

Burst-dependent synaptic plasticity can coordinate learning in hierarchical circuits

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Abstract

Synaptic plasticity is believed to be a key physiological mechanism for learning. It is well-established that it depends on pre and postsynaptic activity. However, models that rely solely on pre and postsynaptic activity for synaptic changes have, to date, not been able to account for learning complex tasks that demand credit assignment in hierarchical networks. Here, we show that if synaptic plasticity is regulated by high-frequency bursts of spikes, then neurons higher in a hierarchical circuit can coordinate the plasticity of lower-level connections. Using simulations and mathematical analyses, we demonstrate that, when paired with short-term synaptic dynamics, regenerative activity in the apical dendrites, and synaptic plasticity in feedback pathways, a burst-dependent learning rule can solve challenging tasks that require deep network architectures. Our results demonstrate that well-known properties of dendrites, synapses, and synaptic plasticity are sufficient to enable sophisticated learning in hierarchical circuits.

Introduction

The current canonical model of synaptic plasticity in the cortex is based on the co-occurrence of activity on the two sides of the synapse, pre and postsynaptic [1,2]. The occurrence of either long-term depression (LTD) or long-term potentiation (LTP) is controlled by specific features of pre and postsynaptic activity [3–12] and a more global state of neuromodulation [2,13–21]. However, local learning rules by themselves do not provide a guarantee that behavioral metrics will improve. With neuromodulation driven by an external reward/punishment mechanism, this guarantee is achievable [22]. But, such learning is very slow in tasks that require large or deep networks because a global signal provides very limited information to neurons deep in the hierarchy [23–25]. Thus, an outstanding question is (Fig. 1): how can neurons high-up in a hierarchy signal to other neurons — sometimes multiple

synapses lower — whether to engage in LTP or LTD in order to improve behavior [2]? This question is sometimes referred to as the “credit assignment problem”: essentially, how can we assign credit for any errors or successes to neurons that are multiple synapses away from the output [26]?

In machine learning, the credit assignment problem is typically solved with the backpropagation-of-error algorithm (backprop [27]), which explicitly uses gradient information in a biologically implausible manner [25] to calculate synaptic weight updates. Many previous studies have attempted to capture the credit assignment properties of backprop with more biologically plausible implementations in the hope that a biological model could match backprop’s learning performance [25, 28–44]. However, a problem with most of these models is that there is always an implicit assumption that during some phases of learning no sensory stimuli are processed, i.e. the models are not “online” in their learning, which is problematic for both biological plausibility and for potential future development of low-energy neuromorphic computing devices. Moreover, there are several well-established properties of real neurons, including nonlinearities in the apical dendrites [45], short-term synaptic plasticity (STP) [46, 47], and inhibitory microcircuits that are ignored. None of the previous studies successfully incorporated all of these features to perform online credit assignment (Table S1). Furthermore, none of these models captured the frequency dependence of synaptic plasticity, which is a very well-established property of LTP/LTD [6, 8, 9, 48, 49].

As established in non-hierarchical systems, such as the electrosensory lateral line lobe of the electric fish [50–52] or the cerebellum [53], feedback connections on dendrites are well-poised to orchestrate learning [54]. But for credit assignment in hierarchical networks, these connections should obey four constraints: 1) Feedback must *steer* the sign and magnitude of plasticity. 2) Feedback signals from higher-order areas should be *multiplexed* with feedforward signals from lower-order areas so that credit information can percolate down the hierarchy with minimal disruption to sensory information. 3) There should be some degree of *alignment* between feedback connections and feedforward connections. 4) Integration of credit-carrying feedback signals should be close to *linear* and avoid saturation (i.e., feedback signals should be linear with respect to any credit information). Experimental and theoretical work have addressed steering [12, 55], multiplexing [56–59], alignment [34, 41, 60, 61] or linearity [62] in isolation. , often by learning in an offline fashion [34–37, 40, 41, 63, 64], without learning rules based on spikes [28, 30, 35–37, 65] or without learning to solve tasks that necessitate hierarchical processing. But, it remains unclear whether a single set of cellular and subcellular mechanisms can address all four requirements for orchestrating learning in cortical hierarchies efficiently.

Here, we address the credit assignment problem with a spike-based learning rule that models how high-frequency bursts determine the sign of synaptic plasticity [6, 8, 9, 48, 49]. Guided by the underlying philosophy first espoused by the work of Körding and König (2001) [28] that the unique properties of pyramidal neurons may contain a solution to biologically plausible credit assignment, we show that combining properties of apical dendrites [45] with our burst-dependent learning rule allows feedback to steer plasticity. We further show that feedback information can be multiplexed across multiple levels of a hierarchy when feedforward and feedback connections have distinct STP [66, 67]. Using spiking simulations, we demonstrate that these mechanisms can be used to coordinate learning across a hierarchical circuit in a fully online manner. We also show that a coarse-grained equivalent of these dynamical properties will, on average, lead to learning that approximates loss-function gradients as used in backprop. We further show that this biological approximation to loss-function gradients is improved by a burst-dependent learning rule performing the alignment of feedback weights with feedforward weights, as well as recurrent inhibitory connections that linearize credit signals. Finally, we show that networks trained with these mechanisms can learn to classify complex image patterns with high accuracy. Altogether, our work highlights that well-known properties of dendritic excitability, synaptic transmission, short-term synaptic plasticity, inhibitory microcircuits, and burst-dependent synaptic plasticity are sufficient to solve the credit assignment problem in hierarchical networks.

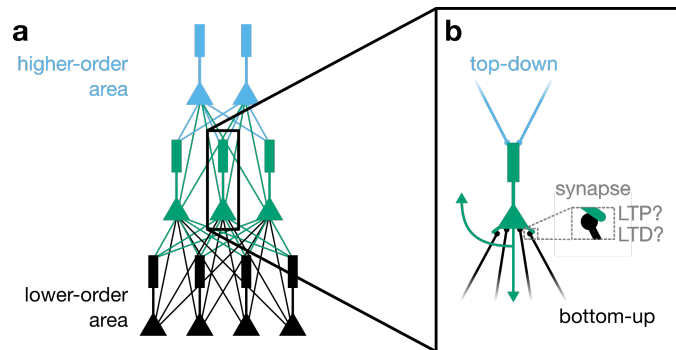


Figure 1. The credit assignment problem for hierarchical networks. (a) Illustration of a hierarchical neural network with feedforward and feedback connections. (b) For an orchestration of learning in this network, the representations in higher-level neurons should steer the plasticity of connections at a lower level.

Results

A burst-dependent rule enables top-down steering of plasticity

Experimental work has demonstrated that the sign of plasticity can be determined by patterns of pre and postsynaptic activity. The most common formulation of this is spike-timing-dependent plasticity (STDP), wherein the timing of pre and postsynaptic spikes is what determines whether LTP or LTD occurs [4, 68, 69]. However, there is also evidence suggesting that in many circuits, particularly mature ones [70], the principal determinant of plasticity is the level of postsynaptic depolarization, with large depolarization leading to LTP and small depolarization leading to LTD [3, 5–7, 11], which is a direct consequence of the dynamics of N-methyl-D-aspartate receptor (NMDAR)-dependent calcium influx [71]. Importantly, one of the easiest ways to induce large magnitude depolarization in dendrites is via backpropagation of high-frequency bursts of action potentials [72] and, therefore, the degree of postsynaptic bursting controls plasticity [6–9, 49]. Since bursting may be modulated by feedback synapses on apical dendrites [45, 73], feedback could control plasticity in the basal dendrites via control of bursting. Thus, in considering potential mechanisms for credit assignment during top-down supervised learning, the burst-dependence of synaptic plasticity appears to be a natural starting point.

To explore how high-frequency bursting could control learning in biological neural networks, we formulated a burst-dependent plasticity rule as an abstraction of the experimental data. We consider a burst to be any occurrence of at least two spikes with a short (i.e. under 16 ms) interspike interval. Following Ref. [59], we further define an event as either an isolated single spike or a burst. Thus, for a given neuron’s output, there is an event train (similar to a spike train, except that events can be either bursts or single spikes) and a burst train, which comprises a subset of the events (see Methods). We note that these definitions impose a ceiling on the frequency of events of 62.5 Hz, which is well above the typical firing frequency of cortical pyramidal neurons [73, 74]. The learning rule states that the change over time of a synaptic weight between postsynaptic neuron i and presynaptic neuron j , dw_{ij}/dt , results from a combination of an eligibility trace of presynaptic activity, \tilde{E}_j , and the potentiating (or depressing) effect of the burst train B_i (or event train E_i) of the postsynaptic cell (Fig. 2a):

$$\frac{dw_{ij}}{dt} = \eta[B_i(t) - \bar{P}_i(t)E_i(t)]\tilde{E}_j(t). \quad (1)$$

The variable \bar{P}_i controls the relative strength of burst-triggered potentiation and event-triggered depression. To ensure a finite growth of synaptic weights, we set this to a moving average of the proportion of events that are bursts in postsynaptic neuron i , with a slow ($\sim 1 - 10$ s) time scale (see Methods). The constant η is the learning rate. The variable $\bar{P}_i \in [0, 1]$ is an exponential moving average of the proportion of events that are bursts in postsynaptic neuron i , with a slow ($\sim 1 - 10$ s) time constant (see

