# Simplitigs as an efficient and scalable representation of de <sup>2</sup> Bruijn graphs

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11

# Abstract

12

### Motivation

De Bruijn graphs play an essential role in computational biology, facilitating rapid alignment-free comparison of genomic datasets as well as reconstruction of underlying genomic sequences. Subsequently, an important question is how to efficiently represent, compress, and transmit de Bruijn graphs of most common types of genomic data sets, such as sequencing reads, genomes, and pan-genomes.

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### Results

We introduce simplitigs, an efficient representation of de Bruijn graphs for alignment-free applications. Simplitigs are a generalization of unitigs and correspond to spellings of vertex-disjoint paths in a de Bruijn graph. We present an easy-to-plug-in greedy heuristic for their computation and implement it in a program called ProphAsm. We use ProphAsm to compare the scaling of simplitigs and unitigs on a range of genomic datasets. We demonstrate that simplitigs are superior to unitigs in terms of the cumulative sequence length as well as of the number of sequences, and that are sufficiently close to theoretical bounds for practical applications. Finally, we demonstrate that, when combined with standard full-text indexes, simplitigs provide a scalable solution for *k*-mer search.

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### Availability

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ProphAsm is written in C++ and is available under the MIT license from <u>http://github.com/prophyle/prophasm</u>.

27

# Introduction

28	Advances in DNA sequencing started the golden age of biology in which phenomena previously unobservable can
29	be studied on an unprecedented scale. However, sequencing capacity has been growing faster than computer
30	performance and memory, and also faster than available human resources. Nowadays large amounts of sequencing
31	data are available, of a decreasing completeness and quality though. In consequence, traditional sequence-based
32	representations and sequence alignment-based techniques [1-3] have become less suitable for real-life scenarios
33	due to the space- and time-complexities they impose as well as due to their sequence-oriented nature in the age of
34	datasets exhibiting graph structure.
35	
36	An example is given by bacterial genomics. Modern large-scale studies of bacterial species comprise tens of
37	thousands of sequenced isolates (see, e.g., [4-6]). However, information about isolates' genomes is almost always
38	incomplete, as sequencing provides only partial observations of the genomes. While it is relatively straightforward
39	to compute draft assemblies of bacterial genomes, completing the genomes is difficult. Due to repetitive regions, a
40	full reconstruction from short reads is mathematically impossible even if the sequencing reads were error-free [7].
41	Long reads are often unavailable and reference sequences are of limited applicability due to the high variability of
42	bacteria and unclear borders between species. While draft assemblies may be sufficient for many analyses, they are
43	often not an ideal universal representation for a multitude of reasons. Most importantly, draft assemblies created
44	using different assemblers are not directly comparable and this can introduce false differential signals into studies
45	[8-10]. In many scenarios it is therefore desirable to move data analysis closer to the sequencing technology and
46	work with graph representations obtained directly from raw reads without assembling the genomes.
17	

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48 De Bruijn graphs belong to the most popular graph representations of genomic datasets. They are defined as 49 directed graphs G = (V, E) where V is the set of all *k*-mers (i.e., substrings of a fixed length *k*) occurring in the

dataset with edges connecting a vertex v to a vertex w if there is a k - 1 long prefix-suffix overlap between v and w. As follows from the definition, a de Bruijn graph is defined by the underlying *k*-mer set and its edges can be defined implicitly (unlike the edge-centric definition where *k*-mer sets are associated with edges [11]). In this paper, we consider only vertex-centric graphs.

54

55 De Bruijn graphs feature remarkable properties. First, their computation from data is easy and deterministic. Algorithms for enumerating and counting k-mers have been extensively studied and many programs are available 56 57 [12–15]. If the datasets contain sequencing errors, the computation may also involve graph cleaning. This aims at 58 removing those k-mers that are the result of sequencing errors and, due to their supposed randomness, are expected 59 to be rare. Second, if k is chosen appropriately, de Bruijn graphs can capture substantial information about the 60 entire molecules under sequencing as these correspond to some walks in the graphs, provided that sequencing was 61 sufficiently deep. Third, de Bruijn graphs can be handled easily, which simplifies software development as well as 62 dataset analysis and interpretation. These properties have led to a large variety of applications of de Bruijn graphs.

63

De Bruijn graphs have been widely studied in the context of sequence assembly [16–18]. Here, their construction is typically the first step to the reconstruction of genomes and transcriptomes under sequencing from retrieved sequencing reads. Many modern assemblers (e.g., SPAdes [19], ABySS [20], Velvet [21], Minia [22], and MEGAHIT [23]) follow the de-Bruijn-graph paradigm.

