Title: FR-Match: A non-parametric multivariate statistical test for matching gene expression clusters from single cell RNA sequencing experiments

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Abstract

Single cell/nucleus RNA sequencing (scRNAseq) provides an unbiased transcriptomic profiling of individual cells, and is emerging as an essential tool to unravel the phenotypic heterogeneity of cells in complex biological systems. While computational methods for scRNAseq cell type clustering have advanced, the ability to integrate datasets to identify common and novel cell types across experiments remains a challenge. Here, we introduce a cluster-to-cluster cell type matching algorithm – FR-Match – that incorporates shared information among cells to determine whether two cell type clusters are from the same underlying multivariate gene expression distribution. In validation studies using simulated data, FR-Match proved to be a stringent method that produces fewer erroneous matches of distinct cell subtypes compared to existing methods. FR-Match also has the unique ability to identify novel cell phenotypes in new datasets. When integrating two real datasets from specimens isolated from overlapping human brain regions (cortical layer one versus full thickness middle temporal gyrus), FR-Match precisely preserved the laminar characteristics of matched cell type clusters that reflect distinct neuroanatomical functions. Open-source software is available at https://github.com/JCVenterInstitute/FRmatch.

1 Introduction

Global collaborations, including the Human Cell Atlas[1] (HCA) and the NIH BRAIN Initiative[2], are

making rapid advances in the application of single cell/nucleus RNA sequencing (scRNAseq) to

characterize the transcriptional profiles of cells in healthy and diseased tissues as the basis for

understanding fundamental cellular processes and for diagnosing, monitoring, and treating

human diseases. The standard workflow for processing and analysis of scRNAseq data

includes steps for quality control to remove poor quality data based on quality metrics[3-5],

sequence alignment to reference genomes/transcriptomes[6-8], and transcript assembly and

quantification[8,9] to produce a gene expression profile (transcriptome) for each individual cell. In

most cases, these expression profiles are then clustered[10-13] to group together cells with similar

gene expression phenotypes, representing either discrete cell types or distinct cell states. Once

these cell phenotype clusters are defined, it is also useful to identify sensitive and specific

marker genes for each cell phenotype cluster that could be used as targets for quantitative PCR,

probes for *in situ* hybridization assays, and other purposes (e.g. semantic cell type

representation where biomarkers can be used for defining cell types based on their necessary

and sufficient characteristics[14,15]).

A major challenge emerging from the broad application of these scRNAseq technologies is the

ability to compare transcriptional profiles across studies. In some cases, basic normalization[16,17]

or batch correction[18,19] methods have been used to combine multiple scRNAseq datasets with

limited success. Recently, several computational methods have been developed to address this

challenge more comprehensively[20-25]. General steps in these methods include feature

selection/dimensionality reduction and quantitative learning for matching. Scmap[20] is a method

that performs cell-to-cell (scmapCell) and cell-to-cluster (scmapCluster) matchings. The feature

selection step is unsupervised and based on a combination of expression levels and dropout

rates, pooling genes from all clusters in the reference dataset. Matching is based on agreement

of nearest neighbor searching using multiple similarity measures. Seurat[21,22] provides a cell-to-

cell matching method within its suite of scRNAseq analysis tools. Feature selection is

unsupervised and selects highly variable features in the reference dataset to define the high-

dimensional space. Both query and reference cells are aligned in a search space projected by

PCA-based dimensionality reduction and canonical correlation analysis, to transfer cluster

labels through "anchors". Among many others[23-25], these methods have focused on individual

cell level strategies when comparing a query dataset to a reference dataset, not relying on

clustering results to guide supervised feature selection or cluster-level matching.

Here, we present a supervised cell phenotype matching strategy, called FR-Match, for cluster-

to-cluster cell transcriptome integration across scRNAseq experiments. Utilizing *a priori* learned

cluster labels and computationally- or experimentally-derived marker genes, FR-Match uses the

Friedman-Rafsky statistical test[26,27] (FR test) to learn the multivariate distributional concordance

between query and reference data clusters in a graphical model. In this manuscript, we first

illustrate the matching properties of FR test in this scRNAseq adaptation using thorough

simulation and validation studies in comparison with other popular matching methods. We then

use FR-Match to match brain cell types defined in the full thickness of human middle temporal

gyrus (MTG) neocortex with cell types defined in a Layer 1 dissection of MTG using public

datasets from the Cell Types Database of the Allen Brain Map [https://portal.brain-

map.org/atlases-and-data/rnaseq]. We also report the cell types that are consistently matched

between the two brain regions using multiple matching methods. An R-based implementation,

user guide, and ShinyApp for FR-Match are available in the open-source GitHub repository

[https://github.com/JCVenterInstitute/FRmatch].

Results

FR-Match: cluster-to-cluster mapping of cell type clusters

FR-Match, is a novel application of the Friedman-Rafsky test[26,27], a non-parametric statistical

test for multivariate data comparison, tailored for single cell clustering results. FR-Match takes

clustered gene expression matrices from query and reference experiments and returns the FR

statistic with p-value as evidence that the query and reference cell clusters being compared are

matched or not, i.e. they share a common gene expression phenotype. The general steps of

FR-Match (Fig. 1a) include: i) select informative marker genes using, for example, the NS-

Forest marker gene selection algorithm[14]; ii) construct minimum spanning trees for each pair of

query and reference clusters (different colors); iii) remove all edges that connect a node from

the query cluster with a node from the reference cluster, and iv) calculate FR statistics and p-

values by counting the number of subgraphs remaining in the minimum spanning tree plots.

