Population-specific F_{ST} and Pairwise F_{ST}:

History and Environmental Pressure

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ABSTRACT

Appropriate estimates of population structure are the basis of population genetics, with applications varying from evolutionary and conservation biology to association mapping and forensic identification. The common procedure is to first compute Wright's F_{ST} over all samples (global F_{ST}) and then routinely estimate between-population F_{ST} values (pairwise F_{ST}). An alternative approach for estimating population differentiation is the use of population-specific F_{ST} measures. Here, we characterize population-specific F_{ST} and pairwise F_{ST} estimators by analyzing publicly available human, Atlantic cod and wild poplar data sets. The bias-corrected moment estimator of population-specific F_{ST} identified the source population and traced the migration and evolutionary history of its derived populations by way of genetic diversity, whereas the bias-corrected moment estimator of pairwise F_{ST} was found to represent current population structure. Generally, the first axis of multi-dimensional scaling for the pairwise F_{ST} distance matrix reflected population history, while subsequent axes indicated migration events, languages and the effect of environment. The relative contributions of these factors were dependent on the ecological characters of the species. Given shrinkage towards mean allele frequencies, maximum likelihood and Bayesian estimators of locus-specific global F_{ST} improved the power to detect genes under environmental selection. In contrast, bias-corrected moment estimators of global F_{ST} measured species divergence and enabled reliable interpretation of population structure. The genomic data highlight the usefulness of the bias-corrected moment estimators of F_{ST}. The R package FinePop2_ver.0.2 for computing these F_{ST} estimators is available at CRAN.

Quantifying genetic relationships among populations is of substantial interest in population

biology, ecology and human genetics (Weir and Hill 2002). Appropriate estimates of

population structure are the basis of population genetics, with applications varying from

evolutionary and conservation studies to association mapping and forensic identification

(Weir and Hill 2002; Weir and Goudet 2017). For such objectives, Wright's F_{ST} (Wright 1951)

is commonly used to quantify the genetic divergence of populations (reviewed by Excoffier

2001; Rousset 2001; Balloux and Lugon-Moulin 2002; Weir and Hill 2002; Rousset 2004;

Beaumont 2005; Holsinger and Weir 2009). Wright (1951) defined F_{ST} as "the correlation

between randomly sampled gametes relative to the total drawn from the same subpopulation";

that is, $F_{ST} = \frac{F_{IT} - F_{IS}}{1 - F_{IS}}$, where F_{IS} and F_{IT} are the inbreeding coefficients of individuals

relative to their substrains and the total. Nei (1973) proposed the G_{ST} measure as a

formulation of Wright's F_{ST}, which is the ratio of between-population heterozygosity to total

gene heterozygosity. Nei (1977) defined Wright's F-statistics (F_{ST}, F_{IS} and F_{ST}) in terms of

heterozygosity. Crow and Aoki (1984) introduced the concept of gene identity and defined

G_{ST}, while Slatkin (1991) defined F_{ST} in terms of probabilities of identity. F_{ST} has also been

defined in terms of gene identity (Rousset 2001, 2002; Excoffier 2001). G_{ST} is identical to F_{ST}

(Nei 1975, 1977; Crow and Aoki 1984). The equality of G_{ST} and F_{ST} has been given for bi-

allelic (Nei 1975, 1977; Crow and Aoki 1984) and multi-allelic cases for pairwise F_{ST} at a

single locus (Kitada *et al.* 2017). Published definitions of G_{ST} and F_{ST}, the relationship

between G_{ST} and F_{ST}, and the F_{ST} estimators used in this study are summarized in

Supplemental Note.

Various F_{ST} estimators based on sampling design as well as maximum likelihood and

Bayesian framework have been considered (reviewed by Weir 1996; Excoffier 2001; Rousset

2001; 2004, Balloux and Lugon-Moulin 2002; Holsinger and Weir 2009). Nei and Chesser

(1983) proposed a moment estimator (hereafter, NC83) that corrects the bias of G_{ST} using

unbiased estimators of the numerator (between-population heterozygosity) and denominator

(total heterozygosity). NC83 takes into account a sample set of subpopulations taken from a

present-day metapopulation but does not consider sample replicates. Weir and Cockerham

(1984) proposed a moment estimator of F_{ST} denoted by θ (hereafter, WC84) that uses

unbiased estimators of the numerator (between-population variance) and the denominator

(total variance). WC84, a coancestry coefficient, considers replicates of samples taken from

an ancestral population. This estimator considers observed variance components of allele and

heterozygote frequencies between populations, between individuals within populations, and

between gametes within an individual, based on the analysis of variance (ANOVA)

framework of Cockerham (1969, 1973). The analysis of molecular variance approach

(Excoffier *et al.* 1992) used in Arlequin (Excoffier and Lischer 2010) also defines F_{ST} as the

proportion of the variance components. Estimators of Wright's F-statistics based on gene

identity coefficients with a different weighting scheme have also been defined (Rousset

2008). These moment F_{ST} estimators, which are implemented in either Arlequin or Genepop

(Raymond and Rousset 1995; Rousset 2008), produce identical or very similar values to those

obtained using WC84 implemented in FSTAT (Goudet 1995).

Wright (1931, 1951) modeled the distribution of gene frequencies in island populations using

a beta distribution. As an extension of Wright's approach, maximum likelihood methods for

estimating F_{ST} and/or genetic differentiation apply beta-binomial (for two alleles) and/or

multinomial-Dirichlet (for multiple alleles) distributions to determine the likelihood of sample

allele counts (Balding and Nichols 1995; Lange 1995; Rannala and Hartigan 1996; Kitada *et*

al. 2000; Balding 2003; Kitada and Kishino 2004; Kitakado *et al.* 2006; Kitada *et al.* 2007).

Bayesian approaches have also been developed to obtain posterior mean F_{ST} values and/or

posterior distributions (Balding *et al.* 1996; Holsinger 1999; Lockwood *et al.* 2001; Holsinger

et al. 2002; Corander *et al.* 2003; Steele *et al.* 2014). These methods use beta and/or Dirichlet

distributions as prior distributions of allele frequencies.

All the above-mentioned F_{ST} estimators were basically developed to estimate mean F_{ST} over

loci and over populations based on a set of population samples, often called global F_{ST} (*e.g.*,

Pérez-Lezaun *et al.* 1997; Rousset 2004). In empirical studies, global F_{ST} is first estimated and

then F_{ST} values between pairs of populations (pairwise F_{ST}) are routinely estimated as

implemented in standard population genetics software programs such as Arlequin (Excoffier

and Lischer 2010), FSTAT (Goudet 1995) and Genepop (Raymond and Rousset 1995;

Rousset 2008). Pairwise differences are tested, similar to one-way ANOVA, when a

significant difference in the means is detected. This procedure has been widely adopted to

study species ranging from plants to animals (Weir and Hill 2002) and, more recently, the

approach has been used in population genomics analyses of various species such as small

freshwater fish (Malinsky 2015), herring (Lamichhaney *et al.* 2017), tobacco cutworm (Cheng

et al. 2017), drosophila (Griffin *et al.* 2017) and humans (Bhatia *et al.* 2013; Lazaridis *et al.*

2016; Anopheles gambiae 1000 Genomes Consortium 2017; Stolarek *et al.* 2018). Bhatia et

al. (2013) proposed the bias-corrected F_{ST} estimator of Hudson (1992) for comparing two

populations at a series of single nucleotide polymorphisms (SNPs). In a later study, this

estimator was applied to measure the difference between ancient and contemporary human

populations (Prohaska et al. 2019). An F_{ST} estimator between two populations that has been

defined for large sample sizes by Weir and Goudet (2017, Equation 10) is applicable to such

situations.

An alternative approach for estimating population differentiation is the use of population-

specific F_{ST} estimators (Balding and Nichols 1995; Nicholson *et al.* 2002; Weir and Hill 2002;

Weir *et al.* 2005; reviewed by Gaggiotti and Foll 2010; Weir and Goudet 2017). Model-based

(Bayesian) approaches for estimating population-specific F_{ST}, referred to as *F*-models (Falush

et al. 2003), have been proposed for bi-allelic (Balding and Nichols 1995; Nicholson *et al.*

2002) and multi-allelic (Falush *et al.* 2003) cases. Karhunen and Ovaskainen (2012) proposed

an admixture *F*-model that extends the *F*-model of Falush *et al.* to account for limited gene

flow and small effective population size. Locus-population-specific F_{ST} is applied to identify

adaptive genetic divergence at a gene among populations using empirical Bayes (Beaumont

and Balding 2004) and full Bayesian methods (BayeScan) (Foll and Gaggiotti 2006, 2008).

Bias-corrected moment estimators of population-specific F_{ST} have also been proposed (Weir

and Hill 2002; Weir *et al.* 2005; Weir and Goudet 2017). Weir and Goudet (2017) derived

unbiased estimators for the components of the coancestry coefficients of the population-

specific F_{ST} estimator (hereafter, WG population-specific F_{ST}). The definition of the

population-specific F_{ST} is $\beta_{ST}^i = \frac{\theta_S^i - \theta^B}{1 - \theta^B}$, where θ_S^i is the average coancestry coefficient

within subpopulation *i*, and θ^B is that "over pairs of populations" (Weir and Goudet 2017).

Therefore, θ^B represents the average coancestry in all population samples, and $\beta_{ST}^i = F_{ST}^i$.

An important property of the population-specific F_{ST} measure is that "the usual global F_{ST}

estimator can be an unweighted average of population-specific F_{ST}"; as defined by Hudson et

al. (1992, Equation 3), this measure is described by the equation $\beta_{ST} = \frac{\theta^S - \theta^B}{1 - \theta^B}$ (Weir and

Goudet 2017). The population-specific F_{ST} for allele frequency data is $\beta_{WT}^i = \frac{\theta_W^i - \theta^B}{1 - \theta^B}$, and its

average over populations has been given previously (*e.g.*, Rousset 2004; Karhunen and

Ovaskainen 2012), namely, $F_{ST} = \frac{\theta^W - \theta^B}{1 - \theta^B}$, which equals the expectation of WC84 for equal

sample sizes (Weir and Goudet 2017). For random mating populations, there will be no need

for distinction between β_{ST} and β_{WT} (Weir and Goudet 2017). The moment estimators of

WG population-specific F_{ST} and WC84 are "ratio of averages" estimators; their precision

becomes higher for larger numbers of markers, and unbiased estimates can be obtained (Weir

and Cockerham 1984; Weir and Hill 2002; Bhatia *et al.* 2013). Because "the combined ratio

estimate (ratio of averages) is much less subject to the risk of bias than the separate estimate

(average of ratios)" (Cochran 1977), the population-specific F_{ST} measure is expected to

accurately reflect population history and provide more informative results than analyses using

pairwise F_{ST} values (Weir and Goudet 2017). Compared with these substantial efforts and

progress related to methodological development, however, empirical examples using

population-specific F_{ST} measures, except for limited applications to human populations (*e.g.,*

Nicholson *et al.* 2002; Weir *et al.* 2005; Foll and Gaggiotti 2006; Buckleton *et al.* 2013), have

been sparse. Furthermore, no comparison of population-specific F_{ST} and pairwise F_{ST} using

real data has been reported.

In this study, we characterized current population-specific F_{ST} estimators to infer population

histories and structures using publicly available human, marine fish and plant data sets. We

also compared our results obtained using pairwise F_{ST} and global F_{ST} estimates. Multi-

dimensional scaling (MDS) was applied to pairwise F_{ST} distance matrices to understand

causal mechanisms, such as environmental adaptation of current populations. The human

population data consisted of microsatellite genotypes collected from 51 world populations,

which may be a good example for characterizing these F_{ST} estimators because their

evolutionary history, migration and population structure has been extensively studied and is

well understood (*e.g.*, Diamond 1997; Rosenberg *et al.* 2002; Ramachandran *et al.* 2005; Liu

et al. 2006; Rutherford 2016; Nielsen *et al.* 2017). The SNP data sets were from a

commercially important marine fish, Atlantic cod (*Gadus morhua*) in the North Atlantic, and

from a tree, wild poplar (*Populus trichocarpa*) in the American Pacific Northwest. The

Atlantic cod genotype data included historical samples collected 50–80 years ago as well as

contemporary samples from the northern range margin of the species in Greenland, Norway

and the Baltic Sea. The inclusion of both types of data might facilitate the detection of the

effects of global warming on population structure. The wild poplar samples were collected

under different environmental conditions over an area of 2,500 km near the Canadian–US

border along with various environmental data and are thus possibly useful for the detection of

environmental effects on population structure.

Materials and Methods

Population-specific F_{ST}

We applied WG bias-corrected population-specific F_{ST} moment estimators (Weir and Goudet

2017) in our data analyses:

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$$\mathrm{ps}\widehat{F}_{\mathrm{ST}}^{i} = \frac{\sum_{l=1}^{L}(\widetilde{M}_{W,l}^{i} - \widetilde{M}_{l}^{B})}{\sum_{l=1}^{L}(1 - \widetilde{M}_{l}^{B})} \,, \qquad (1)$$

where $\widetilde{M}_{W}^{i}$ is the unbiased within-population matching of two distinct alleles of population i,

and $\widetilde{M}^{B}$ is the between-population-pair matching average over pairs of populations $i, i^{'}$. We

derived the asymptotic variance of $\mathrm{ps}\widehat{F}_{\mathrm{ST}}^{i}$ over all loci (Supplemental Note).

