3D single cell migration driven by temporal correlation between oscillating force dipoles

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Abstract

Directional cell locomotion requires symmetry breaking between the front and rear of the cell. In some cells, symmetry breaking manifests itself in a directional flow of actin from the front to the rear of the cell. Many cells, especially in physiological 3D matrices do not show such coherent actin dynamics and present seemingly competing protrusion/retraction dynamics at their front and back. How symmetry breaking manifests itself for such cells is therefore elusive. We take inspiration from the scallop theorem proposed by Purcell for micro-swimmers in Newtonian fluids: self-propelled objects undergoing persistent motion at low Reynolds number must follow a cycle of shape changes that breaks temporal symmetry. We report similar observations for cells crawling in 3D. We quantified cell motion using a combination of 3D live cell imaging, visualization of the matrix displacement and a minimal model with multipolar expansion. We show that our cells embedded in a 3D matrix form myosin-driven force dipoles at both sides of the nucleus, that locally and periodically pinch the matrix. The existence of a phase shift between the two dipoles is required for directed cell motion which manifests itself as cycles with finite area in the dipole-quadrupole diagram, a formal equivalence to the Purcell cycle. We confirm this mechanism by triggering local dipolar contractions with a laser. This leads to

44 directed motion. Our study reveals that these cells control their motility by synchronizing dipolar
45 forces distributed at front and back. This result opens new strategies to externally control cell
46 motion as well as for the design of micro-crawlers.
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48 **Introduction**
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Cell motility is essential in a variety of biological phenomena (Yamada and Sixt, 2019). Cells
move during development in the presence or in the absence of chemical gradients. Their
relevant localisations at the right moment is essential to secure completion of viable developing
embryos. Also defects in migrations are known to be involved in cancer progression with the
increased motility of cells during invasion (Stuelten, Parent and Montell, 2018). Understanding
cell motion in physiological environment is therefore recognised as a central question in basic
and in applied sciences.
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In this context, the determination of genetic and proteins networks has been instrumental in
identifying the central pathways at play for motility (Jia *et al.*, 2022). These steps in outlining
specific partners are instrumental in localising defects and they open potential perspectives for
testing new strategies to act on these situations where cells migration is impaired *in vivo* and *in*
vitro. However cell motion calls also for physical principles because motion at this scale is not
intuitive (Tanimoto and Sano, 2014). This requires alternative approaches both in experiments
and in theory in synergy.
65
Cells motion in 2D flat surfaces has been documented in details (Alberts *et al.*, 2002). The
classical image of extension of lamellipodia and retraction of the back of the cells is known.
Cells crawl and protrusions grow and retract around the cell. New dynamics are also associated
with the motion of confined cells in microfabricated channels where retrograde flow of actin at
the scale of the entire cell was reported to play central roles in motility (Liu *et al.*, 2015; Reversat
et al., 2020). However both approaches – cells crawling on 2D flat surfaces and in channels –
call for tests in actual 3D situations where cells interact with an environment similar to
physiological 3D situations. This experimental challenge of mimicking *in vivo* environments goes
together with theoretical basic questions.
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At cellular scales inertia is negligible which puts some particular constraints on self-propelled
microscopic objects (Purcell, 1977; Tanimoto and Sano, 2014). Low Reynolds number micro-
swimmers in Newtonian fluids must obey the scallop theorem, stating that the cyclic sequence
of shape changes they perform to swim cannot be symmetrical in time (Purcell, 1977; Najafi and
Golestanian, 2004; Golestanian and Ajdari, 2008; Barry and Bretscher, 2010; Leoni and Sens,
2015). In his seminal work, Purcell illustrated such behavior as closed trajectories
encompassing a finite area in some properly chosen phase space (Purcell, 1977).
83
Crawling cells are not strictly bound to obey the scallop theorem, which stems from the time
reversibility of the Stokes equation. Cells moving in 2D or in micro-channels often display clear
spatial polarization, characterized by F-actin flowing from the front to the back of the cell
(Barnhart *et al.*, 2011; Liu *et al.*, 2015). For such fast moving cells, the lack of time reversal

symmetry – the fact that the system looks different when the movie is played backward – clearly
manifests itself by the existence of a coherent actin flow at the scale of the entire cell and the
cell velocity is directly related to the dynamics of the actin flow. This mode of motility has been
studied in detail theoretically, in particular to understand how the positive feedback between
actin flow and the distribution of contractile units (myosin motors) may lead to spontaneous
symmetry breaking (Blanch-Mercader and Casademunt, 2013; Recho, Putelat and
Truskinovsky, 2013; Recho, Joanny and Truskinovsky, 2014; Maiuri *et al.*, 2015). Many cells,
especially mesenchymal cells, do not show such polarized actin flow at the scale of the entire
cell, but instead display cycles of protrusion/retraction at both ends of the cell. The actin
dynamics within protrusions is comparable to that of fast-moving cells, but the existence of
multiple competing protrusion leads to slow cell translocation (see for example (Caballero,
Voituriez and Riveline, 2014; Lo Vecchio *et al.*, 2020)). Slow moving cells in complex
environments such as the extracellular matrix could leverage the visco-elastic nature of the
environment (Qiu *et al.*, 2014; Datt, Nasouri and Elfring, 2018) or the complex dynamics of
adhesion and detachment (Wagner and Lauga, 2013; Leoni and Sens, 2017). This makes the
search for unifying principles underlying 3D cell movement challenging.
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In this article, we report the experimental design of a 3D physiological matrix which single cells
deform while moving. We label fluorescently the important cellular proteins involved in cell
motility. Deformation of the matrix correlated with motility/adhesion proteins localisations allow
us to show that two forces dipoles mediated by acto-myosin at each side of the nucleus are
correlated with a phase shift when cells move directionally. We propose a model which is
consistent with this explanation and test this mechanism by inducing force dipoles. Our results
shed light on generic physical mechanisms at play in cell migration.
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Results

114
Fibroblasts in CDMs generate contractile-extensile regions on either side of the nucleus
To search for generic readouts for 3D cell migration, we designed an assay where cell migration
and the spatial distribution of cell-matrix interactions could be tracked simultaneously and
quantified over time. In our experiment, NIH 3T3 fibroblasts moved inside a fluorescently
labelled Cell Derived Matrix (CDM) (Figure 1a, left panels and Video 1), obtained using a
protocol adapted from (Cukierman, 2001). Briefly, a confluent monolayer of NIH3T3 cells
expressing fluorescently labeled fibronectin was triggered to synthesize extracellular matrix
proteins for eight days. Then, cells were removed by lysis, generating a 3D protein meshwork
(Figure 1 – figure supplement 1a). The resulting CDM had large pores inside, but it was covered
by a dense crust, as shown by electron microscopy (Figure 1 – figure supplement 1b). Despite
this, 3T3 fibroblasts seeded on top of the CDM passed through and spread within the matrix,
which was significantly thicker than cells themselves (Figure 1 – figure supplement 1c and 1d).
We then determined by micromanipulation of embedded beads the mechanical properties of
these cell derived matrices (Figure 1 – figure supplement 1e, Video 2 and Appendix 1). Optical
tweezer experiments showed no hysteresis in the displacement curves, suggesting that the
matrix behaved as an elastic material within the amplitudes and timescales explored (Figure 1 –
figure supplement 1f and 1g), which is in agreement with previous reports (Petrie *et al.*, 2012).

Moreover, the relationship between force and displacement was linear (Figure 1 – figure
supplement 1h) and we could determine the CDM's elastic modulus to be ≈ 50 Pa (Figure 1 –
figure supplement 1h and 1i) and no modification of the meshwork was observed after 24 hours
of cell migration inside (Figure 1 – figure supplement 1j). Altogether, these physiological 3D
porous matrices were thick enough to host 3D cell migration and were sufficiently soft and
elastic to relate cell dynamics to matrix deformation.
138
For migration experiments, 3T3 fibroblasts were plated at low density, spontaneously
penetrated the matrix and could be followed individually. Cells displayed an elongated
morphology (Figure 1 – figure supplement 2), typical of fibroblasts in these soft and elastic
matrices (Cukierman, 2001; Petrie *et al.*, 2012; Caballero *et al.*, 2017). We observed (i) a
cortical distribution of acto-myosin (Figure 1a), (ii) the presence of focal adhesions distributed all
over the cell membrane and mediating its adhesion to the surrounding matrix (Figure 1 – figure
supplement 2 and Video 3), and (iii) the microtubule cytoskeleton expanding from the
centrosome to the periphery of the cell (Figure 1d and Video 4). Strikingly, the CDM was easily
deformed by cells as they moved through (Figure 1a, right panels and Video 5). This enabled us
to quantify the associated matrix deformation (Delanoë-Ayari *et al.*, 2008) via the Kanade-
Lucas-Tomasi (KLT) tracker method (Lucas and Kanade, 1981) (Figure 1b). These
deformations were present at the front and at the back of the nucleus of polarized cells, where
phases with both contractile and extensile patterns were observed. Similar patterns were also
observed in other cell types migrating in CDMs. Both Mouse Embryonic Fibroblasts (MEF) and
Rat Embryo Fibroblasts 52 (REF52) exhibited phases of contraction and extension patterns at
the front and the back of the nucleus (Figure 1 – figure supplement 3). Moreover, the matrix
deformation could be imaged concomitantly with the cellular machinery responsible for force-
generation. We could observe a transient densification of the myosin signal forming clusters of
myosin associated with the contraction observed in the matrix displacement (Figure 1c and
Video 6). This force transmission between the cell and the CDM was also observed at the focal
contact level: enlargement of pores of the fibronectin meshwork suggested a local pulling force
by the cells (Figure 1 – figure supplement 2). Therefore, cells embedded in CDMs generate
forces which translate into contractile and extensile deformations in the surrounding matrix.
162
Dynamics of matrix deformation for migrating and non-migrating cells
During migration experiments, some cells showed persistent motion (Video 7) while others
moved back and forth along a constant central position. Hereafter, we denote as migrating cells
the first type and as non-migrating cells the second type. Interestingly both migrating and non-
migrating cells exhibited local zones of contraction-extension along time (Figure 2a). Such
regions can be seen on both sides of the nucleus (Figure 1b). To characterize the behavior of
these contraction-extension regions over time, we defined the cell axis along the direction of
polarization (defined by a more protrusive cell end) for non-migrating cells and along the
direction of migration for migrating cells (Figure 2b and 2c). Then, we projected the divergence
of the matrix across the x-y plane on the cell axis for every time point and plotted the
corresponding kymographs (Figure 2d and 2e). For non-migrating cells, we could observe
sequences of positive and negative divergence along time (alternating blue and yellow area) on
still regions (black lines in Figure 2d) at both sides of the nucleus. For migrating cells,

