

1 Bidirectional synaptic plasticity rapidly modifies hippocampal representations  
2 independent of correlated activity

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14

## 15 **Abstract**

16 **According to standard models of synaptic plasticity, correlated activity between**  
17 **connected neurons drives changes in synaptic strengths to store associative**  
18 **memories. Here we tested this hypothesis *in vivo* by manipulating the activity of**  
19 **hippocampal place cells and measuring the resulting changes in spatial selectivity.**  
20 **We found that the spatial tuning of place cells was rapidly reshaped via**  
21 **bidirectional synaptic plasticity. To account for the magnitude and direction of**  
22 **plasticity, we evaluated two models – a standard model that depended on**  
23 **synchronous pre- and post-synaptic activity, and an alternative model that**

1 **depended instead on whether active synaptic inputs had previously been**  
2 **potentiated. While both models accounted equally well for the data, they predicted**  
3 **opposite outcomes of a perturbation experiment, which ruled out the standard**  
4 **correlation-dependent model. Finally, network modeling suggested that this form**  
5 **of bidirectional synaptic plasticity enables population activity, rather than pairwise**  
6 **neuronal correlations, to drive plasticity in response to changes in the**  
7 **environment.**

8

## 9 **Main Text**

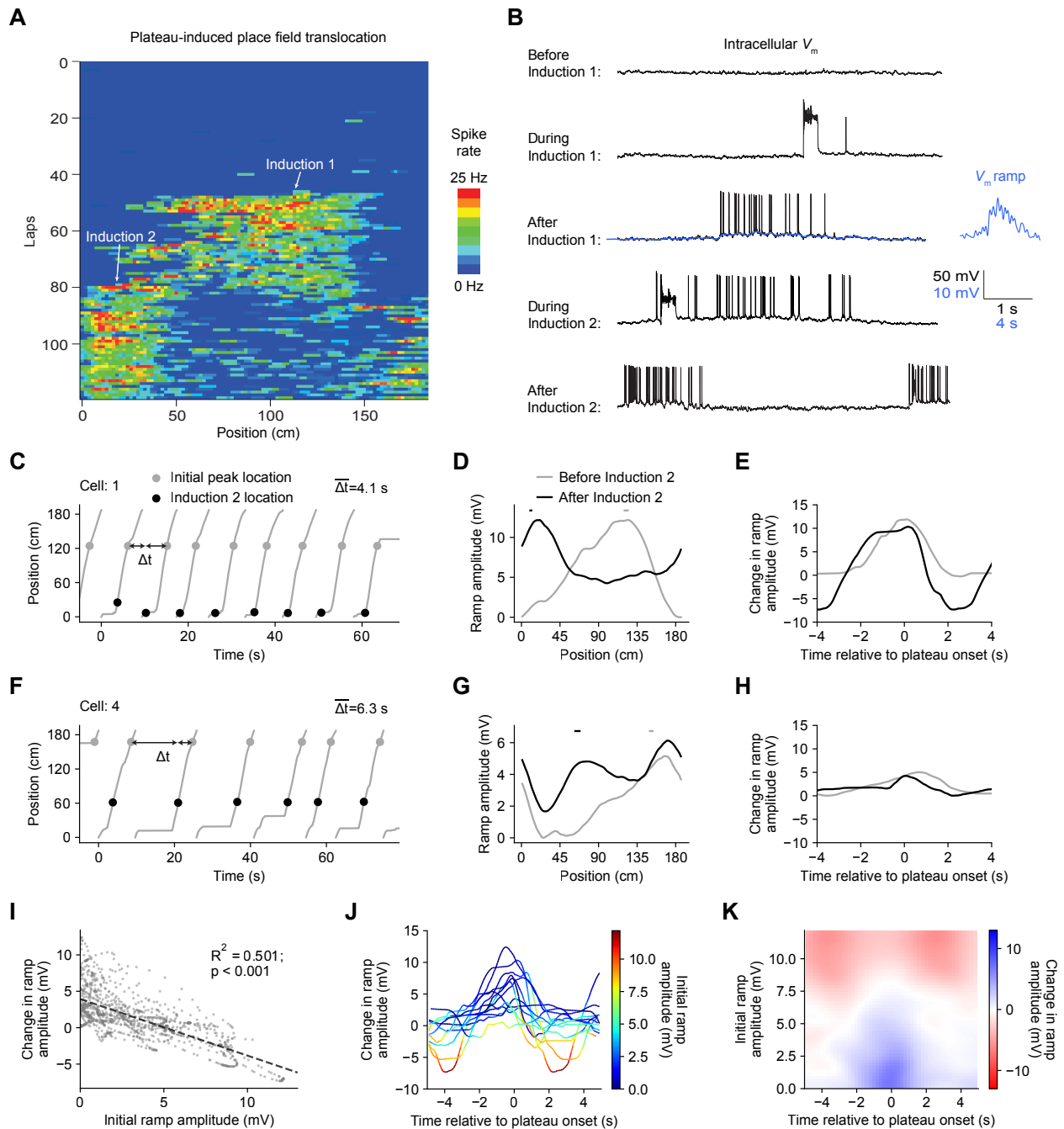
10 Activity-dependent changes in synaptic strength can flexibly alter the selectivity of  
11 neuronal firing for particular features of the environment, providing a cellular substrate for  
12 learning and memory. Various forms of Hebbian synaptic plasticity have been considered  
13 for decades to be the main or even only synaptic plasticity mechanisms present within  
14 most brain regions of a number of species. The core feature of such plasticity  
15 mechanisms is that they are autonomously driven by the repeated presence of correlated  
16 presynaptic and postsynaptic activity that leads to either increases or decreases in  
17 synaptic strength depending on the exact temporal coincidence (1-4).

18       The hippocampus plays an important role in many forms of learning and memory,  
19 and the spatial firing rates of hippocampal place cells have been shown to change with  
20 alterations in environmental context or the locations of salient features, like reward (5-  
21 11). Furthermore in CA1 neurons, place cell activity can emerge in a single trial following  
22 a dendritic calcium spike (also called a plateau potential) (12-14). The form of synaptic  
23 plasticity responsible for this rapid change in selectivity, termed behavioral timescale

1 synaptic plasticity (BTSP), modifies synaptic inputs active within a multi-second time  
2 window around the plateau potential. That BTSP strengthens many synaptic inputs whose  
3 activation did not cause or even coincide with postsynaptic activity suggests that it might  
4 be a fundamentally different form of plasticity than classical correlation-driven Hebbian  
5 plasticity (1-3). Such a plasticity rule could enable representation learning in cortical brain  
6 regions like the hippocampus to be guided by delayed behavioral outcomes, rather than  
7 by short timescale associations of neuronal input and output. However, it was not clear  
8 from previous experiments if short timescale correlations would modulate changes in  
9 synaptic strength induced by BTSP, which may reveal similarities with other correlative  
10 forms of plasticity.

11 In the current study, we sought to directly determine the dependence of BTSP on  
12 the correlation of presynaptic activity and postsynaptic depolarization in individual place  
13 cells. Intracellular voltage recordings from CA1 place cells were established in head-fixed  
14 mice trained to run for a water reward on a circular treadmill decorated with visual and  
15 tactile cues to distinguish spatial positions (187 cm in length). We began by examining  
16 how the induction of BTSP changes the membrane potential ( $V_m$ ) dynamics in neurons  
17 already exhibiting location specific firing (i.e. place cells). To do so we injected brief step  
18 currents (300 ms duration) through the intracellular electrode for a small number of  
19 consecutive laps (5-8 laps; Fig. 1, A to C) to evoke plateau potentials at a second location  
20 along the track some distance from the initial place field (labeled “Induction 2” in Fig. 1, A  
21 to H). We observed that the plasticity induced by experimentally-evoked dendritic  
22 plateaus both increased  $V_m$  ramp amplitude near the plateau induction position, and also  
23 decreased ramp amplitude at the peak location of the original place field (Fig. 1, B and

**Fig 1.**



**Fig. 1. Dendritic calcium spikes translocate hippocampal place fields via bidirectional synaptic plasticity. (A)** Spatial firing of a CA1 pyramidal cell recorded intracellularly from a mouse running laps on a circular treadmill. Dendritic plateau potentials evoked by intracellular current injection first induce a place field at ~120 cm

(Induction 1), then induce a second place field at ~10 cm and suppress the first (Induction 2). **(B)** Black: intracellular  $V_m$  traces from individual laps in **(A)**; blue: example low-pass filtered  $V_m$  ramp superimposed on unfiltered trace, and duplicated with expanded scale (inset). **(C)** Animal position vs. time during laps in which place fields were induced by evoked plateaus (locations marked with colored circles).  $t$  refers to the inter-event intervals between traversals of the initial place field peak location and evoked plateaus. **(D)** Spatially binned subthreshold  $V_m$  ramp depolarizations averaged across laps after plasticity induction. Colored dashes mark the average locations of evoked plateaus. **(E)** For each position, induced changes in  $V_m$  ramp amplitude are plotted against the time interval between plateau onset and traversal of that position during plasticity induction laps. **(F – H)** Same as **(C – E)** for a different example cell in which the amplitude of the original place field was not reduced following the second plasticity induction. **(I)** For all recorded neurons with a pre-existing place field in which plasticity was induced at a second location ( $n=13$ ), changes in ramp amplitude are compared to initial ramp amplitude for each spatial bin (1.87 cm). Induced changes in ramp amplitude are negatively correlated with initial ramp amplitude. Explained variance ( $R^2$ ) and statistical significance ( $p < 0.05$ ) reflect Pearson's correlation and a 2-tailed null hypothesis test. **(J)** For the same neurons as in **(I)**, changes in ramp amplitude are compared to time to plateau onset. Trace color indicates initial ramp amplitude before plasticity induction. **(K)** Two-dimensional Gaussian regression and interpolation of data from all recorded plasticity inductions (20 inductions from 13 cells) was used to estimate the plasticity rule that relates initial ramp amplitude and time to plateau onset to induced changes in ramp amplitude (trace color).

