Coral cover surveys corroborate predictions on reef adaptive potential to thermal stress

Oliver Selmoni[1,2], Gaël Lecellier[2,3], Laurent Vigliola[2], Véronique Berteaux-Lecellier[2], Stéphane Joost[1*]

1 - Laboratory of geographic information systems, Ecole Polytechnique Federale de Lausanne, Lausanne Switzerland

2 - UMR250/9220 ENTROPIE IRD-CNRS-Ifremer-UNC-UR, Labex CORAIL, Nouméa, New Caledonia

3 - UVSQ, Université de Paris-Saclay, Versailles, France

*=corresponding author

Abstract

As anomalous heat waves are causing the widespread decline of coral reefs worldwide, there is an urgent need to identify coral populations tolerant to thermal stress. Heat stress adaptive potential is the degree of tolerance expected from evolutionary processes and, for a given reef, depends on the arrival of propagules from reefs exposed to recurrent thermal stress. For this reason, assessing spatial patterns of thermal adaptation and reef connectivity is of paramount importance to inform conservation strategies.

In this work, we applied a seascape genomics framework to characterize the spatial patterns of thermal adaptation and connectivity for coral reefs of New Caledonia (Southern Pacific). In this approach, remote sensing of seascape conditions was combined with genomic data from three coral species. For every reef of the region, we computed a probability of heat stress adaptation, and two indices forecasting inbound and outbound connectivity. We then compared our indicators to field survey data, and observed that decrease of coral cover after heat stress was lower at reefs predicted with high probability of adaptation and inbound connectivity. Last, we discussed how these indicators can be used to inform local conservation strategies and preserve the adaptive potential of New Caledonian reefs.

Introduction

Coral bleaching is one of the main causes of severe declines of coral reefs around the world[1-3]. This phenomenon is mainly caused by anomalous heat waves leading to the death of hard-skeleton corals, which are the cornerstone of reefs[2]. Over the last 30 years mass coral bleaching events repeatedly struck worldwide, causing losses of local coral cover up to 50%[1,3]. In the coming years, bleaching conditions are expected to occur more frequently and to become persistent by 2050[4]. As up to one third of marine wildlife depends on coral reef for survival and at least 500 million people livelihoods worldwide[5], there is an urgent need to define new strategies to improve the preservation of these ecosystems[6].

Recent research reported reefs that rebounded from repeated heat stress and showed an increased thermal resistance[7–11]. Adaptation of corals against heat stress might explain such observations[12,13]. Under this view, identifying adapted coral populations is of paramount importance, as conservation strategies might be established to protect reefs hosting these corals from local stressors (e.g. via marine protected areas, MPAs)[14]. Furthermore, adapted corals could be of use in reef restoration plans and repopulate damaged reefs[15]. The adaptive potential of corals at a given reef depends on the arrival of propagules from reefs exposed to recurrent thermal stress[16,17]. This is why characterizing spatial patterns of thermal adaptation and reef connectivity is crucial to empower the conservation of the adaptive potential of corals[16,17].

Seascape genomics is a powerful method to evaluate spatial patterns of environmental variation and connectivity[17,18]. This method relies on a thorough analysis of environmental conditions around reefs using satellite data. Daily records of surface temperature are remotely sensed using satellites, and processed to compute indicators of thermal patterns associated with bleaching events[17,19,20]. Corals exposed to different thermal patterns are then sampled and genotyped to identify genetic variants correlated with these indicators[17,18]. The association between genetic variants and a given indicator defines a model of adaptation that can be used to predict the probability of adaptation, based on the value of the indicator itself[17,21]. In addition, by remote sensing sea current movements, it is possible to draw a connectivity map between every reef within an area of interest. This can be done using spatial graphs that resume multi-generational dispersal matching spatial patterns of genetic diversity in a given species[22]. This approach results in indices of connectivity defining, for a reef of

interest, the predisposition in sending (outbound connectivity) and receiving (inbound

connectivity) propagules to/from neighboring reefs[17].

In this study, we predicted spatial patterns of heat stress adaptation and connectivity for over

1000 km of coral reefs of New Caledonia, in the Southern Pacific (Fig. 1). The study area

encompassed the barrier reef surrounding Grande Terre, the main islands of the Archipelago,

as well as the intermediary and fringing enclosed in the lagoon. We also considered reefs

surrounding the Loyalty Islands (Ouvéa, Lifou and Maré) and the Astrolabe (east of Grande

Terre) and those in the Entrecasteaux and Petri atolls (north of Grande Terre). We first used

remote sensing data to (1) evaluate the thermal variability of the study area and (2) estimate

patterns of sea current connectivity between reefs. Next, we employed genomic data from a

seascape genomics study on three coral species of the region[23] in order to (1) compute the

probability of adaptation to heat stress across the whole region, and (2) verify whether

predicted reef connectivity matched genetic correlation between corals. Last, we compared

our predictions with field surveys of living coral cover recorded by the New Caledonian

observational network of coral reef (RORC)[24]. Our results suggest that negative effects of

recent heat stress on coral cover are mitigated at reefs predicted with high probability of heat

stress adaptation and inbound connectivity. We then discuss the conservation status of reefs

around New Caledonia, and assess how conservation indices of probability of adaptation and

connectivity can be used to protect the adaptive potential of corals of the region.

Figure 1. Reef system of New Caledonia. Coral reefs are highlighted in green. The blue dots correspond to sites of coral cover survey of the New Caledonian observational network of coral reef[24]. The red dots correspond to the sampling locations of coral specimen for the seascape genomics study that provide genetic data in the present study[23]. Sea regions highlighted in purple correspond to the marine reserves and protected areas as catalogued by the French agency for MPAs (http://www.aires-marines.fr/).

Results

Heat stress and probability of adaptation

The remote sensing data of sea surface temperature were processed to calculate the frequency of bleaching alert conditions ($BAF_{overall}$) across the reef system of New Caledonia (Fig. 2a). $BAF_{overall}$ was higher in reefs on the western coast of Grande Terre

(average BAF: 0.16±0.04) than in those on the eastern coast (0.08±0.03). Reefs in Lifou, Maré

and Isle of Pines displayed $BAF_{overall}$ values comparable to those on the eastern coast of

Grande Terre (0.09±0.03, 0.10±0.02 and 0.11±0.01, respectively), while in Ouvéa and

Entrecasteaux reefs the $BAF_{overall}$ values (0.15±0.01 and 0.12±0.01, respectively) were closer

to the values observed on the western coast.