68

Alignment-free sequence comparison [24] is another major application of de Bruijn graphs, following the idea that similar sequences share common *k*-mers, and comparing de Bruijn graphs thus provides a good measure of sequence or dataset similarity. This involves applications of de Bruijn graphs to variant calling and genotyping [25–29], transcript abundance estimation [30], and metagenomic classification [31–34]. The latter also demonstrates another particularity of de Bruijn graphs – their remarkable ability to approximate the graph structure of pan-genomes. Indeed, reference databases of bacterial strains are often highly incomplete and noisy;

75	nevertheless, k-mer-based classifiers perform best among all classifiers in inferring abundance profiles [35], which
76	also suggests that de Bruijn graphs can be used to represent pan-genomes. Furthermore, de Bruijn graphs with a
77	large <i>k</i> -mer size can be used for indexing variation graphs [36,37].

78

The importance of de Bruijn graphs leads us to a key problem: their space-efficient representation. While general de Bruijn graphs may impose large space requirements, it has been shown that those of real datasets can be highly compressible. Indeed, given the linearity of DNA and RNA molecules and the nature of sequencing, genomic *k*-mer datasets exhibit the so-called spectrum-like property: the existence of long strings of which most of the *k*-mers are substrings [11].

84

In this paper, we study the problem of representation of de Bruijn graphs for alignment-free data analysis. Building on previous works [38,39], we propose *simplitigs* as an effective representation of de Bruijn graphs. Simplitigs provide a "textual" representation of the graph, in the form of a set of sequences, representing each *k*-mer exactly once and facilitating easy indexing with standard full-text indexes. Simplitigs use the observation that in practical applications, such graphs typically contain long paths. In contrast to unitigs, which are the paths that do not contain any branching nodes, simplitigs can contain branching nodes.

91

Finally, we present ProphAsm, a tool for computing simplitigs for a given dataset, such as reads, genomes,
pan-genomes or metagenomes. ProphAsm proceeds by building the associated de Bruijn graph in memory,
followed by a greedy enumeration of maximal vertex-disjoint paths. We use ProphAsm to demonstrate that
simplitigs are superior to unitigs both in terms of the cumulative sequence length and the number of sequences, and
that they are sufficiently close to theoretical bounds in practical applications. The employed heuristic can be easily
integrated into any software producing de Bruijn graphs.

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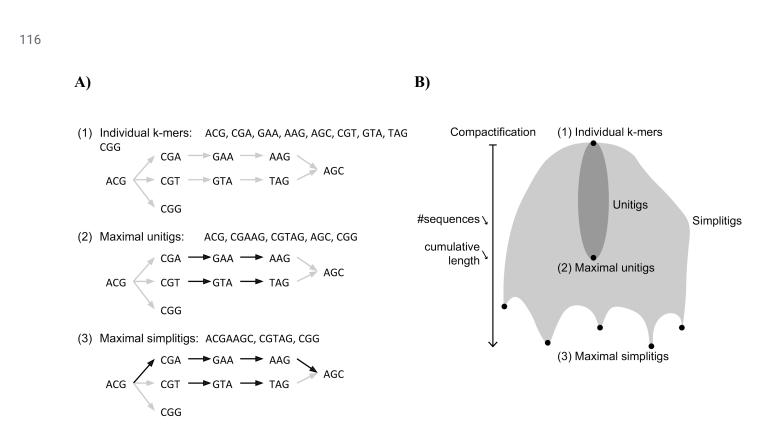
# Results

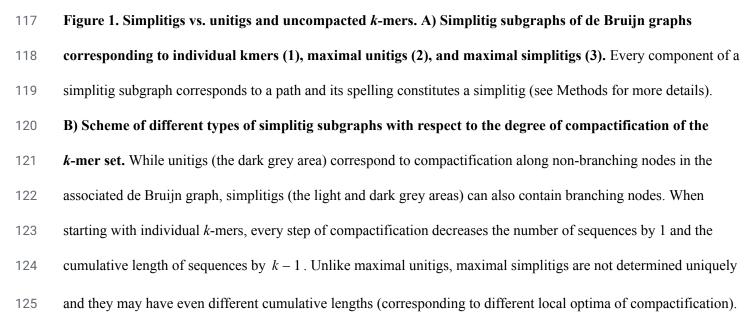
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100	We developed the concept of simplitigs to efficiently represent de Bruijn graphs for alignment-free applications
101	(Figure 1). Simplitigs are a generalization of unitigs and correspond to spellings of vertex-disjoint paths covering a
102	given de Bruijn graph; consequently, maximal simplitigs are such simplitigs that cannot be further compacted by
103	merging (Methods). Note that unitigs and k-mers are also simplifies, but not maximal, in general. The main
104	conceptual difference between maximal simplitigs and maximal unitigs is that unitigs are limited by branching
105	nodes (which are crucial for genome assembly), whereas simplitigs are not limited by this constraint. This allows
106	for further compactification, with a benefit increasing proportionally to the amount of branching nodes in the graph.
107	
108	We designed a greedy heuristic for the computation of simplitigs (Algorithm 1, Methods). At every step, it selects
109	a k-mer from the current k-mer set and keeps extending it forward and then backward as long as possible, while
110	removing the already used k-mers from the set. This process is repeated until all k-mers are covered. We provide an
111	implementation in a program called ProphAsm (github.com/prophyle/prophasm). The heuristic can be easily
112	applied by any other software that outputs de Bruijn graphs or k-mer sets.
113	

Simplifies as an efficient representation of de Bruijn graphs

In the following sections, we use ProphAsm to compare maximal simplitigs with maximal unitigs on different typesof data sets.





