Data and text mining

Visibility Graph Based Community Detection for Biological Time Series

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Abstract

Motivation: Temporal behavior is an essential aspect of all biological systems. Time series have been previously represented as networks. Such representations must address two fundamental problems: (i) How to create the appropriate network to reflect the characteristics of biological time series. (ii) How to detect characteristic temporal patterns or events as network communities. General methods to detect communities have used metrics to compare the connectivity within a community to the connectivity one would expect in a random model, or assumed a known number of communities, or are based on the betweeness centrality of edges or nodes. However, such methods were not specifically designed for network representations of time series. We introduce a visibility-graph-based method to build networks from different kinds of biological time series and detect temporal communities within these networks.

Results: To characterize the uneven sampling of typical experimentally obtained biological time series, and simultaneously capture events associated to peaks and troughs, we introduce the Weighted Dual-Perspective Visibility Graph (WDPVG) for time series. To detect communities, we first find the shortest path of the network between start and end nodes to identify nodes which have high intensities. This identifies the main stem of our community detection algorithm. Then, we aggregate nodes outside the shortest path to the nodes found on the main stem based on the closest path length. Through simulation, we demonstrate the validity of our method in detecting community structures on various networks derived from simulated time series. We also confirm its effectiveness in revealing temporal communities in experimental biological time series. Our results suggest our method of visibility graph based community detection can be effective in detecting temporal biological patterns.

Availability: The methods of building WDPVG and visibility graph based community detection are available as a module of the open source Python package PyIOmica (https://doi.org/10.5281/zenodo.3691912) with documentation at https://pyiomica.readthedocs.io/en/latest/. The dataset and codes we used in this manuscript are publicly available at https://doi.org/10.5281/zenodo.3693984.

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1 Introduction

Longitudinal behavior is an inherent aspect of all biological systems, and has been widely investigated in various contexts, such as systems biology (Alon, 2006), metabolic pathway analysis (Berk et al., 2011), and, recently, gene expression (Bar-Joseph et al., 2012). With the development of novel technologies in sequencing, mass spectrometry and other omics, multi-level biological time series are becoming easier to obtain. An important example is provided by longitudinal data from personal health monitoring devices. Recent studies have shown that omics time series have a wide range of applications in personal health and precision medicine. Multi-omics time series data can be used in precision health (Rose et al., 2019), and have provided insights into the onset of type 2 diabetes mellitus (Zhou et al., 2019) and lung development Ding et al. (2019). Omics time series can also be used to monitor health events, changes in physiological states (Piening et al., 2018; Stanberry et al., 2013) and in molecular and medical phenotypes (Chen et al., 2012). The rapidly increasing
availability of biological time series requires new methods to integrate different types of data, analyze them, and interpret the results in a fast and informative way. Many platforms for multi-biological and multi-omics data integration have been developed, including software such as DAVID (Sherman et al., 2009), Galaxy (Giardine et al., 2005) and GenePattern (Reich et al., 2006). Here, in the NVG formulation, an edge is added connecting nodes based their inter-visibility to obtain a visibility graph (VG) representation of the time series (Lacasa et al., 2008), which recently attracted great interdisciplinary interest (Ahmadlou et al., 2010; Luque et al., 2011; Zhu et al., 2014; Zou et al., 2014; Bhaduri and Ghosh, 2015). There are two types of VG typically considered: (i) the Natural Visibility Graph (NVG) and, (ii) the Horizontal Visibility Graph (HVG) (Luque et al., 2009).

To construct a VG, we consider \( s(t_i), s(t_j) \) as \( i, j \) if any other time point \( t_k \), between \( t_i \) and \( t_j \), has a corresponding intensity \( s(t_k) \) that lies below the line connecting \( s(t_i) \) and \( s(t_j) \) (i.e. there is a direct line-of-sight between these peaks). The HVG has a simpler edge construction condition: an edge is added connecting nodes \( i, j \) if only if all intermediate intensities \( s(t_k) \) are less than both \( s(t_i) \) and \( s(t_j) \).