Previous seascape genomics analyses on three corals of the region (*Acropora millepora,*

Pocillopora damicornis and Pocillopora acuta) revealed the presence of multiple genetic

variants (32 in total) potentially implicated in heat stress resistance[23]. We employed this data

to construct a logistic model of heat stress adaptation defining the probability of presence of

potentially adaptive variants (PA_{HEAT}) as a function of $BAF_{overall}$ (Fig. 2b). This model was then

used to produce a map of predicted PA_{HEAT} values for the whole region (Fig. 2c). It revealed

accentuated differences compared with $BAF_{overall}$ patterns, with PA_{HEAT} generally above 0.65

in reefs on the western coast of Grande Terre, Isle of Pines, Entrecasteaux and Ouvéa. In

contrast, values below 0.35 were observed at reefs located along the east coast of Grande

Terre, in Lifou and Maré.

Figure 2. Bleaching alert frequency and probability of heat stress adaptation. In (a), bleaching alert frequency (BAF$_{overall}$) is displayed for each reef of New Caledonia. This value is derived from remote sensing data of sea surface temperature, and describes the frequency of cumulated heat stress conditions that can lead to bleaching. In (b), a logistic model of heat stress adaptation is shown. This model is based on the frequencies of potentially adaptive genotypes of three coral species of New Caledonia[23]. The plot displays the probability of adaptation to heat stress as a logistic function of BAF$_{overall}$ (blue line, with the grey band showing the 95% interval of confidence). The model shown in (b) was used to translate BAF$_{overall}$ displayed in (a) in the probability of adaptation (PA$_{HEAT}$) against heat stress. The map in (c) displays PA$_{HEAT}$ for every reef of New Caledonia.

Reef connectivity and genetic correlation between corals

Remote sensing of sea current was used to compute a spatial graph of seascape connectivity predicting cost distances between reefs of New Caledonia. By using generalized linear mixed models (GLMMs) regression, we investigated whether such predictions on reef connectivity were representative proxies of the population structures of corals of the region. In three studied species (*A. millepora, P. damicornis* and *P. acuta*), we found that the genetic correlations between corals were significantly associated with the seascape cost distances separating the reefs where corals were sampled (*A. millepora*: p=1.46e-06; *P. damicornis*: p=1.63e-10 and *P.* acuta: p=6.7e-05; Fig. 3). This relationship was more stressed in the two *Pocillopora* species (regression coefficient for *P. damicornis*: β=-8.7E-05+ 1.4E-05; for *P. acuta*: β=-3.1E-05 ± 7.8E-06) than in *A. millepora* (β=-7.9E-06 ± 1.6E-06). The GLMMs accounted for the ancestral distance between pairs of individuals (*i.e.* the difference in

152 admixture from ancestral populations) which was found significantly associated to genetic

153 correlations between corals in all the three species (p~0; Fig. S1).

Figure 3. Seascape cost distance and genetic correlation between corals. The three plots display genetic correlations between pairs of corals sampled in New Caledonia as a function of the cost distance separating reefs where corals were sampled (blue line, with the grey band showing the 95% interval of confidence). Genetic correlations were computed as the correlation of single-nucleotide-polymorphisms, while seascape cost distance was predicted through seascape connectivity graphs. Each plot displays this association for a different species (a: *Acropora millepora*, b: *Pocillopora damicornis*, c: *Pocillopora acuta*).

Reef connectivity indices

The seascape connectivity graph was used in the calculation of two indices describing the

dispersal characteristics of every reef of New Caledonia (Outbound Connectivity Index, OCI,

Fig. 4a; Inbound Connectivity Index, ICI, Fig. 4b). Both indices are expressed in km^2, as they

represent the area of the reefs neighboring a reef of interest. In OCI, neighboring reefs are

those potentially receiving propagules from the reef of interest, while in ICI neighboring reefs

are those potentially sending propagules towards the reef of interest.

Reefs that are more distant to Grande Terre (Entrecasteaux, Lifou, Maré and Ouvéa) had

lower OCI (average OCI: 202±35 km^2, 410±270 km^2, 210±66 km^2, 864±254 km^2, respectively;

Fig. 4a) than reefs surrounding Grande Terre. Reefs surrounding Grande Terre showed highest

values on the southern reefs of the eastern coast (1929±300 km^2), while lower values were

predicted for the rest of the eastern coast (1377±435 km^2) and the southern part of the

western coast (1119±82 km^2). OCI was lower at reefs located at the northern extremity of

Grande Terre (632±244 km^2).

Like with OCI, ICI was lower at reefs furthest from Grande Terre (Entrecasteaux, Ouvéa, Lifou,

Maré; average ICI of 460±93 km^2, 177±7 km^2, 97±30 km^2, 111±6 km^2, respectively; Fig. 4b).

ICI at reefs surrounding Grande Terre displayed a net contrast between the east and west

coasts, where ICI was lower on the east (498±113 km^2) than the west (1287±407 km^2).

Figure 4. Connectivitiy indices. Two connectvitiy indices based on sea current data are shown for every reef of New Caledonia. In a), the Outbound Connectivity Index (OCI) describes the predisposition in sending dispersal to neighboring reefs. In b), the Inbound Connectivity Index (ICI) summarizes the predisposition in receiving propagules from neighboring reefs. Both indices are given in km^2, as this represents the total surface of neighboring reefs.

Coral cover analysis

Underwater surveys of New Caledonian reefs were analyzed to characterize the association

of living coral cover with recent thermal stress (BAF$_{previous\ year}$), probability of heat stress

adaptation (PA$_{HEAT}$) and connectivity indices (ICI and OCI; Fig. 5). We first investigated the

association between coral cover and individual explanatory variables using single fixed effect

GLMMs (Fig. 5a-d). We found that coral cover was significantly associated with BAF$_{previous\ year}$

(p=0.02), and that this association was of negative sign (β=-0.06±0.03; Fig. 5a). In contrast,

none of the other univariate models resulted in a significant association with coral cover

(PA$_{HEAT}$: p=0.93, Fig. 5b; OCI: p=0.46, Fig. 5c; ICI: p=0.41, Fig. 5d). The Akaike Information

Criterion (AIC) suggested a higher quality-of-fit for the model employing BAF$_{previous\ year}$ as

explanatory variable (AIC=-883), compared with the other univariate models (PA$_{HEAT}$: AIC=-

878; OCI: AIC=-879, ICI: AIC=-879).