126 Algorithm 1. Greedy computation of maximal simplitigs for a *k*-mer set. In an iterative fashion, the algorithm

127 draws a k-mer from the set of canonical k-mers K, uses it as a new simplified, and then keeps extending the

simplify forwards and backwards as long as possible, while removing the already used canonical *k*-mers from *K*.

```
Function extend simplitig forward (K, simplitig):
129
130
             extending = True
131
             while extending:
                    extending = False
132
                    q = suffix (simplify, k-1),
133
                    for x in ['A', 'C', 'G', 'T']:
134
135
                           can kmer = canonical(q + x)
                           if can kmer in K:
136
                                  extending = True
137
                                  simplitig = simplitig + x
138
139
                                  K.remove (can kmer)
140
                                  break
             return K, simplitig
141
142
143
      Function get maximal simplitig (K, initial kmer):
             simplitig = initial kmer
144
145
             K.remove (initial kmer)
             K, simplitig = extend simplitig forward (K, simplitig)
146
             simplitig = reverse completent (simplitig)
147
             K, simplitig = extend simplitig forward (K, simplitig)
148
             return K, simplitig
149
150
151
      Function compute simplitigs (kmers):
152
             K = \{ \}
153
             for kmer in kmers:
154
                    K.add (canonical(kmer))
155
             simplitigs = \{\}
             while |K| > 0:
156
                    initial kmer = K.pop ()
157
                    K, simplitig = get maximal simplitig (K, initial kmer)
158
                    simplitiqs.add (simplitiq)
159
160
             return simplitigs
```

161

## Simplitigs of selected model organisms

162	We evaluated the simplified representation on individual genomes of six model organisms for a range of k-mer
163	lengths (Figure 2, Methods). Understanding the scaling based on the <i>k</i> -mer length is important for practical
164	applications; the k-mer size is typically chosen with respect to the used sequencing technology and genomic
165	diversity. The range for our experiments was selected based on values that are most commonly used for
166	alignment-free sequence comparison (see, e.g., [30,31,40]). For each organism and a k-mer length, we computed
167	maximal simplitigs and unitigs, and compared them in terms of two basic characteristics: the number of sequences
168	produced and their cumulative length. Whereas the former defines the number of records to be kept, the latter
169	determines the total memory needed. Note that the two numbers are tightly connected (Methods, (eq 1)).
170	
171	First, we analyzed the number of sequences produced (Figure 2, upper plots). We observe that for all datasets, as
172	the k-mer size increases, the number of simplitigs grows and then decreases slowly. The number of unitigs grows
173	rapidly at the beginning, and subsequently drops substantially, approaching the number of simplitigs. The
174	cumulative length (Figure 2, lower plots) is bounded from below by the number of <i>k</i> -mers in the genome plus
175	k-1, corresponding to the theoretically maximum degree of compactification. In such a case, all k-mers would
176	occur on the same simplifig; however, this is not attainable for most datasets. As we can observe and (eq 1)
177	explains, the shapes of the curves in the lower plots copy the upper plots, while being only shifted up by a factor of
178	the theoretical lower bound. When comparing the simplifig and unitig curves, we can observe the same patterns as
179	for the number of sequences.

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- 181

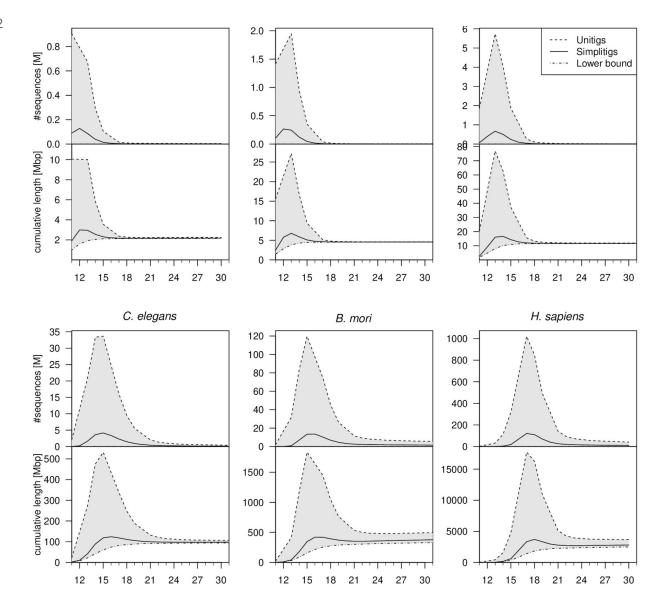


Figure 2. Comparison of the simplifig and unitig representations for selected model organisms and a range of *k*-mers. The number of sequences and their cumulative length for representation obtained by ProphAsm, BCALM 2 and the theoretical lower bound for six model organisms ordered by their genome size: *S. pneumoniae* (2,22Mbp),

