Estimating the Probability of Early Afterdepolarization and Predicting

Arrhythmic Risk associated with Long QT Syndrome Type 1 Mutations

Qingchu Jin[1], Joseph L. Greenstein[1], Raimond L. Winslow[1*]

[1]Department of Biomedical Engineering and Institute for Computational Medicine,

Johns Hopkins University, Baltimore, MD, United States of America

* Corresponding author

E-mail: rwinslow@jhu.edu

**Abstract**

Early after-depolarizations (EADs) are action potential (AP) repolarization abnormalities that can trigger lethal arrhythmias. Simulations using biophysically-detailed cardiac myocyte models can reveal how model parameters influence the probability of these cellular arrhythmias, however such analyses can pose a huge computational burden. We have previously developed a highly simplified approach in which logistic regression models (LRMs) map parameters of complex cell models to the probability of ectopic beats (EBs). Here, we extend this approach to predict the probability of early after-depolarizations (P(EAD)). We use the LRM to investigate how changes in parameters of the slow-activating delayed rectifier current ($I_{Ks}$) affect P(EAD) for 17 different Long QT syndrome type 1 (LQTS1) mutations. We compare P(EAD) for these 17 LQTS1 mutations with two other recently proposed model-based arrhythmia risk metrics. These three model-based risk metrics yield similar prediction performance; however, they all fail to predict relative clinical risk for a significant number of the 17 studied LQTS1 mutations. The consistent successes and failures of all three risk metrics suggest that important functional characteristics of LQTS1 mutations may not yet be fully known.

## **Author summary**

An early after-depolarization (EAD) is an abnormal cellular electrical event which can trigger dangerous arrhythmias in the heart. We use our previously developed method to build a simple logistic regression model (LRM) that estimates the probability of EAD (P(EAD)) as a function of myocyte model parameters. Using this LRM along with two other recently published model-based arrhythmia risk predictors, we estimate risk of arrhythmia for 17 Long QT syndrome type 1 (LQTS1) mutations. Results show that all approaches have similar prediction performance in that there are a set of mutations whose relative clinical risk for arrhythmia are well estimated using these metrics, but that relative risk is consistently over- or under-estimated across all approaches for a significant number of other mutations. We believe this indicates that the functional characterization of the LQTS1 phenotype is incomplete.

## Introduction

Early after-depolarizations (EADs) are abnormal repolarization events that occur during the plateau or rapid repolarization phase of action potentials (APs), which can in turn trigger large scale cardiac arrhythmias in the setting of long QT syndrome [1-3]. Computational modeling of EADs has provided insights into the mechanisms by which they can trigger arrhythmias in the heart [4-6].

We seek to understand how variations in the underlying biophysical properties or physiological state of the myocyte influence the probability of occurrence of EADs. Stochastic mechanisms play a role in EAD initiation. Fowler et al. demonstrated that stochastic $Ca^{2+}$ sparks and local $Ca^{2+}$ waves can generate sufficient $Na^+/Ca^{2+}$ exchanger current to trigger EADs [7]. Tanskanen et al. also showed that a phosphorylation-induced change in LCC stochastic gating contributes to EAD initiation [8]. Therefore, we use a three-dimensional spatial model of the ventricular myocyte developed by Walker et al. [9] in which the fundamental events governing intracellular calcium ($Ca^{2+}$) dynamics are modeled stochastically.

The complexity of this stochastic model makes it challenging to perform the many repeated simulations needed to estimate the probability of EADs, denoted P(EAD), as a function of underlying model parameters. Here, we develop a logistic regression model (LRM) that directly maps myocyte model parameters to P(EAD) [10]. This approach allows for evaluation of the relationship between these event probabilities and model parameters, which we refer to as arrhythmia sensitivity analysis.

We apply arrhythmia sensitivity analysis by analyzing the arrhythmogenic potential of

mutations in the alpha subunit KCNQ1 of the slow-activating delayed rectifier current

$I_{Ks}$ that underlies Long QT Syndrome type 1 (LQTS1) [11]. Studies show that mutant

$I_{Ks}$ in LQTS1 contributes to generation of EADs, which may then lead to Torsades de

Pointes at the level of the whole heart [12, 13]. Jons et al. described electrophysiological

changes associated with 17 different LQTS1 mutations by experimentally measuring

altered values of five $I_{Ks}$-related parameters for each mutation [6]. We use the LRM to

estimate and analyze how these measured changes in $I_{Ks}$ parameters, and their

experimentally observed uncertainties, impact P(EAD) for each of these LQTS1

mutations.

Action potential duration (APD) prolongation and QT-interval prolongation have been

widely used as surrogate indicators for increased arrhythmogenic potential [14-17].

However, the relationship between these surrogate features and the likelihood of

arrhythmia is indirect and sometimes at odds with experimental observations. For

example, ranolazine leads to QT prolongation (a surrogate proarrhythmic indicator) in

multiple clinical trials [18, 19] but has demonstrated anti-arrhythmic effects [20].

Recently, novel approaches for computational prediction of arrhythmogenic potential

have emerged [21-24]. These studies utilize the abovementioned surrogates for

arrhythmia to perform risk prediction. Rather than relying upon these indirect indicators

of arrhythmic potential, in this work we develop model-based methods for directly

estimating the probability of occurrence of the actual cellular events that trigger

arrhythmias, EADs. Using the LQTS1 electrophysiological data of Jons et al. [6], we

directly estimate P(EAD) for each LQTS1 mutation [25]. We compare the model

estimated P(EAD) as an arrhythmia risk metric to those obtained using two other

recently published methods. In the first method, Kernik et al. leveraged a population

model of induced pluripotent stem cell derived cardiomyocytes (iPSC-CMs) to develop

an approach for LQTS1 arrhythmia risk prediction[26]. In this approach, for each

mutation, the parameters of the wild-type $I_{Ks}$ in their control population model are

modified using the distribution of parameters measured in mutant channels. For each

mutation, the percentage of individual models in the population that satisfy all three of

the following conditions is taken as the risk prediction metric: exhibit 1) > 4% increase

of $APD_{90}$, 2) $\geq$ 4% increase of beat-to-beat variation and 3) $\geq$ 4% increase of APD

triangulation ($APD_{90}$-$APD_{30}$) [23]. The larger this percentage is, the greater the risk

associated with the mutation. In the second method, Hoefen et al. used transmural

repolarization prolongation (TRP) calculated using a 1-dimensional myocyte fiber

model as an arrhythmic risk prediction metric [24]. Larger values of TRP are associated

with greater risk.

We show that the relative risk (i.e., the rank ordered risk across the 17 mutations)

estimated for the 17 LQTS1 mutations characterized by Jons et al. [6] are very similar

across these three metrics. We also compare relative risk using these metrics to the

relative clinical risk assessed using the 30-year cardiac event rate for each mutation [6].

All three risk metrics yield consistent estimates of the relative risk for the 17 mutations.

In addition, the metrics are consistent in their identification of a subset of mutations

whose predicted relative risk agree with, and another subset whose relative risks differ

substantially from the measured relative clinical risk. A possible explanation for this discrepancy is that experimental characterization of these LQTS1 mutations is incomplete in functionally important ways.

## Results

### Modeling the Role of $I_{Ks}$ on Probability of EADs

LQTS1 arises from mutations in KCNQ1, the alpha subunit of the $I_{Ks}$ channel [11]. The symptoms of LQTS1 include syncope, cardiac arrest, and sudden death [27]. Jons et al. experimentally characterized the electrophysiological properties of $I_{Ks}$ expressed in Xenopus oocytes for 17 LQTS1 mutations and reported the clinically measured 30-year cardiac event rate for each mutation [6]. The 30-year cardiac event rate is defined as the percentage of people within a population of carriers of the mutant who experienced syncope, cardiac arrest, or sudden death within the first 30 years of life. The outcomes of syncope, aborted cardiac arrest, and sudden cardiac death are defined as cardiac events.