sequences alternating positive and negative divergence were present as well (Figure 2e).
However, these contraction-extension patterns were not still, but moved along with the cell (blue
and red lines in Figure 2e correspond to the back and front of the nucleus respectively). Thus,
we suggest that these contraction-extension regions are equivalent to two force dipoles on
either side of the nucleus.
181
As it can be seen from the kymographs, these deformations were cyclic. To determine their
period of contraction, we extracted temporal profiles of the divergence of the matrix
displacement by averaging over the regions at the front and the back of the nucleus (Figure 2 –
figure supplement 1a - d). By doing so, we obtained the traces of the contractions at the front
and the back over time for single cells (Figure 2 – figure supplement 1e). Measurements of the
magnitude of the peaks observed in the divergence traces showed no difference between front
and back in migrating cells (Figure 2 – figure supplement 2). The same behavior was observed
for non-migrating cells, which were also similar in magnitude to the ones observed in migrating
cells (Figure 2 – figure supplement 2). We then performed the autocorrelation of these traces to
obtain the period of the contractile and extensile patterns (Figure 2 – figure supplement 1f).
Autocorrelation of the divergence profile for individual non-migrating cells (Figure 2f -
representative example for one cell) resulted in periods of oscillation similar at the front and
back of the cell ($\approx$ 6 min) (Figure 2g) (see Methods section for quantification of the oscillations).
For individual migrating cells, autocorrelation of divergence profiles (Figure 2h - representative
example for one cell) gave oscillation periods of $\approx$ 8 mins, similar at the front and the back as
well (Figure 2i). These contraction relaxation cycles with periods of $\approx$ 8 mins and amplitudes of
typically 2.5 µm are reminiscent of previous reports of cell autonomous contractile oscillations
(Kruse and Riveline, 2011). Periods of oscillations were comparable for motile and non-motile
cells (Fig.2 g,i). The phases of contraction seemed to correlate with the formation of local
myosin clusters as described above (Figure 1c), which is consistent with the observation of
distinct myosin-driven contraction centers in the migration of neurons on 2D surfaces (Jiang *et*
al., 2015).
204
We observed more protrusive activity at one of the two ends of elongated cells, in both motile
and non-motile cells. Since this apparent spatial polarization was not sufficient to elicit directed
motion, we looked for other sources of symmetry breaking. We measured the temporal cross-
correlation function of the contraction-extension cycles at the two cell ends (Figure 2 – figure
supplement 1g and Figure 2j). This revealed significant differences between migrating and non-
migrating cells. While non-migrating cells systematically showed no phase shift between the two
ends, with cross-correlation peaks localized at a time shift t = 0, migrating cells showed cross-
correlation peaks at non-zero time lags (Figure 2k), suggesting a phase-shift between the front
and back contraction-extension cycles (differences of phase-shift in migrating and non-migrating
cells were statistically significant with p = 0.0246). A system undergoing directed motion must
exhibit time reversal asymmetry. In our case, this asymmetry manifests itself through a time lag
between the contraction-extension cycles of the two force dipoles.
217
Multipole analysis of the matrix deformation

The most intuitive way to visualize time reversal symmetry breaking is through the existence of
cycles in a properly chosen phase space. This phase space may be based on a multipole
expansion of the traction force exerted by the cell on its surrounding. This approach was
pioneered by Tanimoto & Sano for Dictyostelium discoideum crawling on deformable 2D
substrate (Tanimoto and Sano, 2014). In particular, they showed that crawling Dictyostelium
discoideum exhibits cycles of finite area in the dipole-quadrupole phase space. In the present
work, the traction forces exerted by the cell are analyzed indirectly through the deformation of
the matrix. Indeed, our characterization of the mechanical properties of the CDM showed that it
locally behaves as a linear elastic material with a well-defined elastic modulus (Figure 1 – figure
supplement 1f-j). This supports the approximation of a linear relationship between the moments
of the force distribution and the moments of the resulting matrix displacement distribution. Note
however that the relationship could be more complex due to matrix heterogeneities.
231
We analyzed the 2D projection of the 3D deformation field of the CDM and computed the dipolar
and quadrupolar moments of the rate of matrix deformation (see Appendix 2 and Figure 3 –
figure supplement 1 for details). Briefly, we extracted the 2D projected velocity vector field $u_i^{(n)}$
for the component i of the change of substrate deformation between two consecutive frames at
position n of the mesh. The dipole is a tensor defined as $S_{ij} = \frac{D_{ij}+D_{ji}}{2}$ with $D_{ij} = \sum_n \Delta_i^{(n)} u_j^{(n)}$,
where $\Delta_i^{(n)}$ is the i-th component of the vector joining the cell centre and the point n on the
mesh. Similarly, the quadrupole tensor is defined as $Q_{ijk} = \sum_n \Delta_i^{(n)} \Delta_j^{(n)} u_k^{(n)}$. The largest
eigenvalues of the dipole and quadrupole tensors are defined as the main dipole, D, and the
main quadrupole, Q, and the corresponding eigenvectors are defined as the main dipole and
quadrupole axes. Figure 3a shows an example of the orientation of the main dipole, and Figure
3b shows a sketch of the physical/geometrical meaning of these quantities. The main dipole
axis was aligned with the direction of motion - within experimental noise (see Figure 3 – figure
supplement 2 for a quantification) - as was reported for 2D motion (Tanimoto and Sano, 2014).
245
We then determined the time variation of the main dipole and quadrupole. The level of traction
exerted by the cell on the matrix observed for non-migrating cells are comparable in magnitude
to those of migrating cells (Figure 3 – figure supplement 3b, differences between migrating and
non-migrating cells are not statistically significant with p = 0.2766). This shows that the absence
of migration is not due to the lack of traction forces (see also Figure 3 – figure supplement 1).
Identifying time reversal symmetry breaking phenomena is not straightforward in the temporal
representation of Figure 3c. Therefore, we instead represent the cell trajectory in the
dipole/quadrupole phase space, in which non-reversible periodic trajectories appear as closed
cycles of finite area (Tanimoto and Sano, 2014). We indeed observe that trajectories showed a
cycle enclosing a finite area for migrating cells, but a negligible area for non-migrating cells
(Figure 3d and 3e, and more examples in Figure 3 – figure supplement 3). To further test the
relationship between finite cycle area and motility of individual cells, we analyzed the migration
of a cell that underwent motion and then stopped (Figure 3f-h and Video 8). Strikingly, we
observed that the cycles switched from a finite area while the cell was moving to a vanishing
area when the cell stopped (Figure 3h). The finite area is a direct illustration of the fact that the
phase shift between the contraction-extension cycles at the two ends of migrating cells

observed in Figure 2 also manifests itself in the pattern of matrix displacement. This is a clear
signature of time reversal symmetry breaking. The quantification of the area enclosed by the
trajectories in the D-Q plane of migrating and non-migrating cells is detailed in Appendix 2 and
shown in Figure 3 – figure supplement 3c. Both absolute areas (in $\mu m^5/min^2$) and normalised
areas (in percent of the area of the rectangle fitting the trajectory) were substantially larger for
migrating cells than for non-migrating cells (differences were statistically significant with p =
0.0177 and p = 0.0431 respectively). This supports our claim that the relevant difference
between the two behaviors is the existence of a phase shift rather than a difference in the level
of traction forces.
271
To test whether we could correlate the oscillations at the two cell ends with molecular actors, we
tracked cell motion in the presence of the microtubule depolymerizing agent, nocodazole. Upon
addition of the drug, cell migration stopped (Figure 4 – figure supplement 1h). Some cells then
underwent a forward backward movement in the matrix (Video 9), which hinted at an oscillation
driven by local force dipoles. We observed a similar behavior in nucleus free cells, generated
when protrusions rupture from the cell. The resulting cytoplast underwent a forward backward
movement in the CDM (Figure 1 – figure supplement 3c, Video 10). They switched polarization
over time, with a frequency of one direction reversal every ≈ 36 min. Although the Nocodazole
treated cells did not maintain a fixed cell-polarization either, we extracted matrix displacement
which showed a typical period as for non-treated cells of ≈ 11 min (Figure 2g). Due to the lack or
switch in polarity we could not define a back and a front. However, oscillations at different cell
ends were in phase and cells did not show directed motion. This suggests that the coupling
between oscillators needed to promote directed motion could involve microtubules. Indeed, the
microtubular network spans the entirety of the cell body (Figure 1d and Video 4), and is thus a
natural candidate to transfer information between the two ends of the cell. This suggestion is
consistent with the notion that the microtubular network regulates the polarity axis of migrating
cells (Etienne-Manneville, 2004; Kaverina and Straube, 2011).
289
Persistent speed is related to the period of oscillations
The geometry and dynamics of the distribution of matrix displacement call for a direct
comparison with models of self-propelled objects made of discrete moving beads (Najafi and
Golestanian, 2004; Golestanian and Ajdari, 2008; Wagner and Lauga, 2013; Leoni and Sens,
2015, 2017; Datt, Nasouri and Elfring, 2018). Figure 4a and 4b displays an idealized cell with
two oscillating pairs of beads exerting time-shifted oscillatory force dipoles at its two ends. Here,
the contractions at either ends of the cell are chosen to have the same magnitude for simplicity
and in agreement with our observations (Figure 2 – figure supplement 1 and 2), but this is not
required to elicit net cell translocation. The cell activity is characterized by the amplitude d and
period T of the oscillations and a phase shift $\psi = 2\pi\Delta T/T$ between oscillations at the two ends.
The simplest self-propelled object is a micro-swimmer embedded in a newtonian fluid and
migrating due to hydrodynamic interactions (Najafi and Golestanian, 2004; Golestanian and
Ajdari, 2008; Leoni and Sens, 2015). In this case, the period of oscillation is the only time scale
in the problem, and the swimming velocity must scale inversely with the period. In the limit of
small oscillation amplitudes and weak hydrodynamic interactions, that is if $d \ll a \ll D \ll r$

