1   **Frequency-dependent interactions determine outcome of competition between two breast**

2   **cancer cell lines**

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Highlights:

- Demonstrate how mixed-culture spheroids must be used to characterize competition between two cancer cell lines.

- Competition alters growth dynamics of cancer cells.

- Competition growth models can be used to quantify density-independent, density-dependent and frequency-dependent effects on competition.

- Competition affects tumor progression and structure, making it key to understanding tumor development and evolution.

ABSTRACT:

Tumors are highly dynamic ecosystems in which diverse cancer cell subpopulations compete for space

and resources. These complex, often non-linear interactions govern continuous spatial and temporal

changes in the size and phenotypic properties of these subpopulations. Because intra-tumoral blood

flow is often chaotic, competition for resources may be a critical selection factor in progression and

prognosis. Here, we quantify resource competition using 3D spheroid cultures with MDA-MB-231 and

MCF-7 breast cancer cells. We hypothesized that MCF-7 cells, which primarily rely on efficient aerobic

glucose metabolism, would then dominate the population under normoxic conditions; and MDA-MB-

231 cells, which exhibit high levels of glycolytic metabolism, would dominate under hypoxic conditions.

In spheroids with single populations, MCF-7 cells exhibited equal or superior intrinsic growth rates

(density-independent measure of success) and carrying capacities (density-dependent measure of

success) when compared to MDA-MB-231 cells in both normoxic and hypoxic conditions. However,

when the populations were mixed, MDA-MB-231 cells outcompeted MCF-7 cells under all conditions

with competition dynamics determined by frequency-dependent interactions. When grown together,

MDA-MB-231 suffered little from MCF-7 while MCF-7 cells experienced a disproportionately large

reduction in growth rates in the presence of MDA-MB-231 cells. We frame these results in a game-

theoretic (frequency-dependent) model of cancer cell interactions and conclude that competition assays

can demonstrate critical density-independent, density-dependent and frequency-dependent

interactions that likely contribute to *in vivo* outcomes.

Key Words: cancer cell competition, tumor ecology, tumor evolution, evolutionary therapy

INTRODUCTION:

Each malignant tumor typically contains diverse and heterogeneous habitats due to spatial and temporal

variations in cell density, immune infiltration, and blood flow (1-3). Here, we investigate the

evolutionary effects of variations in substrate (e.g. glucose, oxygen, and glutamine) and metabolites

(e.g. H^+) that are typically governed by alterations in blood flow. These changes, in turn, can alter the

local fitness (competitive advantage) of the extant cell populations that can have dramatic evolutionary

effects on the phenotypic and genotypic properties of the cancer cells.

Recently, two general "niche construction" strategies were observed in clinical and pre-clinical cancers

(4, 5). The first consists of cancer cells that possess high levels of aerobic glycolysis that generate an

acidic environment which promotes invasion and protects cells from the immune system. These cells are

typically invasive and motile. In the second niche construction strategy, cancer cells promote growth by

recruiting and promoting blood vessels. This angiogenic phenotype is typically non-invasive and

maintains near-normal aerobic metabolism of glucose. These divergent phenotypes can be found within

the same tumor (6-9). The invasive "pioneer" phenotype is optimally adapted to survive and thrive at

the tumor edge. There it can co-opt normal tissue vasculature as it invades, and its acidic environment

provides protection from immune cells at the tumor-host interface. In contrast, the "engineer" cancer

cells are well suited to the interior regions of the tumor where their angiogenic phenotype can, with

varying degrees of success, provide blood flow necessary to deliver substrate and remove metabolites.

When the pioneers and engineers interact, they presumably compete for both space and substrate.

However, the specific phenotypic traits that confer maximal fitness under different micro-environmental

conditions have not been well established.

Competition between two species leads to four possible outcomes: 1) species A outcompetes B, 2) B

outcompetes A, 3) A or B outcompetes the other depending upon who establishes first (alternate stable

states), or 4) the two species coexist. These population dynamics can be mathematically framed through

the Lotka-Volterra equations for inter-specific competition (10, 11). Derived independently by Lotka

(1910) and Volterra (1920), the eponymous equations were first tested empirically by Gause (1932) in

the, now classic, competition experiments using various species of *Paramecium* and yeast (12, 13). This,

and subsequent work on fruit flies, flour beetles, and various natural systems, have confirmed the

predictive power of the Lotka-Volterra equations (14, 15). Such assays utilize growth dynamics to

elucidate the critical phenotypic properties that determine fitness under different environmental

conditions (16).

In ecological systems, growth dynamics are divided into three categories: *density dependent* (DD),

density independent (DI), and *frequency dependent* (FD) effects. Density dependent (DD) effects occur

when one cancer cell type outcompetes another because it can achieve a higher equilibrium cell density

(carrying capacity) under conditions of space or nutrient limitations. *Density independent* (DI) effects

include intrinsic growth rate, which measures the capacity of a cell line to grow exponentially under

ideal conditions. In cell biology, these (DD and DI) are often used as indicators of cell fitness (17-19).

This, however, ignores the FD interactions which often determine competitive outcomes. Frequency

dependent (FD) effects occur when one cell type outcompetes another because its phenotype

disproportionately depresses the growth rate of another as a result of more rapid resource uptake, or

via direct interference with the other cell type. This game theoretic effect implies that the success of an

individual cell is context dependent. It depends not only on the density of other cells around it, but the

phenotypes of those cells as well (20, 21). Because of this, FD effects and the outcome of competition

can only be evaluated using Gause-style competition assays in which mixtures of the two cell types are

grown together using different starting frequencies.