Intuitively, the larger the FR statistic, the stronger the evidence that the cell clusters being

compared represent the same cell transcriptional phenotype.

Supervised marker gene selection provides unique cell type clusters "barcodes"

We adopted the NS-Forest algorithm[14] v2.0 (available at

https://github.com/JCVenterInstitute/NSForest) to select informative marker genes for a given

cell type cluster. Applying NS-Forest feature selection to the cortical Layer 1 and full thickness

MTG datasets produced a collection of 34 and 157 marker genes that, in combination, can

distinguish the 16 cortical Layer 1[28] and 75 full MTG[29] cell type clusters, respectively. These

markers include well known neuronal marker genes like *SATB2*, *LHX6*, *VIP*, *NDNF*, *NTNG1*, etc.

(Supplementary Fig. 1). The selected marker genes display on-off binary expression patterns

producing, in combination, a unique gene expression "barcode" for each cell cluster (Fig. 1b). In

addition to producing marker genes for each of the individual cell type clusters, this composite

barcode serves as an effective dimensionality reduction strategy that captures gene features

that are informative for every cell type cluster. The collection of informative marker genes

effectively creates an essential subspace that reflects the composite cell cluster phenotype

structure in the single cell gene expression data. Thus, supervised feature selection by NS-

Forest was used as the dimensionality reduction step for the FR-Match method in this study.

Although NS-Forest was used for marker gene selection here, FR-Match is compatible with any

feature selection/dimensionality reduction approach that selects informative cluster classification

features.

Matching performance in cross-validation and simulation studies

To assess the performance of FR-Match in comparison with other matching methods, we

generated cross-validation datasets utilizing the cortical Layer 1 data and its known 15 cell type

clusters for validation studies (excluding the smallest cluster in the original studies with too few

cells). Matching was performed using six implementations of the three core methods: FR-Match

(using NS-Forest genes), FR-Match incorporating p-value adjustment (FR-Match adj.), scmap

(scmapCluster) with default gene selection (500 genes based on dropout proportions), scmap

with NS-Forest marker genes (scmap+NSF), scmap with extended NS-Forest marker genes

(scmap+NSF.ext) (see Methods section), and Seurat with default gene selection (top 2000

highly variable genes). (Seurat with NS-Forest marker genes was not reported since the results

were similar to the results obtained using default marker genes.)

<u>**Cross-validation assessment of 1-to-1 positive matches**</u>

In the two-fold cross-validation study, half of the cells serve as the query dataset and the other

half as the reference dataset. Exactly one 1-to-1 true positive match should be identified for

each cluster. Figure 2a displays the average matching rate over the cross-validation iterations,

where true positives are expected to lay along the diagonal. Four implementations, FR-Match,

FR-Match adj., scmap+NSF.ext, and Seurat had excellent performance with 0.93~1 true

positive rates (TPR) calculated as the grand average of the diagonal entries. Scmap using its

default gene selection approach performed sub-optimally, especially for glial cell types. This is

likely due to the fact that informative marker genes for these cell types were not selected using

the dropout rate-based feature selection criterion (Supplementary Fig. 2). However, using NS-

Forest marker genes (scmap+NSF) instead of its default genes resulted in a significant

improvement in scmap performance, suggesting that supervised feature selection is

advantageous for cell type matching in general. FR-Match implementations had median

matching accuracies approaching 0.98 and above, while the next tier performers,

scmap+NSF.ext and Seurat, had median accuracies around 0.95 (Fig. 2b). Sensitivity and

specificity metrics further break down the accuracy measure and indicate the balance between

the diagonal (true positive, a.k.a. sensitivity) and off-diagonal (true negative, a.k.a. specificity)

matching performance. FR-Match after p-value adjustment is the only algorithm that identified

all positive matches. Most methods had very high specificities, whereas FR-Match adj. had

somewhat lower specificity due to slightly more false positives.

Cross-validation assessment of 1-to-0 negative matches

Leave-*K*-cluster-out cross-validation was used to test the performance of these methods under

circumstances where one or more cell phenotypes is missing from the reference datasets, i.e. a

situation where a novel cell type has been discovered. The left-out cluster(s) should have 1-to-0

match(s) and should be unassigned. While FR-Match implementations clearly identified the left-

out cluster as unassigned, other methods produced inappropriate matching when query cell

types were missing from the reference dataset (Fig. 3). Figure 3a shows results for when the i5

cluster was left out; Supplementary Figs. 3-8 show results for when other cluster were left-out in

turn. Both FR-Match implementations easily identified the true negative match and correctly

labeled the query i5 cluster as unassigned. Other methods partially or primarily mis-matched the

query cluster (i5) to a similar yet distinct cluster (i1), as seen in the UMAP embedding where the

query i5 nuclei are nearest neighbors to the reference i1 nuclei (Supplementary Fig. 9). The

accuracy measure for leave-1-cluster-out cross-validation again suggests that the FR-Match

method is the best performer with median accuracies approaching 0.99 (Fig. 3b). Furthermore,

as we removed more and more reference clusters, the FR-Match method showed robust

precision-recall curve that consistently outperformed default implementations of scmap and

Seurat in ROC analysis (Fig. 3c). Seurat's curve deteriorated because its current

implementation lacks an option for unassigned matches; therefore, all cells in the query dataset

were forced to map somewhere in the reference dataset. Interestingly, scmap implementations

with NS-Forest selected features also had robust precision-recall curves with respect to the

increasing number of true negatives.

