**The choices we make and the impacts they have: Machine learning and species delimitation in North American box turtles (*Terrapene* spp.)**

**Running title:** Box Turtle machine learning & species delimitation

**Authors:**

Bradley T. Martin[1,5,*], Tyler K. Chafin[1], Marlis R. Douglas[1], John S. Placyk Jr.[2,6], Roger D. Birkhead[3], Chris A. Phillips[4], Michael E. Douglas[1]

[1]Department of Biological Sciences, University of Arkansas, Fayetteville, Arkansas 72701, USA; Email: (BTM) btm002@uark.edu (send reprint requests to this address); (TKC): tkchafin@uark.edu; (MRD): mrd1@uark.edu; (MED): med1@uark.edu.

[2]Department of Biology, University of Texas, Tyler, Texas, 75799, USA; Email: japlacyk@gmail.com

[3]Alabama Science in Motion, Auburn University, Auburn, AL 36849, USA; Email: birkhrd@auburn.edu

[4]Illinois Natural History Survey, Prairie Research Institute, University of Illinois, Champaign, IL 61820; Email: caphilli@illinois.edu

**Correspondence:** BTM

Present Addresses:

[5]Global Campus, University of Arkansas, 2 E. Center St., Fayetteville, Arkansas 72701, USA

[6]Science Division, Trinity Valley Community College, Athens, Texas 75751, USA

**Abstract**

Model-based approaches that attempt to delimit species are hampered by computational

limitations as well as the unfortunate tendency by users to disregard algorithmic assumptions.

Alternatives are clearly needed, and machine-learning (M-L) is attractive in this regard as it

functions without the need to explicitly define a species concept. Unfortunately, its performance

will vary according to which (of several) bioinformatic parameters are invoked. Herein, we gauge

the effectiveness of M-L-based species-delimitation algorithms by parsing 64 variably-filtered

versions of a ddRAD-derived SNP dataset involving North American box turtles (*Terrapene*

spp.). Our filtering strategies included: (A) minor allele frequencies (MAF) of 5%, 3%, 1%, and

0% (=none), and (B) maximum missing data per-individual/per-population at 25%, 50%, 75%,

and 100% (=none). We found that species-delimitation via unsupervised M-L impacted the

signal-to-noise ratio in our data, as well as the discordance among resolved clades. The latter may

also reflect biogeographic history, gene flow, incomplete lineage sorting, or combinations thereof

(as corroborated from previously observed patterns of differential introgression). Our results

substantiate M-L as a viable species-delimitation method, but also demonstrate how commonly

observed patterns of phylogenetic discord can seriously impact M-L-classification.

**Keywords:** ddRAD, discordance, filtering, missing data, species tree, VAE

# 1 INTRODUCTION

Species are recognized as the currency of biodiversity, yet their context has been hampered by numerous inconsistencies in how they are perceived, including subjective interpretations of what constitutes a species. This in turn creates downstream issues for conservation (Mace 2004), where spurious 'splitting' or 'lumping' impede an equitable allocation of limited resources. Although genomic approaches based on the multispecies coalescent (MSC) are promising and have been commonly applied to species problem (Allendorf *et al.* 2010), conflicting genome-wide signals are widely apparent due to incomplete lineage sorting (ILS) and gene flow (Funk & Omland 2003). Two MSC methods, BPP and BFD* (Yang & Rannala 2010; Leaché *et al.* 2014), seemingly over-split in the presence of strong population structure (Sukumaran & Knowles 2017) or with continuous geographic distributions (Chambers & Hillis 2019). Both are also computationally limited when applied to large datasets. As model complexity and data expand concomitantly, so also do: 1) efforts required to computationally explore appropriate parameter space; and 2) the probabilities that models fail to accommodate process. Herein, we explore alternative approaches for the parsing of high-dimensionality data by evaluating the performance of recently developed machine-learning (M-L) algorithms and classificatory approaches in successfully adjudicating variably-filtered versions of a ddRAD-derived SNP dataset.

"Unsupervised" machine learning methods (UML) are of particular interest for group delimitation, in that they do not require *a priori* designations to train the classification model. Several UML classifiers lend themselves to species delimitation, including: Random Forest (RF; Breiman 2001), t-distributed stochastic neighbor embedding (T-SNE; Maaten & Hinton 2008), and variational autoencoders (VAE; Kingma & Welling 2013). Each has distinct advantages: RF

uses randomly replicated data subsets to develop 'decision trees' that are subsequently aggregated

(='forest'), with classificatory decisions parsed as a majority vote. The random sub-setting

approach is robust to correlations among features (=summary statistics or principal components

used for prediction) as well as model overfitting (i.e., over-training the model such that it does not

generalize to new data). One stipulation is that features must lack undue noise (Rodriguez-

Galiano *et al.* 2012). By contrast, T-SNE creates clusters in reduced-dimension space, typically a

2D plane distilled from multi-dimensional data, and as such conceptually resembles principal

components analysis (Maaten & Hinton 2008).

On the other hand, VAE employs neural networks to 'learn' patterns within

multidimensional data extracted from a compressed, low-dimensionality (='encoded')

representation. Again, an ordination technique is simulated but without imposing

linear/orthogonal constraints, such that a statistically interpretable result emerges that is

appropriate for highly-complex data (Derkarabetian *et al.* 2019).

Some algorithms are robust to gene flow (Derkarabetian *et al.* 2019; Newton *et al.* 2020;

Smith & Carstens 2020), yet a greater number of tests must be performed across diverse systems

so as to understand which parameters impinge upon performance. Potentials include: Data

quantity (Newton *et al.* 2020), the proportion missing (Mussmann *et al.* 2020), as well as its

evolutionary complexity (Austerlitz *et al.* 2009). Here, we employ species-delimitation

algorithms relative to coalescent methods such as BFD* (Leaché *et al.* 2014) as vehicles to parse

a taxonomically recalcitrant biodiversity clade. Included algorithms are: Process-based RF

(DELIMITR; Smith *et al.* 2017; Smith & Carstens 2020) and unsupervised RF, T-SNE, and VAE,

as implemented in Derkarabetian *et al.* (2019).

**1.1 Species concepts and their evolution in *Terrapene***

North American box turtles (Emydidae: *Terrapene*) are a primarily terrestrial and include five

currently recognized species (Minx 1996; Iverson *et al.* 2017): Eastern (*Terrapene carolina*),

Ornate (*T. ornata*), Florida (*T. bauri*), Coahuilan (*T. coahuila*), and Spotted (*T. nelsoni*), with a

sixth (*T. mexicana*) proposed (Martin *et al.* 2013). *Terrapene carolina* is split into two subspecies

east of the Mississippi River and south through the Gulf Coast [Woodland (*T. c. carolina*) and

Gulf Coast (*T. c. major*); Figure 1]. *Terrapene mexicana* contains three subspecies: Three-toed

(*T. m. triunguis*); Mexican (*T. m. mexicana*); and Yucatan (*T. m. yucatana*) that range across

southeastern and midwestern United States, the Mexican state of Tamaulipas, and the Yucatan

Peninsula. Ornate (*T. ornata ornata*) and Desert (*T. o. luteola*) inhabit the Midwest and

Southwest U.S. and Northwest México, while Southern and Northern Spotted box turtles (*T.*

*nelsoni nelsoni* and *T. n. klauberi*) occupy the Sonoran Desert in western México. *Terrapene*

*coahuila* is semi-aquatic and restricted to Cuatro Ciénegas (Coahuila, México), while Florida box

turtle occurs in Peninsular Florida.

      Morphological analyses delineate *T. carolina*/*mexicana* as a single species, sister to *T.*

*coahuila* (Minx 1992, 1996), as supported by genetic studies (Feldman & Parham 2002; Stephens

& Wiens 2003). Martin et al. (2013) elevated *T. mexicana*, and nested *T. coahuila* within *T.*

*carolina*. *Terrapene carolina carolina* is sister to *T. c. major*/*T. coahuila*, although gene flow was

suspected with *T. c. major*. *Terrapene carolina major* was recently demoted to an intergrade with

subsequent loss of subspecific status (Butler *et al.* 2011; Iverson *et al.* 2017). However a recent

genomic study supported pure *T. c. major* populations in Florida and Mississippi (Martin *et al.*

2020). Similarly, *T. bauri* (formerly *T. carolina bauri*) was recently elevated (Butler *et al.* 2011;

Iverson *et al.* 2017), but more substantial evidence is needed (Martin *et al.* 2013). For clarity, we

retain the nomenclature of Martin *et al.* (2013, 2014), with *T. c. major* and *bauri* representing *T.*

*carolina* subspecies.

One explanation for the enigmatic classification of *T. carolina* and *T. mexicana* involves

hybridization (Auffenberg 1958, 1959; Milstead & Tinkle 1967; Milstead 1969). Some

researchers (Fritz & Havaš 2013, 2014) interpreted reproductive semi-permeability as

justification sufficient to collapse the southeastern taxa. However, their classificatory status must

be re-examined, as indicated by results modulating the species boundaries of southeastern

*Terrapene* (Martin *et al.* 2020).

Taxonomic disputes in *Terrapene* highlight the philosophical disparity among species

definitions [e.g., biological (Mayr 1963) versus phylogenetic (Eldredge & Cracraft 1980)]. The

approach advocated herein acknowledges that operational criteria among concepts are intimately

related. Specifically, reproductive barriers (through time) beget genealogical concordance, while

contemporary evaluations of gene flow are contextualized via phylogenetic/phylogeographic

perspectives (Avise 2000a; b). We thus subscribe to a 'unified species concept' (De Queiroz

2007) wherein the primary criterion for formal taxonomic rank is the existence of evolutionary

lineages (e.g., as distinct metapopulations), with evidence via reproductive isolation,

phylogenetic-phylogeographic resolution, and phenotypic adaptation, with all acknowledged as

being inherently linked. Here, our clustering and classificatory approaches define molecular

diagnosability, and as such variably place *Terrapene* lineages along a speciation continuum (Via

2009; Nosil & Feder 2012; Edwards *et al.* 2016; Martin *et al.* 2020).

## 2 MATERIALS AND METHODS

### 2.1 DNA extraction and library preparation

Tissue samples were obtained from museums, agencies, and volunteers (Supplemental

Information Table S1) and stored at-20°C. Genomic DNA was extracted via spin-column kits:

DNeasy Blood and Tissue (QIAGEN), QIAamp Fast DNA (QIAGEN), and E.Z.N.A. Tissue

DNA Kits (Omega Bio-tek). Extracted DNA was quantified using Qubit fluorometry (Thermo

Fisher Scientific), and characterized using gel electrophoresis on 2% agarose.

