COUPLED DYNAMICS OF BEHAVIOR AND DISEASE CONTAGION AMONG ANTAGONISTIC GROUPS

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Abstract: Disease transmission and behavior change are both fundamentally social phenom-1 ena. Behavior change can have profound consequences for disease transmission, and epidemic 2 conditions can favor the more rapid adoption of behavioral innovations. We analyze a simple 3 4 model of coupled behavior-change and infection in a structured population characterized by homophily and outgroup aversion. Outgroup aversion slows the rate of adoption and can lead to 5 lower rates of adoption in the later-adopting group or even behavioral divergence between groups 6 when outgroup aversion exceeds positive ingroup influence. When disease dynamics are coupled 7 to the behavior-adoption model, a wide variety of outcomes are possible. Homophily can either 8 9 increase or decrease the final size of the epidemic depending on its relative strength in the two groups and on R_0 for the infection. For example, if the first group is homophilous and the second is not, the second group will have a larger epidemic. Homophily and outgroup aversion can also produce dynamics suggestive of a "second wave" in the first group that follows the peak 12 of the epidemic in the second group. Our simple model reveals dynamics that are suggestive 13 of the processes currently observed under pandemic conditions in culturally and/or politically 14 polarized populations such as the United States. 15

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Keywords: transmission dynamics; coupled contagion; homophily; outgroup aversion; social
 distancing

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1. INTRODUCTION

Behavior can spread through communication and social learning like an infection through a community (Bass, 1969; Centola, 2018). Cavalli-Sforza and Feldman, who 21 pioneered treating cultural transmission in an analogous manner to genetic transmission, noted that "another biological model may offer a more satisfactory interpretation of the 23 diffusion of innovations. The model is that of an epidemic" (Cavalli-Sforza and Feldman, 24 1981, 32-33). The biological success of *Homo sapiens* has been attributed to its capacity for cumulative culture, and particularly to the rapid and flexible adaptability that arises 26 from social learning (Henrich, 2015). Adoption of adaptive behaviors during an epidemic 27 of an infectious disease could be highly beneficial to both individuals and the population 28 in which they are embedded (Fenichel et al., 2011). Coupling models of behavioral 29 adoption and the transmission of infectious disease, what we call *coupled contagion* 30

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models, may thus provide important insights for understanding dynamics and control of epidemics. While we might expect strong selection—both biological and cultural—for adaptive responses to epidemics, complications such as the potentially differing time scales of culture and disease transmission and the existence of social structures that shape adoption may complicate convergence to adaptive behavioral solutions.

In this paper, we explore the joint role of *homophily*—the tendency to form ties with 36 people similar to oneself—and *outgroup aversion*—the tendency to avoid behaviors pref-37 erentially associated with an outgroup. Identity exerts a powerful force on the dynamics 38 of behavior (Hogg and Abrams, 2007; Bishop, 2009; Mason, 2018; Smaldino, 2019; Klein, 39 2020; Moya et al., 2020). This is because identity at least partly determines whom we 40 associate with, communicate with, and strive to either emulate or avoid. Our analysis 41 is predicated on the idea that this matters for the dynamics of infection. For exam-42 ple, Salathé and Bonhoeffer (2008) showed that if rates of vaccine adherence cluster on 43 networks, as when communities collectively adopt identity-based positions on the likely 44 costs and benefits of vaccination (Bauch and Earn, 2004) or when like-minded individu-45 als tend to assort in social networks (Bishop, 2009), the overall vaccination rates needed 46 for herd immunity can be substantially higher than suggested by models that assume 47 random vaccination. 48

Homophily involves interactions with ingroup members at rates higher than expected 49 by chance. Homophily is often treated as though it were a global propensity for as-50 sortment by type (e.g. Centola, 2011). However, homophily is frequently observed to a greater or lesser degree across subgroups, a phenomenon known as differential homophily 52 (Morris, 1991). Consider a case of two interacting groups, where one is more homophilous 53 than the other. The less homophilous group may consist of more "frontline" workers, 54 who are exposed to a broader cross-section of the population by nature of their work. 55 In such cases, differential homophily may lead to differential disease dynamics in each 56 group. 57

Members of opposed identity groups not only engage with the world differently, they 58 can react in divergent ways to identical stimuli. Asked to watch political debates or hear 59 political arguments, partisans often grow more strongly partisan, to the consternation of 60 moderates (Taber et al., 2009). In the U.S., partial identities have become increasingly 61 defined in terms of their opposition to the opposing party (Abramowitz and Webster, 62 When considering the adoption of products, consumers often become disen-63 2016).chanted with otherwise attractive purchases if the products are associated with identity 64 groups viewed as different from their own (Berger and Heath, 2007, 2008). Smaldino 65 et al. (2017) modeled the spread of a behavior among members of two groups who re-66 sponded positively to the behavioral contagion but tended to reject it if it was overly 67 associated with the outgroup. They showed that outgroup aversion not only decreased 68 the overall rate of adoption, but could also delay or even entirely suppress adoption in 69 one of the groups. While populations vary in the extent to which they are polarized or 70 parochial, identity clearly matters to the adoption of health behaviors in at least com-71 munities. For example, in the U.S., people who identify with the right-wing Republican 72 party are much less likely than those identifying with the center-left Democratic party to 73

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endorse mask-wearing or belief in its efficacy in preventing disease transmission during
the COVID-19 pandemic (van Kessel and Quinn, 2020).

Several previous studies have considered the coupled contagion of behavior and infec-76 tion, usually focused on cases where the behavior is one that decreases the spread of the 77 disease (such as social distancing or wearing face masks) and sometimes using the as-78 sumption that increased disease prevalence promotes the spread of the behavior (Tanaka et al., 2002; Epstein et al., 2008; Funk et al., 2010; Verelst et al., 2016; Fast et al., 2015; 80 Fu et al., 2017; Hébert-Dufresne et al., 2020; Mehta and Rosenberg, 2020). These models 81 typically assume that individuals differ only in behavior and disease status. Thus, the 82 spread of both disease and behavior depend primarily on rates of behavior transmission 83 and disease recovery. This is true even of models in which the population is structured on 84 networks. Network structure can change the dynamics of contagion. However, contrary 85 to the assumptions of most models, behavioral distributions on social networks are any-86 thing but random. People assort in highly non-random ways (McPherson et al., 2001) 87 and these non-random associations both drive and are driven by social identity. This 88 suggests that the role of social identity is an important, but under-studied, component 89 of coupled contagion models. 90

Here, we consider how identity—and particularly homophilous interactions with in-91 group members and aversion to adopt behaviors used by an outgroup—influences the 92 spread of novel behaviors that consequently affect the transmission of infectious disease. 93 The model we will present is complex, and hence challenging to analyze. To help us 94 make sense of the dynamics, we will first describe the dynamics of infection and behav-95 ior adoption in isolation, and then explore the full coupled model. We will first show how 96 homophily can introduce temporal delays in the infection trajectories between groups. 97 We will then show how outgroup aversion can lead to reduced or even fully inhibited 98 behavior adoption by the later-adopting group. Finally, we will analyze the fully cou-99 pled model and show how the identity-driven forces we consider can lead differentiated identity groups to experience an epidemic in very different ways.

