Sharing mating opportunities by coalition males in stump-tailed macaques: elucidation of ecological mechanism by diversion of PvS model

Aru Toyoda[1,2]*, Tamaki Maruhashi[3], Suchinda Malaivijitnond[4,5], Hiroki Koda[2], Yasuo Ihara[6]*

[1]Chubu University Academy of Emerging Science, Aichi, Japan.

[2]Primate Research Institute, Kyoto University, Aichi, Japan.

[3]Musashi University, Tokyo, Japan.

[4]Department of Biology, Faculty of Science, Chulalongkorn University, Bangkok, Thailand.

[5]National Primate Research Center of Thailand, Saraburi, Thailand.

[6]Department of Biological Sciences, Graduate School of Science, University of Tokyo, Japan.

*Correspondence to:

Aru Toyoda: aru.toyoda@gmail.com

Yasuo Ihara: iharay@bs.s.u-tokyo.ac.jp

ABSTRACT

Cooperation, or the act of benefiting others at the cost of the benefactor's fitness, has been a central issue in evolutionary theory. Non-human animals sometimes show coalitions or male-male "cooperation" to confront a male rival and challenge the rank hierarchy. Here we observed novel types of coalitions in wild stump-tailed macaques (*Macaca arctoides*); multiple males actively shared the mating opportunities, i.e., a male copulated with a female, while his ally waited his turn and guarded them. Our mathematical simulations revealed that lack of estrous signs, as well as large numbers of males in a group, possibly enhance facultative sharing of females. This is the first demonstration of the sharing of females in non-human primates. , and shed light on the evolutionary theory of cooperation. Overall, our novel observations have revised the existing socioecological models in primate social systems. The characteristics of stump-tailed macaque societies now range from despotism to egalitarianism, and from monopolization of females by a dominant male to male-male coalition coupled with active sharing of mating opportunities, which increases the chances of reproductive success.

KEY WORDS

cooperation, sexual traits, socioecological modeling, stump-tailed macaques

INTRODUCTION

Cooperation, or the act of benefiting others at the cost of the benefactor's fitness, has attracted the attention of evolutionary biologists as its origins constitute an evolutionary puzzle. The modern theoretical framework for the evolution of cooperation originated from Hamilton's inclusive fitness theory (Axelrod & Hamilton, 1981; Hamilton, 1964) for kin altruism, along with the idea of reciprocity, as proposed by Trivers, for cooperation among non-kin (Trivers, 1971). Humans are unique in showing "hyper-cooperation" owing to their "spontaneous" tendency to be helpful (Burkart et al., 2014). For example, helping, a direct form of cooperation, is observed in humans even from infancy, whereas this is rare or absent in non-human animals, especially helping of non-relatives (Tomasello & Vaish, 2013).

Male reproductive success in a multi-male multi-female group is often skewed in the favor of high-ranking males (Kutsukake & Nunn, 2006). Subordinate males may gain more opportunities of copulation by forming a coalition to jointly confront the top-ranking male than by competing individually against each other. Previous studies have developed a mathematical framework for investigating the underlying mechanisms of coalition formation and mitigating the existing reproductive skew both when the formation of coalition does or does not change male ranks (Pandit & van Schaik, 2003) (Van Schaik, Pandit, & Vogel, 2006). While this framework is comprehensive enough to cover different coalition varieties, such as all-down, bridging, and all-up coalitions (Van Schaik et al., 2006), it is still limited by the fact that it only considers the mitigating or leveling effect of coalition formation on the reproductive skew. There is a yet another possibility; two or more top-ranking males may form a coalition to exclude lower-ranking males from mating opportunities, as a result of which the reproductive skew favoring dominant males is strengthened or steepened. However, this type of coalition is, while

intuitively conceivable, not expected to be observed frequently. This is because even if two or

more top-ranking males are able to jointly exclude other males, the mating opportunities thus

obtained may be monopolized by the single top-ranking male after all, unless he actively shares

the spoil with his allies. In other words, the top-ranking male has to pay for others' help.

We observed the behavior which theoretically possible but rarely observed described

above in the wild population of stump-tailed macaques (*Macaca arctoides*) in Thailand. That is

"coalition-like" behavior, which is, certain dominant males guard and actively share mating

opportunities (Fig 1).

Figure 1. The male (FTH-M01) and his ally (FTH-M02) simultaneously engaged in the copulation with one female (FHT-F11), not showing any agonistic conflicts between the two "competitive" males; at that time, one male (right male) mounted over the female inserting penis, while the other male (left) "waited for his turn", touching the female hinds.

The reason why we denote it as "coalition-like" is because, according to the strict definition of behavioral studies on primates, it cannot be a coalition because this behavior is not occur in the context of aggression. Generally, a "coalition" means the behavior which is formed when one animal intervenes in an ongoing conflict between two parties to support one side (Widdig, Streich, & Tembrock, 2000). In brief, coalition is defined as joint aggression by multiple individuals against common targets (van Schaik, Pandit, & Vogel, 2006). In that respect, the "coalition-like" behavior observed in stump-tailed macaques discussing here is a bit different behavior from that observed in other species. It is not a bond between individuals that is observed in the context of conflict/aggression, but rather as a bond between males in the context of mating to monopolize the opportunity to copulate with females. The coalition forming in stump-tailed macaques is that an alpha male forms a coalition with one or two male(s), and they work together to monopolize one female, eliminate other competitors, and eventually alternate copulating with the monopolized female. This behavior can be interpreted as a "highly cooperative" behavior in which they jointly owing the risk of eliminating other rivals, jointly acquire the female as breeding resource, then share the mating opportunities as acquired benefits together.

Cooperative mate guarding by top-ranking males likely affects the distribution of mating opportunities within a group of male stump-tailed macaques. In particular, suppose that the

number of sexually receptive females in a group is larger than that would allow the highest-

ranking male to monopolize reproduction (i.e., complete contest competition), but smaller than

that would lead to complete scramble competition. In such cases, top-ranking males may be able

to exclude subordinates more efficiently from mating competition by guarding females

collaboratively than by doing so individually. This raises the possibility that dominant males may

gain a fitness benefit by having cooperative partners despite the cost of sharing mating

opportunities with them.