Here, we utilize Gause-style competition assays to investigate the competitive interaction between

engineer and pioneer phenotypes. These strategies will be represented by the well-characterized MDA-

MB-231 and MCF-7 cell lines which are often used as representative of the highly glycolytic and invasive

and low glycolytic and non-invasive phenotypes, respectively (22-26). Assays were conducted in 3D

spheroid cultures with varying starting frequencies of each cell type. The spheroid system was selected

as an *in vitro* intermediate between 2D cell culture, which may reach an equilibrium state through

confluence rather than resource competition, and *in vivo* subcutaneous mouse models, which provide

less opportunity for replication and frequent monitoring of the two cell populations (27-34). Spheroids

were grown in various combinations of pH and glucose concentrations, letting the 3D structure provide

natural nutrient and oxygen gradients. Glutamine availability was also varied to test for growth and

competition effects due to secondary nutrients.

As in the Gause experiments, measures of growth dynamics were used to evaluate competitive ability.

DI, DD, and FD effects corresponded to selection for higher growth rates, carrying capacities, and

competitive ability, respectively. Carrying capacities (DD) were estimated from monoculture spheroids in

varying culture conditions. Initial growth rates (DI) of each cell type were estimated from both mono-

and co-cultured spheroids. As FD effects rely on interactions between cell types, their values were

estimated using the Lotka-Volterra competition model. In order to remain agnostic to the mode of

tumor spheroid growth, our growth model was selected by first fitting monoculture spheroids to four

common growth models (exponential, Monod, logistic, and Gompertz), then selecting the model which

best approximated the growth of monoculture spheroids in all culture conditions. This model was then

expanded to its two-species competition form and used to obtain estimates of competition coefficients

for each cell line under eight different nutrient conditions.

Based on published experimental studies, we expected both cell types to have higher growth rates and

carrying capacities at physiological pH (pH 7.4) and higher nutrient levels. MCF-7 cells, which

predominantly use oxidative phosphorylation for metabolism of glucose, was predicted to be

significantly inhibited by low pH, while MDA-MB-231 cells, which exhibit the Warburg phenotype with

high levels of aerobic glycolysis, was expected to be more tolerant. Because the glycolytic MDA-MB-231

cells need more glucose to produce energy compared to the oxygen-consuming MCF-7 cells, we

expected the former to respond more favorably to increased glucose concentrations than the latter. We

also predicted that, based on their metabolic differences, MCF-7 cells would be fitter under conditions

of normal pH and low glucose; and vise-versa for the MDA-MB-231 cells.

Herein, we test our hypothesis through competition experiments between the MCF-7 and MDA-MB-231

cells under varying environmental conditions. We report the outcome of these competition assays as

well as the effect of nutrient availability on DD and DI effects and evaluate their ability to indicate

competitive outcome. We used fluorescent measurements to approximate cell growth in the spheroid

and propose that the logistic growth equation best approximates the growth of both cell types in the

majority of culture conditions. We then used Lotka-Volterra competition equations to determine the

contribution of population growth rates (DI), maximal population size (DD) and/or competition

coefficients (FD) on the outcome of interspecific competition. Lastly, we compared these results to the

outcome of competition between MDA-MB-231 and MCF-7 from mixed tumors *in vivo*.

RESULTS:

MDA-MB-231 out-compete MCF-7 cells under all pH, glucose and glutamine levels, and starting

frequencies

Fluorescently labeled MCF-7 (GFP) and MDA-MB-231 (RFP) cells allowed us to non-destructively

measure population dynamics within each micro-spheroid. We used this spheroid system to: 1) observe

the outcome of competition (mixed culture), 2) compare population growth models (mono-cultures), 3)

measure intrinsic growth rates (DI), 4) measure carrying capacities (DD), and 5) determine competition

coefficients (FD). In experiments 1 and 2, spheroids started with a plating density of 20,000 and 10,000

cells, respectively, with initial conditions of 0%, 20%, 40%, 60%, 80% and 100% MDA-MB-231 cells

relative to MCF-7 cells. In experiment 1, additional treatments included neutral (7.4) versus low (6.5) pH

and varying levels of glucose (0, 1, 2, 4.5 g/L) (Figure 1B). Experiment 2 had treatments of pH (7.4, 6.5),

glucose (0, 4.5 g/L), and glutamine positive and starved media (Figure 1C). Both experiments were

further subdivided into parts A and B based on culture conditions (Figure 1 provides details). In

experiment 1, microspheres were grown for 670 hours with fluorescence measured every 24-72 hours.

In experiment 2, microspheres were grown for 550 hours with fluorescence measured every 6-12 hours.

Growth medium was replaced every 4 days without disturbing the integrity of the microsphere.

A.

	MCF-7	MDA-MB-231
Source Tissue	Luminal Epithelium	Basal Epithelium
Cancer Type	Invasive Ductal Carcinoma	Adenocarcinoma
Receptor Status	ER+, PR+, EGFR-, HER2-	ER-, PR-, EGFR+, HER2-
Properties	Strong Cell-Cell Adhesion	Weak Cell-Cell Adhesion
	Non-Invasive	Invasive
	Normal Glucose Metabolism	Upregulated Aerobic Glycolysis

B.

Glucose

pH	0 g/L / 7.4	0 g/L / 6.5
	1 g/L / 7.4	1 g/L / 6.5
	2 g/L / 7.4	2 g/L / 6.5
	4.5 g/L / 7.4	4.5 g/L / 6.5

C.