(where d is the oscillation amplitude, a the bead size, D the dipole size and r the cell size,
Figure 4a), the net cell velocity over a cycle follows the scaling (Leoni and Sens, 2015)
307

$$V_{swim} = \frac{d^2}{L_s T} f_s(\psi) \tag{1}$$

309
310 where $f_s(\psi)$ is a periodic function of the phase shift satisfying $f_s(\psi = 0) = 0$, *i.e.* no velocity
311 without phase shift, as required by the scallop theorem, and $L_s \sim r^4/(aD^2)$ is a length scale set
312 by the cell geometry. Examples of theoretically computed cell trajectories in the
313 dipole/quadrupole phase space for non-migrating and migrating cells are shown in Figure 4 –
314 figure supplement 2.
315
A key aspect of cell crawling, which is absent for micro-swimmers, is the dynamics of cell
attachment and detachment from the surrounding matrix. Our observations suggest that dipole
contraction is associated with an active contraction of acto-myosin clusters and that dipole
extension corresponds to the elastic relaxation of the CDM following local cell detachment, i.e.
the loss of focal contacts (Video 3 and (Godeau, Delanoë-Ayari and Riveline, 2020)). The
kinetics of cell binding/unbinding to the extracellular matrix defines additional dynamic
parameters, so that the scaling relationship between cell velocity and the oscillation period is
less universal than Eq.1 for the swimmer's case. An important factor is how the rate of
unbinding of adhesion bonds depends on the force applied on them. At the simplest level – in
the limit of fast binding kinetics and small applied force – this can be captured by a velocity
scale $v_{adh} = \delta_{off} k_{off}$, where k_{off} is the unbinding rate under no force and δ_{off} is a matrix
deformation amplitude characterizing bond mechano-sensitivity (Leoni and Sens, 2017). In this
case, the net velocity of the idealized cell sketched in Figure 4a for small oscillation amplitude
reads (Leoni and Sens, 2017):
330

$$V_{crawl} = \frac{d^3}{v_{adh} L_c T^2} f_c(\psi) \tag{2}$$

332
333 where $f_c(\psi = 0) = 0$ as for swimmers, and the length scale $L_c \sim r^2/a$ also includes additional
334 dimensionless factors related to substrate dissipations (see (Leoni and Sens, 2017) for more
335 details).
336
These simple models predict how the velocity should vary with the period of oscillation T. The
result depends on whether the amplitude of oscillations d is fixed or is a function of T. For
oscillations of constant amplitude, the net velocity of both swimmers and crawlers decreases if
the period of oscillation increases. On the contrary, the velocity is expected to increase with the
period if the amplitude increases linearly with the period: $d \sim T$, as can be expected if the self-
propelled object operates under constant force – or equivalently constant contraction/extension
rate.
344
The temporal oscillations of the instantaneous cell velocity are a good readout for the dynamics
of internal force generation. For such self-propelled objects, the instantaneous velocity oscillates
around the average values given by Eqs.1 or 2, with a time dependence that reflects the

dynamics of the underlying force dipoles. An example of such (theoretical) velocity oscillations
can be seen in Figure 4b. Experimental observations indeed report strong oscillations of the
instantaneous cell velocity (Figure 4c).
351
To test how the period of oscillation of migrating cells influenced their velocity, we took
advantage of the inherent variability of cells and plotted the velocity vs. period for WT cells and
observed a clear anticorrelation (Figure 4d). Although the large cellular noise prevented us from
quantitatively comparing the scaling relations given by Eqs.1,2, this is consistent with
locomotion being driven by controlling cell deformation instead of cell traction forces. Similar
conclusions have been reached in the different context of adherent epithelial cells (Saez *et al.*,
2005). To extend the range of variation of the different cellular parameters, we treated cells with
a collection of specific inhibitors that impact cell migration in CDMs (Caballero *et al.*, 2017). We
tracked cell trajectories for control cells (Figure 4 – figure supplement 1a), cells treated with
myosin ATPase activity inhibitor Blebbistatin (Figure 4 – figure supplement 1b and Video 11),
ROCK inhibitor Y27632 (Figure 4 – figure supplement 1c), myosin light chain kinase inhibitor
ML7 (Figure 4 – figure supplement 1d), actin polymerization inhibitor Latrunculin A (Figure 4 –
figure supplement 1e), lamellipodia growth promoter C8-BPA (Figure 4 – figure supplement 1f),
Arp2/3 complex inhibitor CK666 (Figure 4 – figure supplement 1g) and Nocodazole (Figure 4 –
figure supplement 1h). As expected, all pharmacological treatments altered cell migration.
Latrunculin A (Video 12) and Nocodazole (Video 9) stalled migration completely. Among the
others, we observed speed oscillations for cells treated with Y-27632, ML-7, C8-BPA and
CK666. Those treatments reduced persistent cell speed (Figure 4 - figure supplement 1i) and
increased the period of speed oscillations (Figure 4 - figure supplement 1j), showing that we
could indeed alter cell migration behavior. We then plotted the velocity as a function of the
oscillation period, for individual cells of drug treatments with speed oscillations aggregated (Y-
27632, ML-7, C8-BPA and CK666) together with control cells (WT). We could observe an
inverse correlation between period and velocity overall for these cells (Figure 4d, Pearson's
correlation coefficient -0.4978 with p < 0.0001). However when looking at each condition
separately, persistent speed was still significantly anticorrelated with oscillation period for WT
cells and Y-27632 treated cells (Pearson's correlation coefficient -0.4119 with p = 0.0455 and -
0.7435 with p = 0.0217, respectively), but it was not in the case of ML-7, C8-BPA and CK666.
This may be caused by variability among individual cells, since on average cell speed
decreased and oscillation period increased upon treatment with these compounds as well
(Figure 4 - figure supplement 1i and j). Therefore, an inverse correlation between period and
velocity is evident at the population level, both for WT cells and when those are aggregated to
pharmacologically treated cells.
384
Externally triggered contractions by means of laser ablation induce cell translocation
Altogether, these results suggest that the temporal coupling between spatially distributed force
dipoles along the cell promotes cell motion. To verify this, we designed an experiment to
externally trigger localized cellular force dipoles. We observed that localized laser ablation
within the cortex of a cell (Figure 5a and 5b before ablation) triggered the relaxation of the cell
and the surrounding matrix, as marked by the displacement of the matrix away from the cut
region (Figure 5b ablation). This process was then followed by a contraction of the cell along

with the surrounding matrix (Figure 5b after ablation). Remarkably, laser ablation led to the transient recruitment of actin and myosin (Figure 5c bottom left and Figure 5 – figure supplement 1a), which co-localized with cell contraction (Figure 5c bottom right and Video 13). For a polarized cell the laser-induced contraction triggered the translocation of the cell (Figure 5b), whereas for a cell with no clear polarization and multiple attachment points no cell body translocation was observed (Figure 5c). Therefore, by laser ablation we could induce matrix pinching that could lead to a cell translocation given certain cell morphology.

Mimicking the periodic alternation of contractile and extensile dipoles at both ends of the cell, a second contraction at the opposite side of the cell should lead to forward displacement. So, we then used this method to repeatedly locally impose cellular force dipoles, by triggering local contractions alternatively at the front and the back of a polarized cell (see schematics in Figure 5 - figure supplement 1b). We imposed correlated contractions by selecting a constant time interval between consecutive laser ablations: this triggered reiterated translocation and led to a net movement of the cell (Figure 5 – figure supplement 1b and Video 14). This externally induced cell displacement was achieved when laser ablation of equal power was applied sequentially at the front and the back of the nucleus, both with about 6 minutes and 10 minutes intervals between cuts (Figure 5 - figure supplement 1b). In contrast, when this sequential ablation was applied repeatedly only at one side of a polarized cell (front), net displacement was either absent or smaller than when alternating front and back, both with about 5 and 10 minutes intervals between cuts (Figure 5 – figure supplement 1c). This shows that externally induced force-dipoles are sufficient to promote directed cell motion and illustrates that by alternating induced force dipoles at front and back of the nucleus leads to net cell motion. Altogether, this supports the principle of a phase shift between local dipoles as a trigger for cell motility.