An LRM was formulated to capture the quantitative relationship between P(EAD) and the 5 $I_{Ks}$-related parameters measured experimentally (activation time constant scaling factor $\tau_{+}\_sf$; deactivation time constant scaling factor $\tau_{-}\_sf$; shift of the half maximal activation voltage $\Delta V_{1/2}$; scaling factor for voltage-dependent activation curve slope k_sf, and maximal conductance scaling factor $G_{Ks}\_sf$). These 5 parameters were chosen because they have been experimentally measured for a number of different LQTS1 mutations [6]. Fig 1A shows examples of APs computed using the Walker et al. model

[9] without (blue) and with (red) EADs. Because of the stochastic nature of the myocyte

model, for the same parameter value, realizations obtained with different random

number seeds may generate an AP with or without EADs. We defined a biophysically

meaningful region of interest over which model parameters are varied and within which

the LRM is built (S4 Table). Fig 1B demonstrates the relationship between parameters

within this region of interest and P(EAD), where $\underline{B}^T\underline{P}$ (the argument of the logistic

regression function) is the weighted ($\underline{B}$) summation of LRM features ($\underline{P}$). The nonlinear

logistic relationship defines three domains of interest: transition domain, lower plateau

domain, and upper plateau domain. The transition domain is a region in which P(EAD)

is a sensitive function of $\underline{B}^T\underline{P}$, corresponding to the steep part of the curve in Fig 1B.

The lower plateau domain and upper plateau domain are regions where P(EAD) is

relatively insensitive to parameter variation, with P(EAD) = ~0 in the lower plateau

domain and P(EAD) = ~1 in the upper plateau domain. We sampled 200 parameter sets

and ran 100 realizations for each set to train the LRM (see Methods). Once determined,

the LRM enables direct calculation of P(EAD) for any parameter set without the need

to simulate the underlying complex myocyte model. Fig 1B shows the fidelity with

which the LRM model (blue line) reproduces P(EAD) estimated from simulations using

the full myocyte model (red points) for the training data set (200 parameter sets) as a

function of $\underline{B}^T\underline{P}$. Detailed modeling methods and performance metrics are described in

Methods and S1 Text. Fig 1C shows the LRM-predicted P(EAD) versus P(EAD)

computed from the myocyte model simulations. The LRM performs well in predicting

P(EAD) ($R^2$ = 0.971 for the 96 parameter sets inside the transition domain, mean

prediction error of 0.022 ± 0.036 (see S1 Text and Eq S1)), despite the highly complex

nonlinear properties of the myocyte model. To test the ability of the LRM to generalize,

Figs 1D-E compare the LRM predicted P(EAD) to that computed using the myocyte

model for test data consisting of 100 independent parameter sets. The LRM performs

well on the test set ($R^2$ = 0.933 for the 27 parameter sets within the transition domain,

mean prediction error = 0.019 ± 0.043).

The LRM for P(EAD) was formulated with a total of 16 features, 5 being the linear

features (original parameters of $I_{Ks}$) $\tau_{+}$_sf, $\tau_{-}$_sf, $\Delta V_{1/2}$, k_sf, and $G_{Ks}$_sf, and 11 being

quadratic features (derived from the original $I_{Ks}$ parameters) $\tau_{+}$_sf*$G_{Ks}$_sf,

$\Delta V_{1/2}$*$G_{Ks}$_sf, $\tau_{+}$_sf$^2$, $\tau_{-}$_sf*$G_{Ks}$_sf, k_sf$^2$, k_sf*$\Delta V_{1/2}$, $\tau_{-}$_sf$^2$, $\tau_{+}$_sf*$\Delta V_{1/2}$, $G_{Ks}$_sf*k_sf,

k_sf* $\tau_{-}$_sf and $\tau_{-}$_sf*$\Delta V_{1/2}$. Table 1 shows the LRM weights for each feature ranked by

feature importance. In order to ensure interpretability of feature importance from the

LRM weights, parameters were scaled to a range from 0 to 1. The data of Table 1 shows

that $I_{Ks}$ conductance ($G_{Ks}$_sf) is the most important, and this is followed in rank-order

by $\tau_{+}$_sf*$G_{Ks}$_sf, k_sf, and $\Delta V_{1/2}$*$G_{Ks}$_sf.

**Fig 1. EAD study**. (A) Example APs from myocyte model [9] simulations.

Representative APs without EADs (blue) and with EADs (red) are shown. For each

realization, an EAD is considered to have occurred if the membrane voltage at 500 ms

(black vertical line) following the time of stimulus current is greater than -40 mV. (B)

Comparison between LRM-predicted P(EAD) (blue) and P(EAD) computed from

simulations using the myocyte model (red) as a function of $\underline{B}^T\underline{P}$ (weighted summation

of LRM features) for the training set. (C) LRM-predicted P(EAD) (y-axis) vs

corresponding P(EAD) estimated using the myocyte model (x-axis) for the training set.

(D) and (E) show the same analyses described in (B) and (C), respectively, but for the

independent test set. $R^2$ is calculated only from parameter sets within the transition

domain, LRM: logistic regression model, MM: myocyte model

**Table 1. EAD features ranked by relative importance.**

| Ranking | Feature | Weight ± SE from LRM |
|---------|---------|----------------------|
| 1 | $G_{Ks}\_sf$ | $-63.89 \pm 1.86$ |
| 2 | $\tau_+\_sf * G_{Ks}\_sf$ | $34.35 \pm 2.07$ |
| 3 | $k\_sf$ | $14.57 \pm 0.65$ |
| 4 | $\Delta V_{1/2} * G_{Ks}\_sf$ | $12.83 \pm 1.61$ |
| 5 | $\tau_+\_sf$ | $11.90 \pm 0.59$ |
| 6 | $\tau_+\_sf^2$ | $-10.27 \pm 0.73$ |
| 7 | $\tau_-\_sf * G_{Ks}\_sf$ | $8.54 \pm 1.11$ |
| 8 | $k\_sf^2$ | $-7.67 \pm 0.41$ |
| 9 | $k\_sf * \Delta V_{1/2}$ | $-6.31 \pm 0.43$ |

| 10 | $\Delta V_{1/2}$ | -6.05 ± 0.51 |
|---|---|---|
| 11 | $\tau_{-}\_sf^{2}$ | -5.29 ± 0.36 |
| 12 | $\tau_{+}\_sf * \Delta V_{1/2}$ | -4.66 ± 0.69 |
| 13 | $G_{Ks}\_sf * k\_sf$ | -4.00 ±1.11 |
| 14 | $\tau_{-}\_sf$ | 3.09 ± 0.62 |
| 15 | $k\_sf * \tau_{-}\_sf$ | 2.07 ± 0.37 |
| 16 | $\tau_{-}\_sf * \Delta V_{1/2}$ | -1.26 ± 0.37 |

## Effect of LQTS1 Mutations on EAD Probability.

For each mutation, 5 $I_{Ks}$-related functional parameters ($\tau_{+}\_sf$, $\tau_{-}\_sf$, $\Delta V_{1/2}$, $k\_sf$, and

$G_{Ks}\_sf$) were measured experimentally [6]. Measurements were obtained from no less

than 16 oocytes for each mutation. Jons et al. quantified the experimental uncertainty

in the measurement of each $I_{Ks}$ parameter for each mutation by providing a mean ($\mu$)

and standard error for each of the five experimentally measured parameters. We derived

the standard deviation ($\sigma$) from the reported standard error, which is summarized in S1

Table.

The LRM is used to investigate the effects of experimental uncertainty in parameter

estimates on P(EAD) for each mutation. Parameter sets are constructed by choosing

each of the five parameters as independent normally distributed random variables with

mean $\mu$ and standard deviation $\sigma$ measured experimentally. For each of these randomly

generated parameter sets, the LRM maps these parameters to P(EAD). Therefore, the

value of P(EAD) predicted using the LRM is itself a random variable with its own

distribution. We estimate this distribution using Monte Carlo methods by choosing $10^6$

normally distributed parameter sets for each mutation (see details in Methods).

Parameter set distributions estimated in this way reveal the impact of experimental

uncertainties on estimates of P(EAD) dervied from arrhythmia sensitivity analysis.

