

1 The balancing act of *Nipponites mirabilis* (Nostoceratidae, Ammonoidea):
2 managing hydrostatics during a complex ontogenetic trajectory

3

4 Short title: Hydrostatics of *Nipponites mirabilis*

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24 **Abstract**

25 *Nipponites* is a heteromorph ammonoid with a complex and unique morphology that
26 obscures its mode of life and ethology. The seemingly aberrant shell of this Late Cretaceous
27 nostoceratid seems deleterious. However, hydrostatic simulations suggest that this morphology
28 confers several advantages for exploiting a quasi-planktic mode of life. Virtual, 3D models of
29 *Nipponites mirabilis* were used to compute various hydrostatic properties through 14 ontogenetic
30 stages. At each stage, *Nipponites* had the capacity for neutral buoyancy and was not restricted to
31 the seafloor. Throughout ontogeny, horizontally facing to upwardly facing soft body orientations
32 were preferred. These orientations were aided by the obliquity of the shell's ribs, which were
33 parallel to former positions of the aperture during life. Static orientations were somewhat fixed,
34 inferred by stability values that are slightly higher than extant *Nautilus*. The initial open-whorled,
35 planispiral phase is well suited to horizontal backwards movement with little rocking. *Nipponites*
36 then deviates from this coiling pattern with a series of alternating U-shaped bends in the shell.
37 This modification allows for proficient rotation about the vertical axis, while possibly
38 maintaining the option for horizontal backwards movement by redirecting its hyponome. These
39 particular hydrostatic properties likely result in a tradeoff between hydrodynamic streamlining,
40 suggesting that *Nipponites* assumed a low energy lifestyle of slowly pirouetting in search for
41 planktic prey. Each computed hydrostatic property influences the others in some way, suggesting
42 that *Nipponites* maintained a delicate hydrostatic balancing act throughout its ontogeny in order
43 to facilitate this mode of life.

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47 Introduction

48 Heteromorph ammonoids are ectocochleate cephalopods whose shells undergo changes
49 in coiling throughout ontogeny. The seemingly aberrant shape of some heteromorph ammonoids
50 piques curiosity about their enigmatic modes of life and life habit. Arguably, the most bizarre
51 and conspicuous of all heteromorph genera is the Late Cretaceous (Turonian – Coniacian)
52 nostoceratid, *Nipponites* (Fig 1). Previous research has largely focused on the biostratigraphic
53 usefulness of *Nipponites* [1–5] rather than its paleobiology [6–7] and evolutionary significance
54 [8]. The latter two areas are valuable because the morphology of this heteromorph appears
55 deleterious to survival; seemingly defying the basic principles of natural selection [9–15]. It is
56 more likely, however, that its functional morphology is obscured by a complex ontogenetic
57 trajectory in shell growth. The shell of *Nipponites* is characterized by having several open
58 planispiral (crioconic) whorls in early ontogeny, followed by a series of alternating U-bends
59 around the earlier whorls (Fig 1); denoting some degree of regularity in coiling throughout a
60 seemingly-aberrant ontogeny [1,16,17]. Okamoto [18–20] demonstrated that the coiling of
61 *Nipponites mirabilis* is, in fact, well constrained and can be approximated by a few piecewise
62 equations (alternations of sinistral and dextral helicoid phases surrounding the crioconic phase).
63 Similarly, differential geometry has proven a useful tool in modeling these complex
64 heteromorphs [21–22].

65

66 **Fig 1. Hydrostatic Parameters of *Nipponites mirabilis*.** A, Side view of *Nipponites* in life
67 position showing hypothetical centers of buoyancy (B), mass (M), and the horizontal axis of
68 rotation (R). The angle of the aperture (θ_a) is measured as the inclination from the vertical plane.
69 The thrust angle (θ_t) can be used to assess the directional efficiency of movement. This angle is

70 measured between the horizontal plane, and a line passing through R and the location of the
71 hyponome (source of thrust; H). **B**, Front view of *Nipponites* in life position facing the aperture.
72 This view shows the total lever arm (L) and its x-component (L_x) which is proportionate to the
73 amount of rotational movement about the vertical axis produced during jet propulsion. **C**, Top
74 view of *Nipponites* in life position showing the rotational thrust angle (θ_{tr}). This angle is
75 measured between the vertical rotation axis (vert.), which passes through B and M, and the
76 direction of the thrust vector (arrow emanating from H). Rotational thrust angles of 90° result in
77 idealized transmission of thrust into pure rotation.

78

79 The complex, meandering shell of *Nipponites* has invited several different interpretations
80 regarding potential modes of life assumed by this heteromorph. The shell morphology of
81 *Nipponites* has been compared to vermetid gastropods, and by analogy, this heteromorph has
82 been suggested to assume a sessile and benthic mode of life [23–28]. Trueman [29] also
83 considered *Nipponites* as a benthon, but with some degree of mobility. Other nostoceratid genera
84 have been interpreted as negatively buoyant, benthic elements as well [28,30,31]. By similar
85 analogy with other ‘irregularly-coiled’ mollusks, a symbiotic relationship with sponges or
86 hydrozoans occupying the free space between the whorls of *Nipponites* has been speculated [32];
87 although, no fossil evidence currently supports such a relationship. Contrasting benthic
88 interpretations, Ward & Westermann [33] suggest that *Nipponites occidentalis* was capable of a
89 planktic mode of life based on approximate calculations of organismal density. This mode of life
90 is supported by Okamoto [19] for *Nipponites mirabilis* due to the oscillation of rib obliquity of
91 the shell. Changes in rib obliquity suggests that some proper orientation of the soft body was
92 preferred, which would not matter during a negatively buoyant condition. Favoring a planktic

93 mode of life, Westermann [6] inferred *Nipponites* was an occupant of the epipelagic, oceanic
94 waters, perhaps as a vertical migrant or planktic drifter. This morphology is certainly not
95 streamlined, suggesting that it would have experienced considerably more hydrodynamic drag
96 than its planispiral counterparts. The unique shell of this genus raises questions regarding how its
97 changes in coiling may reflect the modification of syn vivo hydrostatic properties; a tactic
98 observed in other morphotypes of heteromorph ammonoids [17,19,20,34-39].

99 **Hydrostatic properties of heteromorph ammonoids**

100 The ability of ectocochleate cephalopods to attain neutral buoyancy is fundamental to
101 reconstruct their modes of life. The variable interpretations for nostoceratid modes of life
102 illustrate the importance of new techniques to determine the physical properties that would have
103 acted on these living cephalopods. A neutrally buoyant condition is achieved when the total
104 organismal mass is equal to the mass of the water displaced by the living animal. This depends
105 upon the body chamber to phragmocone ratio. If the phragmocone (the chambered portion of the
106 shell) is too small, the living cephalopod would not be able to compensate for its organismal
107 weight and it would become negatively buoyant [34,36,40]. This condition also depends upon
108 shell thickness and the densities assigned to each component of the living animal, which have
109 been somewhat variable in previous research [39,41].

110 Previous studies have demonstrated that heteromorph ammonoids may have been able to
111 achieve much different life orientations than their planispiral counterparts [20,29,34–39,42–45].
112 These living cephalopods would have assumed some static orientation when their centers of
113 buoyancy and mass were vertically aligned [41,46,47] (Fig 1). The difficulty to which these
114 living cephalopods could deviate from their static orientation depends on hydrostatic stability,
115 which is proportionate to the separation between the centers of buoyancy and mass [20]. High

116 stability would have reduced the influence of external forms of energy on orientation, but would
117 have simultaneously made it more difficult for the living cephalopod to self-modify its
118 orientation [36].

119 The directional efficiency of movement (thrust angle) depends upon the relative position
120 of the source of thrust (the hyponome) and the center of rotation (the midpoint between the
121 centers of buoyancy and mass; Fig 1A, B). Thrust energy produced by jet propulsion is more
122 efficiently transmitted into movement in the direction where the hyponome and center of rotation
123 are aligned [20,38,39,48,49]. If these two points were horizontally aligned (thrust angle of zero),
124 more energy would be transmitted to horizontal movement with minimal rocking. The rocking
125 behavior of extant nautilids is related to their sub-horizontal thrust angles and the retraction of
126 the soft body during emptying of the mantle cavity [50].

127 A rotational component of energy is increased by turning the direction of thrust out of
128 alignment with the centers of buoyancy and mass (the axis where idealized rotation would occur;
129 Fig 1B, C). An increased distance of the hyponome from these two centers would therefore
130 produce a lever arm that would impart a torque to rotate the living cephalopod about its vertical
131 axis. This type of movement is likely to have taken place for turrilitid heteromorphs [34], as well
132 as other morphotypes with their apertures positioned in a similar relative manner [37]. Idealized
133 rotation about the vertical axis would occur with a long, horizontally oriented lever arm and a
134 thrust vector adjoining its distal end with a right angle.

135 Each of these physical properties would have significantly constrained the hydrostatic
136 and hydrodynamic capabilities of living *Nipponites* throughout its ontogeny. Therefore, they
137 provide fundamental information regarding the possible modes of life and life habit for this
138 unique ammonoid, as well as possible adaptations for locomotion and feeding.

139

140 **Methods**

141 Virtual models were constructed to determine the *syn vivo* hydrostatic properties of
142 *Nipponites mirabilis*. Construction of the shell and other model components largely follow the
143 methods of Peterman et al. [37–39], although a CT scanned specimen was used as the base
144 model instead of using photogrammetry (similar to the methods of Morón-Alfonso [51]). This
145 modification from the previous methods was preferred for this species due to the complex
146 changes in shell ornamentation (rib obliquity). These ribs are parallel to the successive positions
147 of the aperture throughout ontogeny, therefore retaining vital information about life orientation
148 [20]. This method for virtual reconstruction is favorable for *Nipponites* because specimens of this
149 genus are rarely found complete; discouraging destructive sampling techniques like serial
150 grinding tomography. Computed tomography (CT) scans of such specimens also lack contrasts
151 of X-ray attenuation factors to distinguish the shell from its surrounding materials [52].
152 However, each of these tomographic techniques can provide very accurate measurements of
153 hydrostatic properties and volumes when the specimens are adequate for imaging [52–59].