Discussion

Acto-myosin complexes are likely to be the functional elements that control the dynamics of the individual contractile units. The cycles of protrusion/retraction at both ends of the cell likely involves transient retrograde actin flow whose periodic nature could be linked to a stick-slip phenomenon (Sens, 2020). Therefore, although the local actin dynamics within protrusions could be comparable to that fast moving cells in 2D or under confinement (Barnhart *et al.*, 2011; Liu *et al.*, 2015), the absence of a coherent actin flow at the scale of the entire cell and the existence of multiple competing protrusions considerably slows down cell motion. Our results show that for cells moving in 3D CDMs, the lack of time reversal symmetry required for cell motion is associated with a time shift between the oscillating dynamics of the two cell ends. Remarkably, the dynamics of individual dipoles appear similar in migrating and non-migrating cells, suggesting that the same force generation machinery is equally active in both types of cells, and that it is the synchronization between individual units that makes movement possible. Altering the dynamics of individual units can affect motion, in particular, faster oscillations can lead to faster motion, but the coordination between units is key in enabling cell translocation.

Acto-myosin networks commonly show oscillatory dynamics in vitro and in vivo in a variety of systems and over a large range of length scales (Kruse and Riveline, 2011): single filaments in

motility assays (Riveline *et al.*, 1998; Gillo *et al.*, 2009; Plaçais *et al.*, 2009), cells (Negrete *et al.*,
2016) and cell fragments (Paluch *et al.*, 2005), and even entire organisms (Martin, Kaschube
and Wieschaus, 2009). The biological function of these generic dynamics is often unclear.
However, in our case, they appear to be essential. We conjecture that cellular systems could
adapt their velocity by modulating the oscillation period. In this context, it would be interesting to
test this proposal by combining tracking of single moving cells and local matrix deformations *in*
vivo. If confirmed, this would provide an outstanding example of a physiological relevance for
such oscillations. The phase-shift between contractile units encodes cell polarity. Its
maintenance in the course of time requires the existence of a polarity memory. If this type of
phase locking can be expected in non-linear systems (Pikovsky, Rosenblum and Kurths, 2002),
it is more demanding in the cellular context, where it is challenged by strong fluctuations in
protein concentrations and activities. Our results suggest that the microtubular network is
involved. However, other cytoskeletal elements and their interplay with adhesion dynamics are
likely to play a role as well. Disentangling the interplay between mechanics and biochemical
regulation in this process remains an important open question.
451
Our results show that for several cell types moving in CDMs, there exist two contractile units
exerting force dipoles at both ends of the cell, and the lack of time reversal symmetry required
for motion is associated with a time shift between the oscillating dynamics of the two cell ends. It
is interesting to note that in other reports of cell motions in 3D gels (Steinwachs *et al.*, 2016),
cell appears to behave as fluctuating single contractile units, with no mention of coexistence of
contraction at one end and extension at the other as we report here (for instance in Figure 1b).
This type of motion is physically possible (see for instance (Wagner and Lauga, 2013) or (Datt,
Nasouri and Elfring, 2018)). It thus appears that different cell types may undergo distinct
dynamics to promote directed cell motion. Single force dipoles would be related with correlation
of the contractile machinery across the cell whereas two dipoles could be associated with
autonomous acto-myosin contractile units on each side of the cell. It would be interesting to
relate this principle of length scale of mesoscopic unit dynamics with cytoskeletal structures and
compositions in different cell lines.
465
We have explained the mechanisms of our directed cell motion with the concept of
synchronised force dipoles and our results are consistent with the associated model. However
many assumptions were made. The CDMs are not continuous media, they are hydrogels of
porous nature which may halt the motion when the pore size block the nucleus, for example.
This may contribute to phases where cells are trapped and do not move at all. This situation
would not challenge our model, since the directed motion phases presumably bypass this
potential blockage. Also, growth and detachments of cell adhesion at both cell ends could be
involved in the migratory phases along our observations of focal contacts dynamics (Video 3).
Again, this would not challenge the main result of our rule for finite area when cells move
directionally. It may however contribute to alternative mechanisms in the model where
mechanosensing at focal contacts rather than force dipoles or in synergy with force dipoles
mediated by acto-myosin would contribute to the basic synchronization mechanism. These
potential contributions could be disentangled by future experiments tracking both acto-myosin
and focal contact proteins over time together with matrix deformations.

We propose that temporal correlations between distinct contraction-extension units along the
cell body is a general principle used by mesenchymal cells to achieve directional motility in 3D.
This suggests new strategies to control the motion of cells by externally modulating their local
contractile activity, for which we give a proof-of-principle using a standard laser setup. This
concept could also be used to design synthetic micro-crawlers. Whereas there exist many
examples of artificial micro-swimmers (see (Elgeti, Winkler and Gompper, 2015) for a review),
there is to our knowledge no realization of micro-crawler in regimes where inertia is negligible.

Methods

Cell lines. NIH3T3 mouse embryonic fibroblast cell line was obtained from ATCC. Rat Embryo
Fibroblast 52 (REF52) and primary mouse embryonic fibroblasts were obtained from the IGBMC
cell culture facility. Cells lines tested negative for mycoplasma.

Preparation of Cell Derived Matrices. For the CDM preparation (see Figure 1 – figure
supplement 1a and (Godeau, Delanoë-Ayari and Riveline, 2020)), a glass coverslip (CS) was
incubated with 1% gelatin (gelatin from cold water fish skin, Sigma) and put at 37ºC in the
incubator for 1h. After two washing steps with PBS, the CS with the gelatin solution was
incubated for 20 min at room temperature with 1% glutaraldehyde (Sigma). The CS was rinsed
again twice with PBS before incubation for 20−30 min with 1 M glycine (Sigma). Subsequently
the CS was washed twice with PBS before plating of the NIH3T3 fibroblasts. Cells were plated
at high density in order to produce CDMs. For NIH3T3, this corresponded to a cell density of 10^5
cells/mm2 in the Petri dish. The culture medium was supplemented with 50µg/mL L-ascorbic
acid and changed every two days. The culture was maintained for 8−9 days. Cells were
removed by a lysis medium consisting of 20 mM NH4OH and 0.5% Triton (both from Sigma) in
PBS after two washing steps with PBS. The pre-warmed lysis medium was carefully pipetted on
the CS and incubated for up to 10 min at 37ºC in the incubator. PBS solution was added and
the CDM and stored at 4ºC. The day after, the PBS solution was carefully changed three times
to remove residues of Triton. The matrices were covered with PBS and stored for up to one
month at 4ºC. For alignment purposes after image acquisition, beads (200nm, BioSpheres)
were spin-coated on the CS before incubation with gelatin. Beads for optical tweezers
measurements (L4530, Sigma) were inserted when seeding the cells. For visualization of
fibronectin inside the CDM, two methods were used with no apparent differences: we prepared
a stable cell line expressing fluorescent fibronectin (construct kindly provided by Erickson
laboratory, Duke University), alternatively, fluorescently labelled FN (Cytoskeleton Inc.) was
added to the culture.

Cell culture, transfection and inhibitors. Cells were cultured at 37ºC under 5% CO_2 with a
culture medium, high glucose D-MEM with 1% penstrep (Penicillin Streptomycin, Fisher
Scientific) supplemented with 10% Bovine Calf Serum (BCS, Sigma). Transfections were
performed with Lipofectamin 2000 (Invitrogen) using a standard protocol, and the following
constructs were used: mCherry-Lifeact, GFP-NMHC2A (nonmuscle myosin heavy chain 2A,
kindly provided by Ewa Paluch lab, UCL), RFP-zyxin (kindly provided by Anna Huttenlocher lab,

University of Wisconsin-Madison) or mCherry-MRLC2A (Addgene). For experiments with
inhibitors, ROCK inhibitor Y-27632 was used at a concentration of 10µM, microtubule de-
polymerizing agent nocodazole at 10µM, myosin-II inhibitor blebbistatin at 25µM, MLCK inhibitor
ML-7 at 10µM, F-actin depolymerizing agent latrunculin A at 1µM, Arp2/3 inhibitor CK666 at
50µM (all from Sigma) and lamellipodia growth promoter C8-BPA at 100µM (Nedeva *et al.*,
2013). Before drug addition, we performed a control acquisition of at least one hour. To prevent
flows, defocusing or potential damage of the CDM during manipulation, medium with drugs was
added to the running experiment without removing the medium to reach the target
concentration.
533
Time-lapse imaging and laser ablation, Optical set-ups, Electron Microscopy. We used a
Nikon Ti Eclipse inverted microscope equipped with a Lambda DG-4 (Shutter Instruments
Company), a charge coupled device (CCD) camera CoolSNAP HQ2 (Photometrics), a
temperature control system (Life Imaging Services) and, if needed, CO_2 control. The objectives
were the following: PhLL 20x (air, 0.95 NA, phase contrast, Nikon), a Plan Apo 60x objective
(oil, 1.40 NA, DIC, Nikon) and a x40 (air, 0.95 NA, Olympus) objective with a home-made
adapter to fit the Nikon microscope. Images were acquired with the NIS Elements software
(v3.10, SP3, Nikon) and then exported for further processing. We also used a CKX41 inverted
phase-contrast microscope (Olympus) with a cooled CCD camera (Hamamatsu). The system
was equipped with a temperature control (Cube box system) and 4x, 10x, 20x and 40x phase
contrast air objectives. For confocal imaging, we used a Leica TCS SP5-MP inverted
microscope equipped with a Leica Application Suite Advanced Fluorescence LAS AF
2.6.3.8173/LASAF 3.1.2.8785 acquisition system with hybrid detectors (HyD), photomultiplier
tube (PMT) and a heating system (Cube box system); with a HCX PL APO 63X oil objective (1.4
NA, Leica). Additionally, a Leica DMI6000 inverted microscope was used as a spinning disk,
equipped with a Andor iQ 1.9.1 acquisition system, Yokogawa CSU22 spinning disk unit and a
heating system (Tokai Hit Stage Top Incubator, INU incubation system for microscopes). A HCX
PLAPO 40x oil objective (1.25 NA, Leica) was used. The time between two frames ranged from
10s to 5min and typical exposure time was 100−200 ms. The software Imaris was used for
reconstructing and animating 3D data sets. For laser ablation, a Leica TCS SP8-MP based on a
Leica DM6000 CFS upright microscope was used, equipped with a Leica Application Suite
Advanced Fluorescence LAS AF 2.6.3.8173/LAS AF 3.1.2.8785 acquisition system with
photomultiplier tube (PMT) and hybrid detectors (HyD) and an environmental chamber for
temperature control (Cube box system). A 25X HCX IRAPO L water objective (0.95 NA, Leica)
was used and ablation performed with infrared pulsed laser (Coherent Vision II with pre-
compensation). FRAP module was used with point ablation with a wavelength set at 800 nm
and an exposition time of 100-200 ms. During experiments, parameters such as laser power
and gain were set to minimum to have the smallest cut possible while maintaining cell and CDM
integrity. 'Exploding' cells were discarded and analysis performed as described in the section
referring to Image Analysis.
564
Native CDMs with integrated cells were imaged by electron microscopy (EM). To obtain cross-
sections of the CDM, they were grown on Polystyrene sheets. The CDMs were fixed by
immersion in 2.5% glutaraldehyde and 2.5%paraformaldehyde in cacodylate buffer (0.1 M, pH