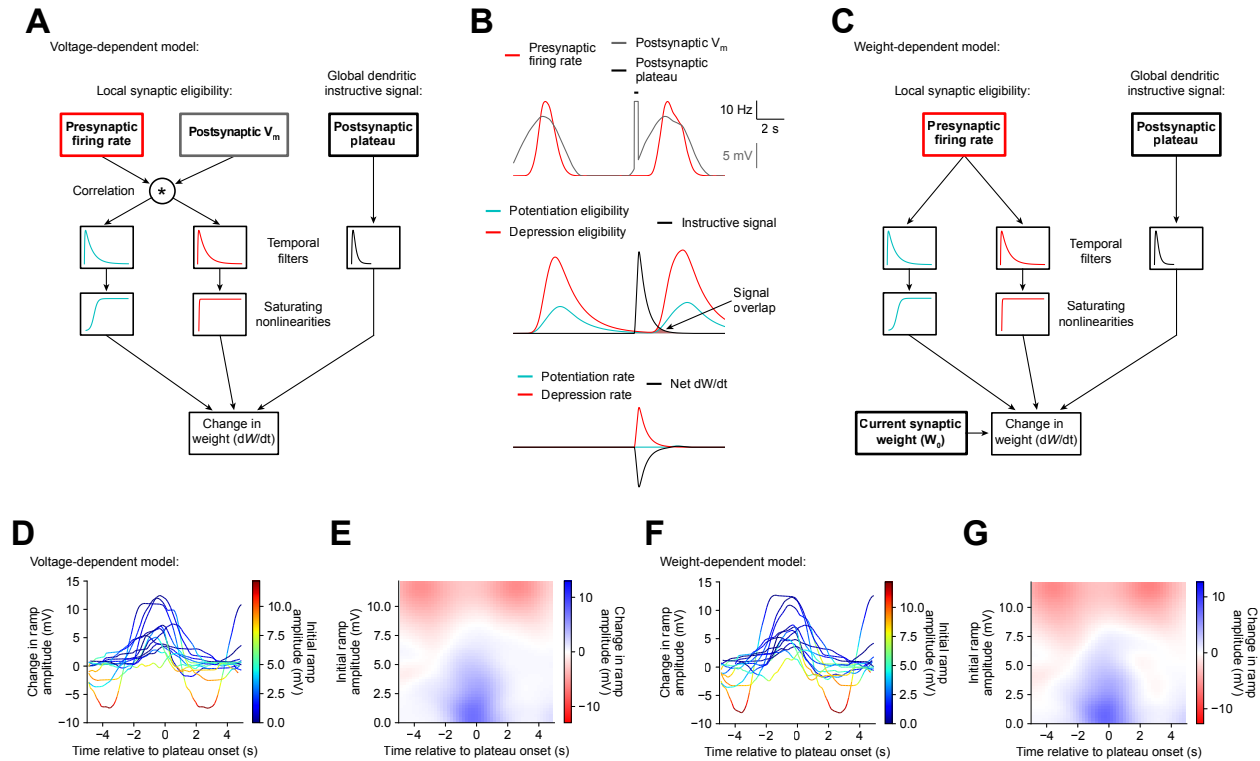
1 D). The time course of the  $V_m$  changes showed that decreases in ramp amplitude  
2 occurred at positions in space that were traversed multiple seconds before or after  
3 induced plateaus (Fig. 1, E and J). Furthermore, the exact magnitude of decreases in  $V_m$   
4 ramp amplitude was greatest at spatial positions where initial ramp amplitude was largest  
5 (Fig. 1I). Interestingly, in a subset of recordings the ramp amplitude at the original place  
6 field location was not reduced (Fig. 1G). Inspection of the animals' run trajectories during  
7 such instances revealed that long pauses in running just before the plateau induction  
8 position on multiple laps "protected" the original place field from depression by excluding  
9 the underlying location-selective inputs from the plasticity time window (Fig. 1, F to H).  
10 When both initial ramp amplitude and relative input timing are considered, it is apparent  
11 that the preferred conditions for large synaptic depression are that spatial inputs 1) have  
12 already been strengthened by previous plasticity, resulting in elevated postsynaptic  
13 depolarization at the time of presynaptic spikes, and 2) are activated within a time window  
14 ~2 – 4 seconds away from a plateau (Fig. 1J, trace color indicates initial ramp amplitude;  
15 Fig 1K; two-dimensional interpolation from data, trace color indicates change in ramp  
16 amplitude, see Materials and Methods). In summary, BTSP can either strengthen or  
17 weaken synapses in a small number of trials, providing a bidirectional learning  
18 mechanism capable of both rapid memory storage and erasure.

19 The above analysis revealed a relationship between initial  $V_m$  ramp amplitude  
20 and bidirectional changes in  $V_m$  depolarization induced by BTSP (Fig. 1, I to K), though  
21 it was inverted compared to most common formulations of correlative plasticity in which  
22 small depolarizations induce synaptic depression and large depolarizations induce  
23 synaptic potentiation (3, 15-17). We next sought to investigate this possible causal

1 relationship between postsynaptic depolarization and plasticity induced by BTSP. First,  
2 we formulated a set of mathematical models of the underlying synaptic learning rule to  
3 generate testable hypotheses and to predict changes in synaptic strength given the  
4 following quantities: presynaptic spike times, postsynaptic depolarization, postsynaptic  
5 plateaus, and the strengths of each synaptic input before each plateau.

6 We compared two classes of plasticity models - a standard model dependent on  
7 coincident presynaptic spiking and postsynaptic depolarization (correlative), and an  
8 alternative model dependent instead on the timing of presynaptic spikes and the  
9 strengths of each synaptic input at the time of activation (non-correlative) (see Materials  
10 and Methods for details). To account for the long time course of BTSP, both models  
11 required temporal filters of synaptic activity to generate slow biochemical intermediate  
12 signals marking synapses as eligible for either synaptic potentiation or depression (local  
13 synaptic eligibility; Fig. 2, A to C; fig. S1, C and D; fig. S2, C and D) (1, 3, 15, 16, 18).  
14 Biologically, these traces could correspond to the enzymatic activity of calcium-  
15 dependent kinases and phosphatases, and post-translational modification and synaptic  
16 localization of proteins that regulate synaptic function (18-23). While in the voltage-  
17 dependent model, the amplitudes of these eligibility signals were modulated by the  
18 value of postsynaptic depolarization at the time of presynaptic activation (Fig. 2A and  
19 fig. S1, A, C and D), in the weight-dependent model (Fig. 2C and fig. S2, C and D),  
20 eligibility for plasticity depended only on presynaptic firing rate. Both models also  
21 required a temporal filter of the plateau potential to generate a second intermediate  
22 signal that extended in time long enough to interact with synaptic activity occurring up to  
23 seconds after a plateau potential (global dendritic instructive signal; Fig. 2, A to C; fig.

**Fig 2.**



**Fig. 2. Two alternative models of bidirectional synaptic plasticity account for**

**measured changes in  $V_m$ .** (A) Diagram depicts a “voltage-dependent” model of

bidirectional BTSP. Three factors influence changes in synaptic strength at each input:

1) presynaptic firing rate and timing, 2) postsynaptic  $V_m$  depolarization at the time of presynaptic spiking, and 3) postsynaptic plateau timing and duration. The product

(degree of correlation) of presynaptic firing rate and postsynaptic depolarization determines the amplitude of long duration “synaptic eligibility signals” that mark each

synapse as eligible for later synaptic potentiation or depression. Synaptic eligibility signals, following an additional nonlinear transformation, are later converted into

changes in synaptic strength when in the presence of a second required “instructive

signal” generated downstream of postsynaptic plateaus. (B) Example traces depict the

signals described in (A) for a single presynaptic input onto a neuron that exhibited a pre-



existing place field before plateau induction. Shown is a single lap on the circular treadmill for a trial in which a plateau was evoked by intracellular current injection. Top: while presynaptic firing at this input (red) does not overlap in time at all with the postsynaptic plateau (black), it does coincide with the spatially-tuned depolarization underlying the cell's initial place field (grey). Middle: this generates long duration eligibility signals (blue: potentiation eligibility; red: depression eligibility) that overlap in time with the delayed instructive signal (black) (shading marks area of signal overlap). Bottom: at this input a large rate of synaptic depression and a small rate of synaptic potentiation result in a net decrease in synaptic strength. **(C)** Diagram depicts an alternative “weight-dependent” model of bidirectional BTSP. Three factors influence changes in synaptic strength at each input: 1) presynaptic firing rate and timing, 2) postsynaptic plateau timing and duration, and 3) the current synaptic weight of each input before each evoked plateau. In this model, synaptic eligibility signals depend only on presynaptic firing. Like in (A), a plateau-related instructive signal is required to convert synaptic eligibility signals into changes in synaptic weight. However, in this model, the current weight of each input influences the magnitude and direction of synaptic plasticity such that weak synapses favor potentiation, and strong synapses favor depression. **(D)** The voltage-dependent model was optimized to generate predicted ramp depolarizations for each neuron in the experimental dataset (20 inductions from 13 neurons). Changes in ramp amplitude are compared to time to plateau onset, with color indicating initial ramp amplitude (compare to Fig. 1J). **(E)** Estimate of plasticity rule obtained by regression and interpolation of model simulation data (compare to Fig. 1K). **(F – G)** Same as (D – E) for the weight-dependent model.

1 S1, C and D; fig. S2, C and D). This plateau-related “instructive signal” was broadcast  
2 globally to all synapses, and was required for plasticity. Changes in synaptic weight in  
3 the models occurred only during periods of temporal overlap between localized eligibility  
4 signals and the global instructive signal (Fig. 2B; fig. S1, C and D; fig. S2, C and D).

5 Model parameters (fig. S3, A to K and fig. S4, A to K, see Materials and Methods)  
6 were optimized by minimizing the difference between measured and predicted  $V_m$  ramp  
7 depolarizations. Both model variants generated predictions in good agreement with  
8 experimental data (fig. S3, L to O; fig. S4, L to O; and fig. S5), which underscores the  
9 importance of the components common to both models – long timescale intermediate  
10 signals downstream of synaptic activation that are transformed into bidirectional changes  
11 in synaptic weight by dendritic plateau potentials. However, the two models made  
12 qualitatively different predictions about the causal role of the activation state of the  
13 postsynaptic neuron in controlling the magnitude and direction of plasticity. While in the  
14 voltage-dependent model, correlation between presynaptic activity and postsynaptic  
15 depolarization influences the sign of plasticity, in the alternative model, the sign of  
16 plasticity is independent of postsynaptic voltage, and is modulated instead by current  
17 synaptic weight such that weak synapses tend to potentiate and strong synapses tend to  
18 depress (3, 24-29).

19 We next sought to distinguish between the two model classes with an *in vivo*  
20 perturbation experiment where neuronal  $V_m$  was experimentally depolarized by  
21 intracellular current injection during plasticity induction trials. In otherwise silent CA1  
22 neurons exhibiting no spatial tuning or spiking during treadmill running, we injected  
23 current through the intracellular recording pipette to depolarize the neuron at steady-state

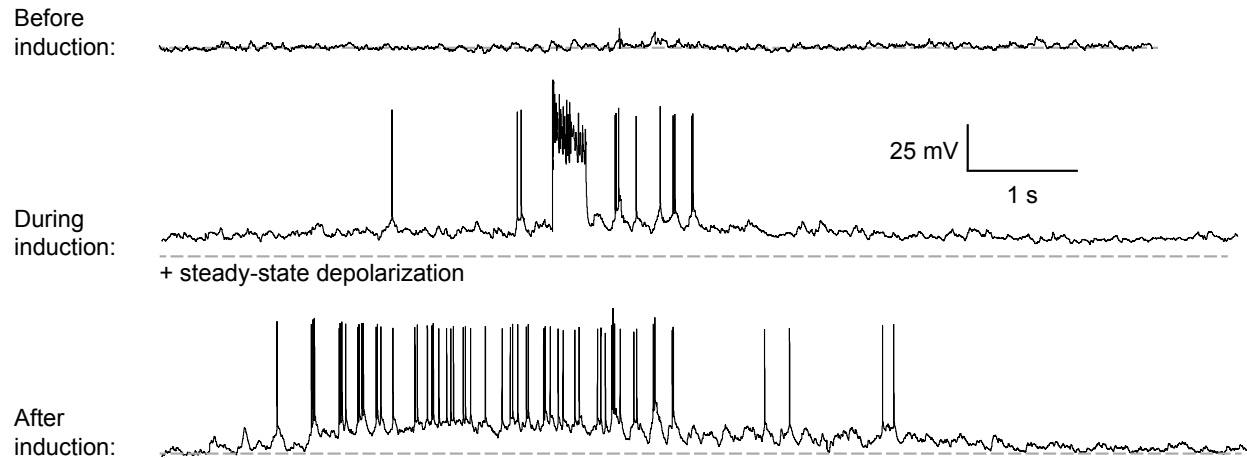
1 by ~10 mV, which often exceeded threshold for spiking (Fig. 3A; see fig. S6, A to C for  
2 simulation results supporting significant dendritic depolarization during this manipulation).  
3 Then, for 4 – 5 consecutive laps, plateau potentials were experimentally induced by an  
4 additional large, brief step current (~ 300 ms) at a fixed location along the track. In all  
5 neurons tested, this procedure resulted in the emergence of a large place field near the  
6 plateau induction site, as evidenced by spiking and a large amplitude  $V_m$  ramp  
7 depolarization (Fig. 3, A and C). Consistent with previous control experiments converting  
8 silent cells to place cells without  $V_m$  depolarization (Fig. 3B) (13), we observed only  
9 increases, and no decreases in ramp amplitude at spatial positions surrounding the  
10 plateau location (Fig. 3C and fig. S6D). This absence of synaptic depression is  
11 inconsistent with the prediction of the standard voltage-dependent model (Fig. 3D), but  
12 instead favors the alternative model, which predicted that only previously potentiated  
13 inputs would be eligible for synaptic depression, independent of postsynaptic voltage.