Fig 2A-C show the distribution of P(EAD) for the three representative mutations *G314S*,

*G168R*, and *Y315C*, with high, medium, and low average P(EAD), respectively. The

P(EAD) distribution for *G314S* is narrow with a single peak at P(EAD) near one. This

indicates that despite the experimental uncertainty (EU) in measurement of this

parameter set, we can be quite certain that this mutation leads to EADs with high

probability. However, the *G168R* and *Y315C* distributions are bimodal with peaks near

zero and one. In these cases, parameter sets belong to two subgroups, one that almost

always leads to EADs and another that seldom does. These bimodal distributions of

P(EAD) can be approximated by a Bernoulli distribution with parameter p, where p =

P(P(EAD) >0.5) for any particular parameter set and 1-p = P(P(EAD) <0.5). The

parameter p, which can be approximated as the mean P(EAD), denoted $P_m$(EAD), is

shown by the red vertical line in Figs. 2B and C, where *G168R* has larger mean P(EAD)

than *Y315C*.

To explain the observed P(EAD) distributions, the probability density function (PDF)

of $\underline{B}^T\underline{P}$ (red) and the model logistic function (blue) that relates $\underline{B}^T\underline{P}$ to P(EAD) is shown

in Fig 2D. Recall that $\underline{B}^T\underline{P}$ is a function of 5 $I_{Ks}$-related parameters which appears in the

LRM. Therefore, probability density functions (PDFs; red) of $\underline{B}^T\underline{P}$ can be derived using

the Monte Carlo method with parameter distributions matching the experimental

uncertanties measured by Jons et al. [6]. For mutation *G314S*, the PDF (squares) is

narrow with mean positioned within the upper plateau domain and part of the transition

domain of the model logistic function. This results in a P(EAD) distribution that is

unimodal and close to 1. For the *G168R* and *Y315C*, PDFs are broader and span all

domains (i.e. lower plateau domain, transition domain, and upper plateau domain) of

the model logistic function, thus resulting in a P(EAD) distribution that is bimodal.

To validate this use of the LRM in uncertainty analyses, we performed Monte Carlo

simulations of the myocyte model with 200 randomly generated sample parameter sets

for the *L266P* mutation (200 realizations were run for each set). Fig 2E shows that the

distribution of P(EAD) predicted by the LRM faithfully reproduces that generated from

the myocyte model. The total computation time required for all myocyte model

simulations was ~17,000 CPU hours whereas the LRM model required less than 1 CPU

second.

**Fig 2. LQTS1 study.** LRM-based estimates of P(EAD) distribution for mutations: (A)

*G314S*, (B) *G168R*, and (C) *Y315C*. Red vertical lines in A-C represent the mean

P(EAD) given the observed experimental uncertainty (EU) in each mutation-specific

parameter set. This is denoted as P( P(EAD) | EU ) on the ordinate. (D) PDFs of $\underline{B}^T\underline{P}$

(red) are shown for each mutation (*G314S*: solid line, *G168R*: star markers, and *Y315C*:

square markers), where $\underline{B}^T\underline{P}$ is the weighted summation of 16 $I_{Ks}$ features (5 parameters

+ 11 quadratic features) for each mutation. The logistic function curve (blue) relates

$\underline{B}^T\underline{P}$ to P(EAD). (E) Comparison of P(EAD) distributions for *L266P* computed using

the LRM (blue) and myocyte model (red).

To further delineate the effects of EU in the measured properties of $I_{Ks}$ for each mutation,

we evaluated the contribution of each individual parameter to the uncertainty of

P(EAD) for each mutation. To do this, only a single parameter is varied while others

are assigned a constant value equal to their experimentally measured mean value, and

this process is repeated for each parameter set. In S2A Fig, PDFs (red curves) are shown

for *G314S* and *Y315C* arising from variations in $\tau_{+}\_sf$ based on its EU with all other

parameter sets held constant. S2B-E Figs show the same analyses for $\tau_{-}\_sf$, $\Delta V_{1/2}$, k_sf,

and $G_{Ks}\_sf$. Note that the PDFs in Fig 2D, where all parameters vary simultaneously,

are nearly identical to those of S2E Fig, indicating that $G_{Ks}$ uncertainty plays a dominant

role in determining overall uncertainty of the P(EAD) across all 5 $I_{Ks}$ parameters for all

mutations.

**LQTS1 mutation arrthymic risk prediction.**

Kernik et al. designed an arrhythmia risk prediction metric that is calculated using a

population model of myocytes (iPSC-CMs) [28]. In this approach, a population model

is built for each mutation by replacing the wild-type $I_{Ks}$-related parameters in their

control population model with those chosen from a distribution of mutation parameters.

The risk prediction metric is taken as the percentage of model myocytes in the

population model for each mutation satisfying all 3 of the following conditions: 1) >

4% increase of $APD_{90}$, 2) $\geq$ 4% increase of beat-to-beat $APD_{90}$ variation, and 3) $\geq$ 4%

increase of APD triangulation ($APD_{90}$-$APD_{30}$)[23]. We refer to this metric as the AP

morphology metric and calculated it for the 17 LQTS1 mutations using this population

myocyte model.

Hoefen et al. used a modified Flaim-Giles-McCulloch [29] 1D fiber model to estimate

transmural repolarization prolongation (TRP) for these 17 mutations [15]. We denote

this metric as the TRP metric. Values of this metric for the 17 LQTS1 mutations were

taken from Fig 1C of Hoefen et al. [15]. Further details are given in Methods.

S2 Table shows prediction of three model-based risk metrics for 17 mutations. S3 Fig

shows that $P_m$(EAD) is well aligned with the AP morphology metric ($R^2$ = 0.93, S3A

Fig) and the TRP metric ($R^2$=0.80, S3B Fig). To compare model-based risk metrics with

clinical risk, we determined the relative risk ranking (r) for each mutation (with rank of

1 denoting the lowest risk and a rank of 17 denoting the highest risk amongst the 17

mutations). The relative risk ranking predicted using a model-based metric is denoted

as $r_{pred}$ and the relative risk ranking based on clinical risk is denoted as $r_{clin}$. For example,

*A341V* has $r_{clin}$=17 (highest clinical risk) and $r_{pred}$ = 6, 8, or 5 (intermediate predicted

risk) for $P_m$(EAD), AP morphology metric, and TRP metric, respectively. S2 Table

shows $r_{pred}$ of the three different risk metrics and $r_{clin}$ for the 17 mutations. We then

calculated the difference ($\Delta r$ = $r_{pred}$ - $r_{clin}$) between the relative risk ranking predicted

using each of the three model-based metrics and the clinical ranking. If $\Delta r$ is negative,

then $r_{pred}$ underestimates arrhythmic risk, and vice versa. The greater the difference in

ranking, the greater is the under- ($\Delta r < 0$) or over- ($\Delta r > 0$) prediction. Fig 3 shows $\Delta r$

for all 3 metrics for the 17 mutations. In Fig 3, mutations are ordered from those with

the greatest underprediction of risk to those with the greatest overprediction of risk. The

three metrics yield similar results for all mutations, consistent with the relationships

among the metrics shown in S3 Fig. Results show that *A341V* and *R494Q* are the two

mutations with the most severely underpredicted risk, while *G168R* and *W305S* are the

two mutations with the most overpredicted risk. The $r_{pred}$ for mutations S225L, R243C,

V254M, D611Y and G314S are in close agreement ($-3 \leq \Delta r \leq 3$) with their respective

$r_{clin}$.

**Fig 3. Relative risk ranking comparison across 3 model-based risk metrics.** The

difference of relative risk ranking ($\Delta r = r_{pred} - r_{clin}$) between that predicted using the

model-based metric ($r_{pred}$) and that based on clinical risk ($r_{clin}$) for all 17 mutations. For

each mutation, there are three $r_{pred}$ values corresponding to each of the three model-

based risk metrics. An average $r_{pred}$, and hence an average $\Delta r$, is calculated for each

mutation and determines their ordering (from most negative to most positive $\Delta r$)

In the study of Jons et al. [15], different numbers of patients exhibited each mutation.

