formed in a manner dependent on the $\alpha_2$-operator \cite{33, 37}. Note that the chemical map–based model predicted the location of this nucleosome at a shifted position that unexpectedly would cover the $\alpha_2$-operator (\textbf{Additional file 1: Figure S5, WT}); the central of the three predicted nucleosomes should have been centered at nucleotide position 0. The shift may be a consequence of the relatively low HBA score for the \textit{in vivo} translational position (position 0), where the nucleosomal DNA contains an artificial sequence of bacterial origin \cite{33, 37}. When telomeric DNA fragments are inserted at the center of the fourth nucleosome, shorter fragments (hTEL2 and hTEL4) were predicted to not affect nucleosome positioning. In contrast, longer fragments (hTEL12 and hTEL29) were predicted to severely compromise nucleosome formation. These prediction results agreed with previous \textit{in vivo} observations \cite{56}. In addition, sequence isomers of the telomeric repeat (SI-A6, SI-A12, SI-B6, and SI-B12) were predicted to not inhibit nucleosome formation, which also agreed with the \textit{in vivo}
The hTEL6 insertion, which causes nucleosome depletion in vivo, appeared not to affect nucleosome formation in the prediction, suggesting a limitation of the prediction. Nonetheless, these results suggest that the chemical map–based models are useful for predicting the effects of genetic alterations on nucleosome positioning.

Local HBA for nucleosomal DNA subsegments

The successful increase in prediction accuracy and better recognition of rotational settings with chemical map–based models suggested that the chemical map–based HBA score for a given 147-bp sequence is a good indicator of the suitability of that sequence for nucleosome formation. However, considering that nucleosomal DNA makes contact with histone proteins at each superhelical location (SHL ±0.5-6.5), we thought that the suitability of intra-nucleosomal DNA segments for each histone-DNA contact could also be calculated as “local” HBA scores. In order to implement this idea, we divided a 147-bp whole nucleosomal segment into 13 overlapping nucleosomal DNA subsegments, designated A through M (Additional file 1: Figure S6, See Methods). Each 20- or 21-bp segment corresponded to two histone-DNA contact sites, each of which was shared by neighboring segments. For example, segment B corresponded to SHL −5.5 and −4.5, which were shared by segments A and C, respectively. We took this overlapping approach because it remains unclear how surrounding sequences affect histone-DNA contacts.

Calculating local HBA scores is conceptually the same as that of HBA calculations, which consider the probability of a whole 147-bp sequence to be a nucleosome [28]. In local HBA calculation, for each intra-nucleosomal segment located at that part of the nucleosome and the probability of the same sequence functioning as a linker are calculated. The log likelihood ratio of these probabilities is defined as the local HBA score for that segment. Thus, the sum of local HBA scores for the non-overlapping set of seven 21-bp segments, A, C, E, G, I, K, and M (147 bp in total), would be nearly equal to the HBA score calculated for the same 147-bp sequence.
In order to examine whether local HBA scores indicate the suitability of nucleosomal subsegments for histone-DNA contacts, we used the 282-bp Widom 601 sequence, which was used for the above HBA analysis (Figure 2A), as a test sequence. At potential translational positions with high HBA scores, local HBA scores for some segments were very high, as expected (Figure 5A, arrows). However, each 147-bp sequence also contained segments with relatively low local HBA scores. Interestingly, at translational positions with low HBA scores (those intervened by the high-scoring HBA positions), some segments exhibited very low local HBA scores (blue blots in the heatmap). This tendency was particularly notable for the central segments E through I. The finding of these low-scoring local HBA segments suggests that sub-sequences that are disfavored in other rotational settings play a role in determining rotational settings.

Next, we focused on the 147-bp Widom 601 sequence, of which the dyad base is located at nucleotide position 154 of the original sequence (Figure 5A, red arrow). We chose this sequence because its derivatives are often used in reconstitution studies, as it forms a homogeneous nucleosome, and because the left and right halves exhibit different features. In agreement with the transcription studies mentioned in the Background section [10, 11], local HBA scores for the 147-bp sequence were highest for segments D and E, both of which share SHL −2.5, in which the high-affinity R3 element is located (Figure 5B, red dots). The region covered by segments D and E (SHL −1.5 to −3.5) are known to exhibit high permanganate reactivity, which is indicative of DNA distortion resulting from very strong histone-DNA interaction at these segments [12]. These data indicate that local HBA scores are useful for evaluating the suitability of nucleosomal subsegments for histone-DNA contacts.

The overall image of the local HBA for the 147-bp Widom 601 sequence did not change with variations in the terminal sequences for biochemical handling (Additional file 1: Figure S7, 601LR, red dots) [12]. In the palindromic sequences made of each half, the local HBA landscapes were conserved compared with that of the original sequence, as expected by their sequence identity (Additional file 1: Figure S7, 601L and 601R, red dots). Indeed, the left-half palindrome (601L) had four segments with very-high HBA
scores (segments D, E, I, and J) and four other segments with relatively low scores (A, B, L, and M). The local HBA score for segment G increased from a low to moderate level following palindromization. In contrast to the left half, the local HBA scores for the right-half palindrome (601R) were moderate for segments A through F and H through M and relatively low for segment G. The absence of segments with very-high local HBA scores in the right-half palindrome may contribute to the lower salt stability of the reconstituted nucleosome [12].

When the translational position was shifted along the 282-bp sequence from nucleotide position 154 to surrounding nucleotide positions ranging from 150 to 158 (Figure 5C, −4 to +4 with respect to 154), the local HBA scores for segments B through I changed dramatically (Figure 5B, black dots). However, such shifting resulted in modest changes at segments J through M, with their scores remaining at relatively high levels. These observations suggest that segments J through M in the right-half sequence are generally suitable for nucleosome formation, which may also be true even when the translational position is shifted by several base pairs. In other words, segments J through M do not seem to have intra-nucleosomal disfavored elements that strongly limit the rotational setting. Reflecting the property of the non-palindromic sequence, palindromization of the left half yielded six segments (D-F and H-J) that exhibited the highest local HBA scores at the in vitro translational position (Additional file 1: Figure S7, 601L, black dots). In addition, the shifting score patterns for segments C and K suggest that shifting to either side may reduce the sum score. Thus, the rotational setting of this sequence appears to be determined through overall suitability for histone-DNA contacts. For the right-half palindrome, only the central segments with low to moderate local HBA scores (E through I) could contribute to the rotational setting. This nature might account for the observed poor crystal development or lower homogeneity [12], as this ‘slippery’ sequence could disrupt the uniformity of histone-DNA interactions.