Samples were processed via ddRADseq (Peterson et al. 2012), with ~500-1,000ng of

genomic DNA/sample digested with *PstI* and *MspI* at 37°C for 24 hours. Samples were bead-

purified (Beckman-Coulter) at 1.5X concentration then standardized at 100ng. Barcoded adapters

were ligated before pooling 48 samples per library. Taxa were spread across libraries to mitigate

batch effects then size-selected on a Pippin Prep (Sage Science). Adapter-extension was

performed via twelve-cycle PCR, followed by 1x100 sequencing on the Illumina Hi-Seq 4000

(University of Oregon/Eugene), with two indexed libraries pooled/lane.

### 2.2 Quality control and assembly

FASTQCv.0.11.5 was used to assess sequence quality (Andrews 2010), with raw reads

demultiplexed via IPYRAD v.0.7.28 (Eaton & Overcast 2020), allowing for one barcode mismatch

as a maximum. Low quality sequences (>5 bases with Q<33) and adapters were removed.

Assembly was reference-guided using *Terrapene mexicana* (GCA_002925995.2), with unmapped

reads discarded. To reduce error, only loci exhibiting ≥20X coverage were retained (Nielsen *et al.*

2011). We also excluded loci with excessive heterozygosity (≥75% of individual SNPs), <50%

global occupancy, or >two alleles/sample.

**2.3 *Phylogenomic inferences***

$F_1$ and $F_2$-generation hybrids previously identified in a population-level analysis (Martin *et al.*

(2020) were excluded as a means of mitigating impacts of contemporary gene flow on species

tree inference (Long & Kubatko 2018). We then employed SVDQUARTETS (Chifman & Kubatko

2014) filtered to one SNP per locus to reduce linkage bias, with exhaustive quartet sampling and

100 bootstrap pseudo-replicates. Taxon partitions were grouped by subspecies and U.S./Mexican

state locality, with *Emydoidea blandingii* and *Clemmys guttata* as outgroups.

We also employed a polymorphism-aware model (POMO: Schrempf *et al.* 2016), as

implemented in IQ-TREE v1.6.9 (Nguyen *et al.* 2015), with full-locus alignments and 1,000

ultrafast bootstrap (UFBOOT) replicates (Hoang *et al.* 2017). The maximum virtual population

size was 19, with discrete gamma-distributed rates=4.

Using ten-thousand re-samplings, we performed topology tests (IQ-TREE) with seven

statistical criteria on the SVDQUARTETS and POMO trees, as well as a previously published

morphological (Minx 1996) and a molecular hypothesis (Martin *et al.* 2013). Additional details

are in Supplemental Information Appendix A.1.1.

A lineage tree was generated (IQ-TREE v2.0.6; Minh *et al.* 2020) and full-locus partitions

merged (Chernomor *et al.* 2016), with the top 10% of combinations employed and a per-partition

model search (MODELFINDER: Kalyaanamoorthy *et al.* 2017). Tree inference involved node

support using 1,000 UFBᴏᴏᴛ replicates and site-wise concordance factors (sCF; Minh *et al.*

2018). The sCF values were calculated from 10,000 randomly sampled quartets.

**2.4 Divergence dating**

A full concatenation tree was time-calibrated via least square dating (LSD2), as implemented in

IQ-TREE (To *et al.* 2016). Four fossil calibration points were used, including the following most

recent common ancestors (MRCA): (1) *T. ornata* and *T. carolina/T. mexicana*, minimally

constrained to 13 million years ago (Mya); (2) *T. o. ornata* and *T. o. luteola* (9.0-13.0 Mya); (3)

*T. carolina* and *T. mexicana* (9.0-11.0 Mya); and (4) *Terrapene* and *Clemmys*/*Emydoidea*

[(maximally constrained to 29.4 Mya) (per Martin *et al.* 2013)]. Branch lengths were simulated

from a Poisson distribution with 1,000 replicates to assess 95% confidence intervals.

**2.5 Species delimitation using BFD***

We employed Bayes Factor Delimitation (BFD*; Leaché *et al.* 2014) as a comparative baseline.

Given its computationally-intense process, each taxon was subset to a maximum of five

individuals containing the least missing data (N=37+outgroups). Sites with >50% missing data in

any population were removed. See Supplemental Information Appendix A.2.1 for prior selection

and data formatting steps in BFD*).

For each BFD* model, we used 48 path-sampling steps, 200,000 burn-in, plus 400,000

MCMC iterations, sampling every 1,000 generations. Path-sampling was conducted with 200,000

burn-in+300,000 MCMC generations, α=0.3, 10 cross-validation replicates, and 100 repeats.

Trace plots were visualized in Tʀᴀᴄᴇʀ v1.7.1 to confirm parameter convergence and compute

effective sample sizes (ESS; Rambaut *et al.* 2018). Bayes factors (BF) were calculated from

normalized likelihood estimates (MLE) as [2 X (MLE$_1$-MLE$_2$)]. We considered the following

scheme for model support: 0<BF<2=no differentiation; 2<BF<6=positive; 6<BF<10=strong; and

BF>10=decisive support (Kass & Raftery 1995).

**2.6 Preparing and executing UML datasets**

To assess the influence of bioinformatic choices on M-L species delimitation, we performed

missing data filtering sweeps to produce 64 datasets across three filtering options. Missing data

was filtered per-individual and per-population, with the maximum permitted occupancy set to

25%, 50%, 75%, and no filtering (=100%). Datasets were also filtered by minor allele frequency

(MAF) at values of 5%, 3%, 1%, and 0% (=no MAF filter). Custom scripts were employed for all

filtering steps (https://github.com/tkchafin/scripts).

RF and T-SNE (Breiman 2001; Maaten & Hinton 2008) were executed and visualized using

an R script [Derkarabetian *et al.* (2019);

https://github.com/shahanderkarabetian/uml_species_delim]. We ran 100 replicates for each of

the 64 datasets, with data subsequently represented as scaled principal components

(ADEGENETv2.1.1; Jombart & Ahmed 2011) in Rv3.5.1 (R Development Core Team 2018). To

generate RF predictions, we averaged 10,000 majority-vote decision trees. Clustered RF output

was visualized using both classic and isotonic multidimensional scaling (CMDS and ISOMDS;

Shepard *et al.* 1972; Kruskal & Wish 1978). We ran T-SNE for 20,000 iterations, with equilibria

of the clusters visually confirmed. Perplexity, which limits the effective number of T-SNE

neighbors, was subjected to a grid search with values from 5-50, incremented by five.

VAE (Derkarabetian *et al.* 2019) employs neural networks to infer the marginal likelihood

distribution of sample means (μ) and standard deviations [(σ) (i.e. 'latent variables')]. As with RF

and T-SNE analyses, VAE was also run with 100 replicates to assess cluster stochasticity. Each of

the 64 datasets were split into 80% training/20% validation datasets using the *train_test_split*

module (*scikit-learn*: Pedregosa *et al.* 2011), with model loss (~error) visualized to determine the

optimal number of 'epochs' (=cycles through the training dataset). VAE should ideally be

terminated when loss converges on a minimal difference between training and validation datasets

[the 'Goldilocks zone'; Supplementary Information Figure S1 (Al'Aref *et al.* 2019)].

Overfitting is indicated when model loss in the validation dataset escalates, whereas

underfitting is a failure to reach minimum points (=inability to generalize to unseen data). Thus,

we added minor modifications to the original Python script (Derkarabetian *et al.* 2019) by

implementing an early stopping callback (*keras.callbacks* Python module; Chollet 2015), which

terminates training when model loss fails to improve for 50 epochs, then restores the best model

prior to the tolerance period (see Supplementary Information Appendix A.2).

**2.7 K-selection for RF, T-SNE, and VAE**

Two clustering algorithms (R-scripts: Derkarabetian *et al.* 2019), were used to identify clusters

and derive optimal *K* for RF and T-SNE analyses. The first [Partitioning Around Medoids (PAM);

Kaufman and Rousseeuw 1987] minimizes the distance of intra-cluster points to a centroid. The

program requires *K* to be defined *a priori*, and thus *K*=1-10 were tested. The second (hierarchical

clustering, HC; Fraley & Raftery 1998) iteratively merges points with minimal dissimilarity.

After clustering, optimal *K* was chosen using the gap statistic (GS) and highest mean silhouette

width [HMSW; Rousseeuw (1987), Tibshirani *et al.* (2001)].

VAE used DBSCAN (Ester *et al.* 1996), as implemented in a custom Python script

(*vae_dbscan.py*), to derive clusters using a distance threshold ($\varepsilon$) rather than *a priori* setting of *K*.

Here we used 2x the standard deviation, but averaged globally across all samples (following

Derkarabetian *et al.* 2019).

For plotting, we implemented a permutation-based heuristic search to align *K* across all

replicates and the 64 datasets ['Cluster Markov Packager Across K;' Kopelman *et al.* (2015)

implemented in POPHELPER (Francis 2017)]. Assignment probabilities were then visualized as

stacked bar plots for each method (via a custom script: *plotUML_missData_maf.R*). For each

dataset, we plotted as heatmaps the optimal *K* and standard deviation (SD) among replicates

*(plot_missData_comparison_maf.R)* (Scripts deposited at:

https://github.com/btmartin721/mecr_boxturtle).

**2.8 Demography, migration history, and species-delimitation**

We tested for reticulation in our phylogenomic dataset, as complementary to a range-wide

evaluation of introgression in *Terrapene* (Martin *et al.* 2020). We first explored reticulation by

identifying candidate edges (TREEMIX; Pickrell & Pritchard 2012), with populations having but

one sample (*T. nelsoni* and *T. m. yucatana*) being excluded from input, which was then thinned to

bi-allelic SNPs. TREEMIX was run 10x with subsets of SNPs randomly sampled per locus at

1,000 bootstrap replicates using the 'global search' option. The optimal number of admixture

edges (*m*) was determined by running for *m*=1-10 and choosing the inflection point of log-

likelihood scores.

TREEMIX results and introgression (Martin *et al.* 2020) were used to generate gene flow

hypotheses in a species-delimitation framework (DELIMITR: Smith *et al.* 2017; Smith & Carstens

2020). DELIMITR uses the joint site-frequency spectrum (JSFS) and FASTSIMCOALV2.6 (Excoffier

*et al.* 2013) to simulate demographic models, including possible variations of lumping/splitting

taxa and primary divergence, secondary contact, or no gene flow. The program then builds an

RF-classifier trained with the simulated models (i.e., 'supervised' M-L) to predict the best model.

Input was generated using EASYSFS (https://github.com/isaacovercast/easySFS), with taxa

reduced to N=6, given computational resources required by larger datasets. Taxa excluded in the

hypothesis were: *T. m. mexicana*, *T. m. yucatana*, *T. o. luteola*, and *T. coahuila*.