We then investigated whether the negative association between coral cover and $BAF_{previous}$

$_{year}$ varied under different values of PA_{HEAT}, OCI or ICI. This analysis employed three bivariate

GLMM setting as fixed effects $BAF_{previous\ year}$ and the interaction between $BAF_{previous\ year}$ and

each of the three other explanatory variables (PA_{HEAT}, OCI, ICI; Fig. 5e-g). In comparison to all

the univariate models, those accounting for the interaction of $BAF_{previous\ year}$ with PA_{HEAT} and

ICI resulted in a higher quality-of-fit (AIC=-886 and AIC=-888, respectively). In both cases, the

effect of $BAF_{previous\ year}$ was significant ($p<0.01$) and of negative sign, whereas the effect of the

interaction was also significant but of positive sign (for the interaction with PA_{HEAT}:

$β=+0.05±0.02$, $p=0.03$; with ICI: $β=+0.07±0.03$, $p=0.01$; Fig. 5e-f). In contrast, the bivariate

model incorporating OCI had a quality-of-fit comparable to univariate models (AIC=-883), and

showed no significant association in interaction with $BAF_{previous\ year}$ (Fig. 5g).

Figure 5. Coral cover association analysis. The plots display the association of coral cover rates (blue line, with the grey band showing the 95% interval of confidence) with recent thermal stress ($BAF_{previous\ year}$), probability of heat stress adaptation (PA_{HEAT}) and connectivity indices (inbound connectivity index, ICI, and outbound connectivity index, OCI). In plots (a) to (d), the association with coral cover rates is shown for each explanatory variable alone (a: $BAF_{previous\ year}$, b: PA_{HEAT}, c: OCI, d: ICI). In the remaining plots, the association between coral cover and $BAF_{previous\ year}$ and is showed across different ranges PA_{HEAT} (e), OCI (f) and ICI (g).

202
203

Discussion

Local divergences in conservation indices

The metrics computed in this study stressed the strong asymmetry, in terms of both probability of heat stress adaptation (PA_{HEAT}) and connectivity (inbound connectivity index, ICI; outbound connectivity index; OCI), between reefs on the two coasts of Grande Terre (Fig. 2a, Fig.4). The climatic differences between the two coasts are modulated by the mountain range covering Grande Terre, and water conditions inside the lagoon reflect the combination of these differences coupled with oceanic influences[25]. For example, the southern part of the west coast of Grande Terre is subjected to coastal upwelling, a seasonal phenomenon bringing cold water to the surface[26]. While logic would suggest that cold water alleviates heat stress, research on the Great Barrier Reef in Australia showed that intense upwelling is followed by severe heat stress, and consequent coral bleaching[27]. While it is unknown whether this same effect occurs on the south-western coast of Grande Terre, this region does enclose the reefs that are predicted to experience the highest frequency of bleaching conditions across New Caledonia, and consequently to host corals with the highest PA_{HEAT} (Fig. 2).

Asymmetrical spatial patterns between the coasts of Grande Terre were also predicted for connectivity (Fig. 4), and this matched the genetic population structure of corals of the region (Fig. 3). In this work, we estimated connectivity using a straightforward approach, conceived to be reproduceable on any reef system around the world but that might lead to local inaccuracies[17]. However, our predictions were generally consistent with previous work that characterized the regional water circulation around New Caledonia using more sophisticated methods (i.e. combining oceanographic models, in situ measurements and shipboard detectors of sea currents)[28]. For instance, we observed a higher inbound connectivity index (ICI) on the west coast of Grande Terre (Fig. 4b), and a higher outbound connectivity index (OCI) on the east coast (Fig. 4a). This west-oriented connectivity was expected because of the South Equatorial Current crossing the archipelago in this direction[28]. This current bifurcates at the encounter of the New Caledonian shelf into 1) a weak and transient south-east oriented current between the Loyalty Islands and Grande Terre, and 2) a strong north-west oriented current flowing north of the Loyalty Islands[26,28,29]. This bifurcation explains the lower OCI observed in Lifou and Maré, compared with Ouvéa and the Astrolabe atolls. Last, the water

circulation inside the lagoon follows the north-west orientation of trade winds[26], resulting in

higher OCI in the south and higher ICI in the north.

Predictions of reef connectivity and PA$_{HEAT}$ varied considerably across the different regions of

the study area (Fig. 2, 4), and conservation planning should account for these regional

peculiarities[14,30]. In table 1, we interpret the local divergences in values of PA$_{HEAT}$, ICI and OCI

under a conservation perspective.

Table 1. Implications for reef conservation in New Caledonia. The table describes the implications for reef conservation of the probability of heat stress adaptation (PA$_{HEAT}$), the outbound and inbound connectivity indices (OCI, ICI) predicted for different regions of the New Caledonia reef system. Information on the existing marine protected areas were retrieved from the French agency for MPAs (http://www.aires-marines.fr/).

East coast of Grande Terre

 | The east coast of Grande Terre hosts reefs predicted with low ICI and PA$_{HEAT}$. In contrast, OCI was generally higher than in the rest of the Archipelago. Reefs of strategic importance might be those located in the southern part as they had the highest OCI of the Archipelago, and also moderate levels of PA$_{HEAT}$. To date, only 4 km^2 of reefs in this area are protected. In addition, the establishment of nurseries with heat stress adapted corals might increase the adaptive potential of these reefs. |
| ***West coast of Grande Terre***

 | Reefs on the west coast of Grande Terre generally displayed higher levels of ICI and PA$_{HEAT}$, compared with the rest of the Archipelago. Under an adaptive potential perspective, reefs in the northern part are of paramount importance as they receive the propagules from all the south-western reefs that experienced frequent heat stress. No MPA is established in this area. Another strategic region are the reefs in front of Noumea, in the southern part of the west coast, since they were predicted with high PA$_{HEAT}$ and OCI. Here, more than 200 km^2 of protected areas are already established. |
| ***South Lagoon***

 | The South Lagoon displayed heterogenous patterns of PA$_{HEAT}$ and connectivity. The highest PA$_{HEAT}$ were observed in the south-western extremity, which in turn was a region predicted with low OCI. The eastern part might be more interesting under a conservation perspective, as it was predicted with moderate PA$_{HEAT}$ and high OCI. These reefs are located upstream of the trade winds, and can simultaneously send propagules to both coasts of Grande Terre. A large marine reserve (180 km^2) is already established to protect these reefs. As for the southern part of the east coast, coral nurseries of heat stress adapted colonies might increase the adaptive potential of this region. |
| ***Northern reefs and Entrecasteaux reefs***