The leave-K-cluster-out cross-validation has important implications for the capability of each

matching method to detect novel cell types in new data sets that are not present in the

reference datasets when integrating single cell experiments. In this important use case, the FR-

Match method exhibits desirable properties for novel cell phenotype discovery.

Simulation of under- and over-partitioning during upstream clustering

Accurate cell type determination from scRNAseq analysis is dependent on accurate partitioning

of the cellular transcriptomes into clusters based on their similarity. Existing neuroscientific

knowledge[28] suggests that the 15 cortical Layer 1 cell clusters are the current "optimal"

clustering of the human brain upper cortical layer scRNAseq data. By combining and splitting

these optimal cell type clusters, we simulated under- and over-partitioning scenarios of the

upstream clustering analysis. Figure 4a summarizes five cluster partitions ranging from 3 to 18

clusters with F-measure scores indicating the classification power of partition-specific marker

genes. The "Top nodes" under-partitioning combines clusters into the three top-level broad cell

type classes: inhibitory neurons, excitatory neurons, and non-neuronal cells, producing well

known GABAergic, glutamatergic, and neuroglia markers with high F-measure score. The "Mid

nodes" under-partitioning combines three groups of closely related GABAergic clusters – i1 + i5,

i3 + i4, and i6 + i8 + i9 – resulting in 11 clusters. Over-partitioning of either one (e1) or three (i1,

i2, and i3) clusters was performed by running k-means clustering with k = 2 independently for

each cluster to simulate real over-partitioning scenarios.

It is important to note that over- and under-partitioning will also have an effect on the gene

selection step; it would be predicted that marker gene selection algorithms would have difficulty

finding maker genes specific for over-partitioned clusters, which would be reflected in the drop

in F-measure scores. Indeed, particularly low F-measure scores may be a good indication of

cluster over-partitioning. Figure 4b describes the expected effects on marker gene identification

and FR-Match performance after p-value adjustment when clusters are under-, optimally-, and

over-partitioned. The types of marker genes that would be selected with different reference

cluster partitioning scenarios would impact their ability to effectively drive cluster matching.

Supplementary Figs. 10-15 show the matching results of all considered matching methods in

various partitioning scenarios. The FR-Match and Seurat methods showed good quality and

expected matching results in most partitioning scenarios; scmap had the same problem with the

unmatched glial clusters. Seurat showed excellent performance when reference clusters were

under-partitioned, but poor performance when query clusters were under-partitioned. Overall,

the FR-Match method had stable matching performance in the cluster partitioning simulations.

Indeed, 1-to-many and many-to-1 matching results using FR-Match could possibly indicate

under- or over-partitioning of the upstream clustering step in scRNAseq data analysis.

Cell type mapping between cortical Layer 1 and full MTG

We next extended the validation testing to a more realistic real-world scenario where a new

dataset has been generated in the same tissue region using slightly different experimental and

computational platforms. We tested FR-Match with p-value adjustment using two single nucleus

RNA sequencing datasets from overlapping human brain regions – the single apical layer of the

MTG cerebral cortex (cortical Layer 1), in which 16 discrete cell types were identified[28], and the

full laminar depth of the MTG cerebral cortex, in which 75 distinct cell types were identified[29].

Matching results were assessed from two perspectives: i) agreement with prior knowledge such

as layer metadata from the design of these experiments[28,29], and ii) agreement with other

matching methods. Since these datasets targeted the same cortical region with overlapping

laminar sampling, we expect that matching algorithm should find 1-to-1 matches of each cell

types in the cortical Layer 1 data to one cell type in layers 1-2 from the full MTG data. The final

matching results were concluded from two matching directions: Layer 1 query to MTG reference

with MTG markers, and MTG query to Layer 1 reference with Layer 1 markers. The two-way

matching approach was applied to all comparable matching algorithms.

FR-Match uniquely maps cell types reflecting the overlapping anatomic regions

Using FR-Match, we mapped each of the 13 Layer 1 cell types uniquely to one MTG cell type

(Fig. 5a), i.e. 1-to-1 two-way matches. These matches precisely reflect the overlapping

anatomic regions in these two independent experiments in that the matched MTG cell types all

have an "L1" layer indicator in their nomenclature. The one exception for the Layer 1 e1 cluster

likely reflects the incidental capture of upper cortical layer 2 excitatory neurons in the original

Layer 1 experiment[28]. And while most of the *SST* cell subtypes are located in deeper cortical

layers, FR-Match specifically selected the small number of L1 *SST* clusters as top matches. The

same was true for *VIP* and *LAMP5* cell subtypes. The minimum spanning tree plots produced by

FR-Match provide a clear visualization of matched and unmatched cell clusters (Fig. 5b).