We also used empirical (Beaumont and Balding 2004) and full Bayesian (Foll and Gaggiotti

2006) population-specific F_{ST} estimators. Beaumont and Balding (2004) maximized the

Dirichlet-multinomial marginal likelihood in their Equation 1 and estimated θ_{li}:

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$$L_{li}\left(\theta_{li}\big|n_{li1}, \dots, n_{lim_l}\right) = \frac{\Gamma(\theta_{li})}{\Gamma(N_{li} + \theta_{li})} \prod_{u=1}^{m_l} \frac{\Gamma(n_{liu} + \theta_{li}\bar{p}_{lu})}{\Gamma(\theta_{li}\bar{p}_{lu})}. \qquad (2)$$

Here, θ_{li} is the scale parameter of the Dirichlet prior distribution for locus l and population i,

$\tilde{p}_{lu}$ is the observed frequency of allele u at locus l, n_{liu} is the observed allele count in

population i, and N_{li} is the total number of alleles. Importantly, $\bar{p}_{lu}$ is the mean allele

frequency over all subpopulations, while $\theta_{li}\bar{p}_{lu} = \alpha_{liu}$, where $\theta_{li} = \sum_{u=1}^{m_l} \alpha_{liu}$. The

parametrization reduces the number of parameters to be estimated ($\theta_{li}, l = 1, \dots L; i =$

$1, \dots, r$). Equation 2 is modeled to estimate locus-population-specific F_{ST} but is basically the

same as the likelihood functions for estimating genetic differentiation and/or global F_{ST}

previously given in Lange (1995), Rannala and Hartigan (1996), Kitada *et al.* (2000), Balding

(2003) and Corander *et al.* (2003). The Dirichlet-multinomial marginal likelihood was also

used for estimating global F_{ST} and linkage disequilibrium (Kitada and Kishino 2004), for

detecting loci with outlier F_{ST} values (Foll and Gaggiotti 2006, 2008), for estimating global

F_{ST} when the number of sampled population is small (Kitakado *et al.* 2006), and for

estimating locus-specific global F_{ST} and posterior distributions of pairwise F_{ST} (Kitada *et al.*

2007). Based on a Dirichlet and/or a beta scale parameter, population-specific F_{ST} values are

estimated for each locus using the following function of $\hat{\theta}_{li}$:

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$$\mathrm{ps}\tilde{F}_{ST,l}^{i} = \frac{1}{\hat{\theta}_{li} + 1}. \qquad (3)$$

216   ***Pairwise F_{ST}***

217   We used Nei and Chesser's (1983) bias-corrected G_{ST} estimator (NC83) for estimating

218 pairwise F_{ST} over loci in our analysis:

$$\text{pw}\widehat{F}_{ST} = \frac{\sum_{l=1}^{L}(\widehat{H}_{T,l} - \widehat{H}_{S,l})}{\sum_{l=1}^{L}\widehat{H}_{T,l}}, \qquad (4)$$

where $\widehat{H}_T$ and $\widehat{H}_S$ are the unbiased estimators of total and within-population heterozygosity,

respectively (Supplemental Note), with each variance component obtained from its moments.

G_{ST} (Nei 1973) is defined "by using the gene frequencies at the present population, so that no

assumption is required about the pedigrees of individuals, selection, and migration in the

past" (Nei 1977). G_{ST} (Nei 1973) assumes no evolutionary history (Holsinger and Weir 2009),

while NC83 does not consider any population replicates (Weir and Cockerham 1984). Our

pairwise F_{ST} values obtained from NC83 therefore measured current population structures

based on a fixed set of samples of subpopulations.

Genome-wide and locus-specific global F$_{ST}$

230 We used Weir and Cockerham's (1984) θ (WC84) for estimating global F_{ST} over all loci

231 (genome-wide F_{ST}) as given by Equation 10 in the original study:

$$\theta_{WC} = \frac{\sum_{l=1}^{L}\sum_{u=1}^{m} a_{lu}}{\sum_{l=1}^{L}\sum_{u=1}^{m}(a_{lu} + b_{lu} + c_{lu})}. \qquad (5)$$

This equation is the ratio of the observed variance components for an allele: *a* for between

subpopulations, *b* for between individuals within subpopulations, and *c* for between gametes

within individuals. Each variance component is an unbiased estimator obtained with the

corresponding method of moment estimation (Supplemental Note). The WC84 moment

estimator of F_{ST} assumes that populations of the same size have descended separately from a

single "ancestral population" that was in both Hardy–Weinberg and linkage equilibrium (Weir

and Cockerham 1984). The statistical model of WC84 regards the sampled set of

subpopulations as having been taken from an ancestral population and considers replicates of

samples. This model also assumes that each population has the same population-specific F_{ST}

derived from the ancestral population (Weir and Hill 2002; Weir and Goudet 2017); it

therefore estimates the mean F_{ST} over subpopulations in terms of the coancestry coefficient

(global F_{ST}). The asymptotic variance of θ_{WC} over all loci was derived in a similar fashion

as that of WG population-specific F_{ST} ($ps\hat{F}_{ST}^i$) as given in Supplemental Note.

A maximum likelihood estimator of a Dirichlet or beta scale parameter θ_l was used to

estimate locus-specific global F_{ST} values using Equation 1 in Kitada et al. (2007):

$$\text{global}\hat{F}_{ST,l} = \frac{1}{\hat{\theta}_l + 1} . \qquad (6)$$

Throughout this paper, we use notations consistent with those of Weir and Hill (2002): i for

populations ($i = 1, \ldots, r$), u for alleles ($u = 1, \ldots, m$) and l for loci ($l = 1, \ldots, L$).

Empirical data

Human microsatellite data: The data in Rosenberg *et al.* (2002) were retrieved from

https://web.stanford.edu/group/rosenberglab/index.html. We removed the Surui sample

(Brazil) from the data because that population was reduced to 34 individuals in 1961 as a

result of introduced diseases (Liu *et al.* 2006). We retained genotype data ($n = 1,035$) of 377

microsatellite loci from 51 populations categorized into six groups as in the original study: 6

populations from Africa, 12 from the Middle East and Europe, 9 from Central/South Asia, 18

from East Asia, 2 from Oceania and 4 from America. Longitudes and latitudes of the sampling

sites were obtained from Cann *et al.* (2002) (Supplemental Data).

Atlantic cod SNP data: The genotype data of 924 markers common to 29 populations

reported in Therkildsen *et al.* (2013a, b) and 12 populations in Hemmer-Hansen *et al.* (2013a,

b) were combined. We compared genotypes associated with each marker in samples that were

identical between the two studies, namely, CAN08 and Western_Atlantic_2008, ISO02 and

Iceland_migratory_2002, and ISC02 and Iceland_stationary_2002, and standardized the gene

codes. We removed cgpGmo.S1035, whose genotypes were inconsistent between the two

studies. We also removed cgpGmo.S1408 and cgpGmo.S893, for which genotypes were

missing in several population samples in Therkildsen *et al*. (2013b). Temporal replicates in

Norway migratory, Norway stationary, North Sea and Baltic Sea samples were removed for

simplicity. The final data set consisted of genotype data ($n = 1,065$) at 921 SNPs from 34

populations: 3 from Iceland, 25 from Greenland, 3 from Norway and 1 each from Canada, the

North Sea and the Baltic Sea. Two ecotypes (migratory and stationary) that were able to

interbreed but were genetically differentiated (Hemmer-Hansen *et al*. 2013a; Berg *et al*. 2016)

were included in the Norway and Iceland samples. All individuals in the samples were adults,

and most were mature (Therkildsen *et al*. 2013a). The longitudes and latitudes of the sampling

sites in Hemmer-Hansen *et al*. (2013a) were used. For the data from Therkildsen *et al*.

(2013a), approximate sampling points were estimated from the map of the original study, and

longitudes and latitudes were recorded (Supplemental Data).

Wild poplar SNP data: Environmental/geographical data and genotype data were retrieved

from the original studies of McKown *et al*. (2014a, b). The genotype data contained 29,355

SNPs of 3,518 genes of wild poplar ($n = 441$) collected from 25 drainage areas (McKown *et*

al. 2014c). Details of array development and selection of SNPs are provided in Geraldes et al.

(2011, 2013). The samples covered various regions over a range of 2,500 km near the

Canadian–US border at altitudes between 0 and 800 m (Supplemental Data). A breakdown of

the 25 drainages (hereafter, subpopulations) is as follows: 9 in northern British Colombia

(NBC), 2 in inland British Colombia (IBC), 12 in southern British Colombia (SBC) and 2 in

Oregon (ORE) (Geraldes *et al.* 2014). The original names of clusters and population numbers

were combined and used for our population labels (NBC1, NBC3,…, ORE30). Each sampling

location was associated with 11 environmental/geographical parameters: latitude (lat),

longitude (lon), altitude (alt), longest day length (DAY), frost-free days (FFD), mean annual

temperature (MAT), mean warmest month temperature (MWMT), mean annual precipitation

(MAP), mean summer precipitation (MSP), annual heat-moisture index (AHM) and summer

heat-moisture index (SHM) (Supplemental Data). The annual heat-moisture index was

calculated in the original study as (MAT+10)/(MAP/1000). A large heat-moisture index

indicates strong drying.

Data analysis

Implementation of F_{ST} estimators: We converted the genotype data into Genepop format

(Raymond and Rousset 1995; Rousset 2008) for implementation in the R package

FinePop2_ver.0.2 (Nakamichi *et al.* 2020). Expected heterozygosity was calculated for each

population with the `read.GENEPOP` function. WG population-specific F_{ST} (Equation 1)

values over all loci were computed using the `pop_specificFST` function. Because WG

population-specific F_{ST} is a linear function of $\widehat{H}_{Si}$ with an intercept of 1 given $\widehat{H}_T$ (Equation

7 in Discussion), we examined the linear relationship between expected heterozygosity (*He*)

and population-specific F_{ST} estimates using the `lm` function in R. In addition to the "ratio of

averages" (Weir and Cockerham 1984; Weir and Hill 2002) used in the F_{ST} function, we

computed the "average of ratios" (Bhatia *et al.* 2013) of the WG population-specific F_{ST} of

the human data for comparison. We maximized Equation 2 and estimated Beaumont and

Balding's population-specific F_{ST} at each locus according to Equation 3. We then averaged

these values over all loci. For the full Bayesian model (Foll and Gaggiotti 2006), GESTE_ver.

2.0 was used to compute population-specific F_{ST} values. Pairwise F_{ST} values (NC83, Equation

4) were computed using the `pop_pairwiseFST` function. Global F_{ST} values over all loci

(genome-wide global F_{ST}) were computed using the `globalFST` function (WC84, Equation

5). In addition, maximum-likelihood locus-specific global F_{ST} values (Equation 6) were

estimated using the `locus_specificFST` function.

Visualization of population structure: All analyses were performed in R. We drew

dendrograms based on pairwise F_{ST} values using the `hclust` function. Sampling points

based on longitudes and latitudes were located on maps using the `sf` package. The size of

each sampling point was drawn to be proportional to the expected heterozygosity, and the

same colors were used as those of the clusters in the dendrograms. Sampling points with

pairwise F_{ST} values smaller than a given threshold were connected by lines to visualize gene

flow between populations. Multi-dimensional scaling (MDS) was applied on pairwise F_{ST}

distance matrices to translate the information into a set of coordinates (axes) using the

`cmdscale` function. As an explained variation measure, we used the cumulative contribution

ratio up to the kth axis $(j = 1, ..., k, ..., K)$, which was computed in the function as $C_k =$

$\sum_{j=1}^{k} \lambda_j / \sum_{j=1}^{K} \lambda_j$, where λ_j is the eigenvalue and $\lambda_j = 0\ if\ \lambda_j < 0$. The signs of MDS values

of coordinates were reversed to be consistent with WG population-specific F_{ST} values.

Population-specific F_{ST} values for each sampling point were visualized by color gradients

based on rgb $(1 - F_{ST,0}, 0, F_{ST,0})$, where $F_{ST,0} = (F_{ST} - \min F_{ST})/(\max F_{ST} - \min F_{ST})$. This

conversion represents the magnitude of a population-specific F_{ST} value at the sampling point

in colors between blue (for the largest F_{ST}) and red (smallest F_{ST} = closest to the coancestral

population).

__Effect of environment on population structure__: We inferred the effect of environmental and geographical variables on population-specific F_{ST} and MDS axes of the pairwise F_{ST} values using a linear regression with the `lm` function. This analysis was only performed on the wild poplar data sets, for which 11 environmental/geographical parameters were associated with each sampling location.

Data availability

The authors affirm that all data necessary for confirming the conclusions of the article are present within the article, figures, tables, and supplemental information. Supplemental material available at figshare: ###. The R package for computing the F_{ST} estimators used in this paper is available in the FinePop2_ver.0.2 package at CRAN (https://CRAN.R-project.org/package=FinePop).

Results

Genome-wide and locus-specific global F_{ST}

The global F_{ST} estimate ± standard error (SE) was unexpectedly similar for the three cases. The estimate was 0.0488 ± 0.0012 for humans with a coefficient of variation (CV) of 0.025. The value for Atlantic cod, 0.0424 ± 0.0026 (CV=0.061), was slightly lower than that of human populations. The lowest global F_{ST} estimate was for wild poplar, 0.0415 ± 0.0002 (CV = 0.005), which was slightly lower than the estimate for Atlantic cod. The maximum likelihood estimator of locus-specific global F_{ST} generated positive F_{ST} values for all loci, and the mean of locus-specific global F_{ST} values ± SE was similar to global F_{ST} values: 0.0423 ± 0.0010 (CV = 0.024) for humans, 0.0390 ± 0.0018 (CV = 0.047) for Atlantic cod and 0.0431

± 0.0002 (CV = 0.004) for wild poplar.

Human

Population-specific F_{ST}: WG population-specific F_{ST} values were smallest in Africa (Figure

1A; Supplemental Data). Interestingly, Bantu Kenyans were associated with the smallest

value in Africa, while the San population, located in southern Africa, had the largest (Figure

S1). In Central/South Asia, the F_{ST} value closest to Africa was that of the Makrani, followed

by Sindhi, Balochi, Pathan and Brahui. Three samples from Uyghur, Hazara and Burusho

populations, which are the nearest to East Asia in terms of location, had the largest F_{ST} values.

The Kalash were isolated from other Central/South Asia populations. In the Middle East, the

closest population to Africa was Mozabite, followed by Palestinian and Bedouin. In Europe,

Adygean, Tuscan, Russian and French populations had similar F_{ST} values, and the largest

were those of Italians, Sardinians, Druze, Orcadians and Basques. In East Asia, the Xibo had

the smallest F_{ST} value, while She and Lahu populations were closest to Papuans and

Melanesians and had the largest F_{ST} values. In America, Mayans possessed the smallest F_{ST}

and the Karitiana the largest. Expected heterozygosity was highest in Africa and lowest in

South America (Figure 1A). The linear regression of population-specific F_{ST} on expected

heterozygosity was highly significant: $y = -0.1895x + 0.8908$ ($R^2 = 0.91, F =$

$501.8\ (1\,, 49\text{DF}), P < 2.2 \times 10^{-16}$).