154 **Virtual modeling of the shell**

155 The shell of *Nipponites mirabilis* was constructed from an initial CT scan [60] of the
156 specimen INM-4-346 (Museum Park Ibaraki Prefectural Museum of Nature), which had a
157 remarkable degree of preservation. Most of the ontogeny is preserved for this specimen with
158 minimal matrix on the inside (Fig 2A). However, two portions had to be virtually reconstructed;
159 1) the crushed ~5 cm section of the adoral-most body chamber, and 2) the earliest crioconic
160 whorls that are partially embedded in a remnant of the original concretion. These two portions of
161 the shell were reconstructed (Fig 2B) with array algorithms [37–40], which replicate a whorl

162 section and simultaneously translate, rotate, and scale it to build the shell from the adoral
163 direction to adapical direction (Table 1). Such arrays are similar to the morphospace parameters
164 of Raup [61]. The CT scanned model [60] (which consists of a stack of .tiff images) was
165 converted to the tessellated .stl format required for model reconstruction and volumetry using the
166 program, Molcer 1.51 [62]. The external mesh of the tessellated file was isolated in order to get
167 rid of internal features like fissures and X-ray attenuation artifacts. External defects were
168 smoothed in Meshmixer 3.3 [63] while maintaining the curvature of neighboring, complete
169 features. This external 3D mesh served as a stencil for the reconstruction of the missing and
170 damaged portions of the shell. After the missing portions of the shell were combined to the
171 model derived from the CT scan, the ornamentation was reconstructed by matching the width
172 and amplitude of ribs with a torus shape in Blender [64], then properly oriented using the ribs
173 present on the inner whorls. The ornamentation, reconstructed portions of the shell (Fig 2B), and
174 the total external mesh were repaired and unified in Netfabb [65] to produce a single manifold
175 mesh of the exterior shell. The program, Blender, was used to assign shell thickness to the
176 external shell model based on measurements from specimen NMNS (National Museum of
177 Nature and Science) MP35490 (Fig 3), producing a mesh denoting the entire shell without septa.
178

179 **Fig 2. Virtual Reconstruction of the Shell of *Nipponites mirabilis*.** **A**, Tessellated (.stl) 3D
180 model generated from a CT scan [60] of specimen INM-4-346. **B**, Reconstructed adoral portion
181 of the body chamber and inner criocone phase with arrays algorithms (Table 1). **C**, Extruded
182 septa generated from the suture pattern. **D**, Extruded shell and septa models unified together to
183 produce a single, manifold 3D mesh of the entire shell.

184 **Fig 3. Thickness Measurements used for Virtual Model Extrusion.** Thicknesses of the shell
 185 (black) and septa (grey) as a function of whorl height. Measurements were recorded from
 186 specimen NMNS PM35490 and used to define thickness in the virtual model.

187

188 **Table 1. Reconstruction of the Shell**

Terminal Body Chamber		Translation (mm)			Rotation (degrees)			Scale		
Array #	# Replications	X	Y	Z	X	Y	Z	X	Y	Z
1*	67	-0.035	0.018	-0.265	-0.70	0.59	0.40	1.000	1.000	1.000
2*	29	-6.722	-6.548	-14.237	-0.70	1.00	-0.60	1.000	1.001	1.002
3*	40	-11.103	-12.910	-16.980	0.20	0.19	-1.70	1.002	0.999	1.001
Criocone Phase		Translation (mm)			Rotation (degrees)			Scale		
Array #	# Replications	X	Y	Z	X	Y	Z	X	Y	Z
1*	55	-30.050	-11.085	2.920	0.53	1.10	0.70	0.996	0.997	0.996
2	100	-30.057	-11.171	2.960	0.37	1.30	0.88	0.996	0.996	0.996
3*	122	-14.760	-14.063	5.757	0.39	0.88	0.69	0.998	0.998	0.998
4*	83	-25.009	-11.595	5.269	-0.15	1.80	0.70	0.997	0.997	0.997
5*	59	-20.306	-15.710	10.206	0.38	1.00	0.50	0.998	0.998	0.998
6	154	-20.286	-15.722	10.188	0.45	1.50	1.00	0.996	0.996	0.996

189 Array instructions used to reconstruct the juvenile criocone phase and the adoral portion of the
 190 terminal body chamber. These arrays were used in a piecewise manner to replicate the whorl
 191 section from the adoral direction to adapical direction by translation, rotation, and scaling in the
 192 x, y, and z directions. Asterisks denote arrays that had their origins reset to their current locations
 193 before replication. If origins were not reset, the origins of their previous arrays were used.

194

195 Septa were constructed by recording a suture pattern from specimen NMNS PM35490
 196 (Fig 4). The external shell of this specimen (Fig 4B, C) was removed with air abrasives and
 197 pneumatic tools under a stereoscopic microscope and the suture (Fig 4D) was recorded with a
 198 digital camera lucida. This suture was imported in the Blender workspace and the curve modifier

199 was used to wrap it around the whorl section of the shell. This suture was then replicated and
200 placed along the majority of the phragmocone so that adjacent lobules and folioles were almost
201 tangential. Ontogenetic changes in the suture pattern were not considered because they probably
202 represent only small differences in mass and its distribution. That is, each suture had the same
203 degree of complexity and its expanded portion was placed adjacent to the venter throughout
204 ontogeny. The crioconic, juvenile phase was reconstructed with array algorithms, which allowed
205 septa to be duplicated with the same equations. The septa within the majority of the
206 phragmocone were constructed by extruding the suture patterns inwards to a single point, then
207 refining and smoothing the interior in order to approximate minimum curvature surfaces. A body
208 chamber ratio of approximately 42% the total curvilinear length was measured from a
209 remarkably complete specimen of *Nipponites mirabilis* from a private collection. This specimen
210 was 3D scanned with an Artec Space Spider (to allow comparisons with the CT scanned
211 specimen) and is housed in the morphosource database [66]. A nearly complete specimen of
212 *Nipponites mirabilis* (MCM-A0435; Mikasa City Museum; Fig 4E) was also compared in this
213 manner and stored in the database [66], which yielded an approximate body chamber ratio of
214 36%. This ratio would be slightly higher if the aperture was not partially crushed. The proper
215 number of septa to maintain the body chamber ratio of around 42% were placed in the
216 phragmocone and extruded based on measured thicknesses from specimen NMNS PM35490
217 (Fig 3). These final septa (Fig 2C) were merged with the extruded, external shell to produce a
218 single, manifold 3D mesh of the entire, septate shell (Fig 2D).

219

220 **Fig 4. Specimens Used for Shell Reconstruction.** A, Original concretion containing NMNS
221 PM35490. Umbilical view (B) and ventral view (C) of the shell section used to record the suture

222 pattern (**D**). **E**, 3D scan of the Mikasa City Museum Specimen (MCM-A0435) used to
223 approximate the body chamber ratio. Scale bar = 2 cm.

224

225 **Virtual modeling of the soft body and camerae**

226 The shell constrains the size and shape of other model components that influence
227 hydrostatics. A model of the soft body was constructed by isolating the internal interface of the
228 body chamber, and similarly, the camerae were isolated from the phragmocone of the shell. The
229 faces of both meshes were inverted so that the normals (vectors denoting the outside) were
230 pointing in their proper directions. The ammonoid soft body is largely unknown; however, due to
231 phylogenetic bracketing [67], the presence of ten arms can be inferred [68–70] with a possibly
232 reduced soft body. A soft body resembling the consensuses of Klug & Lehmann [70] and
233 Landman et al. [71] was constructed for *Nipponites* and unified to the repaired, isolated internal
234 body chamber mesh. The camerae were later partitioned into fractions of cameral liquid and
235 cameral gas for hydrostatic calculations. Both cameral liquid and cameral gas were assumed be
236 evenly distributed in the phragmocone; a reasonable assumption based on the retention of
237 cameral liquid via the pellicle and surface tension along septal margins [72]. This yielded mass
238 distributions of the fractions of cameral liquid and cameral gas that have the same centers as the
239 center of volume for all camerae.

240 **Modeling changes in shell morphology throughout ontogeny**

241 The final hydrostatic model of the adult *Nipponites mirabilis* was used to derive a total of
242 14 models representing different life stages. This was accomplished by deleting the septa in the
243 phragmocone and deleting the adoral portion of the body chamber so that the proper body
244 chamber ratio was maintained throughout ontogeny. The total curvilinear distance along the

245 venter from the apex to the aperture was normalized by this same distance for the terminal stage,
246 yielding a proxy for the age of each model (in terms of a relative percentage through the
247 individual's lifespan).

248 **Hydrostatic calculations**

249 Neutral buoyancy occurs when the sum of organismal mass is equal to the mass of water
250 displaced. The proportion of camerae to be emptied of cameral liquid relative to the total
251 available cameral volume (Φ) that satisfies a neutrally buoyant condition was computed with the
252 following equation (after Peterman et al., 2019a):

$$253 \quad \Phi = \frac{\left(\frac{V_{wd}\rho_{wd} - V_{sb}\rho_{sb} - V_{sh}\rho_{sh}}{V_{ct}} \right) - (\rho_{cl})}{(\rho_{cg} - \rho_{cl})} \quad (1)$$

254 Where V_{wd} and ρ_{wd} are the volume and density of the water displaced, V_{sb} and ρ_{sb} are the volume
255 and density of the soft body, V_{sh} and ρ_{sh} are the volume and density of the shell, ρ_{cl} is the density
256 of cameral liquid, ρ_{cg} is the density of cameral gas, and V_{ct} is the total cameral volume of the
257 phragmocone. A soft body density of 1.049 g/cm³ is preferred based on the measurement of
258 *Nautilus* soft body by Hoffmann & Zachow [73] that was later averaged by a seawater-filled
259 mantle cavity and thin mouthparts by Peterman et al. [38]. A shell density of 2.54 g/cm³ was
260 adopted from Hoffman & Zachow [73]. The cameral liquid density of 1.025 g/cm³ [74] and
261 cameral gas density of 0.001 g/cm³ are used in the current study.

262 The total center of mass is weighted according to each material of unique density (i.e., the
263 soft body, shell, cameral liquid, and cameral gas in the current study). Each individual center of
264 mass for the soft body, shell, cameral liquid, and cameral gas were computed in MeshLab [75]
265 and the total center of mass was computed with the equation:

$$266 \quad M = \frac{\sum(L * m_o)}{\sum m_o} \quad (2)$$

267 Where M is the total center of mass in a principal direction, L is the center of mass of a single
268 object measured with respect to an arbitrary datum in each principal direction, and m_o is the
269 mass of any particular object that has a unique density. Equation 2 was used in the x, y, and z
270 directions to compute the coordinate position of the center of mass.

271 The center of buoyancy (B) is equal to the center of volume of the medium displaced by
272 the external model. A model denoting the exterior interface of *Nipponites* was constructed from
273 the external shell and soft body protruding from the aperture and its center was computed in
274 MeshLab.

275 The static orientation of the total model occurs when B and M are vertically aligned. The
276 hydrostatic stability index is computed from these centers.

$$277 \quad S_t = \frac{|B - M|}{\sqrt[3]{V}} \quad (3)$$

278 The separation between the centers of buoyancy (B) and mass (M) is normalized by the cube root
279 of the organismal volume (V; equal to the volume of seawater displaced) in order to be applied
280 to ectocochleates with irregular coiling [20].

281 Apertural angles (θ_a) were measured with respect to the vertical (Fig 1A). That is, angles
282 of zero correspond to a horizontally facing soft body, angles of +90° correspond to an upward
283 facing soft body, and angles of -90° correspond to a downward facing soft body.