186 Escherichia coli (genome length: 4.64 Mbp), Saccharomyces cerevisiae (genome length: 12.2 Mbp),

187 *Caenorhabditis elegans* (genome length: 100 Mbp), *Bombyx mori* (genome length: 482 Mbp), and *Homo sapiens* 

188 (genome length: 3.21 Gbp). The area highlighted in grey shows the discrepancy between the maximal unitigs and

189 the theoretical lower bound.

Note that the maxima of both functions occur at (or are very close to) the value  $k = log_4 G$ , where G is the genome 191 size. This is readily explained, as for values of k up to  $log_4G$ , an overwhelming fraction of all  $4^k$  k-mers belong 192 193 to the genome, which makes the de Bruijn graph branch at nearly every node. As a consequence, unitigs are essentially reduced to individual k-mers, and their number grows exponentially. Starting from  $k = log_4 G$ , the 194 195 number of k-mers is bounded by the genome length, and they begin to form longer non-branching paths in the 196 graph, which drives down the number of unitigs. Importantly, however, the number of unitigs and their total size 197 keep being much larger than those of simplify even for larger values of k, especially for large eukaryotic 198 genomes.

199

200 Overall, we observed that simplify always provide better performance than unitigs. In particular, they quickly 201 approach the theoretical lower bounds for both characteristics tested. Every data set has a range of k-mer lengths 202 where the difference between simplify and unitigs is striking, and after a certain threshold, the difference almost 203 vanishes. While for short genomes this threshold is located at smaller k-mer lengths than those typically used in 204 alignment-free applications (e.g.,  $k \approx 17$  for *E. coli*), for long genomes this threshold has not been attained on the 205 tested range and seems to be substantially shifted towards large k-mers (e.g., B. mori). All this suggests that in 206 practical applications, simplify are preferable for indexing individual genomes and the benefit is likely to increase 207 with the genome size.

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#### Simplitigs of bacterial pan-genomes

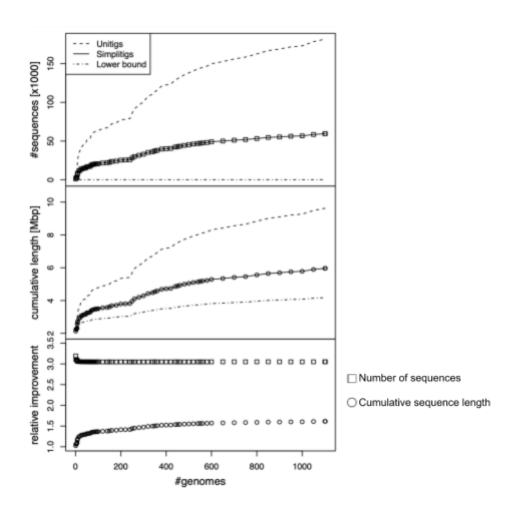
210	Computational pan-genomics has recently emerged as an important sub-branch of bioinformatics [41]. One of the
211	motivations is the analysis of sequencing data in the context of whole species. Species are then represented using
212	so-called pan-genome representations, i.e., reference structures including all within-species variation. De Bruijn
213	graphs are particularly useful as pan-genomic references as they can be easily constructed from a variety of
214	different data types, ranging from assembled reference sequences to the original sequencing reads. We sought to
215	evaluate the usefulness of simplitigs for bacterial pan-genomes, which are particularly challenging due to their high
216	diversity and variability.

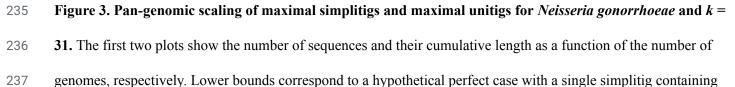
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218 We compared simplify and unitig representations of the *Neisseria gonorrhoeae* pan-genome, as a function of the 219 number of genomes included for the k-mer length 31 (Figure 3, Methods). We used 1,102 clinical isolates collected 220 from 2000 to 2013 by the Centers for Disease Control and Prevention's Gonococcal Isolate Surveillance Project 221 [42]; the data set comprises draft assemblies from Illumina HiSeq reads. As expected, as the number of isolates and 222 the associated variance grow, the number of sequences and their cumulative length grow as well, both for maximal unitigs and simplify. While simplify and unitigs perform comparably well when one bacterial genome is 223 included (consistent with Figure 2), the improvement of simplifies over unitigs grows in the cumulative length as 224 225 more genomes are included and eventually stabilizes at a factor of approximately 1.5 (Figure 3, bottom plot). On 226 the other hand, the improvement in the number of sequences steadily decreases along the whole range and stabilizes 227 at a factor of approximately 3.0.