Glutamine Absent Conditions	Glutamine Positive Conditions
Glucose	Glucose
0 g/L / 7.4, 0 g/L / 6.5, 4.5 g/L / 7.4, 4.5 g/L / 6.5 (pH)	0 g/L / 7.4, 0 g/L / 6.5, 4.5 g/L / 7.4, 4.5 g/L / 6.5 (pH)

Figure 1: A. Phenotype and source information for the "niche constructing" MCF-7 and the "pioneer" MDA-MB-231 cell lines. **B.** Growth dynamics of monoculture and mixed population tumor spheroids in glucose concentrations of 0 g/L and 2 g/L (experiment 1A, in dark gray) and of 1 g/L and 4.5 g/L (experiment 1B, in light gray) were compared at physiological (7.4) and low (6.5) pH. **C.** Experiment 2 measured the growth dynamics of mixed population tumor spheroids in 4.5 g/L glucose and 0 g/L glucose, in physiological (7.4) and low (6.5) pH, and with (experiment 2A, in dark gray) and without (Experiment 2B, in light gray) glutamine to evaluate differences in growth due to the presence of a secondary nutrient.

157   In mixed cultures and regardless of initial conditions (starting frequencies, pH, glucose and glutamine),

158   MDA-MB-231 outcompeted MCF-7 cells (Figure 2). Contrary to our hypothesis, MCF-7 did not

159   outcompete the MDA-MB-231 cells under conditions of low glucose and neutral pH. This raises the

160   question of whether the success of the MDA-MB-231 was a consequence of higher intrinsic growth

161   rates, increased carrying capacities, or consistently favorable competition coefficients.

Figure 2: Outcome of competition for all starting frequencies in 2g/L glucose and neutral pH. In all

starting conditions, MDA-MB-231 outcompete MCF-7.

MCF-7 cells have a higher intrinsic growth rate under all culture conditions

In both experiments, MCF-7 cells had similar or significantly higher intrinsic growth rates compared to

MDA-MB-231 cells (Figures 3A & 4A). The absence of glutamine reduced the difference in instantaneous

growth rates between the two cell types, regardless of pH or glucose concentration (Figure 3A),

consistent with its role as a substrate for respiration, which is more pronounced in MCF-7 cells.

Separate three-way ANOVAs were performed for the two cell types and experiments 1 and 2 to

determine the effects of culture conditions. In these ANOVAs, pH (low versus high), nutrient level

(either various glucose of glutamine levels), and starting frequencies of cell types were the independent

variables (Supplementary tables 1-4).

As expected, the growth rate of MCF-7 cells generally increased with glucose concentration, but pH had

little effect. There were some notable significant interaction effects between glucose and pH. In

experiment 1A, growth rates decreased with pH in the absence of glucose and increased with pH in the

presence of glucose. In experiment 1B, growth rates did not vary with pH at low glucose (1g/L) but

showed a notable and unexpected decline with pH at high glucose (4.5 g/L). In experiment 2, the

exception to increasing growth rates with increased pH and glucose occurred for glutamine positive,

neutral pH conditions. In this case, growth rates declined with glucose. Growth rates did not vary

significantly with glucose concentration or pH in the presence of glutamine. In the absence of glutamine,

the growth rate of MCF-7 cells significantly increased with increased pH and this effect was amplified in

the absence of glucose.

Unexpectedly, the growth rates of MDA-MB-231 tended to decline with glucose. In experiment 1A and

1B, growth rates decreased significantly with glucose concentration and increased with pH. In

experiment 2A, growth rates also declined significantly with glucose. The effect of pH was dependent

on the presence of glutamine. With glutamine, growth rates declined with pH (higher under acidic

conditions) and, without glutamine they increased with pH. It may be that glucose is less an essential

nutrient than a nutrient used to gain a competitive edge on one's neighbors. We will elaborate more on

this counter-intuitive result in the discussion.

The initial frequencies of cell types had revealing effects on the instantaneous growth rates. In all

experiments, both cell types had lower growth rates as the frequency of MDA-MB-231 increased (Figure

3C & 4C). In experiment 2, when there is glutamine present, starting frequency is the only variable which

significantly affected growth rates. At the lower starting densities (experiment 2) in the presence of

glucose, MCF-7 cells show an increase and then a sharp decline (at 80%) as the frequency of MDA-MB-

231 cells in the starting population increased. In general, under all culture conditions, both cell types

have slower initial growth rates with increasing starting frequency of MDA-MB-231. In summary, the

higher intrinsic growth rate of MCF-7 cells (DI effects) does not predict which cell type outcompetes the

other.

MCF-7 cells have a higher Carrying Capacity in all culture conditions

In both experiments, the MCF-7 cells reached the same or significantly higher carrying capacities than

MDA-MB-231 (Figures 3B & 4B). For both cell types, in the presence of glutamine, carrying capacities

increased with glucose in neutral pH conditions. Surprisingly, the MCF-7 cells experienced a decrease in

carrying capacity with increasing pH, whereas the MDA-MB-231 experienced an increased carrying

capacity with pH. This was observed regardless of glutamine status. The only exception to this behavior

was in acidic (2g/L glucose, 6.5 pH with glutamine) conditions, where the MCF-7 cells had a depressed

carrying capacity.

MDA-MB-231 carrying capacities appeared more sensitive to culture conditions than those of MCF-7. In

the presence of glutamine, their carrying capacity increased significantly with pH. Their carrying capacity

increased with glucose up to concentrations of 2g/L but becomes suppressed in high (4.5g/L)

concentrations of glucose. Experiment 2 showed this effect of glucose regardless of glutamine status. In

summary, the carrying capacities (DD effects) also do not predict which cell type outcompetes the other.

Figure 3: Growth estimates of mixed population tumor spheroids for experiment 1. **A.** Instantaneous

growth rate (per day) for each cell type in high and low pH at various glucose concentrations. **B.** Carrying

capacities (in Relative Fluorescent Units (RFU), measured as the average fluorescence in the last ten

experimental time points) for each cell type in high and low pH at various glucose concentrations. **C.**

Instantaneous growth rate (per day) of each cell type in different starting frequencies for all eight

culture conditions.