NVGs and HVGs are connected networks. The VG conserves the structure of the time series in the graph topology (Lacasa et al., 2008). However, the HVG original constructions do not account explicitly for the potential effects of uneven time sampling or missing time points. In the NVG such uneven sampling results in different visibility of timepoints (changes in viewing angles in the construction), which implicitly incorporates the effect of time distances, but without explicitly weighting the edges the actual distance between nodes cannot be accounted for. In realistic situations outside a laboratory setting, uneven sampling occurs often. This may be due to technical limitations (for example in mass spectrometry proteomics technical replicates may still sample different proteins and lead to missing data and hence uneven sampling), or limitations in subject participation (for example in clinical trials and human subject research, the subjects’ work-dependent schedules may affect their regular participation). These shortcomings limit the traditional VG application in biological/medical time series analysis. Another limitation of the traditional VG is the inability to simultaneously capture peaks and troughs (points below the baseline). For example, the VG maps sinusoidal and cosinusoidal time series to different graphs, but these two kinds of time series should be considered equivalent up to a change of phase.

Another challenge in network representations of biological time series is the lack of specific methods for detecting temporal communities. A community is defined as a group of nodes, where the nodes within a community are tightly connected, whereas the nodes between different communities have loose connections (Girvan and Newman, 2002). Each community in complex networks representing biological time series thus identifies nodes with similar temporal behavior that are likely to represent the same biological system status. One highly effective approach for identifying communities is to compare the actual number of intra-community edges to what one would expect by a random placement of the edges (Girvan and Newman, 2002; Clauset et al., 2004; Newman, 2006). This approach is based on the assumption of a random graph null model. However, VGs cannot be considered as random graphs, even if a VG is constructed based on a random time series. This is due to the sequential nature of the nodes, the resulting connected graph, and the underlying degree distribution (Luque et al., 2009).

In this investigation, we introduce the method of “weighted dual perspective visibility graph” (WDPVG) for mapping time series to complex networks. Our WDPVG approach considers uneven sampling effects, and simultaneously captures peaks and troughs of time series. Previously, VG edge weights have been assigned based on the arc tangent of \( (s(t_j) - s(t_i)) / (t_j - t_i) \), which computes the “view angle” along the direct line-of-sight connecting one intensity peak to another (Supriya et al., 2016). Our method provides multiple choices for the edge weights: (i) the Euclidean distance between nodes/intensity peaks, (ii) the tangent of the view angle between two nodes, (iii) the time difference between time points corresponding to connected nodes, or (iv) none. We then combined the natural view perspective VG with the “reflected view perspective VG” introduced in the methods below to create a complex network that can capture both the positive and negative intensities changes. We note, that this is the first time that Euclidean distance has been used for edge weights in VGs, to the best of our knowledge.

We also provide a new VG community detection method, which is based on shortest path calculations between VG nodes. Our method is suitable for VGs as it does not depend on random graph null models, which are commonly used in other widely used approaches, such as Newman’s method (Newman, 2006). Briefly, as described below, we compute the shortest path of the VG between start and end nodes as a main stem. The nodes on the main stem are seeds for communities, and we then aggregate nodes outside the shortest path to their most proximal seed nodes on the main stem, where proximity is determined using graph path lengths.

We used various simulated time series to test our method effectiveness, and demonstrated that our method has high tolerance for uneven sampling and signal noise. Our comparison of our method to traditional community detection methods, such as Girvan-Newman (Girvan and Newman, 2002) and Louvain (Blondel et al., 2008), indicated that our approach is more suitable for VGs. To show that our method can capture biological processes we also applied it to several experimentally obtained time series, longitudinal multi-omics data from blood components in prediabetes (cytokines, glucose and haemoglobin Alc) (Zou et al., 2019), saliva omics data (mean gene expression) (Domanskyi et al., 2019) and signals from wearable biosensors (radioactivity exposure) (Li et al., 2017).