Male collaboration that results in modification of within-group resource allocation has

been theoretically investigated in the context of primate coalition formation (Pandit & Van

Schaik, 2003; van Schaik, Pandit, & Vogel, 2004; van Schaik et al., 2006). Assuming that payoff

distribution within a group follows the priority-of-access model (Altmann, 1962), Pandit and van

Schaik (2003) developed a mathematical model of leveling coalition, in which a skew in the

access to females in favor of dominant males is mitigated by coalition formation of middle- to

low-ranking males. Although our cases of cooperative mate guarding in stump-tailed macaques

do not associate with overt expression of coordinated aggression by multiple males on one or

more targets, a definitive feature of animal coalition (Pandit & Van Schaik, 2003), they are

comparable with male-male coalitions in the way that they modify group-wise allocation of

mating opportunities. More specifically, since those who collaboratively mate-guard in stump-

tailed macaque groups are top-ranking males, the behavior is similar to all-down or conservative

coalition, that is, coalition of higher-rankers against a lower-ranker (Chapais, 1995; van Schaik et

al., 2004, 2006).

Within the framework of Pandit and van Schaik (2003), however, all-down coalition is

not predicted to occur. This is because higher-rankers have nothing to gain from forming a

coalition to "level" the reproductive skew, for they have priority of access to females any way

(Pandit, Pradhan, & van Schaik, 2020; van Schaik et al., 2006). Instead, cooperative mate

guarding by top-ranking males should be better represented as a novel kind of coalition

formation that deprives lower-ranking males of mating opportunities, whereby "steepens" the

skew. For the purpose of investigating cooperative mate guarding in stump-tailed macaques, this

paper extends the Pandit-van Schaik model by allowing all-down coalition to enhance the

efficiency with which top-ranking males keep subordinates from mating, as a result of which the

reproductive skew is heightened. To keep the model simple and tractable, we choose not to

explicitly specify the underlying mechanism by which subordinates are excluded. Alternatively,

a recent study by Pandit et al. (2020) has extended the original Pandit-van Schaik model by

incorporating a specific mechanism to realize more skewed resource allocation, namely, higher-

rankers' usurping of resources owned by lower-rankers. Pandit et al.'s (2020) model is designed

to explore the origins of class formation in human societies, and non-human primates are

unlikely to meet the presumption that individuals possess exploitable or tradable resources.

In this study, we have first described our findings regarding the fieldwork on groups of

stump-tailed macaques and then analyzed the logic underlying these observations using

mathematical modeling.

METHODS

Study site and animals

A wild population of stump-tailed macaques inhabiting the Khao Krapuk Khao Taomor non-

hunting area in the Phetchaburi Province of central Thailand (99°44' E, 12°48' N, encompassing

an area of 3.5–4 km^2) was observed. This site consists primarily of secondary forests, including

stands of bamboo and agricultural areas. The macaques also visited areas immediately adjacent

to this site (including a nearby temple, cassava and pineapple plantations, and human

settlements) on a daily basis. The macaques were occasionally fed by humans, both locals and

tourists, on the temple grounds or along the roadside. This population was first reported in June

of 1984, at which time there were only 22 individuals. Since then, it has grown to a large

population, including at least 391 individuals, who were divided into five groups, namely, Ting,

Nadam, Third, Fourth, and Wngklm groups (Table S1 in Supplementary Materials) by 2017. The

Wngklm group separated from the Third group in November–December 2015. All adults

(completely mature monkeys), most subadults (sexually mature but not completely developed),

and some juveniles (sexually immature, around 3 years of age) were identified based on facial

characteristics. This population is geographically isolated from the other populations, and no new

immigrant males from other sites were detected during this study period (Toyoda &

Malaivijitnond, 2018; Toyoda, Maruhashi, Malaivijitnond, & Koda, 2017).

Stump-tailed macaques are reported as non-seasonal breeders in general (some local

populations/captive groups show seasonality, but Thailand is not in that range). We add this info

with references. Whether or not the stump-tailed macaque male can detect the fertile status of

female by some questionable are still not clear. One paper suggested that make could detect

female ovulation by vagina testing behavior, however, my data comparing the timing of serial

copulation occurred and the giving-birth date of the females suggested that more than half of

copulations occurred in non-fertileable period (unpublished data). At least, to human observers,

female's estrus signals are totally undetectable, however, it's still possible that males are using

some cues which human cannot detect.

        Daily observations

        AT performed the 21-month field observations for the five groups, between September 25, 2015

        to June 15, 2017. In total, the animals were observed for 289 days (970.7 hours). The monkeys

        were followed daily between 09:00 and 17:00 h; the group that was first encountered each day

        was followed for as long as possible. When the target group could not be followed further (e.g.,

        when the monkeys travelled along cliffs), the observation of the target group was terminated, and

        another group was seeking out and followed.

        Copulation definitions and analysis

        All copulations during our observation were recorded using video cameras (JVC GZ-RX500 and

        Sony HDR-PJ675) and their descriptions were noted. Here, a single copulation was defined as a

        single event consisting of single mount-insertion-separation irrespective of ejaculation, based on

        the previous report (Estep, Bruce, Johnston, & Gordon, 1984). In total, 433 cases of single

        copulation events were recorded. Next, the occurrence time of a single copulation event was

        measured, and the inter-copulation intervals (ICIs) of all recorded single copulation events that

        occurred multiple times in a day were calculated for defining copulation bout. A "serial

        copulation bout" was defined as the copulation series including more than four single copulation

        events, of which every ICI was less than 30 min (for the rationale of the interval criterion see

        Figure 1). This definition was modified for quantitativeness from the relatively ambiguous

        definition of the previous studies (Brereton, 1994; Estep et al., 1984). The other bout was defined

        as "non-serial copulation bout". For all copulation events and copulation bouts, the IDs of the

        males and females involved were recorded. The observed counts of the copulation events and

        bouts of those involved simultaneously in the same serial copulation bout were determined.