Figure 4: Growth estimates of mono-culture population tumor spheroids for experiment 2. **A.**

Instantaneous growth rate of MCF-7 (green) and MDA-MB-231 (red) cells in nutrient rich and nutrient

deficient conditions. **B.** Carrying capacity of MCF-7 and MDA-MB-231 cells in nutrient rich and nutrient

deficient conditions. **C.** Instantaneous growth rate (per day) of each cell type in different starting

frequencies for all eight culture conditions.

The Logistic Model Best Describes Individual Cell Growth

Frequency-dependent effects (here measured as competition coefficients) can only be quantified by

modelling the growth of multiple interacting types or species. In order to obtain an accurate estimate of

these, the mode of growth must first be determined. Although several growth models have been

proposed for spheroids, tumors, and organoids, no specific consensus has been reached (35, 36).

Because of this, we agnostically compared four population growth models: exponential, logistic,

Gompertz, and Monod-like.

The exponential growth model is commonly used in bacterial studies and assumes unlimited resources

(37). This was used as a null model which allowed us to confirm that our spheroid cultures experience

limits to growth. Logistic population growth is the simplest constrained growth model and assumes that

per capita population growth rate declines linearly with population size or density (38). Although it

gives a similar shape, Gompertz growth is exponentially constrained by increasing population. Several

authors and works have suggested that the Gompertz equation provides a better fit to the growth of

tumors *in vivo* (36, 39). The Monod-like equation imagines resource matching where per capita growth

rates are proportional to the amount of resources supplied per individual. It provides a good fit to the

population growth curves of bacteria and other single cell organisms grown in chemostats (40). Here,

we consider all four models when estimating the DI parameter of intrinsic growth rate (*r*). We used the

latter three models for estimating the DD parameter of carrying capacity (K).

Due to the increased number of time points, we used the experiment 2 mono-culture spheroids to fit

the four models of single cell-type population growth. Using ordinary least squares approach, all four

models were fit to the four replicate spheroids of MCF-7 or MDA-MB-231 cells under eight

environmental conditions (Supplementary Figure 1). Quality of fit for each model was evaluated using

adjusted R^2 and Root Mean Square Error (RMSE) (Table 1, Supplementary Table 5).

Model	Cell Line	Measure	4.5 g/L Glucose, 7.4 pH, +Glutamine	4.5 g/L Glucose, 7.4 pH, -Glutamine	4.5 g/L Glucose, 6.5 pH, +Glutamine	4.5 g/L Glucose, 6.5 pH, -Glutamine	0 g/L Glucose, 7.4 pH, +Glutamine	0 g/L Glucose, 7.4 pH, -Glutamine	0 g/L Glucose, 6.5 pH, +Glutamine	0 g/L Glucose, 6.5 pH, -Glutamine
Exponential	MCF-7	Adjusted R^2	0.86375925	0.986878377	0.981146959	0.948234222	0.878382763	0.988394753	0.680927938	0.862338251
		RMSE	4.350169084	1.132653242	1.69847635	3.695432283	3.27179314	1.075082735	2.671205198	8.252546774
	MDA-MB-231	Adjusted R^2	0.965940219	0.961195759	0.405939888	0.837579643	0.984098581	0.920137544	0.673358471	0.792081228
		RMSE	0.464566345	0.395146745	0.808032208	0.430099077	0.389104518	0.495043084	0.684053081	0.61219965
Logistic	MCF-7	Adjusted R^2	0.95109814	0.987162238	0.981296804	0.948907945	0.989835743	0.990746769	0.706812568	0.954187534
		RMSE	2.569889623	1.119624296	1.693018458	3.678532642	0.920541516	0.955498916	2.560276438	5.403291938
	MDA-MB-231	Adjusted R^2	0.96590504	0.984894861	0.912214515	0.956642704	0.984068806	0.961748527	0.975726308	0.917447748
		RMSE	0.464826241	0.244756935	0.311220709	0.221858188	0.389432857	0.341782758	0.186174247	0.385055441
Monod	MCF-7	Adjusted R^2	0.931940694	0.970120375	0.927134074	0.865196707	0.96774423	0.944005043	0.715360107	0.784133576
		RMSE	3.027431032	1.708127542	3.338320975	5.959270988	1.669117432	2.349660049	2.522459912	11.38349256
	MDA-MB-231	Adjusted R^2	0.942552982	0.987666692	0.874817759	0.962825606	0.939280229	0.972592786	0.965887218	0.921638951
		RMSE	0.603401178	0.221046584	0.370619137	0.205360395	0.759417203	0.288935986	0.220623679	0.375119346
Gompertz	MCF-7	Adjusted R^2	0.943527504	0.987314557	0.981080261	0.948061608	0.985336984	0.990179344	0.711173682	0.945493131
		RMSE	2.760461987	1.112887278	1.702046991	3.705015484	1.111112845	0.983955476	2.540994298	5.737193572
	MDA-MB-231	Adjusted R^2	0.965812133	0.986346591	0.896293181	0.960341196	0.983941859	0.967290012	0.972497979	0.920364898
		RMSE	0.465418306	0.232605999	0.337719056	0.212122131	0.39072316	0.315765537	0.198161845	0.378158388

Table 1: Average adjusted R2 and RMSE for OLS fitting of four growth models to monoculture spheroids

in experiment 2. Although similar to the Gompertz fits, the Logistic Growth model provided the lowest

RMSE for most culture conditions.