The methods of building WDPVG and visibility graph based community detection are available as a module of the open source Python package PyOMica (Domanskyi et al., 2019). The dataset and codes we used as described below are available with a Python notebook, publicly available online at https://doi.org/10.5281/zenodo.3693984.
2 Materials and methods

2.1 Weighted dual perspective visibility graph (WDPVG)

The VG can characterize time series in terms of complex network theory as it can inherit the structure properties of the time series data from which it was created. VGs are robust to noise and not affected by the selection of method parameters (e.g. cutoffs/thresholds) (Liu et al., 2015). VGs have been widely applied in many fields (Supranya et al., 2016; Stephen et al., 2015; Bezsudnov and Snarskii, 2014). However, as we discussed above, the VG has two disadvantages: first, it does not consider the effect of uneven sampling; second, it cannot capture the time series changes below a zero baseline. Here we provide a new method, WDPVG, to overcome these limitations that restrict VG applications to biological time series analysis.

We use the following four steps to create WDP VGs, utilizing auxiliary natural visibility graphs (NVGs).

Step 1: NVG construction. We create an NVG from time series \(x(t)\), where \(t = 1, 2, 3, \ldots, N\), as it was described above by equation 1, using the NVG mapping criteria.

Step 2: Assign edge weights between two nodes. We have flexible choices for the edge weight between two nodes, including no weight, Euclidean distance (Equation 2), the tangent of the view angle (Equation 3), or the time difference (Equation 4):

\[
\begin{align*}
    w_{ij} & = \sqrt{(s(t_i) - s(t_j))^2 + (t_i - t_j)^2}, \\
    w_{ij} & = \frac{|s(t_i) - s(t_j)|}{t_i - t_j} + 10^{-8}, \\
    w_{ij} & = |t_i - t_j|, \\
\end{align*}
\]

where, \(w_{ij}\) represents the weight of the edge between nodes \(i\) and \(j\), which correspond time points \(t_i\) and \(t_j\) respectively, in time series \(\{s(t)\}\). In equation 3, we added the offset \(10^{-8}\) to account for the case \(s(t_i) = s(t_j)\). The algorithm implementation details are available in the documentation of the functions in PyOmicca. In this manuscript, we use Euclidean distance between nodes as the edge weight.

After Step 2, we compute the adjacency matrix, \(A\), of the normal perspective NVG.

Step 3: Compute the reflected perspective NVG. We invert the time series \(\{s(t)\}\) by reflecting across the time axis, i.e. for each \(s(t_i)\) in \(\{s(t)\}\), let \(s'(t_i) = -s(t_i)\), where we obtain the inverted time series \(\{s'(t)\}\). We then repeat Steps 1 and 2 for \(s'(t)\) to get the reflected perspective NVG and the adjacency matrix \(A'\).

Step 4: Combine the normal perspective NVG and reflected perspective NVG. For any pair of \(i, j\), elements \(A_{ij}\) and \(A'_{ij}\) have two possible relationships: either \(A_{ij} = A'_{ij}\), or one of them is 0 but the other one is non-zero. We can combine the \(A\) and \(A'\) to get the WDPVG adjacency matrix \(A^b\) by the following criteria:

\[
A^b_{ij} = \max\{A_{ij}, A'_{ij}\}
\]

If we use the HVG mapping criteria, i.e. \(s(t_i), s(t_j) > s(t_k)\), \(t_i < t_k < t_j\), instead of the NVG mapping criteria, we can obtain the weighted dual perspective horizontal visibility graph.

It is important to note that in case that either we are not interested in changes below the baseline, or that the intensities of the time series are all non-negative, the normal perspective weighted VG is enough, and we do not need to create a WDPVG.

2.2 Shortest path based community detection

The shortest path in a VG between the start node (corresponding to first time point) and end node (corresponding to last time point) identifies a bundle of nodes which have high intensities, and thus is the determining factor for the entire network structure. This shortest path acts as a stem for community identification in VG. Our method chooses the shortest path between start node and end node in VG as the main stem, and each node on this stem is a natural hub of a community, as described below.