Estimation of parameters

Based on the priority-of-access model (PvS model), we estimated the despotic parameter, β, using nonlinear regression analysis for the count data of copulation events. For strict evaluation of the copulation success, only count data of copulation events with ejaculations were used. Then, the males were descending-sorted by copulation event counts for each group and assigned the "dominance rank"; for example, the male who showed frequent counts of ejaculated copulation event was considered the 1st male in a group. Rank order (i) was fitted to count data (x_i) of copulation events based on the formula (1) or (2) of the PvS model using the nonlinear regression function of Python (curve_fit method in SciPy optimize module). In addition, R^2 values were reported for showing the goodness-of-fitting.

Mathematical model

To understand the logic behind the novel male-male coalition identified in stump-tailed macaques, we developed a simple mathematical model based on the framework developed by Pandit and van Schaik (Pandit & van Schaik, 2003). Our motivation for the mathematical modeling was two-fold. First, it is intuitively conceivable that concealed ovulation, as in stump-tailed macaques, hinders the alpha male from guarding all fertilizations, and thus necessitates collaboration of two or more dominant males for reproductive monopoly. However, it is unclear as to whether and under what circumstances the alpha male tolerates one or more allies copulating with females. Second, we have observed within-species variation in the occurrence of male-male coalition in stump-tailed macaques: it occurs in the Ting, Nadam, and Fourth groups,

but not in the Third and Wngklm groups (see Figure 2). If our model for the underlying logic of

male-male coalition is correct, it should also explain this pattern of within-species variation.

We considered a group of N males and a constant number of females. In the case of a

linear order of dominance among the males, the relative access of the ith male to females, x_i, in

the absence of male-male coalition is described by the priority-of-access model (Altmann, 1962),

namely,

$$x_i = (1 - \beta)^{i-1} x_1, \quad (1)$$

where β represents the degree to which dominant males can monopolize mating opportunities

$(0 < \beta < 1)$.

Ecological and demographic factors have been suggested to affect β (Van Schaik et al.,

2006). Of these, cryptic ovulation in females probably reduces β as it prevents dominant males

from guarding each female intensively only during her fertile periods. Thus, compared to species

in which ovulation is advertised, species with cryptic ovulation are expected to have small β. In

contrast, other factors, such as the number of females in the group, the relative strengths of

dominant males, and the female preference for or against dominant males, are also likely to

affect β. As the latter factors may vary within a species, we expect that different groups of

stump-tailed macaques are characterized by different β values.

In groups with relatively small β, it may be beneficial for top-ranking males to form a

novel type of coalition in which allied males guard potentially fertile females in a collaborative

manner to exclude subordinate males from copulation opportunities, which are then

simultaneously shared among the allies. This type of coalition may be represented by the

following equation:

$$x_i = (1 - s\beta)^{i-1} x_1, \quad (2)$$

where we assume $1 < s < 1/\beta$. Parameter s reflects the effect of male-male coalition to

"steepen" the male reproductive skew, where larger s indicates higher reproductive

monopolization by dominant males. It should be emphasized that our parameter s differs from α,

the similar parameter in Pandit and van Schaik's (2003) model, which considered the effect of

coalition among subordinate males to "level" the reproductive skew (i.e., $0 \le \alpha \le 1$). As this

type of male-male coalition is by definition conservative (Chapais, 1995) or all-down (van

Schaik et al., 2004), it is always feasible as no single male outside the coalition can prevent it

from occurring (Pandit & van Schaik, 2003).

To evaluate the profitability of a male-male coalition, the cost and benefit of coalition

formation has to be defined. We considered two components of a particular male's fitness: the

ratio of the mating opportunities gained by that male to all the mating opportunities, and the cost

of coalition associated with the additional effort of collaborating with others. As for the first

component, y_i denotes the proportion of mating opportunities obtained by the ith male among all

matings; in other words,

$$y_i = \frac{x_i}{\sum_{j=1}^{N} x_j}. \quad (3)$$

244 From (1) and (2), in the absence of male-male coalition, we obtain

$$y_i = \frac{\beta(1-\beta)^{i-1}}{1-(1-\beta)^N}, \quad (4)$$

245 while in the presence of coalition,

$$y_i = \frac{s\beta(1-s\beta)^{i-1}}{1-(1-s\beta)^N}. \quad (5)$$

246 Regarding the second component, we assume that the first components of males forming a

247 coalition are multiplied by $1-c$, where c represents the cost of coalition ($0 < c < 1$), while

those of non-coalition males are multiplied by 1. Therefore, for the ith male, joining a coalition

is profitable if and only if

$$\frac{s\beta(1-s\beta)^{i-1}}{1-(1-s\beta)^N}(1-c) > \frac{\beta(1-\beta)^{i-1}}{1-(1-\beta)^N}, \quad (6)$$

or equivalently,

$$\left(\frac{1-s\beta}{1-\beta}\right)^{i-1} > \frac{1}{s(1-c)}\frac{1-(1-s\beta)^N}{1-(1-\beta)^N}. \quad (7)$$

As $1-s\beta < 1-\beta$, the left-hand side of (7) decreases with increasing i; thus, whenever (7)

holds for the mth male ($m \geq 2$), it also holds for the first to $m-1$th males.

Therefore, from (7), we derive the upper boundary of coalition size, m^*, for specific β,

N, s, and c as

$$m^* = 1 + \frac{\log[s(1-c)] - \log\dfrac{1-(1-s\beta)^N}{1-(1-\beta)^N}}{\log\dfrac{1-\beta}{1-s\beta}}. \quad (8)$$

Equation (8) immediately shows that $s(1-c) > 1$ is necessary for any coalition to be viable;

otherwise, $m^* < 1$ always holds. It also shows that the right-hand side of (8) increases with N

(Figure 2a, 2b). For large N, the upper boundary of the coalition size is obtained approximately

using

$$m^* \approx 1 + \frac{\log[s(1-c)]}{\log\dfrac{1-\beta}{1-s\beta}}, \quad (9)$$

which decreases with increasing β whenever $s(1-c) > 1$. On the other hand, when β is small,

(8) is approximated by

$$m^* \approx 1 + \frac{\log(1-c)}{\log[1+(s-1)\beta]}, \quad (10)$$

261   indicating that as β approaches zero, m^* diverges to minus infinity. In general, however, the

262   dependence of m^* on β is not monotonic (Figure 2c, 2d).