Two-way ANOVAs (one for each cell type with pH and nutrient levels as independent variables) showed

that adjusted R^2's were similar for the three density-dependent models and significantly lower for the

exponential model (Supplementary Table 6). Conversely, the RMSE indicated the best fit for exponential

growth (lowest value), lowest quality fit for the Monod-like equation, and similar, intermediate values

for the logistic and Gompertz growth models. To definitively reject the (null) exponential model, we

evaluated whether the spheroids reached carrying capacity. To do this, we examined the slope of the

final ten time points for both the red and green fluorescent values (RFU's) for all experiment 2 spheroids

(supplementary table 7). As both MCF-7 and MDA-MB-231 mono-culture spheroids showed near, or

approaching, zero slopes, we rejected the exponential growth model. This was further confirmed by

two-way ANOVA (Supplementary table 8). Lastly, the Gompertz, Logistic, and Monod-like models were

directly compared and found to have significantly different RMSEs (supplementary table 9). Of these,

the Logistic model had the lowest RMSE, thus, it provided the best fit for our data.

MDA-MB-231 cells have a competitive advantage over MCF-7 cells in all culture conditions

The Lotka-Volterra competition equations represent a two species extension of logistic growth with the

addition of competition coefficients.

270
$$\frac{dN_1}{dt} = N_1 r_1 \left(1 - \frac{N_1 + \alpha N_2}{K_1}\right)$$

271
$$\frac{dN_2}{dt} = N_2 r_2 \left(1 - \frac{N_2 + \beta N_1}{K_2}\right)$$

where N_i are population sizes, r_i are intrinsic growth rates and K_i are carrying capacities. We let species

1 and 2 be MCF-7 and MDA-MB-231, respectively. The competition coefficients (α and β) scale the

effects of inter-cell-type competition where α is the effect of MDA-MB-231 on the growth rate of MCF-7

in units of MCF-7, and vice-versa for β. If α (or β) is close to zero, then there is no inter-cell-type

suppression; if α (or β) is close to 1 then intra-cell-type competition and inter-cell-type competition are

comparable; and if α (or β) is >1 then inter-cell-type competition is severe.

To fit this model, we used the time series data from experiment 2. The population sizes of the four

replicate spheroids were averaged for each of the eight environmental conditions and starting initial

frequencies of both cell types. Using the ordinary least squares approach, we estimated the values for

instantaneous growth rates, carrying capacities, and competition coefficients α and β (Figure 5). Note

that this gives revised estimates for growth rates and carrying capacities in addition to measuring the

competition coefficients.

+ Glutamine

4.5g/L; 7.4 pH

4.5g/L; 6.5 pH

0g/L; 7.4 pH

0g/L; 6.5 pH

- Glutamine

4.5g/L; 7.4 pH

4.5g/L; 6.5 pH

0g/L; 7.4 pH

0g/L; 6.5 pH

B.

	r_{MCF-7}	$r_{MDA-MB-231}$	K_{MCF-7}	$K_{MDA-MB-231}$	α	β
4.5 g/L Glucose, 7.4 pH, +Glutamine	0.0090083	0.002268243	40.6299239	2479.74226	5.86772365	-190.80898
4.5 g/L Glucose, 7.4 pH, -Glutamine	0.00258612	0.004617902	279.59422	11.5181197	11.9405862	-0.0856875
4.5 g/L Glucose, 6.5 pH, +Glutamine	0.00320443	0.020023245	530.294241	6.29360676	22.2919327	0.10873682
4.5 g/L Glucose, 6.5 pH, -Glutamine	0.00398154	0.008349796	369.570409	6.46236009	43.4810517	0.00420556
0 g/L Glucose, 7.4 pH, +Glutamine	0.01133825	0.002719719	28.3109023	3518.42156	3.41385677	-191.28472
0 g/L Glucose, 7.4 pH, -Glutamine	0.00445318	0.005462004	111.400069	9.63022009	-3.83294222	0.02022454
0 g/L Glucose, 6.5 pH, +Glutamine	0.00529779	0.013626163	28.8414935	6.90636312	0.27455018	0.22164312
0 g/L Glucose, 6.5 pH, -Glutamine	0.02704913	0.009966181	57.0210363	6.9320509	12.2343677	0.00487371

Figure 5: A. Estimation of competition coefficients using OLS fit of Lotka-Volterra competition growth

curves. Fluorescence data (RFU) from experiment 2 replicates were averaged and OLS algorithm used to

obtain curves. **B.** Estimates of growth rate and carrying capacity reflect previous estimates while

estimates of competition coefficients revealed the large competitive effect of MDA-MB-231 on MCF-7

cells.

As before, MCF-7 had higher intrinsic growth rates and carrying capacities than MDA-MB-231 under all 8

culture conditions of high/low glucose, high/low pH and presence/absence of glutamine. For all culture

conditions, $\alpha > 1$ (as high as 12.6) and $\beta \approx 0$. This indicates that the MDA-MB-231 cells had large

competitive effects on MCF-7 growth, and that MCF-7 cells had virtually no inhibitory effects on the

growth of MDA-MB-231 cells. These α/β values indicate that the competitive advantage gained by the

MDA-MB-231 cells is due primarily to frequency dependent (FD) effects.

These effects can also be seen in the slope of the final ten time points of the mixed cultures. Upon the

addition of MDA-MB-231 cells, MCF-7 cells show a large decrease in their final slope, even becoming

negative, then approaching zero as the starting frequency of MDA-MB-231 cells increases. Conversely,

the final slopes of the MDA-MB-231 populations increased in the presence of MCF-7 cells but decreased

with the starting frequency of MDA-MB-231 cells, suggesting that these cells were still replacing MCF-7

cell at the end of our experiments.

