

1                    **Neural Flip-Flops II: Short-Term Memory and**  
2                    **Electroencephalography**

3    Lane Yoder

4    Department of Science and Mathematics, retired

5    University of Hawaii, Kapiolani

6    Honolulu, Hawaii

7    [LYoder@hawaii.edu](mailto:LYoder@hawaii.edu)

8    [NeuralNanoNetworks.com](http://NeuralNanoNetworks.com)

## 9 **Abstract**

10 For certain brain functions, the theoretical networks presented here almost certainly show  
11 how neurons are actually connected. Stripped of details such as redundancies and other error-  
12 correcting mechanisms, the basic organization of synaptic connections within some of the brain's  
13 building blocks is likely to be less complex than it appears. For some brain functions, the  
14 network architectures can even be quite simple.

15 Flip-flops are the basic building blocks of sequential logic systems. Certain flip-flops can  
16 be configured to function as oscillators. The flip-flops and oscillators proposed here are  
17 composed of two to six neurons, and their operation depends only on minimal neuron  
18 capabilities of excitation and inhibition. These networks suggest a resolution to the longstanding  
19 controversy of whether short-term memory depends on neurons firing persistently or in brief,  
20 coordinated bursts. Oscillators can also generate major phenomena of electroencephalography.

21 For example, cascaded oscillators can produce the periodic activity commonly known as  
22 brainwaves by enabling the state changes of many neural structures simultaneously. (The  
23 function of such oscillator-induced synchronization in information processing systems is timing  
24 error avoidance.) Then the boundary separating the alpha and beta frequency bands is

$$25 \quad 125/\{\mu_d + \sqrt{[(\mu_d)^2 + (\sigma_d)^2 \ln(4)]}\} \text{ hertz,}$$

26 where  $\mu_d$  and  $\sigma_d$  are the mean and standard deviation (in milliseconds) of delay times of neurons  
27 that make up the initial oscillators in the cascades. With 4 and 1.5 ms being the best estimates  
28 for  $\mu_d$  and  $\sigma_d$ , respectively, this predicted boundary value is 14.9 Hz, which is within the range of  
29 commonly cited estimates obtained empirically from electroencephalograms (EEGs). The delay  
30 parameters  $\mu_d = 4$  and  $\sigma_d = 1.5$  also make predictions of the peaks and other boundaries of the  
31 five major EEG frequency bands that agree well with empirically estimated values.

32 The hypothesis that cascaded oscillators produce EEG frequencies implies two EEG  
33 characteristics with no apparent function: The EEG gamma band has the same distribution of  
34 frequencies as three-neuron ring oscillators, and the ratios of peaks and boundaries of the major  
35 EEG bands are powers of two. These anomalous properties make it implausible that EEG  
36 phenomena are produced by a mechanism that is fundamentally different from cascaded  
37 oscillators.

38 The cascaded oscillators hypothesis is supported by the available data for neuron delay  
39 times and EEG frequencies; the micro-level explanations of macro-level phenomena; the  
40 number, diversity, and precision of predictions of EEG phenomena; the simplicity of the  
41 oscillators and minimal required neuron capabilities; the selective advantage of timing error  
42 avoidance that cascaded oscillators can provide; and the implausibility of a fundamentally  
43 different mechanism producing the phenomena.

44 The available data are too imprecise for a rigorous statistical test of the cascaded  
45 oscillators hypothesis. A simple, rigorous test of the hypothesis is suggested. The neuron delay  
46 parameters  $\mu_d$  and  $\sigma_d$ , as well as the mean and variance of the periods of one or more EEG bands,  
47 can be estimated from random samples. With standard tests for equal means and variances, the  
48 EEG sample statistics can be compared to the EEG parameters predicted by the delay time  
49 statistics.

50 **Key words:** flip-flop; short-term memory; oscillator; cascaded oscillator;  
51 electroencephalogram; EEG; electroencephalography; brainwave; neuronal network; neural  
52 network; neural correlate; working memory; neural logic circuit; JK flip-flop; toggle; explicit  
53 neural model; bursting neuron; color vision; olfaction; central pattern generator; CPG

## 54 **1. Introduction**

55           This article is the fifth in a series of articles that show how neurons can be connected to  
56 process information. The first three articles [1-3] showed that a neural fuzzy logic decoder can  
57 produce the major phenomena of olfaction and [color vision](#). The fourth article [4] showed that  
58 neurons can be connected to form robust neural flip-flops (NFFs) that can generate the major  
59 phenomena of short-term memory. Some of this material will be reviewed and used here.