To validate further, we compared the matching results to the hierarchical taxonomy of MTG cell

types[29], which reflects cell type relatedness (left side of Fig. 5a). First, the block of one-way

matches in Box A precisely corresponds to a specific sub-clade of *VIP*-expressing cells with

close lineage relationships, suggesting that one-way FR-Match results are evidence of closely

related cell types. Second, FR-Match correctly identified excitatory neurons that were

incidentally captured from upper Layer 2 in the cortical Layer 1 experiment in Box B,

corresponding to L2/3 excitatory neurons in the full MTG dataset. Third, Box C suggests under-

partitioning of the Layer 1 astrocyte cluster as multiple two-way matches were found for the

same cluster.

Directional one-way matching results are shown in Supplementary Fig. 16. Though different

matching patterns are observed from each direction, they reflect the fact that these datasets are

measuring different cell types. There are some cases where the difference might be due to the

cell complexity in the datasets, e.g. the *VIP* or *SST* types, and this might be leading to the

dynamic range and skewness of p-value distributions for each query cluster.

Cell type mapping using other existing approaches

In mapping cell types between cortical Layer 1 and the full MTG, both FR-Match and Seurat

produced similar unique two-way matches (Fig. 6). Examining all matching results and all

matching algorithms, FR-Match produced the most "conservative" mapping of cell types. The

other matching algorithms produced matching results that had more sparsely-distributed *VIP*

types (Box A), and were not laminar specific (Box B). Among all approaches, glial cell types

were mapped somewhat differently (Box C), probably due to their overall lower sampling and

distinct phenotypes compared to the majority of GABAergic and glutamatergic neurons.

FR-Match shows three advantages over the alternative methods. First, by using supervised

feature selection for each cell type, major and minor cell populations are equally represented in

the reduced-dimensional space for cell type matching. This strategy would also benefit other

matching methods with sub-optimal feature selection/dimensionality reduction. Second, FR-

Match clearly excludes the matching of cell types that are only present in one of the datasets.

Third, FR-Match allows one-to-multiple and unassigned matches, which allows for detecting

potential cluster partitioning issues and the discovery of novel cell types.

The other existing cell-level matching approaches naturally provide the probabilistic cluster-level

matching of cell types as the percentage of matched cells in query cluster (Supplementary Figs.

17-20); a deterministic cluster-level match would depend on the selection of an *ad-hoc* cutoff of

the probabilistic matching. Thus, deterministic cell type mapping or discovery of novel cell types

would be difficult as i) individual cells may be alike in the same broad cell class even if the

specific cell type may not be present in the reference dataset, and ii) the probabilistic cutoff may

be subjective. Therefore, both scmap and Seurat identified many more non-specific one-way

matches than FR-Match, which uses an objective p-value cutoff.

Combining all results, we finally report 15 high-confidence ensemble matches between Layer 1

and full MTG cell types in Supplementary Table 1.

Discussion

FR-Match offers a cluster-level approach for mapping cell phenotypes identified in scRNAseq

experiments. It extends the current cell-level matching algorithms by: i) borrowing information

from all the cells in the same cluster using a statistical test that provides both probabilistic

matching in p-values and objective p-value thresholds for deterministic matching, and ii)

providing simple visualization of cell type data clouds in the minimum spanning tree graphical

representation. Matching results of FR-Match are relatively conservative yielding highly specific

matches, which can confirm cell type equivalence, lead to novel cell type discovery, and

diagnose upstream clustering problems. Among many other scRNAseq data integration

strategies, this approach combines informative feature selection and cluster-level integration of

the NS-Forest and FR-Match software suites, producing intuitive results with high interpretability,

including useful intermediate results such as binary marker genes and minimum spanning tree

graphs for users to monitor and gain meaningful insights from the mapping solutions.

Based on the computational and statistical investigation of both simulated and real datasets, we

conclude that: i) the FR-Match and Seurat methods show excellent performance in mapping

neuronal and glial cell types using snRNAseq data from human brain; and ii) supervised feature

selection, such as the NS-Forest algorithm, appears to produce excellent marker gene

combinations that can be used as an effective feature selection/dimensionality reduction

technique for cell type mapping with multiple methods, including FR-Match and scmap.

One of the biggest challenges in scRNAseq alignment at the moment seems to be the proper

assignment of cells from a cell type found in only one dataset. These cells are often matched to

a closely related cell type in a second dataset. In this regard, FR-Match appears to be superior

in being able to determine which cell types from two datasets are *not* matched, for novel cell

type discovery.

For all compared methods in this study, it's interesting to note that under-partitioning the query

clusters leads to degraded performance, except if the reference clusters are also under-

partitioned. This suggests that a useful strategy would be to map to reference types in a

hierarchical manner by first mapping to broad classes of references types and then moving

down the tree to finer types until ambiguous matches appear.

Automated cell type integration of independent scRNAseq datasets remains challenging.

Creating an unbiased, high-resolution and comprehensive cell type reference would be a critical

task for the whole single cell research community. Consensus mapping schemes that survey

both cell-level and cluster-level matchings will be useful for establishing such a reference data

atlas. We believe that final mapping of the brain cell types agreed upon by the type of bi-

directionally and multi-level matchings reported here represents the best-practice for

computational cell type mapping, requiring minimal expert intervention.