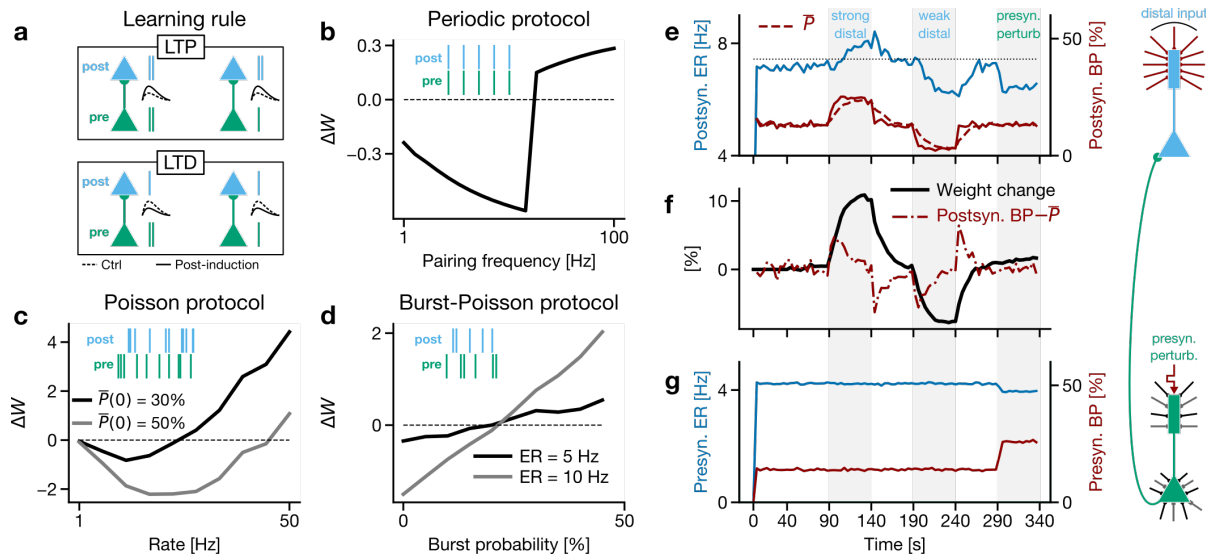


Figure 2. Burst-dependent plasticity rule. (a) Schematics of the learning rule. When there is a presynaptic eligibility trace, the occurrence of a postsynaptic burst leads to potentiation (top) whereas an isolated postsynaptic spike leads to depression of the synapse (bottom). (b-d) Net weight change for different pairing protocols. (b) The periodic protocol consisted of 15 sequences of 5 pairings, separated by a 10 s interval. We used pairings with $t_{\text{post}} = t_{\text{pre}}$. (c) For the Poisson protocol, the pre and postsynaptic activities were Poisson spike trains with equal rates. The protocol was repeated with different initial time-average burst probabilities (\bar{P}). (d) For the burst-Poisson protocol, pre and postsynaptic Poisson events were generated at a fixed rate (ER). For each event, a burst was produced with a probability that varied from 0 to 50%. (e-g) Impact of distal inputs on burst probability and feedforward synaptic weights for constant presynaptic event rate. Positive distal input (90–140 s) increases burst probability (e) and strengthens feedforward synapses (f). Negative distal input (190–240 s) decreases burst probability and weakens synapses. A dendritic input to the presynaptic neuron (290–340 s) increases its burst probability and mildly affects its event rate (g), but does not significantly change the weights (f). (e) Event rate (ER; blue), burst probability (BP; solid red curve) and estimated BP (dashed red curve) for the postsynaptic population. The black dotted line indicates the prestimulation ER and serves as a reference for the variations of the ER with plasticity. (f) Weight change relative to the initial average value of the weights. (g) Same as panel e, but for the presynaptic population. For the schematic on the right-hand side, black and grey axonal terminals onto the presynaptic (green) population represent Poisson input noise; such noise is absent for the postsynaptic (light blue) population for this simulation.

110 Methods). When a postsynaptic event that is not a burst occurs, the weight decreases proportionally to
 111 $\bar{P}_i(t)\tilde{E}_j(t) < 0$. In contrast, if a postsynaptic event is a burst then the weight increases proportionally
 112 to $[1 - \bar{P}_i(t)]\tilde{E}_j(t) > 0$. Hence, this moving average regulates the relative strength of burst-triggered
 113 potentiation and event-triggered depression and can also be implemented by changes in the thresholds
 114 for controlling how NMDA-dependent calcium influx translates into either LTD or LTP [71]. It has been
 115 well established that such mechanisms exist in real neurons [75, 76].

116 The plasticity rule stipulates that when a presynaptic input is paired with a postsynaptic burst LTP is
 117 induced, and otherwise, LTD results (Fig. 2a) [8, 9, 48, 49, 70, 71]. Using this rule, we simulated a series of
 118 synaptic plasticity experiments from the experimental and computational literature. First, we examined
 119 a frequency-dependent STDP protocol [7]. We found that when the spike pairing frequency is low, LTD
 120 is produced, and when the pairing frequency is high, LTP is produced (Fig. 2b). This matches previous
 121 reports on frequency-dependent STDP and shows that a burst-dependent synaptic plasticity rule can
 122 explain this data. Then, we explored the behavior of our rule when the pre and postsynaptic neuron fire
 123 independently according to Poisson statistics [77] (Fig. 2c). Experimental results have established that
 124 in such a situation the postsynaptic firing rate should determine the sign of plasticity [7]. As in similar
 125 learning rules [77], we found that a burst-dependent plasticity rule produces exactly this behavior (Fig.

126 2c). Notably, contrary to the Bienenstock-Cooper Munro (BCM) model [78] where the switching point
127 between LTD and LTP depends on a nonlinear moving average of the forward-feeding activity, in the
128 present case, the adaptive threshold is a burst probability, which can be controlled independently of the
129 forward-feeding activity. These results demonstrate that a burst-dependent plasticity rule is capable of
130 uniting a series of known experimental and theoretical results.

131 The burst-dependent rule suggests that feedback-mediated steering of plasticity could be achieved if
132 there were a mechanism for top-down control of the likelihood of a postsynaptic burst. To illustrate this,
133 in Fig. 2d we simulated another protocol wherein events were generated with Poisson statistics, and each
134 event could become a burst with probability P (x axis in Fig. 2d). Manipulating this burst probability
135 against the initial burst probability estimate ($\bar{P}_i(0) = 20\%$) controlled the occurrence of LTP and LTD,
136 while changing the pre and postsynaptic event rates simply modified the rate of change of the weight
137 (but not the transition point between LTP and LTD). This shows that one way for neurons to control the
138 sign of plasticity to ensure effective learning may be to regulate the probability of high-frequency bursts.
139 Interestingly, evidence suggests that in cortical pyramidal neurons of sensory cortices the probability of
140 generating high-frequency bursts is controlled by inputs to the distal apical dendrites and their activation
141 of voltage-gated calcium channels (VGCCs) [45, 73, 79–81]. Anatomical and functional data has shown
142 that these inputs often come from higher-order cortical or thalamic regions [82, 83].

143 We wondered whether combining a burst-dependent plasticity rule with regenerative activity in apical
144 dendrites could permit top-down signals to act as a “teaching signal”, instructing the sign of plasticity in
145 a neuron. To explore this, we ran simulations of pyramidal neuron models with simplified VGCC kinetics
146 in the apical dendrites (see Methods). We found that by manipulating the distal inputs to the apical
147 dendrites we could control the number of events and bursts in the neurons independently (Figs. 2e, g).
148 Importantly, the inputs to the apical dendrites in the postsynaptic neurons were what regulated the
149 number of bursts, and this also controlled changes in the synaptic weights, through the burst-dependent
150 learning rule. When the relative proportion of bursts increased, the synaptic weights potentiated on
151 average, and when the relative proportion of bursts decreased, the synaptic weights depressed (Fig.
152 2f). Thus, in Fig. 2f, the weight increases (decreases) on average when $P - \bar{P}$ is positive (negative).
153 Modifying the proportion of bursts in the presynaptic neurons had little effect on the weights (see the
154 rightmost gray shaded area in Fig. 2e-g). The sign of plasticity was independent of the number of events,
155 though the magnitude was not. Therefore, while the number of events contributed to the determination
156 of the magnitude of changes, the top-down inputs to the apical dendrites controlled the sign of plasticity.
157 In this way, the top-down inputs acted as a “teaching signal” that determined whether LTP or LTD
158 would occur. These results show that a burst-dependent learning rule paired with the control of bursting
159 provided by apical dendrites enables a form of top-down steering of synaptic plasticity in an online, local,
160 and spike-based manner.

161 **Dendrite-dependent bursting combined with short-term plasticity supports** 162 **multiplexing of feedforward and feedback signals**

163 The question that naturally arises from our finding that top-down inputs can steer synaptic plasticity via
164 a burst-dependent rule is whether feedback can steer plasticity without affecting the communication of
165 bottom-up signals? Using numerical simulations, we previously have demonstrated that in an ensemble
166 of pyramidal neurons the inputs to the perisomatic and distal apical dendritic regions can be distinctly
167 encoded using the event rate computed across the ensemble of cells and the percentage of events
168 in the ensemble that are bursts (the “burst probability”), respectively [59]. When communicated by
169 synapses with either short-term facilitation (STF) or short-term depression (STD), this form of “ensemble
170 multiplexing” may allow top-down and bottom-up signals to be simultaneously transmitted through a
171 hierarchy of pyramidal neurons.

172 To explore this possibility, we conducted simulations of two reciprocally connected ensembles of
173 pyramidal neurons along with interneurons providing feedforward inhibition. One ensemble received
174 currents in the perisomatic region and projected to the perisomatic region of the other ensemble (Fig.
175 3a, green ensemble). The other ensemble (Fig. 3a, light blue) received currents in the distal apical

176 compartment and projected to the distal apical compartment of the first ensemble. As such, we considered
177 the first ensemble to be “lower” (receiving and communicating bottom-up signals), and the other to
178 be “higher” (receiving and communicating top-down signals) in the hierarchy. Furthermore, we made
179 one key assumption in these simulations. We assumed that the synapses in the perisomatic regions
180 were short-term depressing, whereas those in the distal apical dendrites were short-term facilitating.
181 Additionally, we assumed that the inhibitory interneurons targeting the perisomatic region possessed STD
182 synapses, and the inhibitory interneurons targeting the distal apical dendrites possessed STF synapses.
183 These properties are congruent with what is known about parvalbumin-positive and somatostatin-positive
184 interneurons [46, 47, 84], which target the perisomatic and apical dendritic regions, respectively.

185 In these simulations, we observed that currents injected into the lower ensemble’s perisomatic
186 compartments were reflected in the event rate of those neurons (Fig. 3c3), though with a slight phase
187 lead due to spike frequency adaptation. In contrast, the currents injected into the distal apical dendrites
188 of the higher ensemble were reflected in the burst probability of those neurons (Fig. 3b2). Importantly,
189 though, we also observed that these signals were simultaneously propagated up and down. Specifically,
190 the input to the lower ensemble’s perisomatic compartments was also encoded by the higher ensemble’s
191 event rate (Fig. 3b3), whereas the burst rate of the higher ensemble was encoded by the lower ensemble’s
192 burst probability (Fig. 3c2). In this way, the lower ensemble had access to a conjunction of the signal
193 transmitted to the higher ensemble’s distal apical dendrites, as well as the higher ensemble’s event rate
194 (see arrow highlighting amplitude modulation in Fig. 3c2). Thus, since the higher ensemble’s event rate
195 is modulated by the lower ensemble’s event rate, the burst rate ultimately contains information about
196 both the top-down and the bottom-up signals (Fig. 3d). Notably, this is important for credit assignment,
197 as credit signals ideally are scaled by the degree to which a neuron is involved in processing a stimulus
198 (this happens in backprop, for example).

199 These simulations demonstrate that if bottom-up connections to perisomatic regions and perisomatic
200 inhibition rely on STD synapses, while top-down connections to apical dendrites and distal dendritic
201 inhibition utilize STF synapses, then ensembles of pyramidal neurons are capable of simultaneously
202 processing both a top-down signal and a bottom-up signal using a combination of event rates, burst rates,
203 and burst probabilities. We conclude that with the appropriate organization of short-term synaptic
204 plasticity mechanisms, a top-down signal to apical dendrites can 1) control the sign of plasticity locally
205 (steering; Fig. 2a), 2) be communicated to lower ensembles without affecting the flow of bottom-up
206 information (multiplexing; Fig. 3), and 3) be combined with bottom-up signals appropriately for credit
207 assignment.