14         These results strongly indicate that bidirectional BTSP is fundamentally different  
15 from other previously characterized forms of associative synaptic plasticity that depend  
16 on three factors – presynaptic spiking, postsynaptic voltage, and a delayed reinforcement  
17 signal (1, 18, 30, 31). A particular advantage of a voltage-independent plasticity rule (Fig.  
18 2C and fig. S2) is that changes in strength at each synapse are determined independently  
19 by signals generated locally, whereas plasticity rules that depend on the global activation  
20 state of the postsynaptic neuron may not allow independent credit to be assigned to the  
21 subset of synapses that contributed to a desired outcome (32).

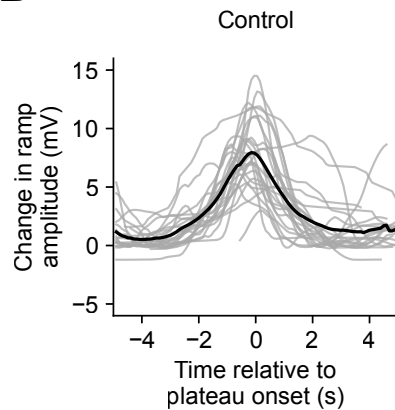
22         We next aimed to explore how this form of plasticity could impact memory storage  
23 at the network level. During goal-directed navigation, hippocampal neurons have been

**Fig 3.**

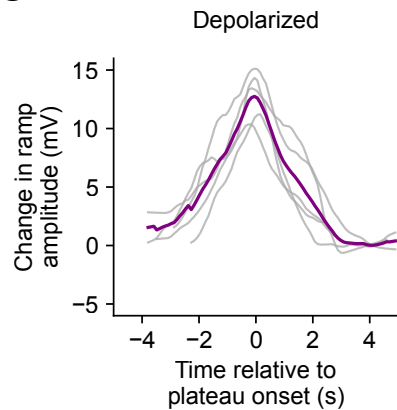
**A**



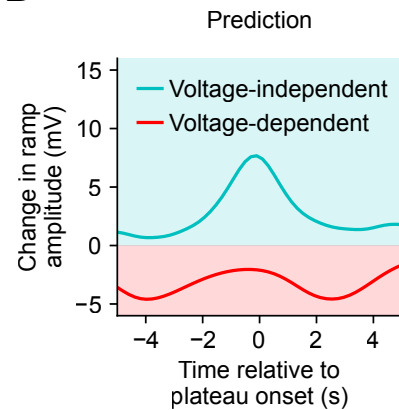
**B**



**C**



**D**



**Fig. 3. Bidirectional BTSP is insensitive to postsynaptic depolarization. (A)**

Intracellular  $V_m$  traces from individual laps in which plasticity was induced by experimentally-evoked plateau potentials in an otherwise silent CA1 cell. During plasticity induction laps, the neuron was experimentally depolarized by ~10 mV at steady-state with an intracellular current injection. On the background of this elevated depolarization at every spatial position, step current injections (300 ms) evoked plateau potentials at the same spatial position for five consecutive laps and induced a place field. (B – C) Place field ramp depolarizations induced by experimentally-evoked

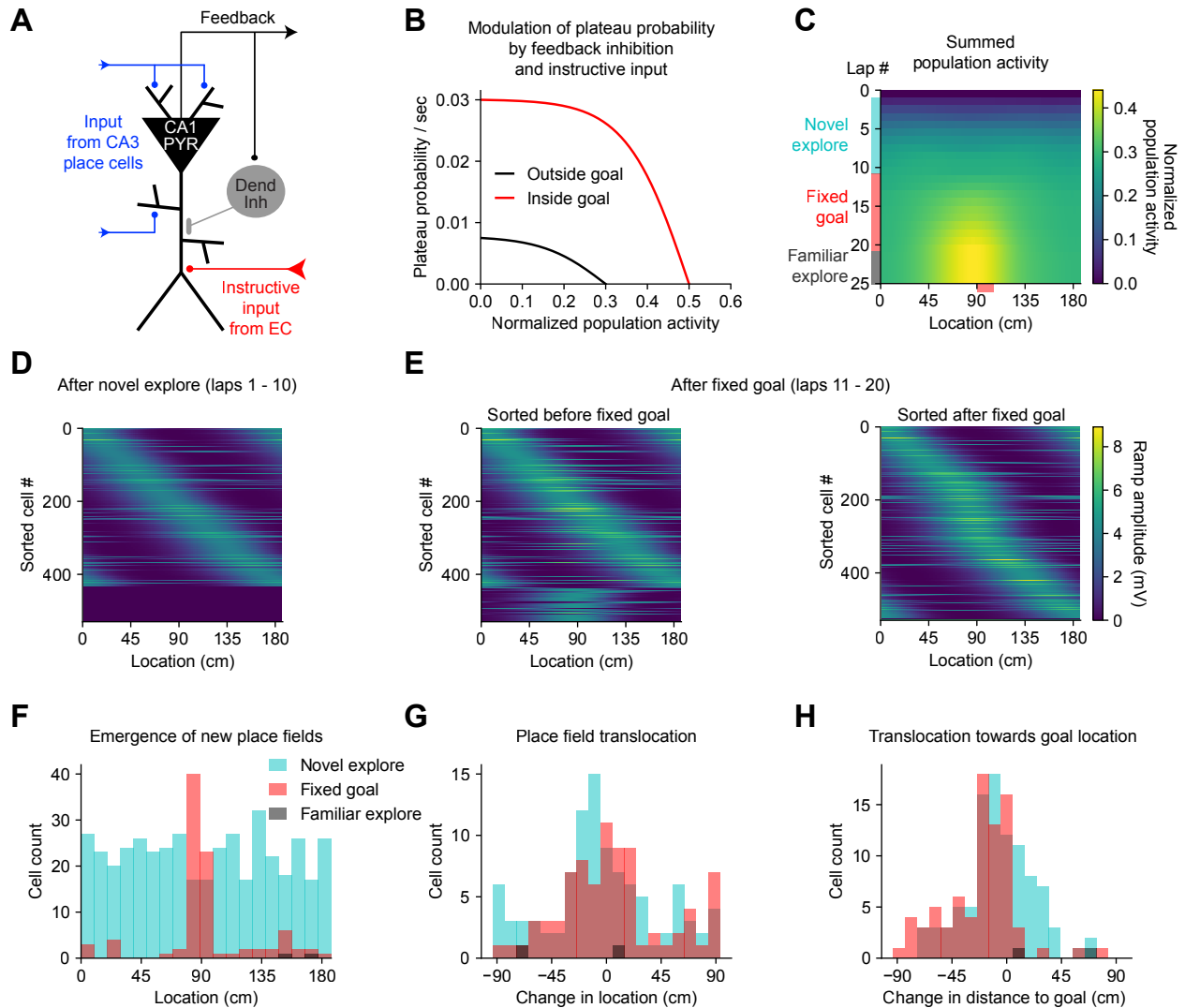
plateaus (individual cells in grey). Similar to control neurons that were converted from silent cells to place cells without steady-state depolarization (n=25, average in black) (B), neurons that underwent plasticity induction during steady-state depolarization (n=5, average in purple) (C) exhibited only synaptic potentiation, and no synaptic depression, at all spatial positions. (D) The data regression and interpolation in Fig. 1K was used to predict the changes in ramp amplitude that would result if BTSP was either dependent on (red) or independent of (blue) postsynaptic voltage.

1 shown to preferentially acquire new place fields near behaviorally-relevant locations, and  
2 to translocate existing place fields towards those locations (8-10, 33). Based on previous  
3 evidence that plateau probability in CA1 is facilitated by long-range feedback inputs onto  
4 distal CA1 dendrites from entorhinal cortex (12, 34, 35), and diminished by dendrite-  
5 targeting inhibition (35-39), we constructed a network model of the CA1 microcircuit  
6 where the probability of plateau initiation and thus BTSP induction was regulated by  
7 feedback inhibition and an instructive input from entorhinal cortex (Fig. 4, A and B) (10,  
8 40-44).

9 We simulated a virtual animal running at a constant velocity on a circular treadmill  
10 for three separate phases of exploration (Fig. 4C). The first phase (ten laps) simulated  
11 exploration of a novel environment. The next phase (ten laps) simulated a goal-directed  
12 search for a target placed at a single fixed location (90 cm). Finally, the stability of  
13 acquired spatial representations were assessed by five additional laps with the goal  
14 removed (Fig. 4C). At each time step (10 ms), instantaneous plateau probabilities were  
15 computed for each cell (Fig. 4B), determining which neurons would initiate a dendritic  
16 plateau and undergo plasticity, following the experimentally validated bidirectional  
17 synaptic learning rule from Fig. 2C.

18 During the first few laps of simulated exploration, CA1 pyramidal neurons rapidly  
19 acquired place fields that, as a population, uniformly tiled the track (Fig. 4; C, D, and F).  
20 As neurons increased their activity over time, feedback inhibition increased proportionally  
21 and prevented further plasticity (Fig. 4, A to C). During laps with a goal presented at a  
22 fixed location, an additional population of silent neurons acquired place fields nearby the  
23 goal location (Fig. 4, E and F), while a separate population shifted their place field

**Fig. 4.**



**Fig. 4. Bidirectional BTSP enables rapid adaptation of population representations**

**in a network model. (A)** Diagram depicts components of a hippocampal network model. A population of CA1 pyramidal neurons receives spatially tuned excitatory input from a population of CA3 place cells and an instructive input from entorhinal cortex (EC) that signals the presence of a behavioral goal. The output of CA1 pyramidal neurons recruits feedback inhibition from a population of interneurons. **(B)** The probability that model CA1 neurons emit plateau potentials and induce bidirectional plasticity is

negatively modulated by feedback inhibition. As the total number of active CA1 neurons increases (labeled “normalized population activity”), feedback inhibition increases, and plateau probability decreases until a target level of population activity is reached, after which no further plasticity can be induced (black). An instructive input signaling the presence of a goal increases plateau probability, resulting in a higher target level of population activity inside the goal region (red). **(C)** Each row depicts the summed activity of the population of model CA1 pyramidal neurons across spatial positions during a lap of simulated running. Laps 1-10 reflect exploration of a previously unexplored circular track. During laps 11-20, a goal is added to the environment at a fixed location (90 cm). During laps 21-25, the goal is removed for additional exploration of the now familiar environment. **(D – E)** Activity of individual model CA1 pyramidal neurons during simulated exploration as described in **(C)**. **(D)** The activity of neurons are sorted by the peak location of their spatial activity following 10 laps of novel exploration. A fraction of the population remains inactive and untuned. **(E)** The activity of neurons after 10 laps of goal-directed search are first sorted by their original peak locations (left), and then re-sorted by their peak locations following exposure to the fixed goal (right). An increased fraction of neurons express place fields near the goal position. **(F)** Histogram depicts neurons recruited to express new place fields in each spatial bin (epochs: novel explore, blue; fixed goal, red; familiar explore, grey). **(G)** Histogram depicts absolute distance of translocated place fields. **(H)** Histogram depicts relative distance of translocated place fields to the goal location.



1 positions towards the goal (Fig. 4; E, G, and H). Overall this resulted in an increased  
2 proportion of place cells with place fields nearby the goal position (Fig. 4E). Simulated  
3 place cell activity remained stable in the final phase of exploration of the now familiar  
4 environment (Fig. 4, C and F to H). These network modeling results recapitulate  
5 experimentally observed statistics of CA1 place cell translocation during goal-directed  
6 behavior (9).

7 This model provides a proof of principle that bidirectional BTSP can enable  
8 populations of place cells to rapidly adapt their spatial representations to changes in the  
9 environment without any compromise to spatial selectivity. An important feature of this  
10 model is that plasticity is regulated by the global activity of populations of neurons, rather  
11 than by pairwise correlations between single neurons and their inputs. This allows the  
12 network to rapidly acquire population-level representations of previously unencountered  
13 stimuli, as well as to modify outdated representations to better reflect changes to  
14 behaviorally relevant stimuli like goal location. Interestingly, bidirectional BTSP is  
15 asymmetric, tending to potentiate inputs more strongly when they are active before a  
16 plateau rather than during or after a plateau. In the network model, this caused the  
17 population representation of the goal to actually peak before the goal location itself (see  
18 also (6)), producing a predictive memory representation that could potentially be used by  
19 an animal to recall the path leading to the goal (45).