As shown on the map in Figure 2A, visualization of human population history based on the

WG population-specific F_{ST} estimator indicated that populations in Africa had the smallest

F_{ST} values (shown in red), followed by the Middle East, Central/South Asia, Europe and East

Asia. The pattern in Oceania was similar to East Asia, but America was much different. As

illustrated by sampling point radii, heterozygosity was high in Africa, the Middle East,

Central/South Asia, Europe and East Asia but relatively small in Oceania and America. The

Kalash were less heterozygous than other populations in Central/South Asia. The Karitiana in

Brazil had the lowest heterozygosity. Bayesian population-specific F_{ST} values estimated using

the methods of Beaumont and Balding (2004) and Foll and Gaggiotti (2006) were nearly

identical, but in African populations they were higher than WG population-specific F_{ST}

(Figure S2). The distributions of F_{ST} values obtained from the two Bayesian methods were

very similar, with the smallest F_{ST} values observed in the Middle East, Europe and

Central/South Asia (Figure 2B, C; Supplemental Data). The "ratio of averages" and "average

of ratios" of the WG population-specific F_{ST} estimator were almost identical in all populations

for this data set (Figure S3).

Pairwise F_{ST}: On the basis of pairwise F_{ST} values, the populations were divided into five

clusters: 1) Africa, 2) the Middle East, Europe and Central/South Asia, 3) East Asia, 4)

Oceania and 5) America (Figure 1B). As indicated by sampling points with F_{ST} values below

the 0.02 threshold (connected by yellow lines in Figure 1C), gene flow from Africa was low.

Gene flow was substantial within Eurasia but was much smaller than that inferred from that

continent to Oceania and America (Figure 1C).

The first axis of MDS of pairwise F_{ST} exhibited a similar pattern to that of population-specific

F_{ST} values, with populations divided into five clusters (Figure 2D) as in the dendrogram

(Figure 1B). The second axis identified Caucasian and Mongoloid populations and indicated

close relationships between East Asia and Oceania (Figure 2E). The third axis uncovered

similarities among Europe, the Middle East, Central/South Asia, Central America and Oceania

and between Africa and South America (the Karitiana in Brazil) (Figure 2F). The contribution

of the first axis was 44% ($C_1 = 0.44$), and 72% of the variation in the pairwise F_{ST} distance

matrix was explained by the first, second and third axes of pairwise F_{ST} ($C_3 = 0.72$) (Figure

S4A; Supplemental Data). The first axis of pairwise F_{ST} was significantly positively

correlated with the population-specific F_{ST} values ($r = 0.85, t = 11.4, P = 2.22 \times 10^{-15}$),

indicating the distance from Africa for each population, but no other axes exhibited any

correlation (Figures 3A and S4B). The second axis divided populations in East Asia and

Oceania from the others, while the third axis characterized three groups: 1) Africa and the

Karitiana, 2) East Asia and 3) the Middle East, Europe, Central/South Asia and Oceania

(Figure 3B). The Kalash population was still isolated.

Atlantic cod

Population-specific F_{ST}: The lowest WG population-specific F_{ST} value was in Canada

(Figures 4A and S5; Supplemental Data). Greenland west-coast populations (in green in

Figure 4A) generally had small F_{ST} values. Fjord populations (in deep purple) had relatively

higher F_{ST} values. Population PAA08 on the southwestern coast of Greenland, INC02 and

TAS10 in Iceland, and the stationary types ICEsta02 and NORsta09 in Norway had larger F_{ST}

values (in magenta). Population-specific F_{ST} values were much higher for offshore samples

OSO10/OEA10 and migratory types ICEmig02, NORmig (feed)09 and NORmig (spawn)09

(in orange). The F_{ST} value for NOS07 from the North Sea was smaller than those of the

migratory type, the highest of which was for BAS0607 from the Baltic Sea (in cyan).

Expected heterozygosity was the highest in Canada and the lowest in the Baltic Sea (Figure

4A). The linear regression of population-specific F_{ST} on expected heterozygosity was highly

significant: $y = -3.397x + 1.004$ ($R^2 = 0.998, F = 20250\ (1\,, 32DF), P < 2.2 \times 10^{-16}$).

The evolutionary history of Atlantic cod populations was clearly visualized on a map using

WG population-specific F_{ST} values (Figure 5A). Heterozygosity (indicated by circle radii)

was very high in Canada and Greenland, low in other areas and lowest in the Baltic Sea.

Pairwise F_{ST}: The populations were divided according to pairwise F_{ST} values into four large

clusters: 1) Canada, 2) Greenland west coast, 3) Greenland east coast, Iceland and Norway,

and 4) North and Baltic seas. Fjord populations formed a sub-cluster within the Greenland

west coast, and migratory and stationary ecotypes also formed a sub-cluster (Figure 4B). On

the basis of pairwise F_{ST} values between sampling points (< 0.02 threshold), substantial gene

flow was detected between Greenland, Iceland and Norway. In contrast, gene flow was low

from Canada and to North and Baltic seas (Figure 4C).

The first axis of pairwise F_{ST} ($C_1 = 0.72$) was significantly correlated with population-

specific F_{ST} values ($r = 0.86, t = 9.4, P = 9.55 \times 10^{-11}$) (Figure S6; Supplemental Data)

and revealed patterns of population structure that were very similar to those inferred from

population-specific F_{ST} values (Figure 5B). The first axis indicated the distance of each

population from Canada (Figure 6A). The second axis of pairwise F_{ST} values, which exhibited

a weak but significant correlation with population-specific F_{ST} values ($r = 0.35, t = 2.2, P =$

0.04), revealed different patterns of population differentiation (Figure 5C). This axis

recognized the migratory ecotypes and also separated out southern Canadian, North Sea and

Baltic Sea populations (Figure 6B). The cumulative contribution of the first and second axes

was 94% ($C_2 = 0.92$). Other axes of pairwise F_{ST} were uncorrelated with population-specific

F_{ST} values (Figure S6).

Wild poplar

Population-specific F_{ST}: Wild-poplar population-specific F_{ST} values were lowest in SBC27, SBC26, IBC15, IBC16 and ORE29 (Figure 7A; Supplemental Data). Samples collected from areas close to the SBC coast had higher population-specific F_{ST} values than other SBC samples. Samples SBC23, SBC24 and especially SBC22 had much higher population-specific F_{ST} values. NBC samples had population-specific F_{ST} values similar to those of the SBC ones. Among NBC samples, NBC8 had the smallest population-specific F_{ST}, and NBC5 had the highest value, followed by NBC6 and NBC7. The population represented by sample ORE30 was isolated from ORE2. Expected heterozygosity was highest in SBC27 and lowest in NBC5. The linear regression of population-specific F_{ST} on expected heterozygosity was highly significant: $y = -1.872x + 0.629$ ($R^2 = 0.82, F = 108$ (1 ,23DF), $P < 3.5 \times 10^{-10}$), but the variation in population-specific F_{ST} values was much larger than those observed in humans and Atlantic cod. WG population-specific F_{ST}-based map visualization of wild-poplar evolutionary history (Figure 8A) revealed that IBC15, IBC16 SBC27, SBC26 and ORE29 had relatively small F_{ST} values and large heterozygosities, while NBC5, NBC6 and SBC22 had the largest F_{ST} values and lowest heterozygosities.

Pairwise F_{ST}: On the basis of pairwise F_{ST} values, the populations were divided into three large clusters: 1) SBC, 2) NBC5, 6 and 7, and 3) NBC and IBC (Figure 7B). ORE samples, however, were nested in the third cluster; in this cluster, the ORE29 sample was closely tied to IBC15 and IBC15, while ORE30 was isolated. As inferred by pairwise F_{ST} values between sampling points connected by yellow lines (< 0.02 threshold) in Figure 7C, substantial gene flow was observed among populations (Figure 7C).

The first axis of pairwise F_{ST} uncovered slightly different patterns of population

differentiation (Figure 8B), which highlighted the dissimilarity between NBC5 and NBC6 (in

blue) and SBC22 (in red). The contribution of the first axis of pairwise F_{ST} was 47% ($C_1 =$

0.47) and had no significant correlation with population-specific F_{ST} values ($r = 0.33, t =$

1.7, $P = 0.108$) (Figure S7; Supplemental Data). The contribution of the second axis of

pairwise F_{ST} was 23% ($C_2 = 0.71$), and no correlation was likewise detected with population-

specific F_{ST} values ($r = 0.36, t = 1.8, P = 0.08$). The second axis strongly differentiated

ORE30 (in red) and SBC22 (in blue) (Figure 8C). The relationship between population-

specific F_{ST} and the first axis of pairwise F_{ST} was not linear, with expansion indicated in two

directions from inner areas: to the coast and to northern areas (Figure 9A). In the plot of the

second axis vs. the first axis of pairwise F_{ST}, ORE30 and SBC22 were distinct and located in

opposite regions of the graph (Figure 9B). The first axis of pairwise F_{ST} was positively

correlated with DAY (Figure 9C). The second axis, however, was negatively correlated with

SHM (Figure 9D), with SBC19 and SBC22 experiencing the wettest environment and ORE30

subjected to the driest conditions in the summer.

Effect of environment on population structure: To avoid multicollinearity, we excluded 7 out

of 11 environmental variables that were significantly correlated with each other, namely, lon,

alt, FFD, MWMT, MSP and AHM. Linear regression of population-specific F_{ST} values on the

four environmental variables (DAY, MAT, MAP and SHM) indicated that DAY, MAP and

SHM were significant (Table 1). DAY was also positive and significant on the first axis of

pairwise F_{ST}, and SHM was significantly negative on the second axis of pairwise F_{ST}. No

significant variable was found on the third axis.

 CPU times

Using a laptop computer with an Intel Core i7-8650U CPU, only 89.8 s of CPU time were

required to compute WG population-specific F_{ST} estimates and SEs of wild poplar (29,355

SNPs; 25 populations, $n = 441$). Only 13.3 s were needed to compute maximum-likelihood

global F_{ST}, with 120.7 s required to obtain pairwise F_{ST} (NC83) between all pairs and 178.5

seconds for genome-wide global F_{ST} with SE (WC84).

Discussion

Global F_{ST} measures species divergence

Interestingly, the global F_{ST} estimate of WC84 was similar for the three species: $0.0488 \pm$

0.0012 (CV = 0.025), 0.0424 ± 0.0026 (CV = 0.061) and 0.0415 ± 0.0002 (CV = 0.005) for

human (377 microsatellite loci), Atlantic cod (921 SNPs) and wild poplar (29,355 SNPs)

populations, respectively. The highest global F_{ST} was that of humans. The rate of human gene

flow ($\theta = \frac{1}{F_{ST}} - 1$, Supplemental Note) was estimated to be 20, thus indicating that 20

effective individuals migrated per generation between subpopulations. Because this global F_{ST}

estimate was inferred using neutral microsatellite markers, it should reflect the random mating

history of humans within and between populations, such as from migration events (Diamond

1997; Rutherford 2016; Nielsen *et al.* 2017). The lowest global F_{ST} was that of wild poplar.

The species had an estimated gene flow rate of 23, which might be due to wind pollination

and/or fluffy seeds being carried by the wind. This gene flow rate was almost the same as that

of Atlantic cod, a migratory marine fish in which long-distance natal homing (>1,000 km)

over 60 years has been documented in the North Atlantic (Bonanomi *et al.* 2016).

The WC84 moment estimator of global F_{ST} is an unweighted average of population-specific

F_{ST} values (Weir and Goudet 2017). Therefore, genome-wide global F_{ST} would be a measure

of a species' genetic divergence, which reflects its evolutionary history. Atlantic cod may have

colonized the waters around Iceland and Norway following the last glacial maximum (LGM;

21 thousand years [kyr] ago) (Kettle *et al.* 2011; Hemmer-Hansen *et al*. 2013a). Wild poplar,

inferred to have been extensively distributed in coastal areas from southern California to

northern Alaska in the last interglacial (LIG; 135 kyr ago), was reduced to British Columbia,

Washington, Oregon and California in the LGM and then expanded to its current distribution

range of southern California to northern Alaska (Levsen *et al.* 2012). This scenario suggests

that our global F_{ST} value for wild poplar based on samples taken from British Columbia and

Oregon reflects population history after LGM, which coincides with the colonization date of

Atlantic cod in Iceland and Norway. For humans, the HapMap unweighted average of

population-specific F_{ST} values over all populations, estimated from 599,356 SNPs, was 0.13

(Weir *et al.* 2005). The earliest-known fossils of anatomically modern humans provide

evidence that modern humans originated in Ethiopia approximately 150–190 kyr ago and

appeared approximately 100 kyr ago in the Middle East and approximately 80 kyr ago in

southern China (reviewed by Nielsen et al. 2017). The genome-wide global F_{ST} value for

humans was three times greater than those of Atlantic cod and wild poplar, thus implying that

humans originated in Africa approximately 63 kyr ago ($= 21 \times 3$). This suggested timing is in

agreement with the best estimate of Liu *et al.* (2006), who inferred that humans initially

expanded 56 kyr ago from a small founding population of 1,000 effective individuals.

Population-specific F_{ST} traces population history as reflected by genetic

diversity

A linear relationship between heterozygosity and WG population-specific F_{ST} was evident in

our case studies (Figures 1A, 4A, 7A). The coefficient of determination, R^2, was 0.91 for 51

human populations (n = 1,035), 0.993 for 34 Atlantic cod populations (n = 1,065) and 0.82 for

25 wild poplar populations (n = 441). The goodness of fit to the linear function should depend

on population sample size (number of individuals). Our results from the three case studies

demonstrate that the population-specific F_{ST} estimator traces population history by way of

population genetic diversity.

In our analysis, WG population-specific F_{ST} clearly indicated that humans originated in

Africa, expanded from the Middle East into Europe and from Central/South Asia into East

Asia, and then possibly migrated to Oceania and America (Figures 1, 2). These results are in

good agreement with the highest levels of genetic diversity being detected in Africa

(Rosenberg *et al.* 2002), the relationship uncovered between genetic and geographic distance

(Ramachandran *et al.* 2005), the shortest colonization route from East Africa (Liu *et al.* 2006)

and major migrations inferred from genomic data (Nielsen *et al.* 2017). Our estimates of WG

population-specific F_{ST} values are consistent with results obtained from 24 forensic STR

markers (Buckleton *et al.* 2016) and successfully illustrate human evolutionary history.