208 **Combining a burst-dependent plasticity rule with short-term plasticity and** 209 **apical dendrites can solve the credit assignment problem**

210 To test whether STP, dendrite-dependent bursting and a burst-dependent learning rule can act simul-
211 taneously in a hierarchy to support learning, we built a simulation of ensembles of pyramidal neurons
212 arranged in three layers, with two ensembles of cells at the input, one ensemble of cells at the output,
213 and two ensembles of cells in the middle (the “hidden” layer; Fig. 4a). The distal dendrites of the top
214 ensemble received “teaching” signals indicating desired or undesired outputs. No other teaching signal
215 was provided to the network. As such, the hidden layer ensembles were informed of the suitability of
216 their output only via the signals they received from the output ensemble’s bursts. Currents injected into
217 the somatic compartments of the input layer populations controlled their activity levels in accordance
218 with the learning task to be discussed below. Compared to Figs. 2-3, for this simulation we made a few
219 modifications to synaptic transmission and pyramidal neuron dynamics to streamline the burst-event
220 multiplexing and decoding (see Methods). The most important addition, however, was that we modified
221 the learning rule in Eq. 1 by multiplying the right-hand side by an additional global term, $M(t)$, that
222 gates plasticity. This term abstracts a number of possible sources of control of plasticity, like dendritic
223 inhibition [62, 73, 85], or disinhibition through vasoactive intestinal peptide (VIP)-positive cells [86], burst
224 sizes [71, 87] or transient neuromodulation [14, 88, 89]. Importantly, $M(t)$ in our model gates plasticity
225 without changing its sign, contrary to some models on the role of neuromodulation in plasticity [21]. Its

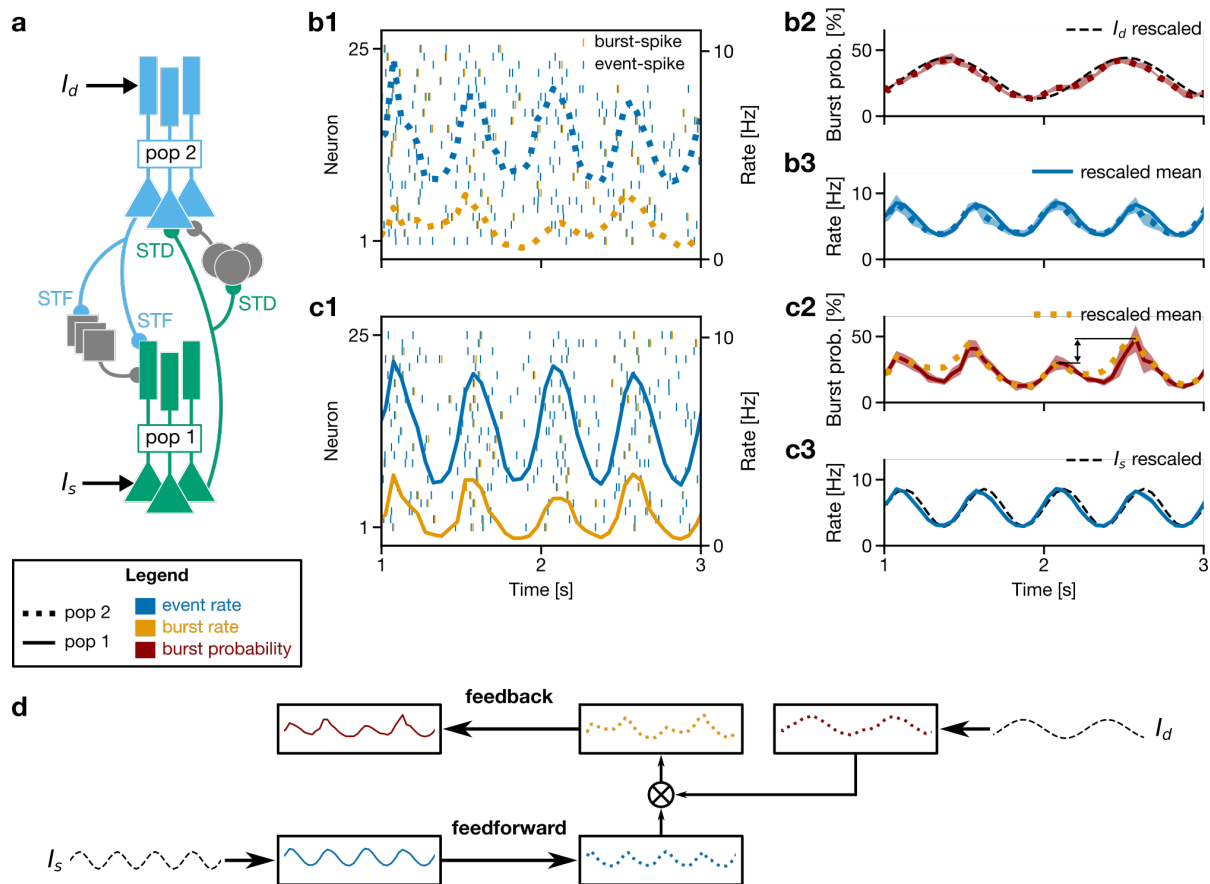


Figure 3. Dendrite-dependent bursting combined with short-term plasticity supports the simultaneous propagation of bottom-up and top-down signals. **(a)** Schematic of the network. Lower-level pyramidal neurons (green) received a somatic current I_s and projected with STD synapses to the somatic compartments of both a higher-level pyramidal neuron population (light blue) and to a population providing disynaptic inhibition (grey discs). The dendritic compartments of the light blue population received a current I_d . The light blue neurons innervated with STF synapses both the dendritic compartments of the green pyramidal neurons and a population providing disynaptic inhibition (grey squares). Results referring to the light blue and green population appear in panels **b1-b3** and **c1-c3**, respectively. **(b1, c1)** Raster plots of 25 out of the 4000 neurons per pyramidal population for the light blue (**b1**) and green (**c1**) populations. Blue ticks show the start of an event, being either a burst or an isolated spike. Orange ticks are the second spike in a burst; the remaining spikes in a burst are not shown. The corresponding population event rates (blue lines) and burst rates (orange lines) are superimposed. **(b2-b3)** Encoding performed by the light blue ensemble (pop 2). Its burst probability (**b2**, dotted red line) reflects the applied dendritic current I_d (dashed black line), whereas its event rate (**b3**, dotted blue line) reflects the event rate of the green population (solid blue line). **(c2-c3)** Encoding performed by the green ensemble (pop 1). Its burst probability (**c2**, solid red line) reflects the *burst rate* (dotted orange line) of the light blue ensemble, whereas its event rate (solid blue line) reflects the applied somatic current I_s (dashed black line). Arrow highlights amplitude modulation arising from the conjunction of top-down and bottom-up inputs. Results are displayed as mean \pm 2SD over five realizations of the Poisson noise applied to all neurons in the network. In each panel, the encoded input signal has been linearly rescaled so that its range matches that of the output. For clarity, the encoded signals in panels **b3** and **c2** are displayed using their averages only (i.e., without the standard deviations). For instance, in panel **c2** the BP of the green population encodes the BR of the light blue population. The bin size used in the population averages was 50 ms. **(d)** Schematic illustrating information propagation in the network.

226 role was to make sure that plasticity elicited by the abrupt onset and offset of each training example
227 does not overcome the plasticity elicited by the teaching signal, i.e. it was used to ensure a supervised
228 training regime. We accomplished this by setting $M = 0$ when no teaching signal was present at the
229 output layer and $M = 1$ under supervision. In this way, we ensured that the teaching signal was the
230 primary driver of plasticity.

231 We trained our 3-layer network on the exclusive or (XOR) task, wherein the network must respond
232 with a high output if only one input pool is active, and low output if neither or both input pools are
233 active (Fig. 4a-b). We chose XOR as a canonical example of a task that requires a nonlinear hierarchy
234 with appropriate credit assignment for successful learning. Before learning, the network was initialized
235 such that the output pool treated any input combination as roughly equivalent (Fig. 4c, dashed line).
236 To compute XOR, the output pool would have to learn to reduce its response to simultaneously active
237 inputs and increase its response to a single active input.

238 We set up the network configuration to address a twofold question: (1) Would an error signal applied
239 to the top-layer neurons' dendrites be propagated downward adequately? (2) Would the burst-dependent
240 learning rule combine top-down signals with bottom-up information to make the hidden-layer neurons
241 better feature detectors for solving XOR?

242 Importantly, if the answer to these two questions were 'yes', we would expect that the two hidden
243 ensembles would learn different features if they receive different feedback from the output. To test this,
244 we provided hidden pool 1 with positive feedback from the output, and hidden pool 2 with negative
245 feedback (Fig. 4a, light blue symbols). With this configuration, adequate error propagation to the two
246 hidden pools would make their responses diverge with learning, and the output pool would learn to take
247 advantage of this change. Indeed, our results showed that the XOR task was solved in this manner after
248 training (Fig. 4c, solid line).

249 To understand how this solution was aided by appropriate credit assignment, we examined the
250 information about the top-down teaching signals in each layer. According to the learning rule, plasticity
251 can be steered by controlling the instantaneous propensity to burst with respect to a moving average of
252 the burst probability (see term $B_i - \bar{P}_i E_i$ in Eq. 1 and Fig. 2e-f). In the output pool, the error signal
253 applied to the apical dendrites induced a temporary decrease in the burst probability when the input
254 pools were both active or both inactive, and a temporary increase when only one input pool was active
255 (Fig. 4d). These changes in the output burst probability modified the output burst rate, which was
256 propagated to the hidden pools. As mentioned above, the hidden pools received top-down signals with
257 different signs (Fig. 4e1-2, orange lines), and indeed their respective burst probabilities were altered
258 in opposite directions (Fig. 4e1-2, red lines). Due to these distinct top-down signals and the adaptive
259 threshold \bar{P}_i , the hidden pools' response diverged during learning (Fig. 4f1-2). For instance, hidden
260 pool 1 reduced its responses to both inputs being active, while hidden pool 2 increased its response.
261 These changes were due to the top-down control of the plasticity of synapses between the input and
262 hidden pools. We verified that solving this task depends on the plasticity of connections from input to
263 hidden units, but only weakly on the size of the ensembles (Fig. S1). Also, we verified that the task
264 was solved when the time constant τ_{avg} was shorter (Fig. S2), and when the feedback pathways had
265 the same sign of connection (Fig. S3). These results demonstrate that the propagation of errors using
266 burst-multiplexing and the burst-dependent learning rule can combine to achieve hierarchical credit
267 assignment in ensembles of pyramidal neurons.