The number of patients evaluated with a given mutation may therefore limit the

statistical significance of the risk associated with that mutation. Therefore, we performed a pairwise Fisher exact test for each pair of mutations (S4 Fig) to determine those pairwise differences in risk that are statistically significant in the Jons et al. study. 42 out of 136 mutation pairs with $p<0.05$ were found to be significant pairs. Three approaches ($P_m$(EAD) in Fig 4A, AP morphology metric in Fig 4B, and TRP metric in Fig 4C) are used to rank order the risk for significant pairs and to compare them with the rank order of clinical risk. An entry of 1 indicates that the predicted rank order of the mutation pair is consistent with the clinical rank order for this pair, whereas an entry of 0 means the predicted rank order is reversed and opposite to that observed clinically. For example, for *V254M-W305S* pair, *V254M* has greater clinical risk than *W305S*, thus the clinical rank order is *V254M > W305S*. Given the predicted risk from $P_m$(EAD) of *V254M* ($P_m$(EAD) = 0.742) and *W305S* ($P_m$(EAD) = 0.184), the predicted rank order is *V254M > W305S*, consistent with the clinical rank order. Thus, in Fig 4A, the element in the lattice for the *V254M-W305S* pair is set to 1. In contrast, based on the prediction by AP morphology metric, the predicted rank order is *V254M < W305S*. Thus, in Fig 4B, the element in the lattice for the *V254M-W305S* pair is set to 0.

To quantify performance of each metric, the accuracy of pairwise relative risk prediction is measured by calculating the percentage of mutation pairs for which the predicted relative risk matched the clinical relative risk. The set of mutation pairs was divided into two subgroups, one in which all pairs have a statistically significant clinical risk difference ($p < 0.05$ in the Fisher exact test), and its complement. The accuracy for each metric is summarized in Table two across all mutation pairs, as well as separately

within these two subgroups. For all metrics, the accuracy within the subgroup of

significant pairs is higher than the accuracies across all pairs and or within the subgroup

of non-significant pairs. The TRP metric has the highest accuracy in both significant

pairs and all pairs. Despite this, there remain 37% of mutation pairs whose relative risk

the TRP metric is unable to predict correctly. The detailed pairwise prediction on all

pairs is shown in S5 Fig. In Fig 4, all metrics performed poorly on *A341V*-associated

pairs, which is consistent with the conclusion from Fig 3 that relative risk associated

with mutation *A341V* is underestimated.

**Fig 4. Performance of pairwise prediction in significant mutation pairs.** Three

approaches, (A) $P_m$(EAD), (B) AP morphology, and (C) TRP, are used to predict the

risk rank order of significant mutation pairs. Mutations are ordered by clinical risk

ranking from lowest to highest (left to right on the x-axis and top to bottom on the y-

axis). A table value of 1 indicates that, for this pair, the ranking of $r_{pred}$ values is

consistent with that of $r_{clin}$ values and a table value of 0 means that predicted rank is

inconsistent with the clinical rank. Since significant pairs are shown only in the lower

triangle of the heatmap, for any pair, the y-axis mutation always has a greater clinical

risk than the x-axis mutation.

**Table 2. Mutation pairwise prediction accuracy**

|  | All pairs | Significant pairs | Non-significant pairs |
|---|---|---|---|
| $P_m(EAD)$ | 0.57 | 0.69 | 0.51 |
| AP morphology | 0.54 | 0.64 | 0.50 |
| TRP | 0.63 | 0.81 | 0.54 |

# Discussion

## Logistic regression model on probability of EAD

Using our previously developed method [10], we built a logistic regression model that

maps 5 $I_{Ks}$-related parameters to P(EAD). Fig 1E shows that P(EAD) predicted using

the LRM agrees well with that estimated from simulations obtained using the Walker

model. The computational efficiency of the LRM approach is what makes arrhythmia

sensitivity analysis for experimentally determined parameter set distributions possible.

In Fig 2E, calculating the *L226P* P(EAD) distribution using the Walker myocyte model

(200 parameter sets and 200 realizations for each set) required ~16,000 CPU hours

whereas the LRM required ~0.5 CPU second to simulate the $10^6$ parameter sets.

**Arrhyhmia sensitivity analysis**

LRMs enable us to quantitatively explore the relationship between parameters and P(EAD). $G_{Ks}$ is the most important parameter of $I_{Ks}$ with regard to P(EAD) because in the ranking of feature importance, it is associated with the first, second, and fourth features in Table 1. To analyze the relationship between parameters and P(EAD), we vary one parameter while fixing the other four parameters at their wild type values. S1A Fig shows that decreasing $G_{Ks}$ results in P(EAD) going from 0 to 1. This result follows from the fact that $I_{Ks}$ is a repolarizing current. With the decrease of conductance of $I_{Ks}$, the action potential becomes more prone to depolarizing events, thus leading to higher likelihood of EAD occurrence [30]. However, with $G_{Ks}$ at its wild-type value, varying any other parameter has no effect on P(EAD), which is always 0. Furthermore, when $G_{Ks}$ is reduced to half of its wild-type value and other parameters are varied ($\tau_{+}$_sf (S1B Fig), $\tau_{-}$_sf (S1C Fig), $\Delta V_{1/2}$ (S1D Fig), and k_sf (S1E Fig)), P(EAD) is positively related to $\tau_{+}$_sf, $\Delta V_{1/2}$, and k_sf. This indicates that a reduction of $G_{Ks}$ not only increases P(EAD), but also increases the sensitivity of the P(EAD) to variation of other parameters.

**Uncertainty analysis on LQTS1 mutations**

In Fig 2B and 2C, a bimodal distribution of P(EAD) for mutations *G168R* and *Y315C* is observed. Fig 2D shows that this arises as an interplay between the PDF of $\underline{B}^T\underline{P}$ (when parameters $\underline{P}$ are modeled as normally distributed random variables, $\underline{B}^T\underline{P}$ is also a random variable with a normal distribution) and the model logistic function. Similar bimodal distributions were observed in our previous study of the probability of ectopic

beats caused by delayed afterdepolarizations [10]. Given the bimodal shape of the

P(EAD) distribution, small perturbations of the 5 $I_{Ks}$-related parameters result in model

cells that either exhibit normal APs exclusively, or APs with EADs exclusively.

In S2 Fig, we evaluated the contribution of each individual parameter to the uncertainty

of P(EAD) for *G168R* and *Y315C*. The PDF of $\underline{B}^T\underline{P}$ in S2E Fig arising from variability

in $G_{Ks}$_sf alone nearly matches the PDF in Fig 2D, where variabilities of all parameters

are considered, indicating that $G_{Ks}$_sf uncertainty alone provides enough information

to approximately reconstruct the P(EAD) distribution. This result indicates that in

LQTS1, $I_{Ks}$ expression variability is more impactful than variations in its kinetic or

voltage-dependent properties with respect to the uncertainty of P(EAD). A similar

conclusion has been made in LQTS type 2 (LQTS2). Anderson et al. showed that

protein trafficking (which ultimately impacts cell-surface expression), rather than

gating or permeation (intrinsic functional properties of the channel), is the dominant

mechanism for loss of Kv11.1 channel function in LQTS2 [31].

**The comparison of arrhythmia risk prediction approaches**

Action potential duration (APD) and QT prolongation have been widely used as

surrogates, both in basic research and in clinical settings, as indicators of disease [14,

15] and drug-related arrhythmogenic effects [16, 17]. However, there are examples

which have shown the dissociation of these two surrogates with risk of arrhythmia. For

example, alfuzosin prolongs APD and QT interval but is not linked to occurrence of

Torsades de Pointes [32]. Ranolazine leads to QT prolongation (surrogate

proarrhythmic indicator) in multiple clinical trials [18, 19] but has demonstrated anti-

arrhythmic effects [20]. Computational methods of arrhythmia risk prediction have

recently emerged[15, 21-23]. These studies focus on simulating the abovementioned

surrogates and other indirect surrogates to predict arrhythmia risk. Unlike these indirect

surrogates, the EAD is a fundamental cellular arrhythmia event. The stochastic myocyte

model, in principle, can be used to estimate P(EAD) but doing so is unrealistic because

of its high computational burden. Such estimates become possible with our highly

simplified LRM approach.