The greatest effect of MDA-MB-231 on MCF-7 (highest α) occurred under conditions of 4.5g/L glucose,

6.5pH, and glutamine absent conditions. The greatest effect of MCF-7 cells on MDA-MB-231 (highest β)

occurred in the absence of glucose and glutamine at neutral pH. This fits our original predictions;

however, the effect of β is not strong enough to rescue MCF-7 cells from competitive exclusion. In

accordance with the hypothesis that glucose permits MDA-MB-231 cells to be highly competitive, the

lowest α's occurred under glucose-starved conditions. Further, both cell types appear to experience

decreased growth efficiency and competition in glucose/glutamine starved, and acidic conditions. This is

consistent with more general ecological studies showing that competition between species is generally

less under harsh physical conditions (41, 42).

As expected, MDA-MB-231 experienced the greatest competitive advantage under high glucose,

glutamine starved, and acidic conditions. Observations of growth curves at different starting frequencies

further confirmed that, although growth of MCF-7 was impacted by starting frequency, under no

conditions were they capable of gaining a competitive advantage. In conclusion, only frequency-

dependent interactions explain the competitive outcomes seen in the co-culture microspheres.

In Vivo Confirmation of Competition Outcome

To evaluate whether our results hold *in vivo*, MDA-MB-231 and MCF-7 cells were grown in the

mammary fat pads of 8-10 week old nu/nu female mice. Three tumor models were evaluated: only MCF-

7, only MDA-MB-231, and 1:1 mix of both cell types with three replicates for each. Tumor volume was

measured weekly. At five weeks, the tumors were harvested and evaluated for ER expression which

marks MCF-7 (ER positive) cells providing estimates of the ratio of MDA-MB-231 to MCF-7 cells (Figure

6)**.**

Figure 6: Results of *in vivo* mono- and co- culture tumors. **A.** Histology slides of MCF-7, MDA-MB-231,

and 1:1 co-cultured tumors. Slides were stained with H&E and ER immune stain. **B.** Average fold change

of tumor volume reflects relative growth. **C.** Tumor viability for all three tumor types. Notice a decrease

in viability and increase in necrosis in the MDA-MB-231 and mixed tumors. **D.** Measures of ER biomarker

staining for each tumor type. **E.** The presence of small clumps of ER staining in mixed tumors reflect the

clumping of MCF-7 cells in the progression of the mixed tumor spheroids. This indicates the eventual

elimination of MCF-7 due to competitive inhibition by MDA-MB-231.

Changes in tumor size over five weeks indicated that the presence of MDA-MB -231, whether alone or in

the presence of MCF-7, resulted in a higher tumor growth rate compared to the MCF-7 only tumors. This

suggests that the growth dynamics of the MDA-MB-231 cells gain some advantage *in vivo*. Beyond 24

days, it appeared that the mixed tumors grew more rapidly than the MDA-MB-231 monoculture tumors.

This suggests that the presence of the competing MCF-7 cell type resulted in less inhibition of the MDA-

MB-231 cells *in vivo*. Like the spheroids, MDA-MB-231 cells seem to have higher growth rates as the

frequency of MCF-7 cells increases.

H&E staining indicated that MCF-7 tumors had the greatest viability and lowest necrosis while MDA-MB-

231 tumors displayed decreased viability and increased necrosis. This illustrates the drastic effect that

these phenotypes have *in vivo*. The small differences in necrotic and viable tissue between the MDA-

MB-231 and mixed tumors are indicative of the expansive effect that MDA-MB-231 phenotype has on

tumor progression.

ER staining was used to identify the final frequency of MDA-MB-231 and MCF-7 cells. The amount of ER

staining in the mixed tumors was comparable to the amount found in the MDA-MB-231 tumor,

indicating loss of MCF-7 clones at the experiment's end point. This matches the results from the

spheroid experiments demonstrating that MDA-MB-231 cells have a competitive advantage *in vivo* as

well. Interestingly, in one of the mixed tumors (shown), we note the presence of clustered ER staining

concentrated in an area of interior viable cells. This might reflect the clustering seen in the loss of MCF-7

cells in our *in vitro* tumor spheroids.

DISCUSSION:

Here we examine competition for resources in cell lines that have been used to represent two

phenotypes ("Pioneers" and "Engineers") frequently observed coexisting within the same tumors (4).

The "Pioneer" phenotype characteristically exhibits a Warburg metabolic phenotype producing high

concentrations of acid in the local microenvironment which promotes invasion and reduces the efficacy

of host immune cells. Pioneers are not angiogenic and typically obtain their vascular supply by co-opting

host vessels. Thus, they are typically found at the tumor-host interface and exhibit high levels of motility

and invasion (43). In contrast, the engineer phenotype is angiogenic, relatively non-invasive with near

normal glucose metabolism, and generally localized away from the tumor-host interface (4, 5). While

these phenotypes are most commonly found in different regions of the tumor, the eco-evolutionary

dynamics that govern their co-existence is not clear. For example, what prevents pioneer cells from

invading the engineer population? Similarly, the angiogenic switch is often regarded as a critical step in

tumorigenesis but this does not permit the engineer cells to invade the pioneer populations.

To understand competition among cancer cell phenotypes within a tumor, we hypothesized that direct

competition experiments are critical for understanding factors that may promote or inhibit coexistence.

Similar to the classic experiments by Gause (12, 13), we conducted competition experiments between

two well-established breast cancer cell lines that exhibit classic phenotypic and in-vivo growth patterns

of the 1) "Pioneer" MDA-MB-231 cells, which are highly invasive, non-angiogenic, and glycolytic and the

2) "Engineer" MCF-7 cells which are angiogenic, non-invasive, estrogen dependent and have near

normal glucose metabolism (4, 5).

Our first experiments investigated monocultures in various conditions likely to be present in some

regions of an *in vivo* tumor. *In vivo*, MCF-7 tumors generally grow slower than MDA-MB-231 tumors

(Figure 6B). Because of this, we were surprised that, in our experimental spheroid model, the growth

rate (ri) and carrying capacity (Ki) for MCF-7 cells in monoculture were the same or greater than those of

MDA-MB-231 cells under all conditions.