7.4), and post-fixed in 1% osmium tetroxide in 0.1M cacodylate buffer for 1 hour at 4ºC. The
samples were dehydrated through graded alcohol (50, 70, 90, 100%), and critical point dried
with hexamethyldisilazane. After mounting on stubs with conductive carbon adhesive tabs, the
CDMs were coated with gold-palladium in a sputter coater (BAL-TEC SCD 005). For imaging
along the z-axis, CDMs were cut and mounted upright with conductive carbon tape. Then they
were examined by XL SIRION 200 FEG SEM (FEI company, Eindhoven, The Netherlands).
574
Image Analysis. For quantification, the myosin intensity profiles were obtained on the raw
images of the selected time frames. Image J was used to obtain the intensity values along a 6
μm long line, with a line width of 20 pixels to average the intensity values. Data was further
normalized by the maximum value of intensity among all the frames analyzed. For visual
representation, images of myosin clusters were filtered with a median filter and the background
signal subtracted. To enhance the contrast of the clusters, a contrast-limited adaptive
histogram equalization (CLAHE) was applied. For KLT analysis, images were pretreated. In the
case of a z-stack, images were projected with average or maximal projection and outliers were
removed with Remove Outlier function of ImageJ. Then deformation was tracked in 2D. A
"pyramidal implementation" of KLT tracker method was used to detect deformation in the mesh
(Godeau, Delanoë-Ayari and Riveline, 2020). This method is based on Kanade-Lucas-Tomasi
algorithm and follows bright features from one image to another. Therefore, a textured patch
with high intensity variation in x and y is required. A multi-resolution pyramid of the image
intensity and its gradients are computed before tracking is performed. Then the KLT algorithm is
first applied to lower resolution image, where it detects coarse movement before a higher
resolution image is taken for fine movement detection. After having reached the maximum
iteration steps for all pyramid levels, the displacement of the feature is extracted (between two
frames). The Computer Vision Toolbox for MatLab was used with a customary written code with
number of features varying between 5000-10000 and a minimum distance from 8-14 px
depending on image size and resolution, making sure that features were sufficiently spaced.
Parameter window interrogation size was set to 40 px and maximal iteration to 20 px. The
number of pyramids was two for all calculations. For each image an overlay of displacement
vectors and phase contrast or fluorescent image of the cell was generated. Drift calculation was
performed with a maximum of 40 px features with a minimum distance of 8 px with a window
size of 20 px and one pyramid. The displacement due to drift was subtracted from the cell
induced displacement of the mesh.
601
Analysis of the contractile and extensile patterns over time. The displacement of the
meshwork calculated via the KLT feature tracker was projected onto a line going through the
cell axis in order to observe 1D matrix displacement and the heatmap of displacement plotted.
The matrix displacement amplitude is color coded in the heatmap. To highlight the cell position
in the heatmap, cell features such as nuclear front, back and cell tail were tracked and plotted in
the heatmap. To investigate recurring contractile and extensile patterns, the divergence of
matrix displacement along the cell axis was obtained. The divergence was averaged over a
region of 2 to 5 μm wide either at the cell back or the cell front, resulting in traces for the front
and the back of at least 30 minutes in duration with points every 30s. Average divergence was
subtracted to reduce background and autocorrelation performed via Matlab using the xcorr

function with coefficient normalization so that the autocorrelation at zero lag equals 1. To determine the period, the first peak next to zero with amplitude larger than 1 standard deviation was selected. Graphs where no peak could be identified were discarded. To compare matrix displacement at two distinct positions along cell axis, cross-correlation analysis was performed with the same parameters as for the autocorrelation. In this case the largest peak (either positive or negative) was extracted. Graphs where no peak could be identified were discarded. To obtain the period of cell speed, cell movement was tracked with the nucleus as reference point using Image J Manual Tracking Plugin. The trajectory was projected on the axis of migration and autocorrelation performed via Matlab. The xcorr function with coefficient normalization was used so that the autocorrelation at zero lag equals 1. The highest peak next to 0 with amplitude larger than 1 standard deviation was extracted. Graphs where no peak could be identified were discarded.

Elasticity CDM measurements by optical tweezers. CDM with fluorescent beads were mounted on a holder and placed on an inverted microscope (Olympus IX71). A Spectra Physics YAG laser (1064 nm) was used and focused through a high numerical oil immersion objective (Zeiss achromat x100 1.25 NA). We acquired the movies with a second objective (Olympus X40 0.6 NA associated with a CCD camera (DCC3240C, Thorlabs). The setup was controlled by LabView 9 (National Instruments). Beads were centered in the optical trap (Figure 1 – figure supplement 1e). The position of the CS (bottom of CDM) was registered to obtain the z position of the measured beads in the CDM. Stage was moved in 0.2 µm/s, covering a distance of 2−4 µm in x/-x and y/-y directions (Video 2). The laser power was calibrated with beads in solution. Subsequent data processing was performed with ImageJ bead Tracker Plugin and further post-processed with IgorPro Wavemetrics.

Statistical analysis. No statistical methods were used to predetermine sample size. The number of experiments (N) and the number of cells (n) included in every experiment can be found at the corresponding figure caption. Individual data points are shown when possible, accompanied by the mean value and error bars corresponding to the standard error of the mean. The statistical analysis was done with Graphpad Prism, pairwise t-tests, Kruskal-Wallis tests and One-way ANOVA for multiple comparisons were performed, and the outcomes are shown in the corresponding panels as well as indicated in the figure captions.

Appendix 1. Optical Tweezers

The optical tweezers setup has been described in Drobczynski et al.(Drobczynski *et al.*, 2009). The calibration of the stiffness as a function of the laser power was performed in PBS buffer. 2µm beads were diluted in PBS buffer and trapped. We, then, acquired a power spectrum (Helfer *et al.*, 2000; Harlepp *et al.*, 2017) on the quadrant photodiode and we extracted the trap stiffness. We checked the linear dependence between the stiffness and the laser power. The elastic modulus of the extracellular matrix is obtained by mixing 2 µm polystyrene beads in the matrix formation process. We follow two beads in the same field of view (Figure 1 – figure supplement 1f). One bead is trapped in the optical tweezers whereas the second is used as a reference. Then the piezoelectrical stage is moved and the 2 beads displacement is recorded

on the CCD camera. A post-acquisition treatment with ImageJ allows us to extract the
displacement expressed in nm of the 2 beads. These displacements are different one from the
other due to the optical restoring force. We haven't detected any hysteresis between back and
forth displacement on the same bead. This observation led us to think that the Extra-Cellular
Matrix in the ranges (frequency and amplitude) we were looking at was totally elastic with no
viscous behavior. The knowledge of the trap stiffness allows us to determine the forces exerted
on the trapped bead. The force curves obtained are linear in the regime we are exploring. We
show a linear relation between the applied force and the indentation allowing us to adjust these
curves with the linear model and extract the Elastic modulus E. We performed 37
measurements at different positions in the ECM and plotted the elastic modulus obtained over
the experiments. The average value of the elastic modulus that we found is around 50 Pa. We
assume that the average refraction index of the ECM is close to the refraction index found in
PBS. We, therefore, use the trap stiffness found in PBS to extract the forces in the ECM. We
move the sample with a piezoelectrical stage at a speed rate of 200 nm/s. The displacement of
the beads was recorded on the CCD camera at a framerate of 10 fps. The position of the
reference bead and the trapped bead were extracted using ImageJ and the particle analysis
plugin. We extracted the subpixel resolution of the center of mass positions of the beads over
time and calculated the beads displacement $r = \sqrt{(x - x_0)^2 + (y - y_0)^2}$. The displacement of
the bead in the trap was linked to the force applied to the ECM, and the difference between the
total displacement (reference bead) and the trapped bead was related to the ECM compression
(indentation). We used several models to extract the Young modulus from the experiments. The
Hertz model described in (Nawaz *et al.*, 2012) and (Yousafzai *et al.*, 2016) were used to
understand how to link the indentation to the displacement. Nevertheless, the models described
in these papers were linked to single cells and not to the fibers present in the medium. We, thus,
used the model described by (Laurent *et al.*, 2002) in the case the bead is totally immersed in
an infinite three dimensional medium. We modified the model to introduce the indentation
instead of the bead displacement in the trap that would have given a linear relation between the
stiffness and the Elastic modulus. Therefore, the linear relationship between the Elastic Modulus
and the force is: $F = 2\pi R E d$ with R the bead radius, E the Elastic Modulus, d the indentation and
F the measured force. The indentation d is given by $d = d_T - d_B$ where d_T is the reference bead
displacement and d_B the displacement of the bead in the trap.
687
688   **Appendix 2. Multipolar expansion**
689
As discussed in the main text, we quantify the cell-matrix interaction via the distribution of matrix
displacement rate around the cell, calling $u_i^{(n)}$ the component i at position n of the meshwork.
We then calculate the monopole vector $M_i = \sum_n u_i^{(n)}$, the dipole matrix $S_{ij} = \frac{D_{ij} + D_{ji}}{2}$ where
$D_{ij} = \sum_n \Delta_i^{(n)} u_j^{(n)}$ and the quadrupole matrix $Q_{ijk} = \sum_n \Delta_i^{(n)} \Delta_j^{(n)} u_k^{(n)}$, with $\Delta_i^{(n)}$ the i-th component
of the vector joining the cell centre (defined below) and the point n on the mesh. We also
compute the characteristic scale of matrix displacement rate defined as $\sum_n |u^{(n)}|$. The largest
component of the monopole vector is called the main monopole, M, and the largest eigenvalues
of the dipole and quadrupole tensors are defined as the main dipole, D, and the main