We not only examined $P_m(EAD)$ as a risk metric, we also contrasted its performance

with two other published metrics: 1) AP morphology metric (a metric based on AP

morphology over a population of myocytes) [33]; and 2) TRP metric (transmural

repolarization prolongation within a 1D cardio fiber model) [24]. S3 Fig shows that all

three approaches yield very similar predictions of relative risk. Fig 3 shows that the

predicted relative risk is consistent across all three model-based risk metrics. Note that

calculation of each metric is done using a different myocyte model. The Walker

stochastic model is used for $P_m(EAD)$. The Kernik iPSC-CM population model [28] is

used to calculate the AP morphology metric. A modified Flaim-Giles-McCulloch [29]

1D fiber model is used for the TRP metric. Thus, results are consistent across risk

metrics and across the different computational models of the cardiac myocyte on which

they are based. Table 2 shows that the TRP metric has the highest accuracy (0.63) in

pairwise mutation relative risk prediction.

To test the generalizability of the $P_m(EAD)$ metric, we also assessed $P_m(EAD)$ using

another stochastic myocyte model, specifically the model of Greenstein et al [25]. A

major difference between these two models is that the Walker model is a spatial model of the myocyte, whereas the earlier Greenstein model is a stochastic, non-spatial, compartmental model. We denote the $P_m(EAD)$ calculated from the Greenstein model as $P_m(EAD)_G$. S3C Fig shows that $P_m(EAD)_G$ is well aligned with the $P_m(EAD)$ ($R^2 = 0.91$) across these two different stochastic models.

qNet is another well-studied drug arrhythmic risk prediction metric based on a modified O'hara Rudy human myocyte model [34]. Detailed results using qNet are shown in S2 Table [34]. S3D, Fig shows that qNet is substantially different from $P_m(EAD)$ for the 17 mutations in this study ($R^2 = 0.07$). In S6 Fig, the qNet metric yields a substantially different prediction of relative risk order compared with the three approaches described here. Parikh et al. performed a global sensitivity analysis on qNet and showed that qNet is insensitive to the perturbation of $I_{Ks}$ current parameters[35]. For this reason, we chose not to focus on use of qNet for predicting the risk of LQTS1 mutations in this study.

Clearly, each of the three metrics studied make significant errors in predicting the relative risk of mutations. Nonetheless, these intrinsically different metrics based on estimates of $P_m(EAD)$, AP morphology across populations of myocyte models (the AP morphology metric), and a 1-D tissue-level model (the TRP metric) yield highly consistent predictions of relative risk across the mutations studied. This consistency across metrics and models suggests to us that for those mutations where risk is significantly under- or over-estimated, the fundamental properties of these mutations may be inadequately characterized by the five $I_{Ks}$ parameters studied by Jons et al. [15]. We give a possible example. Heijman et al. found that in the LQTS1 mutation *A341V,*

not only is $I_{Ks}$ reduced, but that the increase of $I_{Ks}$ observed during βAR-stimulation in

wild-type myocytes is reduced. Given that ~ 88% of triggered cardiac events in LQTS1

patients occurs during exercise or emotional stress [36], the characteristics of $I_{Ks}$ during

βAR-stimulation are relevant to evaluating arrhythmia risk. In the $P_m$(EAD) approach,

our modeling incorporated βAR-stimulation effects. However, the degree of $I_{Ks}$

upregulation was considered to be the same as that measured in wild type $I_{Ks}$. When we

incorporate the Heijman et al. results by reducing βAR-induced upregulation of $I_{Ks}$,

$P_m$(EAD) in the *A341V* mutation increases from 0.17 to 0.50, and overall relative risk

of this mutation within the total 17 mutations increases from rank 6 to rank 12. Mutation

*A341V* has the highest clinical risk. Although there remain components of risk that are

unaccounted for, incorporating βAR effects of this mutation does increase risk

estimated by $P_m$(EAD). Additionally, Heijman et al. also observed that another LQTS1

mutation *G589D* causes the loss of βAR-mediated $I_{Ks}$ upregulation. This indicates that

the suppression effect of $I_{Ks}$ upregulation during βAR-stimulation may also occur on

other LQTS1 mutations. These data suggest that the effects of βAR stimulation on $I_{Ks}$

in LQTS1 mutations are an essential, yet lacking component for risk prediction.

Values of P(EAD), as calculated in this study, do not represent the actual probabilities

of EAD-induced cardiac events given the fact that the electrotonic loads across coupled

cells in tissue are not taken into consideration. The electrotonic load at the location of

any cell in the heart counteracts effects of depolarizing current by shunting charge out

of the cell across gap junctions, thereby reducing the likelihood of triggering events

such as EADs. This load is reduced if neighboring cells depolarize more synchronously,

and under this scenario a collection of cells may locally generate EADs that can successfully propagate in the heart [37]. Therefore, the probability of a propagating tissue-level cardiac event will be much smaller than P(EAD) predicted in an isolated cell model. However, we believe that P(EAD) is intrinsically related to the fundamental probability of tissue-level cardiac events because, given the same electrotonic load, the probability of cardiac events is clearly positively correlated with P(EAD) in a single myocyte, as these events arise from a population of EAD generating cells. Therefore, understanding how mutations and other cellular alterations impact the generation of cellular arrhythmias such as EADs is a fundamental step in understanding how they lead to clinical cardiac events.

In summary, we developed a LRM mapping 5 $I_{Ks}$-related parameters to P(EAD). We used this model to investigate how variation of $I_{Ks}$-related parameters affects P(EAD).

A reduction of $G_{Ks}$ increases P(EAD) and increases its sensitivity to variation of other parameters. We also examined how experimental uncertainties of $I_{Ks}$-related parameters affect model estimated distributions of P(EAD) and their interpretation. The experimental uncertainty of $G_{Ks}$ is more impactful than uncertainties in its kinetic or voltage-dependent properties with respect to the uncertainty of P(EAD). Two other model-based risk metrics were studied, and results were compared to those obtained by calculating mean P(EAD). All approaches yield very similar predictions regarding the relative risk of 17 $I_{Ks}$ mutations, and this result holds despite the fact that these risk metrics and the models to which they are applied are very different. These three model-based risk metrics yield similar prediction performance; however, they all fail to predict

clinical risk for a significant number of the 17 studied LQTS1 mutations. This suggests

that experimental characterization of a number of LQTS1 mutations may be incomplete.

**Methods**

**Modified Walker Ventricular Myocyte Model**

This study uses a modified version of the Walker et al. stochastic ventricular myocyte

model [9] described in Jin et al. [10]. A subset of CRUs (5400 out of 25000) was used

for all simulations to accelerate the computation. β-adrenergic stimulation is simulated

to facilitate generation of cellular arrhythmias. This was done using the β-adrenergic

stimulation protocol described in Walker et al. [9]. The model is available in Github

(https://github.com/JHU-Winslow-Lab/EAD-paper-code.git).

**Long QT syndrome type 1 experimental data and IKs model.**

LQTS1 clinical and experimental electrophysiological data including 30-year cardiac

event rate for 17 mutations are obtained from Jons et al. 2011 [6]. The 30-year cardiac

event rate represents the percentage of mutation carriers that had their first cardiac event

in their first 30 years of life. Cardiac events include syncope, aborted cardiac arrest, and

sudden cardiac death. Clinical and experimental data from their study is summarized in

S1 Table. Five $I_{Ks}$-related parameters for each mutation are taken from from Jons et al.