20 In summary, we found that dendritic plateaus could induce both potentiation and  
21 depression of subsets of synaptic inputs, resulting in translocation of a cell's place field  
22 towards the position where the plateaus were evoked. Quantitative inference of the  
23 underlying learning rule from the experimental data revealed that the direction and

1 magnitude of changes in synaptic strength depended on the current strength of each input  
2 at the time of a plateau, but not the degree of correlation between presynaptic and  
3 postsynaptic activity. In addition, bidirectional BTSP exhibited saturability (fig. S7) and  
4 state-dependence, two important features for stability of learned neuronal representations  
5 (3, 17, 27, 46, 47).

6 Together our experimental and modeling results establish bidirectional BTSP as a  
7 non-correlative mechanism for rapid and reversible learning. Rather than acting to  
8 autonomously reinforce pre-existing short timescale correlations between pre- and post-  
9 synaptic activity like standard Hebbian learning, bidirectional BTSP is capable of  
10 completely reshaping pairwise neuronal correlations in response to instructive input  
11 signals that promote dendritic plateau potentials. While it could be argued that BTSP is  
12 still a correlative form of plasticity due to its requirement that presynaptic spikes occur  
13 within a time window surrounding a plateau, this long timescale correlation is not between  
14 presynaptic spiking and the activation or output state of the postsynaptic neuron, but  
15 rather between presynaptic spiking and activation of a separate instructive input pathway  
16 that drives the postsynaptic plateau (12, 34, 35). Furthermore, since this long timescale  
17 coincidence between two inputs is only permissive for BTSP, but does not determine the  
18 sign of the plasticity, it cannot be classified as correlative in the same sense as classical  
19 Hebbian or even anti-Hebbian forms of plasticity. As suggested by our network model, if  
20 plateau potentials are generated by mismatch between a target instructive input and the  
21 output of the local circuit, as reflected by dendritically-targeted feedback inhibition,  
22 bidirectional BTSP can implement objective-based learning (48, 49). In addition to  
23 providing insight into the fundamental mechanisms of spatial memory formation in the

1 hippocampus, these findings suggest new directions for general theories of biological  
2 learning and the development of artificial learning systems (44, 50).

3

#### 4 **Materials and Methods**

##### 5 *In vivo intracellular electrophysiology*

6 All experimental methods were approved by the Janelia Institutional Animal Care and  
7 Use Committee (Protocol 12-84 & 15-126). All experimental procedures in this study,  
8 including animal surgeries, behavioral training, treadmill and rig configuration, and  
9 intracellular recordings, were performed identically to a previous detailed report (13) in  
10 an overlapping set of experiments, and are briefly summarized here.

11 *In vivo* experiments were performed in 6-12 week-old mice of either sex.

12 Craniotomies above the dorsal hippocampus for simultaneous whole-cell patch clamp  
13 and local field potential (LFP) recordings, as well as affixation of head bar implants were  
14 performed under deep anesthesia. Following a week of recovery, animals were  
15 prepared for behavioral training with water restriction, handling by the experimenter, and  
16 addition of running wheels to their home cages. Mice were trained to run on the cue-  
17 enriched linear treadmill for a dilute sucrose reward delivered through a licking port  
18 once per lap (~187 cm). A MATLAB GUI interfaced with a custom microprocessor-  
19 controlled system for behavioral tracking and control. Position-dependent reward  
20 delivery and intracellular current injection were triggered by photoelectric sensors, and  
21 animal run velocity was measured by an encoder attached to one of the wheel axles. In  
22 a subset of experiments (Fig. 3), in addition to position-dependent step current to evoke  
23 plateau potentials, steady-state current was injected to depolarize neurons beyond

1 threshold for axosomatic action potentials during plasticity induction laps. While steady-  
2 state depolarization of the soma is expected to attenuate along the path to distal  
3 dendrites (51), the pairing of back-propagating action potentials with synaptic inputs has  
4 been shown to significantly amplify dendritic depolarization by inactivating A-type  
5 potassium channels and activating voltage-gated sodium channels and NMDA-type  
6 glutamate receptors (52-55). Simulations of a biophysically-detailed CA1 place cell  
7 model with realistic morphology and distributions of dendritic ion channels (39) suggest  
8 that steady-state somatic depolarization of a silent CA1 pyramidal cell *in vivo* results in  
9 levels of distal dendritic depolarization comparable to place cells at the peak of their  
10 place field (fig. S6, A to C).

11 To establish whole-cell recordings from CA1 pyramidal neurons, an extracellular  
12 LFP electrode was lowered into the dorsal hippocampus using a micromanipulator until  
13 prominent theta-modulated spiking and increased ripple amplitude was detected. Then  
14 a glass intracellular recording pipette was lowered to the same depth while applying  
15 positive pressure. The intracellular solution contained (in mM): 134 K-Gluconate, 6 KCl,  
16 10 HEPES, 4 NaCl, 0.3 MgGTP, 4 MgATP, 14 Tris-phosphocreatine, and in some  
17 recordings, 0.2% biocytin. Current-clamp recordings of intracellular membrane potential  
18 ( $V_m$ ) were amplified and digitized at 20 kHz, without correction for liquid junction  
19 potential.

20

### 21 *Place field analysis*

22 To analyze subthreshold  $V_m$  ramps, action potentials were first removed from raw  $V_m$   
23 traces and linearly interpolated, then the resulting traces were low-pass filtered (<3 Hz).

1 For each of 100 equally sized spatial bins (1.87 cm),  $V_m$  ramp amplitudes were  
2 averaged across periods of 5-10 minutes of running laps on the treadmill. The spatially-  
3 binned ramp traces were then smoothed with a Savitzky-Golay filter with wrap-around.  
4 Ramp amplitude was quantified as the difference between the peak and the baseline  
5 (average of the 10% most hyperpolarized bins). For cells with a second place field  
6 induced, the same baseline  $V_m$  value determined from the period before the second  
7 induction was also used to quantify ramp amplitude after the second induction. Ramp  
8 width was quantified as the peak-normalized area under the curve. Plateau duration  
9 was estimated as the duration of intracellular step current injections, or as the full width  
10 at half maximum  $V_m$  in the case of spontaneous naturally-occurring plateaus. For each  
11 spatial bin, the elapsed time between traversal of that position and onset of a plateau  
12 was variable across induction laps, depending on lap-by-lap differences in run velocity  
13 (e.g. Fig. 1, C and F). To analyze the relationship between this time interval and  
14 changes in ramp amplitude, time relative to plateau onset (Fig. 1, E, H, J and K) was  
15 conservatively estimated as the minimum time delay across all induction laps. Since not  
16 all possible pairs of initial ramp amplitude and time delay relative to plateau onset were  
17 sampled in the experimental dataset, expected changes in ramp amplitude (Fig. 1K; Fig.  
18 2; E and G; Fig. 3D; fig. S5; and fig. S8) were predicted from the sampled experimental  
19 or model data points by a two-dimensional Gaussian process regression and  
20 interpolation procedure using a rational quadratic covariance function, implemented in  
21 the open-source python package *sklearn* (56, 57).

22

23

## 1 *Computational modeling*

2 Two classes of mathematical models of the synaptic learning rule underlying  
3 bidirectional BTSP were built and optimized to predict the spatially tuned  $V_m$  ramp  
4 depolarizations of experimentally recorded CA1 place cells. All code (python) necessary  
5 to reproduce the modeling results is open-source and publicly available (58, 59). The  
6 following components and notation were shared across all model variants. CA1 place  
7 cell ramp depolarization  $\Delta V$  as a function of position  $x$  was modeled as a weighted sum  
8 of the spatial firing rates of a population of 200 CA3 place cell inputs with place fields  
9 spaced uniformly across a 187 cm circular track, with a background level of  
10 depolarization  $V_b$  subtracted. This background is equivalent to the level of activation that  
11 would be produced if all inputs had a uniform weight of 1.

$$12 \quad (1) \quad \Delta V(x) = \alpha \cdot \sum_i W_i \cdot R_i(x) - V_b$$

13 The firing rate  $R_i$  of CA3 place cell  $i$  with place field peak location  $y_i$  was modeled as a  
14 Gaussian function of position  $x$ , accounting for wraparound of the circular track with  
15 length  $\ell$ :

$$16 \quad (2) \quad d_i(x) = \begin{cases} -\ell + (x - y_i), & x - y_i \geq \frac{\ell}{2} \\ x - y_i, & -\frac{\ell}{2} < x - y_i < \frac{\ell}{2} \\ \ell + (x - y_i), & x - y_i \leq -\frac{\ell}{2} \end{cases}$$

$$17 \quad (3) \quad R_i(x) = e^{-\left(\frac{d_i(x)}{\sigma}\right)^2}$$

18 The place field widths of CA3 inputs, controlled by  $\sigma$ , were set to have a full floor width  
19 ( $3 \cdot \sqrt{2} \cdot \sigma$ ) of 90 cm (half-width of  $\sim 34$  cm) throughout the study (60), though models  
20 tuned with alternative values of input field widths generated quantitatively similar  
21 predictions (fig. S8). Initial synaptic weights in silent cells before the first place field

1 induction were assumed to have a value of 1. Initial synaptic weights before the second  
2 place field induction in neurons already expressing a place field were estimated from  
3 the recorded ramp depolarization by least squares approximation. The scaling factor  $\alpha$   
4 was calibrated such that if the synaptic weights of CA3 place cell inputs varied between  
5 1 and 2.5 as a Gaussian function of their place field locations, the postsynaptic CA1 cell  
6 would express a  $V_m$  ramp with 90 cm width and 6 mV amplitude, consistent with  
7 previous measurements of place field properties and the degree of synaptic potentiation  
8 by BTSP (13).

9 For each experimental recording, the position of an animal as a function of time  
10 during a plasticity induction lap  $j$  determined the firing rates of model CA3 inputs as a  
11 function of time  $R_{j,i}(t) = R_{j,i}(x_j(t))$  (Fig. 2B, fig. S1B, and fig. S2B). In accordance with  
12 experimental data (12, 39), the firing rates of model place cell inputs decreased to zero  
13 during periods when the animal stopped running. Postsynaptic dendritic plateau  
14 potentials during each induction lap were modeled as binary functions of time  $P_j(t)$ . To  
15 generate long duration plasticity eligibility signals  $\tilde{L}_{j,i}(t)$  specific to each synaptic input  $i$   
16 and instructive plasticity signals  $\tilde{P}_j(t)$  shared by all synapses, input firing rates and  
17 plateaus were convolved with causal temporal filters with exponential rise and decay  
18 (Fig. 2; fig. S1, C and D; fig. S2, C and D), denoted by a raised tilde.