228

To verify the generality of our findings, we repeated the experiment with the same dataset for the *k*-mer length 18 and also with 616 pneumococcal genomes from a carriage study of children in Massachusetts [43,44] with the *k*-mer lengths 18 and 31 (Methods). In all cases, the results were qualitatively the same, except for small changes in the resulting relative improvements.





- all the *k*-mers. The third plot displays the relative improvement of simplifies compared to unitigs.
- 239

240

### Application of simplitigs for *k*-mer search in bacterial pan-genomes

- Any sequence data can be searched for k-mers using full-text indexes. Importantly, the simplify representation can 241 242 accelerate the k-mer lookup in datasets with redundant k-mer content by removing these redundancies, which we 243 show on the example of *k*-mer look up in bacterial pan-genomes. 244 245 The most popular compact and powerful indexes supporting fast string search are BWT indexes [48], i.e., indexes 246 based on the Burrows-Wheeler Transform [49], sometimes also referred to as FM-indexes. Many highly optimized 247 implementations were developed for read mapping (e.g., [45–47]); in our experiments we used the BWA index 248 [46], following the widespread use and superior performance. 249 Single pan-genome 250 We first evaluated the performance of k-mer presence/absence queries on a single pan-genome (**Table 1**, Methods). 251 We used the same N. gonorrhoeae draft genome assemblies as previously to build a gonococcal k-mer pan-genome 252 for five different k-mer sizes using three strategies: by merging the draft assemblies, by computing comprehensible 253 unitigs, and by computing comprehensive simplifies (Table 1a). For all of them, we constructed BWT indexes 254 using BWA [46], queried ten million k-mers using BWA fastmap [50], and evaluated the resulting memory footprint 255 and query performance (Table 1b). 256 257 Consistent with the previous experiments, simplify provided a clear improvement over unitigs (Table 1a). 258 Maximal simplify improved  $3.0 \times -4.9 \times$  the number of sequences and a  $1.5 \times -2.1 \times$  the cumulative sequence 259 lengths. Intuitively, the resulting memory footprint of BWA should be proportional to the cumulative sequence
- length, and therefore, the improvement in memory footprint was expected to be similar to the one of the cumulative
- sequence length. Surprisingly, the memory footprint improved substantially more  $(2.7 \times -5.6 \times)$  (**Table 1b**). To
- explain this phenomenon, it is important to understand that the underlying full-text engine has to keep information

263	about individual sequences in memory as separate records and standard read mappers are optimized for low
264	numbers of references. As the number of reference sequences grows, it has a negative impact on both the memory
265	footprint and query speed. However, since simplitigs provided 3.0×-4.9× improvement in the number of sequences
266	over unitigs, it helped to alleviate this overhead. Overall, the comparatively high number of maximal unitigs
267	observed throughout our experiments (Figures 1 and 2) provides a further argument for using simplitigs as the
268	preferable representation of k-mer sets.

- 269
- 270

Table 1. *K*-mer queries for the *N. gonorrhoeae* pan-genome. a) Characteristics of the obtained unitigs and
simplitigs. b) Time and memory footprint of BWA for *k*-mer queries (10M *k*-mers).

k	Draft assemblies		Unitigs		Simplitigs	
	# sequences [×10 <sup>3</sup> ]	cumulative length [Mbp]	# sequences [×10 <sup>3</sup> ]	cumulative length [Mbp]	# sequences [×10 <sup>3</sup> ]	cumulative length [Mbp]
15			440	9.3	90	4.4
19			190	6.9	60	4.5
23	79	2,400	180	7.7	59	5.0
27			180	8.6	59	5.5
31			180	9.6	60	6.0

273

274 **b**)

k	Draft assemblies		Unitigs		Simplitigs	
	time [sec]	mem [MB]	time [sec]	mem [MB]	time [sec]	mem [MB]
15	34	3,600	42	78	24	14
19	50		35	37	28	12
23	66		41	37	32	13
27	81		48	38	37	14
31	97		56	40	42	14