Tables 2 and S1. In order to incorporate these five $I_{Ks}$-related parameters into our

myocyte model, we also incorporated their $I_{Ks}$ model into the Walker model. The $I_{Ks}$

model is described by the following equations:

$$
\begin{aligned}
I_{Ks} &= G_{Ks} \cdot G_{Ks\_sf} \cdot \chi_{Ks} \cdot (V - E_{Ks}) \\
\frac{d\chi_{Ks}(t)}{dt} &= \frac{\chi_{Ks}(\infty) - \chi_{Ks}(t)}{\tau_{xKs}} \\
\chi_{Ks}(\infty) &= \frac{1}{1 + e^{-\frac{V - 9.4 + \Delta V_{1/2}}{11.8 \cdot k\_sf}}} \\
a_1 &= 0.0000719 \frac{V}{1 + e^{-0.74V}} \cdot \frac{1}{\tau_{+}\_sf} \\
a_2 &= 0.000786 \frac{V + 40}{e^{0.103(V+40)} - 1} \cdot \frac{1}{\tau_{-}\_sf} \\
\tau_{xKs} &= \frac{1}{a_1 + a_2}
\end{aligned}
\tag{1}
$$

, where $\tau_{+}\_sf$, $\tau_{-}\_sf$, $\Delta V_{1/2}$, $k\_sf$, and $G_{Ks}\_sf$ are mutation-specific terms.

**Simulation protocol for early afterdepolarization modeling**

In the EAD studies, initial states of model state variables were the same in each simulation. These values were obtained in diastole after 10 beats at 1 Hz pacing during the β-adrenergic stimulation protocol. Each model simulation had a duration of 600ms. At 10ms, a 1-ms 10000 pA inward current was injected to trigger an action potential.

**Logistic regression model**

We recently developed a workflow to build a logistic regression model (LRM) on complex myocyte models [10]. It maps model parameters to the probability of a cellular arrhythmia event using the following Logistic equation:

$$
P(\text{event}) = \frac{1}{1 + \exp(-\underline{B}^{\mathrm{T}} \underline{P})}
\tag{2}
$$

, where $\underline{P}$ is a vector of features and $\underline{B}$ is a vector of weights. Features include model parameters and their products. See S1 Text for details description on the LRM method.

**Implementation of arrhythmia risk prediction metrics.**

Implementation details of $P_m(\text{EAD})_G$, AP morphology metric, and qNet are described in S2 Text. Models and results are available in Github (https://github.com/JHU-

516     Winslow-Lab/EAD-paper-code.git).

## References

1.     Cranefield PF, Aronson RS. Torsade de pointes and other pause-induced ventricular
tachycardias: the short-long-short sequence and early afterdepolarizations. Pacing Clin
Electrophysiol. 1988;11(6 Pt 1):670-8.
2.     Qu Z, Weiss JN. Mechanisms of ventricular arrhythmias: from molecular fluctuations to
electrical turbulence. Annu Rev Physiol. 2015;77:29-55.
3.     Rosen MR. Cellular electrophysiology of digitalis toxicity. J Am Coll Cardiol. 1985;5(5 Suppl
A):22A-34A.
4.     Winslow RL, Cortassa S, O'Rourke B, Hashambhoy YL, Rice JJ, Greenstein JL. Integrative
modeling of the cardiac ventricular myocyte. Wiley Interdiscip Rev Syst Biol Med. 2011;3(4):392-
413.
5.     Fink M, Noble PJ, Noble D. Ca(2)(+)-induced delayed afterdepolarizations are triggered by
dyadic subspace Ca2(2)(+) affirming that increasing SERCA reduces aftercontractions. Am J Physiol
Heart Circ Physiol. 2011;301(3):H921-35.
6.     Jons C, J OU, Moss AJ, Reumann M, Rice JJ, Goldenberg I, et al. Use of mutant-specific ion
channel characteristics for risk stratification of long QT syndrome patients. Sci Transl Med.
2011;3(76):76ra28.
7.     Fowler ED, Wang N, Hezzell M, Chanoit G, Hancox JC, Cannell MB. Arrhythmogenic late Ca2+
sparks in failing heart cells and their control by action potential configuration. Proceedings of the
National Academy of Sciences. 2020;117(5):2687-92.
8.     Tanskanen AJ, Greenstein JL, O'Rourke B, Winslow RL. The role of stochastic and modal gating
of cardiac L-type Ca2+ channels on early after-depolarizations. Biophysical Journal.
2005;88(1):85-95.
9.     Walker MA, Gurev V, Rice JJ, Greenstein JL, Winslow RL. Estimating the probabilities of rare
arrhythmic events in multiscale computational models of cardiac cells and tissue. PLoS Comput
Biol. 2017;13(11):e1005783.
10.    Jin Q, Greenstein JL, Winlsow RL. Estimating Ectopic Beat Probability with Simplified Statistical
Models that Account for Experimental Uncertainty. bioRxiv. 2021.
11.    Wang Q, Curran ME, Splawski I, Burn TC, Millholland JM, VanRaay TJ, et al. Positional cloning
of a novel potassium channel gene: KVLQT1 mutations cause cardiac arrhythmias. Nat Genet.
1996;12(1):17-23.
12.    Shimizu W, Antzelevitch C. Cellular basis for the ECG features of the LQT1 form of the long-
QT syndrome: effects of β-adrenergic agonists and antagonists and sodium channel blockers on
transmural dispersion of repolarization and torsade de pointes. Circulation. 1998;98(21):2314-22.
13.    Mikuni I, Torres CG, Bienengraeber MW, Kwok W-M. Partial restoration of the long QT
syndrome associated KCNQ1 A341V mutant by the KCNE1 β-subunit. Biochimica et Biophysica
Acta (BBA)-General Subjects. 2011;1810(12):1285-93.
14.    Schwartz PJ, Crotti L, Insolia R. Long-QT syndrome: from genetics to management. Circulation:
Arrhythmia and Electrophysiology. 2012;5(4):868-77.
15.    Hoefen R, Reumann M, Goldenberg I, Moss AJ, Jin O, Gu Y, et al. In silico cardiac risk
assessment in patients with long QT syndrome: type 1: clinical predictability of cardiac models.

Journal of the American College of Cardiology. 2012;60(21):2182-91.

16.	Guideline IHT. The non-clinical evaluation of the potential for delayed ventricular repolarization (Qt Interval Prolongation) by human pharmaceuticals. S7B (http://www ich org/products/guidelines/safety/article/safety-guidelines html). 2005.

17.	Blinova K, Dang Q, Millard D, Smith G, Pierson J, Guo L, et al. International multisite study of human-induced pluripotent stem cell-derived cardiomyocytes for drug proarrhythmic potential assessment. Cell reports. 2018;24(13):3582-92.

18.	Koren MJ, Crager MR, Sweeney M. Long-term safety of a novel antianginal agent in patients with severe chronic stable angina: the Ranolazine Open Label Experience (ROLE). Journal of the American College of Cardiology. 2007;49(10):1027-34.

19.	Chaitman BR, Pepine CJ, Parker JO, Skopal J, Chumakova G, Kuch J, et al. Effects of ranolazine with atenolol, amlodipine, or diltiazem on exercise tolerance and angina frequency in patients with severe chronic angina: a randomized controlled trial. Jama. 2004;291(3):309-16.

20.	Tzeis S, Andrikopoulos G. Antiarrhythmic properties of ranolazine–from bench to bedside. Expert opinion on investigational drugs. 2012;21(11):1733-41.

21.	Li Z, Dutta S, Sheng J, Tran PN, Wu W, Chang K, et al. Improving the In Silico Assessment of Proarrhythmia Risk by Combining hERG (Human Ether-a-go-go-Related Gene) Channel-Drug Binding Kinetics and Multichannel Pharmacology. Circ Arrhythm Electrophysiol. 2017;10(2):e004628.

22.	Lancaster MC, Sobie EA. Improved Prediction of Drug-Induced Torsades de Pointes Through Simulations of Dynamics and Machine Learning Algorithms. Clin Pharmacol Ther. 2016;100(4):371-9.

23.	Kernik DC, Yang PC, Kurokawa J, Wu JC, Clancy CE. A computational model of induced pluripotent stem-cell derived cardiomyocytes for high throughput risk stratification of KCNQ1 genetic variants. PLoS Comput Biol. 2020;16(8):e1008109.

24.	Hoefen R, Reumann M, Goldenberg I, Moss AJ, O-Uchi J, Gu Y, et al. In silico cardiac risk assessment in patients with long QT syndrome: type 1: clinical predictability of cardiac models. Journal of the American College of Cardiology. 2012;60(21):2182-91.