284 Thrust angles (θ_t) were measured with respect to the horizontal (Fig 1B) between the
285 point source of thrust and the rotational axis. Therefore, as the thrust angle approaches zero,
286 more energy is transmitted into horizontal movement with a lower rotational component.

287 Rotational thrust angles (θ_{tr}) were measured between the thrust vector (perpendicular to
288 the aperture) and the rotational axis (Fig 1C). A rotational thrust angle of 90° would allow pure
289 rotation to take place, while angles of 0° and 180° would result in translational movement.

290

291 Results

292 The unknown soft body can produce errors in buoyancy calculations depending upon its
293 total volume. By comparing the soft body used herein with a soft body that terminates at the
294 aperture, there is only a 0.5% difference in Φ . Similarly, the mass distribution is not significantly
295 different between either model (a 0.7 % difference in S_t).

296 Because the body chamber ratio was variable on measured specimens, this ratio was
297 manipulated by removing one septum and adding one septum to the terminal stage model with a
298 body chamber ratio of 42%. Removing one septum increases the total body chamber ratio to
299 46%. This change yields a 16% increase in Φ (to 84.6%) and a 7% increase in S_t (to 0.0786).
300 Adding one septum decreases the body chamber ratio to 37%. Yielding a 10% decrease in Φ (to
301 65.7%) and an 8% decrease in S_t (to 0.0676). These changes suggest that small error (~10%) in
302 body chamber ratio would not significantly alter calculations of buoyancy or the characteristics
303 of the mass distribution. Small deviations from the ideal body chamber ratio took place (Table 2)
304 during model construction. However, the body chamber ratio test suggests that their hydrostatic
305 influences are minimal.

306

307 **Table 2. Hydrostatic properties of *Nipponites mirabilis*.**

Stage	Age (%)	BC Ratio	Φ	S_t	θ_a	θ_{ao}	L (mm)	L_x (mm)	L norm	L_x norm	θ_t	θ_{tr}
(Crio) 1	0.18	42.7	97.3	0.099	69.5	69.0	11.65	11.43	1.236	1.212	11.1	7.7
2	0.23	38.6	82.6	0.101	74.3	49.5	10.59	10.59	0.902	0.902	1.0	117.8
3	0.29	40.1	83.5	0.094	13.8	14.5	10.04	9.43	0.726	0.682	-20.1	117.1
4	0.33	39.7	76.4	0.093	99.5	99.5	9.58	8.61	0.616	0.554	26.0	98.2
5	0.38	42.8	77.4	0.069	2.0	-30.3	13.28	11.19	0.773	0.651	-32.6	135.5

6	0.41	42.7	75.5	0.082	22.9	24.1	14.61	12.23	0.787	0.659	-33.1	139.1
7	0.49	42.6	81.7	0.070	24.1	5.0	16.64	14.32	0.765	0.658	-30.6	124.5
8	0.55	41.6	79.8	0.083	31.5	22.4	19.51	16.20	0.821	0.682	-33.9	143.0
9	0.60	42.2	79.8	0.083	31.6	18.8	18.88	16.49	0.753	0.658	-29.1	113.4
10	0.71	41.8	81.3	0.079	34.5	15.1	21.92	21.72	0.758	0.752	-7.6	123.2
11	0.77	41.2	76.3	0.075	17.3	-12.7	22.18	17.38	0.720	0.564	-38.4	122.0
12	0.83	43.5	75.4	0.076	50.1	39.8	27.54	27.38	0.835	0.830	-6.2	154.2
13	0.88	39.1	72.2	0.072	-8.2	-11.1	27.66	24.86	0.807	0.726	-26.0	105.9
(Term) 14	1.00	42.1	73.1	0.073	19.9	30.0	28.10	23.44	0.781	0.651	-33.5	131.1

308 Hydrostatic properties computed for the 14 ontogenetic stages examined. Crio = criocone phase;
 309 Term = terminal phase; Age% = curvilinear length for that stage normalized by the curvilinear
 310 length of the terminal specimen; BC Ratio = curvilinear length of body chamber normalized by
 311 the total curvilinear length at a particular stage; Φ = the proportion of the phragmocone to be
 312 emptied of liquid for a neutrally buoyant condition; S_t = hydrostatic stability index; θ_a = apertural
 313 angle; θ_{ao} = apertural orientation if rib obliquity was ignored (normal to shell growth direction);
 314 L = total lever arm; L_x = x-component of the lever arm, norm = normalized by the cube root of
 315 water displaced for each particular stage; θ_t = thrust angle; θ_{tr} = rotational thrust angle.

316

317 **Ontogenetic changes in hydrostatics**

318 Hydrostatic properties were computed for 14 life stages (Figs 5 and 6; Table 2) in order
 319 to assess changes throughout the ontogeny of *Nipponites mirabilis* and other species sharing
 320 similar morphologies. *Nipponites mirabilis* has the capacity for neutral buoyancy at all life
 321 stages, retaining liquid between approximately 3% and 28% of the total cameral volumes. After
 322 the juvenile criocone phase, Φ decreases and stabilizes at its lower values (Fig 7). Hydrostatic
 323 stability (S_t) follows a similar decreasing trend and does not significantly oscillate (Fig 7). These
 324 hydrostatic stability index values ranging between approximately 0.10 and 0.07 are sufficiently

325 large enough to orient the living cephalopod to maintain some static orientation during all of the
326 examined ontogenetic stages. The orientation of the aperture (θ_a) oscillates in a complicated
327 fashion throughout ontogeny, ranging between approximately -11 and 99 degrees (Fig 7).
328 Apertural orientations significantly turned downwards are not observed. The juvenile criocone
329 phase has apertural angles of about 70°, followed by complex oscillations as the alternating U-
330 shaped bends develop. Afterwards, there is some degree of regularity in orientation, mostly
331 exhibiting horizontal and diagonally upwards directions (Fig 7).

332

333 **Fig 5. Final hydrostatic models of the first eight ontogenetic stages (A-H) of *Nipponites***

334 *mirabilis*. All models are oriented so that their ventral apertures face towards the right. The tip of
335 the upper cone corresponds to the center of buoyancy while the tip of the lower cone is the center
336 of mass. These two centers are vertically aligned, denoting the proper static orientation assumed
337 by living *Nipponites mirabilis*.

338 **Fig 6. Final hydrostatic models of the last six ontogenetic stages (A-F) of *Nipponites***

339 *mirabilis*. All models are oriented so that their ventral apertures face towards the right. The tip of
340 the upper cone corresponds to the center of buoyancy while the tip of the lower cone is the center
341 of mass. These two centers are vertically aligned, denoting the proper static orientation assumed
342 by living *Nipponites mirabilis*.

343 **Fig 7. Hydrostatic Properties Computed Throughout Ontogeny.** The proportion of the

344 phragmocone to be emptied of cameral liquid for neutral buoyancy (Φ ; circles), hydrostatic
345 stability index (S_t ; squares), and apertural angles (θ_a ; triangles) as a function of age (proxied by
346 the curvilinear length for that stage normalized by the curvilinear length of the terminal
347 specimen). Dashed lines denote interpolations between the 14 measured stages.

348

349 **Rib obliquity and static orientation**

350 While apertural orientations during the ontogeny of *Nipponites mirabilis* vary, horizontal
351 to upward orientations are preferred. This is further supported by comparing the apertural angles
352 (as denoted by the orientation of the ribs on the shell) with the same angle if ribs were not
353 oblique (i.e., if the aperture was perfectly perpendicular to the direction of shell growth). The
354 obliquity of the ribs generally enhances the apertural orientation by about 10° in the upwards
355 direction (Fig 8).

356

357 **Fig 8. The Influence of Rib Obliquity on Orientation.** Apertural angles with observed rib
358 obliquity (θ_a ; triangles) and the angles normal to the direction of shell growth (zero obliquity;
359 circles) as a function of age (proxied by the curvilinear length for that stage normalized by the
360 curvilinear length of the terminal specimen). Light grey shading and dark grey shading denote
361 rib obliquity that boosts θ_a in the upwards direction and downward directions, respectively.

362

363 **Directional efficiency of movement**

364 During the juvenile crioconic phase, *Nipponites mirabilis* is well suited for horizontal
365 backwards movement (denoted by the near zero thrust angles; θ_t). This trend somewhat persists
366 into later ontogenetic stages, while slightly decreasing and remaining above -40°. However, after
367 the crioconic phase, the rotational thrust angle (θ_{tr}) dramatically increases as the U-shaped bends
368 in the shell develop; suggesting that there is a strong rotational component of movement when
369 thrust is produced normal to the aperture (Fig 9). While the normalized lever arm lengths seem to
370 decrease during ontogeny, sufficient torques for rotation can only be produced when the

371 rotational thrust angle is high. Furthermore, the x-component of the normalized lever arm is not
372 significantly lower than the total normalized lever arm during ontogeny, suggesting that the
373 subhorizontal declination of the total lever arms would still provide significant rotational
374 movement in ontogenetic stages after the crioconic phase (Fig 9).

375

376 **Fig 9. The Directional Efficiency of Movement.** Thrust angles in the vertical direction (θ_t ;
377 black dashed line), rotational thrust angles (θ_{tr} ; grey dashed line), and lever arms as a function of
378 age (proxied by the curvilinear length for that stage normalized by the curvilinear length of the
379 terminal specimen). The total lever arm (grey solid line) and x-component of that lever arm (X
380 Lever Arm; solid black line) are both normalized by the cube root of the volume of water
381 displaced (V_{wd}) for each stage. Idealized rotation would take place with high, relative x-
382 components of the lever arm and θ_{tr} of 90° . Idealized horizontal movement would occur with θ_t
383 of 0° and θ_{tr} of 0° or 180° .

384

385 Discussion

386 The mode of life of *Nipponites*

387 Hydrostatic simulations reveal that *Nipponites mirabilis* had the capacity for neutral
388 buoyancy throughout its ontogeny, retaining some amount of cameral liquid in the shell to
389 compensate for residual buoyancy (Fig 7). These results support the buoyancy calculations of
390 Ward and Westermann [33], who report a similar scenario for *Nipponites occidentalis*. The
391 inferences drawn from rib obliquity most likely functioning in a neutrally buoyant setting [19]
392 are also supported by the hydrostatic results. While the coiling of *Nipponites* is complex and

393 somewhat resembles vermetid gastropods [23–27], considerable negative buoyancy and resultant
394 benthic modes of life are unlikely.