19  $W_{j,i}$  corresponds to the synaptic weight of each input  $i$  prior to each plasticity  
20 induction lap  $j$ . Changes in synaptic weight  $\Delta W_{j,i}$  were calculated once per lap by  
21 integrating a net rate of change of synaptic weight  $\frac{dW_{j,i}(t)}{dt}$  (defined separately for each  
22 model below) over the duration of lap  $j$ . For all models, additional nonlinear gain  
23 functions  $q_{\pm}$  transformed synaptic eligibility signals  $\tilde{L}_{j,i,\pm}(t)$  and contributed to the rate of

1 change  $\frac{dW_{j,i}(t)}{dt}$ . These scaled and rectified sigmoidal functions  $q(\tilde{L})$  were parameterized  
 2 and expressed as follows:

$$3 \quad (4) \quad gain_{slope} = \frac{2}{gain_{peak} - gain_{th}}$$

$$4 \quad (5) \quad \hat{q}(\tilde{L}) = \frac{1}{1 + e^{(-gain_{slope} \cdot (\tilde{L} - gain_{th}))}}$$

$$5 \quad (6) \quad gain_{scale} = \frac{1}{\hat{q}(1) - \hat{q}(0)}$$

$$6 \quad (7) \quad q(\tilde{L}) = \begin{cases} 0, & \hat{q}(\tilde{L}) \leq \hat{q}(0) \\ gain_{scale} \cdot (\hat{q}(\tilde{L}) - \hat{q}(0)), & \hat{q}(0) < \hat{q}(\tilde{L}) < \hat{q}(1) \\ 1, & \hat{q}(\tilde{L}) \geq \hat{q}(1) \end{cases}$$

7

8 *Voltage-dependent model:*

9 The voltage-dependent model (Fig. 2A, fig. S1, and fig. S3) contained the following 11  
 10 free parameters:

11 1) *signal<sub>eligibility</sub>*  $\tau_{rise}$ , 2) *signal<sub>eligibility</sub>*  $\tau_{decay}$ , 3) *signal<sub>instructive</sub>*  $\tau_{rise}$ , 4) *signal<sub>instructive</sub>*  $\tau_{decay}$ ,  
 12 5)  $\Delta V_{max}$ , 6)  $k_+$ , 7)  $k_-$ , 8)  $gain_{th,+}$ , 9)  $gain_{peak,+}$ , 10)  $gain_{th,-}$ , 11)  $gain_{peak,-}$ .

13 In this model, distinct eligibility signals for synaptic potentiation and synaptic depression  
 14 were oppositely sensitive to postsynaptic voltage. The instantaneous postsynaptic  
 15 depolarization amplitude  $\Delta V_j(t)$  during plasticity induction lap  $j$ , including the large brief  
 16 depolarization produced by the dendritic plateau potential, was normalized to a  
 17 saturating amplitude  $\Delta V_{max}$  and rectified:

$$18 \quad (8) \quad \Delta \hat{V}_j(t) = \begin{cases} 0 & \Delta V_j(t) \leq 0 \\ \frac{\Delta V_j(t)}{\Delta V_{max}} & 0 < \Delta V_j(t) < \Delta V_{max} \\ 1 & \Delta V_j(t) \geq \Delta V_{max} \end{cases}$$

19  $\Delta \hat{V}_j(t)$  influenced synaptic eligibility signals according to:



1 (9)  $\tilde{L}_{j,i,+}(t) = (1 - \Delta\hat{V}_j(t)) \cdot R_{j,i}(t)$ ; filtered by *signal*<sub>eligibility</sub>  $\tau_{rise}$  and  $\tau_{decay}$

2 (10)  $\tilde{L}_{j,i,-}(t) = \Delta\hat{V}_j(t) \cdot R_{j,i}(t)$ ; filtered by *signal*<sub>eligibility</sub>  $\tau_{rise}$  and  $\tau_{decay}$

3 The sigmoidal gain functions  $q_+(\tilde{L}_{j,i,+}(t), gain_{th,+}, gain_{peak,+})$  and

4  $q_-(\tilde{L}_{j,i,-}(t), gain_{th,-}, gain_{peak,-})$ , as well as the plateau-related instructive signal  $\tilde{P}_j(t)$

5 contributed to the net rate of change  $\frac{dW_{j,i}(t)}{dt}$  according to:

6 (11)  $\frac{dW_{j,i}(t)}{dt} = k_+ \cdot q_+(\tilde{L}_{j,i,+}(t)) \cdot \tilde{P}_j(t) - k_- \cdot q_-(\tilde{L}_{j,i,-}(t)) \cdot \tilde{P}_j(t)$

7 where  $k_+$  and  $k_-$  are scalar learning rate constants. Synaptic weights were bounded such

8 that  $W_{j,i} \geq 0$ .

9

10 *Weight-dependent model:*

11 The weight-dependent model (Fig. 2C, fig. S2, and fig. S4) contained the following 11

12 free parameters:

13 1) *signal*<sub>eligibility</sub>  $\tau_{rise}$ , 2) *signal*<sub>eligibility</sub>  $\tau_{decay}$ , 3) *signal*<sub>instructive</sub>  $\tau_{rise}$ , 4) *signal*<sub>instructive</sub>  $\tau_{decay}$ ,

14 5)  $\Delta W_{max}$ , 6)  $k_+$ , 7)  $k_-$ , 8)  $gain_{th,+}$ , 9)  $gain_{peak,+}$ , 10)  $gain_{th,-}$ , 11)  $gain_{peak,-}$ .

15 This model was formulated with the aim of obtaining a first order dependence of

16 changes in synaptic weights on the current value of synaptic weight just before each

17 plasticity-inducing plateau potential. We chose a two-state non-stationary kinetic model

18 of the form shown in fig. S2A as a concrete example of a model that satisfies this

19 dependency. Independent and finite synaptic resources at each synapse could occupy

20 either an inactive or an active state, and the synaptic weight of each input  $W_{j,i}$  was

21 defined as proportional to the occupancy of the active state. Since the occupancy of

22 each state in a kinetic model constrains the flow of finite resources between states, the

1 net change in synaptic weight at each input  $\frac{dW_{j,i}(t)}{dt}$  naturally depended on the current  
 2 value of synaptic weight  $W_{j,i}$ . This occupancy could be equivalently interpreted as a  
 3 proportion of synapses that have been potentiated among a subpopulation of inputs  
 4 with shared place field locations and binary weights. Synaptic weights were constrained  
 5 such that

$$6 \quad (12) \quad W_{j,i} = w_{j,i} \cdot W_{max}$$

7 where  $0 \leq w_{j,i} \leq 1$ , and  $W_{max}$  depends on a parameter  $\Delta W_{max}$  that specifies a maximum  
 8 change in weight above a baseline of 1:

$$9 \quad (13) \quad W_{max} = 1 + \Delta W_{max}$$

10 In the absence of any voltage sensitivity of synaptic eligibility signals, both eligibility for  
 11 potentiation and eligibility for depression depended only on a presynaptic firing rate and  
 12 were therefore equivalent in the formulation of this model variant (fig. S3, C and D):

$$13 \quad (14) \quad \tilde{L}_{j,i,+}(t) = \tilde{L}_{j,i,-}(t) = \tilde{L}_{j,i}(t) = R_{j,i}(t); \text{ filtered by } \textit{signal}_{\textit{eligibility}} \tau_{\textit{rise}} \text{ and } \tau_{\textit{decay}}$$

14 Sigmoidal gain functions  $q_+(\tilde{L}_{j,i}(t), \textit{gain}_{\textit{th},+}, \textit{gain}_{\textit{peak},+})$  and  $q_-(\tilde{L}_{j,i}(t), \textit{gain}_{\textit{th},-}, \textit{gain}_{\textit{peak},-})$ , as  
 15 well as the plateau-related instructive signal  $\tilde{P}_j(t)$  and the current normalized synaptic  
 16 weight  $w_{j,i}$  contributed to the net rate of change  $\frac{dW_{j,i}(t)}{dt}$  according to:

$$17 \quad (15) \quad \frac{dW_{j,i}(t)}{dt} = \frac{W_{max} \cdot (1 - w_{j,i}) \cdot k_+ \cdot q_+(\tilde{L}_{j,i}(t)) \cdot \tilde{P}_j(t) - W_{max} \cdot w_{j,i} \cdot k_- \cdot q_-(\tilde{L}_{j,i}(t)) \cdot \tilde{P}_j(t)}$$

18 where  $k_+$  and  $k_-$  are scalar learning rate constants.

19 For both of the above model variants, the values of the bounded free parameters  
 20 were automatically explored using a population-based version of the simulated  
 21 annealing algorithm (59) to minimize an objective error function based on the difference  
 22 between target and predicted ramp waveforms for each cell in the experimental dataset.

1 Additional model variants with either fewer (7) or more (13) free parameters were also  
2 tested (fig. S5). In the simpler model variants, the nonlinear gain functions  $q_{\pm}$  were not  
3 applied to the eligibility signals and the change in synaptic weights instead depended  
4 linearly on the amplitude of the synaptic eligibility signals  $\tilde{L}_{j,i,\pm}(t)$ . These models were  
5 unable to account for the depression component of bidirectional BTSP (fig. S5). In the  
6 more complex model variants, eligibility signals for potentiation  $\tilde{L}_{j,i,+}(t)$  and depression  
7  $\tilde{L}_{j,i,-}(t)$  were filtered with distinct time constants  
8 ( $signal_{eligibility,+} \tau_{rise}$ ,  $signal_{eligibility,+} \tau_{decay}$ ,  $signal_{eligibility,-} \tau_{rise}$ ,  $signal_{eligibility,-} \tau_{decay}$ ). The  
9 additional complexity of these model variants did not result in improved predictions  
10 relative to the original set of models (fig. S5).

11

#### 12 *Goal-directed spatial learning model:*

13 To investigate the implications of bidirectional BTSP for reward learning by a population  
14 of CA1 place cells (Fig. 4), we constructed a network model comprised of 1000 CA1  
15 pyramidal cells each receiving input from a population of 200 CA3 place cells with place  
16 fields spaced at regular intervals spanning the 187 cm circular track. Lap running was  
17 simulated at a constant run velocity of 30 cm/s. The synaptic weights at inputs from  
18 model CA3 place cells to model CA1 cells were controlled by the weight-dependent  
19 model of bidirectional BTSP described above. For this purpose, the 11 free parameters  
20 of that model were tuned to match synthetic data under the following constraints: 1) 5  
21 consecutive induction laps with one 300 ms duration plateau per lap at a fixed location  
22 resulted in a place field ramp depolarization that peaked 10 cm before the location of  
23 plateau onset, had an asymmetric shape (80 cm rise, 40 cm decay), and had a peak

1 amplitude of 8 mV; 2) 5 subsequent plasticity induction at a location 90 cm away from  
2 the initial peak for 5 consecutive laps resulted in a 5 mV decrease in ramp amplitude at  
3 the initial peak location, and an 8 mV peak ramp amplitude at the new translocated  
4 peak position.

5 Before simulated exploration, all synaptic weights were initialized to a value of 1,  
6 which resulted in zero ramp depolarization in all model CA1 cells. Under these baseline  
7 conditions, each model CA1 neuron  $k$  had a probability  $p_k(t) = p_{basal} = 0.0075$  of emitting  
8 a single dendritic plateau potential in 1 second of running. During each 10 ms time step,  
9 this instantaneous probability  $p_k(t)$  was used to weight biased coin flips to determine  
10 which cells would emit a plateau. If a cell emitted a plateau, it persisted for a fixed  
11 duration of 300 ms, and was followed by a 500 ms refractory period during which  $p_k(t)$   
12 was transiently set to zero.

13 After the first lap, CA1 neurons that had emitted at least one plateau and had  
14 induced synaptic potentiation produced nonzero ramp depolarizations (Fig. 4C). The  
15 output firing rates  $R_k(t)$  of each CA1 neuron  $k$  were considered to be proportional to their  
16 ramp depolarizations  $V_k(t)$ . The activity  $R_{inh}(t)$  of a single inhibitory feedback element  
17 was set to be a normalized sum of the activity of the entire population of CA1 pyramidal  
18 neurons:

$$19 \quad (16) \quad R_{inh}(t) = \beta \cdot \sum_k R_k(t)$$

20 where the normalization constant  $\beta$  was chosen such that the activity of the inhibitory  
21 feedback neuron would be 1 if every CA1 pyramidal neuron expressed a single place  
22 field and as a population their place field peak locations uniformly tiled the track. Then,

1 the probability that any CA1 neuron  $k$  would emit a plateau  $p_k(t)$  was negatively  
2 regulated by the total population activity via the inhibitory feedback term  $R_{inh}(t)$ :

$$3 \quad (17) \quad p_k(t) = \begin{cases} f(R_{inh}(t), \gamma_{basal}, p_{basal}), & R_{inh}(t) < \gamma_{basal} \\ 0, & R_{inh}(t) \geq \gamma_{basal} \end{cases}$$

4 where  $\gamma_{basal}$  defined a target normalized population activity (set to 0.3) and  $f$  is a  
5 descending sigmoid (Fig. 4B).