25.	Greenstein JL, Winslow RL. An integrative model of the cardiac ventricular myocyte incorporating local control of Ca2+ release. Biophys J. 2002;83(6):2918-45.

26.	Kernik DC, Morotti S, Wu H, Garg P, Duff HJ, Kurokawa J, et al. A computational model of induced pluripotent stem-cell derived cardiomyocytes incorporating experimental variability from multiple data sources. J Physiol. 2019;597(17):4533-64.

27.	Schwartz PJ, Priori SG, Spazzolini C, Moss AJ, Vincent GM, Napolitano C, et al. Genotype-phenotype correlation in the long-QT syndrome: gene-specific triggers for life-threatening arrhythmias. Circulation. 2001;103(1):89-95.

28.	Kernik DC, Morotti S, Wu H, Garg P, Duff HJ, Kurokawa J, et al. A computational model of induced pluripotent stem-cell derived cardiomyocytes incorporating experimental variability from multiple data sources. The Journal of physiology. 2019;597(17):4533-64.

29.	Flaim SN, Giles WR, McCulloch AD. Contributions of sustained I Na and I Kv43 to transmural heterogeneity of early repolarization and arrhythmogenesis in canine left ventricular myocytes. American Journal of Physiology-Heart and Circulatory Physiology. 2006;291(6):H2617-H29.

30.	Bers D. Excitation-contraction coupling and cardiac contractile force: Springer Science & Business Media; 2001.

31.  Anderson CL, Delisle BP, Anson BD, Kilby JA, Will ML, Tester DJ, et al. Most LQT2 mutations
reduce Kv11.1 (hERG) current by a class 2 (trafficking‑deficient) mechanism. Circulation.
2006;113(3):365‑73.
32.  Lacerda AE, Kuryshev YA, Chen Y, Renganathan M, Eng H, Danthi SJ, et al. Alfuzosin delays
cardiac repolarization by a novel mechanism. Journal of Pharmacology and Experimental
Therapeutics. 2008;324(2):427‑33.
33.  Kernik DC, Yang P‑C, Kurokawa J, Wu JC, Clancy CE. A computational model of induced
pluripotent stem‑cell derived cardiomyocytes for high throughput risk stratification of KCNQ1
genetic variants. PLoS computational biology. 2020;16(8):e1008109.
34.  Dutta S, Chang KC, Beattie KA, Sheng J, Tran PN, Wu WW, et al. Optimization of an in silico
cardiac cell model for proarrhythmia risk assessment. Frontiers in Physiology. 2017;8:616.
35.  Parikh J, Di Achille P, Kozloski J, Gurev V. Global sensitivity analysis of ventricular myocyte
model‑derived metrics for proarrhythmic risk assessment. Frontiers in pharmacology.
2019;10:1054.
36.  Schwartz PJ, Priori SG, Spazzolini C, Moss AJ, Vincent GM, Napolitano C, et al. Genotype‑
phenotype correlation in the long‑QT syndrome: gene‑specific triggers for life‑threatening
arrhythmias. Circulation. 2001;103(1):89‑95.
37.  Xie Y, Sato D, Garfinkel A, Qu Z, Weiss JN. So little source, so much sink: requirements for
afterdepolarizations to propagate in tissue. Biophysical journal. 2010;99(5):1408‑15.

## Supporting information

**S1 Fig. Relationship between 5 IKs‑related parameters and P(EAD).** (A) vary the

$G_{Ks}$_sf while fixed other four parameters at wild type value ($\tau_{+}$_sf = 1, $\tau_{-}$_sf = 1, $\Delta V_{1/2}$

= 0, and k_sf = 1). Similarly, vary one parameters: $\tau_{+}$_sf (B), $\tau_{-}$_sf (C), $\Delta V_{1/2}$ (D) or

k_sf (E) and fix other parameters at wild type except that $G_{Ks}$_sf = 0.5.

**S2 Fig. Uncertainty analysis for individual features underlying LQTS1 mutations.**

PDFs of $\underline{B}^T\underline{P}$ (red) are shown for two mutations (*G314S*: solid line and *Y315C*: square markers). $\underline{B}^T\underline{P}$ is the weighted summation of 16 $I_{Ks}$ features (5 parameters + 11 parameter-derived quadratic features) for each mutation. The MC curve (blue) relates $\underline{B}^T\underline{P}$ to P(EAD). Single feature uncertainty: (A) $\tau_{+}$_sf, (B) $\tau_{-}$_sf, (C) $\Delta V_{1/2}$, (D) k_sf, or (E) $G_{Ks}$_sf is sampled from an experimentally based distribution while other parameters are assumed fixed at their mean.

**S3 Fig. Comparison between model-based risk metrics.** The comparison between

$P_m$(EAD) (at x axis) and other three metrics (at y axis) on 17 mutations: (A) AP

morphology metric, (B) TRP metric, (C) $P_m$(EAD)$_G$ and (D) qNet. Linear regression

between two compared approaches is performed and $R^2$ is reported.

| | D611Y | Y315C | W305S | G269S | G168R | A341E | R591H | T312I | S225L | L266P | S349W | Y184S | R594Q | R243C | V254M | G314S | A341V |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| D611Y | | | | | | | | | | | | | | | | | |
| Y315C | 0 | | | | | | | | | | | | | | | | |
| W305S | 0 | 0 | | | | | | | | | | | | | | | |
| G269S | 0 | 0 | 0 | | | | | | | | | | | | | | |
| G168R | 0 | 0 | 0 | 0 | | | | | | | | | | | | | |
| A341E | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | | | |
| R591H | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | | |
| T312I | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | |
| S225L | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | |
| L266P | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | |
| S349W | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | |
| Y184S | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | |
| R594Q | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | |
| R243C | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | |
| V254M | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | | | |
| G314S | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | | |
| A341V | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | |

**S4 Fig. Fisher exact test on 17 mutations.** The fisher exact test is performed on every

mutation pairs to test if the difference of clinical risk (30-year cardiac event rate) is

statistically different. 1 represents that the mutation pair has significant clinical risk

difference. 0 means that clinical risk difference is not significant. On x axis, from left

to right (and on y axis from top to bottom), mutations are ordered the clinical risk from

least to most.

**S5 Fig. Pairwise prediction in all mutation pairs.** Similar figure as Fig 4 except that

all pairs are considered in this analysis.

**S6 Fig. Ranking comparison across 5 metric – model pairs.** Similar figure as Fig 3

except that the $r_{pred}$ from $P_m(EAD)_G$ and qNet are included.