395 Hydrostatic stability is significantly large enough for living *Nipponites* to assume static,
396 syn vivo orientations throughout its entire ontogeny (excluding some short time after hatching
397 when Reynolds numbers are significantly low). While the hydrostatic stability index slightly
398 decreases throughout ontogeny, the computed values are all larger than the extant *Nautilus*
399 (~0.05 [40]), suggesting that living *Nipponites* probably was not able to significantly modify its
400 own apertural orientation (in terms of its vertical orientation). The highest stability in
401 ectocochleates seem to occur for the orthocones, especially those without cameral deposits
402 [36,40]. Lower stability values should occur for morphotypes with larger body chambers that
403 wrap around the phragmocone (e.g., serpenticones [6,47,49]). At first glance, *Nipponites* seems
404 to fall into this latter category at later ontogenetic stages because of the series of alternating U-
405 bends surrounding the earlier crioconic phase and somewhat large body chamber. However, the
406 sigmoidal soft body (which heavily influences the total mass distribution) actually seems to be
407 somewhat confined in the vertical directions (Figs 5 and 6). That is, most of the soft body is still
408 distributed below the phragmocone, lowering the center of mass relative to the center of
409 buoyancy and increasing hydrostatic stability. In most cases, uncoiling of the shell seems to
410 generally increase hydrostatic stability compared to planispiral ectocochleates
411 [20,36,37,39,45,76].

412 Due to sufficient hydrostatic stability throughout ontogeny, fixed static orientations are
413 assumed by living *Nipponites mirabilis*. That is, upward to horizontally facing orientations are
414 preferred, while downward facing orientations were not observed in any of the examined
415 ontogenetic stages (Fig 7). These observed orientations may have accommodated a lifestyle of

416 feeding upon small prey in the water column, which has been proposed for other nostoceratid
417 heteromorphs [37,45,77]. There is some period of time between about 20% and 40% of the
418 lifespan of *Nipponites mirabilis* (after the crioconic phase and prior to the establishment of
419 regularly alternating U-bends) where orientation oscillates between upward facing and
420 horizontally facing. These somewhat rapid changes may have been an awkward time for these
421 living heteromorphs. On the other hand, this irregularity infers that *Nipponites* was able to
422 assume a functioning lifestyle regardless of these particular differences in orientation. This
423 indifference further suggests that this heteromorph assumed a low energy lifestyle that does not
424 demand athletic predation or predator evasion.

425 If the ribs of *Nipponites mirabilis* were not oblique, the static orientation of this species
426 would be about 10° less (downward) for many of the examined ontogenetic stages (Fig 8). The
427 obliquity of the ribs (which oscillates in magnitude throughout ontogeny [19]), therefore, assists
428 in maintaining a generally horizontal to diagonally upward facing orientation of the soft body.
429 Rib obliquity also suggests that the evasion of downward orientations was required to effectively
430 function for feeding and perhaps locomotion for most stages.

431 **Locomotion of *Nipponites mirabilis***

432 The juvenile crioconic phase of *Nipponites mirabilis* would have been well suited to
433 horizontal backwards movement with minimal rocking due to its low thrust angles and
434 positioning of the hyponome (and thrust vector) relative to the vertical rotational axis (Fig 1A, B;
435 Fig 9). Similar hydrostatic properties are likely for criocone morphotypes with similar
436 proportions. Thrust angles decrease throughout ontogeny with some degree of oscillation but
437 remain above -40°. These thrust angles at later stages suggest that significant amounts of thrust
438 energy would still be transmitted into horizontal backwards movement, though with some degree

439 of rocking. The subzero thrust angles post-criconic phase result in the point of thrust located
440 below the horizontal rotational axis suggesting that movement would be rather complicated, with
441 oscillations in apertural angles about some horizontal axis and vertical axis, simultaneously. By
442 examining the lever arms (normalized for each ontogenetic stage), the horizontal components of
443 the lever arms are not much lower than the total lever arms, suggesting that rotational torque
444 about the vertical axis during jet propulsion would be significant. After the criconic phase, the
445 alternating U-bends in the shell allow the thrust vector to be rotated out of alignment with the
446 vertical rotational axis that passes through the centers of buoyancy and mass. This misalignment
447 after the criconic phase allows rotation about the vertical axis to take place if thrust is produced
448 normal to the orientation of the aperture. However, this rotational thrust angle is not as ideal as
449 torticonic (helical) heteromorphs like the turrilitids [34] and the intermediate phases of
450 *Didymoceras* [37], which are closer to 90°. Instead, these rotational thrust angles, post-criconic
451 phase, fall between pure rotation (90°) and pure translation (180°) at around 135° (with some
452 amount of variation throughout ontogeny). If the hyponome was able to bend 45° right or left,
453 then living *Nipponites* may have been able to select between pure rotational movement and pure
454 translational movement (influenced by some superimposition of chaotic rocking and
455 hydrodynamic drag). This scenario depends upon the largely unknown ammonoid soft body
456 [69,70] and propulsive mechanisms [68]. If the hyponome was not able to significantly bend,
457 then jet thrust for post-cricone phase individuals would be transmitted into a combination of
458 translation and rotation about the vertical axis.

459 The thrust angles and directional efficiency of movement provide useful information
460 about the locomotion and feeding of living *Nipponites*. The lateral movement (and perhaps
461 dispersal potential) of criconic juveniles would have been on par with planispiral ammonoids

462 (albeit with higher hydrodynamic drag), but afterwards, movement is complicated and some
463 amount of rocking and rotation would occur. This rotational movement (pirouetting), however,
464 could have been useful in feeding, perhaps improving the amount of space through which the
465 living ammonoid could have searched for and captured small planktic prey. These hydrostatic
466 properties further support a quasi-planktic, low energy mode of life for *Nipponites*.

467 **Complex heteromorphy in an evolutionary context**

468 Okamoto [78] suggests that *Nipponites* originated from the nostoceratid,
469 *Eubostrioceras* based on comparisons of shell sculpture, early shell morphology, and
470 stratigraphic occurrence. In a theoretical framework, the juvenile crioconic coiling of both
471 *Eubostrioceras japonicum* and its probable descendent, *Nipponites mirabilis*, are very similar.
472 After this phase, the former species retains helical coiling throughout its ontogeny while the
473 latter species alternates sinistral and dextral helical coiling [17–21,78]. While the details of the
474 rather-sudden appearance of *Nipponites* remain unclear, the simulations of the current study infer
475 significant differences in hydrostatic properties between these two nostoceratid genera.
476 *Eubostrioceras japonicum* undergoes similar coiling patterns to the nostoceratid,
477 *Didymoceras*, but has a longer, stretched out helical phase. Hydrostatic simulations by Peterman
478 et al. [37] reveal that *Didymoceras* was poorly suited for lateral movement, yet adept at rotating
479 about its vertical axis. These properties are likely analogous to *Eubostrioceras*. While
480 *Nipponites* has a similar ability to rotate about its vertical axis after the criocone phase,
481 horizontal to diagonally upwards orientations are assumed instead of the likely downward
482 diagonal orientations of *Eubostrioceras*. For *Eubostrioceras* to attain *Nipponites*-like
483 orientations, its shell would have to coil upwards, compromising its helical coiling. Furthermore,
484 the alternating U-bends in *Nipponites* retain some degree of lateral movement potential.

485 Therefore, the seemingly-aberrant coiling of *Nipponites* might represent adaptations to
486 maintaining preferred orientations and effective directions of locomotion.

487 The hydrostatic simulations of *Nipponites mirabilis* also provide a frame of reference for
488 other nostoceratid heteromorphs. *N. occidentalis*, for example, exhibits a larger degree of
489 uncoiling [33], and therefore, may have had higher stability and a larger lever arm for rotation.
490 Similarly, throughout the late Turonian and Coniacian, a larger degree of uncoiling takes place
491 for specimens found in successively younger strata [78]. These specimens cluster into three
492 distinguished morphotypes [78] that may have become more stable and adept at rotation as they
493 progressed through this time interval.

494 **The stigma of heteromorphy**

495 Heteromorph ammonoids have been commonly regarded as bizarre evolutionary
496 experiments or degenerates [8–15], and their unique coiling schemes are enigmatic in terms of
497 their functional morphology and potential modes of life. While the inevitable phylogenetic
498 extinction of heteromorphs (i.e., typolysis) is now rebutted [8], the stigma of this concept has
499 persisted and is further propagated by their seemingly aberrant coiling schemes. Heteromorph
500 ammonoids, however, were very diverse, disparate, and successful throughout the Cretaceous
501 [45,79–81]. Furthermore, the coiling schemes of several morphotypes of heteromorph
502 ammonoids suggest that they exploited unique solutions to manage the physical properties that
503 constrained their modes of life by modifying their shells to serve primarily as specialized
504 hydrostatic devices [36–39]. The hydrostatic simulations of the current study reveal that the
505 coiling of *Nipponites*, which seems biologically absurd, does in fact confer an advantage for
506 specific syn vivo orientations and with rotational capabilities. As suggested for several

507 heteromorphs, the niche currently occupied by cranchid squids may be a suitable analogy for the
508 niche once occupied by *Nipponites* [6,33,76,82].

509

510 **Conclusions**

511 Hydrostatic analyses support a quasi-planktic mode of life for *Nipponites mirabilis* with
512 unique forms of movement that could have enabled a planktotrophic feeding strategy. This
513 species and other heteromorphs with similar proportions had the capacity for neutral buoyancy
514 and were not restricted to the benthos. Throughout the ontogeny of *Nipponites*, horizontally
515 facing to upwardly facing soft body orientations were occupied. These orientations were likely
516 preferred for feeding on small plankton in the water column. This behavior is supported by the
517 tendency for rib obliquity to oscillate [19], which was primarily found to upwardly adjust
518 apertural orientations. Somewhat larger hydrostatic stability values, relative to *Nautilus*, suggest
519 that the vertical component of the apertural orientation would not have significantly changed
520 during locomotion or interaction with external forms of energy. A change in hydrostatics takes
521 place between the juvenile criocone stage and the later stages consisting of alternating U-bends
522 in the shell, specifically regarding the directional propensity for movement. Although the
523 criocone phase of *Nipponites* likely experienced more hydrodynamic drag than planispiral
524 ammonoids of similar size, this morphology was stable, and proficient at backwards horizontal
525 movement. As the alternating U-bends develop, *Nipponites* is better suited for rotational
526 movement about its vertical axis, while possibly maintaining the option to move horizontally
527 backwards by changing the direction of its hyponome. These forms of movement were likely
528 slow, however, suggesting that *Nipponites* assumed a low energy lifestyle while pirouetting to
529 scan for small prey in the water column. The hydrostatic properties throughout the ontogeny of

530 *Nipponites* contrast with those of its probable ancestor, *Eubostriochoceras* [78]. These differences
531 in morphology along with the hydrostatic analyses in the current study infer that the seemingly
532 convoluted coiling scheme of *Nipponites* represents unique adaptive solutions to several
533 hydrostatic constraints, rather than random morphological aberration.

534

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543

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751

752 **Figure and Table Captions**

753 **Fig 1. Hydrostatic Metrics used for *Nipponites mirabilis*.** A, Side view of *Nipponites* in life
754 position showing hypothetical centers of buoyancy (B), mass (M), and the horizontal axis of
755 rotation (R). The angle of the aperture (θ_a) is measured as the inclination from the vertical plane.