### Multiple pan-genomes

277	Finally, we evaluated the performance of the simplifig representation for simultaneous indexing of multiple
278	bacterial pan-genomes (Table 2, Methods). We downloaded all complete bacterial genomes from Genbank (as of
279	December 2019; 10,502 genomes out of which we managed to download 9,570; Methods). We restricted ourselves
280	to the complete genomes as the draft genomes in Genbank are known to be largely impacted by contamination
281	[51–53]. We grouped individual genomes per species which resulted in 719 bacterial pan-genomes. We then
282	computed simplitigs and unitigs for every species, merged the obtained representations, and calculated the same
283	statistics as previously (Table 2a); we performed this experiment for the <i>k</i> -mer lengths 18 and 31. Finally, we
284	constructed BWT indexes using BWA, and measured the resulting k-mer lookup performance using the same ten
285	million <i>k</i> -mers as in the previous section (Table 2b).
286	
287	In this case, the number of sequences was reduced by a factor of $4.2 \times$ and $3.1 \times$ and the cumulative sequence length
288	by a factor of $1.6 \times$ and $1.3 \times$ for $k = 18$ and $k = 31$ , respectively ( <b>Table 2a</b> ). For $k = 31$ simplifies provided $1.2 \times$
289	speedup and $1.8 \times$ improvement in memory consumption ( <b>Table 2b</b> ); for $k = 18$ , the speedup could not be
290	evaluated (Methods). These results are consistent with the previous sections and provide further evidence that
291	simplitigs are useful not only for storage, but also for fast k-mer lookup.

#### **Table 2.** *K*-mer queries for multiple pan-genomes indexed simultaneously. Bacterial pan-genomes were

computed from the complete Genbank assemblies. **a)** Characteristics of the obtained unitigs and simplify. **b)** Time

and memory footprint of BWA for *k*-mer queries (10 million *k*-mers).

#### 295 a)

k	Unit	igs	Simplitigs		
	# sequences [×10 <sup>6</sup> ]	<b>cumulative</b> length [Gbp]	# sequences [×10 <sup>6</sup> ]	cumulative length [Gbp]	
18	250	9.0	59	5.7	
31	110	8.6	36	6.4	

296

#### 297 **b**)

k	Unitigs		Simplitigs	
N	time [s]	mem [GB]	time [s]	mem [GB]
18	NA	21	146	15
31	179	23	149	13

299

# Discussion

300	We introduced the concept of simplitigs, a generalization of unitigs, and demonstrated that simplitigs constitute a
301	compact, efficient and scalable representation of de Bruijn graphs for commonly used genomic datasets. The two
302	representations share many similarities. Both represent de Bruijn graphs in a lossless fashion, correspond to
303	spelling of vertex-disjoint paths, and preserve k-mer sets. Being text-based and stored as FASTA files, both can be
304	easily manipulated using standard Unix tools and indexed using full-text indexes. On the other hand, unlike unitigs,
305	general simplitigs are not expected to have direct biological significance as neighboring segments of the same
306	simplitig may correspond to distant parts of the same DNA molecule or even to different ones. Not all situations
307	allow unitigs to be replaced by simplitigs, but where applicable, simplitigs show much better compression
308	properties.
309	
310	We provided ProphAsm, a tool implementing a greedy heuristic to compute maximal simplitigs from a k-mer set.
311	This heuristic is easy to implement in any software, which suggests its further use as a generic method for
312	serialization of k-mer sets. The simplicity is in contrast to the unitig model, where the complexity of the bi-directed
313	de Bruijn graph model may complicate debugging; for instance, BCALM 2 does not support k-mer lengths that are
314	divisible by four (as for December 2019; unsupported since 2017). As a downside, the naive implementation of the
315	ProphAsm heuristic using a standard hashtable may run into memory issues. However, the memory consumption
316	can be readily improved using more advanced data structures, similarly to what has been done for tools for unitig
317	computation [39,54,55].
318	
319	We note that ProphAsm is a spin-off of the ProPhyle software ( <u>https://prophyle.github.io/</u> , [33]) for
320	phylogeny-based metagenomic classification. Simplitig computation is an important component of ProPhyle [56],
321	allowing efficient indexing of k-mers assigned to nodes of the phylogenetic tree. Independently of the present work,

322 simplifies were also recently studied in [57] under the name "spectrum-preserving strings".

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3	2	J

324	The data presented in this paper highlight the scaling of computational resources as more sequencing data become
325	available [58]. The studied gonococcal dataset constitutes a relatively complete image of a bacterial population in a
326	geographical region and at a given time scale. As such, it can be used to model the "state of completion" of k-mer
327	pan-genomes. On the other hand, the multiple pan-genomes experiment provided insights about the resulting
328	performance when a large number of pan-genomes is queried simultaneously using a BWT index. This allows us to
329	make predictions about the scaling for species where at present only a limited number of assemblies are available,
330	but more data are likely to be generated in the future. Overall, with more data available, the comparative benefits of
331	simplitigs over unitigs grow.
332	
333	Besides the presented advantages, simplitigs also introduce several technical challenges related to the ambiguity (as
334	illustrated in Figure 1). Whereas maximal unitigs are uniquely defined (up to the order and reverse
335	
	complementing), this is not the case for maximal simplitigs. In the presented heuristic, the resulting maximal
336	complementing), this is not the case for maximal simplifies. In the presented heuristic, the resulting maximal simplifies and their characteristics depend on the order in which the initial <i>k</i> -mers are drawn from the underlying
336 337	
	simplitigs and their characteristics depend on the order in which the initial <i>k</i> -mers are drawn from the underlying
337	simplitigs and their characteristics depend on the order in which the initial <i>k</i> -mers are drawn from the underlying set. At every iteration, once a maximal simplifig is built, a new <i>k</i> -mer is drawn from the graph as the new initial