60           In the present article, an additional NFF is presented. The design of this NFF, as well as  
61 the NFF designs in [4], are modifications of standard electronic logic circuit designs. The  
62 modifications are necessary to implement the circuits with neurons. The rest of this article's  
63 network designs are straightforward engineering: The new NFF can be configured to function as  
64 a toggle (a flip-flop with one input that inverts the memory state). An odd number of inverters  
65 connected in a circular sequence forms a ring oscillator. (It was shown in [2] that a neuron can  
66 function as a logic inverter. This will be reviewed here.) An oscillator connected in sequence  
67 with several toggles forms a cascade of oscillators with different frequencies. An oscillator can  
68 synchronize state changes in other networks by enabling them simultaneously. The cascaded  
69 oscillators' properties and robust operation are demonstrated by simulation, but the properties can  
70 be proven directly from the explicit network connections and minimal neuron properties of  
71 excitation and inhibition.

72           The *cascaded oscillators hypothesis* states that the brain structures' matched periods of  
73 neural activity that are found in EEGs are the result of the structures' synchronization by  
74 cascades of neural oscillators. The main implication of the hypothesis is that the EEG bands  
75 have the same distributions of frequencies as the cascaded oscillators. All EEG phenomena  
76 predicted by the hypothesis follow from this one implication. It will be shown here that  
77 cascaded oscillators' frequency distributions are determined by just two parameters: the mean  
78 and variance of the delay times of neurons that make up the initial oscillators in the cascades.

79 With this property and samples of neuron delay times and EEG frequencies, the main implication  
80 of the cascaded oscillators hypothesis can be tested simply and rigorously.

81 Many neuroscientists believe that the specific connectivity of the brain largely determines  
82 how information is processed, and that the brain's connectivity is one of the major open  
83 questions in biology [5]. Little progress has been made in this area, possibly because a way  
84 forward is not apparent. Many of the efforts to find connections between neuroscience and  
85 artificial neural networks have been attempts to apply "brain-like" networks to artificial  
86 intelligence and machine learning. One of the main problems with this approach has been the  
87 lack of an accurate model of how the brain works [6].

88 This situation could change. Recognizing a neuron's simple logic capability makes a  
89 useful connection between neuroscience and the field of logic circuit design in electronic  
90 computational systems. It was shown in [2] that a neuron with excitatory and inhibitory input  
91 can operate as a functionally complete logic primitive, meaning any logic function can be  
92 performed by a network of such components. As demonstrated here and in [1-4], neuroscience  
93 and logic circuit design can inform each other in how certain simple functions can be performed.  
94 For higher-level cognitive functions, the methods of the brain and artificial intelligence are  
95 currently vastly different. However, complex systems can consist of simple building blocks.  
96 With the recognition that the two systems are likely to have similar logical design and essentially  
97 the same building blocks, neuroscience and computer science may inform each other from the  
98 ground up.

## 99 **2. DEEP neural networks**

100 The neural networks proposed here and in [1-4] are dynamic, explicit, evolutionary, and  
101 predictive (DEEP). The networks' dynamic operation means the only changes are the levels of  
102 neuron activity. No structural change is required, such as neurogenesis, synaptogenesis, or  
103 pruning, nor is any change required in the way neurons function, such as a change in synaptic

104 strength or the strength of action potentials. All neurons, connections, and types of synapses are  
105 shown explicitly, and all assumptions of neuron capabilities are stated explicitly. Only minimal  
106 neuron capabilities are assumed, and no network capabilities are assumed. The networks are  
107 evolutionary in the sense that they demonstrate selective advantages for at least some of the  
108 phenomena they generate. This includes phenomena whose functions are apparently uncertain,  
109 such as the matched periods of neural activity found in EEGs. Finally, the networks are  
110 predictive of nervous system phenomena. That is, based on the explicit connections and neuron  
111 capabilities, it can be demonstrated that the models generate known nervous system phenomena,  
112 and they may make testable predictions of phenomena that are as yet unknown.

113 For most brain functions, the four DEEP properties are necessary for a model to show  
114 how neurons are actually connected. The dynamic operation makes the network's speed  
115 consistent with the "real time" of most brain functions (a few milliseconds). Explicitness means  
116 the model is transparent, as opposed to a "black box" to which any property may be assigned.  
117 An evolutionary model performs a useful function, as opposed to an ad hoc model that is  
118 designed to produce a known phenomena without any apparent utility. A realistic model must  
119 predict phenomena.