We expected these advantages would allow the MCF7 cells to dominate the MDA-MB-231 cells in co-

culture. However, the results were entirely opposite to our expectation as the MDA-MB-231 cells

became the dominant "species" under all culture conditions and regardless of the initial sizes of the two

populations. Indicating the outcomes of interactions between the two populations are almost entirely

"frequency dependent". This is reflected in the highly asymmetric and strong competitive effect of

MDA-MB-231 cells on MCF-7 cells exhibited by the Lotka-Volterra equations.

While the growth rates and carrying capacities of both cell types in monocultures were affected by

culture conditions, growth dynamics in co-culture were largely dependent on the presence and

frequency of the second cell type. These results highlight the importance of such frequency-dependent

dynamics on the progression and outcome of intra-tumoral competition.

The magnitude of the competitive effect of one cell type on the other is highly dependent on culture

conditions. In spheroids, MDA-MB-231 cells displayed their greatest competitive effect in high glucose

and low pH culture conditions while MCF-7 cells, although overall less competitive, showed their

greatest competitive effect in low glucose and neutral pH culture conditions. This aligns with the

"pioneer" and "engineer" phenotypic patterns and suggests that tumor heterogeneity is driven not only

by clonal growth efficiency but also by the landscape of the tumor microenvironment. Because

alterations in glucose and pH can significantly affect the competitive ability of different cell phenotypes,

manipulation of the microenvironment via therapies could directly influence intra-tumoral evolution and

cell-type composition.

Our investigation suggests that the competition dynamics observed in tumor spheroids also occur *in*

vivo. This is evident not only in the outcome of competition between MCF-7 and MDA-MB-231 cells, but

also by the spatial patterns observed both *in vivo* and *in vitro*. The emergence of such spatial patterns in

vitro suggests that some aspects of intratumoral spatial distribution are the result of cellular phenotypic

properties. In co-culture spheroids, MCF-7 cells would form a ring of highly clumped cells away from the

spheroids edge. The MDA-MB-231 cells were less clumped and formed the spheroids edge by extending

their range outward beyond that of the MCF-7 cells. Similar results have previously identified and

characterized in vivo by Ibrahim-Hashim et. al. as an integral factor in the outcome of competition

models (5).

The competitive superiority of MDA-MB-231 over MCF-7 from our in vitro and in vivo experiments

suggests new hypotheses. Several eco-evolutionary mechanisms may be responsible. In the competition

experiments, the cancer cells experienced pulsed resource renewal every 3-4 days. Thus, over a four day

period the culture media likely went from nutrient rich to poor, while metabolite concentrations,

including acid, increased (44). In both natural and malignant ecosystems, oscillating resources and

metabolites favor traits of 1) "priority", 2) speed, and 3) efficiency (45-48).

Here, *priority* is defined by the ability to localize, move to, and invade areas of high resource availability.

The higher motility and invasiveness of the MDA-MB-231 allowed them to occupy the outer margins of

the spheroid where nutrient concentrations would be highest (5, 29, 32, 49). *Speed* is defined by the

rate at which an organism can forage. A high speed allows an organism to pre-empt other organisms via

interference with uptake by competitors (50). The high glycolytic capacity of the MDA-MB-231 permits

them to acquire glucose faster than their MCF-7 competitors on a per cell basis. Furthermore, MDA-MB-

231 do not adhere to each other as the MCF-7 cells did. This gives the MDA-MB-231 a higher surface

area for nutrient uptake and less cell-to-cell interference in nutrient uptake. Finally, the motility and

speed of nutrient uptake may both contribute to rapid but inefficient foraging. High speed and efficiency

benefit the cell both through acquisition of resources and by making them unavailable to its

competitors. However, high motility and speed of nutrient uptake often result in rapid but inefficient

foraging. The lower intrinsic growth rates and carrying capacities of MDA-MB-231 are consistent with

this. *Efficiency* is the capacity of an organism to cheaply and profitably exploit resources when they are

scarce. The MCF-7 may be slower, more efficient foragers thus depleting nutrients following the pulse

more slowly but in a manner that allowed for greater per cell survival and proliferation, thus explaining

their higher growth rates and carrying capacity when grown in mono-culture (51).

CONCLUSIONS

Mixed-culture competition experiments in spheroids can successfully track competitive outcomes between cell lines of interest. Such experiments in spheroids may be valuable for quantifying the costs of resistance. Experiments could consider competing a resistant cell line against its sensitive parental cell line under conditions of no therapy (sensitive would be expected to outcompete the resistant cell line) and under conditions of therapy (resistant should outcompete the sensitive cell line). As accomplished here, one could determine differences in growth rates, carrying capacities and competition coefficients. These metrics would be valuable for informing adaptive therapy trials that modulate therapy so as to maintain a population of sensitive cells as a means for competitively suppressing the resistant cells (52-54).

Mixed culture competition experiments demonstrate how both the densities and the frequencies of cell types influence the growth rates and population dynamics of cancer cells. Measurements of resource availability and carrying capacities determine limits to growth. The extent to which inter-specific competition coefficients differ significantly from 1, reveal the extent to which cancer cells engage in eco-evolutionary games where the success of a given cancer cell depends both on its phenotype but the phenotypes of the other cancer cells (55-58). Such understanding of how cancer cell types respond to each other and to therapy will be crucial to evolutionarily informed therapies that aim to anticipate and steer the cancer's eco-evolutionary dynamics (59).