340

Modern bioinformatics applications of de Bruijn graphs often require multiple graphs considered simultaneously.
The resulting structure is usually referred to as a colored de Bruijn graph [25] and its representations have been
widely studied ([59–70]). Even though we touched upon this setting in the section Multiple pan-genomes,
exploiting the similarity between individual de Bruijn graphs for further compression in simplitig-based approaches
is to be addressed in future work.

- 347 With the growing interest in *k*-mer indexing of all genomic datasets [69], we anticipate the simplified representation
- to be valuable as a generic compact representation of de Bruijn graphs.

349

# Methods

350

### De Bruijn graphs

351	All strings are assumed to be over	the alphabet {	$\{A, C, G, T\}$	. A <i>k</i> -mer is a	a string of length $k$	. For a string
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- $s = s_1 \dots s_n$ , we define  $pref_k(s) = s_1 \dots s_k$  and  $suf_k(s) = s_{n-k+1} \dots s_n$ . For two strings s and t of length at least k, we
- define the binary connectivity relation  $s \rightarrow_k t$  if and only if  $pref_k(s) = suf_k(t)$ . Given a set K of k-mers, the de
- Bruijn graph of K is the directed graph G = (V, E) with V = K and  $E = \{(u, v) \mid u \rightarrow_{k-1} v\}$ . This definition of de
- 355 Bruijn graphs is *node-centric*, as nodes are identified with *k*-mers and edges are implicit. Therefore, we can use the
- terms "k-mer set" and "de Bruijn graph" interchangeably.

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365

#### Simplifigs

Consider a set *K* of *k*-mers and the corresponding de Bruijn graph G = (V, E). A *simplitig graph* G' = (V, E') is a spanning subgraph of *G* that is acyclic and the in-degree and out-degree of any node is at most one. It follows from this definition that a simplitig graph is a vertex-disjoint union of paths called *simplitigs*. A simplify is called *maximal* if it cannot be extended forward or backward without breaking the definition of simplitig graph. In more detail, a simplify  $u_1 \rightarrow_{k-1} u_2 \rightarrow_{k-1} ... \rightarrow_{k-1} u_n$  is maximal if the following conditions hold

• either  $u_1$  has no incoming edges in G, or for any edge  $(v, u_1) \in E$ , v belongs to another simplifig and it is not its last vertex,

either  $u_n$  has no outgoing edges in G, or for any edge  $(u_n, v) \in E$ , v belongs to another simplified and it is

#### 366 not its first vertex.

•

A *unitig* is a simplifig  $u_1 \rightarrow_{k-1} u_2 \rightarrow_{k-1} u_n$  such that each of the nodes  $u_2, ..., u_n$  has in-degree 1 in graph *G*. A maximal unitig is defined similarly.

369

# Greedy computation of simplitigs

370	The problem of computing maximal simplitigs that are optimal in the cumulative sequence length corresponds to
371	the vertex-disjoint path cover problem, which is known to be NP-hard in the general case [71] but the complexity is
372	unknown for de Bruijn graphs. Throughout this paper, a greedy approach was used for the computation of
373	simplitigs (Algorithm 1). Simplitigs were constructed iteratively, starting from an arbitrary k-mer and being
374	extended greedily forwards and backwards as long as possible. Note that Algorithm 1 works in the bi-directed
375	setting, in which canonical k-mers are used instead of "standard" k-mers. A formal definition of bi-directed de
376	Bruijn graphs requires complex formalism (see, e.g.,
377	https://github.com/GATB/bcalm/tree/master/bidirected-graphs-in-bcalm2). Since the greedy heuristic works
378	similarly in both setups and does not require the extended formalism, we resorted to the uni-directed model for the
379	explanation of the concepts.
380	
	Comparing simplitigs with unitigs
381	We compare simplitigs and unitigs in terms of the number of sequences produced and their cumulative length. Note
382	that these numbers are related: assuming that the frequency of every k-mer is 1, then
383	$cum\_seq\_len = \#kmers + (k-1) \#seqs \qquad (eq 1)$
384	Finding the optimal solutions can be highly expensive computationally. However, we can easily provide the lower
385	bound $\#kmers + k - 1$ , corresponding to the maximum possible degree of compactification (i.e., a single
386	simplitig covering all k-mers). In the situations where cumulative sequence length of simplitigs approaches this
387	bound, the greedy heuristic presented above is sufficient.
388	
	Correctness evaluation
389	The correctness of simplitigs can be verified using an arbitrary k-mer counter. Simplitigs are correct if and only if
390	every k-mer is present exactly once and the number of distinct k-mers is the same as in the original datasets. To

verify the correctness of ProphAsm outputs, we used JellyFish 2 [12].