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2. The SIR model of infection with homophily

We model infection in a population in which individuals can be in one of three states: 103 Susceptible, Infected, and Recovered. When susceptibles interact with infected individu-104 als, they become infected with a rate equal to the effective transmissibility of the disease. 105 τ . Infected individuals recover with a constant probability ρ per infection per unit time. 106 This is the well-known SIR model of epidemics (Kermack and McKendrick, 1927; Tolles and Luong, 2020). The baseline model assumes random interactions governed by mass 108 action, and the dynamics are described by well-known differential equations. This model yields the classic dynamics in which the susceptible and recovered populations appear 110 as nearly-mirrored sigmoids, while the rate of infected individuals rises and falls. The 111 threshold for the epidemic is given by the basic reproduction number, R_0 , which is a 112 measure of the expected number of secondary cases caused by a single, typical primary 113

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case at the outset of an epidemic in a population entirely composed of uninfected individuals. An epidemic occurs when $R_0 > 1$. For the basic SIR model in a closed population, $R_0 = \frac{\tau}{a}$.

Our analysis will focus on scenarios where individuals assort based on identity. In 117 this case, assume that individuals all belong to one of two identity groups, indicated 118 with the subscript 1 or 2. Let w_i be the probability that interactions are with one's 119 ingroup, $i \in \{1, 2\}$. It is therefore a measure of homophily; populations are homophilous 120 when $w_i > 0.5$. It is important to recognize that groups can differ in their homophily 121 (Morris, 1991). For example, if groups differ in socioeconomic class and group 1 tends 122 to employ members of a group 2 as service workers, homophily will be higher for group 123 1; a member of group 2 is more likely to encounter members of group 1 than the reverse. 124 We can update the equations governing infection dynamics for members of group 1, with 125 analogous equations governing members of group 2. 126

$$\frac{dS_1}{dt} = -\tau S_1 \left(w_1 I_1 + (1 - w_1) I_2 \right)$$
$$\frac{dI_1}{dt} = \tau S_1 \left(w_1 I_1 + (1 - w_1) I_2 \right) - \rho I_1$$
$$\frac{dR_1}{dt} = \rho I_1$$

We assume the disease breaks out in one of the two groups, so the initial number 127 of infected in group 1 is small but nonzero, while the initial number of infected in 128 group 2 is exactly zero. Without loss of generality, we have assumed that group 1 is always infected first. When homophily is low, the model exhibits standard SIR dynamics 130 approximating a single unified population. When an infection breaks out in group 1, 131 homophily can delay the outbreak of the epidemic in group 2. Homophily for each group works somewhat synergistically, but the effect is dominated by w_2 . This is because the 133 infection spreads rapidly in a homophilous group 1, and if group 2 is not homophilous, its 134 members will rapidly become infected. However, if group 2 is homophilous, its members can avoid the infection for longer, particularly when group 1 is also homophilous. If 136 only group 2 is homophilous, the initial outbreak will be delayed, but the peak infection 137 rate in group 2 can actually be higher than in group 1, as the infection is driven by 138 interactions with both populations (Figure 1). 139

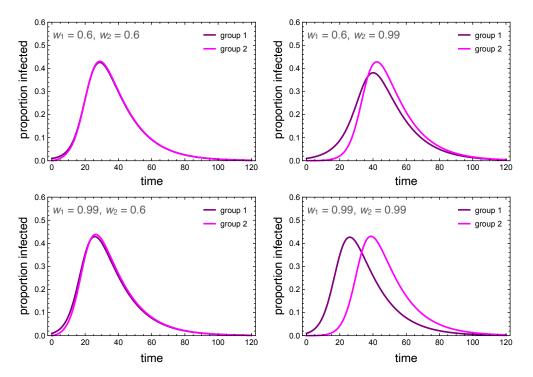
We also considered the case in which the transmissibility of the infection can be reduced to very near the recovery rate, so that R_0 is very close to 1. In this case, homophily can protect groups where infection did not originally break out by keeping members relatively separated from the infection group (Figure S2).

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3. Behavioral Contagion with Outgroup Aversion

We model behavior adoption as a susceptible-infectious-susceptible (SIS) process, in which individuals can oscillate between adoption and non-adoption of the behavior indefinitely. We view this as more realistic than an SIR process for preventative-but-transient behaviors like social distancing or wearing face masks. To avoid confusion with infection



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FIGURE 1. Dynamics of the infected population of each group under low and high homophily ($w_i = 0.6, 0.99$). Other parameters used were $\tau = 0.3, \rho = 0.07, I_1(0) = 0.01, I_2(0) = 0. R_0 \approx 4.28$ in the absence of homophily.

status, we denote individuals who adopted the preventative behavior as Careful (C), and those who have not as Uncareful (U). Unlike a disease, which is reasonably modeled as equally transmissible between any susceptible-infected pairing, where behavior is concerned, susceptible individuals are more likely to adopt when interacting with ingroup adopters, but less likely to adopt when interacting with outgroup adopters. We model the behavioral dynamics for members of group 1 are as follows, with analogous equations¹ governing members of group 2:

$$\frac{dU_1}{dt} = -(\alpha_1 + \beta C_1) U_1 + (\gamma C_2 + \delta) C_1$$
$$\frac{dC_1}{dt} = (\alpha_1 + \beta C_1) U_1 - (\gamma C_2 + \delta) C_1$$

Members of group *i* may spontaneously adopt the behavior independent of direct social influence, and do so at rate α_i . This adoption may be due to individual assessment of the

¹Because all individuals have either adopted or not, $U_1 = 1 - C_1$, these coupled equations can be replaced by a single equation through substitutions. For intuitive reasons, we leave them as two coupled equations.

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behavior's utility, to influences separate from peer mixing, such as from media sources, or to socioeconomic factors that make behavior adoption more or less easy for certain groups. For these reasons, we assume that groups can differ on their rates of spontaneous adoption. In reality, it is possible for groups to differ on all four model parameters, all of which can influence differences in adoption rates. For simplicity, we restrict our analysis to differences in spontaneous adoption.

¹⁶⁴ Uncareful individuals are positively influenced to become careful by observing careful ¹⁶⁵ individuals of their own group, with strength β . However, this is countered by the force ¹⁶⁶ of outgroup aversion, γ , whereby individuals may cease being careful when they observe ¹⁶⁷ this behavior among members of the outgroup. The behavior is eventually discarded at ¹⁶⁸ rate δ , representing financial and/or psychological costs of continuing to adopt preventive ¹⁶⁹ behaviors like social distancing or wearing face masks.

This model assumes no explicit homophily in terms of behavioral influence. On the one hand, it seems obvious that we observe and communicate with those in our own group more than other groups. On the other hand, opportunities for observing outgroup behaviors are abundant in a digitally-connected world, which alter the conditions for cultural evolution (Acerbi, 2019). For simplicity, we do not add explicit homophily terms to this system. Instead, we simply adjust the relative strengths of ingroup influence and outgroup aversion, β/γ . When this ratio is higher, it reflects stronger homophily for behavioral influence.

Numerical simulations that illustrate the influence of outgroup aversion are depicted in Figure 2. In all cases, the careful behavior is first adopted by group 1. In the absence of outgroup aversion, both groups adopt the behavior at saturation levels, with group 2 being slightly delayed. When outgroup aversion is added, the delay increases, but more importantly, overall adoption declines for both groups. This decline continues as long as the strength of outgroup aversion is less than the strength of positive ingroup influence. A phase transition occurs here (Figure 2C,D). Although group 2 may initially adopt the behavior, adoption is subsequently suppressed, resulting in a polarizing behavior that is abundant in group 1 but nearly absent in group 2.