The evolutionary history of Atlantic cod was also clearly visualized using WG population-

specific F_{ST} values (Figures 4A,5A). Our analysis indicated that Atlantic cod originated in

Canada (CAN08) and first expanded to the west coast of Greenland before spreading to

Iceland, the North Sea, Norway and the Baltic Sea. The migratory ecotypes may have played

an important role in this expansion. In the original Atlantic cod study (Therkildsen *et al.*

2013a), strong differentiation of CAN08 was found at neutral markers, which prompted the

authors to suggest that Greenland populations were the result of colonization from Iceland

rather than from refugial populations in southern North America. In our study, CAN08 had the

highest expected heterozygosity, which was lower in Iceland than in Greenland (Figure 4A);

this result implies that Icelandic populations were the descendants of colonists from

Greenland, which in turn originated in Canada. The BAS0607 sample from the Baltic Sea had

the highest population-specific F_{ST} and the lowest heterozygosity values, which suggests that

Baltic cod is the newest population. This result agrees with the findings of a previous study,

which identified Baltic cod as an example of a species subject to ongoing selection for

reproductive success in a low salinity environment (Berg et al. 2015).

The samples used in this study did not cover the whole distribution range of wild poplar,

which extends from southern California to northern Alaska. Population-specific F_{ST} values

suggested that wild poplar trees in southern British Colombia (SBC26, 27), inland British

Colombia (IBC15, 16) and Oregon (ORE29) are the closest to the ancestral population, which

later expanded in three directions: to coastal British Colombia (SBC; rainy summers),

southern Oregon (ORE30; mostly dry summers) and northern British Colombia (NBC; long

periods of daylight) (Figures 7A, 8A). The fact that the largest population-specific F_{ST} value

was found in the population with the smallest heterozygosity, SBC22, may be due to a

bottleneck (Geraldes *et al.* 2014).

The first axis of pairwise F_{ST} reflects population history

Our results reveal that the first axis of pairwise F_{ST} reflects population history. The population

structure estimated for humans (Figure 1B) is in good agreement with that of the original

study (Rosenberg *et al.* 2002). MDS of the pairwise F_{ST} matrix decomposed the current

600 population structure into several independent axes. The first axis of pairwise F_{ST} was

601 significantly correlated with population-specific F_{ST} values ($r = 0.85$), with 72% ($R^2 = 0.72$)

602 of the variation in the current differentiation of the human population explained by their

603 evolutionary history (Figures 2D, 3A).

605 The first axis of pairwise F_{ST} of Atlantic cod was also significantly correlated with

606 population-specific F_{ST} values ($r = 0.86$), with 74% of the variation in the current

607 differentiation explained by the evolutionary history (Figures 5B, 6A). In contrast, the first

608 axis of pairwise F_{ST} of wild poplar was not significantly correlated with population-specific

609 F_{ST} ($r = 0.33$), and population expansion in two directions was detected from inner areas: to

610 the coast and to northern areas (Figure 9A). The first axis of pairwise F_{ST} was related to DAY,

611 the primary evolutionary factor in wild poplar. This result is consistent with the F_{ST} outlier

612 test of the original study (Geraldes et al. 2014), in which Bayescan (Foll and Gaggiotti 2008)

613 revealed that genes involved in circadian rhythm and response to red/far-red light had high

614 locus-specific global F_{ST} values. Moreover, the first principal component of SNP allele

615 frequencies was significantly correlated with daylength, and a previous enrichment analysis

616 for population structuring uncovered genes related to circadian rhythm and photoperiod

617 (McKown *et al*. 2014a). Our regression analysis of wild poplar revealed that long daylight,

618 abundant rainfall and dry summer conditions are the key environmental factors influencing

619 the evolution of this species (Table 1), thereby supporting the results obtained from

620 population-specific and pairwise F_{ST} values. Among our three case studies, wild poplar had

621 the lowest global F_{ST} and thus the highest gene flow. Since plants cannot move, this situation

622 may be due to wind pollination and/or wind transport of seeds, whose fates depend on the

623 environment in which they land.

Subsequent axes of pairwise F_{ST} reflect migration, languages, environmental effects and species specificity

In humans, the second axis distinguished Caucasian and Mongoloid populations (Figure 2E); it also revealed close relationships between populations in East Asia and Oceania, consistent with an expansion from Asia into Polynesia and Micronesia (Diamond 1997). Descendants of Chinese agriculturalists first spread from the islands of New Guinea to the east 3,600 years ago and became the ancestors of modern Polynesians (Diamond 1997). The third axis uncovered similarities among populations in Europe, the Middle East, Central/South Asia, Central America and Oceania and between Africa and South America (Figure 2F). East Asian populations were distinct from other populations. The Kalash population, separated in the third axis (Figure 3B), lives in isolation in the highlands of northwestern Pakistan and comprises approximately 4,000 individuals (Rutherford 2016) speaking an Indo-European language (Rosenberg *et al.* 2002). The Khoisan-speaking San population, located at the opposite end of the third axis in the plot, was separated from other African populations, who speak Niger–Congo languages (Diamond 1997). Our result agrees with the previously uncovered population genetic structure that is consistent with language classifications in Africa (Tishkoff *et al.* 2009). Papuan and Melanesian populations from Papua New Guinea, where the official language is English, had values similar to those of European populations. Portuguese is the major language in Brazil (Karitiana), whereas Spanish predominates in Colombia (Colombian) and Mexico (Maya and Pima). The third axis should reflect languages, which is a consequence of migration events in the early modern period, such as during the Age of Discovery (*e.g.*, Diamond 1997; Rutherford 2016).

In Atlantic cod, the second axis of pairwise F_{ST} had a weak but significant correlation with

population-specific F_{ST} values ($r = 0.35, t = 2.2, P = 0.04$) and exhibited different patterns

of population differentiation (Figure 5C). This axis separated out the migratory ecotype and

separated southern Canadian, North Sea and Baltic Sea populations at the opposite end

(Figure 6B). This placement of southern Canadian, North Sea and Baltic Sea populations

apart from the northern populations (Figure 6B) suggests that central distribution areas arose

to the north because of global warming, with the southern populations then becoming

isolated. Our result is in agreement with the results of an earlier study that identified parallel

temperature-associated clines in the allele frequencies of 40 of 1,641 gene-associated SNPs of

Atlantic cod in the eastern and western North Atlantic (Bradbury *et al.* 2010).

In wild poplar, the second axis of pairwise F_{ST} values was related to SHM gradients (summer

humidity) (Figure 9D), which suggests that precipitation, in addition to daylight detected by

the first axis, is a key factor in the current population structuring of wild poplar. In a previous

study, genes involved in drought response were identified as F_{ST} outliers along with other

genes related to transcriptional regulation and nutrient uptake (Geraldes et al. 2014), a finding

consistent with the results of our regression analysis (Table 1).

Properties of F_{ST} estimators

Ratio of averages: In regard to the WG population-specific F_{ST} estimator, similar results were

obtained for the human data using either the "ratio of averages" or the "average of ratios"

(Figure S3). These similar outcomes may have been due to the relatively small variation in the

locus-specific global F_{ST} values of human microsatellites. The highest precision, which was

dependent on the number of markers, was obtained for wild poplar. These results are in

agreement with previous studies that have suggested or indicated that the "ratio of averages"

works better than the "average of ratios" (Cochran 1977; Weir and Cockerham 1984; Weir and

Hill 2002; Bhatia et al. 2013).

To show the underlying mechanism, we use the observed heterozygosity of population i as

derived in Nei and Chesser (1983) (Supplemental Note). When the number of loci (L)

increases, the average observed heterozygosity over all loci converges to its expected value

according to the law of large numbers as

680
$$\frac{1}{L}\sum_{l=1}^{L}\left(1-\sum_{u=1}^{m}\tilde{p}_{iu}^2\right)\rightarrow\frac{1}{L}\sum_{l=1}^{L}\left(1-E\left[\sum_{u=1}^{m}\tilde{p}_{iu}^2\right]\right).$$

681 The observed gene diversity thus converges to the expected value:

682
$$\widehat{H}_{Si}=\widehat{H}_{Si}\left(1-\frac{1}{n_i}\right)+\frac{\widehat{H}_{0i}}{2n_i}\quad\rightarrow H_{Si}\left(1-\frac{1}{n_i}\right)+\frac{H_{0i}}{2n_i}.$$

In the same way, $\widehat{H}_S$ and $\widehat{H}_T$ converge to their expected values. This example indicates that

the numerators and denominators of bias-corrected F_{ST} moment estimators, whether global,

pairwise or population-specific, converge to their true means and provide unbiased estimates

of F_{ST} in population genomics analyses with large numbers of SNPs. Our analyses

demonstrate that genomic data highlight the usefulness of the bias-corrected moment

estimators of F_{ST} developed in the early1980s (Nei and Chesser 1983; Weir and Cockerham

1984).

Global F_{ST}: We used the WC84 moment estimator to estimate global F_{ST}. This bias-corrected

moment estimator considers replicates of a set of population samples and is an unweighted

average of population-specific F_{ST} values (Weir and Goudet 2017). Given a large number of

loci in a genome, bias-corrected moment estimators of genome-wide F_{ST} ("ratio of averages")

enable reliable estimation of current population structure underpinned with evolutionary

history. For estimating locus-specific global F_{ST} values, maximum likelihood and Bayesian

estimators improve the power to detect genes under environmental selection because of the

shrinkage of allele frequencies toward the mean.

Pairwise F_{ST}: For estimation of pairwise F_{ST}, our previous coalescent simulations based on

ms (Hudson 2002) showed that NC83 performs best, among present F_{ST} estimators, for cases

with 10,000 SNPs (Kitada *et al.* 2017). Other F_{ST} moment estimators within an ANOVA

framework produce values approximately double those of true values. NC83 considers a fixed

set of population samples; in contrast, the other moment F_{ST} estimators consider replicates of

a set of populations (Weir and Cockerham 1984; Holsinger and Weir 2009), which causes the

over-estimation of pairwise F_{ST} (Kitada *et al.* 2017). Our empirical Bayes pairwise F_{ST}

estimator (EBF_{ST}; Kitada *et al.* 2007), which is also based on Equation 2, suffers from a

shrinkage effect similar to that of Bayesian population-specific F_{ST} estimators. EBF_{ST} is only

useful in cases involving a relatively small number of polymorphic marker loci, such as

microsatellites; it performs best by averaging the large sampling variation in allele

frequencies of populations with small sample sizes, particularly in high gene flow scenarios

(Kitada *et al.* 2017). We note, however, that the shrinkage effect on allele frequencies

enhances the bias of EBF_{ST} and other Bayesian F_{ST} estimators, particularly in genome

analyses (SNPs).

Population-specific F_{ST}: The WG population-specific F_{ST} moment estimator measures

population genetic diversity under the framework of relatedness of individuals and identifies

the population with the largest genetic diversity as the ancestral population. This estimator

thus works to infer evolutionary history through genetic diversity. The WG population-

specific F_{ST} estimator is based on allele matching probabilities, where within-population

observed heterozygosity can be written as $1 - \widetilde{M}_W^i$. When Hardy–Weinberg equilibrium is

assumed ($\widehat{H}_{0i} = \widehat{H}_{Si}$), the preceding formula is equivalent to the NC83 unbiased estimator of

the gene diversity of population i $\left(\widehat{H}_{Si}\right)$ (Supplemental Note):

724
$$1 - \widetilde{M}_W^i = \frac{2n_i}{2n_i - 1}\left(1 - \sum_{u=1}^{m} \tilde{p}_{iu}^2\right) = \widehat{H}_{Si}.$$

725   Another variable, $\widetilde{M}^B$, is total homozygosity in terms of paired matching of alleles over all

726   populations. The definition of WG population-specific F_{ST} is

727
$$psF_{ST}^i = \beta_{WT}^i = \frac{\theta_W^i - \theta^B}{1 - \theta^B}$$

728   and the estimator is

729
$$ps\widehat{F}_{ST}^i = \hat{\beta}_{WT}^i = \frac{\widetilde{M}_w^i - \widetilde{M}^B}{1 - \widetilde{M}^B}.$$

730   Weir and Goudet (2017) showed that $E[\hat{\beta}_{WT}^i] = \hat{\beta}_{WT}^i$ and that θ^B is the average of

731   identical-by-descent (ibd) probabilities of alleles from different populations. We may

732   therefore write $1 - \widetilde{M}^B = \widehat{H}_T$. When working with allele frequencies, the population-specific

733   F_{ST} estimator can be written in terms of Nei's gene diversity as

734
$$ps\widehat{F}_{ST}^i = \frac{\widetilde{M}_w^i - \widetilde{M}^B}{1 - \widetilde{M}^B} = \frac{\widehat{H}_T - \widehat{H}_{Si}}{\widehat{H}_T} = 1 - \frac{\widehat{H}_{Si}}{\widehat{H}_T}. \quad (7)$$

735   This formulation is reasonable, since WG population-specific F_{ST} uses "allele matching,

736   equivalent to homozygosity and complementary to heterozygosity as used by Nei, rather than

737   components of variance (Weir and Cockerham 1984)" (Weir and Goudet 2017).

739   In our study, the empirical Bayesian (Beaumont and Balding 2004) and full Bayesian (Foll

740   and Gaggiotti 2006) population-specific F_{ST} estimators consistently indicated that the Middle

East, Europe and Central/South Asia were centers of human origin. The results obtained with

the empirical Bayesian estimator were a consequence of Equation 2, which uses the mean

allele frequency over subpopulations ($\bar{p}_{lu}$) to reduce the number of parameters to be

estimated. The locations of the 51 human populations were as follows: 21 from the Middle

East, Europe and Central/South Asia, 18 from East Asia, 6 from Africa, 2 from Oceania and 4

from America. The mean allele frequency ($\bar{p}_{lu}$) reflected the weight of samples from the

Middle East, Europe and Central/South Asia, thereby resulting in these areas being identified

as centers of origin. Instead of $\bar{p}_{lu}$, the full Bayesian method uses allele frequencies in the

ancestral population, p_{lu}, which are generated from a noninformative Dirichlet prior,

$p_{lu} \sim Dir\,(1, \dots ,1)$. Our result suggests that not enough information is available to estimate

allele frequencies in the ancestral population assumed in the models. The shrinkage effect on

allele frequencies in Bayesian inference (Stein 1956) may shift population-specific F_{ST} values

toward the average of the whole population. Indeed, Bayesian population-specific F_{ST} values

were higher for African populations than WG population-specific F_{ST} ones and close to those

for East Asia (Figures S2B).

Conclusions

The moment estimator of WG population-specific F_{ST} identifies the source population and

traces migration events and the evolutionary history of its derived populations by way of

genetic diversity. In contrast, NC83 pairwise F_{ST} represents the current population structure.