 | Northern reefs and Entrecasteaux reefs were predicted with moderate to high levels of PA$_{HEAT}$, and low values of OCI and ICI, compared with the reefs around Grande Terre. The critical region under an adaptive potential perspective might be the eastern part of Northern reefs. This is because these reefs depend on the incoming propagules from the east coast of Grande Terre, which are predicted with low PA$_{HEAT}$. |
| ***Loyalty Islands, Astrolabe and Petri atolls***

 | The main conservation issue for all the reefs in this region is the low ICI. It is likely that arrival of propagules substantially depends on the reefs from Vanuatu (Fig. 1), located ~200 km upstream on the South Equatorial Current. Reefs in Ouvéa and Astrolabe atolls (already protected) might be of strategic importance, as they were predicted with moderate to high values of PA$_{HEAT}$ and OCI. Since reefs in Maré and Lifou showed low PA$_{HEAT}$, establishment of nurseries with heat stress adapted coral might be useful under an adaptive potential perspective. |

Predictions on adaptive potential match coral cover

Heat exposure is considered to be one of the main drivers of coral mortality worldwide[11,31,32]. Our results were consistent with this view, as we found a significant negative association of coral cover with $BAF_{previous\ year}$ (Fig. 5a). Adaptation might contribute to increase thermal tolerance in corals, but its potential depends on two elements: the existence of adapted corals and the presence of reef connectivity patterns facilitating their dispersal. In this study, we found both of these elements (PA_{HEAT} and ICI) as associated with reduced loss of coral cover after thermal stress.

Previous studies have reported reefs that display increased thermal tolerance after recurrent exposure to heat stress[7–11], and recent research suggested that the thermal contrasts of New Caledonia might have driven adaptive processes in corals of the region[23]. Our results supported this view: while recent thermal stress ($BAF_{previous\ year}$) was associated with a reduction in coral cover, this reduction was mitigated at reefs that have experienced past thermal stress and were therefore predicted with high PA_{HEAT} (Fig. 5e). In addition, PA_{HEAT} alone did not result in a significant association with coral cover rates (Fig. 5b), and this might be due to the fact that thermal adaptation is advantageous only in response to heat stress. Indeed, previous research reported trade-offs in traits involved in local adaptation and acclimatization to heat stress in corals [33]. These trade-offs might explain why the highest rates of coral cover (>0.4) in absence of heat stress ($BAF_{previous\ year}$=0) were mainly observed at reefs with low PA_{HEAT} (Fig. 5e).

Outbound connectivity was not found to be associated with changes in coral cover (Fig. 5c,f). This is not surprising, because beneficial effects of dispersal are expected at reefs receiving incoming propagules, rather than the opposite [16,34]. Indeed, inbound connectivity was found to mitigate the negative association between $BAF_{previous\ year}$ and coral cover (Fig. 5g). Two non-mutually exclusive reasons might explain this observation. First, high levels of incoming propagules might facilitate the turnover of dead colonies caused by heat stress[35], although it has to be noted that this kind of recovery usually requires several years [36]. Second, incoming dispersal facilitates the arrival of adapted propagules, and therefore promotes an adaptive response even at reefs that did not experience thermal stress before[37]. Indeed, we observed that the frequency of adaptive genotypes in *A. millepora* and *P. acuta* was generally higher at reefs predicted with low PA_{HEAT} and high ICI, than in those predicted with both low PA_{HEAT} and

low ICI (Fig. S2). This view on genetic rescue via incoming migration is supported by the fact

that every reef depends, to some extent, on its neighbors for larval recruitment[38].

Limitations and future directions

The associations found between changes in coral cover and the descriptors of thermal stress,

probability of heat stress adaptation and connectivity do not necessarily imply causative

relationships. Despite evidence of effects of thermal patterns on coral cover reported by

previous studies, there might be other environmental constraints that are asymmetrical

between the two coasts of Grande Terre and modulate coral cover changes. Further

validation remains necessary and could be achieved via experimental assays of heat stress

resistance[8] in colonies sampled at reefs with different PA_{HEAT}. This approach would also

enable disentangling of the possible confounding role of acclimatization in heat stress

adaptive responses [12,33].

Another important aspect to consider in future studies is the resolution of remote sensing

datasets used for predictions. Here, we worked at a resolution of ~5 km for thermal variables

and ~8.5 km for sea current data. While the overall environmental patterns appeared

consistent with those characterized in previous studies, it is likely that small scale phenomena

were neglected. For instance, reef heat stress exposure can vary substantially under the fine-

scale (<1km) of a seascape[13]. The same applies to connectivity, since the use of high resolution

(≤1 km) hydrodynamic models could improve the characterization of coral larvae fine-scale

dispersal[39,40].

A third limitation of our approach concerns the generalization of the biological and ecological

characteristics of a reef. Here we assumed that the reef system of New Caledonia was a single

homogenous ecological niche, hosting an "average" species with an "average" heat stress

adaptive response. This simplification is useful to portray an overall prediction, but might lead

to local inaccuracies. This is because the reef types of New Caledonia are variegated and

species distributions varies accordingly[41,42]. Furthermore, different species have different

levels of bleaching sensitivity[43] and reproduce under different strategies[44]. For instance, the

propagules of a broadcast spawning coral as *A. millepora* travel over longer distances,

compared with those of brooding species as *P. damicornis* and *P. acuta*[45]. Consequently, *A.*

millepora showed a lower rate of decrease of genetic correlation between corals per unit of

seascape cost distance, in comparison with the *Pocillopora* species (Fig. 3).

In future studies, PA$_{HEAT}$ and connectivity predictions should be calibrated to match these

biological differences. It is for this reason that seascape genomics studies will become of

paramount importance into the future, as they provide species-specific indications on 1) how

thermal stress might be translated in probability adaptation, and 2) the biological meaning

(e.g. degree of genetic separation) of a cost distance by sea currents[17,18].

Conclusions

In this study, we combined remote sensing of environmental conditions with genomic data

to predict spatial patterns of heat stress adaptation and connectivity for the coral reefs of

New Caledonia. We then retrieved field survey data and showed that recent heat stress was

associated with a decrease in living coral cover, but also that such association appeared to be

mitigated at reefs predicted with 1) high probability of heat stress adaptation and 2) high

levels of incoming dispersal. The metrics computed in this work resumes the adaptive

potential of corals against heat stress, and therefore represents valuable indices to support

spatial planning of reef conservation.