quadrupole, Q. The corresponding eigenvectors are defined as the main dipole and quadrupole
axes.
700
A cell that migrates spontaneously (i.e. in absence of external forces) can be viewed as a force-
free body, hence in the absence of inertia the sum of all the traction forces add up to zero
(Tanimoto and Sano, 2014). Thus, for a homogeneous material under linear elasticity, the
monopole of displacement rate should be zero. In our experiments, 3D imaging is challenged by
a limited and asymmetric field of view which leads to a non-zero value of the monopole. To
reduce these imaging asymmetries, the traction, monopole, dipole and quadrupole are
computed and averaged over discs (Figure 3 – figure supplement 1) of increasing radius
$R_k, k = 0, 1, \dots M$ starting from a minimum radius $R_0 \simeq 20\,\mu m$ and up to a maximum radius R_M
defined as the largest radius such that the circular region is fully contained within the boundaries
of the experimental images. To minimize the spurious monopole, the center of the disc is varied
around the apparent cell center (obtained from cell tracking) and the location for which the
monopole is minimum is adopted as the center of the discs on which the dipoles and
quadrupoles are computed. This is done at every time step. Note that matrix heterogeneities
could also possibly contribute to a non-zero monopole. Figure 3 – figure supplement 2 shows
histograms for difference of orientation between the main dipole axis and the direction of motion
for three examples of migrating cells, showing a clear peak near zero angle difference. In
addition to cellular noise, the rather large spread of these data is also explained by the fact that
the major dipole is a fluctuating quantity which frequently crosses zero, at which point the
largest dipole is the minor dipole, which is typically oriented perpendicular to the direction of
motion.
721
Additional examples of cycles for migrating and non-migrating cells are shown in Figure 3 –
figure supplement 3a. As in the main text, the cycles shown for migrating cells are obtained by
first identifying intervals of time with clear oscillating behavior in the speed and focusing on that
time interval when we compute the multipolar expansion. For cells which are non-migrating, we
cannot apply this scheme as we have no notion of oscillating speed, thus the choice in Figure 3
– figure supplement 3a is somehow arbitrary. Nonetheless, we find that the areas of cycles for
non-migrating cells are systematically smaller when compared to the areas of migrating cells.
Importantly, the comparison between the absolute values of the multipoles of displacement
rates between different cells is not straightforward, as these measures depend on the spatial
and temporal resolution of the movies, which may vary from cell to cell. To support our claim
that the main difference between migrating and non-migrating cells is the existence of a phase
shift and not the cell's ability to exert traction forces, we show in Figure 3 – figure supplement 3b
the average of the absolute value of the rate of deformation field for migrating and non-migrating
cells. This quantity is obtained for each cell by computing the sum of the displacement rate
amplitude within a disc, divided by the number of measurement points within the disc, average
over disc radii spanning the accessible range for each cell, and averaged over time. Although
this quantity varies from cell to cell, there is no significant difference (p = 0.2766) between
migrating and non-migrating cells. On the other hand, the area enclosed by the cycle in the
dipole/quadrupole phase space is systematically higher for migrating than non-migrating cells.
Figure 3 – figure supplement 3 c show the cycle area, defined as the area $A(n_1, n_s) =$

$\sum_{i=n_1}^{n_2-1} I_{i+1,i} + I_{n_1,n_2}$ with $I_{i+1,i} = \int_i^{i+1} Q(D)dD = \frac{1}{2}(Q_{i+1} + Q_i)(D_{i+1} - D_i)$, where D_i and Q_i are the

dipole and quadrupole values at the ith time frame and n_1 and n_2 are the starting and ending

time frames. Both the absolute value of this quantity in physical units and the fraction (in %) of

normalized the area of the rectangle tightly enclosing the cycle are shown.

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Competing interest

764 The authors declare no competing interests.

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Figure captions

Figure 1. **Key players in cell motility. (a)** Left panel (and Video 1): A cell deforms the
fibronectin (FN) network when migrating (FN in yellow and mCherry-LifeAct for actin filaments in
red). Right panel: Enlargement of the white windows of the left panel. Black arrows highlight
displacement of fibers due to cell movement. **(b)** Overlay of phase contrast image and KLT
calculation of mesh displacement (green arrows - with scale bar shown, arrows indicate
displacement between two consecutive frames, Δt=5 min) with local contraction and extension
regions indicated with white windows. **(c)** Myosin clusters (upper panels) form locally within cells
and are correlated with local contraction: KLT deformation (green arrows, arrows indicate
displacement between two consecutive frames, Δt=30s) and myosin-mCherry signal (middle
panels). Average myosin intensity profile along the red dashed-square of the frames shown in
the upper panels (lower panels). **(d)** α-tubulin staining of a cell inside CDM. Microtubules extend
from the centrosome to the periphery of the cell (see also Video 4). Scale bars: (a) 25 μm (10
μm in the enlargements) (b,c,d) 10 μm.

Figure 2. **Dynamics of matrix deformation for migrating and non-migrating cells. (a)**
Snapshots overlaying phase contrast images and KLT calculation of matrix rate of deformation
(green arrows indicate displacement between two consecutive frames, Δt=1 min) showing a
contraction/extension center, scale bar 10 μm, time in minutes. **(b-c)** Schematics of the
alternating phases of contraction and extension for a non-migrating cell (b) and a migrating cell
(c). **(d-e)** Heatmap of the divergence of the corresponding matrix displacement. Contractile and
extensile force dipoles correspond to blue and yellow spots, respectively. Non-migrating cells
(d) show two oscillating dipoles (their centers are approximately indicated by the solid black
lines), while migrating cells (e) show a different spatio-temporal pattern with sequences of
alternating positive and negative divergence. The blue and red solid lines in (e) indicate the two
sides of the nucleus. **(f)** Correlation function of the contraction-extension time series at the back
of a non-migrating cell, with a first peak at ≈ 5 min. Time trace 36 min. **(g)** Average periods of
contraction-extension cycles: 4.8±1.5 min for the front, 7.5±2.0min for the back and 11.0±1.9
min for nocodazole treated cells. Error bars represent standard error of the mean (SEM). **(h)**
Correlation function of the divergence at the back of a migrating cell, with a first peak at ≈ 10
min. Time trace 100 min. **(i)** Average period of the contraction-extension cycles for migrating
cells of 8.5±1.8 mins for the front and 7.8±1.4 mins for the back. **(j)** Typical cross-correlation
function between back and front divergence for a migrating cell and a non-migrating cell. Time
trace non-migrating cell 36 min and migrating cell 100 min. **(k)** Distribution of the values of the
time-lag for migrating and non-migrating cells. Distribution of time-lag for migrating cells is
statistically significant to the time-lag for non-migrating cells (p = 0.0246, Kruskal-Wallis test).
Error bars represent SEM. t-tests show differences in oscillation periods between motile, non-
motile and Nocodazole treated cells are not statistically significant (with n_{mot} = 13 motile cells,
n_{nomot} = 6 non-motile cells, n_{Noco} = 6 and N > 3 biological repeats).

Figure 3. **Multipole analysis of the matrix deformation rate. (a)** Snapshots of a cell with:
matrix rate of deformation, green arrows, the main dipole axis, blue, the axis of the cell motion,
red. **(b)** Schematic representation of dipoles (D) and quadrupoles (Q) of the 1D matrix
displacement (rate) distributions. The distribution on top has non-zero dipole but vanishing
quadrupole, and that on the bottom has vanishing dipole and non-zero quadrupole. **(c)** Time
series of the main dipole, blue, and quadrupole, magenta, - projected on the cell axis - for a
migrating cell (squares) and a non-migrating cell (circles), sampling approximately 1/10 of the
duration of the entire experiment. **(d-e)** Cell trajectory in the dipole/quadrupole phase space for
a migrating cell (d) and a non-migrating cell (e). The migrating cell follows a cycle with a finite
area and the non-migrating cell does not. The error bars are obtained following the procedure
described in Appendix 2. The individual cycles for different radii are shown in light gray. **(f)**
Snapshots of a cell which in the course of the same experiment displays a transition from
migrating to non-migrating behavior (LifeAct in red and fibronectin in yellow), scale bar 10 µm.
(g) Cell positions in the x-y plane (blue and orange curves) showing a transition from migrating
to non-migrating phase. **(h)** Trajectories in the dipole/quadrupole phase space for three different
time intervals showing cycles with finite area in the migrating phase and with vanishing area in
the non-migrating phase (see also Video 8).