Generally, the first axis of MDS of the pairwise F_{ST} distance matrix reflects population

history, while subsequent axes reflect migration events, languages and the effect of

environment. The relative contributions of these factors depend on the ecological

characteristics of the species. Because of shrinkage towards mean allele frequencies,

maximum likelihood and Bayesian estimators of locus-specific global F_{ST} improve the power

to detect genes under environmental selection. In contrast, the WC84 bias-corrected moment

estimator of global F_{ST} enables reliable estimation of current population structure, reflecting

evolutionary history. Given a large number of loci, bias-corrected F_{ST} moment estimators,

whether global, pairwise or population-specific, provide unbiased estimates of F_{ST} supported

by the law of large numbers. Genomic data highlight the usefulness of the bias-corrected

moment estimators of F_{ST}. All F_{ST} estimators described in this paper have reasonable CPU

times.

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Literature Cited

Anopheles gambiae 1000 Genomes Consortium, 2017 Genetic diversity of the African malaria

vector *Anopheles gambiae*. Nature 552 (7683): 96. https://doi:10.1038/nature24995

Balding, D. J., 2003 Likelihood-based inference for genetic correlation coefficients. Theor.

Popul. Biol. 63: 221–230. https://doi.org/10.1016/S0040-5809(03)00007-8

Balding, D. J., and R. A. Nichols, 1995 A method for quantifying differentiation between

populations at multi-allelic loci and its implications for investigating identity and

paternity. Genetica 96: 3–12. https://doi.org/10.1007/BF01441146

Balding, D. J., M. Greenhalgh, and R. A. Nichols, 1996. Population genetics of STR loci in

Caucasians. Int. J. Legal Med. 108: 300–305. https://doi.org/10.1007/BF02432124

Balloux, F., and N. Lugon-Moulin, 2002 The estimation of population differentiation with

microsatellite markers. Mol. Ecol. 11: 155–165. https://doi.org/10.1046/j.0962-

1083.2001.01436.x

Beaumont, M. A., and D. J. Balding, 2004 Identifying adaptive genetic divergence among

populations from genome scans. Molec. Ecol. 13: 969–980.

https://doi.org/10.1111/j.1365-294X.2004.02125.x

Beaumont, M. A., 2005 Adaptation and speciation: what can F_{ST} tell us? Trends Ecol. Evol.

20: 435–440. https://doi.org/10.1016/j.tree.2005.05.017

Berg, P. R., S. Jentoft, B. Star, K. H. Ring, H. Knutsen *et al.* 2015 Adaptation to low salinity

promotes genomic divergence in Atlantic cod (*Gadus morhua* L.). Genome Biol. Evol.

7: 1644–1663. https://doi.org/10.1093/gbe/evv093

Berg, P. R., B. Star, C. Pampoulie, M. Sodeland, J. M. Barth *et al.* 2016 Three chromosomal

rearrangements promote genomic divergence between migratory and stationary

ecotypes of Atlantic cod. Sci. Rep. 6: 23246. https://doi.org/10.1038/srep23246

Bhatia, G., N. Patterson, S. Sankararaman, and A. L. Price, 2013 Estimating and interpreting

F_{ST}: the impact of rare variants. Genome Res. 23: 1514–1521.

http://www.genome.org/cgi/doi/10.1101/gr.154831.113

Bonanomi, S., N. Overgaard Therkildsen, A. Retzel, R. Berg Hedeholm, M. W. Pedersen, *et*

al., 2016 Historical DNA documents long-distance natal homing in marine fish. Molec.

Ecol. 25: 2727–2734. https://doi.org/10.1111/mec.13580

Bradbury, I. R., S. Hubert, B. Higgins, T. Borza, S. Bowman, *et al.*, 2010 Parallel adaptive

evolution of Atlantic cod on both sides of the Atlantic Ocean in response to

temperature. Proc. Royal Soc. B: Biol. Sci. 277: 3725–3734.

813 https://doi.org/10.1098/rspb.2010.0985

814 Browning, S. R., and B. S. Weir, 2010 Population structure with localized haplotype clusters.

815  Genetics, 185: 1337–1344. https://doi.org/10.1534/genetics.110.116681

816 Cann, H. M., C. De Toma, L. Cazes, M. F. Legrand, V. Morel, *et al.*, 2002 A human genome

817  diversity cell line panel. Science, 296: 261–262. DOI: 10.1126/science.296.5566.261b

818 Cheng, T., J. Wu, Y. Wu, R. V. Chilukuri, L. Huang *et al.*, 2017 Genomic adaptation to

819  polyphagy and insecticides in a major East Asian noctuid pest. Nat. Ecol. Evol. 1, 1747.

820  http://doi:10.1038/s41559-017-0314-4

821 Cockerham, C. C., 1969 Variance of gene frequencies. Evolution 23: 72–84.

822  https://doi.org/10.1111/j.1558-5646.1969.tb03496.x

823 Cockerham, C. C., 1973 Analyses of gene frequencies. Genetics 74: 679–700. PubMed

824  17248636

825 Cochran, W. G. 1977 *Sampling Techniques*. John Wiley & Sons, New York.

826 Corander, J., P. Waldmann, and M. J. Sillanpää, 2003 Bayesian analysis of genetic

827  differentiation between populations. Genetics 163: 367–374. PubMed

828  12586722

829 Crow, J. F., and K. Aoki, 1984 Group selection for a polygenic behavioral trait: estimating the

830  degree of population subdivision. Proc. Natl. Acad. Sci. 81: 6073–6077.

831  https://doi.org/10.1073/pnas.81.19.6073

832 Diamond, J. 1997 *Guns, Germs and Steel: The Fates of Human Societies.* Random House,

833  London.

834 Excoffier, L., 2001 Analysis of population subdivision, pp. 271–307 in Handbook of

835  Statistical Genetics, edited by D. J. Balding, M. Bishop and C. Cannings. Wiley,

836  Chichester, UK.

Excoffier, L., and H.E. L. Lischer (2010) Arlequin suite ver 3.5: A new series of programs to

perform population genetics analyses under Linux and Windows. Molec. Ecol. Res. 10:

564–567. https://doi.org/10.1111/j.1755-0998.2010.02847.x

Foll, M., and O.Gaggiotti, 2006 Identifying the environmental factors that determine the

genetic structure of populations. Genetics 174: 875–891.

https://doi.org/10.1534/genetics.106.059451

Foll, M., and O.Gaggiotti, 2008. A genome-scan method to identify selected loci appropriate

for both dominant and codominant markers: a Bayesian perspective. Genetics 180:

977–993. https://doi.org/10.1534/genetics.108.092221

Geraldes, A., J. Pang, N. Thiessen, T. Cezard, R. Moore *et al.* 2011 SNP discovery in black

cottonwood (*Populus trichocarpa*) by population transcriptome resequencing. Molec.

Ecol. Resour. 11: 81–92. https://doi.org/10.1111/j.1755-0998.2010.02960.x

Geraldes, A., S. P. Difazio, G. T. Slavov, P. Ranjan, W. Muchero *et al.*, 2013 A 34K SNP

genotyping array for *Populus trichocarpa*: design, application to the study of natural

populations and transferability to other *Populus* species. Molec. Ecol. Resour. 13: 306–

323. https://doi.org/10.1111/1755-0998.12056

Geraldes, A., N. Farzaneh, C. J. Grassa, A. D. McKown, R. D. Guy *et al.*, 2014 Landscape

genomics of *Populus trichocarpa* the role of hybridization limited gene flow and

natural selection in shaping patterns of population structure. Evolution 68: 3260–3280.

https://doi.org/10.1111/evo.12497

Goudet, J. 1995 FSTAT (version 1.2): a computer program to calculate *F*-statistics. J. Hered.

86: 485–486.

Griffin, P. C., S. B. Hangartner, A. Fournier-Level, and A. A. Hoffmann, 2017 Genomic

trajectories to desiccation resistance: convergence and divergence among replicate

selected Drosophila lines. Genetics 205: 871–890.

https://doi.org/10.1534/genetics.116.187104

Hemmer‑Hansen, J., E. E. Nielsen, N. O. Therkildsen, M. I. Taylor, R. Ogden *et al.*, 2013a A

genomic island linked to ecotype divergence in Atlantic cod. Molec. Ecol. 22: 2653–

2667. https://doi.org/10.1111/mec.12284

Hemmer‑Hansen, J., E. E. Nielsen, N. O. Therkildsen, M. I. Taylor, R. Ogden *et al.*, 2013b

Data from: A genomic island linked to ecotype divergence in Atlantic cod, Dryad,

Dataset, https://doi.org/10.5061/dryad.9gf10

Holsinger, K. E., 1999 Analysis of genetic diversity in geographically structured populations:

a Bayesian perspective. Hereditas 130: 245–255. https://doi.org/10.1111/j.1601-

5223.1999.00245.x

Holsinger, K. E., P. O. Lewis, and D. K. Dey, 2002 A Bayesian approach to inferring

population structure from dominant markers. Mol. Ecol. 11: 1157–1164.

https://doi.org/10.1046/j.1365-294X.2002.01512.x

Holsinger, K.E., and B. S. Weir, 2009 Genetics in geographically structured populations:

defining, estimating and interpreting F_{ST}. Nat. Rev. Genet. 9: 639–650.

https://doi.org/10.1038/nrg2611

Hudson, R. R. 2002 Generating samples under a Wright–Fisher neutral model of genetic

variation. Bioinformatics 18: 337–338. https://doi.org/10.1093/bioinformatics/18.2.337

Kettle AJ, Morales-Muniz A, Rosello-Izquierdo E, Heinrich D, Vollestad LA (2011) Refugia

of marine fish in the northeast Atlantic during the last glacial maximum: concordant

assessment from archaeozoology and palaeotemperature reconstructions.

Kitada, S., and H. Kishino, 2004 Simultaneous detection of linkage disequilibrium and

genetic differentiation of subdivided populations. Genetics 167: 2003–2013.

https://doi.org/10.1534/genetics.103.023044

Kitada, S., T. Kitakado, and H. Kishino, 2007. Empirical Bayes inference of pairwise F_{ST} and

its distribution in the genome. Genetics 177: 861–873.

https://doi.org/10.1534/genetics.107.077263

Kitada, S., R., Nakamichi, and H. Kishino, 2017 The empirical Bayes estimators of fine-scale

population structure in high gene flow species. Molec. Ecol. Resour.17: 1210–1222.

https://doi.org/10.1111/1755-0998.12663

Kitakado, T., S. Kitada, H. Kishino, and H. J. Skaug, 2006 An integrated-likelihood method

for estimating genetic differentiation between populations. Genetics 173: 2073–2082.

https://doi.org/10.1534/genetics.106.055350

Lamichhaney, S., A. P. Fuentes-Pardo, N. Rafati, N. Ryman, G. R. McCracken *et al.*, 2017

Parallel adaptive evolution of geographically distant herring populations on both sides

of the North Atlantic Ocean. Proc. Natl. Acad. Sci. USA 114: E3452–E3461.

https://doi.org/10.1073/pnas.1617728114

Lange, K., 1995 Application of the Dirichlet distribution to forensic match probabilities.

Genetica 96: 107–117. https://doi.org/10.1007/BF01441156

Lazaridis, I., D. Nadel, G. Rollefson, D. C. Merrett, N. Rohland *et al.*, 2016 Genomic insights

into the origin of farming in the ancient Near East. Nature, 536(7617), 419.

https://doi:10.1038/nature19310

Levsen, N. D., P. Tiffin, and M. S. Olson, 2012 Pleistocene speciation in the genus *Populus*

(Salicaceae). System. Biol. 61: 401. https://doi.org/10.1093/sysbio/syr120

Liu, H., F. Prugnolle, A. Manica, and F. Balloux, 2006 A geographically explicit genetic

model of worldwide human-settlement history. Am. Hum. Genet. 79: 230–237.

https://doi.org/10.1086/505436

Lockwood, J. R., K. Roeder, and B. Devlin, 2001 A Bayesian hierarchical model for allele

frequencies. Genet. Epidemiol. 20: 17–33. https://doi.org/10.1002/1098-

2272(200101)20:1<17::AID-GEPI3>3.0.CO;2-Q

McKown, A. D., R. D. Guy, J. Klápště, A. Geraldes, M. Friedmann *et al.*, 2014a Geographical

and environmental gradients shape phenotypic trait variation and genetic structure in

Populus trichocarpa. New Phytol. 201, 1263–1276. https://doi.org/10.1111/nph.12601

McKown, A. D., J. Klápště, R. D. Guy, A. Geraldes, I. Porth *et al.*, 2014b Genome‐wide

association implicates numerous genes underlying ecological trait variation in natural

populations of *Populus trichocarpa*. New Phytol. 203: 535–553.

https://doi.org/10.1111/nph.12815

McKown, A. D., R. D. Guy, L. Quamme, J. Klápště, J. La Mantia *et al.*, 2014c Association

genetics, geography and ecophysiology link stomatal patterning in *Populus trichocarpa*

with carbon gain and disease resistance trade‐offs. Molec, Ecol. 23: 5771‐5790.

https://doi.org/10.1111/mec.12969

Malinsky, M., R. J. Challis, A. M. Tyers, S. Schiffels, Y. Terai *et al.*, 2015 Genomic islands of

speciation separate cichlid ecomorphs in an East African crater lake. Science 350: 1493-

1498. DOI: 10.1126/science.aac9927

Nakamichi, R., H. Kishino, S. Kitada, 2020 Fine-Scale Population Analysis 2. CRAN

(https://CRAN.R-project.org/package=FinePop).

Nei, M., 1973 Analysis of gene diversity in subdivided populations. Proc. Natl. Acad. Sci.

USA 70: 3321–3323. https://doi.org/10.1073/pnas.70.12.3321

Nei, M., 1975 *Molecular population genetics and evolution*. North-Holland. Amsterdam.

Nei, M., 1977 *F*‐statistics and analysis of gene diversity in subdivided populations. Ann.

Hum. Genet. 41: 225–233. https://doi.org/10.1111/j.1469-1809.1977.tb01918.x

Nei, M., and R. K. Chesser, 1983 Estimation of fixation indices and gene diversities. Ann.

Hum. Genet. 47: 253–259. https://doi.org/10.1111/j.1469-1809.1983.tb00993.x

Nicholson, G., A. V. Smith, F. Jónsson, Ó. Gústafsson, K. Stefánsson *et al.*, 2002 Assessing

population differentiation and isolation from single‑nucleotide polymorphism data. J.