263   For coalition of at least two males (i.e., $m^* > 2$), (9) shows that β should be smaller than

264   a threshold, specified by

$$\beta < \frac{s(1-c)-1}{s^2(1-c)-1}. \quad (11)$$

265   Hence, for any coalition to occur, β has to be relatively small, but not extremely small. Figure 5

266   illustrates the combinations of N and β values, for which $m^* > 2$ (based on (8)).

Figure 2. The dependence of the upper bound of coalition size, m^*, on the number of males, N, and the extent to which dominant males monopolize matings and/or fertilizations, β, in the absence of coalition formation. The solid and broken curves represent m^* for s=1.1 and s=1.2, respectively. The upper bound increases and approaches the right-hand side of (9) as N increases (a, b), while the dependence of m^* on β is non-monotonic (c, d). For all panels, c=0.05. (a) β=0.1, (b) β=0.3, (c) N=10, (d) N=40.

Ethics approval

All data acquisitions and procedures during the fieldwork were approved by the National

Research Council of Thailand (NRCT, Permission No. 0002/6910) and the Department of

National Parks, Wildlife and Plant Conservation of Thailand (DNPT). We also complied with the

guidelines for field studies of the Primate Research Institute, Kyoto University.

Conflicts of interest/Competing interests

Authors declare no competing interests.

RESULTS

Behavioral analysis

During our 21 months of field observations, we counted 433 cases of copulations (defined as a

single event consisting of single mount-insertion-separation, see Materials and method section)

from five subject groups (391 individuals consisting of 97 adult males, 124 adult females, 114

infants ($\leq$ 2 years), and 56 subadult unidentified subjects (see Toyoda et al 2018). The inter-

copulation intervals (ICI) of all recorded single copulation events that occurred multiple times

between the female and male(s) in a day ($N_{ICI} = 206$) were measured; the median with ranges of

ICI were 7 (0−359) min (Figure 3), and 95% events occurred within 30 min ICI. We defined the

serial copulation bout as the copulation series including more than four single copulation events,

of which every ICI was less than 30 min, which partially followed the definitions of the previous

study (Brereton, 1994; Estep et al., 1984) (for details, see Materials and method section). Out of

the 433 copulation events, 213 (49.2 %) cases occurred in serial copulation bouts, i.e., repeated

single mount-insertion-separation copulation event with one female recipient partner. In contrast,

220 (50.8%) cases occurred as non-serial copulations. In total, 26 serial copulation bouts

(number of single copulation events with ejaculation per bout, median: 6.0 times; range: 1–31

times) were recorded in the five-subject groups (Ting group: 9 times; Nadam: 4; Third: 5;

Fourth: 6; Wngklm: 2, for details see Table S2 and Figure S1 in Supplementary Materials). Thus,

almost 50% of single copulation events occurred as a part of the serial copulation bout. The

seven cases of serial copulations in the Third and Wngklm groups were of alpha males (named

TRD-M01 and WKM-M01 for Third and Wngklm groups, respectively), i.e., one male

maintained the proximity to females and was involved in most of the copulations. In total, we

recorded 80 copulations include 68 ejaculatory copulations (81.8% of all copulation occurrences,

86.1% of all ejaculated copulation) of TRD-M01, and 26 copulations 22 ejaculatory copulations

(59.1%, 78.6%) of WKM-M01 as well, indicating their monopoly over copulations (Figure 2, see

"alpha-male-monopoly type).

In contrast, the serial copulation patterns of the Ting, Nadam, and Fourth groups

differed from those of the Third and Wngklm groups (Figure 4, see "coalition" type).

Interestingly, we observed that multiple males were involved in a single serial copulation bout;

each of the males first performed the single mount-insertion-separation copulation event several

times and the other male(s) maintained close proximity to the copulating male-female pair

without any agonistic interaction, after which the males serially changed positions as copulators

(Figure 4). These multi-male serial copulation bouts were observed 26 times in total (Table S2).

Six, two, and three males were involved in the multi-male serial copulations for the Ting, Nadam

and Fourth groups, respectively. The number of bouts where two males were involved

simultaneously was 10, while the number for those involving three males was 16 (Table S2).

Serial copulation bouts involving four or more males were never observed. The membership of

the males involved in the multiple serial copulations was stable; the same male members were

always involved in maintaining close proximities and participating in the copulations (Table S2).

Consequently, male members, who were tolerant of each other's approaching a female,

dominantly occupied the copulatory opportunities; 108 (93.1%), 30 (96.8%), and 68 (95.8%)

copulations were recorded for the Ting, Nadam, and Fourth groups, respectively (Table S2,

Figure 4). The occupancy rates of copulations for the coalition were apparently higher than those

of non-coalition males. Thus, we concluded that the males formed a stable coalition for sharing

copulation opportunities.

Figure 3. Occurrences of the inter-copulatory event intervals (ICIs) of all recorded single

copulation events occurred multiple times in a day (N_ICI=206). Note that the cases of only one

copulation within a day were excluded for the calculations of ICIs because the intervals should

be defined by the two consecutive events.

Figure 4. Ratios of copulation events (with an ejaculation) for social status, i.e., coalition males

(coalitions), males outside of coalitions in a group (non-coalitions), a male solely dominating

copulations (alpha), and non-group member males (out-group), for each group.

Mathematical modeling analysis

Our mathematical modeling analysis indicates the presence of conditions under which formation

of a coalition by the top-ranking males with other males to guard and share mating opportunities

might be beneficial. Hence, we have established a theoretical basis for the occurrence of the

novel male-male competition observed in stump-tailed macaques. Regarding the within-species

variation in the occurrence of male-male coalition, two qualitative predictions were derived: first,

a large coalition is more likely to be observed in larger male groups (Figure 5); second, among

sufficiently large male groups, a coalition is more likely to occur in a group where the extent of

reproductive monopolization by dominant males is relatively small, unless it is extremely small

(Figure 5).