To improve efficiency, we also used EASYSFS to down-project the JSFS to six alleles for

*T. c. bauri,* and ten each for the remaining taxa. Samples were selected to maximize per-

individual occupancy, followed by a maximum 50% per-population missing data filter. The

SVDQUARTETS result served as our topological prior for DELIMITR. Models considered were: No

gene flow, primary divergence, secondary contact, and up to four migration edges. Migration was

permitted between: *T. c. carolina* x *T. c. major*, *T. c. carolina* x *T. c. bauri*, *T. c. major* x *T. m.*

*triunguis*, and *T. m. triunguis* x *T. o. ornata.* Population size priors were set broadly (1,000-

100,000) and divergence times were obtained from LSD2 results. We defined a rule set that

ranked overlapping coalescence times for *T. c. bauri*/*T. m. triunguis* and *T. c. major* from

Mississippi/Florida. The migration rate prior range ($1.96 \times 10^{-6}$–$9.78 \times 10^{-5}$) was estimated from

the number of migrants (GENEPOP v4.7.5; Rousset 2008). We applied three JSFS binning classes

and 5,000 RF trees to build the classifier and predict the models.

## 3 RESULTS

### 3.1 Sampling and data processing

We sequenced 214 geographically-widespread *Terrapene* (Figure 1; Supplementary Information Table S1) including all recognized species and subspecies save the rare *T. nelsoni klauberi*. IPYRAD recovered 134,607 variable sites (of 1,163,463 total) across 14,760 retained loci, with 90,777 as parsimony informative. The mean per-individual depth was 56.3X (Supplementary Information Figure S2).

### 3.2 Species tree inference

The lineage tree contained N=214 tips (Figure 2), whereas those from SVDQUARTETS (Figure 3a) and POMO (Figure 3b) grouped individuals into N=26 populations, again per locality and subspecies. SVDQUARTETS examined 10,299 unlinked SNPs and the species tree was assembled from 87,395,061 quartets. Full loci were used for POMO. All trees clearly delineated eastern *versus* western clades, with *T. mexicana*, *T. carolina*, and *T. coahuila* composing the eastern clade, with western represented by *T. ornata* and *T. nelsoni*.

All phylogenies delineated *T. ornata* and *T. nelsoni*. However, SVDQUARTETS nested *T. o. luteola* within a paraphyletic *T. o. ornata*, whereas IQ-TREE and POMO represented them as reciprocally monophyletic. In the eastern clade, SVDQUARTETS displayed two subdivisions: *Terrapene mexicana* (all subspecies) and *T. carolina*+*T. coahuila*. POMO included *T. m. triunguis* as sister to *T. c. carolina*+*T. c. major* but paraphyletic within *T. m. mexicana*+*T. m. yucatana*. Furthermore, SVDQUARTETS, POMO, and IQ-TREE each differed with respect to the placement of *T. c. bauri*, *T. coahuila*, and two previously recognized populations within *T. c. major* (Martin

*et al.* 2013, 2020). SVDQUARTETS depicted *T. c. bauri* as sister to the *major/coahuila/carolina*

clade, whereas POMO placed *T. c. major* from Mississippi/*coahuila* as sister to *T. c. major*

(FL)/*bauri/carolina*. IQ-TREE placed *T. c. bauri* sister to *T. carolina*/*T. mexicana*, and *T.*

*coahuila*/*T. c. major* (MS) sister to *T. c. carolina*/*T. c. major* (FL).

The topology tests failed to reject either Martin *et al*. (2013) or the SVDQUARTETS trees,

whereas morphology-based and POMO trees were significantly rejected (Table 1). Although the

SVDQUARTETS tree was ranked highest, site-likelihood scores indicated a minority of sites drove

those topologies (Supplemental Information S3).

**3.3 Species delimitation via BFD\* and DELIMITR**

TREEMIX converged upon four migration edges (Figure 3c; Supplementary Information S4), with

gene flow identified between: *Terrapene m. mexicana* x *T. o. ornata*+*T. o. luteola*; T. *c. carolina*

x *T. c. bauri*; *T. m. triunguis* x *T. c. major* (MS); and *T. coahuila* x *T. c. major* (FL).

To target specific reticulation hypotheses, DELIMITR was run with a reduced set of sub-species, in

compliance with computational constraints. The best-fitting DELIMITR model within selected taxa

(*T. m. triunguis, T. o. ornata, T. c. major, T. c. bauri,* and *T. c. carolina*) was *K*=4 (posterior

probability=0.98; Table 3; Figure 3d). Also, *T. c. major* and *T. c. carolina* were collapsed, and

three secondary contact migration edges were apparent: *T. o. ornata* x *T. c. carolina*+*T. c. major*;

*T. c. bauri* x *T. c. carolina*+*T. c. major*; and *T. o. ornata* x *T. m. triunguis*. The second-best model

was identical save for excluding the latter migration, although it also had the highest error (Table

3).

BFD* supported two top models (Table 2), each delimited (*K*=9), and all distinct except

*T. o. ornata*/*T. o. luteola* (*K*=8; Figure 3d). Although not statistically distinguishable (BF<2),

both were decisively better than others (BF>10). Convergence was confirmed for the likelihood

traces, with mean per-model ESS>300 (Supplementary Information Table S2).

**3.4 UML species delimitation**

UML results varied considerably (Figures 4, 5; Supplemental Information S5-S10), with mean

optimal *K* greatest for T-SNE, followed by CMDS, VAE, and ISOMDS (Figures 4a, 5a). Across

datasets, PAM clustering with the gap statistic (PAM+GS) exhibited the largest *K*, whereas PAM

with the highest mean silhouette width (PAM+HMSW) was lowest (Figure 5b). Hierarchical

clustering (HC)+HMSW and VAE were intermediate (Figures 4a, 5a; Supplementary Information

S5). Each algorithm delimited *T. ornata* from *T. carolina*+*T. mexicana* in most datasets, save

PAM+HMSW in some of the larger datasets, and among some T-SNE replicates (e.g.,

Supplementary Information Appendix B, B1). In all cases, CMDS with PAM+GS and

HC+HMSW further delimited *T. m. triunguis*+*T. m. mexicana* from *T. carolina*, whereas CMDS

with PAM+HMSW did not. Whether the remaining algorithms did so depended upon filtering

parameters. Finally, CMDS with PAM+GS and HC+HMSW further partitioned subgroups within

*T. carolina* in most datasets, whereas ISOMDS did so in a limited fashion, and T-SNE split *T.*

*carolina* into multiple clusters without a phylogenetic pattern. Bar plots for 64 filtered datasets

are in Supplemental Information B1-B60.

We present representative results (Figure 3d) that displayed minimal inconsistencies

among replicates and with respect to the phylogeny, with parameter choice also reflecting how

each algorithm interacted with filtering values (below). This included 25% per-individual and

per-population filters for all algorithms, a 5% MAF filter for CMDS, T-SNE, and VAE, and a 1%

MAF filter for ISOMDS. Five groups were delineated by CMDS with PAM+GS: *T. o. ornata*

(ON)+*T. o. luteola* (DS), *T. c. major* from Mississippi (GUMS), *T. c. major* from Florida

(GUFL), *T. c. carolina* (EA), and *T. m. mexicana* (MX)+*T. m. triunguis* (TT).

However, *T. c. bauri* displayed mixed assignment between *T. c. carolina* and GUMS.

CMDS with HC+HMSW also delimited $K=5$ but lumped the two populations of *T. c. major*,

splitting *T. c. bauri*, and grouped some *T. c. carolina* individuals with *T. c. bauri*. It also split *T.*

*ornata* and *T. carolina*+*T. mexicana*. While ISOMDS with PAM+GS resembled CMDS with

HC+HMSW, it also clustered *T. c. bauri* with *T. c. carolina*. Similarly, ISOMDS with

HC+HMSW showed *T. o. ornata*+*T. o. luteola*, *T. c. carolina*+GUMS+GUFL, and *T. m.*

*mexicana*+*T. m. triunguis*. However, ISOMDS with PAM+HMSW only delimited *T. ornata* from

*T. carolina*+*T. mexicana*. The model T-SNE (at perplexity=15) clearly partitioned *T. ornata*, *T.*

*carolina*, and *T. mexicana*, though the PAM+GS algorithm exhibited spurious groupings within

*T. carolina*. However, T-SNE with HC+HMSW clustered many *T. c. carolina* with GUFL and the

remaining with GUMS. We found VAE and T-SNE with PAM+HMSW only delimited *T. ornata*,

*T. carolina*, and *T. mexicana*.

**3.5 Effects of data filtering**

Among all dimensionality reduction and clustering algorithms, greater per-individual and per-

population missing data generally increased mean optimal $K$ and SD (Figures 4a-b and 5a-b;

Supplemental Information S5). PAM+HMSW deviated due to low $K$, regardless of filtering. This

was manifested as two types of noise in the bar plots (Supplemental Information B1-B60):

'vertical striping' (inconsistency of assignment among replicates) and 'horizontal striping'

(groupings inconsistent with phylogeny). We found the former largely driven by increased

missing data per-individual, whereas the latter by increased missing data per-locus. However,

performance varied among algorithms in how they interacted with both missing data parameters.

We found that T-SNE consistently resolved *T. ornata* and *T. carolina*+*T. mexicana*, but *T.*

*mexicana* was only partitioned when per-population filtering was 25%. However, T-SNE did not

further partition *T. carolina* in any dataset and displayed a tendency to form phylogenetically

spurious groupings (=vertical striping). The perplexity grid search (Figures 4c-d and 5b;

Supplemental Information S6-S10) suggested that the highest $K$ and SD among replicates was at

perplexity=5-10, with a plateau at higher perplexities.

We also found CMDS with PAM+GS and HC+HMSW delineated most clades, save for

inconsistency amongst the *T. c. major* populations and *T. coahuila*. In contrast, CMDS and

ISOMDS with PAM+HMSW typically displayed $K$=2 or 3 and contained no phylogenetically

meaningful clusters with ≥75% missing data per-individual (e.g., Supplemental Information

B62). Finally, VAE partitioned *T. ornata* from *T. carolina*+*T. mexicana* in all datasets, but *T.*

*mexicana* was only delineated from *T. carolina* when per-individual missing data was ≤50% and

with MAF filter.