756 The thrust angle (θ_t) can be used to assess the directional efficiency of movement. This angle is
757 measured between the horizontal plane, and a line passing through R and the location of the
758 hyponome (source of thrust; H). **B**, Front view of *Nipponites* in life position facing the aperture.
759 This view shows the total lever arm (L) and its x-component (L_x) which is proportionate to the
760 amount of rotational movement about the vertical axis produced during jet propulsion. **C**, Top
761 view of *Nipponites* in life position showing the rotational thrust angle (θ_{tr}). This angle is
762 measured between the vertical rotation axis (vert.), which passes through B and M, and the
763 direction of the thrust vector (arrow emanating from H). Rotational thrust angles of 90° result in
764 idealized transmission of thrust into pure rotation.

765 **Fig 2. Virtual Reconstruction of the Shell of *Nipponites mirabilis*.** **A**, Tessellated (.stl) 3D
766 model generated from a CT scan [60] of specimen INM-4-346. **B**, Reconstructed adoral portion
767 of the body chamber and inner criocone phase with arrays algorithms (Table 1). **C**, Extruded
768 septa generated from the suture pattern. **D**, Extruded shell and septa models unified together to
769 produce a single, manifold 3D mesh of the entire shell.

770 **Fig 3. Thickness Measurements used for Virtual Model Extrusion.** Thicknesses of the shell
771 (black) and septa (grey) as a function of whorl height. Measurements were recorded from
772 specimen NMNS PM35490 and used to define thickness in the virtual model.

773 **Fig 4. Specimens Used for Shell Reconstruction.** **A**, Original concretion containing NMNS
774 PM35490 Umbilical view (**B**) and ventral view (**C**) of the shell section used to record the suture
775 pattern (**D**). **E**, 3D scan of the Mikasa City Museum Specimen (MCM-A0435) used to
776 approximate the body chamber ratio. Scale bar = 2 cm.

777 **Fig 5. Final hydrostatic models of the first eight ontogenetic stages (A-H) of *Nipponites***
778 ***mirabilis*.** All models are oriented so that their ventral apertures face towards the right. The tip of

779 the upper cone corresponds to the center of buoyancy while the tip of the lower cone is the center
780 of mass. These two centers are vertically aligned, denoting the proper static orientation assumed
781 by living *Nipponites mirabilis*.

782 **Fig 6. Final hydrostatic models of the last six ontogenetic stages (A-F) of *Nipponites***

783 *mirabilis*. All models are oriented so that their ventral apertures face towards the right. The tip of
784 the upper cone corresponds to the center of buoyancy while the tip of the lower cone is the center
785 of mass. These two centers are vertically aligned, denoting the proper static orientation assumed
786 by living *Nipponites mirabilis*.

787 **Fig 7. Hydrostatic Properties Computed Throughout Ontogeny.** The proportion of the
788 phragmocone to be emptied of cameral liquid for neutral buoyancy (Φ ; circles), hydrostatic
789 stability index (S_t ; squares), and apertural angles (θ_a ; triangles) as a function of age (proxied by
790 the curvilinear length for that stage normalized by the curvilinear length of the terminal
791 specimen). Dashed lines are interpolated between the 14 measured stages.

792 **Fig 8. The Influence of Rib Obliquity on Orientation.** Apertural angles with observed rib
793 obliquity (θ_a ; triangles) and the angles normal to the direction of shell growth (zero obliquity;
794 circles) as a function of age (proxied by the curvilinear length for that stage normalized by the
795 curvilinear length of the terminal specimen). Light grey shading and dark grey shading denote
796 rib obliquity that boosts θ_a in the upwards direction and downward directions, respectively.

797 **Fig 9. The Directional Efficiency of Movement.** Thrust angles in the vertical direction (θ_t ;
798 black dashed line), rotational thrust angles (θ_{tr} ; grey dashed line), and lever arms as a function of
799 age (proxied by the curvilinear length for that stage normalized by the curvilinear length of the
800 terminal specimen). The total lever arm (grey solid line) and x-component of that lever arm (X
801 Lever Arm; solid black line) are both normalized by the cube root of the volume of water

802 displaced (V_{wd}) for each stage. Idealized rotation would take place with high, relative x-
803 components of the lever arm and θ_{tr} of 90° . Idealized horizontal movement would occur with θ_t
804 of 0° and θ_{tr} of 0° or 180° .

805 **Table 1.** Array instructions used to reconstruct the juvenile criocone phase and the adoral portion
806 of the terminal body chamber. These arrays were used in a piecewise manner to replicate the
807 whorl section from the adoral direction to adapical direction by translation, rotation, and scaling
808 in the x, y, and z directions. Asterisks denote arrays that had their origins reset to their current
809 locations before replication. If origins were not reset, the origins of their previous arrays were
810 used.

811 **Table 2.** Hydrostatic properties computed for the 14 ontogenetic stages examined. Crio =
812 criocone phase; Term = terminal phase; Age% = curvilinear length for that stage normalized by
813 the curvilinear length of the terminal specimen; BC Ratio = curvilinear length of body chamber
814 normalized by the total curvilinear length at a particular stage; Φ = the proportion of the
815 phragmocone to be emptied of liquid for a neutrally buoyant condition; S_t = hydrostatic stability
816 index; θ_a = apertural angle; θ_{ao} = apertural orientation if rib obliquity was ignored (normal to
817 shell growth direction); L = total lever arm; L_x = x-component of the lever arm, norm =
818 normalized by the cube root of water displaced for each particular stage; θ_t = thrust angle; θ_{tr} =
819 rotational thrust angle.