As a comparison, we analyzed the palindromic sequence of NCP147 (Additional file 1: Figure S7, NCP147). In this sequence, the local HBA scores for outer segments A through C and K through M were high, whereas the inner part (segments D through J) scored lower (red dots). In contrast to the Widom
derivatives, local HBA scores for most of the segments were not high at the in vitro translational position. However, each segment appeared to contribute to the determination of rotational setting. For example, while the score for segment B decreased when the translational position was shifted to the left side, that for segment C decreased when shifted to the opposite side. The same was true for segments K and L. Similarly, local HBA scores for segments F and H decreased when the translational position was shifted inward. These observations suggest that being a palindrome itself helps generate homogeneous nucleosomes by preventing alternative positioning.

**Local HBA scores for modified nucleosome-forming sequences**

The above testing with the sequences previously used in reconstitution studies suggested that calculating local HBA scores would enhance understanding of how DNA sequences characterize the nucleosomes formed in vitro. This prompted us to examine whether we could apply local HBA calculations to the evaluation of intracellular nucleosome formation. González et al. reported that sequence-based determinants of nucleosome positioning are dispersed across nucleosomes [55]. One gene that they thoroughly investigated was the fission yeast gene, *ura4*. This gene has six representative nucleosomes (designated +1 to +6) that overlap the coding sequence, five of which were predictable with the chemical map–based dHMM (Additional file 1: Figure S4, nuCpos). Although the remaining nucleosome (+5) was not clearly observed in the predicted occupancy plot, there was one position with a relatively high HBA score that reasonably corresponded to the in vivo nucleosome (marked with an asterisk in the figure). A heatmap of local HBA scores for this gene suggested that there is an element disfavored for nucleosome formation near the +5 nucleosome (Figure 6A, WT, see the blueish slanted line spanning segments A through M around position 700). Thus, this element may have caused the lower predicted occupancy of the +5 nucleosome.

González et al. also generated three modified sequences, namely Dyad, Linker, and Int, for the *ura4* gene and studied nucleosome positioning on these sequences in vivo [55]. In Dyad and Linker, 51-bp sequences centered to each nucleosome dyad and each linker, respectively, were replaced with...
artificial randomized sequences of the same length. In the sequence Int, two
intra-nucleosomal sequences of each nucleosome (positions from −51 to −24
and 24 to 51) were replaced. According to their report, the occupancy of the +1
nucleosome was markedly decreased in the Dyad sequence, that of the +2
nucleosome was slightly increased in the Dyad and Linker sequences, and the
position of the +3 nucleosome was shifted in the Int sequence [55]. However,
why these changes selectively occur on specific nucleosomes in vivo remains
unclear due to a lack of appropriate analytical methods.

A heatmap of local HBA scores for the Dyad sequence clearly showed
that the replacements in this sequence caused a marked decrease in local HBA
scores only around the position of the +1 nucleosome (Figure 6A, Dyad, blue
lines not present in the WT map). The heatmap also suggested that the replaced
segment in the +1 nucleosome exerts a strong effect only on the central
nucleosomal subsegments (E through I). Indeed, at the in vivo translational
position, the Dyad replacement caused marked decreases in HBA scores
(Figure 6B, +1 Nuc., left, compare gray and green lines), and the effect was
limited to the central segments (Figure 6B, +1 Nuc., right, asterisks). In contrast,
the 51-bp replacements at other nucleosomal centers did not appear to
dramatically change their suitability for nucleosome formation. As to the +2
nucleosome, we did not observe any supportive signatures that could explain
why the Dyad and Linker replacements slightly increased its occupancy (Figure
6A, Dyad and Linker, and Figure 6B, +2 Nuc.). We observed that the Int
replacements primarily affected local HBA scores around the position of the +3
nucleosome (Figure 6A, Int, see the blueish slanted line spanning segments A
through M). The Int replacement caused decreases in neighboring HBA scores,
and the effect was greatest at segments C and D (asterisks), where local HBA
scores were among the highest (Figure 6B, +3 Nuc., compare gray and black
lines). This suggests that the mutation triggers a shift of the nucleosome to a
more suitable position in vivo. Giving these results, local HBA score calculation
for nucleosomal subsegments is useful for in silico assessment of modified
nucleosome-forming sequences.

Chemical map–based prediction of nucleosome positioning in mice
The improved prediction accuracy of the chemical map–based models in both yeasts suggested that the prediction accuracy in mice would also be improved. A big difference between the genomes of yeasts and vertebrates is that the latter have CG modifications. We observed that the CG dinucleotide frequency in mouse nucleosomal DNA sequences was much lower than the frequencies of other SS dinucleotides (each S stands for a C or G nucleotide) (Additional file 1: Figures S8A and S8B). Even in yeast nucleosomes, CG was the least favored dinucleotide, as previously discovered in budding yeast H2A.Z-containing nucleosomes [23]. This suggests that CG could be targeted by modification-mediated regulation of nucleosome-forming suitability. After normalization with the genomic frequency, mouse nucleosomes did not appear to exhibit a strong bias in CG frequency overall (Figure 7A). In detail, when compared with the two yeasts, the normalized CG frequency in mouse nucleosomes was relatively low at SHL 0 (Figure 7B, marked with a triangle) and high at the inner parts of some histone-DNA contact sites (asterisks), as well as some parts of outer regions (gray horizontal lines). This suggests that CG dinucleotides can affect the formation of murine nucleosomes at these intra-nucleosomal regions.