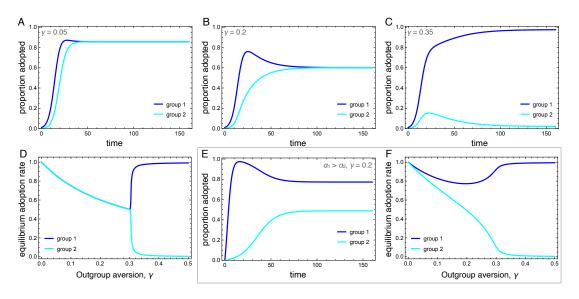
We also consider the case in which one group has a higher intrinsic adoption rate, which could be driven by differences in personality types, norms, or media exposure between the two groups. When $\alpha_1 > \alpha_2$, the equilibrium adoption rate for group 1 could be considerably higher than for group 2, even when ingroup positive influence was greater than outgroup aversion (Figure 2E, F). Note that these differences arise entirely because of outgroup aversion. When $\gamma = 0$, both groups adopt at maximum levels.

Outgroup aversion has a strong influence on adoption dynamics. It can delay adoption, reduce equilibrium adoption rates, and even suppress adoption entirely in the lateradopting group. As we will see, when the behavior being adopted influences disease transmission, quite interesting dynamics can emerge.

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4. COUPLED CONTAGION WITH HOMOPHILY AND OUTGROUP AVERSION

Before we explore the coupled dynamics of this system, we must add one more consideration to the model. We focus on the adoption of preventative behaviors that decrease

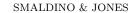


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FIGURE 2. Dynamics of the behavioral adoption. (A-C) Behavior adoption dynamics in each group for different levels of outgroup aversion, γ . Parameters used were $\alpha_1 = \alpha_2 = 0.001$, $\beta = 0.3$, $\delta = 0$, $C_1(0) = 0.01$, $C_2(0) = 0$. (D) Equilibrium adoption rates for each group as a function of outgroup aversion, γ . A bifurcation occurs when outgroup aversion overpowers the forces of positive influence. (E) Behavior adoption dynamics for $\gamma = 0.2$ where group 1 has a higher spontaneous adoption rate, $\alpha_1 = 0.1$. Here, the two groups converge to different equilibrium adoption rates. (F) Equilibrium adoption rates for each group as a function of outgroup aversion, γ , when $\alpha_1 = 0.1$.

the effective transmission rate of the infection, such as social distancing or wearing face masks. We model this by asserting that the transmission rate is τ_C for careful individuals and τ_U for uncareful individuals, such that $\tau_U \geq \tau_C$. When considering the interaction between careful and uncareful individuals, we use the geometric mean, so the transmissibility between SU and IU (that is, between susceptible and infected individuals who are both uncareful) is $\sqrt{\tau_U \tau_C}$. We use the geometric mean so that if either population reduces its transmissibility to zero, transmission among its members becomes impossible.

The full model has six compartments, with two-letter abbreviations denoting the disease and behavioral state (Figure 3). The coupled dynamics for members of group 1 are as follows, with analogous equations governing members of group 2, such that the full system is defined by 12 coupled differential equations. A list of all parameters is



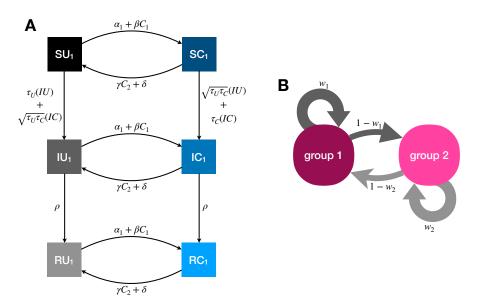


FIGURE 3. Illustration of the dynamics for the coupled contagion model. (A) Transition probabilities between compartments for members of group 1. For simplicity these probabilities do not include the influence of homophily. (B) homophilous interactions. Members of group *i* have physical contact with members of their own group with probability w_i and members of the outgroup with probability $1 - w_i$.

presented in Table 1.

$$\begin{split} \frac{d(SU_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(SC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(SU_1\right) - \\ \tau_U(SU_1) \left[w_1(IU_1) + (1 - w_1)IU_2\right] - \sqrt{\tau_U\tau_C}(SU_1) \left[w_1(IC_1 + (1 - w_1)IC_2\right] \\ \frac{d(SC_1)}{dt} &= -\left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(SC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(SU_1\right) - \\ \sqrt{\tau_U\tau_C}(SC_1) \left[w_1(IU_1) + (1 - w_1)IU_2\right] - \tau_C(SC_1) \left[w_1(IC_1 + (1 - w_1)IC_2\right] \\ \frac{d(IU_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(IC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(IU_1\right) + \\ \tau_U(SU_1) \left[w_1(IU_1) + (1 - w_1)IU_2\right] + \sqrt{\tau_U\tau_C}(SU_1) \left[w_1(IC_1 + (1 - w_1)IC_2\right] - \rho(IU_1) \\ \frac{d(IC_1)}{dt} &= - \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(IC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(IU_1\right) + \\ \sqrt{\tau_U\tau_C}(SC_1) \left[w_1(IU_1) + (1 - w_1)IU_2\right] + \tau_C(SC_1) \left[w_1(IC_1 + (1 - w_1)IC_2\right] - \rho(IC_1) \\ \frac{d(RU_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IU_1) \\ \frac{d(RC_1)}{dt} &= - \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IU_1) \\ \frac{d(RC_1)}{dt} &= - \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) - \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_2 + RC_2\right)\right] \left(RC_1\right) + \left[\alpha_1 + \beta \left(SC_1 + IC_1 + RC_1\right)\right] \left(RU_1\right) + \rho(IC_1\right) \\ \frac{d(RC_1)}{dt} &= \left[\delta + \gamma \left(SC_2 + IC_$$

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TABLE 1. Model parameters.

Parameter	Definition
$ au_C$	disease transmissibility for careful individuals
$ au_U$	disease transmissibility for uncareful individuals
ho	disease recovery rate
w_i	homophily for group i
$lpha_i$	spontaneous behavior adoption rate for group i
β	ingroup positive influence on behavior
γ	outgroup negative influence on behavior
δ	behavior discard rate

Behavioral adoption is independent of infection status in this model. This may not be a realistic assumptions for some systems, such as Ebola, where the both the infection status of the adopter and the perceived incidence in the population are likely to influence behavior. The assumption seems more realistic for infections like influenza and COVID-19, where infection status is not always transparent and decisions are likely to be made on the basis of more abstract socially-transmitted information. There are intermediate cases, however, such as where media reports of disease prevalence or the perceived availability may influence the adoption of preventative behaviors (Lau et al., 2010; Zhang et al., 2015; Seale et al., 2020). We do not consider such cases here.

To make the behavioral adoption most meaningful, we focus on the case where instantaneous and universal adoption of the careful behavior would decrease the disease transmissibility so that $R_0 < 1$. That is, if everyone immediately adopted the behavior, the epidemic would fizzle out. However, behavior adoption does not typically work this way. We have already noted that under assumptions of between-group variation and outgroup aversion, a behavior is likely to be adopted neither instantaneously nor universally. The question we tackle now is how those socially-driven facets of behavioral adoption influence disease dynamics.