Figure 4. **Persistent speed is related to the period of oscillations. (a)** Schematics of dipoles
distribution highlighting quantities used in the theoretical model: two dipolar units ("A" and "B")
made up of disks of radius a, through which cells exert traction forces on the extracellular
environment. The dipoles, at distance r apart, oscillate with period T, with minimum amplitude D
and a maximum amplitude D + d. **(b)** Model dynamics. Left: Alternate phases of
extension/contraction are imposed to the two dipoles, defining a cycle ("1, 2, 3, 4, 1...") that is
not time-reversible. Right: the extension/contraction rates of dipole "A" and "B" are shown in red
and black, respectively, in unit d/T. The cell velocity, calculated using the model discussed in
(Leoni and Sens, 2015), is shown in green in the same units. It oscillates between positive and
negative values - with a non-vanishing mean - with a period equal to that of individual dipoles.
(c) Typical plot of the experimentally measured instantaneous speed of a migrating cell over
time, showing oscillation with a non-vanishing mean. **(d)** Persistent speed as a function of
speed period for control cells and cells treated with specific inhibitors: 10µM ROCK inhibitor Y-
27632; 10µM MLCK inhibitor ML-7; 100µM lamellipodia growth promoter C8-BPA and 50µM
Arp2/3 inhibitor CK666. Error bars derived from acquisition time in x and pixel resolution in y,
both divided by two. Each data point corresponds to one cell (see Figure 4 – figure supplement
1 for the number of cells). The plot displays a decay consistent with a power law. The
continuous lines show the fits for $V \sim 1/T$ (dark blue) and $V \sim 1/T^2$ (magenta), following Eqs.
(1,2) for WT cells.

Figure 5. **Cell motion is triggered by means of laser induced force dipoles. (a)** Schematic
of laser ablation experiment. **(b)** (Left panel: LifeAct, middle panel: phase contrast and KLT,
arrows indicate displacement between two consecutive frames, Δt=10s). Ablation at the back of
the cell (white arrow) immediately followed by an extension, and later by a contraction of the
matrix, (both highlighted using white square window). Scale bar LifeAct: 10 µm KLT: 20 µm.
Right panel. Bottom: Plot of the displacement rate along the cell axis at different timepoints

(colour coded) showing extension and contraction. Top: Heatmap of displacement rates
indicating the initial extension and the subsequent contraction. **(c)** Top: sequence of snapshots
during laser ablation on a cell expressing mCherry-LifeAct. Intensity drops locally immediately
after the cut, followed by a local recruitment of actin, scale bar 20 µm, scale bar in zoom 5 µm.
Bottom: the intensity heatmap reveals a focused actin flow (see also Video 13). As shown in the
deformation map, the contraction precedes this flow. **(d)** Consecutive ablations (indicated with
white arrows) mimic contraction-extension cycles at the front and back of the cell. Ablation is
performed in the following order: at the cell back, at the front and then at the back again. In all
panels, scale bar 10 µm and time in mm : ss. Note cell motion to the right (see also Video 14),
scale bar 10 µm. The cell is outlined in red and the back of the nucleus with a blue dashed line.
1038
Figure 1 – figure supplement 1. **Characterization of CDM. (a)** Schematics of the CDM
preparation. **(b)** Electron microscope images of the top layer (x−y) and the side view (x−z) of
CDM; scale bars 10 µm. (c) Cells are embedded in the CDM. Top: schematic; middle: a typical
image with actin in red and fibronectin in yellow; bottom: cell thickness is 7.8±0.3 µm compared
to CDM thickness 12.8±0.7 µm. The boxplot encloses 50% of the data around the median, the
black line represents the mean of the data. The upper/lower whisker extends from the hinge to
the largest/smallest value no farther than 1.5 * IQR from the hinge, respectively (where IQR is
the interquartile range, or distance between the first and third quartiles). T-test CDM thickness
vs cell thickness p<0.0001 and error bars represent SEM. **(d)** Typical image of fibronectin
labeling within CDM. Top, view in the x−y plane (scale bar:20µm) and, bottom, side view in the
x−z plane (scale bar: 10 µm). **(e)** Scheme of the experiment where 2 beads are embedded in
the Extra-Cellular Matrix and in the same field of view of the camera. The gray bead is the
reference bead as the blue one is trapped with the optical tweezers. The sample is moved with
the piezoelectrical device. The sample displacement is linked to the reference bead
displacement whereas the bead in the trap shows a differential movement linked to the traps
restoring force and the matrix compression. **(f)** Plot of the displacement of the bead in the trap
(red) and the reference bead (black) as a function of time. The inset shows the displacement of
the trapped bead when moved back and forth. **(g)** Plots of the force at different laser power as a
function of time. **(h)** Extraction of the Young modulus from the force/displacement curve. **(i)**
Graph of the extracted Young modulus values obtained over 37 experiments at different height
z and laser power. The average value is 53 Pa. **(j)** The CDM keeps its shape over time; CDM
was visualized before at t= 0 (red) and after the passage of cells at t= 24h (green); the merged
image (last panel) shows that the CDM network remains unchanged. Scale bar: 10µm.
1062
1063   Figure 1 – figure supplement 2. **Cells deform the CDM network.** FN in yellow and cell
1064   expressing RFP-zyxin, scale bar 25µm. Right side shows a blow up of one of the zones
1065   highlighted by the squares, scale bar 5µm. White arrows show the movement of a FN fiber,
1066   taken at two consecutive instants of time. Bottom panels: The enlargement of a pore behind the
1067   cell suggests a local pulling force by the cell. Time in min.
1068
Figure 1 – figure supplement 3. **Different types of fibroblasts generate contractile-extensile**
regions on either side of the nucleus in CDMs. **(a)** Top: Snapshot of Mouse embryonic
fibroblast (MEF) embedded in a CDM. Scale bar 50 µm. Overlay of phase contrast image and

KLT calculation of the mesh displacement (green arrows - with scale bar shown, arrows indicate
displacement between two consecutive frames, Δt=3 min) with local contraction and extension
regions indicated with white windows while the cell migrates. **(b)** Top: Snapshot of Rat embryo
fibroblast 52 (REF52) cell embedded in a CDM. Scale bar 50 μm. Overlay of phase contrast
image and KLT calculation of mesh displacement (green arrows - with scale bar shown, arrows
indicate displacement between two consecutive frames, Δt=5 min) with local contraction and
extension regions indicated with white windows while cell migrates. **(c)** Left - Snapshots of the
formation of a cytoplast (Video 10): A protrusion of a cell detaches from the cell. Scale bar 10
μm. Middle - Kymograph of a cytoplast over time. The nucleus free cell performs an oscillatory
motion. Red arrows indicate points of switching direction. Vertical scale bar 10 min, horizontal
scale bar 10 μm. Right - Plot of the displacement of the cytoplast along the x-axis. Several
turning points can be observed. Red arrows on turning points correspond to the red arrows in
the kymograph. Histogram of frequency of periods of persistent motion between turning points
for various cytoplasts. Average period 36.0±2.4 min. Error SEM. N > 3, n=6.

Figure 2 – figure supplement 1. **Analysis pipeline. (a)** Overlay of phase contrast image and
KLT calculation of mesh displacement (green arrows indicate displacement between two
consecutive frames, Δt=1 min) of a NIH3T3 fibroblast in CDM. A contraction can be observed at
the front of the cell. **(b)** Heatmap of the matrix displacement along time for a migrating cell. Red
line denotes front of nucleus, and black back of the nucleus. **(c)** Heatmap of divergence
corresponding to matrix displacement in (b). Contractile and extensile force dipoles correspond
to blue and yellow spots, respectively. **(d)** Heatmap of the matrix divergence in the cell
framework. It is centered at the back of the nucleus to delimit the front and back of the cell.
Black squares indicate the area where average divergence is calculated. **(e)** Plot of average
divergence calculated on a centered heatmap of divergence for front (red) and back (blue)
region of the cell. **(f)** Autocorrelation of the divergence signal at front (red) and back (blue) of a
cell. **(g)** Cross-correlation calculation between front and back divergences. A negative peak is
visible at 3 min. Time trace 50 min.

Figure 2 – figure supplement 2. **Divergence amplitudes**. Plot of average divergence
amplitudes at front and back of migrating (n=13) and non-migrating cells (n=6), N>3. Migrating:
back 0,010±0,005 min^{-1} and front 0,009±0,005 min^{-1}. Non-migrating: back 0,004±0,001 min^{-1}
and front 0,006±0,002 min^{-1} (Mean±SEM). Outliers were discarded. t-tests show differences in
oscillation periods between motile, non-motile and Nocodazole treated cells are not statistically
significant (p-values for each comparison are shown).

Figure 3 – figure supplement 1. **Method to compute the multipolar terms**. The same cell of
Figure 3f in the course of the same experiment shows a transition between migrating phase and
non-migrating phase, Figure 3g. (Left): experimental image showing a cell in light blue, and the
vector field restricted to a circular region used to compute the multipoles. The center (red cross)
is obtained starting from the cell center position and searching for the coordinates (X_*, Y_*) that
minimize the monopole term. We consider regions enclosed by different radii R_k, with k= 1, 2,...
and compute the multipoles in each of these regions. We then compute the average values of
the multipolar terms and obtain error bars as the standard deviations over all these regions.