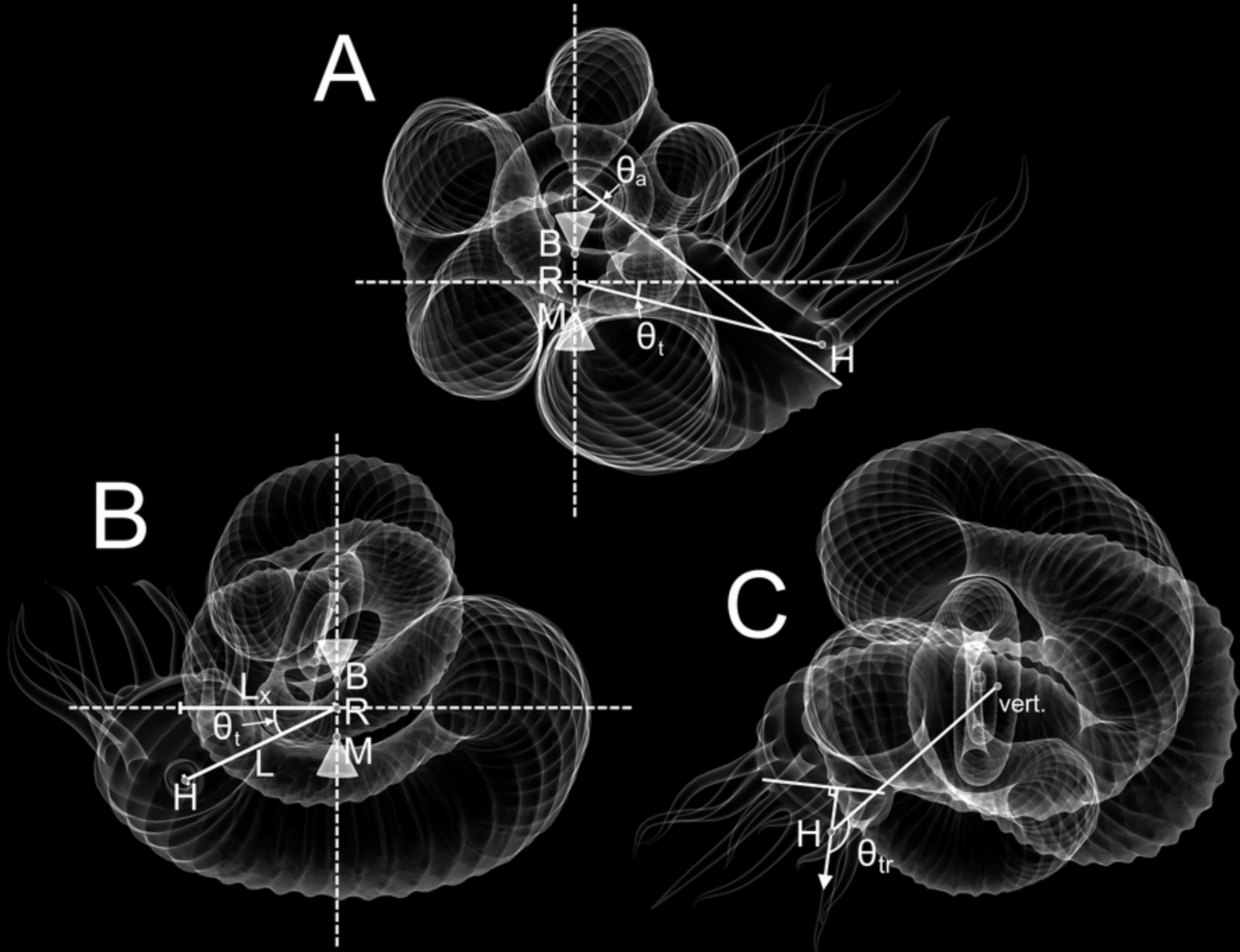


Figure 1

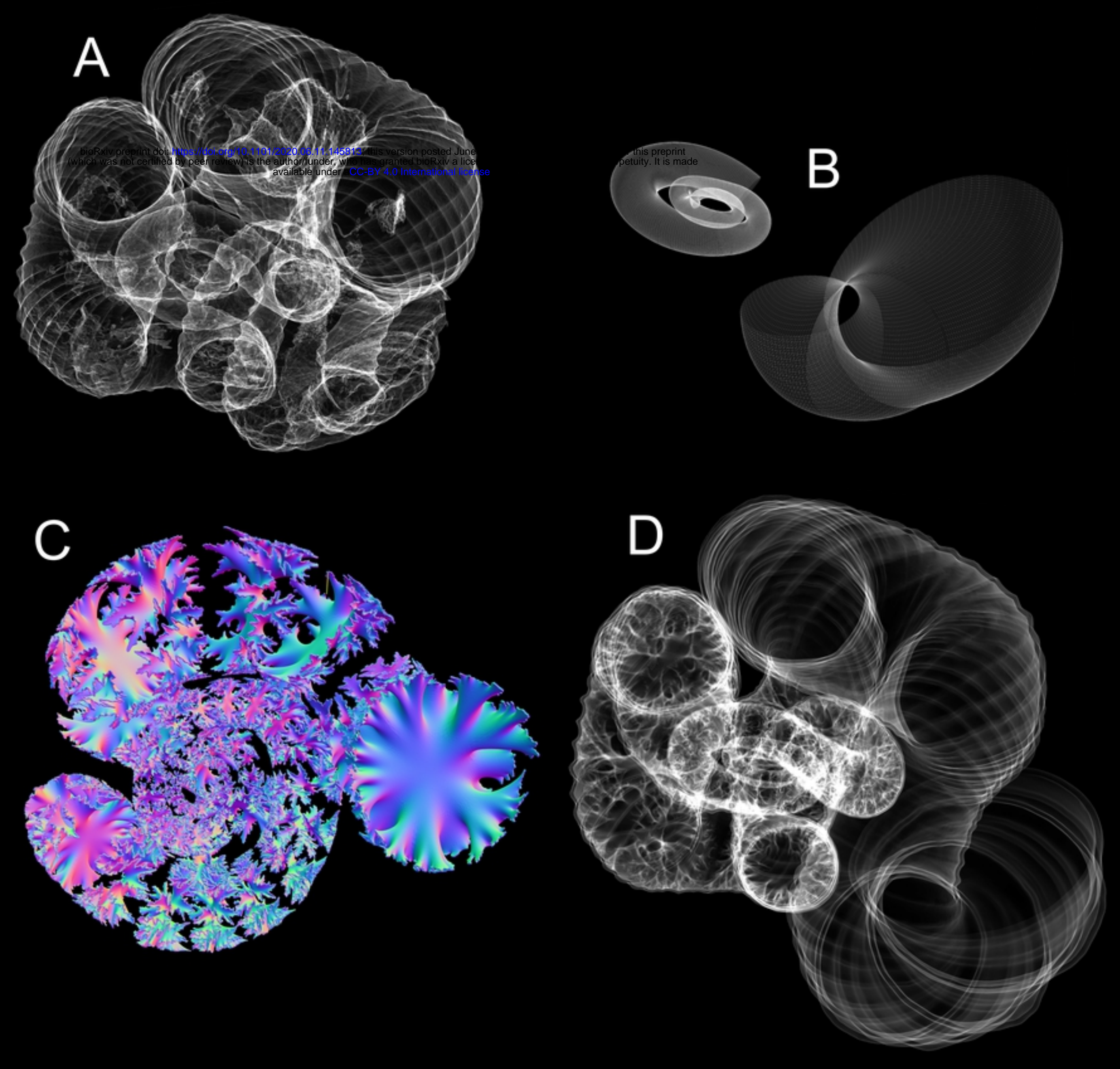


Figure 2

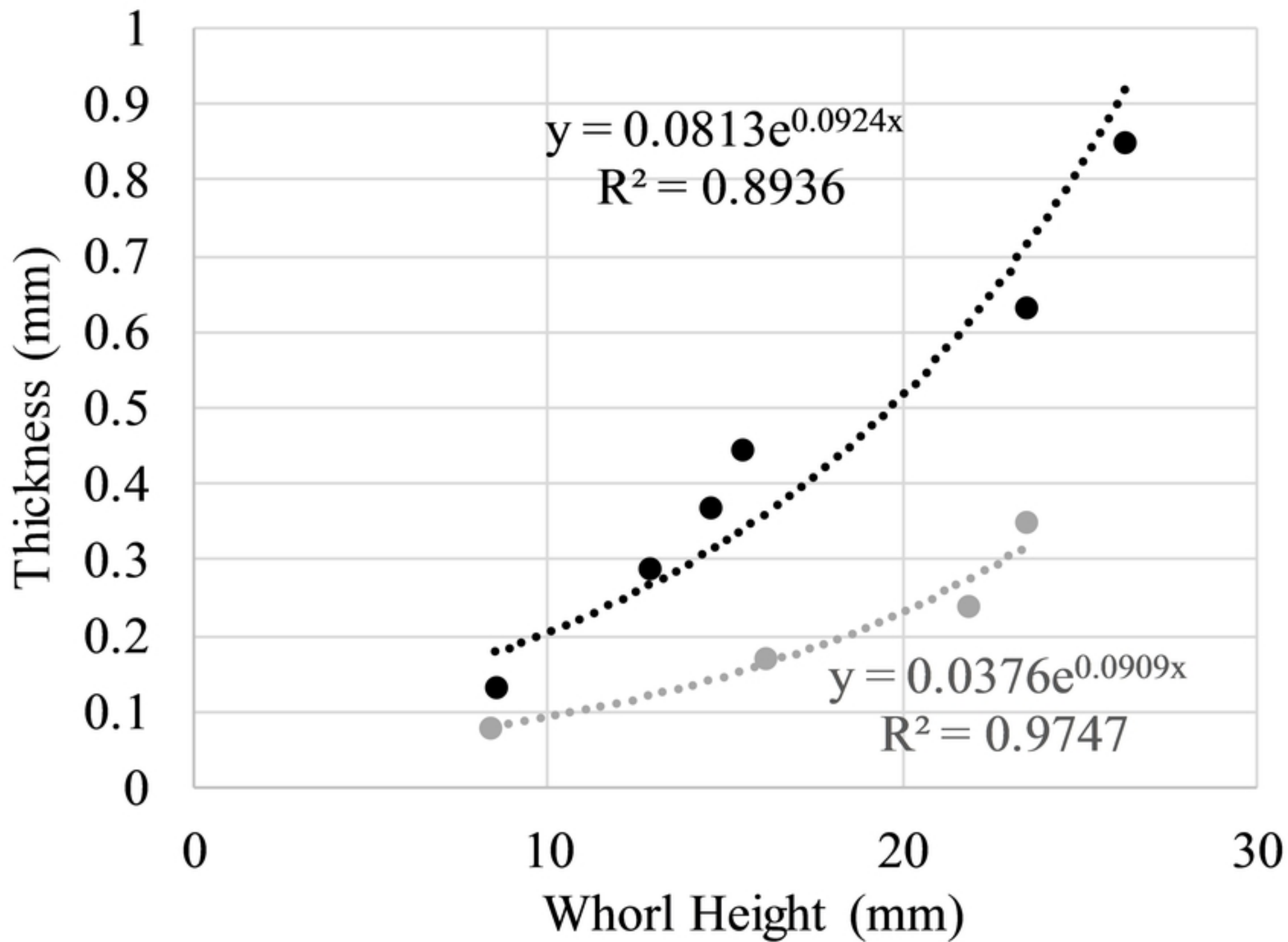
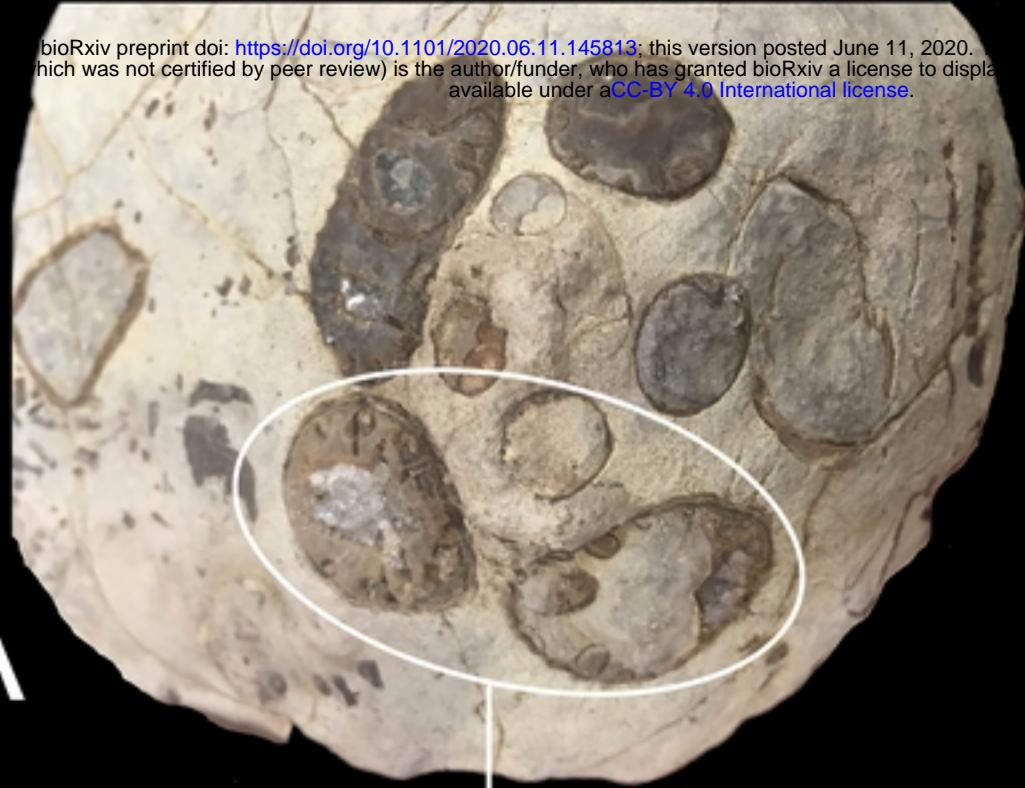