Figure 4 illustrates the wide range of possible disease dynamics under varying assumptions of homophily and outgroup aversion. A wider range of homophily values are explored in the Supplemental Materials (Figures S4, S5). In the absence of either homophily or outgroup aversion, our results mirror previous work on coupled contagion in which the adoption of inhibitory behaviors reduces peak infection rates, flattening the curve of infection. Due to differences in spontaneous adoption rates, however, group 2 may see a higher peak infection rate even when the infection breaks out in group 1, because the inhibitory behavior spreads more slowly in that group (Figure 4A).

Homophilous interactions further lower infection rates. If group 1 alone is homophilous, the infection rate declines in that group, while peak infections actually increase in group 2 (Figure 4C). This is because group 1 adopts the careful behavior early, decreasing their transmission rate and simultaneously avoiding contact with the less careful members of group 2, who become infected through their frequent contact with group 1. If group 2 alone is homophilous, on the other hand, the infection is staved off even more so than if both groups are homophilous (Figure 4B, D). This is because members of group 2 avoid

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contact with group 1 until the careful behavior has been widely adopted, while members of group 1 diffuse their interactions with some members of group 2, and these are less likely to lead to new infections.

Outgroup aversion considerably changes these dynamics. First and foremost, outgroup 242 aversion leads to less widespread adoption of careful behaviors, dramatically increasing 243 the size of the epidemic. Moreover, because under many circumstances there will be 244 between-group differences in equilibrium behavior-adoption rates, this can lead to dra-245 matic group differences in infection dynamics. In the absence of outgroup aversion, we 246 saw that homophily in group 2 could lead to an almost total suppression of the epidemic. 247 Not so with outgroup aversion, in which the peak infection rates *increase* relative to the 248 low homophily case (Figure 4E, F). This occurs because homophily causes a delay in 249 the infection onset in group 2. Behavioral adoption slows the epidemic initially in both groups. However, when the infection finally reaches group 1, behavioral adoption has 251 decreased past its maximum due to the outgroup aversion, causing peak infections in 252 both groups to soar. 253

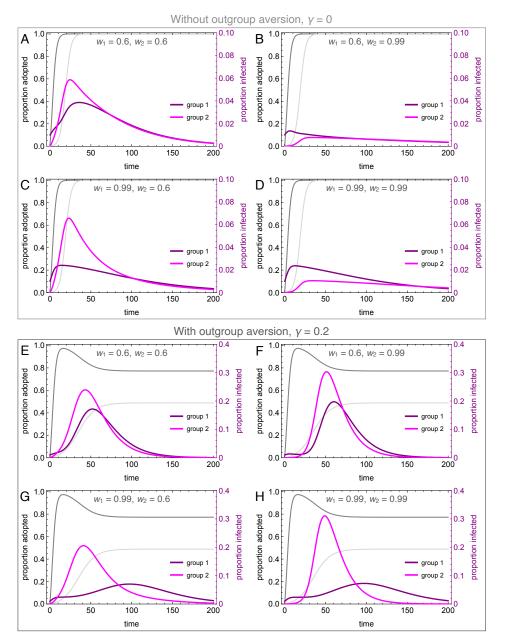
The dynamics are particularly interesting for the case where the group in which the 254 epidemic first breaks out (group 1 in our analyses) is also strongly homophilous. Due to homophily along with rapid behavior adoption, the epidemic is initially suppressed in this group. However, due to slower and incomplete behavior adoption, the infection 257 spreads rapidly in group 2. As the infection peaks in group 2 while group 1 decreases 258 its behavior adoption rate, we observe a delayed "second wave" of infection in group 1, well after the infection has peaked in group 2 (Figure 4G). This effect is exacerbated 260 when both groups are homophilous, as the epidemic runs rampant in the less careful 261 group 2 (Figure 4H). As shown in the Supplementary Material, the timing of the second 262 wave is also delayed to a greater extent when the adopted behavior is more efficacious 263 at reducing transmission (Figure S6). 264

We explored the differences in the timing of the infection peaks between the two 265 groups, as illustrated in Figure 5. As noted, homophily in group 1 has a larger effect than 266 homophily in group 2 because the infection first breaks out in group 1. Without outgroup 267 aversion, the infection peak in group 1 is usually closely timed to the infection peak in 268 group 2, usually coming slightly later due to group 2's lagged adoption of the preventative 269 behavior (Figure 5A). If group 1 has very strong homophily, however, the infection can peak earlier there, as its spread to group 2 is impeded. When outgroup aversion is strong, 271 however, group 2's adoption of the preventative behavior is severely impeded, which cases 272 its infection rate to peak much earlier than in group 1, and this effect is only bolstered 273 by strong homophily in group 1 (Figure 5B). The effect of outgroup aversion on the 274 differential timing between groups of infection rate peaks is non-monotonic (Figure 5C). peaking at intermediate values of γ . 276

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5. Discussion

It is well known that disease transmission is influenced by behavior. What is often overlooked is how behavior itself changes within heterogeneous cultural populations.



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FIGURE 4. Coupled contagion dynamics when the behavior leads to highly effective reduction in transmissibility, under varying conditions of homophily and outgroup aversion. Notice difference in y-axis scale for infection rate between top and bottom sets of graphs. Parameters used: $\tau_U = 0.3$, $\tau_C = 0.069$, $\rho = 0.07$, $\alpha_2 = 0.1$, $\alpha_2 = 0.001$, $\beta = 0.3$, $\delta = 0$, $SU_1(0) = 0.98$, $SC_1(0) = 0.01$, $IU_1(0) = 0.01$, $IC_1(0) = RU_1(0) = RC_1(0) = 0$, $SU_2(0) = 1.0$, $SC_2(0) = IU_2(0) =$ $IC_2(0) = RU_2(0) = RC_2(0) = 0$.

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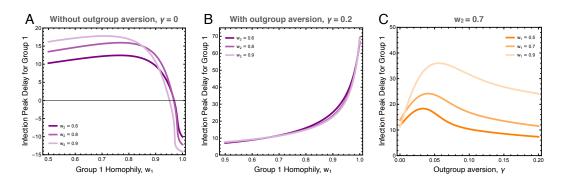


FIGURE 5. Difference in the timing of the peak infection rates between groups. These plots show the extend to which the peak in group 1 lags behind the peak in group 2. The first two plots show the peak delay for group 1 as a function of group 1 homophily, (A) with and (B) without outgroup aversion, γ . The third plot (C) more systematically varies outgroup aversion, for several values of group 1 homophily and moderate group 2 homophily, $w_2 = 0.7$. Other parameters used: $\tau_U = 0.3$, $\tau_C = 0.069$, $\rho = 0.07$, $\alpha_2 = 0.1$, $\alpha_2 = 0.001$, $\beta = 0.3$, $\delta = 0$.

Both population structure and social identity influence who interacts with whom, affecting disease transmission, and who learns from whom, affecting behavior change. We have highlighted two of these forces—homophily and outgroup aversion—and shown their dramatic influence on disease dynamics in a simple model.

In terms of social interaction and behavior adoption dynamics, group identity exerts 284 its influence by way of homophily, a powerful social force. Aral et al. (2009), for ex-285 ample, showed that homophily accounted for more than 50% of contagion in a natural experiment on behavioral adoption. The effect of homophily on diffusion dynamics can 287 be variable. For example, homophily can slow down convergence toward best responses in strategic networks (Golub and Jackson, 2012). This can be critical when the time scales of learning and infection are different. Homophily can also lower the threshold for 290 desirability (or the selective advantage) required for adoption of a behavior. Creanza and 291 Feldman (2014) showed that homophily and selection can have balancing effects—the 292 selective advantage of a trait does not need to be as high to spread when it is trans-293 mitted assortatively by its bearers. In the case of our coupled-contagion model, strong 294 homophily interferes with the adaptive adoption of protective behavior. Centola (2011) 295 showed that homophily can increase the rate of adoption of health behaviors, but his 296 experimental population could assort only on positive cues, and had no ability to signal 297 or perceive group identity.