We predicted nucleosome positioning in the mouse genome using the MNase-seq–based and chemical map–based models. Based on the prediction results, we drew ROC curves and calculated AUC scores (Figure 7C). The prediction performance of the MNase-seq–based model for the unique nucleosomes measured by AUC was 0.511, and it was 0.509 for the redundant nucleosomes. As expected, the chemical map–based model performed better for both unique (AUC=0.711) and redundant (AUC=0.646) nucleosomes. Matching of the predicted nucleosomes on the Viterbi paths at a 2-bp resolution also demonstrated the better performance of the chemical map–based model (Figure 7D). In the MNase-seq–based prediction, 1.4% and 11.0% of predicted nucleosomes matched unique and redundant nucleosomes, respectively. In contrast, the chemical map–based prediction scored 10.0% and 41.1%, respectively. Thus, although the accuracy was not as high as in the case of yeasts (Figure 1C, scored over 50%), the chemical map–based model predicted
the suitability of given sequences for nucleosome formation in mice better than the MNase-seq–based model.

In order to determine whether the mouse chemical map–based model could better predict the rotational setting of nucleosomes, as shown in the case of yeasts, we calculated the matching rate between predicted and in vivo nucleosomes with stepwise widening of the matching window (Additional file 1: Figure S9). As expected, the matching rate for MNase-seq–based prediction increased gradually as the matching window widened. In chemical map–based predictions, a dramatic increase in matching rate was observed when the matching window was widened from 0 to 1 bp. However, unexpectedly, the matching rate also increased gradually as the matching window was widened further (See Additional file 1: Figures S2 and S9 for comparison between species). The shapes of the matching rate curves suggested the chemical map–based model still distinguished rotational settings to some extent. However, the mouse chemical model did not appear to be as good at discriminating rotationally mispredicted nucleosomes compared with the yeast models.

Discussion:
We developed a chemical map–based computational method for predicting nucleosome positioning and assessed the prediction results. Training dHMMs with chemical maps improved prediction accuracy in budding yeast, fission yeast, and the house mouse, Mus musculus (Figures 1 and 7, and Additional file 1: Figures S2 and S9 and Table S1). 41-54% of the predicted nucleosomes on the Viterbi paths matched those of in vivo nucleosomes at 2-bp resolution. Genome- and locus-level evaluations showed that the software successfully predicted the positions of representative in vivo nucleosomes (Figures 3 and 4, and Additional file 1: Figures S3 and S4). The in vivo nucleosomes that were not predicted as being representative had high HBA scores at reasonably near genomic positions. Furthermore, we demonstrated that perturbation of nucleosome positioning associated with genetic alterations could also be predicted (Figures 4 and 6, and Additional file 1: Figure S5). Thus, we
propose that the software nuCpos can be used for predicting nucleosome positioning and also for engineering of nucleosome-forming sequences. As expected, the use of chemical maps in prediction led to strict recognition of rotational settings, which was demonstrated with in vitro and in vivo nucleosome-forming sequences (Figure 2 and Additional file 1: Figures S2 and S9). Indeed, chemical map–based HBA scores for the original Widom 601 sequence indicated that the 147-bp sequence centered at nucleotide position 154 was suitable for nucleosome formation (Figure 2A). The in vitro nucleosome positions formed on natural sequences were also predictable at a rotational level (Figures 2B and C); however, the HBA amplitude along these sequences was smaller than along the in vitro–optimized Widom sequence. In contrast to the chemical map–based models, the MNase-seq–based models largely failed to recognize rotational settings (Figure 2 and Additional file 1: Figures S2 and S9). This may have been due to the A/T preference of MNase and the difficulty of dyad base calling in the construction of MNase-seq–based nucleosome maps [19, 27]. Indeed, the MNase-map–based model simply predicted A/T-rich regions as nucleosome-depleted regions (Figure 3 and Additional file 1: Figure S4). Therefore, instead of lower-resolution MNase-seq–based maps, base-pair-resolution chemical maps should be used in the development of bioinformatics methods to obtain better prediction results.

In the field of synthetic biology, the MNase-seq–based method NuPoP has contributed to the design of synthetic promoters and terminators [38, 39]. However, some studies reported that the histone binding affinity and predicted nucleosome occupancy output by NuPoP do not correlate with synthetic promoter and terminator activity [43, 44]. Differences in the DNA sequences of the tested synthetic elements may of course account for this discrepancy, as discussed elsewhere [43, 44]. Clearly, the A/T frequency does affect the prediction results of NuPoP (Figure 3 and Additional file 1: Figure S4). As demonstrated in the Results section, the chemical map–based method is more accurate and not affected by the A/T frequency. Thus, we expect that nuCpos is applicable to prediction-based engineering and more effective for synthesizing functional elements. Similarly, nuCpos can also be used to examine whether
DNA sequences of interest are suitable for nucleosome formation, as previously done with NuPoP [46, 47]. Dividing 147-bp nucleosomal DNA into subsegments and calculating subsegment local HBA scores revealed unexpected landscapes of the tested nucleosomes. Our study revealed that the Widom sequence had segments that are both favored and disfavored for nucleosome formation (Figure 5A). Importantly, segments with high local HBA scores in the Widom 601–derived sequences matched the high-affinity histone-contacting regions (Figure 5B and Additional file 1: Figure S7). Furthermore, the Widom derivatives had segments exhibiting the highest local HBA scores at the in vitro rotational settings, which was further emphasized by palindromization with the left-half sequence (Additional file 1: Figure S7). In contrast to the left-half sequence, the right-half sequence contained segments exhibiting relatively high local HBA scores that did not change markedly with different rotational settings. Thus, these sequence-specific features may account for the different behavior of the Widom derivatives in in vitro experiments. For the NCP147 sequence, it appeared that palindromization itself repressed the shifting of rotational settings (Additional file 1: Figure S7). Collectively, our data indicate that local HBA scores for given sequences provide insights that enhance understanding of nucleosome features.

Locus-level assessments of prediction results suggested that software users should not place undue confidence in the predicted nucleosome occupancy output from chemical map–based models. Indeed, there was a misplaced nucleosome that occupied the replication origin ARS1 (Figure 3) and a shifted nucleosome that covered the α2-operator (Additional file 1: Figure S5). Also, the +5 nucleosome of ura4+ was not predicted as a representative nucleosome (Additional file 1: Figure S4). We speculate that these discrepancies were due primarily to the fact that the models do not consider involvement of functional DNA elements or transacting factors that regulate nucleosome formation at specific genomic locations. In other words, chromatin regions highlighted by the differences in nucleosome occupancy between prediction and in vivo observations could be the targets of future investigations aiming to uncover region-specific regulatory mechanisms. From another point of view,
view, software users should keep in mind that the dHMMs consider linker length
distribution but do not consider partial unwrapping of nucleosomal DNA in
calculating probable paths of nucleosome and linker states. Instead, our
observations suggest that HBA scores indicate redundant positioning of
nucleosomes in the cells; HBA scores are simply calculated for a given 147-bp
sequence, independently of surrounding sequences.