Figure 5. Combinations of N∈[1,30] and $\beta \in (0,1)$ values for which coalition of more than two

males is possible (i.e., m^*>2) for several parameter s and c (see plot titles). Each contour

represents the coalition size (m^*>2).

We evaluated the above predictions for within-species variation on the basis of our

observational data from the five groups of stump-tailed macaques. For each group, we estimated

β', which denotes either β in (1) or $s\beta$ in (2) based on whether male-male coalition is absent (Third, Wngklm) or present (Ting, Nadam, Fourth), respectively. For this purpose, the observed number of copulations in which ejaculation is confirmed for the ith male is used as the observed value of x_i. β' is estimated using the means of non-linear fitting of (1) or (2) to the observations (Figure 6). Figure 7 shows the estimates of β' and the numbers of males, N, in the five groups. It is to be noted that the vertical axis represents $s\beta$ for Ting, Nadam, and Fourth, such that β in these groups without male-male coalition will be lower than these values. Consistent with the model predictions, the Ting group, in which the largest coalition ($m = 6$) was observed, had the combination of the largest N and the smallest β' (and thus β) among the five groups. In addition, as predicted, Fourth ($m = 3$) and Nadam ($m = 2$), the two other groups in which coalitions were observed, have the second and third lowest values of β' (and thus β), respectively. On the other hand, male-male coalition is absent in the Third group with the second largest N, which might appear to contradict our predictions. We tentatively interpret this as a result of large β' in this group; in other words, β may be too large to satisfy (11), although a quantitative evaluation of this claim has been challenging so far. In sum, we concluded that our model accounts well for the patterns of within-species variation in the male-male coalition observed in stump-tailed macaques.

Figure 6. Nonlinear fitting of copulation occurrences with copulation success ranks. The formula

in the plot area shows the estimated parameters, and plot title showed the R^2.

Figure 7. The estimates of β' and the numbers of males, N, in the five groups.

DISCUSSION

To the best of our knowledge, this is the first mammalian observation of collaborative mate guarding by males, followed by facultative sharing of mating opportunities. Males in other species, such as chimpanzees, olive baboons, and lions, also collaborate to guard females against other males. The "cooperative mate guarding by coalition males" in these species appear to be similar to those in the stump-tailed macaque; however, they fundamentally differ in social relationships between/among coalition allies or non-allies. The stump-tailed macaque forms multi-male multi-female societies, which includes a large number of males in the group, among

which only certain individuals tolerate sexual competition and show exclusive attitude toward

others. Male allies in a coalition exclude rivals and then share the mating opportunities with each

other. Thus, coalitions of stump-tailed macaques act as dominant males' strategy for overcoming

reproductive competition within a group, by sharing the mating opportunities, as well as by

excluding other rivals. In the case of lions, a pride is the unit of a group, which mainly consists

of females and only few males, who collectively defend the females from other invasive males.

This is similar to coalitions of stump-tailed macaques, although alpha (the highest ranking) males

mostly monopolize the mating opportunities, whereas subordinate allies may either have no

access to the females or are allowed limited number of copulations, albeit not through active

sharing. Similarly, olive baboons are a well-known species forming male-male "coalition for

reproduction" but differ from the stump-tailed macaques regarding the formation of coalitions.

The subordinate baboons form a coalition to jointly attack the dominant male, thereby increasing

their future access to females, while not showing any active sharing of copulations. The

observations made with one chimpanzee group might be comparable to our observations

regarding the stump-tailed macaque, where active sharing copulation (a female copulated with 8

males within a short period) was observed (Watts, 1998). However, these were considered

exceptions only in the Ngogo population, which are considerably larger than the other

populations (Watts, 1998).

In stark contrast, stump-tailed macaques showed active sharing of mating opportunities

that they jointly obtain among the male allies. In this novel type of coalition, the alpha male

appeared to pay a reproductive cost by giving mating opportunities away to benefit his allies, and

the subordinate males in return repay in terms collaborative work efforts, as a result of which

they gain reproductive advantage as a team. Furthermore, the cooperation among three males is

another novel feature. Generally, coalition formation has been observed in the context of aggression, characterized by triadic relations, such as the attacker, attack recipient, and supporter. In the cognitive aspect, coalition formation may require higher abilities of social cognition, termed "triadic awareness" (Harcourt, de Waal, & others, 1992; Paxton et al., 2010; Schino, Tiddi, & Di Sorrentino, 2006; Silk, 1999), where the individual must recognize not only the dyadic relationship between two individuals, but also the relationships with other individuals (Hemelrijk, Puga-Gonzalez, & Steinhauser, 2013). The collaboration among three individuals, which is rarely observed in non-human animals, may require the more expanded capacity of social cognition in this species. Hence, we consider coalition formation in stump-tailed macaques as a unique instance of male-male cooperation to achieve reproductive gain, which we believe is rare in non-human animals.

Why do male stump-tailed macaques, unlike males of closely related species, exhibit this peculiar behavior? To put it in another way, what are the socio-ecological factors in stump-tailed macaques that may have favored the evolution of this behavior? Here, we tentatively hypothesize that the absence of signs of ovulation in female stump-tailed macaques is key to understanding the evolution of male-male coalition, followed by facultative sharing. In many primate species, the females exhibit visual or olfactory signs of ovulation during the fertile period of the reproductive cycle. Conspicuous estrous signals such as sexual swellings enhance male-male competition, providing females more opportunities for mate choice (C. L Nunn, van Schaik, & Zinner, 2001; Charles L. Nunn, 1999; Zinner, van Schaik, Nunn, & Kappeler, 2004). Advertisement of female reproductive status is often seen in Old World monkeys living in multi-male multi-female societies, such as most macaques, baboons, and chimpanzees (C. L Nunn et al., 2001; Charles L. Nunn, 1999; Zinner et al., 2004). When female reproductive status is

advertised, it is relatively easy for the alpha male to monopolize fertilizations, as in that case he
can concentrate all his guarding efforts on the females fertile at that moment. On the other hand,
when female ovulation is cryptic, the alpha male is no longer able to adopt the selective guarding
strategy, and reproductive monopoly is only possible if all cycling females are guarded all the
time. Our hypothesis is that the difficulty in establishing reproductive monopoly by the alpha
male due to concealed ovulation may have promoted coalition formation of top-ranking males.
Despite the low copulating frequency, it is surprising that the males adopt a strategy to efficiently
monopolize and share the copulating opportunities—a critical reproductive resource—among
multiple coalition males.