Consider the observed adoption dynamics under differential homophily. When the homophily of group 1 is less than group 2, group 1 can be interpreted as "frontline" workers, who are exposed to a broader cross-section of the population by nature of their work. Outgroup avoidance of this group's adopted protective behavior can arise if there are status differentials across the groups. Prestige bias, the tendency to adopt behaviors

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associated with high-status individuals, is a mechanism that can drive differential uptake 304 of novel behavior by different groups (Boyd and Richerson, 1985), for which there is quite 305 broad support (Jiménez and Mesoudi, 2019). When both groups are highly homophilous 306 and outgroup aversion is strong, the resulting dynamics suggest the case of negative 307 partisanship, a type of outgroup aversion in which partisans select actions based not on 308 explicit policy preferences but in opposition to the outgroup (Abramowitz and Webster, 309 2016). In this case, differences in the relative size of the epidemic will be driven purely 310 by differences in the rates of preventative behavior adoption by the two groups, including 311 those differences induced by outgroup aversion. 312

Incorporating adaptive behavior into epidemic models has been shown to significantly 313 alter dynamics (Fenichel et al., 2011). Prevalence-elastic behaviors (Funk et al., 2010) 314 are those behaviors that increase with the growth of an epidemic. While these behav-315 iors may be protective, they can also lead to cycling of incidence, which can prolong 316 epidemics. Similarly, the adoption of some putatively-protective behaviors that are ac-317 tually ineffective can be driven by the existence of an epidemic when the cost of adoption 318 is sufficiently low (Tanaka et al., 2009). We have shown in this paper that group-identity 319 processes can have large effects, leading groups that would otherwise respond adaptively 320 to the threat of an epidemic to behave in ways that put them, and the broader popula-321 tions in which they are embedded, at risk. 322

The context of the ongoing COVID-19 pandemic provides some interesting and timely 323 perspective on the relationship between behavior, adaptive or otherwise, and transmis-324 sion dynamics. While there remains much uncertainty about the infection fatality ratio 325 of COVID-19, and how this varies according to individual, social, and environmental 326 context, it is clear that the great majority of infections do not lead to death (Russell 327 et al., 2020; Meyerowitz-Katz and Merone, 2020). Furthermore, the extensive presymp-328 tomatic (or even asymptomatic) transmission of the SARS-CoV-2 (He et al., 2020; Li 329 et al., 2020; Arons et al., 2020) is likely to reduce associations between behavior and local 330 infection rates. We expect that such a situation will not induce strong prevalence-elastic behavioral responses, and that the sorts of identity-based responses we describe here will 332 dominate the behavioral effects on transmission. 333

How do we intervene in a way to offset the pernicious effects of negative partisanship on the adoption of adaptive behavior? While it may seem obvious, strategies for spreading efficacious protective behaviors in a highly-structured population with strong outgroup aversion will require weakening the association between protective behaviors and particular subgroups of the population. Given that we are writing this during a global pandemic in which perceptions and behaviors are highly polarized along partisan lines, attempts to mitigate partisanship in adaptive behavioral responses seem paramount to support.

The models we have analyzed in this paper are broad simplifications of the coupled dynamics of behavior-change and infection. It would therefore be imprudent to use them to make specific predictions. The goal of this approach is to develop strategic models in the sense of Holling (1966), sacrificing precision and some realism for general understanding of the potential interactions between social structure, outgroup aversion,

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347 348	and coupled contagion (Levins, 1966; Smaldino, 2017). Such models provide a scaffold for the development of richer theories concerning coupled disease and behavioral contagions.
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352 353	PES led the work on model conceptualization and analysis, with extensive contribution from JHJ. Both authors wrote and edited the manuscript.
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357	n/a
358	Research Transparency and Reproducibility
359	n/a
360	References
361 362	Abramowitz, A. I. and Webster, S. (2016). The rise of negative partisanship and the nationalization of U.S. elections in the 21st century. <i>Electoral Studies</i> , 41:12–22.
363 364 365	 Acerbi, A. (2019). Cultural Evolution in the Digital Age. Oxford University Press. Aral, S., Muchnika, L., and Sundararajana, A. (2009). Distinguishing influence-based contagion from homophily-driven diffusion in dynamic networks. Proceedings of the
366 367	National Academy of Sciences, USA, 106(51):21544–21549. Arons, M. M., Hatfield, K. M., Reddy, S. C., Kimball, A., James, A., Jacobs, J. R.,
368	Taylor, J., Spicer, K., Bardossy, A. C., Oakley, L. P., Tanwar, S., Dyal, J. W., Harney,
369 370	J., Chisty, Z., Bell, J. M., Methner, M., Paul, P., Carlson, C. M., McLaughlin, H. P., Thornburg, N., Tong, S., Tamin, A., Tao, Y., Uehara, A., Harcourt, J., Clark, S.,
371	Brostrom-Smith, C., Page, L. C., Kay, M., Lewis, J., Montgomery, P., Stone, N. D.,
372	Clark, T. A., Honein, M. A., Duchin, J. S., and Jernigan, J. A. (2020). Presymptomatic
373	SARS-CoV-2 infections and transmission in a skilled nursing facility. New England
374	Journal of Medicine, 382(22):2081–2090.
375	Arthur, R. F., Gurley, E. S., Salje, H., Bloomfield, L. S. P., and Jones, J. H. (2017).
376	Contact structure, mobility, environmental impact and behaviour: the importance of social forces to infectious disease dynamics and disease ecology. <i>Philosophical Trans</i> -
377 378	actions of the Royal Society B: Biological Sciences, 372(1719):1–9.
379	Bass, F. M. (1969). A new product growth for model consumer durables. <i>Management</i>
380	Science, 15(5):215–227.

Bauch, C. T. and Earn, D. J. (2004). Vaccination and the theory of games. *Proceedings* of the National Academy of Sciences, 101(36):13391–13394.