268 **Burst-dependent plasticity promotes linearity and alignment of feedback**

269 Having demonstrated that a burst-dependent learning rule in pyramidal neurons enables online, local,
270 spike-based solutions to the credit assignment problem, we were interested in understanding the potential
271 relationship between this algorithm and the gradient-descent-based algorithms used for credit assignment
272 in machine learning. To do this, we wanted to derive the average behavior of the burst-dependent
273 learning rule at the coarse-grained, ensemble-level, and determine whether it provided an estimate of
274 a loss-function gradient. More precisely, in the spirit of mean-field theory and linear-nonlinear rate
275 models [90–92], we developed a model where each unit represents an ensemble of pyramidal neurons,

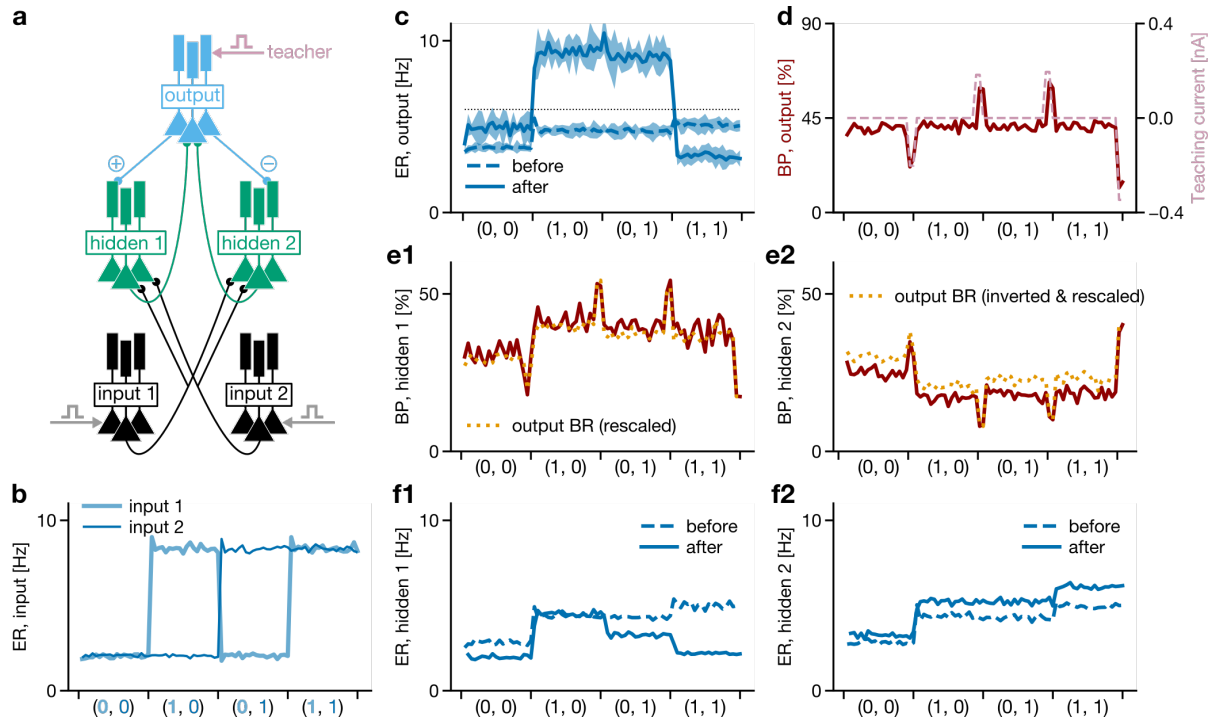


Figure 4. Burst-dependent plasticity can solve the credit assignment problem for the XOR task. (a) Each neuron population contained 2000 500 pyramidal neurons. Feedforward connections transmitted events, while feedback connections transmitted bursts. The teacher (pink arrow) was applied by injecting a hyperpolarizing current into the output ensemble’s dendrites if their event rate was high in the presence of inputs that are either both active or both inactive. A depolarizing current was injected into the output ensemble’s dendrites if their event rate was low when only one of the inputs was active. The activity of the input populations was controlled by somatic current injections (grey arrows). The \oplus and \ominus symbols represent the initialization of the feedback synaptic weights as mainly excitatory or inhibitory. (b) Input layer event rates (ERs) for the four input conditions presented sequentially in time. The duration of each example was 20 s 8 s. (c) Output ER before and after learning. The output ensemble acquired strong firing (event rate above the dotted line) at the input conditions associated with “true” in XOR. Results are displayed as mean \pm 2SD over 5 random initializations of the single-neuron connectivity. In other panels, a single realization is displayed for clarity. Mean \pm 2SD, in the same order as displayed: before: 3.3 ± 0.1 , 4.7 ± 0.1 , 4.7 ± 0.1 , 4.9 ± 0.1 ; after: 4.9 ± 0.1 , 7.1 ± 0.2 , 6.6 ± 0.2 , 5.0 ± 0.1 (in Hz). (d) During learning, the dendritic input (dashed pink) applied to the output ensemble’s neurons controlled their burst probability in the last two seconds of the input condition. (e1-e2) During learning, the burst rate (BR) at the output layer is encoded into the BP of the hidden layer to propagate the error. For the hidden-2 population, this inherited credit is inverted with respect to that in the hidden-1 population. (f1-f2) After (full line) vs. before (dashed line) learning for the hidden layer. The ER decreased in hidden-1 but increased in hidden-2. The bin size used in the population averages was 0.4 s.

with event rates, burst probabilities, and burst rates as described above (Fig. S4). In this step we lump together aspects of the microcircuitry, such as feedforward inhibition by parvalbumin-positive cells which helps to linearize the transfer function of event rates and preventing bursting in the absence of apical inputs [93,94]. Specifically, for an ensemble of pyramidal neurons, we defined $e(t)$ and $b(t)$ as ensemble averages of the event and burst trains, respectively. Correspondingly, $p(t) = b(t)/e(t)$ refers to the ensemble-level burst probability. We then defined the connection weight between an ensemble of presynaptic neurons and an ensemble of postsynaptic neurons, $W_{\text{post,pre}}$, as the effective impact of the presynaptic ensemble on the postsynaptic ensemble, taking into consideration potential polysynaptic interactions. Note that this means that the ensemble-level weight, $W_{\text{post,pre}}$, can be either positive or negative, as it reflects the cumulative impact of both excitatory and inhibitory synapses (see Supplemental Materials).

Our goal was then to derive the ensemble-level weight updates from the burst-dependent plasticity rule (Eq. 1). We assumed that any given pair of neurons were only weakly correlated on average, a reasonable assumption if the synaptic weights in the circuit are small [95]. Moreover, decorrelation between neurons is observed when animals are attending to a task [95], which suggests that this is a reasonable assumption for active processing states. We further assumed that the neuron-specific moving average burst probability (\bar{P}_i) is independent of the instantaneous occurrence of events. Using these assumptions, it can be shown (see Supplemental Materials) that the effective weight averaged across both pre and postsynaptic ensembles obeys:

$$\frac{dW_{\text{post,pre}}}{dt} = \eta M(t) [p_{\text{post}}(t) - \bar{p}_{\text{post}}(t)] e_{\text{post}}(t) e_{\text{pre}}(t) \quad (2)$$

where the learning rate η is different from that appearing in Eq. 1, and $\bar{p}_{\text{post}}(t)$ is a ratio of moving averages for the postsynaptic burst rate and event rate. This learning rule can be shown to implement an approximation of gradient descent for hierarchical circuits, like the backpropagation-of-error algorithm [96]. Specifically, if we assume that the burst probabilities remain in a linear regime (linearity), that the feedback synapses are symmetric to the feedforward synapses (alignment), and that error signals are received in the dendrites of the top-level ensembles, then $-[p_{\text{post}}(t) - \bar{p}_{\text{post}}(t)] e_{\text{post}}(t)$ is equivalent to the error signal sent backwards in backpropagation (see Supplemental Materials). For the sake of computational efficiency, when simulating this ensemble-level learning, we utilized simplifications to the temporal dynamics (i.e. we implemented a discrete-time version of the rule), though the fundamental computations being implemented were identical to the continuous-time equation above (see Methods and Supplemental Materials).

The assumptions of feedback linearity and alignment can be supported by the presence of additional learning mechanisms. First, we examined learning mechanisms to keep the burst probabilities in a linear regime. Multiple features of the microcircuit control linearity (Fig. S5), including distal apical inhibition [30,59], which is consistent with the action of somatostatin-positive Martinotti cells in cortical circuits [45,62]. We used recurrent excitatory and inhibitory inputs to control the apical compartments' potential (Fig. 5a). These dendrite-targeting inputs propagated bursts from neural ensembles at the same processing stage in the hierarchy, which provided them with the necessary information to keep the burst probabilities in a linear range of the burst probability function. We found that a simple homeostatic learning rule (see Methods) could learn to keep burst probabilities in a linear regime, thus improving gradient estimates (Fig. 5b).

Second, we explored potential mechanisms for learning weight symmetry. Symmetry between feedforward and feedback weights is an implicit assumption of many learning algorithms that approximate loss-function gradients. However, such an assumption is unnecessary, as it has been shown that it is possible to learn weight symmetry [61]. In one classic algorithm [97], weight symmetry is obtained if feedforward and feedback weights are updated with the same error signals, plus some weight decay [41]. In our model, this form of feedback weight update could be implemented locally because the error signal used to update the feedforward weights in discrete time is the deviation of the burst rates from the moving average baseline, and this, we propose, is also determining the updates to the feedback weights (see Methods). In brief, what this rule means in practice is that the apical dendrites would have a

317 different learning rule than the basal dendrites, something that has been observed experimentally [8,98].
318 As well, the specific learning rule used here assumes that the sign of plasticity at the feedback synapses
319 is based on presynaptic bursts, rather than postsynaptic bursts. Whether such a phenomenon exists
320 in real apical dendrites has, to our knowledge, not yet been examined. However, we note that there
321 are many different potential algorithms for training feedback weights, and we selected this one largely
322 because it has been shown to perform well in artificial neural networks [41,99]. Thus, we anticipate that
323 this feedback learning rule could be updated in the future based on experimental findings. Here, it is a
324 tool we used to determine whether the burst-dependent plasticity rule can learn challenging tasks if it is
325 paired with a feedback learning rule that promotes weight alignment. Indeed, when we implemented this
326 form of learning on the ensemble-level feedback weights we observed rapid weight alignment (Fig. 5c and
327 Fig. S6) and convergence to a loss-function gradient (Fig. 5d). Altogether, these results demonstrate
328 that the burst-dependent learning rule, averaged across ensembles of pyramidal neurons, and paired with
329 biologically plausible learning rules for recurrent inputs and feedback connections, can provide a good
330 estimate of loss-function gradients in hierarchical networks.

331 **Ensemble-level burst-dependent plasticity in deep networks can support good** 332 **performance on standard machine learning benchmarks**

333 We wanted to determine whether the ensemble-level learning rule could perform well on difficult tasks
334 from machine learning that previous biologically plausible learning algorithms have been unable to solve.
335 Specifically, we built a deep neural network comprised of pyramidal ensemble units that formed a series
336 of convolutional layers followed by fully-connected layers (Fig. 6a). We then trained these networks
337 on two challenging image categorization datasets that previous biologically plausible algorithms have
338 struggled with: CIFAR-10 and ImageNet [31].