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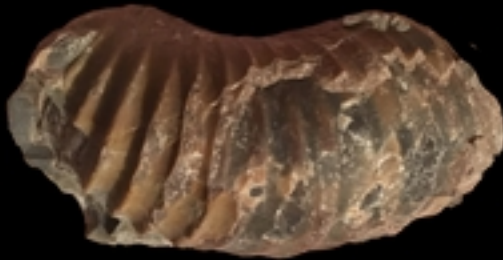
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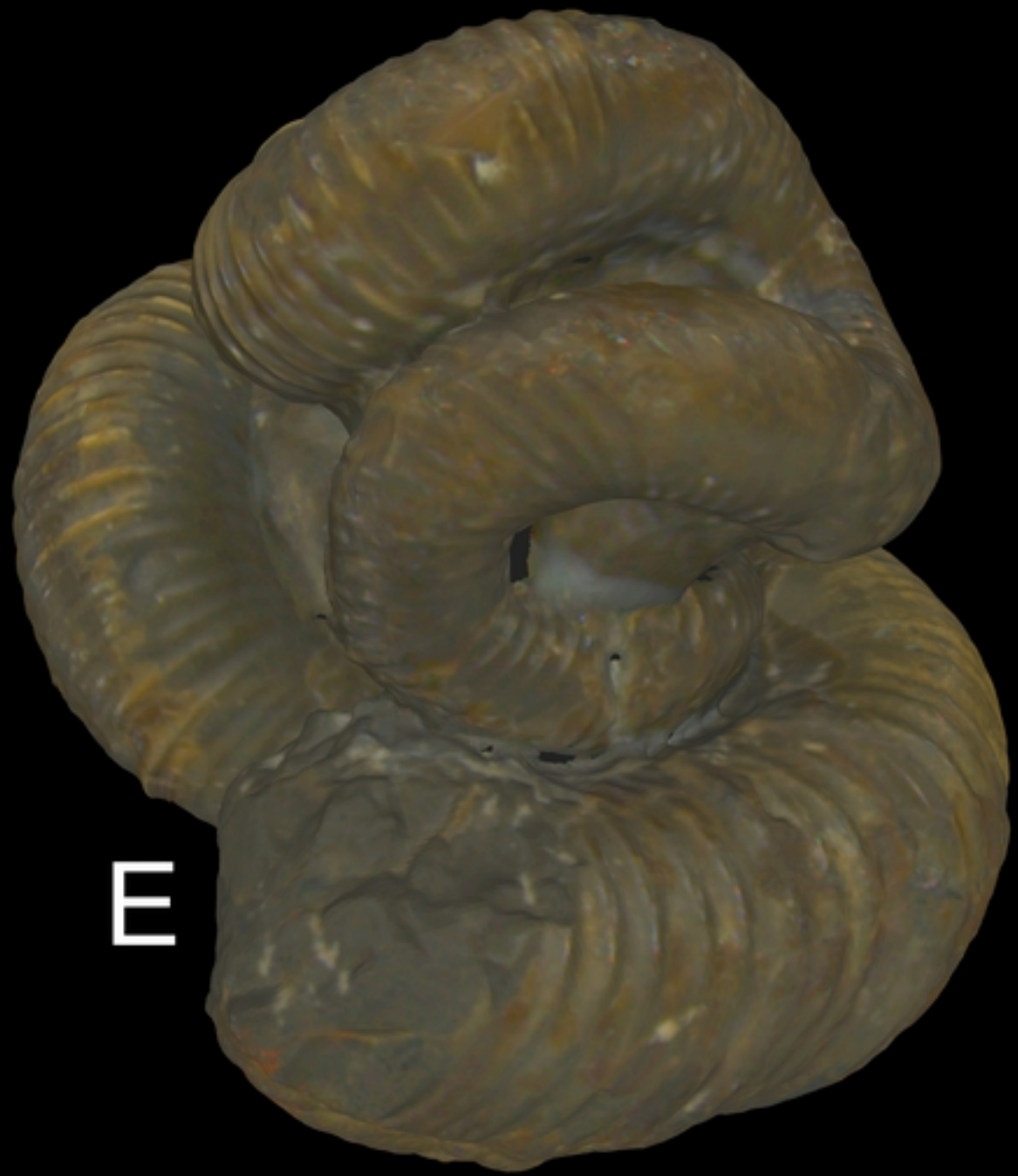
B



C



E



D



Figure 4

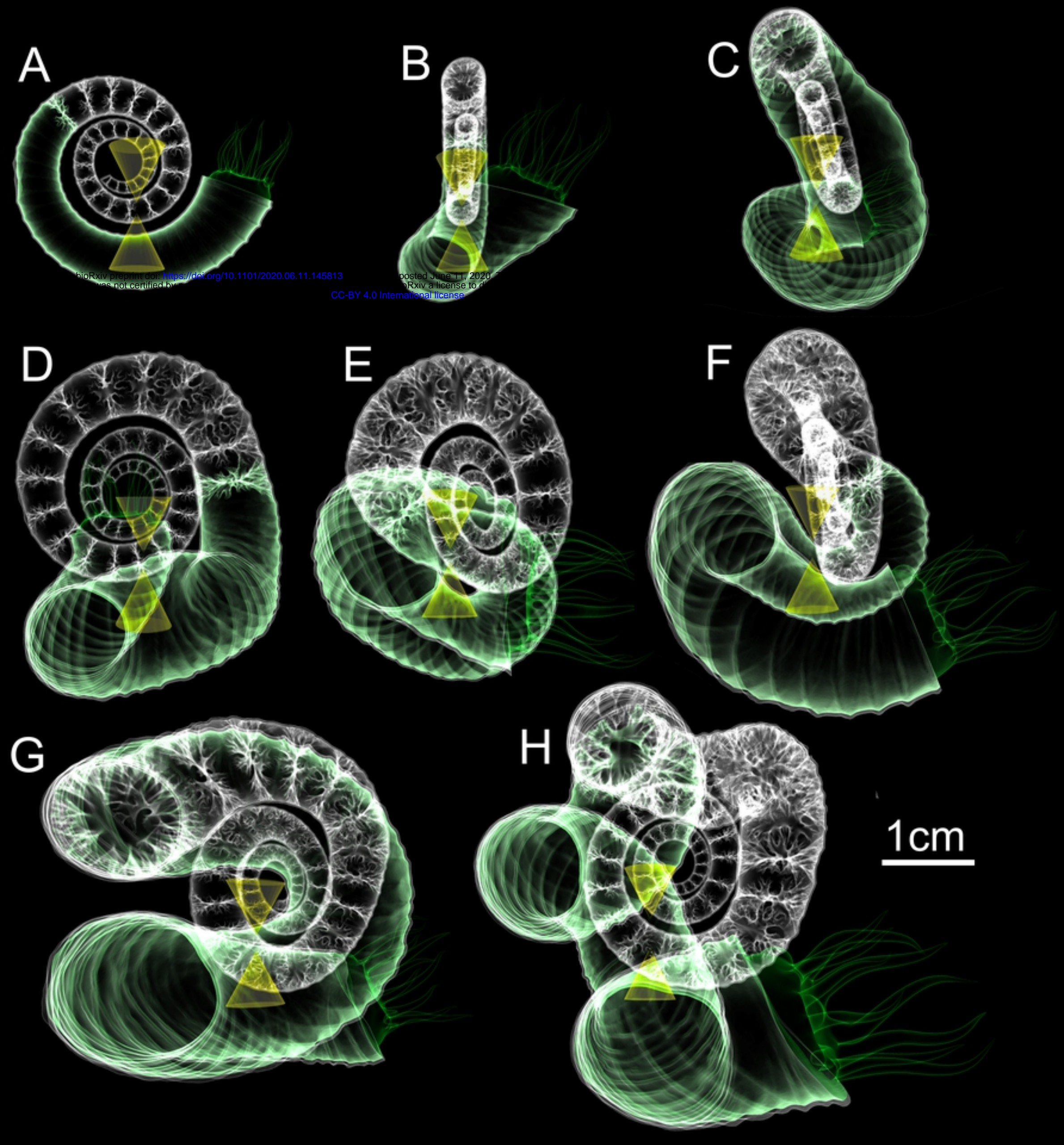


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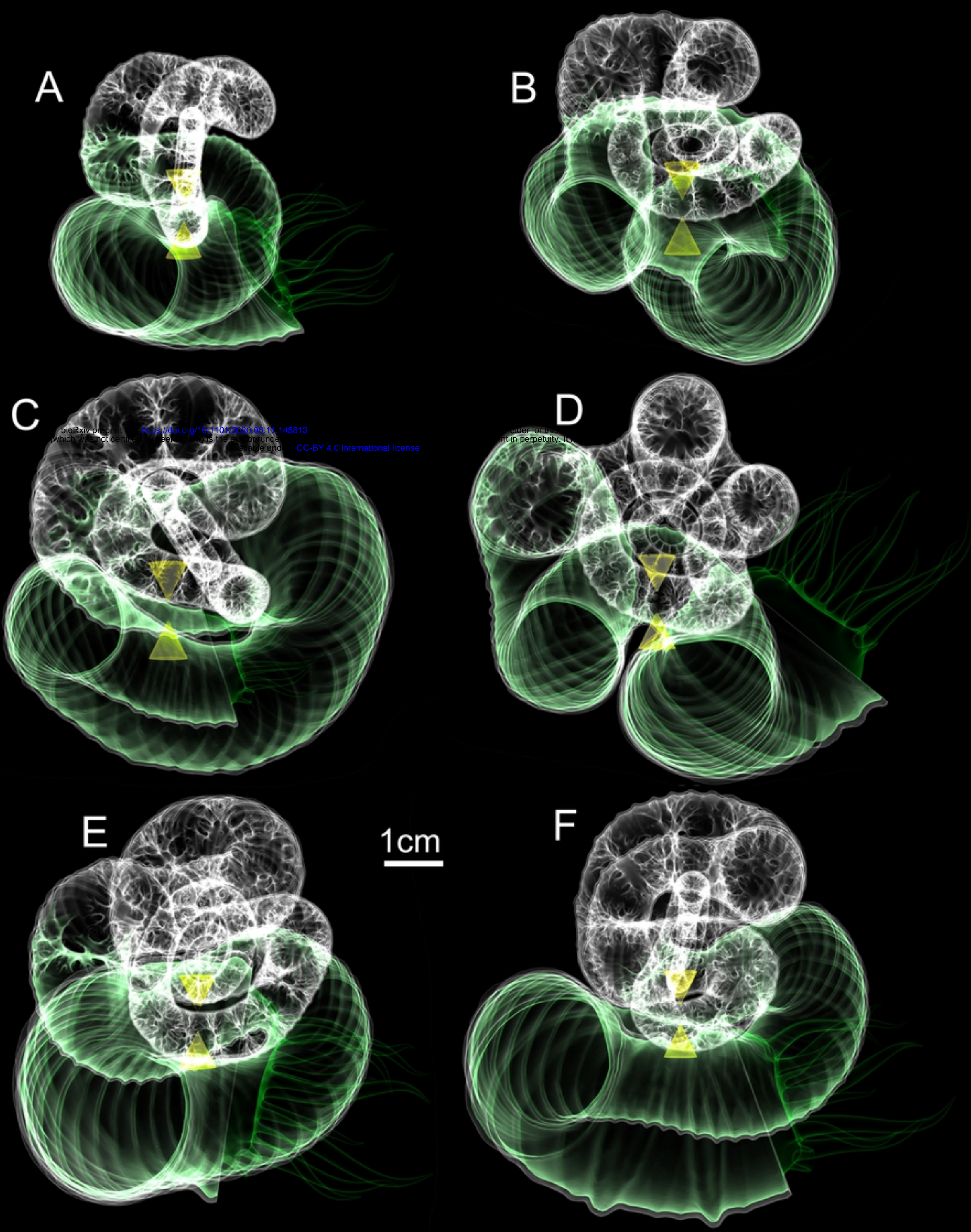