COUPLED DYNAMICS OF BEHAVIOR AND DISEASE

- Berger, J. and Heath, C. (2007). Where consumers diverge from others: Identity signaling and product domains. *Journal of Consumer Research*, 34(2):121–134.
- Berger, J. and Heath, C. (2008). Who drives divergence? identity signaling, outgroup
 dissimilarity, and the abandonment of cultural tastes. Journal of Personality and
 Social Psychology, 95(3):593.
- Bishop, B. (2009). The big sort: Why the clustering of like-minded America is tearing us apart. Houghton Mifflin Harcourt.
- Boyd, R. and Richerson, P. J. (1985). *Culture and the evolutionary process*. University of Chicago press, Chicago.
- Cavalli-Sforza, L. L. and Feldman, M. (1981). Cultural transmission and evolution: A
 quantitative approach, volume 16 of Monographs in Population Biology. Princeton
 University Press, Princeton.
- Centola, D. (2011). An experimental study of homophily in the adoption of health behavior. *Science*, 334(6060):1269–1272.
- Centola, D. (2018). How behavior spreads: The science of complex contagions. Princeton
 University Press.
- Creanza, N. and Feldman, M. W. (2014). Complexity in models of cultural niche construction with selection and homophily. *Proceedings of the National Academy of Sci- ences*, 111(Supplement 3):10830–10837.
- Diekmann, O., Heesterbeek, J. A. P., and Metz, J. A. J. (1990). On the definition and
 the computation of the basic reproduction ratio r0 in models for infectious diseases in
 heterogeneous populations. *Journal of Mathematical Biology*, 28(4):365–382.
- Epstein, J. M., Parker, J., Cummings, D., and Hammond, R. A. (2008). Coupled con tagion dynamics of fear and disease: mathematical and computational explorations.
 PLoS One, 3(12).
- Fast, S. M., González, M. C., Wilson, J. M., and Markuzon, N. (2015). Modelling the
 propagation of social response during a disease outbreak. *Journal of The Royal Society Interface*, 12(104):20141105.
- Fenichel, E. P., Castillo-Chavez, C., Ceddia, M. G., Chowell, G., Parra, P. A. G., Hickling, G. J., Holloway, G., Horan, R., Morin, B., Perrings, C., Springborn, M., Velazquez, L., and Villalobos, C. (2011). Adaptive human behavior in epidemiological
- ⁴¹⁴ models. Proceedings of the National Academy of Sciences, 108(15):6306–6311.
- Fu, F., Christakis, N. A., and Fowler, J. H. (2017). Dueling biological and social conta gions. *Scientific Reports*, 7:43634.
- Funk, S., Salathé, M., and Jansen, V. A. (2010). Modelling the influence of human
 behaviour on the spread of infectious diseases: a review. *Journal of the Royal Society Interface*, 7(50):1247–1256.
- Golub, B. and Jackson, M. O. (2012). How homophily affects the speed of learning and best-response dynamics. *The Quarterly Journal of Economics*, 127(3):1287–1338.
- 422 He, X., Lau, E. H. Y., Wu, P., Deng, X., Wang, J., Hao, X., Lau, Y. C., Wong, J. Y.,
- 423 Guan, Y., Tan, X., Mo, X., Chen, Y., Liao, B., Chen, W., Hu, F., Zhang, Q., Zhong,
- 424 M., Wu, Y., Zhao, L., Zhang, F., Cowling, B. J., Li, F., and Leung, G. M. (2020). Tem-
- ⁴²⁵ poral dynamics in viral shedding and transmissibility of COVID-19. *Nature Medicine*.

SMALDINO & JONES

- 426 Hébert-Dufresne, L., Mistry, D., and Althouse, B. M. (2020). Spread of infectious disease
- and social awareness as parasitic contagions on clustered networks. arXiv preprint
 arXiv:2003.10604.
- Heffernan, J., Smith, R., and Wahl, L. (2005). Perspectives on the basic reproduction
 ratio. Journal of the Royal Society Interface, 2:281–293.
- Henrich, J. (2015). The Secret of Our Success: How Culture Is Driving Human Evolution,
 Domesticating Our Species, and Making Us Smarter. Princeton University Press,
 Princeton.
- Hogg, M. A. and Abrams, D. (2007). Intergroup behavior and social identity. The Sage
 handbook of social psychology: Concise student edition, pages 335–360.
- 436 Holling, C. S. (1966). The strategy of building models of complex ecological systems. In
- 437 Watt, K. E. F., editor, Systems Analysis in Ecology, pages 195–214. Academic Press.
- Jiménez, A. V. and Mesoudi, A. (2019). Prestige-biased social learning: current evidence
 and outstanding questions. *Palgrave Communications*, 5(1):20.
- Keeling, M. J. and Rohani, P. (2007). Modeling Infectious Diseases in Humans and
 Animals. Princeton University Press, Princeton.
- Kermack, W. O. and McKendrick, A. G. (1927). A contribution to the mathematical
 theory of epidemics. *Proceedings of the Royal Society of London A*, 115:700–721.
- Klein, E. (2020). Why we're polarized. Simon and Schuster.
- Lau, J. T., Griffiths, S., Choi, K.-c., and Lin, C. (2010). Prevalence of preventive
 behaviors and associated factors during early phase of the H1N1 influenza epidemic.
 American Journal of Infection Control, 38(5):374–380.
- Levins, R. (1966). The strategy of model building in population biology. *American Scientist*, 54(4):421–431.
- Li, R., Pei, S., Chen, B., Song, Y., Zhang, T., Yang, W., and Shaman, J. (2020). Substantial undocumented infection facilitates the rapid dissemination of novel coronavirus (sars-cov2). *Science*, 368(6490):489–493.
- Mason, L. (2018). Uncivil agreement: How politics became our identity. University of
 Chicago Press.
- McPherson, M., Smith-Lovin, L., and Cook, J. M. (2001). Birds of a feather: Homophily
 in social networks. Annual Review of Sociology, 27:415–444.
- Mehta, R. S. and Rosenberg, N. A. (2020). Modeling anti-vaccine sentiment as a cultural
 pathogen. *Evolutionary Human Sciences*.
- Meyerowitz-Katz, G. and Merone, L. (2020). A systematic review and meta-analysis of
 published research data on COVID-19 infection-fatality rates. *International Journal* of Infectious Diseases.
- Morris, M. (1991). A log-linear modeling framework for selective mixing. *Mathematical Biosciences*, 107(2):349–377.
- Moya, C., Cruz y Celis Peniche, P., Kline, M. A., and Smaldino, P. E. (2020). Dynam-
- ics of behavior change in the COVID world. American Journal of Human Biology,
 32:e23485.
- ⁴⁶⁷ Russell, T. W., Hellewell, J., Jarvis, C. I., van Zandvoort, K., Abbott, S., Ratnayake,
- 468 R., group, C. C.-. w., Flasche, S., Eggo, R. M., Edmunds, W. J., and Kucharski,
- 469 A. J. (2020). Estimating the infection and case fatality ratio for coronavirus disease