Single cell evaluation is a fast-evolving field. Although not explored here, we expect FR-Match

to be applicable to cross-platform, cross-specimen, cross-anatomy, and cross-species matching

of scRNAseq clustered data. The effect of dropouts and the dynamic range of single cell

sequencing data from protocols other than the Smart-seq[30] protocol stand out as key challenges

to be overcome. To address these challenges, we are now developing add-on features to the

core FR-Match algorithm, including imputation techniques[31] for the relatively high dropout rates

in 10X Genomics droplet-based protocols[32], and moment-based normalization options[33] for the

discrete and dispersed values produced in single cell spatial *in-situ* hybridization protocols[34-36].

While these emerging technologies will produce more complicated data integration challenges,

the adaptation of methods like FR-Match are poised to play an essential role in the broad

integration of scRNAseq cell phenotyping experiments.

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Author contributions

Y.Z. and R.H.S. designed the study, conceived the statistical model, and wrote the manuscript.

Y.Z. and B.D.A. developed the software suites. Y.Z. and B.D.A applied the software to real data

analysis. Y.Z., B.D.A, T.B., J.A.M., and R.H.S. interpreted the real data analysis. R.H., T.B.,

J.A.M., R.H.S., and E.S.L. performed the single nucleus RNA sequencing experiments used.

R.H.S. and E.S.L. supervised the work.

 Figures

a *I. Dimensionality reduction*

II. Cluster-to-cluster matching

b

Figure 1. FR-Match schematic and marker gene "barcodes". (a) FR-Match cluster-to-cluster

matching schematic diagram. Input data: query/new and reference datasets, each with cell-by-

gene expression matrix and cell cluster membership labels. Step I: dimensionality reduction by

selecting expression data of reference cell type marker genes from the query dataset. Here, we

use the NS-Forest marker genes selected for the reference cell types. Step II: Cluster-to-cluster

matching through the Friedman-Rafsky (FR) test. From left to right: multivariate data points of

cell transcriptional profiles (colored by cell cluster labels) in a reduced dimensional (reference

marker gene expression) space; construct a complete graph by connecting each pair of vertices

(i.e. cells); find the minimum spanning tree that connects all vertices with minimal summed edge

lengths; remove the edges that connect vertices from different clusters; count the number of

disjoint subgraphs, termed "multivariate runs" and denoted as R; calculate the FR statistic W,

which has asymptotically a standard normal distribution. **(b)** "Barcodes" of the cortical Layer 1

NS-Forest marker genes in four Layer 1 clusters. Heatmaps show marker gene expression

levels of 30 randomly selected cells in each cell cluster. The "Marker" column indicates if the

gene is a marker gene of the cluster or not (1=yes, 0=no).

Figure 2. Cross-validation results. Two-fold cross-validation were repeated 20 times on the

cortical Layer 1 data with all clusters. Training (reference) and testing (query) data were evenly

split in proportion to the cluster sizes. Cluster-level matching results for the cell-level matching

methods were summarized as the most mapped cluster labels beyond a defined threshold (see

Methods section). Matching output: 1 if a match; 0 otherwise. If a query cluster is not matched to

any reference cluster, then it is unassigned. **(a)** Heatmaps show the average matching result for

each matching method. True positive rate (TPR) is calculated as the average of the diagonal

matching rates, i.e. true positives. **(b)** Median, interquartile range, and full range of accuracy,

sensitivity, and specificity of all cluster-matching results in cross-validation for each matching

method is shown.

Figure 3. Leave-*K*-cluster-out cross-validation results. The same cross-validation settings

as in Fig. 2 were used. After data split, $K \geq 1$ reference clusters were held-out to simulate the

situation in which the query dataset contains one or more novel cell type clusters. **(a)** Heatmaps

show the average matching result for each matching method when the i5 "rosehip" cluster was

left out. **(b)** Accuracy, sensitivity, and specificity of the leave-1-cluster-out cross-validation

performance for each matching method is shown. Each cluster was left out in turn, and

performance was evaluated across all turns. **(c)** Precision-Recall Curves of the leave-*K*-cluster-

out cross-validation performance for $K = 1, 3, 5$, and 7 are shown and Area-Under-the-Curves

(AUC) statistics are calculated. Performance was evaluated across 20 iterations of randomly

selected *K* clusters. Curves for the FR-Match with and without p-value adjustment have the

same shape since the adjustment preserves the order of p-values. Note that the Seurat

package by default does not provide for unassigned cells/clusters as a direct output.

Cluster partitioning		# clusters	F-measure
Under-partition	**Top nodes**	3	0.959
	Mid nodes	11	0.929
Optimal-partition	**15 clusters**	15	0.874
Over-partition	**Split e1**	16	0.864
	Split i1, i2, i3	18	0.818

b

	Partition *Marker type (F-measure)*	Query cluster		
		Under-partition	Optimal-partition	Over-partition
Reference cluster	Under-partition *Common marker (higher)*	1-to-1 (TPR=0.98)	Many-to-1 (TPR=0.94)	Many-to-1 (TPR=0.95)
	Optimal-partition *Specific markers (high)*	1-to-many or missing (TPR=0.72)	1-to-1 (TPR=1)	Many-to-1 (TPR=0.99)
	Over-partition *Noisy markers (low)*	1-to-many or missing (TPR=0.78)	1-to-many (TPR=0.99)	Many-to-many (TPR=0.94)