In the three species with available chemical nucleosome maps, mouse
genomic DNA undergoes covalent modification of cytosine in CG dinucleotides,
whereas that of budding or fission yeast does not. There is a negative correlation
between CG frequency and nucleosome occupancy in mammalian cells [57]. In
addition, hypermethylation of cytosine is observed when the chromatin of the
mouse Pou5f1 gene, which encodes the pluripotency factor Oct4, is changed to
a closed state, suggesting a link between DNA methylation and nucleosome
positioning [58-60]. Furthermore, DNA methylation is correlated with
nucleosome occupancy in humans [61]. Indeed, the nucleosome structure itself
has been suggested as necessary for the maintenance of DNA methylation [62,
63]. In addition, many histone variants exist in mice, which might cause
variability in the preferred sequence for nucleosome formation [64-66]. Taking
this species- or mammalian-specific evidence into account, for nucleosome
positioning prediction in mice, statistical models should be better constructed
from the nucleosome map of mice, not by rescaling yeast models, if applicable.

We demonstrated that the prediction accuracy of the chemical
map–based mouse model was apparently lower than that of yeast models
(Figures 2 and 7). A disadvantage of mouse prediction is that the chemical map
probably contains substantial numbers of pseudo nucleosomes [26], which could
not be omitted due to the lower cleavage depth than yeasts. As a consequence,
the density of nucleosomes on the mouse genome is one redundant
nucleosome per 3 bp, which is about 10 times higher than yeast values (see
Methods). Thus, we speculate that the accuracy of mouse nucleosome
positioning prediction can be increased if other chemical maps of higher quality
are produced and used for model construction. In human genomics, the
relationship between various phenotypes and genetic variants has been
explored [67-70]. However, the effects of genetic variants on nucleosome

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formation in this regard remain to be studied. Now that our study showed that
insertions and replacements that disrupt nucleosomes in yeast cells can be
predictable \textit{in silico}, it is possible that nucleosome-disrupting human mutations
can be found with the aid of chemical map–based predictions. We showed that
cross-species chemical map–based models exhibit relatively high prediction
accuracy compared with MNase-seq–based models (Figure 1). Therefore,
before generating high-quality chemical maps for species other than the budding
and fission yeasts, the yeast models can alternatively be applied for the
prediction of nucleosome positioning in those species.

Conclusions:
In this study, we demonstrated that the accuracy of dHMM-based nucleosome
positioning prediction can be substantially increased by using
base-pair-resolution nucleosome maps for model construction. Our prediction
results suggest that chemical map–based models are useful for predicting
nucleosome positioning in wild-type and modified sequences at the locus level.
We also demonstrated that strong histone-DNA contacts in a nucleosome and
their rotational settings can be predicted. Furthermore, as another advantage of
bioinformatics methods, our models indicate that the commonly used Widom
sequence contains subnucleosomal segments that are disfavored, or statistically
very rare, \textit{in vivo} nucleosomes at their nucleosomal positions in shifted
rotational settings. We expect that our prediction method will provide further
insights that will enhance understanding of nucleosome-based epigenetic
regulation.

Methods:

Software and data sets
Most analyses were performed in the GNU R environment
(https://www.r-project.org, ver. 3.6.1). R packages were obtained from CRAN
(https://cran.r-project.org/) and Bioconductor (http://bioconductor.org/). Chemical
maps for budding yeast, fission yeast, and house mouse (\textit{Mus musculus})
embryonic stem cells [24-26] were used for model construction and testing the
prediction accuracy. The budding yeast's chemical map in the sacCer2
coordinate was lifted over to the sacCer3 coordinate, as described elsewhere [36]. The number of unique and redundant nucleosomes in the budding yeast genome was 67,548 and 344,709, respectively; fission yeast, 75,828 and 425,653; mice, 10,677,016 and 850,701,275. Reference genomes of budding yeast (R64-1-1), fission yeast (ASM294v2), and mice (mm9/NCBIM37.67) were used.

Construction of the nuCpos package

The codes for the construction of parameters used in the nuCpos package (ver. 1.2.0) are available online (https://doi.org/10.5281/zenodo.3362065). Genomic regions covered with the 147-bp non-redundant (unique) chemically mapped nucleosomes and uncovered were defined as nucleosome and linker regions, respectively. DNA sequences of these regions were used to construct parameters that were transferred to internal Fortran programs. Nucleosomes of which dyads were located within 73 bp of the chromosomal ends were omitted. For construction of the mouse model, hard-masked genomic sequences were used, and nucleosome and linker regions containing N were omitted before parameter construction to avoid potential prediction bias caused by repeat elements. In total, 67,538 nucleosome regions and 50,622 linker regions were obtained for the budding yeast genome (sacCer3); fission yeast (ASM294v2), 75,826 nucleosome and 46,557 linker regions; mice (mm9), 4,147,972 nucleosome and 2,484,347 linker regions.

We developed an R function designated predNuCpos, which predicts nucleosome positioning based on a dHMM, as previously proposed by Xi et al. [28]. Like its ancestral function predNuPoP in the NuPoP package (https://doi.org/doi:10.18129/B9.bioc.NuPoP, ver. 1.34.0), predNuCpos receives a DNA sequence of any length, invokes an internal Fortran program, and outputs the prediction result either in the working directory or in the working environment of R. In predNuCpos, construction of the dHMM is based on chemical maps, as described below.