COUPLED DYNAMICS OF BEHAVIOR AND DISEASE

- (COVID-19) using age-adjusted data from the outbreak on the Diamond Princess
 cruise ship, February 2020. *Eurosurveillance*, 25(12):2000256.
- Salathé, M. and Bonhoeffer, S. (2008). The effect of opinion clustering on disease outbreaks. Journal of The Royal Society Interface, 5(29):1505–1508.
- 474 Seale, H., Heywood, A. E., Leask, J., Sheel, M., Thomas, S., Durrheim, D. N., Bolsewicz,
- K., and Kaur, R. (2020). COVID-19 is rapidly changing: Examining public perceptions
 and behaviors in response to this evolving pandemic. *PLOS ONE*, 15(6):e0235112.
- 477 Smaldino, P. E. (2017). Models are stupid, and we need more of them. In Vallacher,
- R. R., Read, S. J., and Nowak, A., editors, *Computational social psychology*, pages 311–331. Routledge.
- Smaldino, P. E. (2019). Social identity and cooperation in cultural evolution. *Behavioural Processes*, 161:108–116.
- Smaldino, P. E., Janssen, M. A., Hillis, V., and Bednar, J. (2017). Adoption as a social
 marker: Innovation diffusion with outgroup aversion. *The Journal of Mathematical* Sociology, 41(1):26-45.
- Taber, C. S., Cann, D., and Kucsova, S. (2009). The motivated processing of political arguments. *Political Behavior*, 31(2):137–155.
- Tanaka, M. M., Kendal, J. R., and Laland, K. N. (2009). From traditional medicine
 to witchcraft: Why medical treatments are not always efficacious. *PLOS ONE*,
 4(4):e5192.
- Tanaka, M. M., Kumm, J., and Feldman, M. W. (2002). Coevolution of pathogens and
 cultural practices: a new look at behavioral heterogeneity in epidemics. *Theoretical Population Biology*, 62(2):111–119.
- Tolles, J. and Luong, T. (2020). Modeling epidemics with compartmental models. *JAMA*, 323:2515–2516.
- van den Driessche, P. and Watmough, J. (2002). Reproduction numbers and sub threshold endemic equilibria for compartmental models of disease transmission. *Math- ematical Biosciences*, 180:29–48.
- van Kessel, P. and Quinn, D. (2020). Both Republicans and Democrats cite masks as
 a negative effect of COVID-19, but for very different reasons. *Pew Research Center*, https://pewrsr.ch/3jHpDT7.
- Verelst, F., Willem, L., and Beutels, P. (2016). Behavioural change models for infectious
 disease transmission: a systematic review (2010–2015). Journal of The Royal Society
 Interface, 13(125):20160820.
- ⁵⁰⁴ Zhang, L., Kong, Y., and Chang, H. (2015). Media use and health behavior in H1N1
- flu crisis: The mediating role of perceived knowledge and fear. Atlantic Journal of Communication, 23(2):67–80.

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507APPENDIX (ONLINE SUPPLEMENT)508Coupled Dynamics of Behavior and Disease509Contagion Among Antagonistic Groups

510 Appendix A. The SIR model with homophily

We extended the SIR model to explore scenarios where individuals assort based on identity, as described in the main text. Here we present some additional analyses of this model.

Figure S1 illustrates that when an infection breaks out in group 1, homophily can delay the outbreak of the epidemic in group 2. Homophily for each group works somewhat synergistically, but the effect is dominated by w_2 . This is because the infection spreads rapidly in a homophilous group 1, and if group 2 is not homophilous its members will rapidly become infected. However, if group 2 is homophilous, its members can avoid the infection for longer, particularly when group 1 is also homophilous.

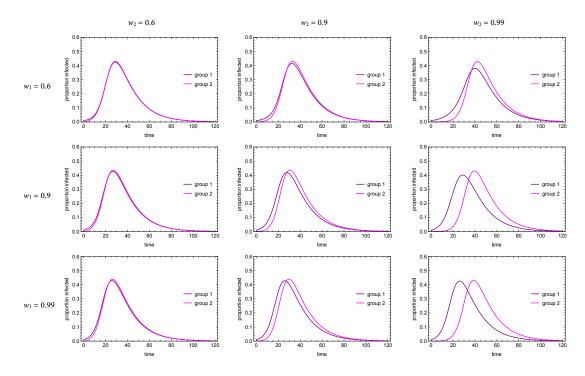


FIGURE S1. Infection dynamics in the SIR model with asymmetric homophily. Here $\tau = 0.3$, $\rho = 0.07$.

We also explored a scenario where R_0 for the basic model was very close to 1, indicating a small epidemic (we used $R_0 = 1.14$; Figure S2). Note that this calculation of R_0 does not account for homophily; we derive R_0 for the homophily model in the SI Appendix and show that this is a reasonable approximation. When homophily was low (w = 0.6), the populations mixed a lot. The proportion of infected individuals in group 1 briefly fell,

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as the majority of new infected individuals were in group 2. However, the groups quickly matched their pace and experienced the outbreak in tandem. When homophily was high (w = 0.99), not only did group 2 experience a delayed outbreak, it also experienced a substantially lower peak infection rate, because the total number of infected individuals at the start of its outbreak was so much lower than that experienced by group 1. Thus, homophily can serve not only to delay an epidemic, but also to reduce it in the cases of lower transmissibility infections.

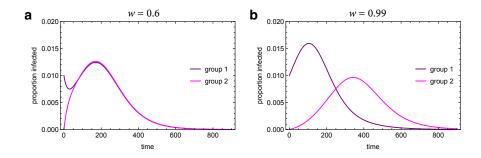


FIGURE S2. Infection dynamics in the SIR model with homophily when R_1 is close to 1. Here $\tau = 0.08$, $\rho = 0.07$, $w_1 = w_2 = w$.

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APPENDIX B. BASIC REPRODUCTION NUMBER

⁵³³ We can calculate the basic reproduction number, R_0 , for the homophily model. We ⁵³⁴ employ the next-generation matrix approach described by Heffernan et al. (2005), which ⁵³⁵ concisely summarizes the ideas for calculating R_0 in structured populations articulated ⁵³⁶ by, e.g., Diekmann et al. (1990) and van den Driessche and Watmough (2002).

Following the notation of Heffernan et al. (2005), the next generation matrix **G** is comprised of two component matrices: F and V^{-1} , where

(1)
$$\boldsymbol{F} = \begin{bmatrix} \frac{\partial F_i(x_0)}{\partial x_j} \end{bmatrix},$$

539 and

(2)
$$\boldsymbol{V} = \begin{bmatrix} \frac{\partial V_i(x_0)}{\partial x_j} \end{bmatrix}.$$

These are square matrices of the partial derivatives of new infections (F_i) and transfers between different compartments (V_i) . The rank of these matrices is the number of distinct classes of infections. x_0 is the disease-free equilibrium state. This matrix should be non-negative, irreducible, and primitive.

is given by the dominant eigenvalue of the matrix $G = FV^{-1}$.

For the homophily model, the only two equations that yield new infections are those for \dot{I}_1 and \dot{I}_2 :

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(3)
$$\frac{dI_1}{dt} = \tau S_1 \left(w_1 I_1 + (1 - w_1) I_2 \right) - \rho I_1$$

(4)
$$\frac{dI_2}{dt} = \tau S_2 \left(w_2 I_2 + (1 - w_2) I_1 \right) - \rho I_2$$

Applying the next-generation-matrix approach described above to these equations, and noting that in the disease-free equilibrium $S_1 + S_2 = 1$, we get the next-generation matrix:

(5)
$$\boldsymbol{G} = \begin{pmatrix} \frac{S_1 \tau w_1}{\rho} & \frac{S_1 \tau (1-w_1)}{\rho} \\ \frac{S_2 \tau (1-w_2)}{\rho} & \frac{S_2 \tau w_2}{\rho} \end{pmatrix}.$$

Letting $S_2 = 1 - S_1$ in the disease-free equilibrium, the larger of the two eigenvalues of this matrix is:

$$(6) \\ R_0 = \frac{\tau}{2\rho} \left(\sqrt{S_1^2 w_1^2 + 2(1-S_1)S_1 w_1 w_2 - 4(1-S_1)S_1 w_1 + (1-S_1)^2 w_2^2 - 4(1-S_1)S_1 w_2 + 4(1-S_1)S_1 + \rho^2 S_1 w_1 + \rho^2 (1-S_1) w_2} \right)$$

This relationship is greatly simplified by assuming uniform homophily $(w_1 = w_2 = w)$:

(7)
$$R_0 = \frac{\tau}{2\rho} (w + \sqrt{S_1^2(8w - 4) + S_1(4 - 8w) + w^2}).$$

Note that if we collapse the structure of the population such that $S_1 = 1$ (which also implies that w = 1), then equation 7 reduces to $R_0 = \tau/\rho$, the standard definition for the basic reproduction number in an unstructured SIR model (Keeling and Rohani, 2007). We see from figure S3 that structure and homophily (in the absence of coupled adaptive behavior and outgroup aversion) are actually somewhat protective from an epidemic

perspective. R_0 is lowest when the population is evenly split between the two groups and when homophily is extreme. This makes sense since structure generally slows epidemics by subdividing the potential for contacts and thereby slowing mixing (Arthur et al., 2017).