Figure 4. Design of the under-, optimally-, and over-partitioned cluster simulations and

their matching properties. (a) A schematic of simulating cluster partitions. The optimal

partitioning produced nodes where cells were consistently co-clustered across 100 bootstrap

iterations for clustering and curated by domain expert knowledge[13,28]. Connectivity (edge width)

between nodes are measured by the number of intermediate cells/nuclei shared by similar

nodes. Two under-partition scenarios, "Mid nodes" and "Top nodes", were simulated by merging

similar/hierarchically-connected nodes (e.g. i1 + i5 clusters and all inhibitory clusters,

respectively). Two over-partition scenarios, split e1 and split i1, i2, and i3, were simulated by

splitting those large size clusters by k-means clustering with k=2. Median F-measure of the NS-

Forest marker genes for each partition are reported in the table. **(b)** FR-Match properties and

expected marker gene types with respect to under-, optimally-, and over-partitioned reference

and query cluster scenarios, summarized from the simulation results (Supplementary Fig. 11).

Green blocks in the table are cases with high true positive rate (TPR); red blocks are warning

cases with low TPR.

Figure 5. FR-Match results for cell type matching between the cortical Layer 1 and full

MTG datasets. (a) Two-way matching results are shown in three colors: red indicates that a

pair of clusters are matched in both directions (Layer 1 query to MTG reference with MTG

markers, and MTG query to Layer 1 reference with Layer 1 markers); yellow indicates that a pair

of clusters are matched in only one direction; and blue indicates that a pair of clusters are not

matched. The hierarchical taxonomy of the full MTG clusters is from the original study[29]. FR-

Match produced 13 unique, and two non-unique two-way matches between the two datasets.

Box A shows densely located one-way matches in the subclade of *VIP*-expressing clusters. Box

B shows incidentally captured cells from upper cortical Layer 2 mixed in the Layer 1 e1 cluster.

Box C shows the non-unique two-way matches of astrocyte clusters. **(b)** Examples of matched

and unmatched minimum spanning tree plots from the FR-Match graphical tool. Top row:

examples of two-way matched inhibitory clusters. Middle row: examples of two-way matched

non-neuronal clusters. Bottom row: examples of unmatched excitatory clusters from different

layers. Legend: cluster name (cluster size).

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Figure 6. Cell type matching results between the cortical Layer 1 and full MTG datasets

using other matching methods. Two-way cluster-level matching results for the cell-level

matching methods were summarized as the most mapped cluster labels beyond a defined

threshold (see Methods section). Box A shows matches in the *VIP*-expressing subclade. Box B

shows matches spanning multiple layers among the MTG clusters. Box C shows matches of

glial clusters.

Methods

Human brain cells datasets

Two published single-nucleus RNA-seq datasets from the Allen Institute of Brain Science of

human brain were used: i) cortical Layer 1 of middle temporal gyrus (MTG)[28] and ii) full

thickness MTG[29]. The Layer 1 dataset contains expression data from 871 intact nuclei that form

16 cell type clusters, including four non-neuronal type clusters, one excitatory neuron type

cluster, and 11 inhibitory neuron type clusters. The MTG dataset contains filtered expression

data from 15,603 nuclei that form 75 cell type clusters, subdivided into six non-neuronal type

clusters, 24 excitatory neuron type clusters, and 45 inhibitory neuron type clusters. These cell

type clusters are regarded as transcriptionally distinct cell types with nomenclature asserted

after iterative clustering analysis[13]. Gene-level read count values were preprocessed to log-

CPM (counts per million) values for all nuclei.

The cell type matching problem

Consider two single cell RNA sequencing experiments – one query/new experiment and one

reference experiment. A cell-by-gene expression matrix for each experiment is obtained by

standard scRNAseq data processing and analysis workflows, including quality control, reference

alignment, sequence assembly, and transcript quantification. Cell cluster labels are also

obtained from clustering analysis using, for example, the community detection Louvain

algorithm[10], and/or other domain specific knowledge. These cell clusters represent

transcriptionally-distinct cellular phenotypes within each experiment. The cell type matching

problem is whether a pair of query and reference cell clusters identified in related but

independent experiments are instances of the same or different transcriptionally-defined cell

phenotypes.

We propose a computational solution to the cell type matching problem – FR-Match – an

adaptation the Friedman-Rafsky statistical test for scRNAseq data, which takes two input

datasets (query and reference) each with a gene expression matrix and cell cluster membership

labels (Fig. 1a). Importantly, FR-Match uses a set of informative marker genes that characterize

the reference cell type clusters. Dimensionality reduction is done by imposing the same set of

marker genes on the query dataset, to select the most informative features shared with the

reference dataset. For each pair of cross-dataset clusters, we perform cluster-to-cluster

matching via the Friedman-Rafsky statistical test. As a result, FR-Match outputs the following

types of match (format: query-to-reference): 1-to-0 or unassigned (indicative of a novel cell type),

1-to-1 (indicative of a uniquely matched cell type), 1-to-many (indicative of an under-partitioned

query cluster or over-partitioned reference cluster), many-to-1 (indicative of an over-partitioned

query cluster or an under-partitioned reference cluster).