Our discovery of male-male coalition, followed by active sharing of mating opportunities
in stump-tailed macaques, demands a revision of the existing socioecological models in primate
social systems. To the best of our knowledge, this is the first documented case in non-human
primates of non-kin collaborative effort for acquiring resources based on active sharing among
allies. We have hypothesized that the lack of estrous signs in female stump-tailed macaques,
unlike many Old-World monkeys, is a key factor enhancing male-male coalition coupled with
active sharing. Concealed ovulation is likely to reduce the extent to which fertilizations are
monopolized by dominant males. In our mathematical model, this effect is represented by the
reduction in parameter β. The model predicts that male-male coalition is more likely to occur
when β is small, confirming the logical consistency of our hypothesis. From the female's
perspective, monopolization by dominant males is indicative of limited opportunities for females
to select mates, particularly when they prefer copulations with subordinate or out-group males.
Thus, concealed ovulation may be considered as a female strategy to facilitate mate choice.
Further extending the argument, the formation of coalition followed by active sharing of mating

opportunities may be a counter strategy of dominant males. In other words, being unable to control female reproduction on his own, the alpha male may be better suited surrendering some fertilization opportunities to elicit cooperation by subordinates. Hence, the intensified sperm competition in stump-tailed macaques may be a joint consequence of female concealment of fertility states and male sharing of mating opportunities. In addition, a potentially relevant observation is that female stump-tailed macaques do not produce copulation calls (Blurton Jones & Trollope, 1968). Although the function of female copulation calls is still a matter of contention (Bernstein, Sheeran, Wagner, Li, & Koda, 2016; Maestripieri & Roney, 2005), a possible interpretation is that female stump-tailed macaques do not make any effort to induce male mate guarding.

The present study has also revealed the importance of the number of males in a group as a predictor for the formation of copulation coalitions among dominant males. In other words, male-male coalition is more likely to be formed when there are more males in a group. In our field site, we observed five groups of stump-tailed macaques consisting of 391 individuals, or on an average 78.2 individuals per group. The relatively large group size is primarily due to the semi-provisioning conditions in our study site, and this factor also appears to affect the socioeconomic sex ratio, i.e., the ratio of the number of adult females to the number of adult males. The average socioeconomic sex ratio in our sample is 1.33, while those that have been previously reported for other populations of stump-tailed macaques are approximately 5.7 (Fooden, 1990). The smaller socioeconomic sex ratio indicates more intense male-male contest. Hence, both large number of males per group and small socioeconomic ratio may have facilitated the occurrence of coalition formation by dominant males in our study population.

Per our observational data, the coalition sizes were two or three, but did not exceed four;

however, our current model predicts the monotonic increase of the coalition size over four,

depending on the number of males in a group. This "discrepancy" might indicate three as the

limit of the coalition size in non-human animals. Actually, psychological experiments on

cooperative tasks revealed possibilities of collaboration by two or three subjects, but difficulties

were encountered with four or more subjects even in chimpanzees, probably due to the

limitations of social cognition. For the recognition of quadradic relations, an individual has to

recognize the possible combinations of dyadic and triadic relations, exponentially increasing the

socio-cognitive loading in the brain. Thus, such a socio-cognitive background might limit the

coalition size in stump-tailed macaques. In contrast, humans have evolved a hyper-cooperative

manner beyond the triadic allies, as suggested by the Machiavellian intelligence hypothesis.

We have also observed within-species variation to the extent to which copulations are

monopolized by dominant males, which is represented by β in our model. Despite the marked

ecological similarities between groups, the estimated β' ranged from 0.30 to 0.97. In the Third

($\beta' = 0.97$) and Wngklm ($\beta' = 0.78$) groups, copulations were almost completely monopolized

by the alpha males, a situation that is called "despotic." This contrasts with the conventional

classification of primate societies, in which stump-tailed macaques are characterized as having

"egalitarian" societies (Matsumura, 1999), or class 3 social systems (Thierry, Singh, &

Kaumanns, 2004). The traditional classification intends to place each species on a single position

on the despotic-egalitarian spectrum, based largely on the species-level characterizations of

ecological factors, such as whether or not a given species is seasonal breeder, or the abundance

and spatial distribution of food resources (Sterck, Watts, & van Schaik, 1997). However, our

observations clearly suggest that the level of despotism as indicated by β is determined not

necessarily in such a top-down manner, but in a more bottom-up way, such that it may vary

within species according to the idiosyncrasies of each group. For example, our field observation

indicates that the despotic nature of the Third group may have been caused not only by the

physical strength of the alpha male, THR-M01, but by the absence of competent rivals; in fact,

other males seem either too old or immature to challenge him. Therefore, it appears that bottom-

up mechanisms determine β in each group, which then determines whether the alpha male will

adopt the solo monopolization strategy or the coalition strategy.

Finally, our model predicts the future dynamics in the stump-tailed macaque groups. For

example, when youngsters in the Third group become sufficiently mature to challenge the alpha

male, and as a consequence β is reduced, our model predicts that the alpha male will form

coalition with other males. We expect that a longitudinal observation of wild stump-tailed

macaques will confirm these model predictions. In conclusion, stump-tailed macaques are

characterized by societies ranging from despotism to egalitarianism, and from monopolization of

females by a dominant male to male-male coalition coupled with active sharing of mating

opportunities. Future studies on wild stump-tailed macaques may shed new light on the origins

and evolution of altruism and cooperation in mammalian societies, including the hyper-

cooperation in human societies.