Methods

Remote sensing of sea surface temperature

Satellite data characterizing sea surface temperature (SST) were retrieved from a publicly

available database (dataset: ESA SST CCI reprocessed sea surface temperature analyses)[46,47].

This dataset provides daily records of SST at a ~5 km resolution from the years 1981 to 2017

across the whole study area (Fig. 1). The shapes of the reef of the region[48] were transformed

into a regular grid (1,284 cells with maximal size of 5x5 km), and for each reef cell we extracted

the average temperature for every day of the observational period using QGIS software[49].

We performed calculations of heat stress patterns in the R environment using the *raster*

package (v. 3.0)[50,51]. For each reef cell, patterns of heat stress were computed using the

bleaching alert definition developed by the Coral Reef Watch briefly described hereafter[20].

For every day, we calculated the "hotspot value" as the difference between SST and the

maximal monthly mean (MMM, usually the monthly average of February in New Caledonia).

The hotspot value was retained only when SST exceeded the MMM by at least 1 °C. Next, for

each day, we calculated the cumulated hotspot values over the previous 84 days (3 months),

and if this sum is > 0, the day is flagged as being 'under bleaching alert'. Finally, we computed

the frequency of days under bleaching alert for every year (BAF$_{year}$) from 1985 to 2017. For

the preceding years (1981-1984), BAF$_{year}$ was not calculated such to avoid bias caused by

estimating MMM over a limited number of years. An overall measure of BAF (BAF$_{overall}$) was

calculated as the average of all the BAF$_{year}$ from 1985 to 2017.

Seascape connectivity graph

For the estimation of connectivity we applied a method based on spatial graphs previously

employed to study coral reef connectivity[17] and briefly outlined hereafter. We retrieved a

publicly available dataset describing the eastward and northward surface water velocity

(Global Ocean Physics Reanalysis)[46]. This dataset provided daily records at ~8.5 km resolution

from 1993 to 2017. Since this resolution can be inaccurate close to coastlines, we increased

the resolution to 1 km using the "resample" function ("bilinear" method) of the *raster* R

package, and used high resolution bathymetry data (100 m resolution[52]) to remove the sea

velocity value from pixels located on land. We then used the R package *gdistance* (v. 1.2)[53] to

create a matrix describing the transition costs between each adjacent pixel in the study area.

These costs were inversely proportional to the frequency of transition based on sea currents.

This seascape connectivity graph was calculated as the shortest cost distances across this

matrix between for each pair of the 1,284 reef cells. Of note, two least-cost-paths were

calculated for each pair of reef cells, one for each direction of the transition.

Connectivity indices

The seascape connectivity graph was used to compute two indices connectivity for every reef

cell of the study area: inbound connectivity and outbound connectivity. These indices had

been defined in previous work on corals[17] and were calculated in the R environment.

- Outbound connectivity index (OCI): represents the predisposition of a reef to send coral

propagules to its neighbors. For a given reef cell, it is calculated by defining all the neighboring

reef cells that can be reached under a determined cost distance threshold (CDt). OCI is the

total area (in km^2) of the destination reef cells.

- Inbound connectivity index (ICI): represents the predisposition of a reef to receive coral

recruits from its neighbors. For a given reef cell, it is calculated by defining all the neighboring

reef cells that can reach this target reef cell under a determined CDt. ICI is the total area (in

km^2) of these departure reef cells.

We set the value of CDt to 800 units in order to maximize the neighborhood without causing

border effects. This value was calculated based on the reef cells' cost distance to and from

the borders of the study area (located ~250 km around the most peripheral reef cells), where

the minimal cost distances to and from the border were 836 and 801 units, respectively.

SNPs dataset

We retrieved genomic data employed in previous seascape genomics analyses on three coral

species of New Caledonia: *Acropora millepora, Pocillopora damicornis* and *Pocillopora*

acuta[23]. This dataset encompassed more than one hundred individuals per population (167

in *A. millepora,* 118 in *P. damicornis*, 110 in *P. acuta*), collected at multiple sampling sites

around Grande Terre (20 sites for *A. millepora,* 17 for *P. damicornis*, 17 for *P. acuta*) and

genotyped using a Genotype-By-Sequencing approach[54] characterizing thousands of single-

nucleotide-polymorphisms (SNPs; 11,935 in *A. millepora*, 7,895 in *P. damicornis* and 8,343 in

P. acuta). Of note, SNPs in this dataset were already filtered for rare allelic variants (minor

allele frequency<0.05%) and linkage disequilibrium (LD-pruning threshold=0.3[55]).

Probability of heat stress adaptation

The previous seascape genomics study investigated the genotype-environment associations

between SNPs and 47 environmental descriptors (among which is BAF$_{overall}$) using LFMM

software[23,56]. In each of the three species, the analysis reported significant associations

(q<0.01) of BAF$_{overall}$ with potentially adaptive SNPs (10 in *A. millepora*, 18 in *P. damicornis,*

and 4 in *P. acuta*). We employed these genotype-environment associations to predict the

probability of heat stress adaptation (PA_{HEAT}) from $BAF_{overall}$ values. We used a method based on logistic regressions[21,57] that was previously applied to corals[17], with some modifications outlined hereafter.

For each individual used in the analysis, we retrieved the $BAF_{overall}$ value at the sampling location. Next, we encoded the presence/absence of the putatively adaptive genotype as a binary variable using a custom function in the R environment. We then employed a generalize linear mixed model (GLMM) to evaluate how the presence/absence of putative adaptive genotypes (response variable) responded to $BAF_{overall}$ (explanatory variable) across all the selected SNPs, individuals and species combined. This was done through the R package glmmTMB (v 1.0)[58], using a logistic regression model where SNP identifier, sample identifier and species were introduced as random factor. The resulting model then was used to transform $BAF_{overall}$ values associated with each of the 2,284 reef cells of New Caledonia in PA_{HEAT}. The model was plotted using the visreg R package (v. 2.6.1)[59].