Parameters used in the predNuCpos function were constructed according to the NuPoP paper [28] using the functionalities of the Biostrings package (https://doi.org/doi:10.18129/B9.bioc.Biostrings, ver. 2.52.0).
parameters were as follows: \( freq_L \), one-base frequencies for linker regions; \( tran_L \), \( tran_{L2} \), \( tran_{L3} \), and \( tran_{L4} \), 1st- to 4th-order transition probabilities for linker regions, respectively; \( freq_{N4} \), four-base frequencies at the first four nucleotide positions of nucleosome regions; \( tran_{N4} \), time-dependent 4th-order transition probabilities for nucleosome regions; \( P_d \), linker length distribution that ranges from 1 to 500 bp. Linker sequences of 7-500 bp in length were used for linker model construction, as described elsewhere [28]. \( freq_L \) and \( freq_{N4} \) were obtained using the \texttt{oligonucleotideFrequency} function of Biostrings; \( tran_L \), \( tran_{L2} \), \( tran_{L3} \), \( tran_{L4} \), and \( tran_{N4} \) were obtained using the \texttt{oligonucleotideTransitions} function of Biostrings. Moving average smoothing using the \texttt{SMA} function of the TTR package (https://cran.r-project.org/package=TTR, ver. 0.23-4) at a 3-bp window was applied to the 4th-order transition probability parameter \( tran_{N4} \) and to the linker length distribution parameter \( P_d \). The parameters used in \texttt{predNuCpos} were also used in another function \texttt{mutNuCpos}, which predicts the effect of genetic alterations on nucleosome positioning.

Xi et al. proposed the HBA score as the log likelihood ratio of the probability for a given 147-bp sequence to be a nucleosome versus a linker [28]. According to their definition, the HBA score for the 147-bp region \( x \) centering at position \( i \) (\( a_i \)) on a given genomic sequence is,

\[
a_i := \log \left[ \frac{P_N(x_{i-72}, \ldots, x_{i+73})}{G_L(x_{i-72}, \ldots, x_{i+73}, 147)} \right],
\]

where \( P_N \) and \( G_L \) represent the probability of observing the 147-bp sequence as a nucleosome or a linker, respectively [28]. The probability of being a nucleosome is calculated by referring to the parameters \( freq_{N4} \) and \( tran_{N4} \), which are derived from nucleosomal DNA sequences. Similarly, calculation of the probability of being a linker is based on linker DNA sequences. As nucleosomal and linker sequences do not overlap in terms of their genomic coordinates, negativity of HBA does not directly mean that the tested sequence is inappropriate for nucleosome formation. The \texttt{predNuCpos} function calculates chemical map–based HBA scores along the input sequence and outputs them as raw values as its default behavior. We developed an independent function designated \texttt{HBA}, which only calculates the HBA score for a given 147-bp
sequence. The HBA function uses the abovementioned chemical parameters for $\text{predNuCpos}$: $\text{freqL, tranL, tranL2, tranL3, tranL4, freqN4, and tranN4.}$

We defined 13 overlapping nucleosomal subsegments, A through M, and developed a function designated $\text{localHBA}$ that calculates "local" HBA scores for each segment. Segment A corresponds to nucleosomal nucleotide positions 1-21; B, 12-31; C, 22-42; D, 33-52; E, 43-63; F, 54-73; G, 64-84; H, 75-94; I, 85-105; J, 96-115; K, 106-126; L, 117-136; and M, 127-147. Similar to the calculation of HBA [28], the local HBA score for segment A of the 147-bp potential nucleosomal region $x$ centering at position $i (l_i)$ on a given genomic sequence is calculated as,

$$l_i := \log \left[ \frac{P_N(x_{1-73} - x_{1-53})}{G_L(x_{1-73} - x_{1-53})} \right],$$

where $P_N$ and $G_L$ represent the probability of observing the 21-bp sequence as segment A of a nucleosome or a linker, respectively. Local HBA scores for the other segments are calculated in the same way, except that the considered nucleotide positions are set appropriately. At the implementation level, four-base frequency values for the first four nucleotide positions of each segment were prepared: $\text{freqN4SA}$ corresponds to nucleosome positions 1-4; $\text{freqN4SB}$, 12-15; $\text{freqN4SC}$, 22-25; $\text{freqN4SD}$, 33-36; $\text{freqN4SE}$, 43-46; $\text{freqN4SF}$, 54-57; $\text{freqN4SG}$, 64-67; $\text{freqN4SH}$, 75-78; $\text{freqN4SI}$, 85-88; $\text{freqN4SJ}$, 96-99; $\text{freqN4SK}$, 106-109; $\text{freqN4SL}$, 117-120; and $\text{freqN4SM}$, 127-130. These four-base frequency values were used to calculate the probability of the segment as that part of nucleosomal DNA as done for HBA calculations [28]. The parameter $\text{freqN4SA}$ was identical to $\text{freqN4}$, which was used for HBA calculations.

**Prediction of nucleosome positioning with nuCpos and NuPoP and evaluation of the prediction results**

The codes for prediction, evaluation, and figure drawing used in this study are available online (https://doi.org/10.5281/zenodo.3523573). Unmasked reference genomes for the budding yeast, fission yeast, and house mouse ($\text{Mus musculus}$) were used as prediction target sequences. For the mouse experiments, only the 19th chromosome (Chr19) was used for prediction.
because its length (61,342,430 bp) was sufficient for evaluation, at
approximately five-times longer than the total length of yeast chromosomes
(budding yeast, 12,071,326 bp; fission yeast, 12,571,820 bp). Mouse Chr19
contained 249,210 unique and 19,965,481 redundant nucleosomes that had
been determined based on histone H4 S47C-dependent cleavage [26]. The
density of redundant nucleosomes on mouse Chr19 was one per 3.07 bp. With
this density, one in three randomly located nucleosomes in the chromosome
could be counted as a truly predicted nucleosome. Thus, we selected 2,044,747
nucleosomes with the highest NCP scores as true redundant nucleosomes for
the matching experiment. This selection yielded a density of one nucleosome
per 30.0 bp, which was comparable to that of budding yeast and fission yeast
(one nucleosome per 35.0 bp and 29.5 bp, respectively).