120 The dual purpose of this article is to call attention to the dearth of DEEP models in the  
121 literature and to demonstrate that it is possible to design DEEP neural networks. DEEP models  
122 are needed to make progress in discovering how synaptic connections are organized at the local  
123 level.

### 124 **3. Unexplained phenomena and alternative models**

125 There is no consensus on the brain's organization of synaptic connections at the local  
126 level. Consequently, many brain phenomena lack explicit explanations.

### 127 **3.1. Short-term memory: persistent firing or brief, coordinated bursts?**

128 Memory tests have shown that certain neurons fire continuously at a high frequency  
129 while information is held in short-term memory. These neurons exhibit seven characteristics  
130 associated with memory formation, retention, retrieval, termination, and errors. One of the  
131 neurons in the NFFs proposed in [4] was shown to produce all of the characteristics.

132 In addition to neurons firing persistently, other neurons firing in brief, coordinated bursts  
133 are also associated with short-term memory [7]. Which of these two phenomena actually  
134 produces short-term memory has been a longstanding controversy [7, 8]. Neural oscillators and  
135 NFFs together suggest a resolution to this issue.

### 136 **3.2. Electroencephalograms**

#### 137 **3.2.1. EEG phenomena and previous models**

138 Electroencephalograms show widespread rhythms that consist of many neurons firing  
139 with matched periods. The spectrum of frequencies has been partitioned into bands according to  
140 the behavioral and mental state associated with the frequencies in each band. Five EEG  
141 frequency bands are considered here: gamma, beta, alpha, theta, and delta. Some researchers  
142 have found more bands or divided the bands into sub-bands depending on the focus of their  
143 research, but these five are discussed most often in the literature.

144 The distribution of frequencies within each of these bands is unimodal [9-12]. The ratios  
145 of consecutive band boundaries [13] and the ratios of consecutive band peak frequencies [9-12]  
146 are approximately 2. The gamma band peaks at about 40 Hz [9-12], although it contains  
147 frequencies of 100 Hz or more [14, 15]. Several estimated frequencies have been found for each  
148 boundary between bands.

149           The EEG phenomena raise several questions. What produces the widespread,  
150           synchronized, periodic firing? What is the function of this widespread synchronization? What  
151           produces and what is the function of the wide distribution of EEG frequencies in bands? What  
152           produces the unimodal distribution in each band and the octave relationships between the peaks  
153           and boundaries? What determines the specific frequencies of the peaks and boundaries? Why  
154           do gamma oscillations peak at about 40 Hz? Why does the gamma band contain frequencies that  
155           are considerably faster than 40 Hz? Why is there little agreement on the boundaries separating  
156           the EEG bands?

157           Answers to a few of these questions have been proposed, but there has been no explicit  
158           model that can explain more than one or two phenomena. Most models are based on "black box"  
159           networks or broad assumptions of neuron capabilities. Below are two prominent examples of  
160           proposed oscillator models.

161           Pacemaker cells are natural oscillators that cause involuntary muscles and other tissues to  
162           contract or dilate. They are spontaneously active neurons with a specialized cell membrane that  
163           allows sodium and potassium to cross and generate regular, slow action potentials (around 100  
164           spikes per minute) [16, 17]. Modulating input controls the spike frequency. Except for  
165           generating periodic signals, pacemaker cells do not offer answers to any of the questions above.  
166           It is not clear, for example, how pacemaker cells could generate the wide distribution of EEG  
167           frequencies, their unimodal distribution in bands, or the octave relationships of the bands. Also a  
168           single spike would not be a good enabler of state changes because the duration of an enabling  
169           input needs to be long enough to overlap the input that is being enabled.

170           The Kuramoto model [18] provides a widely accepted explanation of synchronized firing  
171           found in EEGs. The model assumes, without supporting evidence and without an explanation of  
172           a mechanism or function for any of these behaviors, that the neurons' signals oscillate naturally,  
173           that these oscillations are nearly identical, and that each neuron is linked to all the others. The



174 model does not appear to answer any of the above questions besides how synchronization occurs.  
175 The model is a macro-level explanation of a macro-level phenomenon. The EEG data are quite  
176 distant from the micro-level explanation given here based on neuron delay times.

177 The cascaded oscillators model proposed here can produce the synchronized firing found  
178 in EEGs by enabling neural structures' state changes simultaneously. It will be shown that the  
179 model provides answers to all of the questions above.