Reef connectivity and genetic correlations between corals

The SNPs dataset was used to evaluate whether reef connectivity predictions were representative proxies of the structure of three coral populations. In the R environment, we applied the following framework to the genotype matrix of each of the three species. First, we evaluated the relatedness between each pair of individuals in the dataset (13,861 pairs in *A. millepora*, 6,903 pairs in *P. damicornis*, 5,995 pairs in *P. acuta*) by calculating the genetic correlation (Pearson) based on SNPs values[60,61]. We then computed the distribution of the genetic correlation values, and excluded pairs of individuals with anomalously high or low correlation (*i.e.* exceeding the boundaries defined by the median of the distribution ± three times the interquartile range).

Next, we investigated the drivers of genetic correlations by using GLMMs designed through the R package glmmTMB[58]. We set two fixed effects as possible drivers of genetic correlation between individuals: ancestral distance and reef connectivity. Accounting for ancestral genetic structure is particularly important as corals are prone to hybridization or cryptic speciation[62,63]. The computation of ancestral distance featured the R package ALStructure (v. 0.1)[64]. For a given SNP matrix, ALStructure predicts the number of ancestral populations, and then estimates, for every individual, the admixture proportions to the ancestral populations.

For every pair of individuals, we then calculated the ancestral distance as the Euclidean

distance between the respective admixture proportions. For which concerns reef

connectivity, the fixed effect corresponded to the least-cost-path (from the seascape graph)

linking the sampling sites of every pair of individuals. Since genetic correlations could not

exceed the 0-1 boundaries, GLMMs were built using a beta regression[65]. The random factors

in the GLMM were the identifiers of the individuals in the pairs, as well as the identifier of the

pair of sampling sites.

Finally, we evaluated the relationship between ancestral distance, reef connectivity and

genetic correlations of corals by 1) reporting the estimate and its standard deviation, as well

as the p-value associated with Wald statistic[58]; 2) plotting the association using the visreg R

package[59].

Coral cover data

Living coral cover data was retrieved from the 2017-18 report of the New Caledonian

observational network of coral reefs ('Réseau d'observation des récifs coralliens de Nouvelle

Calédonie', RORC)[24]. Overall, we used data from 74 survey stations distributed across the

Archipelago of New Caledonia (Fig. 1). At each station, yearly coral cover surveys were

performed along the same 100m transect using the "point intercept" technique. Surveys

covered the period from 2003 to 2017, where 18 sites have been visited for less than five

years, 27 for five to ten years, and 29 for more than ten years. The exact coordinates of survey

stations were retrieved from the geographic information web-portal of New Caledonia

(https://georep.nc/).

Environmental characterization of survey sites

The coordinates of survey stations were used to find the corresponding reef cells and the

associated values of the connectivity indices (OCI and ICI). For each survey record (i.e. survey

at a given station in a specific year) we also calculated $BAF_{overall}$ as the average BAF since 1985

to the year proceeding the survey. Based on the values of $BAF_{overall}$ we computed PA_{HEAT} for

each survey record. In addition, we calculated BAF values on a rolling temporal window

describing average BAF for the year ($BAF_{previous\ year}$) that preceded the year of survey.

Analysis of coral cover change

We investigated the association of $BAF_{previous\ year}$, PA_{HEAT} and connectivity indices (ICI and OCI;

in total 4 explanatory variables) with coral cover rates (response variable) using GLMMs. This

analysis focused on the coral cover rates of every survey record (total of 574 records). The

computation of GLMMs was performed using the R package glmmTMB (v 1.0)[58], which

allowed us to model coral cover rates via beta regression [65]. We accounted for the non-

independence of survey records originated at the same station but on different years by

setting the station effect as random factor on the coral cover rate[66]. This approach is

recommended for studies of longitudinal data with irregular time points[67]. To avoid bias due

to scale differences between explanatory variables, each variable was standardized to mean

0 and standard deviation 1 using the R "scale" function.

We built two types of GLMMs: univariate and bivariate. In univariate GLMMs, $BAF_{previous\ year}$,

PA_{HEAT}, ICI and OCI were employed each as unique fixed effect. The goal was to determine

whether the explanatory variables showed a standalone association (*i.e.* independent from

other variables) with coral cover change. In bivariate models, GLMMs were constructed each

with two fixed effects: 1) $BAF_{previous\ year}$ and 2) the interaction between $BAF_{previous\ year}$ and each

of the remaining explanatory variables: PA_{HEAT}, ICI and OCI. The goal of bivariate models was

to investigate whether the potential effect of recent thermal stress ($BAF_{previous\ year}$) on coral

cover might be modulated by PA_{HEAT}, ICI or OCI.

For each GLMM, we reported the estimate and its standard deviation, as well as the p-value

(deemed significant when <0.05) associated with Wald statistic[58] of the fixed effects. In

addition, we compared the quality-of-fit of models by calculating the Akaike Information

Criterion (AIC)[68].

Acknowledgments

We thank the *Réseau d'observation des récifs coralliens* of New Caledonia for collecting and
sharing the field survey data. We thank Annie Guillaume for the comments and suggestions
provided during the redaction of this paper. This work was supported by the United Nations
Environment Programme (UNEP) and International Coral Reef Initiative (ICRI) coral reefs small
grants programme (grant number: SSFA/18/MCE/005). We also thank the Government of
France and the Government of the Principality of Monaco who provided the funding for the
small grants.