Let nodes \(\{v_i'; i = 1, 2, 3, \ldots, k\}\) be the \(k\) nodes on the shortest path of start node and end node in a VG. \(\{v_i'; i = 1, 2, 3, \ldots, m\}\) are the nodes outside the shortest path, where \(m = N - k\). For any nodes \(v_i'\) in \(\{v_i';\}\), we compare the shortest path length between \(v_i'\) and each node in \(\{v_i'\}\) to identify the minimal path length \(l_{iq}\) and corresponding node \(v_j\) in \(\{v_i'\}\), to assign the left hub, which corresponds to the earlier time point, as the target community’s hub. We then iterate through all nodes in \(\{v_i'\}\), to get the initial community structure.

Finally, we measure the shortest path length between any pairs of hubs, i.e. the nodes in \(\{v_i'\}\), and if the shortest path length between them is less than a chosen cutoff, \(\epsilon\), we then combine the two communities to obtain the final community structure.

Normally, the minimal \(\epsilon\) is the cutoff for which the network has the same number of communities as the number of hubs. Similarly, the maximal value of \(\epsilon\) corresponds to the case where the whole network becomes a single community. By changing the value of \(\epsilon\) between minimum and maximum, we can get the most stable community structure, i.e. the number of communities stabilizes when iterating with increasingly larger \(\epsilon\). Thus, we can optimize the community structure. In our algorithm, we have provided the following options for cutoff selection: (i) with or without cutoff, (ii) fixed cutoff, or (iii) automatically optimized cutoff based on a plateau in number of communities as a function of \(\epsilon\). This feature is unique to our method.

Another unique feature of our method is that we can choose the direction of how the nodes are connected in the community construction. Specifically, we can restrict the nodes \(v_i'\) in \(\{v_i'\}\) to only link to the community with hub \(v_o'\) for which the corresponding time point \(t_o\) is earlier than the time point \(t_i\) corresponding to \(v_i'\). This feature essentially imposes a causality condition, where time points only depend on other past time points, and not future ones. It is important to keep time order in the community detection for characterizing biological time series from living systems. We have allowed flexibility in the implementation of the method, so the user can also choose node linking directions as earlier side, later side or both sides - this may be required for systems where there is time reversal symmetry.

Note that our method of shortest path based community detection may be used not only for WDPVG, but also for all kinds of visibility graphs, such as HVG and NVG.

Figure 1 provides a simple illustration of how our method works. A simulated time series is created from a cosine wave signal mixed with 40 percent random noise (Figure 1 A). Then, we construct the weighted NVG and the reflected perspective NVG in Figure 1 B and C. Afterwards, the weighted dual natural visibility graph is created by combining the NVG and the reflected perspective NVG (Figure 1 D). We use our community detection method to the graph in Figure 1 E showing the communities corresponding to the original time series.

2.3 Simulation

We used simulated time series to evaluate our method. We illustrate here three types of time series: cosine, square, and saw-tooth wave signals. Then we added different intensity random noise to each of
Illustration of the construction of weighted perspective visibility graph and community structure based on the shortest path length community detection method. A is the simulated time series cosine signal with 40 percent noise in intensity. We construct the weighted NVG and reflected NVG, where the edge weights are based on Euclidean distance. Edge connections of NVG and reflected NVG are illustrated in B and C respectively. The dual weighted perspective visibility graph is created by combining NVG and reflected NVG, as shown in D. Where the links with red color come from NVG, and the blue links come from the reflected NVG. Using our shortest path length based community detection method, we can find the community structure of the time series, as shown in E. The time points in the same community are encircled by a blue outline, and the color of the nodes represents the signal intensity. The time series separates into two communities that capture the cosine signal’s periodicity.

These signals to test the tolerance of the community detection to noise. We also randomly removed different percentages of time points from these time series to check the robustness to missing data and the resulting uneven sampling. We then built the WDPVG for these time series, and detected communities using our method. The results of our method were compared to traditional community detection methods such as the Louvain method, which is a widely used method of fast greedy optimization of modularity (Blondel et al., 2008), and the Girvan-Newman hierarchical method which is based on centrality notions (Girvan and Newman, 2002). The Louvain method was implemented using the Python python-louvain package, (https://github.com/taynaud/python-louvain). The Girvan-Newman method is available in NetworkX, which is the most popular open source network analysis package in Python (Hagberg et al., 2008).