CONCLUSION

We reported a novel type of animal coalition as a part of male copulatory strategy, and simulated

the phenomenon using a mathematical model. We observed novel types of coalitions in wild

stump-tailed macaques; multiple males actively shared the mating opportunities. Our

mathematical simulations revealed that lack of estrous signs, as well as large numbers of males
in a group, possibly enhanced facultative sharing of females.

ACKNOWLEDGEMENTS

We thank Warayut Nilpaung and Chuchat Choklap, Phanlerd Inprasoet, Wanchai Inprasoet,
Napatchaya Techaatiwatkun, Yuzuru Hamada, Ikuma Adachi, Takeshi Nishimura, Ikki Matsuda
for their kind support. We got funding from JSPS KAKENHI (#16H04848 to HK, #16J0098 to
AT), Young Science Explorer Grant of National Geographic Foundation for Science and
Exploration – Asia (to AT), Kyoto University Foundation (to AT), the Cooperation Research
Programs of Wildlife Research Center (to AT), Japan Science and Technology Agency Core
Research for Evolutional Science and Technology 17941861 (#JPMJCR17A4), and Ministry of
Education, Culture, Sports, Science and Technology, Grant-in-Aid for Scientific Research on
Innovative Areas #4903 (Evolinguistic) 17H06380 to HK and 17H06381 to YI.

APPENSICS

We have Tables S1, S2, and Figure S1 in Supplementary Materials as separately attached.

REFERENCES

Altmann, S. A. (1962). A field study of the sociology of rhesus monkeys, Macaca mulatta.
Annals of the New York Academy of Sciences, *102*(2), 338–435.
https://doi.org/10.1111/j.1749-6632.1962.tb13650.x

Axelrod, R., & Hamilton, W. (1981). The evolution of cooperation. *Science*, *211*(4489), 1390–

1396. https://doi.org/10.1126/science.7466396

Bernstein, S. K., Sheeran, L. K., Wagner, R. S., Li, J.-H., & Koda, H. (2016). The vocal

repertoire of Tibetan macaques (Macaca thibetana): A quantitative classification.

American Journal of Primatology, *78*(9), 937–949. https://doi.org/10.1002/ajp.22564

Blurton Jones, N. G., & Trollope, J. (1968). Social behaviour of stump-tailed macaques in

captivity. *Primates*, *9*(4), 365–393.

Brereton, A. R. (1994). Copulatory behavior in a free-ranging population of stumptail macaques

(Macaca arctoides) in Mexico. *Primates*, *35*(2), 113–122.

https://doi.org/10.1007/BF02382048

Burkart, J. M., Allon, O., Amici, F., Fichtel, C., Finkenwirth, C., Heschl, A., … van Schaik, C.

P. (2014). The evolutionary origin of human hyper-cooperation. *Nature Communications*,

5(1), 4747. https://doi.org/10.1038/ncomms5747

Chapais, B. (1995). Alliances as a means of competition in primates. *American Journal of*

Physical Anthropology, *38*, 115–136.

Estep, D. Q., Bruce, K. E. M., Johnston, M. E., & Gordon, T. P. (1984). Sexual Behavior of

Group-Housed Stumptail Macaques (Macaca arctoides): Temporal, Demographic and

Sociosexual Relationships. *Folia Primatologica*, *42*(2), 115–126.

https://doi.org/10.1159/000156154

Fooden, J. (1990). The bear macaque,Macaca arctoides: a systematic review. *Journal of Human*

Evolution, *19*(6–7), 607–686. https://doi.org/10.1016/0047-2484(90)90002-S

Hamilton, W. D. (1964). The genetical evolution of social behaviour. II. *Journal of Theoretical*

Biology, *7*(1), 17–52. https://doi.org/10.1016/0022-5193(64)90039-6

Harcourt, A. H., de Waal, F. B. M., & others. (1992). *Coalitions and alliances in humans and*

other animals. Oxford University Press Oxford.

Hemelrijk, C. K., Puga-Gonzalez, I., & Steinhauser, J. (2013). Cooperation, Coalition, and

Alliances. In *Handbook of Paleoanthropology* (pp. 1–27). Berlin, Heidelberg: Springer

Berlin Heidelberg. https://doi.org/10.1007/978-3-642-27800-6_43-4

Kutsukake, N., & Nunn, C. L. (2006). Comparative tests of reproductive skew in male primates:

the roles of demographic factors and incomplete control. *Behavioral Ecology and*

Sociobiology, *60*(5), 695–706. https://doi.org/10.1007/s00265-006-0213-1

Maestripieri, D., & Roney, J. R. (2005). Primate copulation calls and postcopulatory female

choice. *Behavioral Ecology*, *16*(1), 106–113. https://doi.org/10.1093/beheco/arh120

Matsumura, S. (1999). The evolution of "egalitarian" and "despotic" social systems among

macaques. *Primates*, *40*(1), 23–31. https://doi.org/10.1007/BF02557699

Nunn, C. L, van Schaik, C. P., & Zinner, D. (2001). Do exaggerated sexual swellings function in

female mating competition in primates? A comparative test of the reliable indicator

hypothesis. *Behavioral Ecology*, *12*(5), 646–654. https://doi.org/Article

Nunn, Charles L. (1999). The evolution of exaggerated sexual swellings in primates and the

graded-signal hypothesis. *Animal Behaviour*, *58*(2), 229–246.

https://doi.org/10.1006/anbe.1999.1159

Pandit, S. A., Pradhan, G. R., & van Schaik, C. P. (2020). Why Class Formation Occurs in
Humans but Not among Other Primates: A Primate Coalitions Model. *Human Nature*,
31(2), 155–173. https://doi.org/10.1007/s12110-020-09370-9

Pandit, S. A., & van Schaik, C. P. (2003). A model for leveling coalitions among primate males:
toward a theory of egalitarianism. *Behavioral Ecology and Sociobiology*, *55*(2), 161–168.
https://doi.org/10.1007/s00265-003-0692-2

Pandit, S. A., & Van Schaik, C. P. (2003). A model for leveling coalitions among primate males:
Toward a theory of egalitarianism. *Behavioral Ecology and Sociobiology*, *55*(2), 161–168.
https://doi.org/10.1007/s00265-003-0692-2