6 In some laps, a specific location was assigned as the target of a goal-directed  
7 search. To mimic the activation of an instructive input from entorhinal cortex signaling  
8 the presence of the goal, for a period of 500 ms starting at the goal location, the  
9 probability that a CA1 neuron would emit a plateau potential  $p_k(t)$  was transiently  
10 increased. Within the goal region, the relationship between  $p_k(t)$  and  $R_{inh}(t)$  was  
11 instead:

$$12 \quad (18) \quad p_k(t) = \begin{cases} f(R_{inh}(t), \gamma_{goal}, p_{goal}), & R_{inh}(t) < \gamma_{goal} \\ 0, & R_{inh}(t) \geq \gamma_{goal} \end{cases}$$

13 where  $p_{goal}$  is an elevated peak plateau probability of 0.03 per second,  $\gamma_{goal}$  is an  
14 elevated target normalized population activity (set to 0.5) and  $f$  is a descending sigmoid  
15 (Fig. 4B).

16

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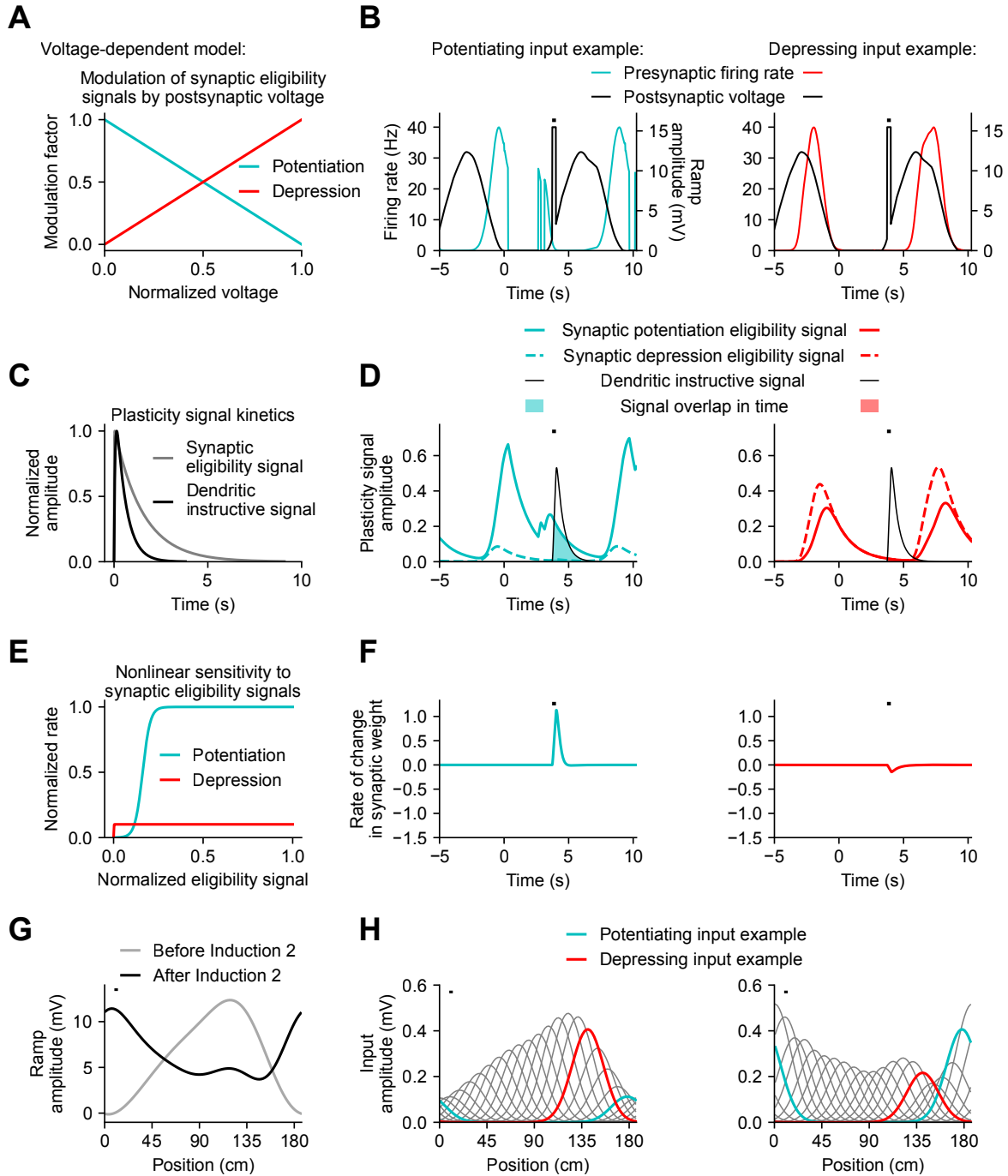
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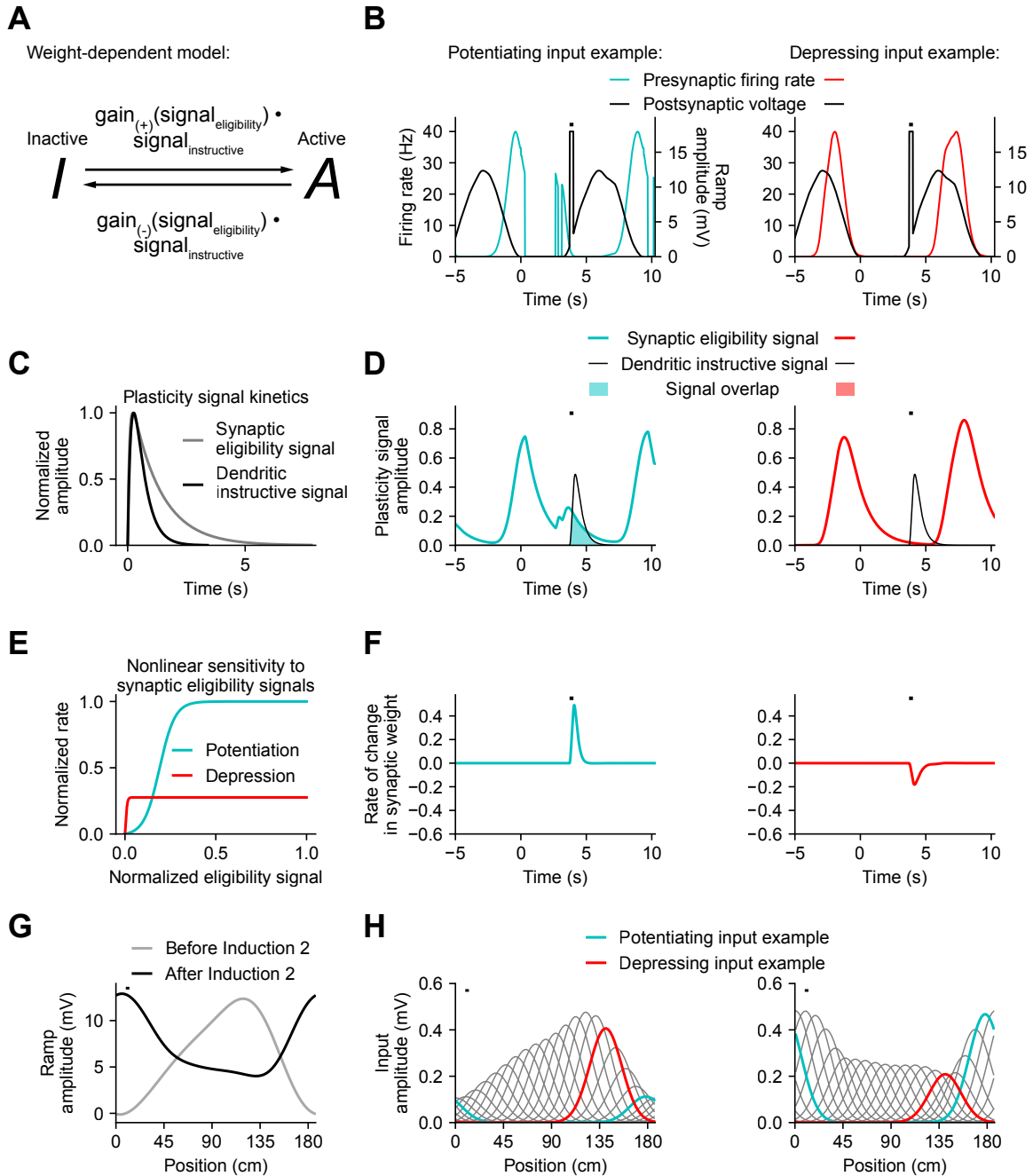
**Fig S1.**



**Fig. S1. Voltage-dependent model: example simulation results. (A)** Voltage-sensitivity of synaptic eligibility signals for potentiation and depression. **(B)** Model presynaptic firing rates and postsynaptic  $V_m$  during simulation of one lap of treadmill

running during plasticity induction. The timing of a dendritic plateau potential is indicated with a black dash. Example traces depict two presynaptic inputs, one that potentiates (left, blue) and one that depresses (right, red). **(C)** Temporal filters with exponential rise and decay (synaptic eligibility signal filter, grey; dendritic instructive signal filter, black). **(D)** Presynaptic input firing rates **(B)** were convolved with the eligibility signal filter **(C)** and multiplied by a voltage modulation factor **(A)** to generate long duration synaptic eligibility signal traces for potentiation (solid blue and red lines) and depression (dashed blue and red lines) (potentiating input example from **(B)**, left; depressing input example from **(B)**, right). The dendritic plateau potential was convolved with the instructive signal filter **(C)** to generate a long duration dendritic instructive signal (black). Periods of temporal overlap of eligibility and instructive signals that drive plasticity are shaded. **(E)** Sigmoidal gain functions sensitive to the amplitude of synaptic eligibility signals regulate the rates of synaptic potentiation (blue) and depression (red). **(F)** Net rates of change in synaptic weight (potentiating input example from **(B)** and **(D)**, blue, left; depressing input example from **(B)** and **(D)**, red, right). **(G)** Spatially-binned  $V_m$  ramp depolarization predicted by the model (before Induction 2, grey; after Induction 2; black). **(H)** Weighted contributions of individual presynaptic inputs to the postsynaptic ramp (before Induction 2, left; after Induction 2, right). The potentiating (blue) and depressing (red) input examples shown in **(B)**, **(D)** and **(F)** are highlighted in color.