Figure 6

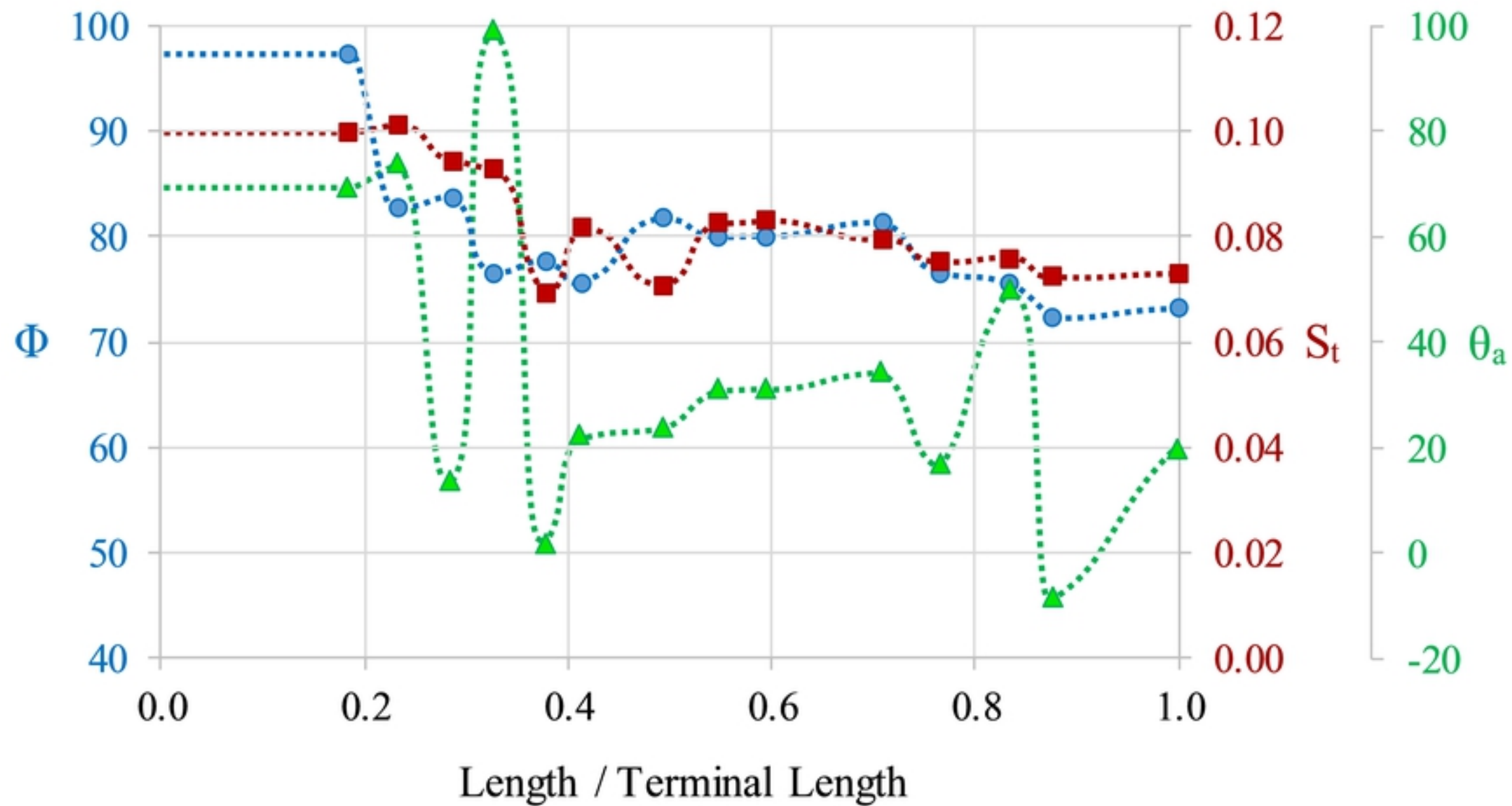


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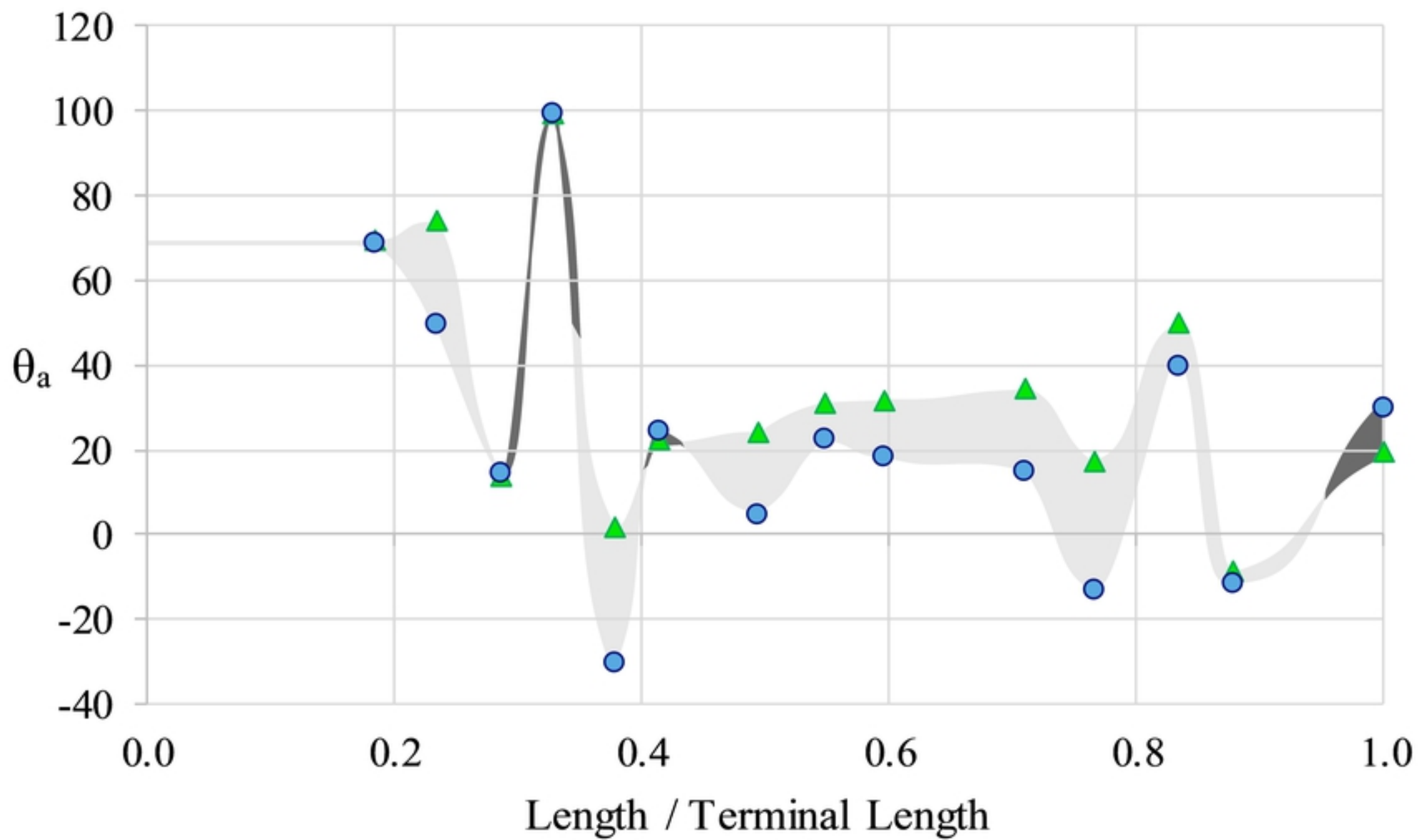


Figure 8

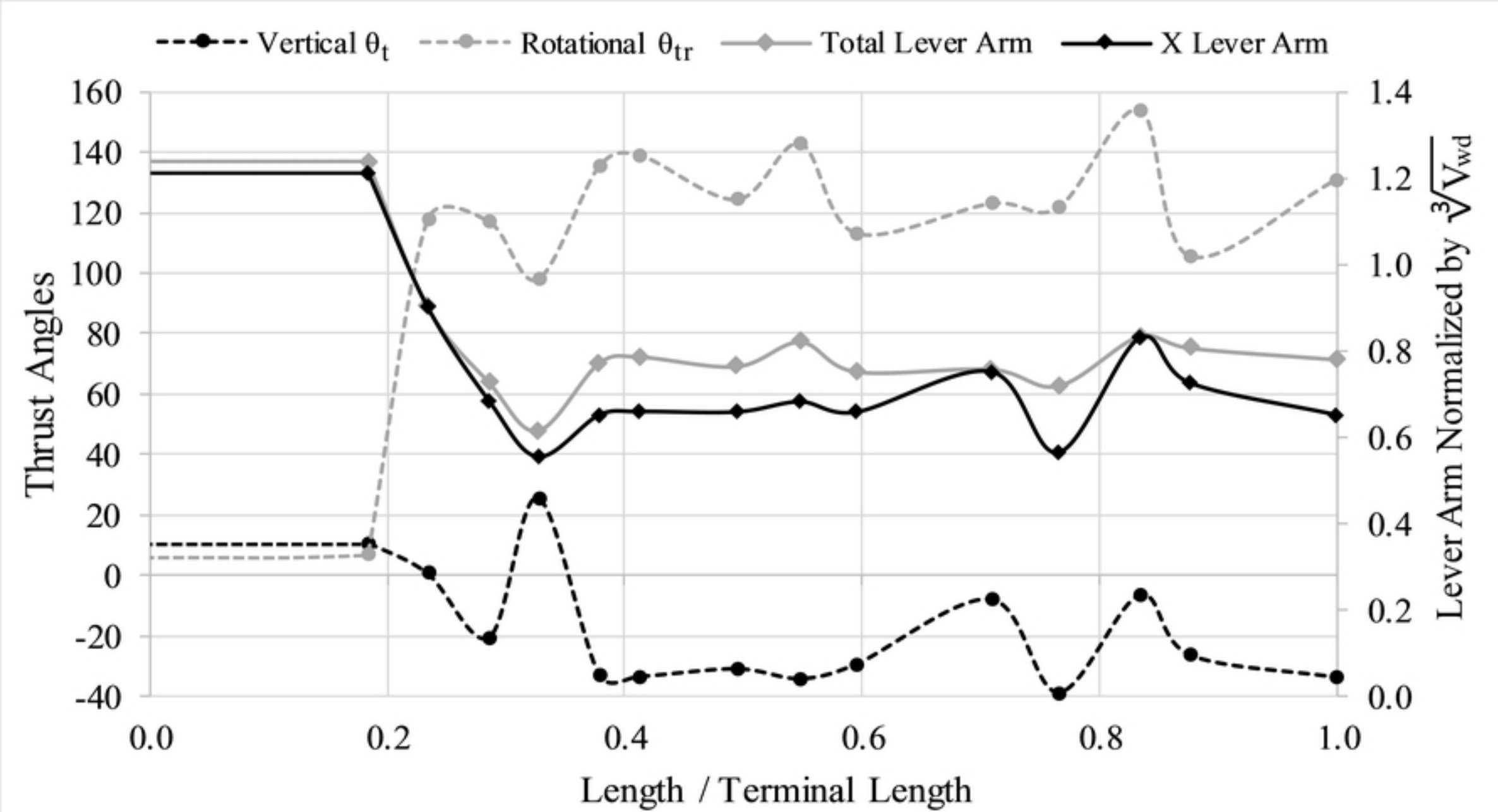


Figure 9