### 180 **3.2.2. Implausibility of alternative mechanisms**

181 A natural question is whether the EEG phenomena listed above are actually produced by  
182 a mechanism or mechanisms that are fundamentally different from the cascaded oscillators  
183 proposed here. This is unlikely for at least three reasons.

184 First, it is unlikely that another mechanism that could produce all of the EEG phenomena  
185 would be as simple as cascaded oscillators. Only two types of simple networks are required: a  
186 three-neuron ring oscillator and a six-neuron NFF. The neurons require no special capabilities  
187 other than excitation and inhibition. Second, nature has limits. Besides limitations on neuron  
188 capabilities, evolutionary changes proceed in incremental steps with selective improvements at  
189 each step. Even if all of the phenomena could be generated by a different mechanism, evolution  
190 may not be able to produce it.

191 Perhaps most importantly, even if evolution could produce another mechanism that  
192 generates the phenomena, selective pressure to do so is unlikely. Cascaded oscillators are a  
193 possible response to two specific selective pressures. As side effects, cascaded oscillators imply  
194 two anomalous characteristics of EEG frequencies that have no apparent function.

195 Toggles connected in sequence to function as oscillators are a possible response to a  
196 selective pressure for a wide variety of frequencies in the trade-off between speed and accuracy  
197 in processing different kinds of information. This would produce the octave relationship that has

198 been observed between EEG frequency bands. There is no apparent selective advantage in  
199 distributions of frequencies with an octave relationship. If a mechanism other than cascaded  
200 toggles evolved to produce oscillations with a wide variety of frequencies, it is unlikely that the  
201 frequencies would be distributed in bands with the octave relationship.

202 Similarly, a three-neuron ring oscillator as the cascade's initial oscillator is a possible  
203 response to a selective pressure for some information to be processed as fast as possible. This  
204 implies the EEG gamma band has the same distribution of frequencies as three-neuron ring  
205 oscillators. As shown below, that distribution in the gamma band is consistent with available  
206 data. There is no apparent selective advantage in that particular distribution of frequencies. If a  
207 different mechanism evolved to produce fast oscillations, it would be unlikely to have the same  
208 distribution of frequencies as three-neuron ring oscillators.

#### 209 **4. Simulation methods**

210 The cascaded oscillators were simulated in MS Excel. For this simulation, the number  $t_i$   
211 represents the time after  $i$  neuron delay times. The neurons' outputs are initialized in a stable  
212 state at time  $t_0 = 0$ . For  $i > 0$ , the output of each neuron at time  $t_i$  is computed as a function of the  
213 inputs at time  $t_{i-1}$ . Specific probabilities of unusually large gamma band frequencies were  
214 approximated numerically from the initial oscillator's estimated frequency PDF with Converge  
215 10.0, although this could also be done with a substitution of  $u = 1,000/x$  to convert the frequency  
216 PDF to a normal distribution of periods.

#### 217 **5. Analysis**

##### 218 **5.1. Neuron signals**

219 This section summarizes part of [4] that will be used here.

### 220 **5.1.1. Binary neuron signals**

221 Neuron signal strength, or intensity, is normalized here by dividing it by the maximum  
222 possible intensity for the given level of adaptation. This puts intensities in the interval from 0 to  
223 1, with 0 meaning no signal and 1 meaning the maximum intensity. The normalized number is  
224 called the *response intensity* or simply the *response* of the neuron. Normalization is only for  
225 convenience. Non-normalized signal strengths, with the highest and lowest values labeled Max  
226 & Min rather than 1 and 0, would do as well. The responses 1 and 0 are collectively referred to  
227 as binary signals and separately as high and low signals. If 1 and 0 stand for the truth values  
228 TRUE and FALSE, neurons can process information contained in neural signals by functioning  
229 as logic operators.

230 The strength of a signal consisting of action potentials, or spikes, can be measured by  
231 spike frequency. A high signal consists of a burst of spikes at the maximum spiking rate. For a  
232 signal that oscillates between high and low, the frequency of the oscillation is the frequency of  
233 bursts, not the frequency of spikes.

234 For binary signals, the response of a neuron with one excitatory and one inhibitory input  
235 is assumed to be as shown in Table 1.  
236

Excitatory X	Inhibitory Y	Response
0	0	0
0	1	0
1	0	1
1	1	0

237 **Table 1. Neuron response to binary inputs.** Of the 16 possible binary functions of two  
238 variables, this table represents the only one that is consistent with the customary meanings of  
239 "excitation" and "inhibition." Table 1 is also a logic truth table, with the last column  
240 representing the truth values of the statement X AND NOT Y.