METHODS:

Cell Culture and acid adaptation in vitro

MCF-7 and MDA-MB-231 cells were acquired from American Type Culture Collection (ATCC, Manassas,

VA, 2007–2010) and were maintained in DMEM-F12 (Life Technologies) supplemented with 10% FBS

(HyClone Laboratories). Cells were tested for mycoplasma contamination and authenticated using short

tandem repeat (STR) DNA typing according to ATCC guidelines. Growth media was supplemented to

contain adjusted glucose and glutamine concentrations, depending on desired environmental

conditions. Media was also supplemented with 25 mmol/L each of PIPES and HEPES to increase the

buffering capacity of the media and the pH adjusted to 7.4 or 6.5 for each spheroid growth condition.

Transfection (GFP/RFP plasmids)

To establish stable cell lines, the MCF-7 and MDA-MB-231 cells were infected with Plasmids expressing

RFP or GFP using Fugene 6 (Promega) at an early passage and were selected using 2 µg/ml puromycin

(Sigma).

3D spheroid co-culture

Perfecta3®96-Well Hanging Drop Plates or non-adhesive U shape bottom 96 well plates were used to

grow the primary spheres containing 10,000 or 20,000 total cells. For each experimental condition, the

ratio between MCF-7-GFP and MDA-mb-231-RFP was from 0 to 100 percent as follows: 0/100, 20/80,

40/60, 60/40, 80/20, 100/0. Each ratio had four replicates for each experiment. An incucyte microscope

kept at 37°C and 5% CO2 was used to image the spheroid growth over approximately 30 days. Images

and fluorescent intensity were analyzed in Incucyte built-in software and image J. Relative fluorescent

units (RFUs) were normalized by averaging red/green fluorescence when the corresponding cell type

was absent then subtracting this value from other fluorescent values of that cell type.

Experimental conditions:

Two experiments were conducted. The first consisted of spheroids with a starting density of 20,000 cells

under conditions of high (4.5g/L), medium (2g/L), intermediate (1g/L) and no glucose fully crossed with

physiological (7.4) and low (6.5) pH. Spheroids were allowed to grow for roughly 670 hours with

fluorescence measured every 24-72 hours. Relative fluorescent units (RFUs) were used to generate

estimates of growth rates and carrying capacities.

Observations from these spheroids prompted us to conduct a second set of experiments consisting of

spheroids with a lower starting density (10,000 cells) cultured under the extremes of nutrient

concentration (0 g/L and 4.5 g/L glucose) fully crossed with physiological and low pH. Resilience of

growth under no glucose prompted a repeat of the experiment (0 g/L and 4.5 g/L glucose fully crossed

with physiological and low pH) with medium lacking glutamine. To improve accuracy of model-fitting,

fluorescent values were collected every 6 or 12 hours. These spheroids were also compared using three-

way ANOVAs (Ph, nutrient level and starting frequency of cells as independent variables). Additionally,

mechanism of growth was determined by fitting growth models as described below.

Calculation of growth rate and carrying capacity:

Growth rates were calculated as the log change of the first 72 hours after plating. Growth rates were

calculated from mono-cultures only. Carrying capacities were calculated as the mean fluorescence of

the final ten time points for each experiment. Since their values were similar regardless of starting

frequency, and since they dominated the tumor spheroid in all experiments, we could estimate the

carrying capacities of MDA-MB-231 cells using all cultures with a starting frequency of $\geq$ 20% MDA-MB-

231. Due to competitive effects, MCF-7 carrying capacities were estimated using only the 100% MCF-7

spheroids.

Testing among growth models:

The Ordinary Least Squares (OLS) fitting algorithm was used to fit exponential, Monod-like, Lotka-

Volterra, and Gompertz growth models to all monoculture spheroids in experiment 2. Fits were

performed by allowing adjustment of all input parameters. This provided the best fits (highest adjusted

R^2, lowest RMSE). Estimates of growth rates and carrying capacities obtained this way were very close to

our original estimates, providing further validity.

Competition Coefficient Estimation:

For each culture condition in experiment 2, fluorescent values were averaged across the four

experimental replicates. OLS fitting was used with no initial guess for growth rate or carrying capacity.

All plotting, optimization, and analysis was performed using MATLAB.

In Vivo Tumor Culture:

MCF7 and MDA-MB-231 breast cancer cell lines were purchased from ATCC. Both cells were

authenticated by short tandem repeat analysis and tested for mycoplasma. Xenograft studies were

performed by the guidelines of the IACUC of the H. Lee Moffitt Cancer Center using eight- to ten-week-

old female nu/nu mice (Envigo). Mice had free access to water and food for the whole duration of the

experiment. For MDA-MB-231 and MCF7 mono-tumor formation, 10 million cells were injected into

cleared mammary fat pads as described previously (4). For mixed cultures, a 1:1 mixture of 5 million

MDA-MB231 and 5 million MCF7 cells were injected. One week before cell injection, an estrogen pellet

(0.72 mg slow-release, Innovative Research of America) was implanted to allow for the growth of ER-

positive MCF7 tumors. Five weeks later, tumors were harvested.

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ACKNOWLEDGEMENTS:

We thank Jeffrey West for assistance with coding, we thank Chris Whelan and Dorothy Wallace for discussion and good ideas. Funding was provided by NIH/NCI 1U54CA193489-01A1, Cancer as a Complex Adaptive System, NIH/NCI U54 Supplement, The tumor-host evolutionary arms race, and R01 CA077575. This work was supported in part by the Analytic Microscopy Core Facility and the Tissue Core Facility at the H. Lee Moffitt Cancer Center & Research Institute; an NCI designated Comprehensive Cancer Center (P30-CA076292).

AUTHOR CONTRIBUTIONS:

All authors participated in the study ideas and the writing of the paper. M.D., A.I., A.R.F. and J.S.B designed the experiments. M.D., A.I. and A.R.F. collected the data. A.R.F., J.J.C. and J.S.B. performed the statistical analyses.

COMPETING INTERESTS:

The authors declare no competing financial interests.