504
505
506
507 **References**
508
1. Hughes, T. P. *et al.* Global warming and recurrent mass bleaching of corals. *Nature*
543, 373–377 (2017).
2. Bellwood, D. R., Hughes, T. P., Folke, C. & Nyström, M. Confronting the coral reef
crisis. *Nature* **429**, 827–833 (2004).
3. Hughes, T. P. *et al.* Spatial and temporal patterns of mass bleaching of corals in the
Anthropocene. *Science (80-.).* **359**, 80–83 (2018).
4. Van Hooidonk, R., Maynard, J. A. & Planes, S. Temporary refugia for coral reefs in a
warming world. *Nat. Clim. Chang.* **3**, 508–511 (2013).
5. Costanza, R. *et al.* Changes in the global value of ecosystem services. *Glob. Environ.*
Chang. **26**, 152–158 (2014).
6. Moberg, F. & Folke, C. Ecological goods and services of coral reef ecosystems. *Ecol.*
Econ. **29**, 215–233 (1999).
7. Hughes, T. P. *et al.* Ecological memory modifies the cumulative impact of recurrent
climate extremes. *Nature Climate Change* **9**, 40–43 (2019).
8. Krueger, T. *et al.* Common reef-building coral in the northern red sea resistant to
elevated temperature and acidification. *R. Soc. Open Sci.* **4**, 170038 (2017).
9. Penin, L., Vidal-Dupiol, J. & Adjeroud, M. Response of coral assemblages to thermal
stress: are bleaching intensity and spatial patterns consistent between events?
Environ. Monit. Assess. **185**, 5031–5042 (2013).
10. Thompson, D. M. & van Woesik, R. Corals escape bleaching in regions that recently
and historically experienced frequent thermal stress. *Proc. Biol. Sci.* **276**, 2893–2901
(2009).
11. Sully, S., Burkepile, D. E., Donovan, M. K., Hodgson, G. & van Woesik, R. A global
analysis of coral bleaching over the past two decades. *Nat. Commun.* **10**, 1–5 (2019).
12. Thomas, L. *et al.* Mechanisms of Thermal Tolerance in Reef-Building Corals across a
Fine-Grained Environmental Mosaic: Lessons from Ofu, American Samoa. *Front. Mar.*
Sci. **4**, 434 (2018).
13. Bay, R. A. & Palumbi, S. R. Multilocus adaptation associated with heat resistance in
reef-building corals. *Curr. Biol.* **24**, 2952–2956 (2014).
14. Wilson, K. L., Tittensor, D. P., Worm, B. & Lotze, H. K. Incorporating climate change
adaptation into marine protected area planning. *Glob. Chang. Biol.* **26**, 3251–3267
(2020).
15. Baums, I. B. *et al.* Considerations for maximizing the adaptive potential of restored
coral populations in the western Atlantic. *Ecol. Appl.* **29**, (2019).
16. Matz, M. V., Treml, E. & Haller, B. C. Predicting coral adaptation to global warming in
the Indo-West-Pacific. *bioRxiv* 722314 (2019). doi:10.1101/722314
17. Selmoni, O., Rochat, E., Lecellier, G., Berteaux-Lecellier, V. & Joost, S. Seascape
genomics as a new tool to empower coral reef conservation strategies: an example
on north-western Pacific Acropora digitifera. *Evol. Appl.* 588228 (2020).
doi:10.1101/588228
18. Riginos, C., Crandall, E. D., Liggins, L., Bongaerts, P. & Treml, E. A. Navigating the
currents of seascape genomics: how spatial analyses can augment population

genomic studies. *Curr. Zool.* **62**, doi: 10.1093/cz/zow067 (2016).

19.   Maina, J., Venus, V., McClanahan, T. R. & Ateweberhan, M. Modelling susceptibility of
coral reefs to environmental stress using remote sensing data and GIS models. *Ecol.*
Modell. **212**, 180–199 (2008).

20.   Liu, G., Strong, A. E. & Skirving, W. Remote sensing of sea surface temperatures
during 2002 Barrier Reef coral bleaching. *Eos, Trans. Am. Geophys. Union* **84**, 137–141
(2003).

21.   Rochat, E. & Joost, S. Spatial Areas of Genotype Probability (SPAG): predicting the
spatial distribution of adaptive genetic variants under future climatic conditions.
bioRxiv 2019.12.20.884114 (2019). doi:10.1101/2019.12.20.884114

22.   Boulanger, E., Dalongeville, A., Andrello, M., Mouillot, D. & Manel, S. Spatial graphs
highlight how multi-generational dispersal shapes landscape genetic patterns.
Ecography (Cop.). ecog.05024 (2020). doi:10.1111/ecog.05024

23.   Selmoni, O. *et al.* Seascape genomics reveals candidate molecular targets of heat
stress adaptation in three coral species. *bioRxiv* 2020.05.12.090050 (2020).
doi:10.1101/2020.05.12.090050

24.   Job, S. *Réseau d'observation des récifs coralliens (RORC) de Nouvelle-Calédonie.*
Campagne 2017-2018. Rapport Pays. Rapport CORTEX. Pour le compte de :
Conservatoire d'espaces naturels de Nouvelle-Calédonie - Province des îles Loyauté -
Observatoire de l'environne. (2018).

25.   Lefèvre, J., Marchesiello, P., Jourdain, N. C., Menkes, C. & Leroy, A. Weather regimes
and orographic circulation around New Caledonia. *Mar. Pollut. Bull.* **61**, 413–431
(2010).

26.   Marchesiello, P., Lefèvre, J., Vega, A., Couvelard, X. & Menkes, C. Coastal upwelling,
circulation and heat balance around New Caledonia's barrier reef. *Mar. Pollut. Bull.*
61, 432–448 (2010).

27.   Berkelmans, R., Weeks, S. J. & Steinberga, C. R. Upwelling linked to warm summers
and bleaching on the Great Barrier Reef. *Limnol. Oceanogr.* **55**, 2634–2644 (2010).

28.   Cravatte, S. *et al.* Regional circulation around New Caledonia from two decades of
observations. *J. Mar. Syst.* **148**, 249–271 (2015).

29.   Hénin, C., Guillerm, J. & Chabert, L. Circulation superficielle autour de la Nouvelle-
Cal{é}donie. *Oc{é}anographie Trop.* **19**, 113–126 (1984).

30.   Magris, R. A., Pressey, R. L., Weeks, R. & Ban, N. C. Integrating connectivity and
climate change into marine conservation planning. *Biological Conservation* **170**, 207–
221 (2014).

31.   Hughes, T. P. *et al.* Global warming transforms coral reef assemblages. *Nature* **556**,
492–496 (2018).

32.   Welle, P. D., Small, M. J., Doney, S. C. & Azevedo, I. L. Estimating the effect of multiple
environmental stressors on coral bleaching and mortality. *PLoS One* **12**, e0175018
(2017).

33.   Kenkel, C. D., Almanza, A. T. & Matz, M. V. Fine-scale environmental specialization of
reef-building corals might be limiting reef recovery in the Florida Keys. *Ecology* **96**,
3197–3212 (2015).

34.   Palumbi, S. R. Population genetics, demographic connectivity, and the design of
marine reserves. *Ecol. Appl.* **13**, 146–158 (2003).