Roy. Stat. Soc. B. Stat. Method. 64: 695‑715. https://doi.org/10.1111/1467-9868.00357

Nielsen, R., J. M. Akey, M. Jakobsson, J. K. Pritchard, S. Tishkoff, and E. Willerslev, 2017

Tracing the peopling of the world through genomics. Nature 541: 302–310.

doi:10.1038/nature21347

Pérez-Lezaun, A., F. Calafell, E. Mateu, D. Comas, R. Ruiz-Pacheco *et al.,* 1997

Microsatellite variation and the differentiation of modern humans. Human Genet. 99:

1–7. https://doi.org/10.1007/s004390050299

Prohaska, A., F. Racimo, A. J. Schork, M. Sikora, A. J. Stern *et al.*, 2019 Human disease

variation in the light of population genomics. Cell 177: 115–131.

https://doi.org/10.1016/j.cell.2019.01.052

Ramachandran, S., O. Deshpande, C. C. Roseman, N. A. Rosenberg, M. W. Feldman, and L.

L. Cavalli-Sforza, 2005 Support from the relationship of genetic and geographic

distance in human populations for a serial founder effect originating in Africa. Proc.

Natl. Acad. Sci. 102: 15942–15947. https://doi.org/10.1073/pnas.0507611102

Rannala, B., and J. A. Hartigan, 1996 Estimating gene flow in island populations. Genet. Res.

67: 147–158. https://doi.org/10.1017/S0016672300033607

Raymond, M., and F., Rousset,1995 GENEPOP (version 1.2): population genetics software

for exact tests and ecumenicism. J. Hered. 86: 248–249.

Rosenberg, N. A., J. K. Pritchard, J. L. Weber, H. M. Cann, K. K. Kidd, L. A. Zhivotovsky,

and M. W. Feldman, 2002 Genetic structure of human populations. Science 298: 2381–

2385. DOI: 10.1126/science.1078311

Rousset, F., 2001 Inferences from spatial population genetics, pp. 239–269 in Handbook of

Statistical Genetics, edited by D. J. Balding, M. Bishop and C. Cannings. Wiley,

Chichester, UK.

Rousset, F., 2002 Inbreeding and relatedness coefficients: what do they measure? Heredity 88:

371–380.

Rousset, F., 2004 *Genetic Structure and Selection in Subdivided Populations*. Princeton

University Press, Princeton, NJ.

Rousset, F., 2008 Genepop'007: a complete reimplementation of the Genepop software for

Windows and Linux. Mol. Ecol. Resour. 8: 103–106. https://doi.org/10.1111/j.1471-

8286.2007.01931.x

Rutherford, A. 2016 *A Brief History of Everyone Who Ever Lived: The Human Story Retold*

Through Our Genes. The Experiment, NY.

Slatkin, M. 1991 Inbreeding coefficients and coalescence times. Genet. Res. 58: 167–175.

https://doi.org/10.1017/S0016672300029827

Stein, C. 1956 Inadmissibility of the usual estimator for the mean of a multivariate

distribution, pp. 197–206 in Proceedings of the Third Berkeley Symposium on

Mathematical Statistics and Probability Vol. 1, University of California Press, Berkeley,

CA.

Steele, C. D., D. S. Court, and D. J. Balding, 2014 Worldwide estimates relative to five

continental‑scale populations. Ann. Hum. Genet. 78: 468–477.

https://doi.org/10.1111/ahg.12081

Stolarek, I., A. Juras, L. Handschuh, M. Marcinkowska-Swojak, A. Philips *et al.*, 2018 A

mosaic genetic structure of the human population living in the South Baltic region

during the Iron Age. Sci. Rep. 8(1), 2455. https://doi.org/10.1038/s41598-018-20705-6

Therkildsen, N. O., J. Hemmer‐Hansen, R. B. Hedeholm, M. S. Wisz, C. Pampoulie *et al.*

2013a Spatiotemporal SNP analysis reveals pronounced biocomplexity at the northern

range margin of Atlantic cod *Gadus morhua*. Evol. Appl. 6: 690–705.

https://doi.org/10.1111/eva.12055

Therkildsen, N. O., J. Hemmer‐Hansen, R. B. Hedeholm, M. S. Wisz, C. Pampoulie *et al.*

2013b Data from: Spatiotemporal SNP analysis reveals pronounced biocomplexity at

the northern range margin of Atlantic cod *Gadus morhua*, v2, Dryad, Dataset,

https://doi.org/10.5061/dryad.rd250

Therkildsen, N. O., J. Hemmer‐Hansen, T. D. Als, D. P. Swain, M. J. Morgan *et al.*, 2013c

Microevolution in time and space: SNP analysis of historical DNA reveals dynamic

signatures of selection in Atlantic cod. Molec. Ecol. 22: 2424–2440.

https://doi.org/10.1111/mec.12260

Tishkoff, S. A., F. A. Reed, F. R. Friedlaender, C. Ehret, A. Ranciaro *et al.*, 2009 The genetic

structure and history of Africans and African Americans. Science 324: 1035–1044.

DOI: 10.1126/science.1172257

Weir, B. S., 1996 *Genetic data analysis II*. Sinauer, Sunderland.

Weir, B. S., and C. C. Cockerham, 1984 Estimating *F*-statistics for the analysis of population

structure. Evolution 38: 1358–1370.

Weir, B. S., and W. G. Hill, 2002 Estimating *F*-statistics. Annu. Rev. Genet. 36: 721–750.

https://doi.org/10.1146/annurev.genet.36.050802.093940

Weir, B. S., L. R. Cardon, A. D. Anderson, D. M. Nielsen, and W. G. Hill, 2005 Measures of

human population structure show heterogeneity among genomic regions. Genome Res.

15: 1468–1476. doi: 10.1101/gr.4398405

Weir, B. S., and J. Goudet, 2017 A unified characterization of population structure and

relatedness. Genetics 206: 2085–2103. https://doi.org/10.1534/genetics.116.198424

Wright, S., 1931 Evolution in mendelian populations. Genetics 16: 97–158. PMID: 17246615

Wright, S., 1951 The genetical structure of populations. Ann. Eugen. 15: 323–354.

https://doi.org/10.1111/j.1469-1809.1949.tb02451.x

Figure legends

Figure 1 Population structure of 51 human populations (n = 1,035; 377 microsatellites). (A) He vs. population-specific F_{ST} (Weir and Goudet 2017). (B) Population structure and (C) gene flow based on pairwise F_{ST}. Populations connected by yellow lines are those with pairwise F_{ST} < 0.01. The radius of each sampling point is proportional to the level of He as visualized by H_e^{12}.

Figure 2 Population-specific F_{ST} visualization of the population structure of 51 human populations. (A) WG (Weir and Goudet 2017). (B) BB (Beaumont and Balding 2004). (C) FG (Foll and Gaggiotti 2006). (D–F) First to third MDS axes of pairwise F_{ST} with 72% goodness of fit. Data from Rosenberg *et al.* (2002).

Figure 3 Relationships between population-specific F_{ST} and MDS axes of pairwise F_{ST} for 51 human populations. (A) First axis of pairwise F_{ST} vs. population-specific F_{ST} (Weir and Goudet 2017). (B) Second vs. third axes of pairwise F_{ST}. Data from Rosenberg *et al.* (2002).

Figure 4 Population structure of 34 geographical samples of wild Atlantic cod (n = 1,065; 921 SNPs). (A) He vs. population-specific F_{ST} (Weir and Goudet 2017). (B) Population structure and (C) gene flow based on pairwise F_{ST}. Populations connected by yellow lines are those with pairwise F_{ST} < 0.04. The radius of each sampling point is proportional to the level of heterozygosity (He) as visualized by H_e^{100}. Data are combined data from Therkildsen *et al.* (2013) and Hemmer-Hansen *et al.* (2013).

1034

1035 **Figure 5** Population-specific F_{ST} visualization of the population structure of 34

1036 samples of Atlantic cod. (A) Population-specific F_{ST} (Weir and Goudet 2017). (B) First

1037 and (C) second axes of pairwise F_{ST} with 97% goodness of fit. Data are combined

1038 data from Therkildsen *et al.* (2013) and Hemmer-Hansen *et al.* (2013).

1039

1040 **Figure 6** Relationships between population-specific F_{ST} and MDS axes of pairwise

1041 F_{ST} for 34 Atlantic cod populations. (A) First axis of pairwise F_{ST} vs. population-

1042 specific F_{ST} (Weir and Goudet 2017). (B) First vs. second axes of pairwise F_{ST}.

1043 Combined data from Therkildsen *et al.* (2013) and Hemmer-Hansen *et al.* (2013).

1044

Figure 7 Population structure of 25 geographical samples of wild poplar (*n* = 441;

29,355 SNPs). (A) *He* vs. population-specific F_{ST} (Weir and Goudet 2017). (B)

Population structure and (C) gene flow based on pairwise F_{ST}. Populations

connected by yellow lines are those with pairwise F_{ST} < 0.02. The radius of each

sampling point is proportional to the level of heterozygosity (*He*) as visualized by

H_e^{100}. Data from McKown *et al.* (2014b).

1051

1052 **Figure 8** Population-specific F_{ST} visualization of the population structure of 25

1053 samples of wild poplar. (A) Population-specific F_{ST} (Weir and Goudet 2017). (B) First

1054 and (C) second axes of pairwise F_{ST} with 71% goodness of fit. Data from McKown *et*

1055 *al.* (2014b).

1056

Figure 9 Relationships between population-specific F_{ST}, MDS axes of pairwise F_{ST}

and environmental variables for 25 wild poplar samples. (A) First axis of pairwise F_{ST}

vs. population-specific F_{ST} (Weir and Goudet 2017). (B) First vs. second axes of

pairwise F_{ST}. (C) Longest day length (h) vs. first axis of pairwise F_{ST}. (D) Summer

heat-moisture index vs. second axis of pairwise F_{ST}. Data from McKown *et al.*

(2014a,b).

Table 1 Multiple regression of environmental variables of wild poplar on population-specific F_{ST} values of 25 populations

Explanatory variables	Population-specific F_{ST}				First axis of pairwise F_{ST}				Second axis of pairwise F_{ST}			
	Estimate	SE	t	p	Estimate	SE	t	p	Estimate	SE	t	p
Intercept	-0.7992	0.3229	-2.468	0.0224*	-0.2790	0.0858	-3.255	0.0040**	0.0341	0.0615	0.555	0.5851
DAY	0.0392	0.0165	2.354	0.0289*	0.0159	0.0044	3.600	0.0018**	-0.0004	0.0032	-0.134	0.8948
MAT	-0.0165	0.0104	-1.578	0.1302	-0.0019	0.0028	-0.678	0.5053	0.0008	0.0020	0.380	0.7082
MAP	0.0001	0.0000	2.793	0.0112*	0.0000	0.0001	0.222	0.8268	0.0000	0.0000	-0.579	0.5690
SHM	0.0028	0.0011	2.444	0.0239*	0.0004	0.0003	1.241	0.2290	-0.0005	0.0002	-2.448	0.0237*

DAY; longest day length (hours), MAT; mean annual temperature (℃), MAP; mean annual precipitation (mm), SHM; summer heat-moisture index, *p < 0.05 and **p < 0.01

  Supplemental Note

1. Definitions of F_{ST} in the literature

10   Wright defined F_{ST} as "the correlation between random gametes, drawn from the

11   same subpopulation, relative to the total" and mentioned that "the inbreeding coefficient from

12   matching random lines of ancestry is the type of F_{ST}" (Wright 1951, p. 328). Wright defined

13   F_{ST} in terms of variance as

$$F_{ST} = \frac{\sigma^2_{ST}}{\bar{p}(1-\bar{p})}, \quad (Eq. S1)$$

15   where σ^2_{ST} is the variance of the distribution of allele frequencies in a meta-population

16   described as a beta distribution (two alleles), namely, Beta $(4Nm\bar{p}, 4Nm(1-\bar{p}))$, where $\bar{p}$

17   is the mean allele frequency and $\sigma^2_{ST} = \bar{p}(1-\bar{p})/(4Nm+1)$ (Wright 1931, 1965; Rousett

18   2004). Substituting the latter expression into Equation S1 gives

$$F_{ST} = \frac{1}{4Nm+1} = \frac{1}{\theta+1}$$

20   as expressed by the scale parameter of the beta distribution ($\theta = \alpha + \beta$) (Wright 1951). F_{ST}

21   has been defined as the ratio of the between-population variance to the total variance of allele

22   frequencies (Cockerham 1973; Weir and Cockerham 1984; Excoffier 2001; Balloux and

23   Lugon-Moulin 2002; Holsinger and Weir 2009), namely,

24
$$F_{\text{ST}} = \frac{\sigma_p^2}{\bar{p}(1-\bar{p})},$$

25   which is of the same form as Equation S1.

26   Nei (1973) proposed the G_{ST} measure to explicitly formulate Wright's F-statistics

27   using gene diversities allowing multiple alleles. G_{ST} is defined as the ratio of between-

28   population heterozygosity to total heterozygosity, that is,

36
$$G_{\text{ST}} = \frac{H_T - H_S}{H_T}, \quad (\text{Eq. S2})$$

29   where H_T is total heterozygosity and H_S is within-population heterozygosity. Nei (1977)

30   also defined Wright's fixation indices as follows:

37
$$F_{\text{IS}} = \frac{H_S - H_0}{H_S}$$

38
$$F_{\text{IT}} = \frac{H_T - H_0}{H_T}$$

39
$$F_{\text{ST}} = \frac{H_T - H_S}{H_T}.$$

31   In these equations, $H_0 = 1 - \sum_{u=1}^{m} P_{uu}$, $H_S = 1 - \sum_{u=1}^{m} \overline{p_u^2}$, and $H_T = 1 - \sum_{u=1}^{m} \bar{p}_u^2$. Here,

32    $P_{uu} = \sum_{i=1}^{r} w_i P_{iuu}$, $\overline{p_u^2} = \sum_{i=1}^{r} w_i p_{iu}^2$ and $\bar{p}_u^2 = (\sum_{i=1}^{r} w_i p_u)^2$, where w_i is the relative size

33   of population i with $\sum_{i=1}^{r} w_i = 1$. Since the relative size of a population is not known in most

34   cases, Nei and Chesser (1983) suggested an equal weight: $w_i = \frac{1}{r}$. In this setting, $P_{uu} =$

35    $\frac{1}{r}\sum_{i=1}^{r} P_{iuu}$, $\overline{p_u^2} = \frac{1}{r}\sum_{i=1}^{r} p_{iu}^2$ and $\bar{p}_u^2 = \left(\frac{1}{r}\sum_{i=1}^{r} p_u\right)^2$. Thus, apparently,

40
$$G_{\text{ST}} \equiv F_{\text{ST}}.$$

41   Crow and Aoki (1984) introduced the concept of gene identity and defined G_{ST} as

42
$$G_{\text{ST}} = \frac{F_0 - \bar{F}}{1 - \bar{F}}.$$

43   Here, F_0 is "the probability that two homologous genes drawn at random from a group are

44   the same (identical in state)," and $\bar{F}$ is "the probability for genes drawn at random from the

45   entire population." Slatkin (1991) defined F_{ST} in terms of probabilities of identity:

49
$$F_{ST} = \frac{f_0 - \bar{f}}{1 - \bar{f}} ,$$

46   where "f_0 is the probability of identity of two genes sampled from the same subpopulation

47   and $\bar{f}$ is the probability of identity of two genes sampled at random from the collection of

48   subpopulations being considered."