Filtering by MAF ubiquitously reduced noise, although results varied by algorithm

(Supplemental Information B1-B60). For T-SNE, optimal $K$ and SD were reduced. In contrast, the

clusters yielded by CMDS with PAM+GS and HC+HMSW were only marginally affected. We

found CMDS and ISOMDS with PAM+HMSW and MAF filters ≥3% were less noisy, but for

ISOMDS with PAM+GS and HC+HMSW the MAF filter effect was dependent on the number of

individuals present in the dataset. With a maximum of 25% per-individual missing data (N=117),

a 1% MAF filter shows minimal striping and higher $K$ than did a >1% MAF filter. However,

larger MAF filters have a greater effect above 25% per-individual filtering. Lastly, optimal $K$,

SD, and striping in VAE were strongly influenced by MAF filters (Figures 4e-f, 5a,

Supplementary Information S5). With lower per-individual filters (≤50%) and a 5% MAF filter,

VAE consistently delineated *T. mexicana* from *T. carolina*, even with high per-population filters.

However, lower MAF and higher per-individual (>50%) filters introduced progressively more

noise and grouped *T. carolina* and *T. mexicana*.

**3.6 Relative performance among approaches**

The CMDS model with PAM+GS and HC+HMSW consistently displayed the highest $K$ and was

less susceptible to data filtering. However, ISOMDS with PAM+GS and HC+HMSW was more

influenced by filtering parameters, but still consistently resolved the highest level of hierarchical

structure (*T. ornata/T. carolina+T. mexicana*). Both CMDS and ISOMDS with PAM+HMSW

consistently displayed the lowest $K$ at the top hierarchy and were usually in complete agreement.

We note that T-SNE was highly susceptible to horizontal and vertical striping, and only

partitioned *T. mexicana* from *T. carolina* ssp. at 25% per-individual filtering. Similarly, VAE

performed far more consistently with a 5% MAF filter and ≤50% per-individual filtering. VAE

also consistently hovered between K=2 and K=3, making it the second most conservative

algorithm next to PAM+HMSW. In contrast, BFD* delimited the most taxa among all the

approaches, splitting all save *T. o. luteola* and *T. o. ornata*, and DELIMITR partitioned *T. ornata*,

*T. carolina*, *T. mexicana*, and *T. c. bauri*.

In terms of computational resources, the UML algorithms were far less intensive than

BFD* and DELIMITR, enabling stochasticity to be assessed in many replicates. Each UML

algorithm needed ~1-3GB RAM per replicate and ~2-3 days runtime for 100 replicates.

Comparatively, BFD* required the greatest memory and time, often using >200GB RAM (with

16 CPU threads) and a ~10-day runtime per model. We note DELIMITR used much less memory

and was faster than BFD*, but output ~3.2 TB with six tips and 51 models.

**4 DISCUSSION**

We observed substantial heterogeneity in resolving *Terrapene* via M-L approaches, which echoed

previous morphological and single-gene results (Milstead 1967, 1969; Milstead & Tinkle 1967;

Butler *et al.* 2011; Martin *et al.* 2013). We interpret this variability as reflecting inherent

differences in dimensionality-reduction, clustering, and *K*-selection, as well as the manner by

which methodologies interact with biological aspects of the data and user-defined filtering.

**4.1  Delimitation hypotheses and biological interpretations reconciled**

Two factors likely contribute to the observed heterogeneity: 1) An hierarchical arrangement of

phylogenetic signal (Martin *et al.* 2013); and 2) Phylogenetic discord (Martin *et al.* 2020). Both

reverberate noticeably within prior literature and phylogenetic evaluations.

The most consistent grouping was eastern (*T. carolina*+*T. mexicana*) versus western (*T.*

*ornata*) clades, representing the deepest *Terrapene* divergence (Figures 3a-b). This is

unsurprising given it is the most prominent axis of molecular variation (morphologically

corroborated; Milstead & Tinkle 1967; Dodd 2001) Nominal species have been identifiable since

late Miocene (Holman & Fritz 2005), as corroborated by molecular dating (Figure 2).

**4.2** *Terrapene ornata*

Although introgression between *T. o. ornata* and *T. m. triunguis* occurred during secondary

contact (Table 3; Figure 3d), no contemporary evidence for introgression among these clades

emerged from previous evaluations, except rare $F_1$ hybrids between *T. o. ornata* and *T. carolina*

(Martin *et al.* 2020). TREEMIX also suggested introgression between *T. ornata* and *T. m.*

*mexicana* (Figure 3c). Although contact with *T. mexicana* was certainty possible during glacial

expansion-contraction (Martin *et al.* 2020), we echo earlier conclusions that hybridization lacks

justifiable taxonomic implications, per hybridization between *T. ornata* and *T. carolina* (Martin

*et al.* 2020).

Regarding *T. ornata,* algorithms failed to further partition *T. o. ornata*/*T. o. luteola*,

suggesting a lack of diagnosability at our most recent scale. Notably, both also lack reciprocal

monophyly in some phylogenomic (Figure 3a) and single-gene analyses (Martin et al. 2013).

They also lack clear morphological synapomorphies (Minx 1996). Although *T. o. luteola* exhibits

habitat and movement patterns markedly different from mesic conspecifics (Nieuwolt 1996), few

investigations have similarly compared *T. ornata* subspecies, such that inferences regarding

reproductive isolation (or potential thereof) are difficult. Populations of *T. o. luteola* also do not

exhibit thermal adaptations that are mutually exclusive from *T. o. ornata,* as might be surmised

given other desert-dwelling tortoise (Plummer 2003).

Previous authors hypothesized *T. o. luteola* as a relict population (Milstead & Tinkle

1967). Weak differentiation [molecular: Martin *et al.* (2013); morphological: Dodd (2001)], as

well as possible paraphyly of *T. o. ornata* (Figure 3a) suggest isolation was recent. Although

phylogenetic structuring was present in some analyses (e.g., Figure 2), it is insufficient to

mandate recognition beyond the subspecific level. However, special guidelines that delineate

relictual lineages may be warranted (Mussmann *et al.* 2020), particularly given the isolation and

reduced $N_e$ in *T. o. luteola* (Nieuwolt 1996).

**4.3 *Terrapene mexicana***

The second most frequent split (Figures 2, 3a) divided *T. mexicana* and *T. carolina*,

corresponding to the second-deepest phylogenetic node (Figures 2, 3a). This lends further support

to a prior elevation of *T. mexicana* (Martin *et al.* 2013). Conspecifics of *T. mexicana* also share

multiple morphological characteristics, such as carapace coloration and a degree of concavity to

the posterior plastron, that separate the group from *T. carolina* (Minx 1996). *Terrapene mexicana*

*mexicana* (as well as *T. m. yucatana*, excluded due to sample size) have isolated, allopatric ranges

(Smith & Smith 1980; Ernst & Lovich 2009), with reproductive isolation difficult to assume.

Evidence for interbreeding of *T. m. triunguis* with *T. carolina* subspecies in the

southeastern United States (Butler *et al.* 2011) has led some to conclude that species-level

recognition of *T. mexicana sensu lato* is unwarranted (Fritz & Havaš 2014). Indeed, our own

results suggest introgression between *T. m. triunguis* and *T. carolina* in secondary contact (Figure

3d). Martin *et al.* (2020) confirmed hybridization of *T. m. triunguis* with both *T. c. major* and *T.*

*c. carolina* in the southeast, yet found genetic exchange was restricted, given that: (1) Genetically

'pure' individuals are predominant throughout the contact zone; and (2) patterns of gene-level

exchange exhibit strong sigmoidal patterns, suggesting selection against interspecific

heterozygotes. Additionally, the sigmoidal pattern was strongest within a subset of genes

involved in thermal adaptation (Martin *et al.* 2020), suggesting species boundaries are modulated

by an adaptive barrier between co-occurring *T. mexicana* and *T. carolina* sub-species. This

functional perspective corroborates the proposed taxonomy herein, and by Martin et al. (2013).

**4.4 *Terrapene carolina***

Partitioning within *T. carolina* echoed inconsistencies in our phylogenies (Figures 2, 3a-b), and

seemingly depended upon algorithm and filtering regime (Figure 3d; Supplementary Information

B). *Terrapene carolina major*, for example, occasionally split from the remaining *T. carolina*

(usually including *T. coahuila*; CMDS+HC, Figure 3d), whereas in other cases, *T. c. major* (FL

and MS) were separated (with the former grouped into *T. c. carolina*) (T-SNE+HC, Fig. 3d) .

468           In contrast to steep clines in interspecific comparisons (Martin *et al.* 2020; see above), a

transect of the *T. c. carolina* and *T. c. major* contact zone revealed shallow genetic transition,

with multiple loci showing potential signatures of selection-driven introgression. Previous

authors have hypothesized either direct ancestry (Bentley & Knight 1998) or historic admixture

with a now extinct taxon, [*T. c. putnami*; Butler *et al.* (2011)]. While such 'ghost' admixture can

mislead population structure (Lawson *et al.* 2018), such a signal is unlikely manufactured in

entirety. In contrast to Butler *et al.* (2011), Martin *et al.* (2020) found a pervasive signal of

population structure and strong molecular diagnosability in *T. c. major*, with a cryptic east-west

division roughly defined by the Apalachicola River [a recurring phylogeographic discontinuity

reflecting recolonization from disparate Gulf Coast refugia; Soltis *et al.* (2006)]. Our

interpretations refuted the 'genetic melting pot' assertion (Fritz & Havaš 2014) and favored

instead recognition of the two as distinct evolutionarily significant units (ESUs). Additionally,

differences in habitat use and movement patterns distinguish *T. c. major* (Meck *et al.* 2020),

which spends greater time in mesic habitats (e.g., floodplain swamps). In support, early studies

observed a distinct webbing of the hind foot in *T. c. major* (Taylor 1895). Given the genetic data

herein, we reject the taxonomic coalescence of *T. c. major*.

*Terrapene carolina bauri* was similarly resistant to straightforward classification,

although generally grouping with *T. c. major* (when the latter was separated from *T. c. carolina*;

Figure 3b). We found *T. c. bauri* as sister to either the remaining *T. carolina* group, *T. c.*

*carolina+T. c. major*, or only *T. c. carolina* (Figures 2-3; Martin *et al*. 2013). This argues against

it being sister to *T. m. triunguis* (per Spinks *et al.* 2009). Osteologically, it alone shares a

complete zygomatic arch with *T. c. major* (Taylor 1895; Ditmars 1934), although other

morphological investigations have allied it more closely with *T. c. carolina* (Minx 1996). Thus,

phylogenetic inconsistency for *T. c. bauri* clearly extends beyond our results.