The predNuPoP function of NuPoP and the predNuCpos function of
nuCpos were used for dHMM-based predictions. In order to predict using
budding yeast models, the species arguments were set as “7” for predNuPoP
and “sc” for predNuCpos. Similarly, fission yeast (“9” and “sp”) and mouse (“2”
and “mm”) models were specified. We defined any nucleosomes with \( P \)-values
greater than zero \( (P>0) \) as predicted nucleosomes. Matching of predicted
nucleosomes using \textit{in vivo} chemical nucleosomes was done by widening the
genomic coordinates of \textit{in vivo} nucleosomes to both sides in a step-wise manner
from zero to nine base pairs. For instance, at 1-bp resolution, a predicted
nucleosome was regarded as “matched” when the genomic coordinate of its
dyad was equal to that of the nearest \textit{in vivo} nucleosome. If the dyad of the
predicted nucleosome was 1 bp away from that of the nearest \textit{in vivo}
nucleosome, it was regarded as “not matched.” At 2-bp resolution, a predicted
nucleosome was regarded as “matched” when the distance from its dyad to that
of the nearest \textit{in vivo} nucleosome was <2 bp. For drawing ROC curves and
calculation of AUC, a matrix of two columns was generated for each prediction
result. In the first column, \( P \)-values of nucleosomes that were \( P>0 \) were stored.
In the second column, the matching status for each nucleosome according to the
matching experiments at 1-bp resolution was stored. After processing using the
\texttt{prediction} function of the ROCR package
(https://cran.r-project.org/package=ROCR, ver. 1.0-7), ROC curves were drawn
using the `plot` function of R. The AUC was calculated using the `performance` function of ROCR. The matching rate of the nucleosomes on the Viterbi paths, which were predicted by `predNuPoP` and `predNuCpos`, was calculated using in-house scripts and plotted using the `barplot` function of R.

Dinucleotide frequencies for nucleosomal DNA and unmasked genomic DNA were calculated using the `oligonucleotideFrequency` function of Biostrings. For normalization of dinucleotide frequencies, the nucleosomal frequency was divided by the genomic frequency. Heatmaps of 16 dinucleotide frequencies along the nucleosome were drawn using the `levelplot` function of the rasterVis package (https://cran.r-project.org/package=rasterVis, ver. 0.46). The `plot` function was used for plotting the frequencies of CG and other SS dinucleotides.

Chemical map–based HBA scores were calculated using the `predNuCpos` function or the `HBA` function of nuCpos, which yield the same scores. The species argument was set as “sc” for budding yeast sequences and sequences of `in vitro` reconstitution studies; for the fission yeast sequences, “sp.” Non-smoothed MNase-seq–based HBA scores were calculated using in-house functions that utilize the parameters for the `predNuPoP` function of NuPoP. For comparison of `in vivo` nucleosomes, 5,542 sets of −1 and +1 nucleosomes determined by Chereji et al. [27] were used for HBA calculations. The 347-bp sequences around these nucleosomes (from −173 to +173 nucleotide positions with respect to the dyads) were extracted from the budding yeast genome. The HBA score was calculated for each possible 147-bp segment along the sequences. A/T-frequency was calculated using the `letterFrequency` function of Biostrings for each 147-bp sequence. HBA and A/T-frequency scores were averaged at each coordinate with respect to the −1 or +1 nucleosomes.

Chemical map–based local HBA scores were calculated using the `localHBA` function of nuCpos. Heatmaps of local HBA scores were drawn using the `levelplot` function of rasterVis.

List of abbreviations:

- **AUC**: area under the curve
CG: cytosine-guanine dinucleotide

dHMM: duration hidden Markov model

HBA: histone binding affinity

LTR: long terminal repeat

MMTV: mouse mammary tumor virus

MNase: *Micrococcus* nuclease

NCP: nucleosome core particle

NDR: nucleosome depleted region

ROC: receiver operating characteristic

SELEX: Systematic Evolution of Ligands by EXponential enrichment

SHL: superhelical location

Declarations:

Ethics approval and consent to participate:
Not applicable.

Consent for publication:
Not applicable.

Availability of data and materials:
The datasets generated and analyzed during the current study are available online (see Methods for the URLs).

Competing interests:
The authors declare that they have no competing interests.

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Authors' contributions:
H.K. designed the study, created the software, performed the experiments, and was a major contributor in writing the manuscript. T.U. and M.S. were involved in
study design, data validation, and manuscript writing. All authors read and approved the final manuscript.

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40. Wight A, Yang D, Ioshikhes I, Makrigiannis AP: Nucleosome Presence at AML-1 Binding Sites Inversely Correlates with Ly49 Expression:


Figure legends:

Figure 1. Comparison of prediction accuracy between chemical map–based and MNase-seq-based models for yeasts. (A) ROC curves of prediction results with matched-species models (upper panels) and cross-species models (lower panels). Orange lines represent lines of slope 1 and y-intercept 0. The species of genomic sequences used for prediction (Target) and the species used for model construction (Model) are indicated. “Sc” stands for S. cerevisiae, whereas “Sp” stands for S. pombe. Chemical map–based (nuCpos) and MNase-seq–based (NuPoP) models were used for predictions. Prediction performance for representative (Unique) and redundant (Redundant) nucleosomes are presented. Matching window was set to 0 bp. (B) Distance between predicted nucleosomes and nearest in vivo nucleosomes.

Probabilities of Viterbi nucleosomes located at a particular distance from the nearest in vivo redundant nucleosomes are plotted. Species of the target genome and for model construction were both S. cerevisiae (matched-species models). Magnified view is presented inside each plot. Arrows point to the probability of predicted nucleosomes that are 1-bp apart from in vivo nucleosomes. (C) Matching of nucleosomes on the Viterbi paths with in vivo unique and redundant nucleosomes. Note that the redundant nucleosome datasets contain both unique nucleosomes, which are representative (colored red in the bar graphs), and non-representative nucleosomes (orange).
Figure 2. HBA scores along in vitro nucleosome-forming sequences. (A-C)

HBA scores along nucleosome-forming sequences were calculated using chemical map–based and MNase-seq–based budding yeast models. Sequences analyzed were the 282-bp original Widom sequence (A), the 3′-LTR of MMTV (B), and the Xenopus borealis 5S rDNA dinucleosome-forming sequence (C). The scores were normalized by subtracting the mean value from the raw value on a per sequence basis. The HBA score for a given 147-bp nucleosome sequence was assigned to its dyad position. Orange vertical lines indicate the dyad positions of in vitro reconstituted nucleosomes: nucleotide positions 154 (A), 139 and 335 (B), and 106 and 303 (C). Asterisks indicate high-scoring HBA positions around the in vitro positioning sites. Note that for the 5S rDNA sequence, two identical sequences are joined at position 230, causing a difference in HBA scores around the left sides of the two in vitro nucleosome positions.