339 The training in all components of the network used our burst-dependent plasticity rule and recurrent
340 inputs for linearization at fully-connected hidden layers. For the CIFAR-10 dataset, we observed a
341 classification test error rate of 20.1 % after 400 epochs (where an epoch is a pass through all training
342 images), similar to the error rate achieved with full gradient descent in a standard artificial neural
343 network (Fig. 6b). Training the feedback weights was critical for enabling this level of performance on
344 CIFAR-10, as fixed feedback weights led to much worse performance, even when the number of units was
345 increased in order to match the total number of trainable parameters (see Tables S3 and S4), in line with
346 previous results [31]. Furthermore, rich unit-specific feedback signals were critical. A network trained
347 using a global reward signal, plus activity correlations, while theoretically guaranteed to follow gradient
348 descent on average [22,23], was unable to achieve good performance on CIFAR-10 in a reasonable amount
349 of time (Fig. 6b, node perturbation). For the ImageNet dataset, we observed a classification error rate
350 of 56.1 % on the top 5 predicted image classes with our algorithm, which is much better than the error
351 rate achieved when keeping the feedback weights fixed, and much closer to that of full gradient descent
352 (Fig. 6c). The remaining gap between the ensemble-level burst-dependent learning rule and backprop
353 performance on ImageNet can likely be explained by the fact that we could not use recurrent input at
354 convolutional layers due to memory limitations, which led to degraded linearity of feedback at early
355 layers (Fig. S7). We also trained a network on the MNIST dataset, and achieved a similar performance
356 of 1.1% error on the test set with all three algorithms (Fig. S8). Therefore, these results demonstrate
357 that the ensemble-level burst-dependent learning rule, coupled with additional mechanisms to promote
358 multiplexing, linearity and alignment, can solve difficult tasks that other biologically plausible learning
359 algorithms have struggled with.

360 **Discussion**

361 In this paper, we asked the following question: could high-frequency bursts in pyramidal neurons provide
362 an instructive signal for synaptic plasticity that can coordinate learning across hierarchical circuits (Fig.
363 1)? We have shown that the well-known burst-dependence of plasticity rule combined with STP and

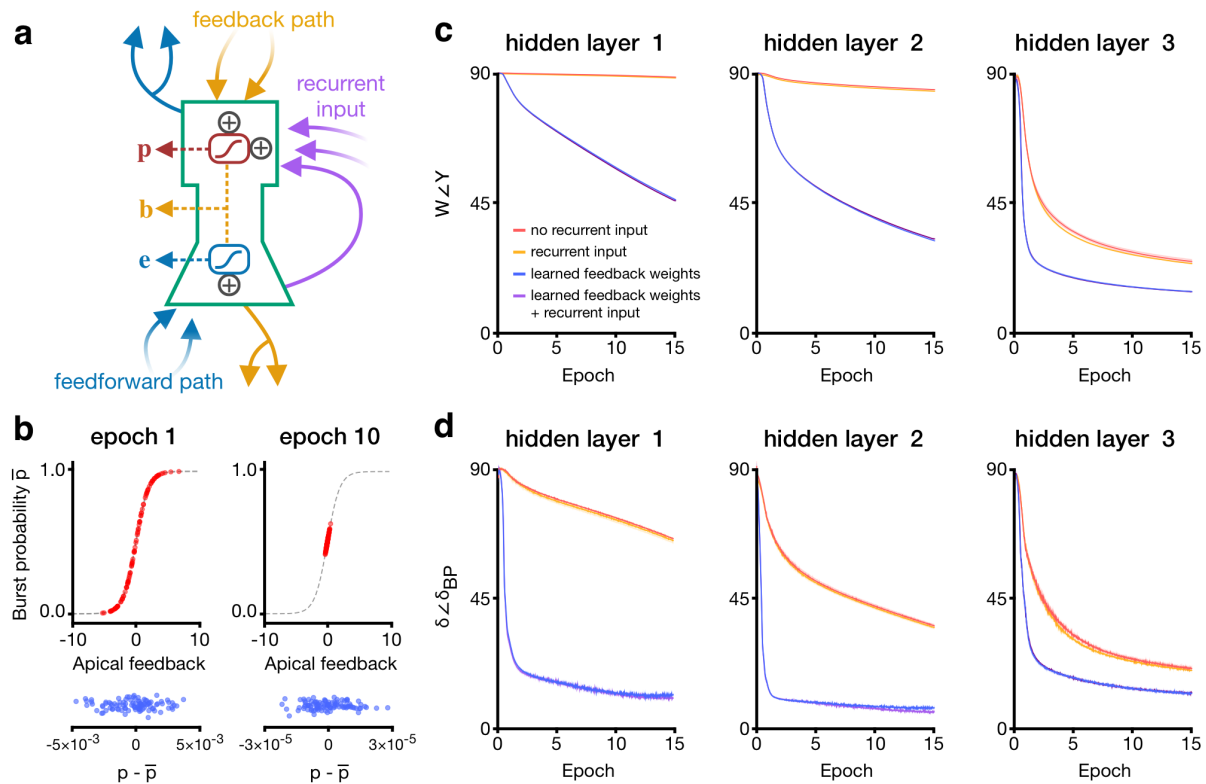


Figure 5. Burst-dependent plasticity of recurrent and feedback connections promotes gradient-based learning by linearizing and aligning feedback. **(a)** Diagram of a hidden-layer unit in the rate model. Each unit (green outline) in the network represents an ensemble of pyramidal neurons. Recurrent inputs (purple arrows) from all ensembles in a layer provide homeostatic control of the dendritic potential. **(b)** Throughout learning, recurrent weights were updated in order to push the burst probabilities towards the linear regime (top). This led to an overall decrease in the magnitudes of burst probabilities, while continuing to support positive and negative values necessary for credit assignment (bottom). **(c)** Alignment of feedback weights Y and feedforward weights W for three layers in a three-hidden-layer network trained on MNIST. Each hidden layer contained 500 units. Homeostatic recurrent inputs slightly reduce the angle between the two sets of weights, denoted $W \angle Y$, while learning on the feedback weights dramatically improves weight alignment. Each datapoint is the angle between feedforward and feedback weights at the start of a training epoch. **(d)** Angle between our weight updates (δ) and those prescribed by the backpropagation algorithm (δ_{BP}), for three layers in a three-hidden-layer network trained on MNIST. Recurrent inputs slightly improve the approximation to backpropagation, whereas learning on the feedback weights leads to a much closer correspondence. Each datapoint is the average angle between weight updates during a training epoch. In **c** and **d**, results are displayed as mean \pm SD over $n = 5$ trials.

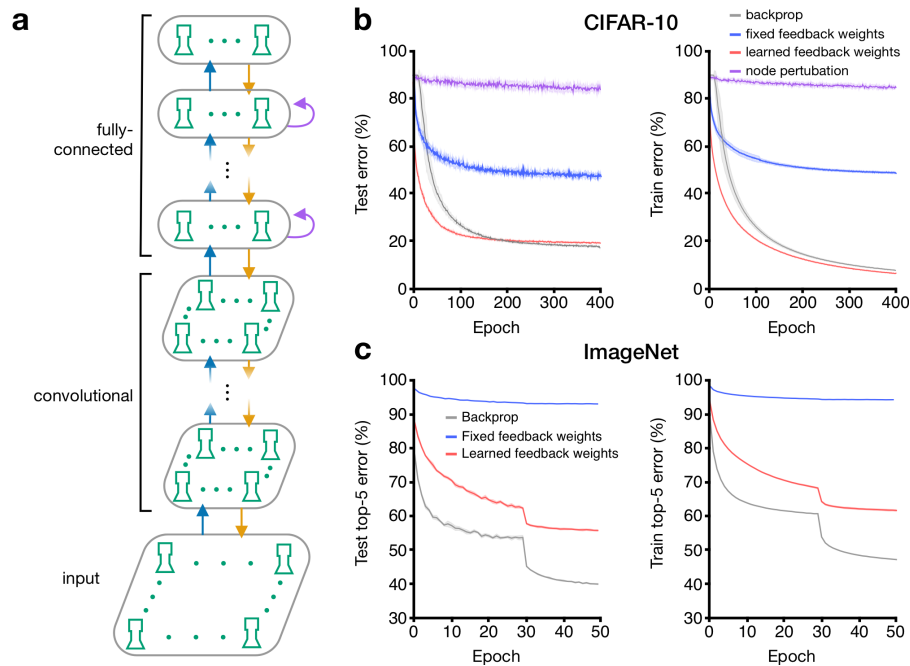


Figure 6. Ensemble-level burst-dependent plasticity supports learning in deep networks. (a) The deep networks consisted of an input layer, a series of convolutional layers, and a series of fully-connected layers. Layers were connected with sets of feedforward weights (blue arrows) and feedback weights (orange arrows). Fully-connected hidden layer contained recurrent connections (purple arrows). (b) Our learning rule, combined with learning of the feedback weights, was able to reach the performance of the backpropagation algorithm (backprop) on the CIFAR-10 classification task. (c) A network trained using our learning rule was able to learn to classify images in the ImageNet dataset when feedback weights were also updated. In b and c, results are displayed as mean \pm SD over $n = 5$ trials.

364 regenerative dendritic activity turns feedback connections into a teacher (Fig. 2), which by multiplexing
365 (Fig. 3) can coordinate plasticity across multiple synaptic jumps (Fig. 4). We then showed that, with
366 some additional burst-dependent learning at recurrent and feedback synapses, these mechanisms provide
367 an approximation of a loss-function gradient for supervised learning (Fig. 5) and perform well on
368 challenging image classification tasks (Fig. 6). Together, these results show that a local, spike-based and
369 experimentally supported learning rule that utilizes high-frequency bursts as an instructive signal can
370 enable sophisticated credit assignment in hierarchical circuits.

371 Decades of research into biologically plausible learning have struggled to find a confluence of biological
372 properties that permit efficient credit assignment. In this manuscript, we focused on the frequency-
373 dependence of LTP/LTD, STP, dendritic nonlinearities, and inhibitory microcircuits. We focused on
374 these aspects in part because the previous literature has established that these properties have important
375 links with synaptic plasticity [6, 73, 85, 100], but also because they are very well-established properties of
376 cortical circuits. Our burst-dependent learning rule itself could readily be implemented by previously
377 established synaptic plasticity signalling pathways [76]. Overall, our model can be seen as a concrete
378 implementation of a recent proposal from [25], which posited that differences in activity over time could
379 carry gradient signals. Here, we have shown that differences in the probability of high-frequency bursts
380 can carry gradient signals without affecting the time-dependent flow of sensory information. Therefore,
381 one of the primary lessons from our model is that when local synaptic plasticity rules are sensitive
382 to high-frequency bursts, then pyramidal neurons possess the necessary machinery for backprop-like
383 top-down control of synaptic plasticity.

384 It is important to note that there are a number of limitations to our model. First, our ensemble-level
385 models utilized many “ensemble units” that incorporated the activity of many pyramidal neurons, which
386 could potentially require networks of disproportionate size. However, the functional impact of using
387 many neurons in an ensemble is to provide a means for averaging the burst probabilities. Theoretically,
388 this averaging could be done over time, rather than over neurons. If so, there is no reason that the
389 algorithm could not work with single-neuron ensembles, though it would require a much longer time
390 to achieve good estimates of the gradients. To some extent, this is simply the typical issue faced by
391 any model of rate-based coding: if rates are used to communicate information then spatial or temporal
392 averaging is required for high-fidelity communication. Furthermore, we suspect that allowing population
393 coding could reduce the number of neurons required for a reliable representation [101].