50   Rousset (2001) defined F_{ST} as follows:

63
$$F_{ST} = \frac{Q_w - Q_b}{1 - Q_b} . \qquad (Eq. S3)$$

51   Here, Q_w is "the probabilities of identity of genes from adults sampled within a deme, and

52   Q_b is the probabilities of identity of genes from different demes." Rousset (2004) noted that

53   "$H_i = 1 - Q.$ is known as gene diversity or heterozygosity." Excoffier (2001) also formulated

54   the definition

64
$$F_{ST} = \frac{Q_S - Q_T}{1 - Q_T} ,$$

where Q_S and Q_T are "the probabilities that two genes within subpopulations and within the

total population are identical, respectively." Although definitions differ, Q_b is "the

probability of identity between genes in two different subpopulations" (Rousset 2002). Q_b is

calculated for all combinations of population pairs; therefore, Q_b would apply to the total

population (see p. 2089 in Weir and Goudet 2017). Indeed, $1 - Q_b$ represents the total

variance component (Rousset 2008). Therefore, $Q_b = Q_T$. Karhunen and Ovaskainen (2012)

also defined a coancestry coefficient in line with the coalescent-based definition of F_{ST}

(Rousset 2004):

70
$$F_{ST} = \frac{\theta^W - \theta^B}{1 - \theta^B}.$$

65 In the above equation, θ^W is the average coancestry within subpopulations, and θ^B is that

66 between subpopulation pairs. The definitions of F_{ST} and G_{ST} are thus identical, and

71
$$F_{ST} = G_{ST} = \frac{\text{between heterozygosity}}{\text{total heterozygosity}}.$$

67 The values of gene identity (*e.g.*, Q_S and Q_T) can differ, however, depending on spatial and

68 mutation models and weighting schemes (*e.g.*, Crow and Aoki 1984; Slatkin 1991;

69 Cockerham and Weir 1993; Rousset 2001, 2002, 2004, 2008), as stated by Excoffier (2001).

2. G_{ST} is identical to F_{ST}

In this section, we revisit Kitada *et al.* (2017) and describe the relationship between

the definitions of Wright's F_{ST} and Nei's G_{ST} using notations consistent with those of Weir

and Hill (2002): i for populations ($i = 1, …, r$), u for alleles ($u = 1, …, m$) and l for loci ($l =$

$1, …, L$).

Nei (1973) first defined the coefficient of gene differentiation known as G_{ST}, which is

a multi-allelic analog of F_{ST} among a finite number of subpopulations (Balloux and Lugon-

Moulin 2002). Nei's G_{ST} formula is the ratio of between-population heterozygosity to total

heterozygosity (Equation S2). At a single locus, H_T (total heterozygosity) and H_S (within-

population heterozygosity) are

83
$$H_S = 1 - \frac{1}{r}\sum_{i=1}^{r}\sum_{u=1}^{m} p_{iu}^2 \quad (\text{Eq. S4})$$

84
$$H_T = 1 - \sum_{u=1}^{m}\left(\frac{1}{r}\sum_{i=1}^{r} p_{iu}\right)^2. \quad (\text{Eq. S5})$$

85   The F_{ST} over a meta-population is often called global F_{ST}. When estimating

86   population structure, F_{ST} values between pairs of population samples (pairwise F_{ST}) are

87   routinely used in addition to global F_{ST}. Here, we focus on F_{ST} between population pairs

88   (pairwise F_{ST}) at a single locus. Let population i $(i = 1, 2)$ have the allele frequencies p_{iu}. In

89   such cases, the denominator of G_{ST} is

90
$$H_T = 1 - \frac{1}{4}\sum_{u=1}^{m}(p_{1u}+p_{2u})^2 = 1 - \sum_{u=1}^{m}\left(\frac{p_{1u}+p_{2u}}{2}\right)^2 = 1 - \sum_{u=1}^{m}\bar{p}_u^2.$$

91   This is decomposed as

92
$$H_T = 1 - \sum_{u=1}^{m}\bar{p}_u^2 = 1 - \left(\sum_{u=1}^{m-1}\bar{p}_u^2 + \left(1 - \sum_{u=1}^{m-1}\bar{p}_u\right)^2\right) = 2\left[\sum_{u=1}^{m-1}\bar{p}_u(1-\bar{p}_u) - \sum_{u<u'}^{m-1}\bar{p}_u\bar{p}_{u'}\right].$$

93   As the second term can be written as

94
$$-2\sum_{u<u'}^{m-1}\bar{p}_u\bar{p}_{u'} = \bar{p}_m(1-\bar{p}_m) - \sum_{u=1}^{m-1}\bar{p}_u(1-\bar{p}_u),$$

95   we have

96
$$2\left[\sum_{u=1}^{m-1}\bar{p}_u(1-\bar{p}_u) - \sum_{u<u'}^{m-1}\bar{p}_u\bar{p}_{u'}\right]$$

97
$$= 2\sum_{u=1}^{m-1}\bar{p}_u(1-\bar{p}_u) + \bar{p}_m(1-\bar{p}_m) - \sum_{u=1}^{m-1}\bar{p}_u(1-\bar{p}_u) = \sum_{u=1}^{m}\bar{p}_u(1-\bar{p}_u).$$

98   Therefore,

99
$$H_T = 1 - \sum_{u=1}^{m}\bar{p}_u^2 = \sum_{u=1}^{m}\bar{p}_u(1-\bar{p}_u).$$

100   The numerator of G_{ST} is

101
$$H_T - H_S = 1 - \frac{1}{4}\sum_{u=1}^{m}(p_{1u} + p_{2u})^2 - \left[1 - \frac{1}{2}\sum_{u=1}^{m}(p_{1u}^2 + p_{2u}^2)\right] = \frac{1}{2}\sum_{u=1}^{m}(p_{1u}^2 + p_{2u}^2)$$

102
$$-\frac{1}{4}\sum_{u=1}^{m}(p_{1u} + p_{2u})^2 = \frac{1}{4}\sum_{u=1}^{m}(p_{1u} - p_{2u})^2. \quad \text{(Eq. S6)}$$

103 For the numerator, we consider the general case of variance of random variables $V[x] =$

104 $\frac{1}{n-1}\sum_{i=1}^{n}(x_i - \bar{x})^2$. The variance can be written as

105
$$V[x] = \frac{1}{n-1}\sum_{i=1}^{n}(x_i - \bar{x})^2 = \frac{1}{n-1}\sum_{i=1}^{n}(x_i - \frac{1}{n}\sum_{j=1}^{n}x_i)^2$$

106
$$= \frac{1}{n-1}\sum_{i=1}^{n}\left(\frac{1}{n}\sum_{j=1}^{n}(x_i - x_j)\right)$$

107
$$= \frac{1}{(n-1)n^2}\sum_{i=1}^{n}\sum_{j=1}^{n}\sum_{k=1}^{n}(x_i - x_j)(x_i - x_k)$$

108
$$= \frac{1}{(n-1)n^2}\sum_{i=1}^{n}\sum_{j=1}^{n}\sum_{k=1}^{n}(x_i^2 - x_i x_k - x_i x_j - x_j x_k)$$

109
$$= \frac{1}{(n-1)n^2}\left[n^2\sum_{i=1}^{n}x_i^2 - n\left(\sum_{i=1}^{n}x_i^2 + \sum_{i\neq k}x_i x_k\right) - n\left(\sum_{i=1}^{n}x_i^2 + \sum_{i\neq j}x_i x_j\right)\right.$$

110
$$\left. + n\left(\sum_{i=1}^{n}x_i^2 + \sum_{j\neq k}x_j x_k\right)\right] = \frac{1}{(n-1)n}\left[(n-1)\sum_{i=1}^{n}x_i^2 - \sum_{i\neq j}x_i x_j\right]$$

111
$$= \frac{1}{2(n-1)n}\sum_{i\neq j}^{n}(x_i - x_j)^2.$$

112 In the case of pairwise F_{ST} $(n = 2)$, the numerator is expressed as

113
$$V[x] = \frac{1}{4}(x_1 - x_2)^2.$$

114   The numerator of G_{ST} (Equation S6) is thus the variance of allele frequencies between

115   subpopulations. From Equations S4 and S5, we have

116
$$G_{ST} = \frac{\frac{1}{4}\sum_{u=1}^{m}(p_{1,u} - p_{2,u})^2}{\sum_{u=1}^{m}\bar{p}_u(1 - \bar{p}_u)} = \frac{\sigma_{ST}^2}{\sum_{u=1}^{m}\bar{p}_u(1 - \bar{p}_u)}. \quad (\text{Eq. S7})$$

117   For bi-allelic cases, $H_T - H_S = \frac{1}{2}(p_1 - p_2)^2$ and $H_T = 2\bar{p}(1 - \bar{p})$, and

118
$$G_{ST} = \frac{\frac{1}{4}(p_1 - p_2)^2}{\bar{p}(1 - \bar{p})} = \frac{\sigma_{ST}^2}{\bar{p}(1 - \bar{p})}. \quad (\text{Eq. S8})$$

119   Equation S8 is equal to Equation S1, and we have

120
$$G_{ST} \equiv F_{ST}.$$

121   From Equations S6 and S7, the definition of pairwise F_{ST} (pwF_{ST}) at a single locus for

122   multi-allelic cases is

123
$$\text{pw}F_{ST} = \frac{\frac{1}{4}\sum_{u=1}^{m}(p_{1u} - p_{2u})^2}{\sum_{u=1}^{m}\bar{p}_u(1 - \bar{p}_u)} = \frac{\sum_{u=1}^{m}(p_{1u} - p_{2u})^2}{4\sum_{u=1}^{m}\bar{p}_u(1 - \bar{p}_u)}.$$

124   For bi-allelic cases ($m = 2$), it is

125
$$\text{pw}F_{ST} = \frac{\frac{1}{2}(p_1 - p_2)^2}{2\bar{p}(1 - \bar{p})} = \frac{(p_1 - p_2)^2}{4\bar{p}(1 - \bar{p})}.$$

3. Bias-corrected moment estimators of F_{ST}

3.1 Nei and Chesser's F_{ST} estimator (NC83)

129   F_{ST} is the ratio of between to total variance. The estimator is therefore a ratio

130   estimator and consequently biased. To correct the bias, Nei and Chesser (1983) derived the

131   unbiased estimators of H_S and H_T in diploid populations. This estimator (hereafter, NC83)

132   assumes that samples (n_i individuals) are randomly chosen from a set of fixed

133   subpopulations ($i = 1, \dots, r$). The gene diversities in population i are written based on the

homozygote genotype frequencies P_{iuu} and allele frequencies p_{iu}, respectively given as

$$H_{0i} = 1 - \sum_{u=1}^{m} P_{iuu}$$

$$H_{Si} = 1 - \sum_{u=1}^{m} p_{iu}^2 .$$

Because observed genotype frequencies are unbiased, H_{0i} is unbiasedly estimated by

$$\widehat{H}_{0i} = 1 - \sum_{u=1}^{m} \tilde{P}_{iuu} ,$$

where $\tilde{p}_{iuu}$ denotes observed homozygote genotype frequencies. For estimating H_{Si}, Nei

and Chesser (1983) took the expectation of $\tilde{p}_{iu}^2$, since $\tilde{p}_{iu}^2$ is biased, as

$$E[\tilde{p}_{iu}^2] = p_{iu}^2 + \frac{P_{iuu}}{n_i} + \sum_{u \neq u}^{m} \frac{P_{iuu'}}{4n_i} - \frac{p_{iu}^2}{n_i} .$$

Those authors then calculated the expectation of observed gene diversity in population i: since

$$p_{iu} = P_{uu} + \frac{\sum_{u \neq u}^{m} P_{uu'}}{2},$$

$$1 - E\left[\sum_{u=1}^{m} \tilde{p}_{iu}^2\right] = 1 - \sum_{u=1}^{m} p_{iu}^2 - \frac{1}{n_i}\sum_{u=1}^{m} P_{iuu} - \frac{1}{2n_i}\sum_{u=1}^{m} (p_{iu} - P_{uu}) + \frac{1}{n_i}\sum_{u=1}^{m} p_{iu}^2$$

$$= 1 - \sum_{u=1}^{m} p_{iu}^2 - \frac{1}{n_i}\sum_{u=1}^{m} P_{iuu} - \frac{1}{2n_i} + \frac{1}{2n_i}\sum_{u=1}^{m} P_{uu} + \frac{1}{n_i}\sum_{u=1}^{m} p_{iu}^2$$

$$= H_{Si}\left(1 - \frac{1}{n_i}\right) + \frac{H_{0i}}{2n_i} . \qquad \text{(NC83 Eq. 6)}$$

Using the method of moments, they obtained the unbiased estimator of gene diversity in

population i (H_{Si}):

$$\widehat{H}_{Si} = \frac{n_i}{n_i - 1}\left(1 - \sum_{u=1}^{m} \tilde{p}_{iu}^2 - \frac{\widehat{H}_{0i}}{2n_i}\right) . \qquad \text{(NC83 Eq. 7)}$$

150   Because observed genotype frequencies are unbiased, H_{0i} was unbiasedly estimated by

151     $\widehat{H}_{0i} = 1 - \sum_{u=1}^{m} \tilde{P}_{iuu}$. Thus, they unintentionally derived population-specific gene diversity.