2.4 Experimental biological time-series applications

We also compared the results of our method to the Louvain and Girvan-Newman methods when applied to several experimentally acquired biological datasets. These datasets used are summarized below.

**Saliva Set (DS1).** We used a saliva RNA-sequencing dataset we generated, that was obtained from a clinical trial monitoring individualized response to the standard 23-valent pneumococcal polysaccharide vaccine (PPSV23). The saliva was sampled from a healthy individual. We constructed the VG from the time series and detected the communities, as well as community structures.

**Diabetes Set (DS2).** The second dataset came from personal multi-omics profiling data (e.g. including blood measurements of A1C, fasting glucose and selected immune cytokines etc.) from individuals with Type 2 diabetes mellitus at its earliest stage (Zhou et al., 2019). As an example, we chose one individual’s A1C, fasting glucose and selected immune cytokines data from the rich dataset, as reported by the authors. These time series include 14 time points with different healthy condition. We constructed the VG from the time series and detected the communities, to assess whether our method can capture the physiological status of the subject for these time series.

**Radiation Exposure Set (DS3).** Finally, we analyzed a radiation exposure time series dataset from wearable biosensors (Li et al., 2017). The data collected were hourly personal radiation exposure, assessed by a wearable biosensor for more than 100 days. We chose one day spans (24 hours, from 12 am to 11 pm) as the natural time window. We then analyzed separately four days when the individual of this study had flight activity, and the radiation reported on these days was higher than non-flight days. We then applied our methods to assess if we can detect the radiation events as community structures.

3 Results

3.1 Simulation

To investigate whether our method captures periodic features we simulated well-defined periodic time series. We compared our path-length based method (PL) with two widely used community detection method, the Louvain method (LN) (Blondel et al., 2008) and the Girvan-Newman method (GN) (Girvan and Newman, 2002). Figure 2 shows the signal intensity and communities for the cosine and square wave signals’ time series (top and bottom, respectively). The communities our method detected matched exactly with the signal periods. The Louvain method obtained some unmatched results in the case of the cosine signal time series. Finally, the Girvan-Newman method obtained coarser results compared to the other two methods. In addition, Figure 3 shows results on the tolerance to noise and missing data for cosine wave (Figure 2A-D), square wave (Figure 2E-H), and saw-tooth wave signals (Figure 2I-L). Compared to the Louvain and Girvan-Newman methods, our method displays higher tolerance in either situation of noisy signals or uneven sampling. Whenever we added noise from 20 percent to 80 percent, or additionally removed time points from 10 percent to 40 percent, our method still captured the periodic changes. To the contrary, the results of the two traditional methods were irregular, with coarsely defined communities and multiple nodes in communities unmatched with the corresponding signal’s period. Even though the Louvain method worked well in the perfect square wave signal time series (e.g. without noisy and uneven sampling), the method showed low tolerance to noise or time point removal.

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**Fig. 1.** Illustration of the construction of weighted perspective visibility graph and community structure based on the shortest path length community detection method. A is the simulated time series cosine signal with 40 percent noise in intensity. We construct the weighted NVG and reflected NVG, where the edge weights are based on Euclidean distance. Edge connections of NVG and reflected NVG are illustrated in B and C respectively. The dual weighted perspective visibility graph is created by combining NVG and reflected NVG, as shown in D. Where the links with red color come from NVG, and the blue links come from the reflected NVG. Using our shortest path length based community detection method, we can find the community structure of the time series, as shown in E. The time points in the same community are encircled by a blue outline, and the color of the nodes represents the signal intensity. The time series separates into two communities that capture the cosine signal’s periodicity.
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3.2 Experimental biological time-series applications

We then applied our method to the experimentally acquired biological time series summarized in the method section above. First we used our method to detect communities from the saliva omics monitoring experiment, DS1. We chose genes signals from the data displaying autocorrelation at lag 1 (simulation adjusted p-value < 0.01), and calculated the average across the signals for each time point. The average signal intensity is shown in Figure 4 A top. We then built the WDPVG from this signal and we obtained temporal communities using the different methods in Figure 4 A bottom. The community structure was found to reflect the four physiological states over the 24 hours: (i) pre-vaccination baseline, (ii) post-vaccination to fever onset, (iii) fever onset to resolution, (iv) post vaccination baseline.