394 Next, by focusing on learning, we ignored other ongoing cognitive processes. For instance, the
395 close link between attention and credit assignment implies that the same mechanisms may serve both
396 attention and learning purposes [65, 102]. Although some experimental data points to a role of bursting
397 in attention [103, 104], further work is required to establish if burst coding can give rise to attention-like
398 capabilities in neural networks.

399 The presence of the gating term, $M(t)$, may be seen as an additional limitation in the model, since
400 it is left in an abstract form and not directly motivated by biology. This term was introduced in
401 order to ensure that learning was driven by the teaching signal and not by changes in the stimuli.
402 Of course, if the goal is not supervised learning, but unsupervised learning, then this term may be
403 unnecessary. Indeed, one may view this as a prediction of sorts, i.e. that learning to match a target
404 should involve additional gating mechanisms that are not required for unsupervised learning. These
405 gating mechanisms could be implemented, e.g., by dendritic disinhibition [62, 73, 85, 86] (Fig. S5b)
406 or transient neuromodulation [14, 88, 89]. Our model did not include any sophisticated disinhibition
407 mechanisms or neuromodulatory systems. Yet, we know both disinhibition and neuromodulation can
408 regulate synaptic plasticity [14]. Future work could investigate how burst-dependent plasticity and
409 disinhibition/neuromodulation could interact to guide supervised learning.

410 Another set of limitations derive from how we moved from detailed cellular-level simulations to abstract
411 neural network models that were capable of solving complex tasks. For example, in moving to the abstract
412 models, we gradually made a number of simplifying assumptions, including clear separation between
413 bursts and single spikes, simplified STP, simplified bursting mechanisms, and ensemble-level units that
414 represented spiking activity across multiple neurons with a single value. We highlight these limitations
415 because it is important to keep them in mind when considering the potential for the cellular-level

416 plasticity rule to implement sophisticated credit assignment. Ideally, we would have the computational
417 resources to fully simulate many thousands of ensembles of pyramidal neurons and interneurons with
418 complex synaptic dynamics and bursting in order to see if the cellular-level burst-dependent rule could
419 also solve complicated tasks. However, these questions will have to be resolved by large-scale projects
420 that can simulate millions of biophysically realistic neurons with complicated internal dynamics [105, 106].

421 Similarly, we did not include recurrent connections between pyramidal neurons within a layer, despite
422 the fact that such connections are known to exist. We did this for the sake of simplicity, but again, we
423 consider recurrent connectivity to be fully compatible with our model and a subject of future investigations.
424 Moreover, our model makes some high-level assumptions about the structure of cortical circuitry. For
425 example, we assumed that top-down signals are received at apical dendrites while bottom-up signals
426 are received at basal dendrites. There is evidence for this structure [82], but also some data showing
427 that it is not always this way [107]. Likewise, we assumed that pyramidal neurons across the cortical
428 hierarchy project reciprocally with one another. There is some evidence that the same cells that project
429 backwards in the cortical hierarchy also project forwards [108], but the complete circuitry of cortex is far
430 from determined.

431 Our model makes a number of falsifiable experimental predictions that could be examined experimen-
432 tally. First, the model predicts that there should be a polarization of STP along the sensory hierarchy,
433 with bottom-up synaptic projections being largely STD and top-down synaptic projections being largely
434 STF. There are reports of such differences in thalamocortical projections [66, 67], which suggests that an
435 important missing component of our model is the inclusion of thalamic circuitry. There are also reports
436 of polarization of STP along the basal dendrosomatic axis [109], and our model would predict that this
437 polarization should extend to apical dendrites. Second, because our model proposes that burst firing
438 carries information about errors, there should be a relationship between burst firing and progress in
439 learning. Specifically, our model predicts that the *variance* in burst probabilities across a population
440 should be correlated with the errors made during learning (Fig. S9). Experimental evidence in other
441 systems supports this view [58, 73]. Finally, our model predicts that inhibition in the distal apical
442 dendrites serves, in part, to homeostatically regulate burst probabilities to promote learning. Thus, a
443 fairly simple prediction from the model is that manipulations of distal dendrite targeting interneurons,
444 such as somatostatin positive interneurons, should lead to unusual levels of bursting in cortical circuits
445 and disrupt learning. Some recent experimental evidence supports this prediction [73, 85].

446 Linking low-level and high-level computational models of learning is one of the major challenges in
447 computational neuroscience. Our focus on supervised learning of static inputs was motivated by recent
448 progress in this area. However, machine learning researchers have also been making rapid progress in
449 unsupervised learning on temporal sequences in recent years [110, 111]. We suspect that many of the
450 same mechanisms we explored here, e.g. burst-dependent plasticity, but also many of the mechanism not
451 explored here, e.g. NMDA-spikes inducing cooperativity [112, 113], or bursting induced by feedforward
452 activity escaping feedforward inhibition [93, 94], could be adapted for unsupervised learning of temporal
453 sequences in hierarchical circuits. It is likely that the brain combines unsupervised and supervised
454 learning mechanisms, and future research should be directed towards how neurons may combine different
455 rules for these purposes. Ultimately, by showing that a top-down orchestration of learning is a natural
456 result of a small set of experimentally observed physiological phenomena, our work opens the door to
457 future approaches that utilize the unique physiology of cortical microcircuits to implement powerful
458 learning algorithms on dynamic stimuli using time-varying signals.

459 Methods

460 Spiking model

461 Spiking simulations were performed using the Auryn simulator [114], except for the pairing protocols of
462 Fig. 2b-d, which used Python.

463 Event and burst detection

An *event* was said to occur either at the time of an isolated spike or at the time of the first spike in a burst. A *burst* was defined as any occurrence of at least two spikes with an interspike interval (ISI) less than the threshold $b_{\text{th}} = 16$ ms [59, 115]. Any additional spike with $\text{ISI} < b_{\text{th}}$ belonged to the same burst. A neuron i kept track of its time-averaged burst probability \bar{P}_i by using exponential moving averages of its event train E_i and burst train B_i :

$$\bar{E}_i(t) = \frac{1}{\tau_{\text{avg}}} \int_0^\infty E_i(t - \tau) e^{-\tau/\tau_{\text{avg}}} d\tau \quad (3)$$

$$\bar{B}_i(t) = \frac{1}{\tau_{\text{avg}}} \int_0^\infty B_i(t - \tau) e^{-\tau/\tau_{\text{avg}}} d\tau \quad (4)$$

$$\bar{P}_i(t) = \frac{\bar{B}_i(t)}{\bar{E}_i(t)}, \quad (5)$$

464 where τ_{avg} is a slow time constant (~ 1 -10 s). Also, $E_i(t) = \sum_{\text{event}} \delta(t - t_{i,\text{event}})$ and $B_i(t) = \sum_{\text{burst}} \delta(t -$
465 $t_{i,\text{burst}})$, where $t_{i,\text{event}}$ and $t_{i,\text{burst}}$ indicate the timing of an event and of the second spike in a burst,
466 respectively.

467 Plasticity rule

Weights were updated upon the detection of a postsynaptic event or burst according to

$$\frac{dw_{ij}}{dt} = \eta M \left\{ [(1 + H_i)B_i + (-\bar{P}_i + H_i)E_i] \tilde{E}_j + G_i E_j \right\} \quad (6)$$

468 where $\tilde{E}_j(t) = \int_0^\infty E_j(t - \tau) e^{-\tau/\tau_{\text{pre}}} d\tau$ is a presynaptic trace with time constant τ_{pre} . Here, τ_{pre} is typically
469 much smaller than τ_{avg} , with $\tau_{\text{pre}} \sim 10$ ms, but it could possibly be made larger to accommodate plasticity
470 rules with slower dynamics [100]. The prefactor M gates plasticity during training: in the XOR task
471 (Fig. 4), $M = 1$ when the teaching signal is present and 0 otherwise. In Fig. 2, $M = 1$ throughout.

Homeostatic terms help to restrict the activity of neurons to an appropriate range. The homeostatic functions H_i and G_i were defined as

$$H_i(t) = - \left(1 - \frac{e_{\text{max}}}{\bar{E}_i(t)} \right) \Theta(\bar{E}_i(t) - e_{\text{max}}) \quad (7)$$

$$G_i(t) = [e_{\text{min}} - \bar{E}_i(t)] \Theta(e_{\text{min}} - \bar{E}_i(t)), \quad (8)$$

472 where e_{min} (resp. e_{max}) is a minimum (resp. maximum) event rate, and $\Theta(\cdot)$ denotes the Heaviside step
473 function. When the neuron-specific running average of the event rate, $\bar{E}_i(t)$, lies within these limits,
474 $H_i = G_i = 0$, and we recover the learning rule of Eq. 1. In most simulations, network parameters were
475 chosen in such a way that the homeostatic plasticity had little to no effect. Typically, we used $e_{\text{min}} = 2$
476 Hz and $e_{\text{max}} = 10$ Hz.

477 Pairing protocols

478 For all pairing protocols of Fig. 2b-d, we had $\tau_{\text{pre}} = 50$ ms, $\tau_{\text{avg}} = 15$ s, $\eta = 0.1$, and we set the
479 homeostatic terms to zero.

- 480 • *Periodic protocol.* Five consecutive pairings were separated by a quiescent period of 10 s, 15 times.
 481 We used pairings with $\Delta t = 0$. For each pairing frequency the starting value for the estimated
 482 burst probability was $\bar{P}_i(t = 0) = 0.15$ and $\bar{E}_i(t = 0) = 5$ Hz.
- 483 • *Poisson protocol.* Both the pre and postsynaptic neurons fired spikes at a Poisson rate r with
 484 no refractory period a refractory period of 2 ms. For each r , the induction lasted 100 s and we
 485 averaged over 20 independent realizations. We used $\bar{E}_i(t = 0) = 5$ Hz.
- 486 • *Burst-Poisson protocol.* Both the pre and postsynaptic neurons produced events at a Poisson rate
 487 r , including a refractory period $\tau_{\text{ref}}^{(E)} > b_{\text{th}}$. For each event, a burst was generated with probability
 488 p and an intraburst ISI was sampled from $\text{Unif}(\tau_{\text{ref}}^{(B)}, \tau_{\text{ref}}^{(B)} + t_{\text{max}})$, with $\tau_{\text{ref}}^{(B)} + t_{\text{max}} < b_{\text{th}}$. For
 489 the simulations in Fig. 2d, we used $\tau_{\text{ref}}^{(E)} = 20$ ms, $\tau_{\text{ref}}^{(B)} = 2$ ms and $t_{\text{max}} = 10$ ms. We set
 490 $\bar{P}_i(t = 0) = 0.2$ and the event rate of the pre and postsynaptic neurons were set to $r = 5$ Hz and
 491 $r = 10$ Hz, with corresponding values for the initial postsynaptic event rate estimates. For each r ,
 492 the induction lasted 100 s and we averaged over 20 independent realizations.