**S1 Table. Long QT syndrome type 1 clinical data and cellular experimental data**

**obtained from Jons et al., n: number of patients.**

| | | Clinical outcome | $\tau_+\_sf =$ $\tau_+$ (mut) / $\tau_+$ (WT) | | $\tau_-\_sf =$ $\tau_-$ (mut) / $\tau_-$ (WT) | |
|---|---|---|---|---|---|---|
| | n | 30-year cardiac event rate | Mean | SE | Mean | SE |
| *Wild type* | 48 | 0.0865 | 1.000 | 0.032 | 1.000 | 0.029 |
| *G168R* | 68 | 0.2560 | 1.301 | 0.043 | 0.882 | 0.039 |
| *Y184S* | 14 | 0.4398 | 1.226 | 0.032 | 1.000 | 0.029 |
| *S225L* | 14 | 0.3589 | 1.430 | 0.054 | 0.725 | 0.029 |
| *R243C* | 13 | 0.5624 | 1.269 | 0.032 | 0.775 | 0.020 |
| *V254M* | 62 | 0.7418 | 1.957 | 0.086 | 1.108 | 0.039 |
| *L266P* | 24 | 0.3698 | 1.344 | 0.043 | 0.814 | 0.029 |
| *G269S* | 41 | 0.1926 | 1.247 | 0.032 | 0.667 | 0.029 |
| *W305S* | 16 | 0.1838 | 1.280 | 0.065 | 0.696 | 0.029 |
| *T312I* | 17 | 0.3523 | 1.398 | 0.054 | 0.745 | 0.029 |
| *G314S* | 19 | 0.8009 | 1.344 | 0.065 | 0.882 | 0.029 |
| *Y315C* | 10 | 0.0895 | 1.108 | 0.043 | 0.765 | 0.029 |
| *A341E* | 10 | 0.2976 | 1.237 | 0.065 | 0.912 | 0.029 |
| *A341V* | 21 | 0.8797 | 1.301 | 0.043 | 0.765 | 0.029 |
| *S349W* | 15 | 0.3961 | 1.409 | 0.054 | 0.980 | 0.039 |
| *R591H* | 19 | 0.3063 | 1.043 | 0.032 | 0.971 | 0.020 |
| *R591Q* | 14 | 0.5077 | 1.011 | 0.043 | 0.951 | 0.029 |
| *D611Y* | 10 | 0.0088 | 0.935 | 0.065 | 0.931 | 0.069 |
| | $\Delta V_{1/2} =$ $V_{1/2}$ (mut) - $V_{1/2}$ (WT) | | $k\_sf =$ $k$ (mut) / $k$ (WT) | | $G_{Ks}\_sf =$ $G_{Ks}$ (mut) / $G_{Ks}$ (WT) | |
| | Mean | SE | Mean | SE | Mean | SE |
| *Wild type* | 0.00 | 0.77 | 1.000 | 0.020 | 1.000 | 0.042 |
| *G168R* | 3.25 | 0.89 | 1.010 | 0.030 | 0.417 | 0.033 |
| *Y184S* | 2.22 | 0.93 | 1.030 | 0.020 | 0.683 | 0.058 |
| *S225L* | 9.51 | 0.86 | 1.030 | 0.020 | 0.725 | 0.050 |
| *R243C* | 6.74 | 0.81 | 1.051 | 0.818 | 0.508 | 0.033 |
| *V254M* | 23.31 | 1.31 | 1.101 | 0.020 | 0.758 | 0.058 |
| *L266P* | 3.75 | 1.60 | 1.010 | 0.020 | 0.325 | 0.042 |
| *G269S* | 6.63 | 0.79 | 1.061 | 0.030 | 0.550 | 0.050 |
| *W305S* | 4.56 | 1.16 | 0.939 | 0.030 | 0.492 | 0.050 |
| *T312I* | 3.40 | 0.89 | 0.848 | 0.040 | 0.333 | 0.050 |
| *G314S* | 2.86 | 1.69 | 1.030 | 0.091 | 0.258 | 0.025 |
| *Y315C* | -1.41 | 0.81 | 1.000 | 0.030 | 0.500 | 0.033 |
| *A341E* | 3.10 | 1.17 | 1.061 | 0.051 | 0.500 | 0.042 |
| *A341V* | 1.78 | 0.83 | 0.970 | 0.030 | 0.842 | 0.100 |
| *S349W* | 18.28 | 1.54 | 1.273 | 0.020 | 1.250 | 0.058 |
| *R591H* | -0.46 | 0.91 | 1.040 | 0.020 | 0.933 | 0.058 |
| *R591Q* | 0.83 | 0.73 | 1.051 | 0.030 | 0.817 | 0.050 |
| *D611Y* | 0.11 | 0.92 | 1.051 | 0.030 | 1.125 | 0.075 |

656 **S2 Table. Five approaches prediction and ranking on 17 mutations**

| | Clinical data | | $P_m(EAD)$ | | $P_m(EAD)_G$ | |
|---|---|---|---|---|---|---|
| | risk | ranking | metric | ranking | metric | ranking |
| *D611Y* | 0.009 | 1 | 0.025 | 2 | 0.072 | 1 |
| *Y315C* | 0.090 | 2 | 0.260 | 8 | 0.573 | 8 |
| *W305S* | 0.184 | 3 | 0.404 | 11 | 0.625 | 10 |
| *G269S* | 0.193 | 4 | 0.347 | 9 | 0.604 | 9 |
| *G168R* | 0.256 | 5 | 0.551 | 14 | 0.819 | 14 |
| *A341E* | 0.298 | 6 | 0.383 | 10 | 0.651 | 11 |
| *R591H* | 0.306 | 7 | 0.033 | 3 | 0.120 | 2 |
| *T312I* | 0.352 | 8 | 0.664 | 15 | 0.850 | 15 |
| *S225L* | 0.359 | 9 | 0.199 | 7 | 0.488 | 7 |
| *L266P* | 0.370 | 10 | 0.699 | 16 | 0.873 | 16 |
| *S349W* | 0.396 | 11 | 0.024 | 1 | 0.143 | 3 |
| *Y184S* | 0.440 | 12 | 0.159 | 5 | 0.404 | 6 |
| *R594Q* | 0.508 | 13 | 0.051 | 4 | 0.180 | 4 |
| *R243C* | 0.562 | 14 | 0.548 | 13 | 0.806 | 13 |
| *V254M* | 0.742 | 15 | 0.436 | 12 | 0.759 | 12 |
| *G314S* | 0.801 | 16 | 0.900 | 17 | 0.962 | 17 |
| *A341V* | 0.880 | 17 | 0.172 | 6 | 0.304 | 5 |
| | AP morphology | | TRP | | Qnet | |
| | metric | ranking | metric | ranking | metric | ranking |
| *D611Y* | 0.006 | 2 | -2.76 | 1 | 75.162 | 1 |
| *Y315C* | 2.313 | 8 | 19.66 | 6 | 74.460 | 4 |
| *W305S* | 3.731 | 13 | 29.41 | 11 | 73.403 | 8 |
| *G269S* | 2.883 | 10 | 26.34 | 9 | 73.212 | 10 |
| *G168R* | 3.990 | 14 | 33.43 | 13 | 73.321 | 9 |
| *A341E* | 2.814 | 9 | 27.93 | 10 | 73.508 | 6 |
| *R591H* | 0.000 | 1 | 6.33 | 2 | 74.631 | 3 |
| *T312I* | 5.666 | 16 | 37.62 | 14 | 73.190 | 11 |
| *S225L* | 1.893 | 7 | 22.05 | 7 | 72.401 | 15 |
| *L266P* | 5.289 | 15 | 38.36 | 15 | 73.148 | 13 |
| *S349W* | 0.024 | 3 | 15.5 | 4 | 71.428 | 16 |
| *Y184S* | 1.010 | 6 | 17.55 | 5 | 73.638 | 5 |
| *R594Q* | 0.133 | 4 | 12.44 | 3 | 74.688 | 2 |
| *R243C* | 3.161 | 11 | 30.55 | 12 | 73.119 | 14 |
| *V254M* | 3.620 | 12 | 43.92 | 16 | 70.040 | 17 |
| *G314S* | 5.811 | 17 | 46.89 | 17 | 73.183 | 12 |
| *A341V* | 0.308 | 5 | 24.56 | 8 | 73.490 | 7 |

658 **S3 Table. Parameters chosen for P(EAD) prediction.**

| parameters | Lower bound | Upper bound |
|---|---|---|
| $\tau_{+}\_sf$ | 0.2903 | 2.8510 |
| $\tau_{-}\_sf$ | 0.2051 | 1.6577 |
| $\Delta V_{1/2}$ | -11.9267 | 36.4100 |
| $k\_sf$ | 0 | 10.8687 |
| $G_{Ks}\_sf$ | 0 | 1.9044 |

| | D611Y | Y315C | W305S | G269S | G168R | A341E | R591H | T312I | S225L | L266P | S349W | Y184S | R594Q | R243C | V254M | G314S | A341V |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| D611Y | | | | | | | | | | | | | | | | | |
| Y315C | 0 | | | | | | | | | | | | | | | | |
| W305S | 0 | 0 | | | | | | | | | | | | | | | |
| G269S | 0 | 0 | 0 | | | | | | | | | | | | | | |
| G168R | 0 | 0 | 0 | 0 | | | | | | | | | | | | | |
| A341E | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | | | |
| R591H | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | | |
| T312I | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | |
| S225L | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | |
| L266P | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | |
| S349W | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | |
| Y184S | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | |
| R594Q | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | |
| R243C | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | |
| V254M | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | | | |
| G314S | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | | |
| A341V | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | |

**a** $P_m$(EAD)

**b** AP morphology metric

**c** TRP metric