Finally, we applied our method to four separately days’ radiation exposure measurements from DS3. We show the four separate day results with high radiation exposure changes (when the individual was traveling by flight on these days) in Figure 4 C. The community structures of these four days all capture the radiation exposure changes, acting as an adverse event detector. Again, the PL method is more concordant with the radiation exposure timeframes overall, without mixing of timepoint in the communities.

4 Conclusion

We have introduced new methods to characterize graphs derived from time series through the application of VGs. We have introduced WDPVGs that combine normal perspective and reflected perspective visibility graphs, so that the peaks and troughs of a time series can be simultaneously represented. The WDPVGs also take into account uneven sampling effects through weight assignments to the edges. The WDPVG approach thus produces a graph that captures well the characteristics of the underlying time series.

We have also developed a new method to detect communities of VG. Our VG community detection method is based on the graphs geometry and considers the shortest path from the start node to the end node. The method does not assume a random graph null model. This makes the method advantageous and more appropriate for all kinds of VGs (e.g. NVG, HVG or WDPVG), because VGs cannot be compared to random graphs due to the sequential nature of time points.

The several simulated time series we used to test our WDPVG and VG community detection methods supported their validity. Our methods also showed high tolerance for uneven sampling and signal noise. Our PL community detection method showed robustness to noise compared to traditional community detection methods such as the Louvain and Girvan-Newman methods. Overall, the results suggest that our approach is better suited for community detection within VGs.

The application of our method to experimental biological datasets gave examples of how the method may be used to identify temporal communities that correspond to physiological states (e.g. physiological state of a subject, changes in molecular measurements due to vaccination, or detection of radiation exposure). The method has great potential not only for detecting the boundaries of biological temporal states, but for medical implementation in detecting potential adverse medical events from temporal measurements.

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References


Fig. 3. Community structure of different simulated signal time series. We simulated 3 types of signals: cosine time series $A$-$D$, square wave time series $E$-$H$ and saw-tooth wave time series $I$-$L$. The community structure is represented by color bar, with time points in same community assigned the same color. For each kind of signal, we also added 20 percent and 80 percent noise (the first and second subplots of each row respectively) to check the robustness to missing data and uneven sampling. We compared our method (PL, first color bar of each subplot) with the two traditional community detection methods, Louvain method (LN, second color bar) and Girvan-Newman method (GN, third color bar). Our method identifies community structures matching with the characteristics of the various time series, even in the presence of noise or missing data.
Fig. 4. Results of our visibility graph based community detection method applied to experimental biological datasets. A shows the results of applying different methods to an individual’s saliva-omics time series before and after their vaccination, over a 24 hour period. The time series indicates average gene expression for a subset of genes with autocorrelated behavior. The VG nodes’ color in A bottom represents the intensities of the time series, and nodes belonging to the same detected community are framed by a blue border. The communities correspond well to the four physiological subject states of biological significance: prior to vaccination, after vaccination, a post vaccination fever period and resolution, post fever relative recovery.

B The standardized intensities of A1C, fasting glucose and selected immune cytokines time series from a subject with Type 2 diabetes (B top left) and their community structure (B left) are shown for different methods. The data are ordered temporally from left to right, and physiological states are indicated per timepoint as one of H (healthy), S (stress), Ax (antibiotic regiment) and Im (immunization) states. For the experimental data, warm colors indicate higher and colder colors lower intensities respectively. In the methods’ results, nodes belonging to the same community are depicted with the same color bar. The communities structure reflects the changes in physiological state that result from molecular intensity differences.

C The radiation intensity data from wearable biosensors in four separate days including flight activity are shown. The red disc indicates that the radiation was recorded during the airport carry-on luggage check. Stars represent radiation monitored during flight timepoints. Again, nodes in the same community are indicated with the same color in the horizontal bars. The PL community structures during each of these four days indicate the periods of varying radiation exposure, and correctly identify the onset of the exposure.