152   Under the assumption that all subpopulations are in Hardy–Weinberg equilibrium, $\widehat{H}_{Si} = \widehat{H}_{0i}$,

153   and we have

$$\widehat{H}_{Si} = \frac{2n_i}{2n_i - 1}\left(1 - \sum_{u=1}^{m} \tilde{p}_{iu}^2\right). \quad (\text{Eq. S9})$$

155   The expectation of the average of observed gene diversity over all populations was

156   similarly derived as

$$1 - E\left[\sum_{u=1}^{m} \overline{\tilde{p}_u^2}\right] = \frac{1}{r}\left[\sum_{i=1}^{r}\left\{H_{Si}\left(1 - \frac{1}{n_i}\right) + \frac{H_{0i}}{2n_i}\right\}\right] = H_S\left(1 - \frac{1}{\tilde{n}}\right) + \frac{H_{0i}}{2\tilde{n}}, \quad (\text{NC Eq. 8})$$

158   where $\overline{\tilde{p}_u^2} = \frac{1}{r}\sum_{i=1}^{r} \tilde{p}_{iu}^2$, and $\tilde{n}$ is the harmonic mean of n_i, namely, $\tilde{n} = \frac{r}{\sum_{i=1}^{r}\frac{1}{n_i}}$. The

159   unbiased moment estimator of gene diversity over all populations was derived as

$$\widehat{H}_S = \frac{\tilde{n}}{\tilde{n} - 1}\left(1 - \sum_{u=1}^{m} \overline{\tilde{p}_u^2} - \frac{\widehat{H}_0}{2\tilde{n}}\right). \quad (\text{NC83 Eq. 9})$$

161   Here, $\widehat{H}_0$ is the unbiased estimator of observed gene diversity based on the homozygote

162   genotype frequencies over all populations:

$$\widehat{H}_0 = 1 - \sum_{u=1}^{m} \overline{\tilde{P}}_{uu}, \quad (\text{NC83 Eq. 5})$$

164   where $\overline{\tilde{P}}_{uu} = \frac{1}{r}\sum_{i=1}^{r} \tilde{P}_{uu}$. To obtain the unbiased estimator of H_T, they derived the expectation

165   of observed mean gene diversity over all populations:

$$1 - E\left[\sum_{u=1}^{m} \overline{\tilde{p}}_u^2\right] = H_T - \frac{H_S}{\tilde{n}r} + \frac{H_0}{2\tilde{n}r}, \quad (\text{NC83 Eq. 10})$$

167   where $\overline{\tilde{p}}_u = \frac{1}{r}\sum_{i=1}^{r} \tilde{p}_{iu}$. From this equation, they obtained the unbiased moment estimator of

168   H_T as

$$169 \qquad \widehat{H}_T = 1 - \sum_{u=1}^{m} \bar{\tilde{p}}_u^2 + \frac{\widehat{H}_S}{\tilde{n}r} - \frac{\widehat{H}_0}{2\tilde{n}r}. \quad \text{(NC83 Eq. 11)}$$

170   Under the assumption that all subpopulations are in Hardy–Weinberg equilibrium,

171    $H_0 = H_S$. In this situation, the estimators are a function of allele frequencies only at a single

172   locus:

$$173 \qquad \widehat{H}_S = \frac{2\tilde{n}}{2\tilde{n}-1} \left(1 - \sum_{u=1}^{m} \overline{\tilde{p}_u^2} \right) \qquad \text{(NC83 Eq. 15)}$$

$$174 \qquad \widehat{H}_T = 1 - \sum_{u=1}^{m} \bar{\tilde{p}}_u^2 + \frac{\widehat{H}_S}{2\tilde{n}r}. \qquad \text{(NC83 Eq. 16)}$$

176   **3.2 Weir and Cockerham's F_{ST} estimator (WC84)**

177   Weir and Cockerham (1984) derived the moment estimator of F_{ST} as a coancestry

178   coefficient denoted by θ, which we call θ_{WC} according to Weir and Goudet (2017):

$$179 \qquad \theta_{WC} = \frac{a}{a+b+c}. \quad \text{(WC84 Eq. 1)}$$

180   This moment estimator of F_{ST} is the ratio of observed unbiased variance components for an

181   allele: a for between-subpopulation components, b for those between individuals within

182   subpopulations and c for those between gametes within individuals, given as

$$183 \qquad a = \frac{\bar{n}}{n_c} \left\{ s^2 - \frac{1}{\bar{n}-1} \left[\bar{p}(1-\bar{p}) - \frac{r-1}{r} s^2 - \frac{1}{4}\bar{h} \right] \right\} \quad \text{(WC84 Eq. 2)}$$

$$184 \qquad b = \frac{\bar{n}}{\bar{n}-1} \left[\bar{p}(1-\bar{p}) - \frac{r-1}{r} s^2 - \frac{2\bar{n}-1}{4\bar{n}} \bar{h} \right] \quad \text{(WC84 Eq. 3)}$$

$$185 \qquad c = \frac{1}{2}\bar{h}, \quad \text{(WC84 Eq. 4)}$$

186   where $\bar{n} = \frac{1}{r}\sum_{i=1}^{r} n_i$, $n_c = \frac{r\bar{n} - \frac{1}{r\bar{n}}\sum_{i=1}^{r} n_i^2}{r-1}$, $\bar{p} = \frac{1}{r\bar{n}}\sum_{i=1}^{r} n_i \tilde{p}_i$, $s^2 = \frac{1}{r-1}\sum_{i=1}^{r} \frac{n_i}{\bar{n}}(\tilde{p}_i - \bar{p})^2$, $\bar{h} =$

187     $\frac{1}{r}\sum_{i=1}^{r}\frac{n_i}{n}\tilde{h}_i$ and $\tilde{h}_i$ is the observed heterozygote frequency in a diploid population. For

188   multiple alleles at a locus, the combined ratio estimator is given in Weir and Cockerham

189   (1984) as

$$\theta_{\text{WC}} = \frac{\sum_{u=1}^{m} a_u}{\sum_{u=1}^{m}(a_u + b_u + c_u)}.$$

191   The combined ratio estimator over all loci ("ratio of averages") is

$$\theta_{\text{WC}} = \frac{\sum_{l=1}^{L}\sum_{u=1}^{m} a_{lu}}{\sum_{l=1}^{L}\sum_{u=1}^{m}(a_{lu} + b_{lu} + c_{lu})}. \qquad \text{(WC84 Eq. 10)}$$

193   Here, we formulate the asymptotic variance of θ_{WC}. Let $\bar{y}$ be the numerator and $\bar{x}$

194   be the denominator of θ_{WC} over loci:

$$\theta_{\text{WC}} = \frac{\frac{1}{L}\sum_{l=1}^{L} a_l}{\frac{1}{L}\sum_{l=1}^{L}(a_l + b_l + c_l)} = \frac{\bar{y}}{\bar{x}}.$$

196   By Taylor series expansion for the first term, we have the asymptotic variance as

$$V[\theta_{\text{WC}}] \simeq \frac{\bar{y}^2}{\bar{x}^4}V[\bar{x}] + \frac{1}{\bar{x}^2}V[\bar{y}] - 2\frac{\bar{y}}{\bar{x}^3}Cov[\bar{x},\bar{y}], \qquad \text{(Eq. S10)}$$

198   where the variance and covariance components are calculated by

199     $V[\bar{x}] = \frac{1}{L(L-1)}\sum_{l=1}^{L}(x_l - \bar{x})^2$, $V[\bar{y}] = \frac{1}{L(L-1)}\sum_{l=1}^{L}(y_l - \bar{y})^2$ and

200     $Cov[\bar{x},\bar{y}] = \frac{1}{L(L-1)}\sum_{l=1}^{L}(x_l - \bar{x})(y_l - \bar{y}).$

202   **3.3 Weir and Goudet's population-specific F_{ST} estimator (WG)**

203   Weir and Goudet (2017) defined population-specific F_{ST} as

$$\text{ps}F_{\text{ST}}^i = \beta_{\text{WT}}^i = \frac{\theta_W^i - \theta^B}{1 - \theta^B}, \qquad \text{(Eq. S11)}$$

where θ_W^i is the identical-by-descent (ibd) probability of two alleles drawn from population

i, and θ^B is the average of ibd probabilities for alleles from different populations. The

definition refers to the "probability two alleles drawn from population i are ibd, relative to the

probability an allele drawn from one population is ibd to an allele drawn from another

population." Equation S11 corresponds to allele-based F_{ST}, and the average over

subpopulations is the usual "population-average F_{ST}" (Weir and Goudet 2017):

213
$$F_{\text{ST}} = \beta_{\text{WT}} = \frac{\theta^W - \theta^B}{1 - \theta^B} \; ,$$

211   as given previously (Equation S3) (*e.g.*, Rousset 2004; Karhunen and Ovaskainen 2012). Weir

212   and Goudet's other definition of population-specific F_{ST} is

214
$$\text{ps}F_{\text{ST}}^i = \beta_{\text{ST}}^i = \frac{\theta_S^i - \theta^B}{1 - \theta^B} ,$$

215   which uses θ_S^i instead of θ_W^i. According to Weir and Goudet, the use of θ_S^i "for within-

216   population pairs of alleles indicates that we are referring to genotypes, whereas, if we work

217   only with alleles, we write θ_W^i." Averaging over population, they gave

218
$$F_{\text{ST}} = \beta_{\text{ST}} = \frac{\theta^S - \theta^B}{1 - \theta^B} .$$

219   "For random mating populations, there will be no need for distinction between β_{ST} and

220   β_{WT}" (Weir and Goudet 2017).

221   Weir and Goudet (2017) derived β_{WT}, the bias-corrected moment estimator of

222   population-specific F_{ST} when only allele frequencies are used, as

223
$$\text{ps}\hat{F}_{\text{ST}}^i = \hat{\beta}_{\text{WT}}^i = \frac{\widetilde{M}_w^i - \widetilde{M}^B}{1 - \widetilde{M}^B} .$$

224    $\widetilde{M}_W^i$ is the unbiased within-population matching of two distinct alleles of population i:

225
$$\widetilde{M}_W^i = \frac{2n_i}{2n_i - 1} \sum_{u=1}^{m} \tilde{p}_{iu}^2 - \frac{1}{2n_i - 1} ,$$

226   where n_i is the sample size (number of individuals) taken from population i, and $\tilde{p}_{iu}$ is the

227   observed frequency of allele u. We note that $1 - \tilde{M}_W^i$ equals to $\hat{H}_{Si}$ (Equation S9):

228
$$1 - \tilde{M}_W^i = \frac{2n_i}{2n_i - 1}\left(1 - \sum_{u=1}^{m}\tilde{p}_{iu}^2\right) = \hat{H}_{Si}. \quad (\text{Eq. S11})$$

229    $\tilde{M}^B$ is the between-population-pair matching average over pairs of populations i, i':

230
$$\tilde{M}^B = \frac{1}{r(r-1)}\sum_{i=1}^{r}\sum_{i'=1(i'\neq i)}^{r}\tilde{M}_B^{ii'}.$$

231    $\tilde{M}_B^{ii'}$ is the matching of one allele in j, j' individuals taken from each of populations i, i':

232
$$\tilde{M}_B^{ii'} = \frac{1}{n_i n_{i'}}\sum_{j=1}^{n_i}\sum_{j'=1}^{n_{i'}}\tilde{M}_{jj'}^{ii'} = \sum_{u=1}^{m}\tilde{p}_{iu}\tilde{p}_{i'u}.$$

233   Average pair-matching of alleles over all populations is therefore calculated from the product

234   of allele frequencies over populations i, i':

235
$$\tilde{M}^B = \frac{1}{r(r-1)}\sum_{i=1}^{r}\sum_{i'=1(i'\neq i)}^{r}\sum_{u=1}^{m}\tilde{p}_{iu}\tilde{p}_{i'u}.$$

236   We can write $\text{ps}\hat{F}_{ST}^i$ over all loci as

237
$$\text{ps}\hat{F}_{ST}^i = \frac{\frac{1}{L}\sum_{l=1}^{L}(\tilde{M}_{W,l}^i - \tilde{M}_l^B)}{\frac{1}{L}\sum_{l=1}^{L}(1 - \tilde{M}_l^B)} = \frac{\bar{y}}{\bar{x}}.$$

238   Equation S10 can be applied for use with the population-specific F_{ST} estimator in the same

239   way, thereby yielding

240
$$V\left[\text{ps}\hat{F}_{ST}^i\right] \simeq \frac{\bar{y}^2}{\bar{x}^2}\left\{\frac{V[\bar{x}]}{\bar{x}^2} + \frac{V[\bar{y}]}{\bar{y}^2} - \frac{2Cov[\bar{x}, \bar{y}]}{\bar{x}\bar{y}}\right\}. \quad (\text{Eq. S12})$$

Supplemental Figures for

Population-specific F_{ST} and Pairwise F_{ST}:
History and Environmental Pressure

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This PDF file includes Figures S1 to S7.

Figure S1 Sampling locations of 51 human populations. Data from Cann *et al.* (2002).

Figure S2 Relationships between different population-specific F_{ST} estimators for 51 human populations. (A) BB (Beaumont and Balding 2004) vs. FG (Foll and Gaggiotti 2006) ($R^2 = 0.9885, p = 2.2 \times 10^{-16}$). (B) WG (Weir and Goudet 2017) vs. FG ($R^2 = 0.8630, p = 2.2 \times 10^{-16}$). Data from Rosenberg *et al.* (2002).

Figure S3 Relationship between the "ratio of averages" and "average of ratios" of population-specific F_{ST} (Weir and Goudet 2017) for 51 human populations ($R^2 = 0.9989, p = 2.2 \times 10^{-16}$). Data from Rosenberg *et al.* (2002).

Figure S4 Multi-dimensional scaling (MDS) axes of pairwise F_{ST} for 51 human populations. (A) Goodness of fit. (B) Correlation between the MDS axis of pairwise F_{ST} and population-specific F_{ST} (Weir and Goudet 2017). Data from Rosenberg *et al.* (2002).

Figure S5 Sampling locations of 37 wild Atlantic cod populations. (A) Entire area. (B) Enlarged view of the area around Greenland. Data from Therkildsen *et al.* (2013) and Hemmer-Hansen (2013).

Figure S6 MDS axes of pairwise F_{ST} for 37 wild Atlantic cod populations. (**A**) Goodness of fit. (**B**) Correlation between the MDS axis of pairwise F_{ST} and population-specific F_{ST} (Weir and Goudet 2017). Data from Therkildsen *et al.* (2013) and Hemmer-Hansen (2013).

Figure S7 MDS axes of pairwise F_{ST} for 25 wild poplar populations. (**A**) Goodness of fit. (**B**) Correlation between the MDS axis of pairwise F_{ST} and population-specific F_{ST}. Data from McKown et al. (2014b).