Although hybridization likely contributes to this issue (as with *T. c. major*), the

biogeography of the region may provide insight, with peninsular Florida recognized as a distinct

biogeographic province (Ennen *et al.* 2017). Intraspecific division are recognized in multiple

species [e.g., *Chelydra serpentina*, *Deirochelys reticularia* (Walker & Avise 1998)], a

phylogenetic legacy likely reflecting periodic isolation from the mainland that may have inflated

genetic divergences (Douglas *et al.* 2006), and facilitated secondary contact. This scenario is

supported by DELIMITR and TREEMIX (Figures 3c-d). Here, we again stress that evidence is

sufficient to support continued recognition, yet not for taxonomic elevation.

**4.5 *Terrapene coahuila***

*Terrapene coahuila* represents a persistent phylogenetic uncertainty (Spinks *et al.* 2009; Wiens *et*

*al.* 2010; Martin *et al.* 2013). It is unique in that it occupies streams, ponds, and marshes, with

terrestrial movements restricted to the rainy seasons (Webb *et al.* 1963). Milstead (1967)

postulated that *T. coahuila* evolved as a relictual population of a *Terrapene* ancestor (potentially

the extinct *T. c. putnami*) during pluvial periods associated with Pleistocene glacial-interglacials

across the broad eastern coastal plain of Mexico. In this scenario, relictual populations are what

remains from those north-south migrations, as hypothesized for *T. m. mexicana* and *T. m.*

*yucatana*. This scenario is plausible, given semi-aquatic adaptations in the presumed ancestor (*T.*

*c. putnami*) and closely related *T. c. major*, as well as shared morphologies between extinct *T. c.*

*putnami* and modern *T. coahuila* (Milstead 1967). The phylogenetic placement of *T. coahuila*, as

nested within *T. c. major*, offers further evidence (Figure 2-3), as does the almost unanimous

UML grouping in our results (Figure 3d; Supplementary Information B1-B60). As with *T. o.*

*luteola*, small, isolated populations that differ in evolutionary rates in could contribute to a lack of

molecular similarity with extant *T. c. major*, despite a unique functional morphology (Brown

1971).

**4.6 Relative performance of species-delimitation methods**

As with prior studies (Derkarabetian *et al.* 2019; Mussmann *et al.* 2020), we also found

considerable variation among methods, some of which can be attributed either to idiosyncrasies

in the data or to algorithms and their implementation. For example, among RF methods ISOMDS

generally yielded smaller *K* (Figure 3d), attributed by Derkarabetian *et al.* (2019) to the retention

of only two dimensions. We also found some methods (PAM+HMSW; Figure 3d) trended

towards $K$=2, corresponding to the deepest *Terrapene* bifurcation, and suggesting a potential

failure in identifying hierarchical clusters. Here, a solution might include partitioning divergent

subtrees for separate analyses.

In contrast to Derkarabetian *et al.* (2019), we found T-SNE the most inclined to produce

inconsistent groupings, a pattern most prevalent with the gap statistic (Supplementary

Information B1-B60). Mussmann *et al.* (2020) concurred, although in their case it was

PAM+HMSW. We see this as an inherent problem relating to data structure. Previous

comparisons of T-SNE found low fidelity with global data patterns, and latent space distances

were poor proxies for 'true' among-group distances, particularly when compared to VAE (Becht

*et al.* 2019; Battey *et al.* 2020). This potentially explains our observed 'plateau' of mean optimal

$K$ and SD in the T-SNE perplexity grid-search, in that perplexity defines relative weighting of

local versus global components (Wattenberg *et al.* 2016). It may also explain the formation of

spurious clusters even at higher perplexities, in that clusters are formed *post hoc* (PAM or HC).

Thus, T-SNE may perform poorly when inter-cluster distances/dispersion in global data structure

are skewed, although it is not clear to what degree hyperparameter choice and initializations

contribute (Belkina *et al.* 2019; Kobak & Berens 2019).

In our case, VAE with DBSCAN yielded higher fidelity to the underlying phylogeny

(Figure 3a), and was also more robust to missing data (Figures 4e-f). A particular benefit of the

VAE approach is the output of a standard deviation around samples in latent space

(Derkarabetian *et al.* 2019). Our DBSCAN hyperparameters were informed directly from latent

variable uncertainties, and in so doing, we circumvented the issue of $K$-selection that drove

heterogeneity in the RF and T-SNE methods [also recognized with other clustering approaches

(Janes *et al.* 2017)].

By comparison, BFD* partitioned all groups, which may reflect a vulnerability to local

structure at the population level, as reported by others for MSC methods (Sukumaran & Knowles

2017). BFD* and VAE partitioned equally in Mussmann *et al*. (2020), although their populations

were relictual and without contemporary connectivity, whereas *Terrapene* reflects both historical

(Figure 3d) and contemporary gene flow (Martin *et al*. 2020). In corroboration, other studies have

also demonstrated reticulation to condense VAE clusters (Derkarabetian *et al.* 2019; Newton *et*

*al.* 2020). Although not run on a full dataset, DELIMITR formed clusters consistent with (or similar

to) several of the UML methods (e.g., ISOMDS+GS; Figure 3d, Table 3). The latter displayed a

particular utility regarding testing targeted hypotheses relating to demographic processes such as

migration, whereas these must be applied to UML results *post hoc*.

**4.7 Data treatment and assignment consistency**

We generally found a tendency for UML methods to 'over-split' regarding large amounts of

missing data, with phylogenetically inconsistent groupings ('horizontal striping') most

pronounced when missing data was elevated per-individual (Supplementary Information B1-

B60). However, low-level, undetected introgression could also drive such a pattern. Mussmann *et*

*al*. (2020) noted a similar pattern with the RF methods, possibly reflecting an artificial similarity

among samples generated by a non-random distribution of missing data. A similar 'vertical

striping' effect was seen when missing data was elevated per-locus (e.g., Supplemental

Information B13), often manifested as inconsistency among replicates. However, effects varied

across methods, as per previous analyses [phylogeographic: Graham *et al.* (2020); phylogenetic:

Molloy & Warnow (2018)].

Missing-data bias is a particular concern when patterns are non-random (i.e., presence or

absence of observations are data-dependent; Rubin 1976). Here, the temptation is to filter

stringently, yet we found highly filtered datasets were biased towards smaller $K$, generally

retaining only nodes deepest within the phylogeny. The same pattern was identified using the

VAE method (Newton *et al.* 2020), and is intuitive given expectations that a major subset of

missing ddRAD data are systematically distributed [defined by mutation-disruption of restriction

sites: Gautier *et al.* (2013); Eaton *et al.* (2017)]. Thus, indiscriminate exclusion may unintendedly

bias information content leading to the underestimation of diversity (Arnold *et al.* 2013; Leaché

*et al.* 2015; Huang & Knowles 2016). Again, care must be taken to filter the data such that

sufficient discriminatory signal remains, while also mindful of the signal-to-noise ratio, and the

underlying biases driving interactions of sparse data versus information content (Nakagawa &

Freckleton 2008).

A potential solution involves the input of genotypes to fill in missing values (per Howie *et

al.* 2009; Durbin 2014; Das *et al.* 2016). However, a cautious *a priori* designation of population

references is needed, particularly when group-delimitation is the goal. It may be appropriate to

employ phylogenetically-informed methods previously applied in comparative studies (e.g.,

Goolsby *et al.* 2017).

We found MAF filters dampened the effect of missing data, likely by removing

sequencing errors and uninformative variants at low-frequency (Mathieson & McVean 2012;

Jakobsson *et al.* 2013). In a similar context, Linck & Battey (2019) found MAF filters to

significantly increase in the discriminatory capacity of assignment-test methods (STRUCTURE;

Pritchard *et al.* 2000). In our case, MAF filtering reduced noise and improved group

differentiation (e.g., resulting in lower variability among replicates; Figures 4-5, Supplementary

Information S5-S6). Thus, we view it as a parameter in need of further empirical exploration.

**4.8 Conclusions**

UML approaches identify groups based on the structure of the data, and as such, represent a

natural extension to species-delimitation approaches. However, we found idiosyncrasies

regarding: Phylogenetic context of the study system (e.g., hierarchical structure, reticulation); the

manner by which clustering and *K*-selection approaches were applied *post hoc*; and regarding the

bioinformatic treatment of the data. We particularly note that lax filtering, performed to maximize

size and information content, actually promote spurious groupings and inflate variability among

replicates. An alternate method, i.e., filtering via MAF to promote informative characters,

favorably altered the signal-to-noise ratio and increased the consistency of our delimitations. We

conclude that UML approaches, when applied to formulate taxonomic hypotheses and reduce

dimensionality of complex data, are a valuable and computationally efficient tools for integrative

species-delimitation, as demonstrated within our study system.

**ACKNOWLEDGEMENTS**

Many thanks to those volunteers, organizations, and agencies that contributed tissue samples

(Supplementary Information Table S1). We also thank colleagues for guidance at various stages

of this project: A. Alverson, W. Anthonysamy, M. Bangs, J. Beaulieu, J. Koukl, P. Martin, S.

Mussmann, J. Pummill, and Z. Zbinden. Sample collections were approved under Animal Care

and Use Committee (IACUC) protocols: #113 (University of Texas/Tyler), #16160 and #18000

(University of Illinois/Champaign-Urbana). Funding sources were the Lucille F. Stickle Fund of

the North American Box Turtle Committee, the American Turtle Observatory, and University of

Arkansas endowments to MRD and MED. The Arkansas High Performance Computing Cluster

(AHPCC) and Jetstream cloud (XSEDE #TG-BIO160065) provided computational resources.

## AUTHOR CONTRIBUTIONS

BTM and TKC designed the research, implemented laboratory protocols, and authored scripts.

BTM conducted lab work and bioinformatic analyses, analyzed data, and wrote the manuscript.

MRD and MED guided the study design, provided funding, and contributed to manuscript development. JSP facilitated collection of *Terrapene* tissues and provided methodological expertise. RDB collected *Terrapene* tissues from southeastern North America and initiated access to additional individuals. CAP provided taxon expertise and provided many *T. ornata* tissues. All authors contributed to and revised the manuscript.

## DATA AVAILABILITY STATEMENT

Raw ddRADseq data are available on the GenBank Nucleotide Database at https://www.ncbi.nlm.nih.gov/bioproject/563121 (BioProject ID: 563121). Scripts for parsing and plotting UML output are available on GitHub at https://github.com/btmartin721/mecr_boxturtle. Input and output files for all analyses can be found in a Dryad Digital Repository (DOI: https://doi.org/10.5061/dryad.xgxd254fc).

**REFERENCES**

Al'Aref SJ, Anchouche K, Singh G, Slomka PJ, Kolli KK, Kumar A, Pandey M, Maliakal G, Van Rosendael AR, and Beecy AN (2019) Clinical applications of machine learning in cardiovascular disease and its relevance to cardiac imaging. *European Heart Journal*, **40**, 1975–1986.