493 Neuron models

- *Pyramidal neurons* The somatic compartment obeyed

$$\begin{aligned} C_s \dot{V}_s &= -(C_s/\tau_s)(V_s - E_L) + g_s f(V_d) + I_s - w_s \\ \tau_{w_s} \dot{w}_s &= -w_s + b\tau_{w_s} S(t) \end{aligned} \quad (9)$$

494 where V_s is the somatic membrane potential, w_s is an adaptation variable, I_s is the total current
 495 applied to the soma (includes noise and other synaptic inputs) and $S(t)$ is the spike train of
 496 the neuron. The function $f(V_d)$ in the equation for V_s takes into account the coupling with the
 497 dendritic compartment, with $f(V_d) = 1/\{1 + \exp[-(V_d - E_d)/D_d]\}$ and parameters $E_d = -38$ mV
 498 and $D_d = 6$ mV. A spike occurred whenever V_s crossed a moving threshold from below. The latter
 499 jumped up by 2 mV right after a spike and relaxed towards -50 mV with a time constant of 27 ms.
 500 Other somatic parameters were: $\tau_s = 16$ ms, $C_s = 370$ pF, $E_L = -70$ mV, $\tau_{w_s} = 100$ ms, $b = 200$
 501 pA, and $g_s = 1300$ pA. The reset voltage after a spike was $V_r = -70$ mV.

The dendritic compartment obeyed

$$\begin{aligned} C_d \dot{V}_d &= -(C_d/\tau_d)(V_d - E_L) + g_d f(V_d) + c_d(K * S)(t) + I_d - w_d \\ \tau_{w_d} \dot{w}_d &= -w_d + a_w(V_d - E_L). \end{aligned} \quad (10)$$

502 The function $f(V_d)$ is the same as above and is responsible for the regenerative dendritic activity.
 503 The term $c_d(K * S)(t)$ represents the backpropagating action potential, with the kernel K modeled
 504 as a box filter of amplitude one and duration 2 ms, delayed by 0.5 ms with respect to the somatic
 505 spike. Other dendritic parameters were: $\tau_d = 7$ ms, $C_d = 170$ pF, $E_L = -70$ mV, $\tau_{w_d} = 30$ ms,
 506 $a = 13$ nS, and $g_d = 1200$ pA.

507 This model and its parameters are described in more detail and compared with experimental data
 508 in Ref. [59].

- *Dendrite-targeting inhibition.* We modeled somatostatin-positive interneurons [116–118] using the
 adaptive exponential integrate-and-fire (AdEx) model [119]:

$$\begin{aligned} C \dot{V} &= -g_L(V - E_L) + g_L \Delta_T e^{\frac{V - V_T}{\Delta_T}} + I - w \\ \tau_w \dot{w} &= a(V - E_L) + b\tau_w S(t) - w \end{aligned}$$

509 where I is the total current applied to the neuron. A spike occurred whenever V crossed $V_{\text{cut}} = 24$
 510 mV and was followed by a refractory period τ_{ref} . Parameter values were $C = 100$ pF, $g_L = 5$ nS,
 511 $E_L = -70$ mV, $V_T = -62$ mV, $\Delta_T = 4$ mV, $\tau_w = 500$ ms, $a = 0.5$ nS, $b = 10$ pA, $V_r = -65$ mV
 512 and $\tau_{\text{ref}} = 2$ ms. In Fig. 3, these model neurons (grey squares in Fig. 3a) were receiving top-down
 513 excitation from higher-level pyramidal cells.

514 • *Perisomatic inhibition* We modeled parvalbumin-positive neurons [120] using the AdEx model
515 with parameters chosen to reproduce qualitatively their typical fast-spiking phenotype. Parameter
516 values were $C = 100$ pF, $g_L = 10$ nS, $E_L = -70$ mV, $V_T = -48$ mV, $\Delta_T = 2$ mV, $V_r = -55$ mV,
517 $\tau_{\text{ref}} = 1$ ms and $a = b = 0$. In Fig. 3, these model neurons (grey discs in Fig. 3a) were receiving
518 bottom-up excitation from the lower-level pyramidal cells.

519 Connectivity

520 In general, connections between distinct neural ensembles were sparse ($\sim 5 - 20\%$ connection probability).
521 Pyramidal neurons within an ensemble had no recurrent connections between their somatic compartments.
522 Within a pyramidal ensemble, burst-probability linearization was enacted by sparse STF inhibitory
523 synapses onto the dendritic compartments (Fig. S10). These STF connections were not illustrated in Fig.
524 3a for clarity. The net strength of inputs onto the apical dendrites was chosen to preserve a stationary
525 burst probability between 10 and 50 %, as in vivo experimental data reports burst probability between
526 15 and 25 % [74,104].

527 Synapses

528 All synapses were conductance-based. The excitatory (resp. inhibitory) reversal potential was 0 mV
529 (resp. -80 mV) and the exponential decay time constant was 5 ms (resp. 10 ms). There were no NMDA
530 components to excitatory synapses. For a given connection between two ensembles, existing synapses
531 had their strengths all initialized to the same value.

532 Noise

533 Each neuron (for single-compartment neurons) and each compartment (for two-compartment neurons)
534 received its own (private) noise in the form of a high-frequency excitatory Poisson input combined to an
535 inhibitory Poisson input. The only exception was the noise applied to the neural populations in Fig.
536 2e-g, where we used sparse connections from a pool of excitatory and inhibitory Poisson neurons. Noise
537 served to decorrelate neurons within a population and to imitate *in vivo* conditions.

538 Short-term plasticity

539 STP was modeled following the extended Markram-Tsodyks model [47]. Using the notation of Ref. [121],
540 the parameters for STF were $D = 100$ ms, $F = 100$ ms, $U = 0.02$ and $f = 0.1$. For STD, the parameters
541 were $D = 20$ ms, $F = 1$ s, $U = 0.9$ and $f = 0.1$. These sets of parameters were chosen following [59] to
542 help decode bursts (using STF) and events (using STD).

543 Spiking XOR gate

544 A XOR gate maps binary inputs (0, 0) and (1, 1) onto 0 and inputs (1, 0) and (0, 1) onto 1. In the context
545 of our spiking network, input 0 corresponded to a low event rate (~ 2 Hz) and input 1 to a higher event
546 rate (~ 10 Hz). These were obtained by applying a hyperpolarizing (resp. depolarizing) current for 0
547 (resp. 1) to the corresponding input-layer population. Importantly, compared to the spiking simulations
548 described above, our implementation of the spiking XOR gate used three simplifications to reduce the
549 dimension of the parameter search space. First, events and bursts were propagated directly instead of
550 relying on STP (see Fig. S11). Second, disynaptic inhibition was replaced by direct inhibition coming
551 from the pyramidal cells. Third, we used a simplified pyramidal neuron model. Below, we describe this
552 model, as well as the initialization of the network, the error generation and the learning protocol for the
553 XOR gate.

554 • *Simplified pyramidal neuron model.* The effect of dendritic regenerative activity on the somatic
555 compartment (controlled by g_s in Eqs. 9-10) was replaced by a conditional burst probability:
556 whenever a somatic event occurred, a burst was produced with probability $f(V_d)$. This function is

557 the same as that appearing in Eqs. 9-10, but with $E_d = -57$ mV. This model permitted a cleaner
558 burst-detection process and burst-ensemble multiplexing.

559 • *Initialization of the network.* The feedforward synaptic strengths were initialized so that the event
560 rates of all pyramidal ensembles in the network belonged to $[e_{\min}, e_{\max}]$ for all inputs. Excitatory
561 synaptic strengths from the input layer to the hidden layer were all equal, and likewise for the
562 inhibitory synapses. For the hidden-to-output feedforward connections, the ratio of the excitatory
563 synaptic strengths was 1.4:1.05 in favor of hidden 1. This ratio for inhibition was 5:0.3 in favor
564 of hidden 2. All existing feedforward excitatory synaptic strengths were equal together, and
565 likewise for the inhibitory synapses. The feedback synaptic strengths from the output population
566 to the hidden populations—the only existing ones—were initialized so that one coarse-grained
567 connection would be predominantly excitatory and the other inhibitory (the one onto hidden pool 2
568 in Fig. 4). As with the feedforward connections, the excitatory feedback synapses belonging to the
569 same coarse-grained connection shared the same strength, and likewise for inhibition. A constant
570 depolarizing current was applied to the hidden pool 2's dendritic compartments to compensate for
571 the stronger inhibition.

- *Error generation.* At the output layer, we specified a maximum and a minimum event rate, e_{\max}
and e_{\min} (the same as in the learning rule of Eq. 6). The following linearly transformed \bar{E}_i

$$\bar{E}'_i = \frac{\bar{E}_i - e_{\min}}{e_{\max} - e_{\min}}$$

was then used in conjunction with a cross entropy loss function to compute the error for each
neuron of the output population. As a result, a current, $I_i^{(d)}$ (where d indicates “dendritic”), was
injected into every neuron so that its burst probability would increase or decrease according to the
running average of its event rate and the desired output:

$$\begin{aligned} \text{if desired output} = 0 &\Rightarrow I_i^{(d)} = -c/(e_{\max} - \bar{E}_i) \\ \text{if desired output} = 1 &\Rightarrow I_i^{(d)} = c/(\bar{E}_i - e_{\min}). \end{aligned}$$

572 where $c \sim 1$ nA · Hz. For instance, if the desired output was 0 and \bar{E}_i was large, then the injected
573 current was strongly hyperpolarizing. The injected current was set to zero when \bar{E}_i was to within
574 1 Hz of the desired value.

575 • *Learning protocol.* A simulation proceeded as follows. With the plasticity off, there was first a
576 relaxation interval of duration $3\tau_{\text{avg}}$, with no input applied to the network. In Fig. 4, we have set
577 $\tau_{\text{avg}} = 2$ s, although a faster time scale can still yield adequate learning (Fig. S2). Then, the four
578 different input pairs were applied consecutively to give the “before learning” response in Fig. 4d.
579 Afterward, the four input/output pairs were applied consecutively for 20 s each (typically in the
580 same order); namely one epoch (for one epoch), typically in the same order (but see Fig. S1e).
581 For each input/output pair, first, the input alone was applied to the input populations with the
582 plasticity off. We let the network reach its steady state for that input for the first 90% of the
583 duration of an example. During this prediction interval, the moving average of the burst probability
584 would converge towards the actual burst probability of the population for that given input. The
585 duration of an example was chosen to be $4\tau_{\text{avg}} = 8$ s to provide enough time for this steady state to
586 be reached to a good approximation, although relaxing that assumption can still produce adequate
587 learning (Fig. S2). During the last 10% of the example duration, the plasticity was activated for
588 all feedforward excitatory synapses and the teacher was applied. For computational efficiency,
589 the error was computed once, at the very end of the prediction interval. The total number of
590 epochs required to reach decent performance depended on the initialization of the network and the
591 learning rate; for Fig. 4, we used 500 epochs. At the end of learning, the plasticity was switched
592 off for good and the “after learning” response was computed.