Paxton, R., Basile, B. M., Adachi, I., Suzuki, W. A., Wilson, M. E., & Hampton, R. R. (2010).
Rhesus monkeys (Macaca mulatta) rapidly learn to select dominant individuals in videos of
artificial social interactions between unfamiliar conspecifics. *Journal of Comparative
Psychology*, *124*(4), 395–401. https://doi.org/10.1037/a0019751

Schino, G., Tiddi, B., & Di Sorrentino, E. P. (2006). Simultaneous classification by rank and
kinship in Japanese macaques. *Animal Behaviour*, *71*(5), 1069–1074.
https://doi.org/10.1016/j.anbehav.2005.07.019

Silk, J. B. (1999). Male bonnet macaques use information about third-party rank relationships to
recruit allies. *Animal Behaviour*, *58*(1), 45–51. https://doi.org/10.1006/anbe.1999.1129

Sterck, E. H. M., Watts, D. P., & van Schaik, C. P. (1997). The evolution of female social
relationships in nonhuman primates. *Behavioral Ecology and Sociobiology*, *41*(5), 291–309.
https://doi.org/10.1007/s002650050390

Thierry, B., Singh, M., & Kaumanns, W. (2004). *Macaque societies: a model for the study of social organization* (Vol. 41). Cambridge University Press.

Tomasello, M., & Vaish, A. (2013). Origins of Human Cooperation and Morality. *Annual Review of Psychology*, *64*(1), 231–255. https://doi.org/10.1146/annurev-psych-113011-143812

Toyoda, A., & Malaivijitnond, S. (2018). The First Record of Dizygotic Twins in Semi-Wild Stump-Tailed Macaques (Macaca arctoides) Tested Using Microsatellite Markers and the Occurrence of Supernumerary Nipples. *Mammal Study*, *43*(3), 207–212. https://doi.org/10.3106/ms2017-0081

Toyoda, A., Maruhashi, T., Malaivijitnond, S., & Koda, H. (2017). Speech-like orofacial oscillations in stump-tailed macaque (Macaca arctoides) facial and vocal signals. *American Journal of Physical Anthropology*, *164*(2), 435–439. https://doi.org/10.1002/ajpa.23276

Trivers, R. L. (1971). The Evolution of Reciprocal Altruism. *The Quarterly Review of Biology*, *46*(1), 35–57. https://doi.org/10.1086/406755

van Schaik, C. P., Pandit, S. A., & Vogel, E. R. (2004). A model for within-group coalitionary aggression among males. *Behavioral Ecology and Sociobiology*, *57*(2), 101–109. https://doi.org/10.1007/s00265-004-0818-1

van Schaik, C. P., Pandit, S. A., & Vogel, E. R. (2006). Toward a general model for male-male coalitions in primate groups. In *Cooperation in Primates and Humans* (pp. 151–171). Berlin, Heidelberg: Springer Berlin Heidelberg. https://doi.org/10.1007/3-540-28277-7_9

Van Schaik, C. P., Pandit, S. A., & Vogel, E. R. (2006). Toward a general model for male-male

coalitions in primate groups. In *Cooperation in Primates and Humans: Mechanisms and*

Evolution (pp. 151–171). https://doi.org/10.1007/3-540-28277-7_9

Watts, D. P. (1998). Coalitionary mate guarding by male chimpanzees at Ngogo, Kibale National

Park, Uganda. *Behavioral Ecology and Sociobiology*, *44*(1), 43–55.

https://doi.org/10.1007/s002650050513

Widdig, A., Streich, W. J., & Tembrock, G. (2000). Coalition formation among male Barbary

macaques (Macaca sylvanus). *American Journal of Primatology*, *50*(1), 37–51.

https://doi.org/10.1002/(SICI)1098-2345(200001)50:1<37::AID-AJP4>3.0.CO;2-3

Zinner, D., van Schaik, C. P., Nunn, C. L., & Kappeler, P. M. (2004). Sexual selection and

exaggerated sexual swellings of female primates. In *Sexual Selection in Primates: New and*

Comparative Perspectives (pp. 71–89). https://doi.org/10.1002/evan.10023

FIGURE LEGENDS

Figure 1. The male (FTH-M01) and his ally (FTH-M02) simultaneously engaged in the

copulation with one female (FHT-F11), not showing any agonistic conflicts between the

two "competitive" males; at that time, one male (right male) mounted over the female

inserting penis, while the other male (left) "waited for his turn", touching the female hinds.

Figure 2. The dependence of the upper bound of coalition size, m^*, on the number of males, N,

and the extent to which dominant males monopolize matings and/or fertilizations, β, in the

absence of coalition formation. The solid and broken curves represent m^* for $s=1.1$ and

$s=1.2$, respectively. The upper bound increases and approaches the right-hand side of (9) as

N increases (a, b), while the dependence of m^* on β is non-monotonic (c, d). For all

panels, c=0.05. (a) β=0.1, (b) β=0.3, (c) N=10, (d) N=40.

Figure 3. Occurrences of the inter-copulatory event intervals (ICIs) of all recorded single

copulation events occurred multiple times in a day (N_ICI=206). Note that the cases of only

one copulation within a day were excluded for the calculations of ICIs because the intervals

should be defined by the two consecutive events.

Figure 4. Ratios of copulation events (with an ejaculation) for social status, i.e., coalition males

(coalitions), males outside of coalitions in a group (non-coalitions), a male solely

dominating copulations (alpha), and non-group member males (out-group), for each group.

Figure 5. Combinations of $N \in [1,30]$ and $\beta \in (0,1)$ values for which coalition of more than two

males is possible (i.e., m^*>2) for several parameter s and c (see plot titles). Each contour

represents the coalition size (m^*>2).

Figure 6. Nonlinear fitting of copulation occurrences with copulation success ranks. The formula

in the plot area shows the estimated parameters, and plot title showed the R^2.

Figure 7. The estimates of β' and the numbers of males, N, in the five groups.