Necessary and sufficient marker gene identification by random forest

In order to perform dimensionality reduction, random forest machine learning as implemented in

the NS-Forest algorithm[14,15] (v2.0 at https://github.com/JCVenterInstitute/NSForest) was used

to select necessary and sufficient marker genes for each reference cell type cluster. NS-Forest

includes steps for: i) feature selection, ii) feature ranking, and iii) minimum feature determination.

Let X be an $n \times m$ dimensional cell-by-gene matrix, where n is the number of cells and m is the

number of genes. Let y be an $n \times 1$ vector of cluster labels. In step (i), random forest models,

with 10,000 decision trees each, are built for input data X and each cluster label in y under a

binary classification scheme. From each random forest model, the average information gain

based on the Gini index for each gene is extracted, which is then used as a measure of feature

importance to rank the gene features. In step (ii), for the top 15 ranked genes, a binary

expression score for gene g in cluster k is calculated as

$$\text{Score}_{g,k} = \frac{\sum_{k'=1}^{K} \left(1 - \frac{med_{g,k'}}{med_{g,k}}\right)^{+}}{K-1},$$

where $med_{g,k}$ is the median expression level of gene g in cluster k, K is the total number of

clusters, and $(\cdot)^{+}$ defines the non-negative value of the equation. The binary expression score

ranges from 0 to 1, where 1 indicates absolute binaryness, i.e. the gene exclusively expressed

in the target cluster and not at all in non-target clusters. In step (iii), the top 6 genes from step (ii)

are selected and all combinations are evaluated by the F-beta score. F-beta is an F-measure

weighted by β such that

$$F_{\beta} = (1 + \beta^2) \cdot \frac{\text{precision} \cdot \text{recall}}{\beta^2 \cdot \text{precision} + \text{recall}}.$$

$\beta = 0.5$ was set to weight precision more than recall, which compensates the effect of false

negatives dropouts due to technical artifacts in scRNAseq experiments. The output from step (iii)

is a minimum set of marker genes for each cell type cluster (usually $1 - 4$), whose expression in

combination is sufficient to discriminate the target cell type cluster from the rest of the cells. In

addition to the minimum set of NS-Forest marker genes, the algorithm also provides an

extended list of binary marker genes as a supplementary output from step (ii), which may

achieve higher discriminative power under certain circumstances. The top 15 NS-Forest genes

for each cell type formed an NS-Forest extended gene list as an alternative feature selection

option for matching algorithms.

Friedman-Rafsky test

The Friedman-Rafsky (FR) test[26] is a multivariate generalization of the non-parametric two-

sample comparison problem. This classical statistical test is distribution free. Consider two

general distributions F_X and F_Y for samples $(x_1, \cdots, x_m)$ and $(y_1, \cdots, y_n)$ in a p-dimensional space,

respectively. (In the context of FR-Match, the x's and y's denote the expression profiles of each

cell in the query and reference clusters; m and n are the number of cells in each cluster; p is

determined by the number of informative marker genes from the reference dataset). Under the

hypothesis testing framework, the original FR test is designed for testing

$$H_0: F_X = F_Y \qquad \text{versus} \qquad H_1: F_X \neq F_Y,$$

in which the null hypothesis states that the cells from both query and reference clusters are from

the same transcriptional distribution; the alternative hypothesis states that the two cell

populations are from different transcriptional distributions. Thus, the cell type matching problem

becomes a statistical test to detect comparisons for which H_0 is true.

The underlying model of the FR test is a graphical model based on the minimum spanning tree

of pooled samples (Fig. 1a). In the multi-dimensional informative marker gene space, cells from

different clusters (indicated by colors) are pooled and form a mixture of data points. A complete

graph can be constructed, which connects all cells to each other and uses the edge length to

preserve the pairwise Euclidean distance between cells in the original space. Next, the

complete graph is trimmed to a tree graph that connects all cells with the minimum total length

of edges, i.e. the minimum spanning tree. Edges that connect cells of different clusters are then

removed and the number of disjoint subtrees is counted. Intuitively, if there are a large number

of subtrees, it implies that the pooled cells are closely interspersed and therefore more likely to

be from the same multivariate gene expression distribution.

Formally, let R be the total number of subtrees – "multivariate runs" in the FR test framework,

with mean $E(R)$ and variance $\mathrm{Var}(R)$ directly derived from graph theory. The FR statistic is

defined as

$$W = \frac{R - E(R)}{\mathrm{Var}(R)^{1/2}}.$$

Friedman and Rafsky showed that the asymptotic distribution of W follows a standard normal

distribution for large sample sizes:

$$W \sim N(0,1) \text{ as } m, n \to \infty \text{ with } m/n \text{ bounded away from } 0 \text{ and } \infty. \qquad (1)$$

For the hypothesis testing purpose, H_0 is rejected for small values of W, i.e. p-value is one-

sided such that $p = \Pr(W \leq w)$. Note that, in the cell type matching application, we determine a

match if $p > 0.05$, but other p-value thresholds could also be used.