Allendorf FW, Hohenlohe PA, and Luikart G (2010) Genomics and the future of conservation genetics. *Nature Reviews Genetics*, **11**, 697–709.

Andrews S (2010) FastQC: a quality control tool for high throughput sequence data. https://www.bibsonomy.org/bibtex/2b6052877491828ab53d3449be9b293b3/ozborn.

Arnold B, Corbett☐Detig RB, Hartl D, and Bomblies K (2013) RAD seq underestimates diversity and introduces genealogical biases due to nonrandom haplotype sampling. *Molecular Ecology*, **22**, 3179–3190.

Auffenberg W (1958) Fossil turtles of the genus *Terrapene* in Florida. *Bulletin of the Florida State Museum*, **3**, 53–92.

Auffenberg W (1959) A Pleistocene *Terrapene* hibernaculum, with remarks on a second complete box turtle skull from Florida. *Quarterly Journal of the Florida Academy of Science*, **22**, 49–53.

Austerlitz F, David O, Schaeffer B, Bleakley K, Olteanu M, Leblois R, Veuille M, and Laredo C (2009) DNA barcode analysis: a comparison of phylogenetic and statistical classification methods. *BMC Bioinformatics*, **10**, S10.

Avise JC (2000a) *Phylogeography: the history and formation of species*. Harvard University Press, Cambridge, MA.

Avise JC (2000b) Cladists in Wonderland. *Evolution*, **54**, 1828–1832.

Battey CJ, Coffing GC, and Kern AD (2020) Visualizing population structure with variational autoencoders. *bioRxiv*, 248278.

Becht E, McInnes L, Healy J, Dutertre C-A, Kwok IWH, Ng LG, Ginhoux F, and Newell EW (2019) Dimensionality reduction for visualizing single-cell data using UMAP. *Nature Biotechnology*, **37**, 38–44.

Belkina AC, Ciccolella CO, Anno R, Halpert R, Spidlen J, and Snyder-Cappione JE (2019) Automated optimized parameters for t-distributed stochastic neighbor embedding improve visualization and analysis of large datasets. *Nature Communications*, **10**, 1–12.

Bentley CC and Knight JL (1998) Turtles (Reptilia: Testudines) of the Ardis local fauna late Pleistocene (Rancholabrean) of South Carolina. *Brimleyana*, **25**, 1–33.

Breiman L (2001) Random Forests. *Machine Learning*, **45**, 5–32.

Brown WS (1971) Morphometrics of *Terrapene coahuila* (Chelonia, Emydidae), with comments on its evolutionary status. *The Southwestern Naturalist*, **16**, 171–184.

Butler JM, Dodd Jr. CK, Aresco M, and Austin JD (2011) Morphological and molecular evidence indicates that the Gulf Coast box turtle (*Terrapene carolina major*) is not a distinct evolutionary lineage in the Florida Panhandle. *Biological Journal of the Linnean Society*, **102**, 889–901.

Chambers EA and Hillis DM (2019) The multispecies coalescent over-splits species in the case of geographically widespread taxa. *Systematic Biology*, **69**, 184–193.

Chernomor O, Von Haeseler A, and Minh BQ (2016) Terrace aware data structure for

phylogenomic inference from supermatrices. *Systematic Biology*, **65**, 997–1008.

Chifman J and Kubatko L (2014) Quartet inference from SNP data under the coalescent model. *Bioinformatics*, **30**, 3317–3324.

Chollet F (2015) Keras. https://keras.io.

Das S, Forer L, Schönherr S, Sidore C, Locke AE, Kwong A, Vrieze SI, Chew EY, Levy S, and McGue M (2016) Next-generation genotype imputation service and methods. *Nature Genetics*, **48**, 1284–1287.

Derkarabetian S, Castillo S, Koo PK, Ovchinnikov S, and Hedin M (2019) A demonstration of unsupervised machine learning in species delimitation. *Molecular Phylogenetics and Evolution*, **139**, 106562.

Ditmars RL (1934) A review of the box turtles. *Zoologica*, **17**, 1–44.

Dodd KC (2001) *North American Box Turtles, A Natural History*. University of Oklahoma Press, Norman, OK, USA.

Douglas MRE, Douglas MRE, Schuett GW, and Porras LW (2006) Evolution of rattlesnakes (Viperidae; Crotalus) in the warm deserts of western North America shaped by Neogene vicariance and Quaternary climate change. *Molecular ecology*, **15**, 3353–3374.

Durbin R (2014) Efficient haplotype matching and storage using the positional Burrows–Wheeler transform (PBWT). *Bioinformatics*, **30**, 1266–1272.

Eaton DAR and Overcast I (2020) ipyrad: Interactive assembly and analysis of RADseq datasets. *Bioinformatics*, **36**, 2592–2594.

Eaton DAR, Spriggs EL, Park B, and Donoghue MJ (2017) Misconceptions on missing data in RAD-seq phylogenetics with a deep-scale example from flowering plants. *Systematic Biology*, **66**, 399–412.

Edwards S V, Potter S, Schmitt CJ, Bragg JG, and Moritz C (2016) Reticulation, divergence, and the phylogeography–phylogenetics continuum. *Proceedings of the National Academy of Sciences*, **113**, 8025–8032.

Eldredge N and Cracraft J (1980) *Phytigenetic Patterns and the Evolutinary Process: Methods and Theory in Comparative Biology*. Columbia University Press, New York, NY, USA.

Ennen JR, Matamoros WA, Agha M, Lovich JE, Sweat SC, and Hoagstrom CW (2017) Hierarchical, quantitative biogeographic provinces for all North American turtles and their contribution to the biogeography of turtles and the continent. *Herpetological Monographs*, **31**, 114–140.

Ernst CH and Lovich JE (2009) *Turtles of the united states and Canada, 2nd Edition*. The John Hopkins University Press, Baltimore, MD, USA.

Ester M, Kriegel H-P, Sander J, and Xu X (1996) A density-based algorithm for discovering clusters in large spatial databases with noise. In: *Proceedings of the Second International Conference on Knowledge Discovery and Data Mining*, pp. 226–231.

Excoffier L, Dupanloup I, Huerta-Sánchez E, Sousa VC, and Foll M (2013) Robust demographic inference from genomic and SNP data. *PLoS Genetics*, **9**, e1003905.

Feldman CR and Parham JF (2002) Molecular phylogenetics of emydine turtles: Taxonomic revision and the evolution of shell kinesis. *Molecular Phylogenetics and Evolution*, **22**, 388–398.

Fraley C and Raftery AE (1998) How many clusters? Which clustering method? Answers via model-based cluster analysis. *The Computer Journal*, **41**, 578–588.

Francis RM (2017) pophelper: an R package and web app to analyse and visualize population

structure. *Molecular Ecology Resources*, **17**, 27–32.

Fritz U and Havaš P (2013) Order Testudines: 2013 update. In: Zhang, Z.-Q. (Ed.) Animal Biodiversity: An Outline of Higher-level Classification and Survey of Taxonomic Richness (Addenda 2013). *Zootaxa*, **3703**, 12–14.

Fritz U and Havaš P (2014) On the reclassification of Box Turtles (*Terrapene*): A response to Martin et al. (2014). *Zootaxa*, **3835**, 295–298.

Funk DJ and Omland KE (2003) Species-level paraphyly and polyphyly: frequency, causes, and consequences, with insights from animal mitochondrial DNA. *Annual Review of Ecology, Evolution, and Systematics*, **34**, 397–423.

Gautier M, Gharbi K, Cezard T, Foucaud J, Kerdelhué C, Pudlo P, Cornuet J-M, and Estoup A (2013) The effect of RAD allele dropout on the estimation of genetic variation within and between populations. *Molecular Ecology*, **22**, 3165–3178.

Goolsby EW, Bruggeman J, and Ané C (2017) Rphylopars: fast multivariate phylogenetic comparative methods for missing data and within☐species variation. *Methods in Ecology and Evolution*, **8**, 22–27.

Graham MR, Santibáñez☐López CE, Derkarabetian S, and Hendrixson BE (2020) Pleistocene persistence and expansion in tarantulas on the Colorado Plateau and the effects of missing data on phylogeographical inferences from RADseq. *Molecular Ecology*, **29**, 3684–3701.

Hoang DT, Chernomor O, von Haeseler A, Minh BQ, and Vinh LS (2017) UFBoot2: improving the ultrafast bootstrap approximation. *Molecular Biology and Evolution*, **35**, 518–522.

Holman JA and Fritz U (2005) The box turtle genus Terrapene (Testudines☐: Emydidae) in the Miocene of the USA. *Herpetol. J.*, **15**, 81–90.

Howie BN, Donnelly P, and Marchini J (2009) A flexible and accurate genotype imputation method for the next generation of genome-wide association studies. *PLoS Genet*, **5**, e1000529.

Huang H and Knowles LL (2016) Unforeseen Consequences of Excluding Missing Data from Next-Generation Sequences: Simulation Study of RAD Sequences. *Systematic Biology*, **65**, 357–365.

Iverson JB, Meylan PA, and Seidel ME (2017) Testudines—Turtles. In: *Scientific and Standard English Names of Amphibians and Reptiles of North America North of Mexico, with Comments Regarding Confidence in Our Understanding* (ed Crother BI), pp. 82-91. SSAR Herpetological Circular 43.

Jakobsson M, Edge MD, and Rosenberg NA (2013) The relationship between FST and the frequency of the most frequent allele. *Genetics*, **193**, 515–528.

Janes JK, Miller JM, Dupuis JR, Malenfant RM, Gorrell JC, Cullingham CI, and Andrew RL (2017) The K = 2 conundrum. *Molecular Ecology*, **26**, 3594–3602.

Jombart T and Ahmed I (2011) adegenet 1.3-1: new tools for the analysis of genome-wide SNP data. *Bioinformatics*, **27**, 3070–3071.

Kalyaanamoorthy S, Minh BQ, Wong TKF, von Haeseler A, and Jermiin LS (2017) ModelFinder: fast model selection for accurate phylogenetic estimates. *Nature Methods*, **14**, 587–589.

Kass RE and Raftery AE (1995) Bayes Factors. *Journal of the American Statistical Association*, **90**, 773–795.

Kaufman L and Rousseeuw P (1987) Clustering by means of medoids. *Statistical Data Analysis Based on the L1-Norm and Related Methods*, 405–416.