392

### Experimental evaluation – model organisms

393	Reference sequences for six selected model organisms were downloaded from RefSeq: S. pneumoniae str. ATCC
394	700669 (accession: NC_011900.1, length 2.22 Mbp), Escherichia coli str. K-12 (accession: NC_000913.3, length:
395	4.64 Mbp), Saccharomyces cerevisiae (accession: NC_001133.9, length: 12.2 Mbp), Caenorhabditis elegans
396	(accession: GCF_000002985.6, length: 100 Mbp), <i>Bombyx mori</i> (accession: GCF_000151625.1, length: 482 Mbp),
397	and Homo sapiens (HG38, http://hgdownload.soe.ucsc.edu/goldenPath/hg38/bigZips/hg38.fa.gz, length: 3.21 Gbp).
398	For each of them, simplitigs and unitigs were computed using ProphAsm and BCALM 2, respectively, for the range
399	of k-mer sizes [11,31]. As the BCALM 2 algorithm does not support k-mer sizes that are multiples of 4, the
400	corresponding experiments had been excluded from the evaluation. When applied to HG38, both programs also
401	experienced in a single case of an integer overflow error: BCALM 2 and ProphAsm failed with $k = 31$ and
402	k = 16, respectively.
403	Experimental evaluation – pan-genomic scaling

First, 1,102 draft assemblies of N. gonorrhoeae clinical isolates (collected from 2000 to 2013 by the Centers for 404 405 Disease Control and Prevention's Gonococcal Isolate Surveillance Project [42], and sequenced using Illumina 406 HiSeq) were downloaded from Zenodo [72]. Second, 616 draft assemblies of S. pneumoniae isolates (collected 407 from 2001 to 2007 for a carriage study of children in Massachusetts, USA [43,44], and sequenced using Illumina HiSeq) were downloaded from the SRA FTP server using the accession codes provided in Table 1 in [44]. For each 408 409 of these datasets, an increasing number of genomes was being taken, merged and simplify and unitigs computed using ProphAsm and BCALM 2, respectively. This experiment was performed for k = 18 and k = 31. To avoid 410 411 excessive resource usage the functions were evaluated at points in an increasing distance (for intervals [10, 100] 412 and  $[100, +\infty]$  only multiples of 5 and 20 were evaluated, respectively).

л	1	2	
4	1	3	

### Experimental evaluation – fulltext *k*-mer queries

414	In the single pan-genome experiment, the same 1,102 assemblies of N. gonorrhoeae were merged into a single file.
415	ProphAsm and BCALM 2 were then used to compute simplitigs and unitigs from this file for
416	k = 15, 19, 23, 27, 31. All three obtained FASTA files (assemblies, simplifies, and unitigs) were used to construct
417	a BWA index, which was then queried for k-mers using 'bwa fastmap -l {kmer-size}'. The k-mers were previously
418	generated from the same pan-genome using DWGsim [73] (version 0.1.11, with the parameters '-z 0 -1 {kmer-size}
419	-2 0 -N 10000000').
420	
421	For the multiple pan-genome experiment, a list of available bacterial assemblies was downloaded from
422	ftp://ftp.ncbi.nlm.nih.gov/genomes/genbank/bacteria/assembly_summary.txt. For all assemblies marked as
423	complete, accessions were extracted and used for their download using RSync (files matching
424	*v?_genomic.fna.gz'). The assemblies were then merged and the obtained master file then used for computing
425	simplitigs and unitigs using ProphAsm and BCALM 2. The obtained simplitig and unitig files were used to
426	construct a BWA index and queried for the same k-mers as in the previous section using 'bwa fastmap -l
427	{kmer-size}'. The times of loading the indexes into memory were measured separately and subtracted from the
428	query times. With unitigs for $k = 18$ , bwa repeatedly crashed in the middle of k-mer matching for an unspecified
429	reason.

430

### Computational setup

The model organism experiment was performed on the HMS O2 research high-performance cluster on nodes with
120 GB RAM. All other experiments were performed on an iMac 4.2 GHz Quad-Core Intel Core i7 with 40 GB
RAM and an SSD disk. The reproducibility of computation was ensured using BioConda [74]. All benchmarking
was performed using ProphAsm v0.1.0 and BCALM 2 v2.2.1 (commit c8ac60252fa). Times and memory footprint
were measured using GNU time.

#### 436

### Implementation and availability

437 ProphAsm is written in C++ and available under the MIT license from <a href="http://github.com/prophyle/prophasm">http://github.com/prophyle/prophasm</a>. The
438 software package is also available from BioConda [74].

439

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