FR-Match method

Extending from the classical statistical test, FR-Match is a novel application of FR test to

approach the cell type matching problem with scRNAseq data. The full FR-Match algorithm not

only implements the basic testing procedure, but also adapts modifications for specific issues

pertaining to the scRNAseq application. A major issue is that two cell clusters to be compared

may have very different cluster sizes, such as a dozen cells versus hundreds of cells

(Supplementary Fig. 21). The unbalanced cluster sizes will often cause two problems: i)

unstable statistical power as the ratio of cluster sizes deviates from the asymptotic condition,

and ii) exponentially long computational time needed for constructing minimum spanning tree for

large number of cells. To address these problems, an iterative subsampling scheme was

implemented, which repeatedly performs sampling without replacement of S cells, or all cells if

S > cluster size, from each cell cluster for B times. Default values of S and B are 10 and 1000,

respectively, but are tunable. The median p-value of all iterations is outputted. Other

modifications include filtering small clusters with less than C cells each, and p-value adjustment

for multiple hypothesis testing correction. Empirically, $C = 10$ was chosen for defining a cell type

cluster with high confidence since it appeared to provide enough cell instances to be

representative. It is suggested to set $S = C$, but it is not a necessary condition for the algorithm.

A disproportionate ratio of S to C would adversely affect the underlying statistical assumptions

due to the unmet asymptotic condition in Equation (1).

The FR-Match algorithm is summarized in the following pseudocode.

algorithm FR-Match **is**

input: Query dataset of clustered gene expression matrix,

488   reference dataset of clustered gene expression matrix,

489   informative marker genes

output: Binary matching matrix, and other optional results

1 Remove clusters with less than C cells

2 Subset the query dataset with only the informative marker genes

3 Subset the reference dataset with only the informative marker genes

4 **for each** pair (query cluster, reference cluster) **do**

5   **for** i **in** 1 **to** B **do**

6          $X \leftarrow$ sample without replacement min$\{S,$ cluster size$\}$ cells

497   from query cluster

498   7 $Y \leftarrow$ sample without replacement min$\{S,$ cluster size$\}$ cells

499   from reference cluster

500   8   Perform FRtest_function(X,Y), and store p-value in p_each_i

501   9   **end for**

502   10 $p\_each \leftarrow$ med$\{p\_each\_1,\ \ldots,\ p\_each\_B\}$

```
503    11 end for

504    12 Store p_each's in a matrix where columns are query clusters and

505       rows are reference clusters

506    13 P-value adjustment using chosen method

507    14 Determine final matches based on adjusted p-value cutoff, and store

508       them in a binary matching matrix with 1 = match and 0 = no match

509    15 return binary matching matrix, optionally, adjusted p-value matrix
```

In the Layer 1 and full MTG matching analysis, tunable parameters were set at the default

values described above, and Benjamini & Yekutieli[37] was used for p-value adjustment.

Determining cluster-level match for the cell-level matching methods

In comparison with other popular matching methods, a voting rule was adopted after obtaining

the cell-level matching results from algorithms scmap (cell-to-cluster) and Seurat (cell-to-cell).

Scmap provides a map: query cell → reference cluster. We calculate the % of reference cluster

labels grouped by the query cell labels, and thereby obtain a quantitative measure ranging from

0 to 1 that indicates the probability of being the same cell type between the query and reference

cell clusters. Similarly, the Seurat alignment is extended to query cell → reference cell →

reference cluster, and calculate the cluster-to-cluster matching measure in the same way. For a

specific query cluster, its cluster-level match is determined by the votes of its member cells for

their mapped reference cluster labels. An ad-hoc threshold at 30% was used for defining a

deterministic match, which accounts for both the detection of a substantial proportion of query

cells matched to one reference cluster and the possibility that some query clusters might be

matched to multiple reference clusters. If the 30%-criterion is not met, then the query cluster is

defined as unassigned in the matching results. The cluster-level matching results may change

depending on the ad-hoc threshold used. For example, if changing the threshold to 40%, Seurat

would identify the same set of two-way matches, but with three fewer one-way matches

(Supplementary Fig. 22). A data-driven decision on such a threshold can be guided by the

distribution of % of matched cells in Supplementary Figs. 17-20.

Cross-validation and simulation design

Data generation for the cross-validation and simulation studies were from the cortical Layer 1

data with 15 cell clusters[28] (excluding one cluster, i11, with too few cells). All cross-validation

designs were two-fold by evenly splitting data into training and testing in proportion to the

original cluster sizes. All cross-validations were repeated 20 times each design.

Real data-guided simulations were used to mimic under-/over-partitioned scenarios (Fig. 4).

"Top nodes" under-partitions are cells merged into three broad classes: GABAergic inhibitory

neurons, glutamatergic excitatory neurons, and neuroglial cells. "Mid nodes" under-partitions are

cells merged into similar inhibitory neurons according to the constellation diagram of cluster

network from the original study[28]; for the purpose of simulation, i1 and i5, i3 and i4, and i6, i8,

and i9 were merged. For over-partitions, large cell clusters were split by running k-means

clustering with k = 2 independently for each over-partitioned cluster. "Split e1" divided the

excitatory cluster into two sub-clusters of sizes 180 and 119 cells, resulting in 16 (= 15 + 1)

over-partitioned clusters. "Split i1, i2, i3" divided each of the inhibitory clusters into two sub-

clusters of sizes 56 and 34, 39 and 38, 32 and 24 cells, respectively, resulting in 18 (= 15 + 3)

over-partitioned clusters in total. NS-Forest marker genes were identified for each of the

simulated datasets. Matching performances of the under-/over-partitioned datasets were

evaluated through two-fold cross-validation repeated 20 times.

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