Figure 3. Comparison between chemical map–based and MNase-seq–based models on selected in vivo regions. (A and B) Chemical map–based and MNase-seq–based HBA scores (A) and A/T nucleotide frequency (B) along the sequences containing budding yeast −1 and +1 nucleosomes for protein-coding genes. Gray vertical lines indicate the dyad positions of respective nucleosomes. Asterisks indicate positions with relatively high HBA scores. NDR: nucleosome-depleted region. (C) Prediction results for the budding yeast TRP1ARS1 mini-chromosome. Schematic representation of in vivo nucleosome positioning is shown above the plots. Nucleosomes labeled I through VII are indicated as ovals. Note that this sequence is circularized in vivo by being linked at the EcoRI sites. The top two panels show the prediction results output by nuCpos, whereas the next two panels show NuPoP results. The upper panel in each set shows predicted occupancy of the nucleosome (Occup., gray polygons) and probabilities of the tested 147-bp sequences for being in the nucleosome state (P-dyad, blue vertical lines). The lower panels show HBA values for the tested 147-bp sequences calculated using the indicated models. The very bottom panel shows the A/T-frequencies for the tested 147-bp sequences. Horizontal lines at the bottom of each plot indicate a
unit of the circular TRP1ARS1 mini-chromosome (colored in gray, nucleotide positions 0 to 1,464), the coding region of TRP1 (red, 115-879), and the B3 (black, 763-788), B2 (purple, 810-820), B1 (green, 847-859), and ACS (blue, 869-879) elements of ARS1. Inverted triangles indicate the histone H4 S47C-dependent cleavage centers determined by indirect end-labeling; orange for mini-chromosome and light blue for genomic experiments [36].

Figure 4. Predicting the effects of repeat insertion on nucleosome positioning. Chemical map–based HBA scores and predicted nucleosomal occupancy were calculated for original and modified BAR1 promoter sequences. The sequences were centered at the dyad position of the repressive nucleosome, in which the indicated repeat sequences were inserted. Horizontal lines at the bottom of each plot indicate the α2-operator (purple), the TATA (blue) element, the coding region of BAR1 (orange), and the insert (red). Note: the sequence insertion caused a shift of the left of the three predicted nucleosomes to the right to cover the α2-operator in the occupancy plots. Overconfidence should not be placed in this shift, as it may simply reflect that the dHMM tends to follow the linker length distribution, which generally does not allow longer linkers.

Figure 5. Local HBA analysis of the Widom 601 sequence. (A) Chemical map–based local HBA scores along the 282-bp Widom 601 sequence. The scores for each tested 147-bp sequence were heatmapped at the center position of that sequence. The heatmap scale indicates the local HBA score. Black arrows indicate high-HBA-score positions (124, 135, 143, 164, and 175). Red arrow indicates the dyad position of the in vitro reconstituted nucleosome (154). The region evaluated in (B) is indicated as a horizontal gray bar under the X-axis. (B) Local HBA scores at (red) and around (black) the in vitro translational position for each segment are plotted in columns. The scores for the M segment are magnified to the left to show the indices on the X-axis. The relative positions −4, 0, and +4 correspond to nucleotide positions 150, 154, and 158 of the 282-bp sequence. The location of the R3 element is indicated at the top. (C) Schematic representation of shifting of translational positions in (B). Nucleotide
positions relative to the dyad of the central translated position ($i=154$) are indicated. Only three ($-4$, $0$, and $+4$) of the nine positions evaluated in (B) are shown.

**Figure 6. Local HBA analysis of modified nucleosome-forming sequences.**

(A) Chemical map–based local HBA scores along the original and modified fission yeast $ura4^+$ gene. The scores for each tested 147-bp sequence were heatmapped at the center position of that sequence. The heatmap scale indicates the local HBA score. Black arrows indicate the nucleosome centers (nucleotide positions $+17$, $+164$, $+332$, $+470$, $+629$, and $+806$) determined by MNase-seq [55]. (B) Chemical map–based HBA and local HBA scores for +1 to +3 nucleosomes of the $ura4^+$ gene. Relative dyad positions with respect to the *in vivo* positions are indicated for HBA plots. Local HBA scores for the *in vivo* positions are shown. Asterisks indicate substantially affected segments.

**Figure 7. Comparison of prediction accuracy between chemical map–based and MNase-seq–based models for mice.** (A) Normalized frequencies of dinucleotides starting at indicated nucleosomal positions. The heatmap scale indicates the normalized dinucleotide frequency. (B) Normalized CG frequency across the nucleosome. Triangles, stars, and horizontal bars indicate positions and regions with mouse-specific characteristics. Gray vertical lines indicate the positions of dyad (solid) and histone-DNA contact sites (SHL ±0.5-6.5). (C) ROC curves of prediction results with matched-species models. “Mm” stands for *M. musculus*. Prediction performance for representative (Unique) and redundant (Redundant) nucleosomes are presented. (D) Matching of nucleosomes on the Viterbi paths with *in vivo* unique and redundant nucleosomes.

**Supplementary Figure Legends:**

Additional file 1: Figure S1. Linker length distributions utilized in the construction of chemical map–based and MNase-seq–based models. The linker length distributions of three species implemented in each package are
plotted. A magnified view ranging from 0 to 100 bp in linker length is presented inside each plot.

Additional file 1: Table S1. Area under the curve scores for the prediction results shown in Figure 1A.

Additional file 1: Figure S2. Matching rate between predicted and \textit{in vivo} nucleosomes with variable matching windows. The species of genomic sequences used for prediction (Target) and the species used for model construction (Model) are indicated. “Sc” stands for \textit{S. cerevisiae}, whereas “Sp” stands for \textit{S. pombe}. Chemical map–based (nuCpos) and MNase-seq–based (NuPoP) models were used for predictions. Matching rates for representative (Unique) and redundant (Redundant) nucleosomes are presented.

Additional file 1: Figure S3. Magnified view of prediction results for \textit{TRP1ARS1}. Prediction results for the budding yeast \textit{TRP1ARS1} mini-chromosome output by nuCpos and NuPoP (Figure 3C) were magnified, being centered at nucleosome II.