Insets: characteristic scale of matrix displacement rate, computed as the average of the
absolute value of the rate of deformation field within the circular region. This quantity is slightly
smaller during the non-migrating phase than during the migrating phase but the two values are
comparable. (Right): the cell does not move because the vector field has changed compared to
the migrating phase, showing now mainly a dipolar field.
1121
1122 Figure 3 - figure supplement 2. **Quantification of cell and dipole orientation.** Histograms of
1123 the angle difference $\delta\theta$ between the main dipole axis and the direction of motion (blue and red
1124 axes, respectively, in the top-left panel). The full histogram (yellow) is a merge of data from
1125 three examples corresponding to Figure 3 d, Figure 3 h and the leftmost migrating cell of Figure
1126 3 - supplementary figure 3 (individual histograms are overlaid in different colors).
1127
Figure 3 – figure supplement 3. **Quantification of cell motion. (a)** Examples of cell trajectories
represented in the dipole/quadrupole phase space**.** Comparison between cycle curves obtained
in different experiments for different migrating (top panels) and non-migrating (bottom panels)
cells. We observe a variability in the traction forces for both migrating and non-migrating cells,
but we exclude that non-migration is due to lack of traction (compare leftmost top and bottom
panels). **(b)** Average of the matrix displacement rate (same as the inset of Figure 3 – figure
supplement 1 averaged over time) for the six cells shown in **(a)**. Statistical significance of the
differences between the conditions was assessed by a t-test (p = 0.2766). **(c)** Quantification of
the area enclosed by the cycles in the dipole/quadrupole space. The left panel shows the
absolute area in physical units, and the right panel shows the normalized area: the fraction of
the area of the rectangle fitting the trajectory of the cycle (see Appendix 2). Statistical
significances of the differences between the conditions were assessed by a Kruskal-Wallis test
(left panel – p = 0.0177) and a t-test (right panel – p = 0.0431).
1141
Figure 4 – figure supplement 1. **Cell motion in CDM is modified in the presence of specific**
inhibitors. Typical cell morphologies and typical trajectories of cells migrating over 5 hours.
Bright field and LifeAct labeling. **(a)**, Control (n=49). **(b)**Blebbistatin (n=31). **(c)** Y-27632 (n=9).
(d) ML-7 (n=24). **(e)** Latrunculin A. **(f)** C8-BPA (n=21). (**g**) CK666 (n=19). **(h)** Nocodazole. **(i)**
Persistent speed for control and cells treated with specific inhibitors which show oscillatory
behavior. Persistent speeds are: 0.79±0.44 µm/min (control, n=24); 0.25±0.10 µm/min (100µM
C8-BPA, n=7); 0.40±0.03 µm/min (50µM CK666, n=6); 0.40±0.12 µm/min (10µM ML-7, n=7)and
0.42±0.09 µm/min (10 µM Y-27632, n=9); and (**j**) Average of the period of the cell speed
calculated by autocorrelation analysis of speed projected on axis of migration: 17±8 min
(control, n=24); 29±10 min (100µM C8, n=7); 27±9 min (50µM CK666, n=6); 22±9 min (10 µM
ML-7, n=7) and 26±7 min (10µM Y-27632, n=9); On-way ANOVA with Tukey's test for multiple
comparisons. The p-value is indicated on the graph, otherwise differences were non-significant.
Scale bars 25µm.
1155
Figure 4 – figure supplement 2: **Simulated cell trajectories in the dipole/quadrupole phase**
space. (a) Reproduction of the idealized model of cell dynamics (from Figure 4b) showing
alternate phases of dipole contraction/extension at the two cell ends. Sinusoidal oscillations
have been chosen in this example **(b)** Cell trajectories in the phase space. Dipoles and

quadrupoles of the strain rate are computed assuming a viscous response of the environment.
In the non-migrating case, the two dipoles oscillate in phase, leading to a cycle of vanishing
area (vanishing quadrupole). In the migrating case, the dipoles oscillate with a fixed phase shift
$\psi = \pi/2$, leading to a cycle of finite area. In both cases, the blue trajectories are without noise
and the red trajectories with added noise (random independent variation of the oscillation
dynamics of the two dipoles). Error bars are computed as in Figure 3 – figure supplement 1.
1166
Figure 5 – figure supplement 1: **Cell motion is triggered by means of laser induced force**
dipoles. (a) Cell expressing mCherry-LifeAct and GFP-NMHC show increased signal following
laser cut indicated with white dashed squares. Inset shows region of cut. Scale bar 20 µm (left)
and 10 µm (right). **(b)** Sequential cuts alternating the back and the front of the nucleus in a
polarized cell. Displacement over time of cells ablated 2-3 times consecutively with a time lag of
6 minutes. (left) and with a time lag of 10 minutes (right). Dashed lines indicate the moment of
each cut starting with cut 1 at time 0 and with different time lags, 6 min (blue) and 10 min
(orange) in respective plots. n=5 cells from N=3 experiments. (c) Sequential cuts at the front of
the nucleus in a polarized cell. Displacement over time of cells ablated 3 times consecutively at
the front of the nucleus with a time lag of 5 minutes (left) and 10 minutes (right). Dashed lines
indicate the moment of each cut starting with cut 1 at time 0. n=4 cells from N=2 experiments.
1178
1179 **Movie captions:**
1180
1181 Video 1: NIH3T3 fibroblast transfected with mCherry-LifeAct deforms the fibronectin network in
1182 yellow while moving, scale bar 20 µm, time in hh:mm.
1183
1184 Video 2: CDM is elastic, as shown by optical tweezer characterization, time in mm:ss.
1185
1186 Video 3: Cells motion in 3D with CDM and the associated focal contacts dynamics fibronectin in
1187 yellow and zyxin in red, time in hh:mm:ss.
1188
1189 Video 4: Microtubule asymmetric distribution (left) is associated with cell polarity during motion,
1190 time in hh:mm.
1191
1192 Video 5: Cell deforms the CDM, time in hh:mm.
1193
1194 Video 6: Formation of myosin clusters simultaneously to contraction, time in mm:ss.
1195
1196 Video 7: Another example of cell motion in CDM, scale bar 25 µm, time in hh:mm.
1197
1198 Video 8: Phase-shift between local dipoles is associated with cell motion; cell motion (left,
1199 LifeAct red), fibronectin network deformation (center yellow), merge, time in hh:mm:ss.
1200
1201 Video 9: Cell motility in the presence of nocodazole added at time 0, time in hh:mm, scale bar
1202 25 µm.
1203

1204 Video 10: Nucleus free cell forms and shows oscillatory motion in CDM. Time in hh:mm and
1205 scale bar 25 μm.
1206
1207 Video 11: Cell motility in the presence of blebbistatin added at time 0, time in hh:mm, scale bar
1208 25 μm.
1209
1210 Video 12: Cell motility in the presence of latrunculin A added at time 0, time in hh:mm, scale bar
1211 25 μm
1212
1213 Video 13: Local laser ablation triggers the local recruitment of actin and local contraction, time in
1214 mm:ss.
1215
1216 Video 14: Induced dipoles by local laser ablations (indicated by arrows) trigger cell motion, time
1217 in mm:ss.
1218
1219 **Source data**
1220
1221 **Figure 1 – source data 1: (i)** Values for the height and the thickness of the CDM. **(ii)** Raw
1222 values of the CDM's Young's modulus. **(iii)** Values for the cytoplasts' period of oscillation.
1223
1224 **Figure 2 – source data 1: (i)** Raw values for the periods of non-migrating and nocodazole
1225 trated cells. **(ii)** Raw values fot the periods of migrating cells. **(iii)** Front-back pahse shift for
1226 migrating and non-migrating cells. **(iv)** Raw values for the amplitude of the divergence peaks.
1227
1228 **Figure 3 – source data 1: (i)** Raw data for the dipole and quadrupole moments in panel figure
1229 3d. **(ii)** Raw data for the dipole and quadrupole moments in panel figure 3e. **(iii)** Raw data for
1230 the angular distibution.
1231
1232 **Figure 4 – source data 1: (i)** Data shown in the panel Figure 4d, persistent speed vs period. **(ii)**
1233 Persitent speed for WT cells, C8-BPA treated cells, CK666 treated cells, ML-7 treated cells and
1234 Y27632 treated cells. **(iii)** Period of WT cells, C8-BPA treated cells, CK666 treated cells, ML-7
1235 treated cells and Y27632 treated cells. **(iv)** Dipole and quadrupole moments of simulated cells
1236 (migrating and non-migrating).
1237
1238 **Figure 5 – source data 1: (i)** migration trajectories of cells which are exposed to laser ablation
1239 induced contractions.

a
Cells produce and secrete matrix proteins

Removing cells by lysis: CDM

b
Top View

Side View

Polystyrene sheet   Surface of CDM

c
Side View

Thickness (µm)

CDM   Cell

****

d
Top View Projection

Side View

e
Sample Displacement   Reference bead Displacement

Optical Trap   Trapped bead
                      Indentation

f
Displacement (µm)
— Bead in the trap
— Reference Bead

Elastic   Indentation

Displacement Ref

Piezo moving   Trapped bead

Time (s)

g
Force (pN)
— P=700mW
— P=1710mW
— P=2050mW

Time (s)

h
Force (pN)

E=52.27 Pa

Displacement (nm)

i
Elastic modulus (Pa)

j
FN Ypet

Before   After   Overlap
0h   24h   Δt

RFP zyxin

0   25   60

RFP zyxin/Fibronectin

Front

0   25

Center

25   60

Back

0   60

← Position at initial frame of observation

Figure 4

a

Dipole A Dipole B

①

amplitudes

②

③

④

①

time