35.   Hock, K. *et al.* Connectivity and systemic resilience of the Great Barrier Reef. *PLoS*
Biol. **15**, (2017).

36. Robinson, J. P. W., Wilson, S. K. & Graham, N. A. J. Abiotic and biotic controls on coral
recovery 16 years after mass bleaching. *Coral Reefs* **38**, 1255–1265 (2019).
37. Kawecki, T. J. Adaptation to Marginal Habitats. *Annu. Rev. Ecol. Evol. Syst.* **39**, 321–
342 (2008).
38. Treml, E. A. *et al.* Reproductive output and duration of the pelagic larval stage
determine seascape-wide connectivity of marine populations. in *Integrative and*
Comparative Biology **52**, 525–537 (2012).
39. Storlazzi, C. D., van Ormondt, M., Chen, Y.-L. & Elias, E. P. L. Modeling Fine-Scale Coral
Larval Dispersal and Interisland Connectivity to Help Designate Mutually-Supporting
Coral Reef Marine Protected Areas: Insights from Maui Nui, Hawaii. *Front. Mar. Sci.* **4**,
381 (2017).
40. Colberg, F., Brassington, G. B., Sandery, P., Sakov, P. & Aijaz, S. High and medium
resolution ocean models for the Great Barrier Reef. *Ocean Model.* **145**, 101507
(2020).
41. Andréfouët, S., Cabioch, G., Flamand, B. & Pelletier, B. A reappraisal of the diversity of
geomorphological and genetic processes of New Caledonian coral reefs: A synthesis
from optical remote sensing, coring and acoustic multibeam observations. *Coral Reefs*
28, 691–707 (2009).
42. Dalleau, M. *et al.* Use of habitats as surrogates of biodiversity for efficient coral reef
conservation planning in Pacific Ocean islands. *Conserv. Biol.* **24**, 541–552 (2010).
43. Loya, Y. *et al.* Coral bleaching: the winners and the losers. *Ecol. Lett.* **4**, 122–131
(2001).
44. Darling, E. S., Alvarez-Filip, L., Oliver, T. A., McClanahan, T. R. & Côté, I. M. Evaluating
life-history strategies of reef corals from species traits. *Ecol. Lett.* **15**, 1378–1386
(2012).
45. Ayre, D. J. & Hughes, T. P. Genotypic diversity and gene flow in brooding and
spawning corals along the great barrier reef, Australia. *Evolution (N. Y).* **54**, 1590–
1605 (2000).
46. EU Copernicus Marine Service. Global Ocean - In-Situ-Near-Real-Time Observations.
(2017). Available at: http://marine.copernicus.eu. (Accessed: 2nd February 2017)
47. Merchant, C. J. *et al.* Satellite-based time-series of sea-surface temperature since
1981 for climate applications. *Sci. data* **6**, 223 (2019).
48. UNEP-WCMC, WorldFish-Center, WRI & TNC. Global distribution of warm-water coral
reefs, compiled from multiple sources including the Millennium Coral Reef Mapping
Project. Version 1.3. (2010). Available at: http://data.unep-wcmc.org/datasets/1.
(Accessed: 9th May 2017)
49. QGIS development team. QGIS Geographic Information System. Open Source
Geospatial Foundation Project. (2009).
50. Hijmans, R. J. raster: Geographic Data Analysis and Modeling. (2016).
51. R Core Team. R: A Language and Environment for Statistical Computing. (2016).
52. Ryan, W. B. F. *et al.* Global multi-resolution topography synthesis. *Geochemistry,*
Geophys. Geosystems **10**, (2009).
53. van Etten, J. gdistance: Distances and Routes on Geographical Grids. (2018). Available
at: https://cran.r-project.org/package=gdistance.
54. Kilian, A. *et al.* Diversity arrays technology: A generic genome profiling technology on
open platforms. *Methods Mol. Biol.* **888**, 67–89 (2012).
55. Zheng, X. *et al.* A high-performance computing toolset for relatedness and principal

645   component analysis of SNP data. *Bioinformatics* **28**, 3326–3328 (2012).

646 56. Frichot, E., Schoville, S. D., Bouchard, G. & François, O. Testing for associations
647   between loci and environmental gradients using latent factor mixed models. *Mol.*
648   *Biol. Evol.* **30**, 1687–1699 (2013).

649 57. Joost, S. *et al.* A spatial analysis method (SAM) to detect candidate loci for selection:
650   Towards a landscape genomics approach to adaptation. *Mol. Ecol.* **16**, 3955–3969
651   (2007).

652 58. Brooks, M. E. *et al.* glmmTMB balances speed and flexibility among packages for zero-
653   inflated generalized linear mixed modeling. *R J.* **9**, 378–400 (2017).

654 59. Breheny, P. & Burchett, W. Visualization of regression models using visreg. *R J.* **9**, 56–
655   71 (2017).

656 60. Novembre, J. *et al.* Genes mirror geography within Europe. *Nature* **456**, 98–101
657   (2008).

658 61. Patterson, N., Price, A. L. & Reich, D. Population structure and eigenanalysis. *PLoS*
659   *Genet.* **2**, 2074–2093 (2006).

660 62. van Oppen, M. J. H., Willis, B. L., Van Rheede, T. & Miller, D. J. Spawning times,
661   reproductive compatibilities and genetic structuring in the Acropora aspera group:
662   Evidence for natural hybridization and semi-permeable species boundaries in corals.
663   *Mol. Ecol.* **11**, 1363–1376 (2002).

664 63. Schmidt-Roach, S. *et al.* Assessing hidden species diversity in the coral Pocillopora
665   damicornis from Eastern Australia. *Coral Reefs* **32**, 161–172 (2013).

666 64. Cabreros, I. & Storey, J. D. A likelihood-free estimator of population structure bridging
667   admixture models and principal components analysis. *Genetics* **212**, 1009–1029
668   (2019).

669 65. Ferrari, S. L. P. & Cribari-Neto, F. Beta regression for modelling rates and proportions.
670   *J. Appl. Stat.* **31**, 799–815 (2004).

671 66. Verbeke, G., Molenberghs, G. & Rizopoulos, D. Random effects models for
672   longitudinal data. in *Longitudinal Research with Latent Variables* 37–96 (Springer
673   Berlin Heidelberg, 2010). doi:10.1007/978-3-642-11760-2_2

674 67. Garcia, T. P. & Marder, K. Statistical Approaches to Longitudinal Data Analysis in
675   Neurodegenerative Diseases: Huntington's Disease as a Model. *Current Neurology*
676   *and Neuroscience Reports* **17**, 14 (2017).

677 68. Bozdogan, H. Model selection and Akaike's Information Criterion (AIC): The general
678   theory and its analytical extensions. *Psychometrika* **52**, 345–370 (1987).