Kingma DP and Welling M (2013) Auto-encoding variational bayes. In: Proceedings of the
International Conference on Learning Representations (ICLR). arXiv:1312.6114 [stat.ML].
Kobak D and Berens P (2019) The art of using t-SNE for single-cell transcriptomics. *Nature*
*Communications*, **10**, 1–14.
Kopelman NM, Mayzel J, Jakobsson M, Rosenberg NA, and Mayrose I (2015) CLUMPAK: a
program for identifying clustering modes and packaging population structure inferences
across *K. Molecular Ecology Resources*, **15**, 1179–1191.
Kruskal JB and Wish M (1978) *Multidimensional Scaling*. Sage Publisiinig, Thousand Oaks, CA,
USA.
Lawson DJ, van Dorp L, and Falush D (2018) A tutorial on how not to over-interpret
STRUCTURE and ADMIXTURE bar plots. *Nature Communications*, **9**, 3258.
Leaché AD, Banbury BL, Felsenstein J, De Oca AN-M, and Stamatakis A (2015) Short tree, long
tree, right tree, wrong tree: new acquisition bias corrections for inferring SNP phylogenies.
*Systematic Biology*, **64**, 1032–1047.
Leaché AD, Fujita MK, Minin VN, and Bouckaert RR (2014) Species delimitation using
genome-wide SNP data. *Systematic Biology*, **63**, 534–542.
Linck EB and Battey CJ (2019) Minor allele frequency thresholds strongly affect population
structure inference with genomic datasets. *Molecular Ecology Resources*, **19**, 639–647.
Long C and Kubatko L (2018) The effect of gene flow on coalescent-based species-tree
inference. *Systematic Biology*, **67**, 770–785.
Maaten L van der and Hinton G (2008) Visualizing data using t-SNE. *Journal of Machine*
*Learning Research*, **9**, 2579–2605.
Mace GM (2004) The role of taxonomy in species conservation. *Philosophical Transactions of*
*the Royal Society B: Biological Sciences*, **359**, 711–719.
Martin BT, Bernstein NP, Birkhead RD, Koukl JF, Mussmann SM, and Placyk JS (2013)
Sequence-based molecular phylogenetics and phylogeography of the American box turtles
(*Terrapene* spp.) with support from DNA barcoding. *Molecular Phylogenetics and*
*Evolution*, **68**, 119–134.
Martin BT, Bernstein NP, Birkhead RD, Koukl JF, Mussmann SM, and Placyk Jr JS (2014) On
the reclassification of the *Terrapene* (Testudines: Emydidae): a response to Fritz & Havaš.
*Zootaxa*, **3835**, 292–294.
Martin BT, Douglas MR, Chafin TK, Placyk JS, Birkhead RD, Phillips CA, and Douglas ME
(2020) Contrasting signatures of introgression in North American box turtle (*Terrapene*
spp.) contact zones. *Molecular Ecology*, **29**, 4186–4202.
Mathieson I and McVean G (2012) Differential confounding of rare and common variants in
spatially structured populations. *Nature Genetics*, **44**, 243–246.
Mayr E (1963) *Animal Species and Evolution*. Belknap Press at Harvard University Press,
Cambridge, MA.
Meck JR, Jones MT, Willey LL, and Mays JD (2020) Autecological study of Gulf Coast box
turtles (Terrapene carolina major) in the Florida Panhandle, USA, reveals unique spatial and
behavioral characteristics. *Herpetological Conservation and Biology*, **15**, 293–305.
Milstead WW (1967) Fossil box turtles (*Terrapene*) from central North America, and box turtles
of eastern Mexico. *Copeia*, **1967**, 168–179.
Milstead WW (1969) Studies on the evolution of the box turtles (genus *Terrapene*). *Bulletin of*
*the Florida State Museum, Biological Science Series*, **14**, 1–113.

Milstead WW and Tinkle DW (1967) *Terrapene* of Western Mexico, with comments on species
groups in the genus. *Copeia*, **1967**, 180–187.
Minh BQ, Hahn MW, and Lanfear R (2018) New methods to calculate concordance factors for
phylogenomic datasets. *bioRxiv*, 487801.
Minh BQ, Schmidt HA, Chernomor O, Schrempf D, Woodhams MD, Von Haeseler A, and
Lanfear R (2020) IQ-TREE 2: New models and efficient methods for phylogenetic inference
in the genomic era. *Molecular Biology and Evolution*, **37**, 1530–1534.
Minx P (1992) Variation in phalangeal formulas in the turtle genus *Terrapene*. *Journal of
Herpetology*, **26**, 234–238.
Minx P (1996) Phylogenetic relationships among the box turtles, Genus *Terrapene*.
*Herpetologica*, **52**, 584–597.
Molloy EK and Warnow T (2018) To include or not to include: the impact of gene filtering on
species tree estimation methods. *Systematic Biology*, **67**, 285–303.
Mussmann SM, Douglas MR, Oakey DD, and Douglas ME (2020) Defining relictual
biodiversity: Conservation units in speckled dace (Leuciscidae: *Rhinichthys osculus*) of the
Greater Death Valley ecosystem. *Ecology and Evolution*, **10**, 10798–10817.
Nakagawa S and Freckleton RP (2008) Missing inaction: the dangers of ignoring missing data.
*Trends in Ecology & Evolution*, **23**, 592–596.
Newton LG, Starrett J, Hendrixson BE, Derkarabetian S, and Bond JE (2020) Integrative species
delimitation reveals cryptic diversity in the southern Appalachian Antrodiaetus unicolor
(Araneae: Antrodiaetidae) species complex. *Molecular Ecology*, **29**, 2269–2287.
Nguyen L-T, Schmidt HA, von Haeseler A, and Minh BQ (2015) IQ-TREE: A fast and effective
stochastic algorithm for estimating maximum-likelihood phylogenies. *Molecular Biology
and Evolution*, **32**, 268–274.
Nielsen R, Paul JS, Albrechtsen A, and Song YS (2011) Genotype and SNP calling from next-
generation sequencing data. *Nature Reviews Genetics*, **12**, 443.
Nieuwolt PM (1996) Movement, activity, and microhabitat selection in the western box turtle,
*Terrapene ornata luteola*, in New Mexico. *Herpetologica*, 487–495.
Nosil P and Feder JL (2012) Genomic divergence during speciation: causes and consequences.
*Philosophical Transactions of the Royal Society B: Biological Sciences*, **367**, 332–342.
Pedregosa F, Varoquaux G, Gramfort A, Michel V, Thirion B, Grisel O, Blondel M, Prettenhofer
P, Weiss R, and Dubourg V (2011) Scikit-learn: Machine learning in Python. *Journal of
Machine Learning Research*, **12**, 2825–2830.
Peterson BK, Weber JN, Kay EH, Fisher HS, and Hoekstra HE (2012) Double digest RADseq: an
inexpensive method for de novo SNP discovery and genotyping in model and non-model
species. *PLOS ONE*, **7**, e37135.
Pickrell JK and Pritchard JK (2012) Inference of population splits and mixtures from genome-
wide allele frequency data. *PLoS Genetics*, **8**, e1002967.
Plummer M V (2003) Activity and thermal ecology of the box turtle, Terrapene ornata, at its
southwestern range limit in Arizona. *Chelonian Conservation and Biology*, **4**, 569–577.
Pritchard JK, Stephens M, and Donnelly P (2000) Inference of population structure using
multilocus genotype data. *Genetics*, **155**, 945–959.
De Queiroz K (2007) Species concepts and species delimitation. *Systematic Biology*, **56**, 879–
886.
R Development Core Team (2018) R: A language and environment for statistical computing.

https://cran.r-project.org/.

Rambaut A, Drummond AJ, Xie D, Baele G, and Suchard MA (2018) Posterior summarization in bayesian phylogenetics using Tracer 1.7 (E Susko, Ed,). *Systematic Biology*, **67**, 901–904.

Rodriguez-Galiano VF, Ghimire B, Rogan J, Chica-Olmo M, and Rigol-Sanchez JP (2012) An assessment of the effectiveness of a random forest classifier for land-cover classification. *ISPRS Journal of Photogrammetry and Remote Sensing*, **67**, 93–104.

Rousseeuw PJ (1987) Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. *Journal of Computational and Applied Mathematics*, **20**, 53–65.

Rousset F (2008) genepop '007: a complete re-implementation of the genepop software for Windows and Linux. *Molecular Ecology Resources*, **8**, 103–106.

Rubin DB (1976) Inference and missing data. *Biometrika*, **63**, 581–592.

Schrempf D, Minh BQ, De Maio N, von Haeseler A, and Kosiol C (2016) Reversible polymorphism-aware phylogenetic models and their application to tree inference. *Journal of Theoretical Biology*, **407**, 362–370.

Shepard RN, Romney AK, and Nerlove SB (1972) *Multidimensional Scaling: Theory and Applications in the Behavioral Sciences: I. Theory.* Seminar Press.

Smith ML and Carstens BC (2020) Process□based species delimitation leads to identification of more biologically relevant species. *Evolution*, **74**, 216–229.

Smith ML, Ruffley M, Espíndola A, Tank DC, Sullivan J, and Carstens BC (2017) Demographic model selection using random forests and the site frequency spectrum. *Molecular Ecology*, **26**, 4562–4573.

Smith HM and Smith RB (1980) Synopsis of the herpetofauna of Mexico: Volume VI, guide to Mexican turtles, bibliographic addendum III. John Johnson, North Bennington, Vermont ("1979"), xviii + 1044 pp.

Soltis DE, Morris AB, McLachlan JS, Manos PS, and Soltis PS (2006) Comparative phylogeography of unglaciated eastern North America. *Molecular Ecology*, **15**, 4261–4293.

Spinks PQ, Thomson RC, Lovely GA, and Shaffer HB (2009) Assessing what is needed to resolve a molecular phylogeny: Simulations and empirical data from emydid turtles. *BMC Evolutionary Biology*, **9**, 56.

Stephens PR and Wiens JJ (2003) Ecological diversification and phylogeny of emydid turtles. *Biological Journal of the Linnaean Society*, **79**, 577–610.

Sukumaran J and Knowles LL (2017) Multispecies coalescent delimits structure, not species. *Proceedings of the National Academy of Sciences of the United States of America*, **114**, 1607–1611.

Taylor WE (1895) The box tortoises of North America. *Proceedings of the United States National Museum*, **17**, 573–588.

Tibshirani R, Walther G, and Hastie T (2001) Estimating the number of clusters in a data set via the gap statistic. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, **63**, 411–423.

To T-H, Jung M, Lycett S, and Gascuel O (2016) Fast dating using least-squares criteria and algorithms. *Systematic Biology*, **65**, 82–97.

Via S (2009) Natural selection in action during speciation. *Proceedings of the National Academy of Sciences*, **106**, 9939–9946.