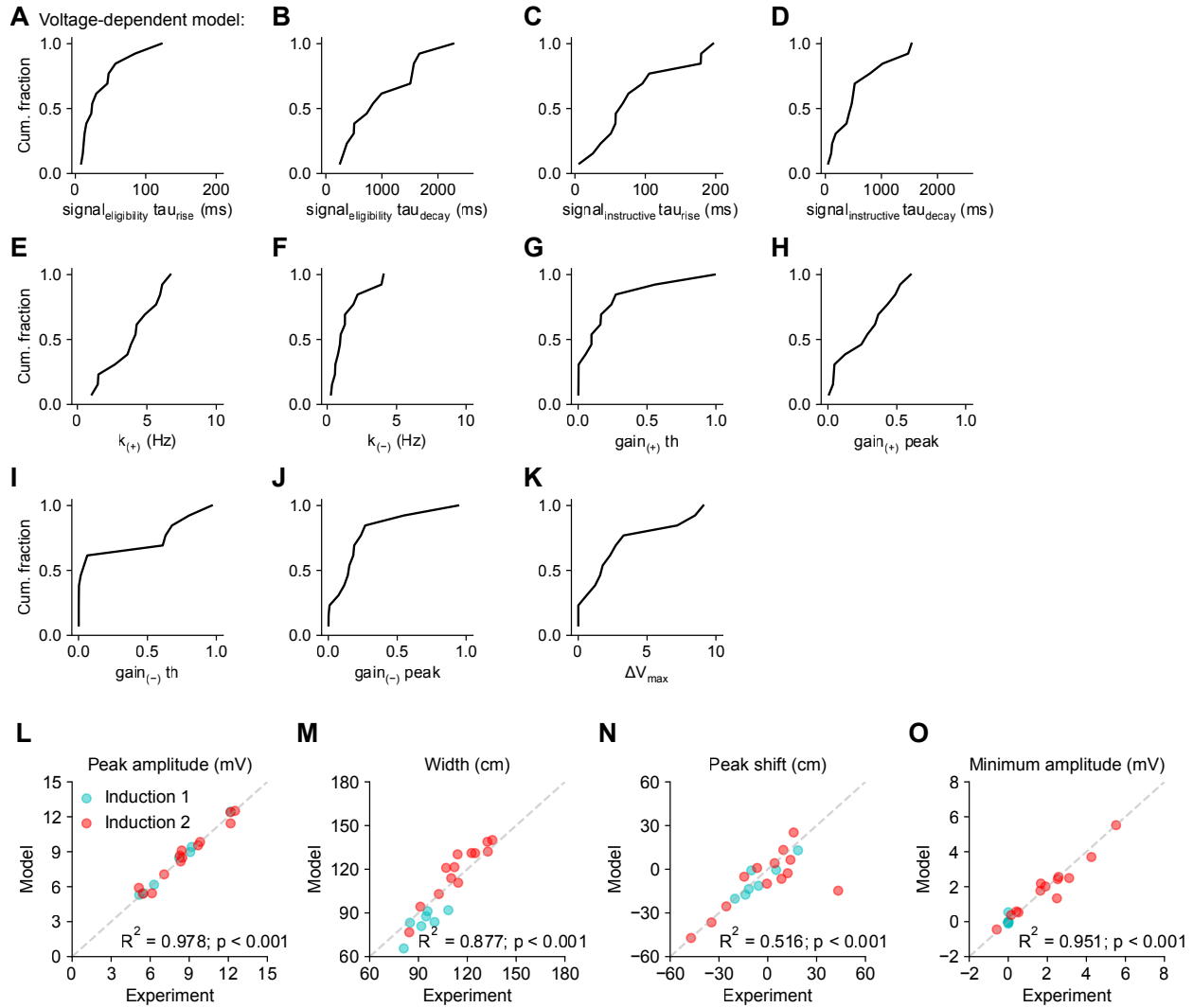
**Fig. S2.**



**Fig. S2. Weight-dependent model: example simulation results. (A)** State diagram for two-state kinetic model describing the flow of finite synaptic resources. **(B – H)** Same as fig. S1, B to H for simulation of the weight-dependent model of bidirectional BTSP. **(D)** Same as fig. S1D, except only a single synaptic eligibility signal is shown (red and

blue lines). In the weight-dependent model, postsynaptic voltage does not modulate the amplitude of synaptic eligibility traces, so eligibility for potentiation and depression are both marked by a single trace generated by convolving presynaptic firing rates (B) with the synaptic eligibility signal filter (C).

**Fig S3.**



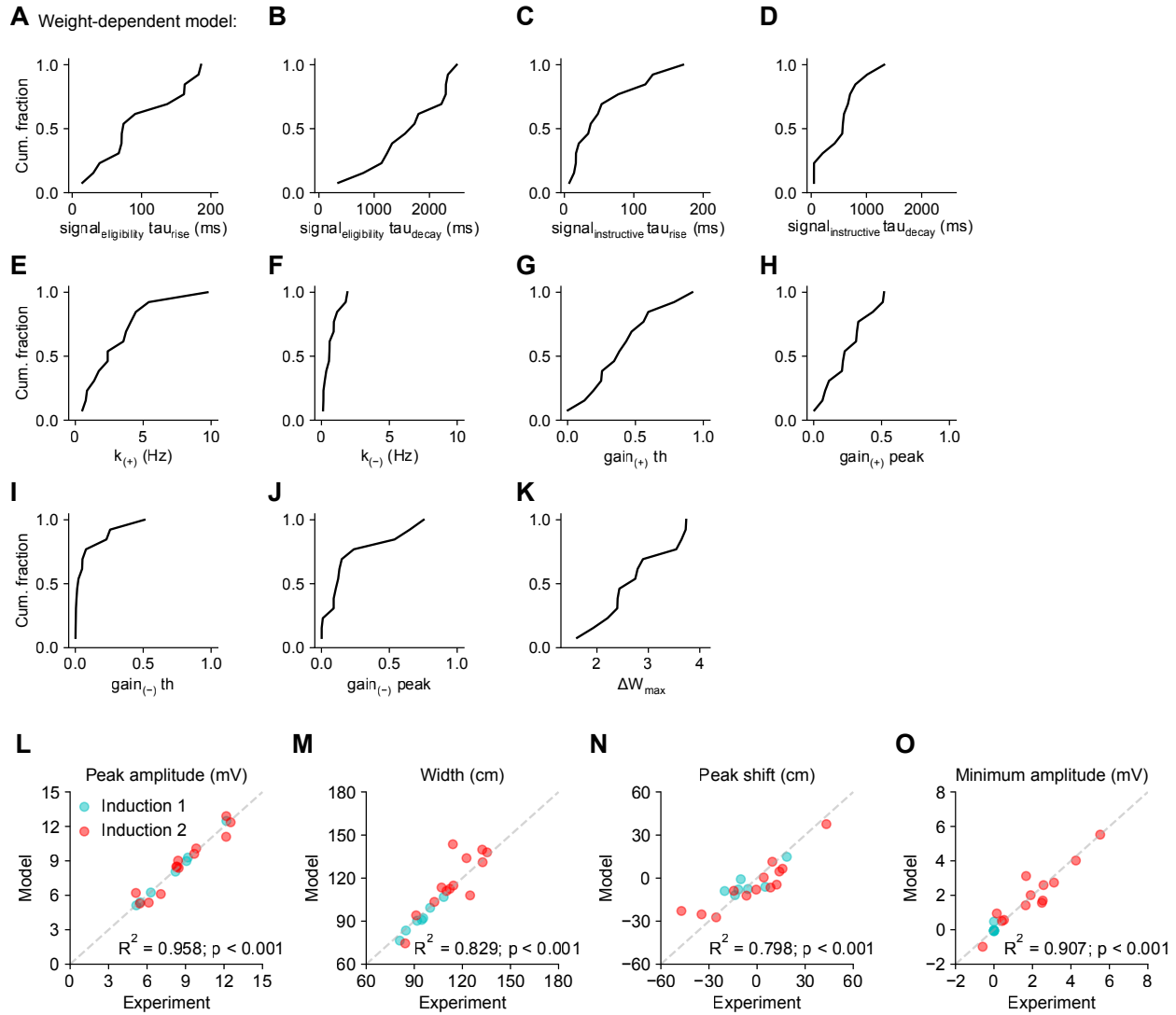
**Fig. S3. Voltage-dependent model: model parameter distributions and comparison**

**of model predictions to experimental data. (A – K)** The free parameters of the voltage-dependent model of bidirectional BTSP were optimized for each cell in the experimental dataset. Shown here are the distributions of parameter values across cells. **(L – O)** Model predictions and experimental data are compared for features measured from spatially binned  $V_m$  ramp depolarizations. In 7/13 neurons with a second place field induced (Induction 2, red), the first place field was also experimentally-

induced (Induction 1, blue), so the model was fit to predict both place field inductions with the same set of parameters. Explained variance ( $R^2$ ) and statistical significance ( $p < 0.05$ ) reflect Pearson's correlation and 2-tailed null hypothesis tests. **(L)** Peak ramp amplitude. **(M)** Ramp width. **(N)** Shift of ramp peak location relative to mean location of plateau onset. **(O)** Minimum ramp amplitude across spatial bins.

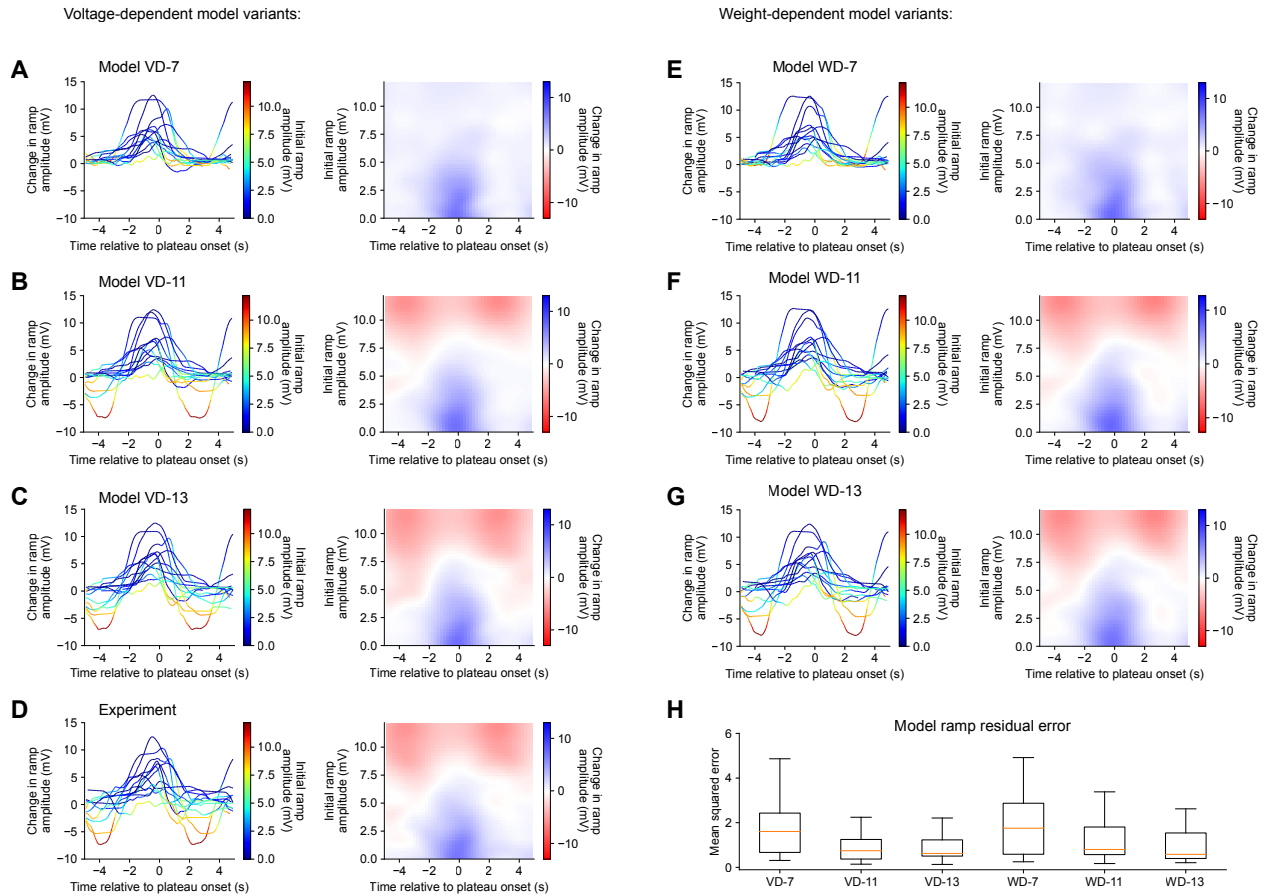


**Fig. S4.**



**Fig. S4. Weight-dependent model: model parameter distributions and comparison of model predictions to experimental data. (A – O)** Same as fig. S3, A to O for parameters and predictions of the weight-dependent model of bidirectional BTSP.