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APPENDIX C. COUPLED CONTAGION DYNAMICS

Here we present an extended version of the full model analysis presented in the main text, that includes intermediate homophily of $w_i = 0.9$. Analysis with no outgroup aversion is shown in Figure S4, and with outgroup aversion is shown in Figure S5. The figures illustrate how homophily and outgroup aversion can interact to produce unintuitive dynamics. When both forces are present, an infection that begins in group 1 can peak earlier and stronger in group 2, followed by a smaller peak in the group where it began.

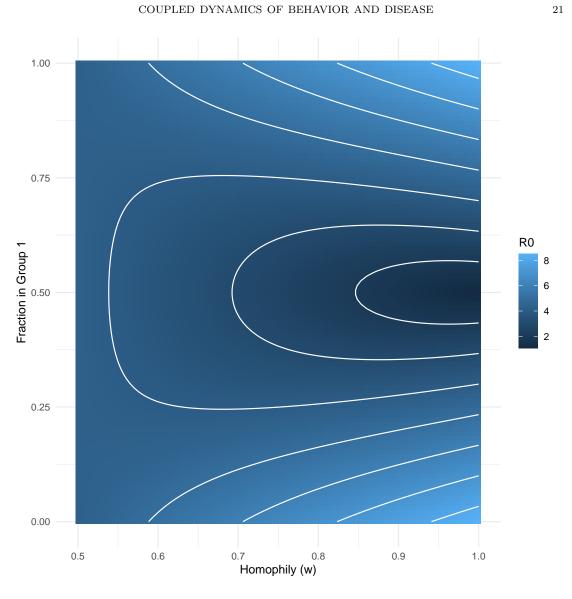


FIGURE S3. R_0 for the uniform-homophily model (Equation 7) as a function of the strength of homophily (w) and the initial population structure. $\tau = 0.3$, $\rho = 0.07$.

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APPENDIX D. ANALYSIS OF BEHAVIORAL EFFICACY

In the main text analysis, we assumed that the adopted behavior reduced the transmission to below the threshold for $R_0 < 1$. In other words, if everyone immediately and universally adopted the behavior at the start of the outbreak, it would not become an epidemic. Although we view this as a reasonable assumption (that is, the efficacy of the

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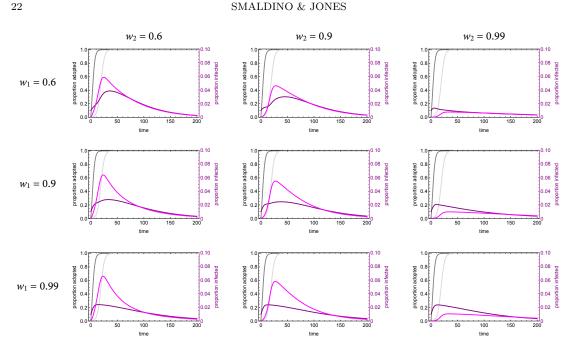
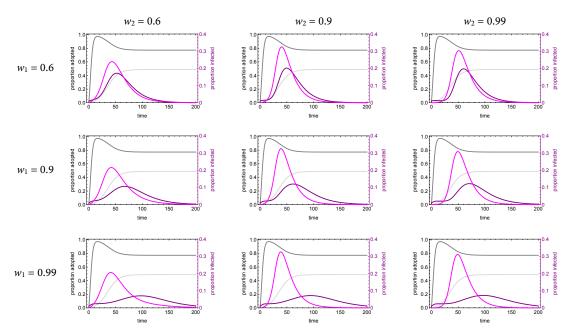


FIGURE S4. Coupled dynamics of the full model without outgroup aversion ($\gamma = 0$) for with varying homophily. Darker lines are group 1, lighter lines are group 2. Parameters used: $\tau_U = 0.3$, $\tau_C = 0.069$, $\rho = 0.07$, $\alpha_2 = 0.1, \, \alpha_2 = 0.001, \, \beta = 0.3, \, \delta = 0.$

behavior is reasonable, not the expectation that it will be either immediately or univer-575 sally adopted), it is also worth examining what happens with the spread of behaviors 576 that reduce transmission, but not below epidemic levels. Figure S6 illustrates the model 577 dynamics for varying levels of behavior efficacy (τ_C) with and without outgroup aversion 578 and for both weak and strong homophily. 579

Without outgroup aversion ($\gamma = 0$), the effect is clear: the more efficacious the behav-580 ior, the smaller the epidemic. This occurs because the behavior spreads effectively. With outgroup aversion, two things happen. First, the more effectively the behavior reduces 582 transmission (that is, the smaller τ_C is), the smaller the overall epidemic, but with an 583 effect that is much stronger in group 1. In group 2, the effect of increased behavior 584 efficacy is relatively small, because adoption is reduced and delayed. Second, the better the behavior reduces transmission, the bigger the delay in when group 1 experiences a 586 "second wave." This illustrates that the dynamics of disease transmission can become 587 quite complex when even simple assumptions about behavior and group structure are considered.



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FIGURE S5. Coupled dynamics of the full model with outgroup aversion $(\gamma = 0.2)$ for with varying homophily. Darker lines are group 1, lighter lines are group 2. Parameters used: $\tau_U = 0.3$, $\tau_C = 0.069$, $\rho = 0.07$, $\alpha_2 = 0.1$, $\alpha_2 = 0.001$, $\beta = 0.3$, $\delta = 0$.

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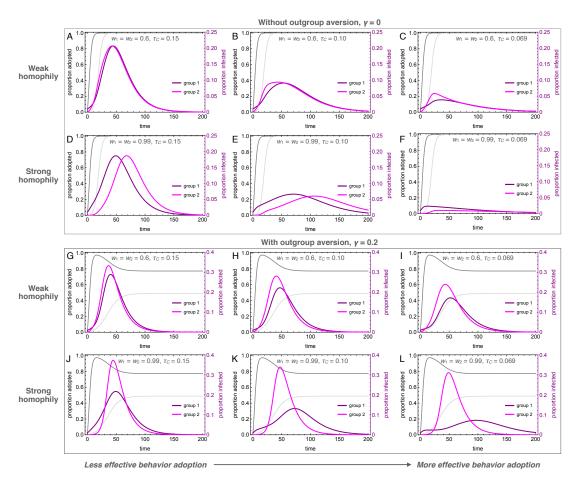


FIGURE S6. Coupled dynamics of the full model for varying levels of behavior efficacy, $\tau_C = \{0.15, 0.1, 0.069\}$, where only the last case would provide $R_0 < 1$ if immediately and universally adopted at the start of the outbreak. We provide analyses with and without outgroup aversion and for both weak and strong homophily. Darker lines are group 1, lighter lines are group 2. Parameters used: $\tau_U = 0.3$, $\rho = 0.07$, $\alpha_2 = 0.1$, $\alpha_2 = 0.001$, $\beta = 0.3$, $\delta = 0$.