Walker DE and Avise JC (1998) Principles of phylogeography as illustrated by freshwater and terrestrial turtles in the southeastern United States. *Annual Review of Ecology and*

*Systematics*, **29**, 23–58.
Wattenberg M, Viégas F, and Johnson I (2016) How to use t-SNE effectively. *Distill*, **1**, e2.
Webb RG, Minckley WL, and Craddock JE (1963) Remarks on the Coahuilan box turtle,
Terrapene coahuila (Testudines, Emydidae). *The Southwestern Naturalist*, **8**, 89–99.
Wiens JJ, Kuczynski CA, and Stephens PR (2010) Discordant mitochondrial and nuclear gene
phylogenies in emydid turtles: implications for speciation and conservation. *Biol. J. Linn.*
*Soc. Lond.*, **99**, 445–461.
Yang Z and Rannala B (2010) Bayesian species delimitation using multilocus sequence data.
*Proceedings of the National Academy of Sciences*, **107**, 9264–9269.
910
911

912 **TABLE 1** Topology tests for hypothesized *Terrapene* phylogenies. Sanger sequencing and
913 morphology trees are based on previously published data whereas those representing
914 SVDQUARTETS and POMO (Polymorphism-Aware Model) were generated in this study from
915 ddRADseq data. *P*-values in bold with * indicate significance (P>0.05/highly weighted).
916
917

| Guide Tree | Log-likelihood | ΔLL | BP-RELL | P-KH | P-SH | C-ELW | P-AU |
|---|---|---|---|---|---|---|---|
| Morphology | -2639307.9 | 601.5 | 0.00 | 0.01 | 0.02 | 0.00 | 0.01 |
| PoMo | -2639200.2 | 493.8 | 0.01 | 0.03 | **0.06***  | 0.01 | 0.03 |
| Sanger | -2638898.4 | 192.0 | **0.23*** | **0.24*** | **0.41*** | **0.23*** | **0.26*** |
| SVDquartets | -2638706.4 | 0.0 | **0.75*** | **0.76*** | **1.00*** | **0.75*** | **0.81*** |

ΔLL=change in log-likelihood
BP-RELL=Bootstrap proportions using RELL method (weights sum to 1)
P-KH=Kishino-Hasegawa test
P-SH=Shimodaira-Hasegawa test
C-ELW=Expected likelihood weight (sum to 1)
P-AU=Approximately unbiased test
924
925

**TABLE  2** Species-delimitation results from Bayes Factor Delimitation (BFD) in *Terrapene.*
Bayes factors (BF) depict support among models and were calculated as 2 X (MLE$_1$-MLE$_2$). An
*=best supported models;+=taxa grouped together; /=multiple groupings. DS=*T. o. luteola*,
ON=*T. o. ornata*, EA=*T. c. carolina*, GUFL=*T. c. major* from Florida, GUMS=Mississippi *T. c.*
*major*, CH=*T. coahuila*, FL=*T. c. bauri*, TT=*T. m. triunguis*, and MX=*T. m. mexicana*. East=all
*T. carolina* and *T. mexicana*, West=all *T. ornata*. Outgroup (not shown) included *Clemmys*
*guttata*.
933

| BFD* Model | MLE† | K‡ | Rank§ | BF¶ |
|---|---|---|---|---|
| All Separate* | -2403.39 | 10 | 1 | - |
| DS+ON* | -2404.34 | 9 | 2 | 1.90 |
| EA+GUFL | -2417.84 | 9 | 3 | 28.91 |
| GUMS+GUFL | -2427.58 | 9 | 4 | 48.39 |
| GUMS+CH | -2448.61 | 9 | 5 | 90.44 |
| GUMS+CH/GUFL+EA | -2461.28 | 8 | 6 | 115.79 |
| GUMS+GUFL+CH | -2489.62 | 8 | 7 | 172.45 |
| EA+FL | -2511.83 | 9 | 8 | 216.89 |
| GUMS+GUFL+CH+EA | -2514.86 | 7 | 9 | 222.94 |
| EA+FL+GUFL | -2552.22 | 8 | 10 | 297.66 |
| EA+FL/CH+GUMS | -2555.16 | 8 | 11 | 303.53 |
| EA+FL+GUFL/CH+GUMS | -2594.91 | 7 | 12 | 383.04 |
| EA+CH+GUMS+GUFL+TT | -2607.72 | 6 | 13 | 408.66 |
| EA+CH+GUMS+GUFL+MX | -2657.48 | 6 | 14 | 508.19 |
| EA+FL+CH+GUMS+GUFL | -2693.37 | 6 | 15 | 579.96 |
| EA+CH+GUMS+GUFL+TT+MX | -2719.02 | 5 | 16 | 631.27 |
| ON+DS/EA+TT+MX+CH+GUMS+GUFL/FL | -2720.23 | 4 | 17 | 633.69 |
| EA+FL+CH+GUMS+GUFL+TT | -2800.56 | 5 | 18 | 794.35 |
| EA+FL+CH+GUMS+GUFL+TT+MX | -2926.20 | 4 | 19 | 1045.62 |
| East/West | -2926.56 | 3 | 20 | 1046.35 |

934  †MLE=Marginal likelihood estimates
935  ‡*K*=# tips
936  §Rank=model ranking based on MLE (lower=better)
937  ¶BF=Bayes factors
938
939

**TABLE 3** Five best (of 51) DELIMITR models describing six *Terrapene* taxa. Model=rank
determined by random forest (RF) vote counts (=# Votes). An *=best supported model. Grouped
taxa are separated by+, whereas /=distinct groups. "x" separates migration events promoting
secondary contact, with multiple migrations per model separated by commas. ON=*T. o. ornata*,
TT=*T. m. triunguis*, FL=*T. c. bauri*, GUMS=*T. c. major* from Mississippi, GUFL=Florida *T. c.*
*major*, EA=*T. c. carolina*. Error=proportion of incorrect model choices.
946

| Model | # Votes | Species (# delimited) | Secondary Contact | Error |
|-------|---------|-----------------------|-------------------|-------|
| 17* | 464 | ON/TT/FL/GUMS+GUFL+EA (4) | ONxTT, TTxGU+EA, FLxGU+EA | 0.017 |
| 14 | 445 | ON/TT/FL/GUMS+GUFL+EA (4) | TTxGU+EA, FLxGU+EA | 0.036 |
| 3 | 441 | ON/TT+FL+GUMS+GUFL+EA (2) | ONxTT+FL+GU+EA | 0.009 |
| 8 | 359 | ON/TT/FL+GUMS+GUFL+EA (3) | ONxTT, TTxFL+GU+EA | 0.009 |
| 30 | 218 | ON/TT/FL/GUMS+GUFL/EA (5) | TTxGU, FLxEA, GUxEA | 0.007 |

947
948

**FIGURE 1** Range map and sample localities (=circles) for N=214 *Terrapene*. Closed circles=*T. carolina* samples without subspecific identification in the field. Cross-hatched areas=known hybrid zones. Headings and subheadings represent species and subspecies. *Terrapene carolina major*=*T. carolina major* and includes distinct subpopulations from Mississippi (GUMS) and Florida panhandle (GUFL).

958
959
**FIGURE 2** Chronogram reflecting relationships among 214 *Terrapene* ddRADseq samples as
generated in IQ-TREE v2.1.2 and time-calibrated using LSD2. Node support was assessed with
1,000 ultrafast bootstrap (UFBoot) replicates, and site concordance-factors (sCF) calculated from
10,000 randomly-sampled quartets. Well-supported nodes (UFBoot≥95%, sCF≥50%) are
represented by color-coded circles or squares, with squares showing fossil calibration points.
Node bars reflect 95% confidence intervals based on 1,000 simulated trees. *Clemmys guttata* and
*Emydoidea blandingii* represent outgroups.

**FIGURE 3** Species trees, TREEMIX, and species delimitation results among *Terrapene* ddRADseq samples. Phylogenies (N=214) were generated by (a) SVDQUARTETS and (b) POMO with 26 populations grouped by subspecies and state locality. An * and+above branches=100% and≥95% bootstrap support. (c) Migration supported by TREEMIX (blue/solid arrows) and previously published results (red/dashed arrows). (d) Species delimitations for UML (N=117), multispecies coalescent (MSC; BFD=Bayes Factor Delimitation; N=37), and process-based (DELIMITR; N=28) methods. UML data filtering allowed ≤ 25% missing data per-individual and per-population, with minor allele frequency filters=5% (CMDS/T-SNE/VAE), 1% (ISOMDS), and T-SNE perplexity=15. UML includes RF=random forest, visualized with CMDS and ISOMDS ordination, T-SNE, and VAE, with bar plots depicting assignment proportions among 100 replicates and aligning with chronogram tips. RF and T-SNE optimal *K* were assessed using partition around medoids (PAM)+gap statistic (GS), PAM+highest mean silhouette width (HMSW), and hierarchical clustering (HC)+HMSW, whereas VAE, BFD*, and DELIMITR used DBSCAN, Bayes Factors (BF) and RF votes. Blue/dashed arrows show gene flow supported by DELIMITR.

984
985
**FIGURE 4** Heatmaps depicting mean and standard deviation (SD) of optimal *K* among 100
unsupervised machine learning species-delimitation replicates. Input ddRADseq alignments were
filtered with a maximum of 25%, 50%, 75%, and 100% (=no filter) missing data allowed per-
individual and per-population, and with minor allele frequency (MAF) filters as 5%, 3%, 1%,
and 0% (=no filter). (a) and (b)=Pairwise missing data heatmaps for three dimensionality-
reduction methods (CMDS and ISOMDS=classical and isotonic multidimensional scaling), T-
SNE=t-distributed stochastic neighbor embedding *versus* three clustering algorithms [(partition
around medoids+gap statistic (GS)]; HC=hierarchical clustering+highest mean silhouette width
(HMSW); PAM=partition around medoids+HMSW. (c) and (d)=T-SNE heatmap panels
comparing clustering algorithms with ten perplexity settings. (e) and (f)=VAE (variational
autoencoder) heatmaps with optimal *K* chosen via DBSCAN.

998
999
**Figure 5** Regressions showing relationship between mean optimal *K (*y-axes), missing data, and
minor allele frequency (MAF) filtering parameters. Missing data was filtered both per-individual
(x-axes) and per-population (panel rows), with a maximum allowed of 25%, 50%, 75%, and
100% (=no filtering). Minor allele frequency (MAF) filters of 5%, 3%, 1%, and 0% (=no
filtering) were also applied (panel columns). (a) Colors correspond to the dimensionality-
reduction methods: CMDS and ISOMDS=classical and isotonic multidimensional scaling, T-
SNE=t-distributed stochastic neighbor embedding, VAE=variational autoencoder. (b) Colors
indicate three clustering algorithms: GS=partition around medoids+gap statistic,
HC=hierarchical clustering+highest mean silhouette width (HMSW), PAM=partition around
medoids+HMSW.