Additional file 1: Figure S4. Prediction results for the fission yeast \textit{ura4}+ gene. Schematic representation of \textit{in vivo} nucleosome positioning is shown above the plots. Nucleosomes numbered +1 to +6 are indicated as ovals. The top two panels show the prediction results output by nuCpos, whereas the next two panels show NuPoP results. The upper panel in each set shows predicted occupancy of nucleosomes (Occup., gray polygons) and probability that the tested 147-bp sequences are in the nucleosome state (P-dyad, blue vertical lines). Lower panels show HBA values for the tested 147-bp sequences calculated using the indicated models. The very bottom panel shows the A/T-frequency for the tested 147-bp sequences. Horizontal lines at the bottom of each plot indicate the 5’- and 3’-untranslated regions (colored in gray, nucleotide positions −151 to −1 and +795 to +986, respectively) and the protein-coding region (red, 0 to +794) of the \textit{ura4}+ gene. Inverted triangles indicate the nucleosome centers determined by MNase-seq [55].
Additional file 1: Figure S5. Prediction of the effects of repeat insertion in the fourth nucleosome of the TALS minichromosome. Chemical map–based HBA scores and predicted nucleosomal occupancy were calculated for original and modified TALS sequences [56]. The sequences were centered at the dyad position of the fourth nucleosome (0 bp), in which the indicated repeat sequences were inserted. Note: the position for the fourth nucleosome was predicted to shift to the right. Horizontal lines at the bottom of each plot indicate the \( \alpha_2 \)-operator (purple) and the insert (red). hTEL stands for human telomeric repeat (5'-TTAGGG-3'); SI-A, sequence isomer-A (5'-TGTAGG-3'); SI-B, sequence isomer-B (5'-TGTGAG-3').

Additional file 1: Figure S6. Thirteen overlapping nucleosomal DNA subsegments for local HBA calculation. Segments A through M are colored in orange on the nucleosome structure 1AOI [1]. The structures were drawn using MacPyMOL (v1.8.4.1). The base pair length (red) and corresponding superhelical locations (black) of each segment are indicated. The color of the right-half segments (H-M) is faded because they are behind the front helix.

Additional file 1: Figure S7. Local HBA analysis of the \textit{in vitro} reconstitution sequences. Local HBA scores at (red) and around (black) the \textit{in vitro} nucleosome position for each segment are plotted in columns. Due to the lack of flanking sequences, shifting the translational position to the left and right sides inhibits local HBA calculations for terminal segments. Names of reconstituted nucleosomes are indicated to the left. Note that the 601LR sequence is not completely identical to the original 147-bp sequence centering at nucleotide position 154 (\textit{Figure 5B}). The sequences of 601LR, 601L, and 601R differ at their termini for biochemical handling. For 601LR, the four original terminal bases (5'-CTGG-3' and 5'-CTGT-3') have been replaced with three-base sequences (5'-ATC-3' and 5'-GAT-3'; i.e., blunt ends created by \textit{EcoRV} digestion) [12, 13]. Here, the nucleotide base A was added to both ends of the 145-bp sequence to lengthen it to 147-bp for local HBA calculations.
Additional file 1: Figure S8. Dinucleotide frequency across chemical unique nucleosomes. (A) Non-normalized frequencies of dinucleotides starting at indicated nucleosome positions. The heatmap scale indicates the dinucleotide frequency (log10). Note: AA-TT, AC-GT, AG-CT, CA-TG, CC-GG, and GA-TC dinucleotide pairs exhibit rotational symmetry to each other, whereas AT, CG, GC, and TA dinucleotides exhibit point symmetry by themselves. AA-TT, AC-GT, AG-CT, and TA dinucleotides are highly enriched at SHL ±0.5. (B) SS dinucleotide frequency. Gray vertical lines indicate the positions of dyad (solid) and histone-DNA contact sites (SHL ±0.5-6.5). Mean frequency of each dinucleotide in the unique nucleosomes is indicated to the right and shown as an orange horizontal bar in the plot.

Additional file 1: Figure S9. Matching rate analysis for the mouse model. Matching rate between predicted and in vivo nucleosomes with variable matching window is shown. The sequence of mouse Chr19 was used for prediction with the mouse chemical map–based (nuCpos) and MNase-seq–based (NuPoP) models.
Figure 1

A

**Matched-species models**

![Graphs showing True-Positive rate vs False-positive rate for matched-species models.

B

**Cross-species models**

![Graphs showing Probability vs Distance for cross-species models.

C

**Matched-species models**

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**Cross-species models**

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Figure 2

A

Chemical map–based model

Morse-seq–based model

Normalized HBA

Dyad position (bp)

Normalized HBA

Dyad position (bp)

B

Chemical map–based model

Morse-seq–based model

C

Chemical map–based model

Morse-seq–based model
Figure 3

A

Mean HBA

Distance from -1 Nuc. (bp)

Distance from +1 Nuc. (bp)

B

Mean A/T frequency of tested 147-bp seq.

Distance from -1 Nuc. (bp)

Distance from +1 Nuc. (bp)

C

nuCpos

NuPoP

A/T

Position from the EcoRI site of TRP1ARS1 (bp)
Figure 4
Figure 6

A

WT

Dyad

Linker

Int

Dyad position (bp)

-250 0 250 500 750 1000

B

+1 Nuc.

+2 Nuc.

+3 Nuc.

HBA

Local HBA

+1

+2

+3

-15 -10 -5 0 5 10 15

-10 -5 0 5 10 15

-10 -5 0 5 10 15

Dyad position (bp)

Segment

Local HBA

WT

Dyad

Linker

Int

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Figure 7

A. Heatmaps showing dinucleotide positions for S. cerevisiae, S. pombe, and M. musculus. The color scale indicates the density of nucleosomes.

B. Graphs showing normalized CG frequency across different position (bp) values for S. cerevisiae, S. pombe, and M. musculus. The graphs indicate ** and *** significance levels.

C. ROC curves comparing nuCpos (Chemical) and NuPoP (MNase) for unique and redundant nucleosomes. The AUC values are 0.711 for nuCpos (Chemical), 0.646 for NuPoP (MNase) unique, and 0.509 for NuPoP (MNase) redundant.

D. Bar graph showing nucleosomes on the Viterbi path for matching models. The graph distinguishes between matched and matched cases.