593 Deep network model for categorical learning

594 We now describe the deep network model that was used to learn the classification tasks reported in
 595 Figs. 5-6. The model can be seen as a limiting case of a time-dependent rate model, which itself can be
 596 heuristically derived from the spiking network model under simplifying assumptions (see Supplemental
 597 Materials).

598 For the fully-connected layers in the network, we defined the “somatic potentials” of units in layer l
 599 as:

$$\mathbf{v}_l = \mathbf{W}_l \mathbf{e}_{l-1},$$

where \mathbf{W}_l is the weight connecting layer $l-1$ to layer l . Note that in this formulation we include a bias term as a column of \mathbf{W}_l . The event rate of layer l was given by

$$\mathbf{e}_l = f_l(\mathbf{v}_l),$$

600 where f_l is the activation function for layer l . In models trained on MNIST and CIFAR-10, the activation
 601 function was a sigmoid. In the model trained on ImageNet, a ReLU activation was used for hidden layers
 602 and a softmax activation was used at the output layer.

During the feedforward pass, the burst probability at the output layer ($l = L$) was set to a constant, $p_L^{(0)}$ (in these experiments, this was set to 0.2). Our previous research [59] has shown that the dendritic transfer function is a sigmoidal function of its input (see also Fig. S5). Therefore, the hidden-layer burst probabilities, \mathbf{p}_l , for $l < L$, were computed using a sigmoidal function of a local “dendritic potential” \mathbf{u}_l as

$$\mathbf{p}_l = \sigma(\beta \mathbf{u}_l + \alpha),$$

where α and β are constants controlling the dendritic transfer function. In our experiments, we set $\beta = 1$ and $\alpha = 0$. Figure S5 illustrates various mechanisms affecting these parameters. The dendritic potentials were given by

$$\mathbf{u}_l = h(\mathbf{e}_l) \odot (\mathbf{Y}_l \mathbf{b}_{l+1}), \quad (11)$$

where \odot is the elementwise product. The vector-valued function $h(\mathbf{e}_l) \equiv f'(\mathbf{v}_l) \odot \mathbf{e}_l^{-1}$ depends on the chosen activation function; of course, some caution is required when ReLU and softmax activations are used (see Supplemental Materials). The burst rate is given by

$$\mathbf{b}_{l+1} = \mathbf{p}_{l+1} \odot \mathbf{e}_{l+1}. \quad (12)$$

603 Finally, \mathbf{Y}_l is the feedback weight matrix. For the feedback alignment algorithm, \mathbf{Y}_l is a random matrix
 604 and is fixed throughout learning [34]. In the standard backpropagation algorithm, the feedforward and
 605 feedback weight matrices are symmetric so that $\mathbf{Y}_l = \mathbf{W}_{l+1}^T$, where T denotes the transpose. Below, we
 606 also describe how to learn the feedback weights to make them symmetric with the feedforward weights
 607 using the Kolen-Pollack algorithm [41].

With the teacher present, the output-layer burst probabilities were set to a squashed version of $p_L^{(0)} - h(\mathbf{e}_l) \odot \nabla_{\mathbf{e}_L} \mathcal{L}$, where \mathcal{L} is the loss function (a mean squared error loss for Figs. 5-6). The squashing function was to make sure that $p_{L,i} \in [0, 1]$. The Supplemental Materials provide a few examples of squashing functions. The burst probabilities of the hidden layers were then computed as above. Finally, the weights were updated according to

$$\Delta \mathbf{W}_l = \eta_l ((\mathbf{p}_l - \bar{\mathbf{p}}_l) \odot \mathbf{e}_l) \mathbf{e}_{l-1}^T - \lambda \mathbf{W}_l, \quad (13)$$

where \mathbf{p}_l and $\bar{\mathbf{p}}_l$ denote the burst probabilities with and without teacher, respectively, η_l is the learning rate hyperparameter for units in layer l , and λ is a weight decay hyperparameter. Note that, for this model, $\bar{\mathbf{e}}_l$ lags \mathbf{e}_l by a single computational step (see Supplemental Materials). Therefore, when the teacher appears, $\bar{\mathbf{e}}_l = \mathbf{e}_l$ and we can write

$$(\mathbf{p}_l - \bar{\mathbf{p}}_l) \odot \mathbf{e}_l = \mathbf{b}_l - \bar{\mathbf{b}}_l.$$

608 This means that, in this model, the error is directly represented by the deviation of the burst rate with
 609 respect to a reference.

In the case of convolutional layers, the event rates of ensembles in layer l were given by

$$\mathbf{e}_l = f_l(\mathbf{W}_l * \mathbf{e}_{l-1}),$$

where $*$ represents convolution. Similarly, the dendritic potentials in layer l were given by $\mathbf{u}_l = \mathbf{Y}_l * \mathbf{b}_{l+1}$ while burst probabilities were calculated as in the fully-connected layers. Finally, the weights of convolutional layers were updated as

$$\Delta \mathbf{W}_l = \eta_l \psi(\mathbf{b}_l - \bar{\mathbf{b}}_l, \mathbf{e}_{l-1}) - \lambda \mathbf{W}_l, \quad (14)$$

610 where ψ combines the burst deviations and event rates to compute an approximation of the gradient
 611 with respect to the convolutional weights \mathbf{W}_l .

612 Learning the recurrent weights

In certain experiments, we introduced recurrent inputs into the hidden layers that served to keep burst probabilities in the linear regime of the sigmoid function. At layer l , we set the reference dendritic potentials to

$$\bar{\mathbf{u}}_l = h(\mathbf{e}_l) \odot \mathbf{Y}_l \bar{\mathbf{b}}_{l+1} - \mathbf{Z}_l \bar{\mathbf{b}}_l, \quad (15)$$

where \mathbf{Z}_l is the recurrent weight matrix and the burst rates used here, in bold sans-serif, are calculated as the burst rate *without* any recurrent inputs and *without* the teaching signal:

$$\bar{\mathbf{b}}_l = \sigma(\beta h(\mathbf{e}_l) \odot \mathbf{Y}_l \bar{\mathbf{b}}_{l+1} + \alpha) \odot \mathbf{e}_l. \quad (16)$$

Otherwise, the dendritic potentials and burst rates must be solved self-consistently, slowing down computations. Recurrent weights are then updated in order to minimize $\bar{\mathbf{u}}_l$:

$$\Delta \mathbf{Z}_l = -\eta_r \bar{\mathbf{u}}_l \bar{\mathbf{b}}_l^T, \quad (17)$$

where η_r is the learning rate. Note that, with these recurrent inputs, the updates of matrix \mathbf{W}_l are the same as before, but now with

$$\mathbf{p}_l = \sigma[\beta(h(\mathbf{e}_l) \odot \mathbf{Y}_l \mathbf{b}_{l+1} - \mathbf{Z}_l \bar{\mathbf{b}}_l) + \alpha].$$

613 .

614 Learning the feedback weights

Kolen and Pollack [97] found that if the feedforward and feedback weights are updated such that

$$\begin{aligned} \Delta \mathbf{W}_l &= \eta \mathbf{A} - \lambda \mathbf{W}_l \\ \Delta \mathbf{Y}_l &= \eta \mathbf{A} - \lambda \mathbf{Y}_l, \end{aligned}$$

where \mathbf{A} is any matrix with the same shape as \mathbf{W}_l and \mathbf{Y}_l , then \mathbf{Y}_l and \mathbf{W}_l will converge. This means that if the feedback weights are updated in the same direction as the feedforward weights and weight decay is applied to both sets of weights, they will eventually become symmetric. Thus, we implemented the following learning rule for the feedback weights between layer $l+1$ and layer l :

$$\Delta \mathbf{Y}_l = \eta_l (\mathbf{b}_{l+1} - \bar{\mathbf{b}}_{l+1}) \mathbf{e}_l^T - \lambda \mathbf{Y}_l, \quad (18)$$

where λ is a weight decay hyperparameter. In convolutional layers, we used the following weight update:

$$\Delta \mathbf{Y}_l = \eta_l \psi(\mathbf{b}_{l+1} - \bar{\mathbf{b}}_{l+1}, \mathbf{e}_l) - \lambda \mathbf{Y}_l. \quad (19)$$

615 Training the model with CIFAR-10 and ImageNet

616 The network architectures described in Tables S3 and S4 of the Supplemental Materials were trained
617 on standard image classification datasets, CIFAR-10 [122] and ImageNet [123]. The CIFAR-10 dataset
618 consists of 60,000 32×32 px training images belonging to 10 classes, while the ImageNet dataset consists
619 of 1.2 million images (resized to 224×224 px) split among 1000 classes.

620 Each unit in these networks represents an ensemble of pyramidal neurons and has an event rate, burst
621 probability, and burst rate. For each training example, the input image is presented and a forward pass
622 is done, where event rates \mathbf{e}_l throughout the network are computed sequentially, followed by a feedback
623 pass where burst probabilities $\bar{\mathbf{p}}_l$ and burst rates $\bar{\mathbf{b}}_l$ are computed. Then, the teaching signal is shown at
624 the output layer, and new burst probabilities \mathbf{p}_l and burst rates \mathbf{b}_l are computed backward through
625 the network. Weights are then updated using our weight update rules. Networks were trained using
626 stochastic gradient descent (SGD) with mini-batches, momentum and weight decay. ReLU layers were
627 initialized from a normal distribution using Kaiming initialization [124], whereas Xavier initialization
628 was used in sigmoid layers [125]. Hyperparameter optimization was done on all networks using validation
629 data (see Supplemental Materials for details).

630 Training the model using node perturbation

Node perturbation is a technique that approximates gradient descent by randomly perturbing the
activations of units in the network, and updating weights according to the change in the loss function
[22, 23]. In the model trained using node perturbation, at each step, first the input is propagated through
the network as usual, after which the global loss, L , is recorded. Then, the same input is propagated
again through the network but the activations of units in a single layer l are randomly perturbed:

$$\mathbf{e}_l = f_l(\mathbf{W}_l * \mathbf{e}_{l-1} + \boldsymbol{\xi}_l), \quad (20)$$

where the elements of $\boldsymbol{\xi}_l$ are chosen from a normal distribution with mean 0 and standard deviation
 σ . The new loss, L_{NP} , is recorded. The weights in layer l are then updated using the following weight
update rule:

$$\Delta \mathbf{W}_l = \eta_l ((L_{\text{NP}} - L) \boldsymbol{\xi}_l / \sigma^2) \mathbf{e}_{l-1}^T. \quad (21)$$

631 The layer to be perturbed, l , is changed with each mini-batch by iterating bottom-up through all of the
632 layers in the network.

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639 Author contributions

640 All authors contributed to the burst-dependent learning rule. AP performed the spiking simulations.
641 JG designed the recurrent plasticity rule and performed the numerical experiments on CIFAR-10 and
642 ImageNet. BAR and RN wrote the manuscript, with contributions from JG and AP. BAR and RN
643 co-supervised the project.

Code availability

The codes used in this article are available at <https://github.com/apayeur/spikingburstprop> and <https://github.com/jordan-g/Burstprop>.

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