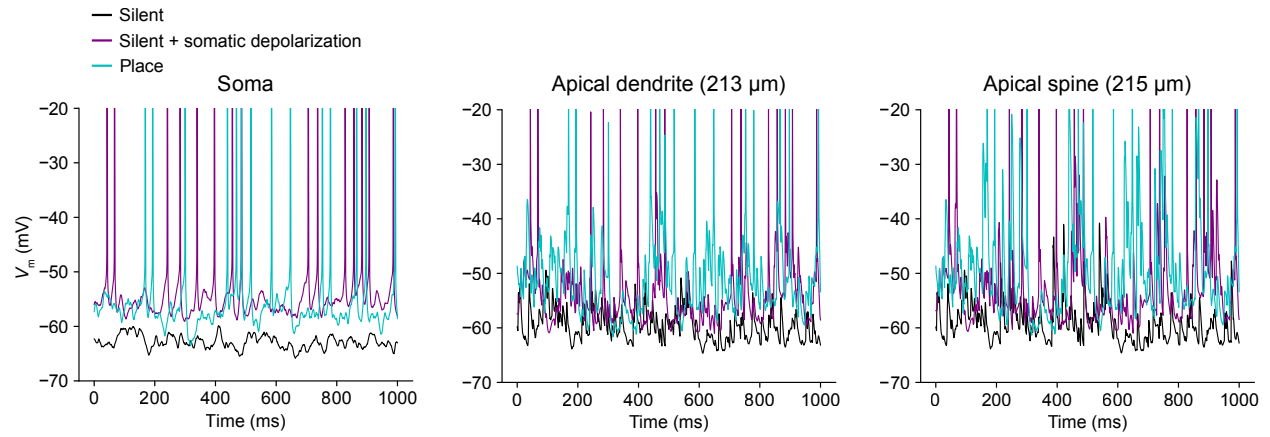
**Fig. S5.**



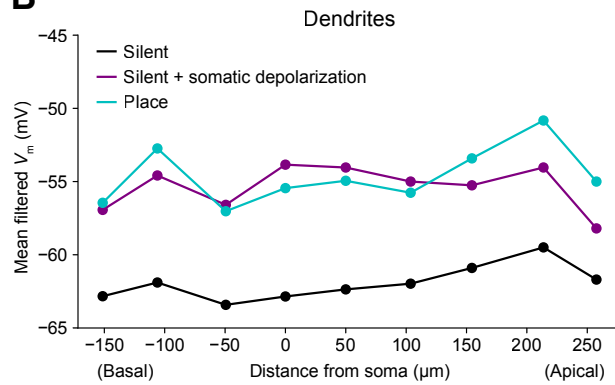
**Fig. S5. Evaluation of additional model variants.** (A – G) Additional model variants of varying complexity were also evaluated for their capability to predict experimentally measured bidirectional changes in  $V_m$  ramp amplitude by BTSP. The plasticity rule was estimated by two-dimensional interpolation from model data (see Materials and Methods). (A – C) Model predictions from variants of the voltage-dependent model with 7 (A), 11 (B), or 13 (C) free parameters (see Materials and Methods). (D) Plasticity rule estimated from the experimental data. (E – G) Model predictions from variants of the weight-dependent model with 7 (E), 11 (F), or 13 (G) free parameters (see Materials and Methods). (H) Residual error of ramp depolarizations predicted by each model is averaged across spatial bins and cells.

**Fig. S6.**

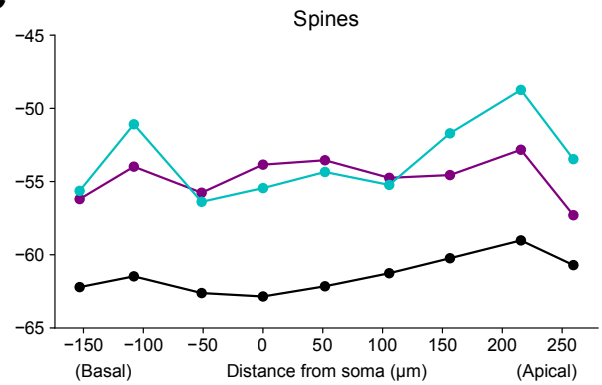
**A** Model:



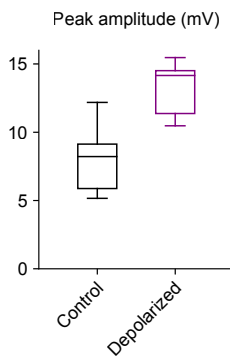
**B**



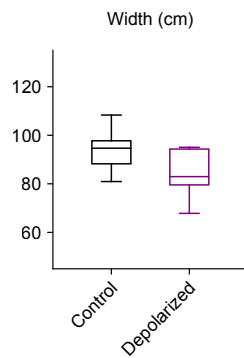
**C**



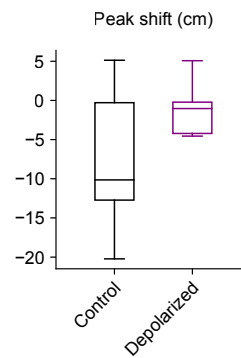
**D** Experiment:



**E**



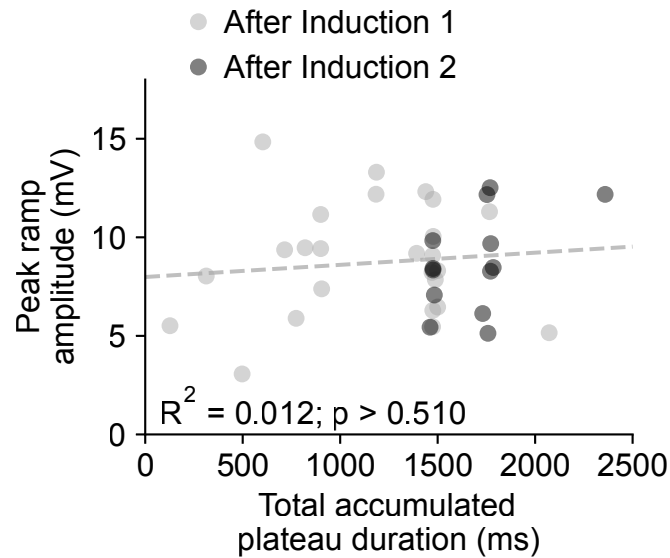
**F**



**Fig. S6. Postsynaptic voltage perturbation experiment: simulation of dendritic depolarization and quantification of experimental data. (A – C) Simulation of a**

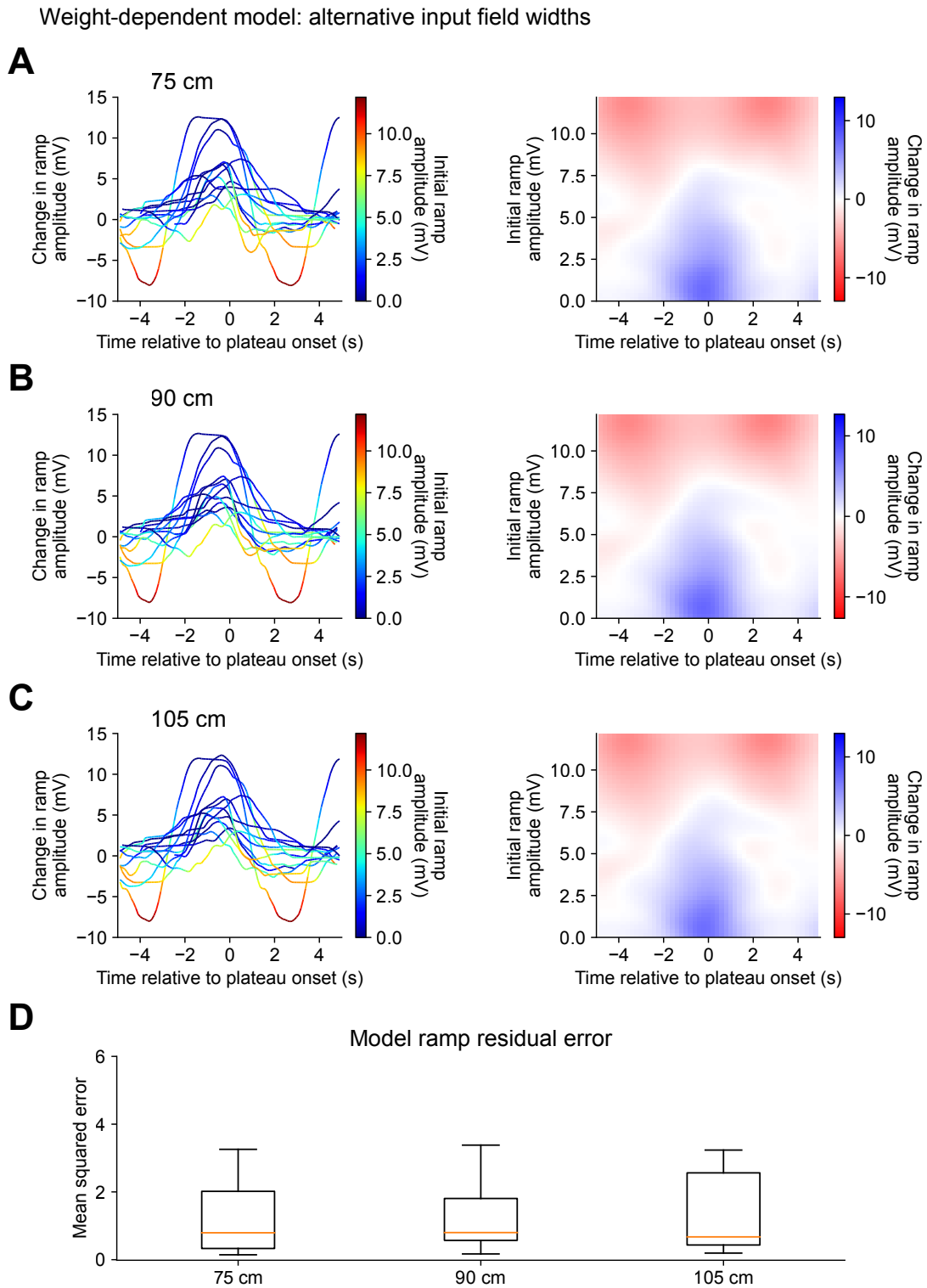
biophysically-detailed CA1 pyramidal cell model with realistic morphology and dendritic ion channel distributions (39) to estimate the effect of steady-state somatic depolarization on distal dendritic  $V_m$ . Three conditions are compared: a silent cell with uniform input weights (black), a silent cell with ~10 mV of steady-state depolarization induced by somatic current injection (purple), and a place cell receiving potentiated inputs at the peak of its place field (blue). Under conditions of somatic current injection, a combination of attenuated propagating depolarization and back-propagating action potentials amplifies local synaptic input by activating dendritic voltage-gated ion channels, resulting in a level of dendritic depolarization comparable to the place field condition. **(A)** Simulated  $V_m$  traces recorded from soma (left), distal apical oblique dendrite (center), and a distal apical dendritic spine (right). **(B)** Mean low-pass filtered  $V_m$  at simulated dendritic recording sites at varying distances from the soma. **(C)** Same as (B) for simulated recordings from dendritic spines. **(D – F)** Quantification of experimental ramp depolarizations induced by BTSP under conditions of somatic depolarization (Fig. 3). **(D)** Peak ramp amplitude ( $p < 0.015$ ). **(E)** Ramp width ( $p > 0.143$ ). **(F)** Shift of ramp peak location relative to mean location of plateau onset ( $p > 0.255$ ). p-values reflect two-sided Mann-Whitney U tests.

**Fig. S7.**



**Fig. S7. Evidence for saturability of synaptic potentiation by BTSP.** Peak  $V_m$  ramp amplitudes are not correlated with the total accumulated duration of plateau potentials across laps during plasticity induction, indicating a saturating nonlinearity. Shown are data from both silent cells in which *de novo* place fields were induced (light grey,  $n=25$ ), and place cells in which a second plasticity induction translocated a pre-existing place field (dark grey,  $n=13$ ). Explained variance ( $R^2$ ) and statistical significance ( $p < 0.05$ ) reflect Pearson's correlation and a 2-tailed null hypothesis test.

**Fig. S8.**



**Fig. S8. Evaluation of bidirectional BTSP models with alternative CA3 input place field widths.** (A – D) Additional model variants with alternative values of place field width for presynaptic CA3 place cell inputs were also evaluated for their capability to predict experimentally measured bidirectional changes in  $V_m$  ramp amplitude by BTSP. Plasticity rules were estimated by two-dimensional interpolation from model data (see Materials and Methods). (A – C) Model predictions from variants of the weight-dependent model with 75 cm (A), 90 cm (B), or 105 cm (C) CA3 input place field widths. (D) Residual error of ramp depolarizations predicted by each model is averaged across spatial bins and cells.