241 The networks presented here require continuous, high input. In the figures, this input is  
242 represented by the logic value "TRUE." For an electronic logic circuit, the high input is  
243 normally provided by the power supply. If the components represent neurons, the high input can  
244 be achieved by neurons in at least four ways. 1) A continuously high signal could be provided  
245 by a neuron that has excitatory inputs from many neurons that fire independently [19]. 2) The  
246 brain has many neurons that are active spontaneously and continuously without excitatory input  
247 [20, 21]. A network neuron that requires a high excitatory input could receive it from a  
248 spontaneously active neuron, or 3) the neuron itself could be spontaneously active. 4) The high  
249 input could be provided by one of a flip-flop's outputs that is continuously high.

### 250 **5.1.2. Additive noise in binary neuron signals**

251 All binary results for the networks presented here follow from the neuron response in  
252 Table 1. Analog signals (intermediate strengths between high and low) were considered in [4]  
253 only to show how the NFFs in the figures can generate robust binary signals in the presence of  
254 moderate levels of additive noise in binary inputs. The NFF simulation in [4] will not be  
255 repeated here, but the same noise-reducing neuron response function will be used in the cascaded

256 oscillators simulation with additive noise. This function and the minimal conditions for adequate  
257 noise reduction will be reviewed briefly in this section.

### 258 **5.1.2.1. Noise reduction**

259 Reduction of noise in both excitatory and inhibitory inputs can be achieved by a response  
260 function of two variables that generalizes a sigmoid function's noise reducing features. The  
261 noise reduction need only be slight because the proposed NFFs have feedback loops that  
262 continually reduce the effect of noise.

263 Let  $F(X, Y)$  represent a neuron's response to an excitatory input  $X$  and an inhibitory input  
264  $Y$ . The function must be bounded by 0 and 1, the minimum and maximum possible neuron  
265 responses, and must satisfy the values in Table 1 for binary inputs. For other points  $(X, Y)$  in the  
266 unit square, suppose  $F$  satisfies:

- 267 1.  $F(X, Y) > X - Y$  for inputs  $(X, Y)$  near  $(1, 0)$  and
- 268 2.  $F(X, Y) < X - Y$  or  $F(X, Y) = 0$  for inputs  $(X, Y)$  near the other three vertices of the  
269 unit square.

270 Neurons that make up the networks proposed here are assumed to have these minimal noise-  
271 reducing properties.

272 Conditions 1 and 2 are sufficient to suppress moderate levels of additive noise in binary  
273 inputs and produce the NFF results found here. The level of noise that can be tolerated by the  
274 NFFs depends on the regions in the unit square where conditions 1 and 2 hold. If a binary input  
275  $(X, Y)$  has sufficiently large additive noise to change the region in which it lies, an error can  
276 occur.

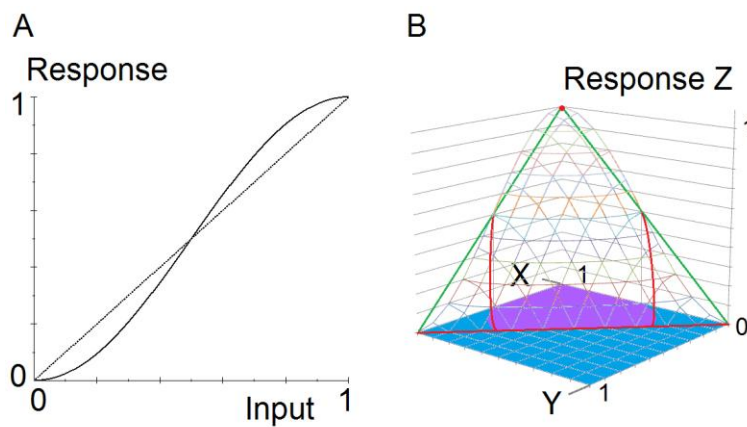
277 **5.1.2.2. Example of a neuron response that satisfies conditions 1 and 2**

278 For any sigmoid function  $f$  from  $f(0) = 0$  to  $f(1) = 1$ , the following function has the noise-  
279 reducing properties 1 and 2 and also satisfies Table 1:

280  $F(X, Y) = f(X) - f(Y)$ , bounded below by 0.

281 The function  $F$  is illustrated in Fig 1 for a specific sigmoid function  $f$ .

282



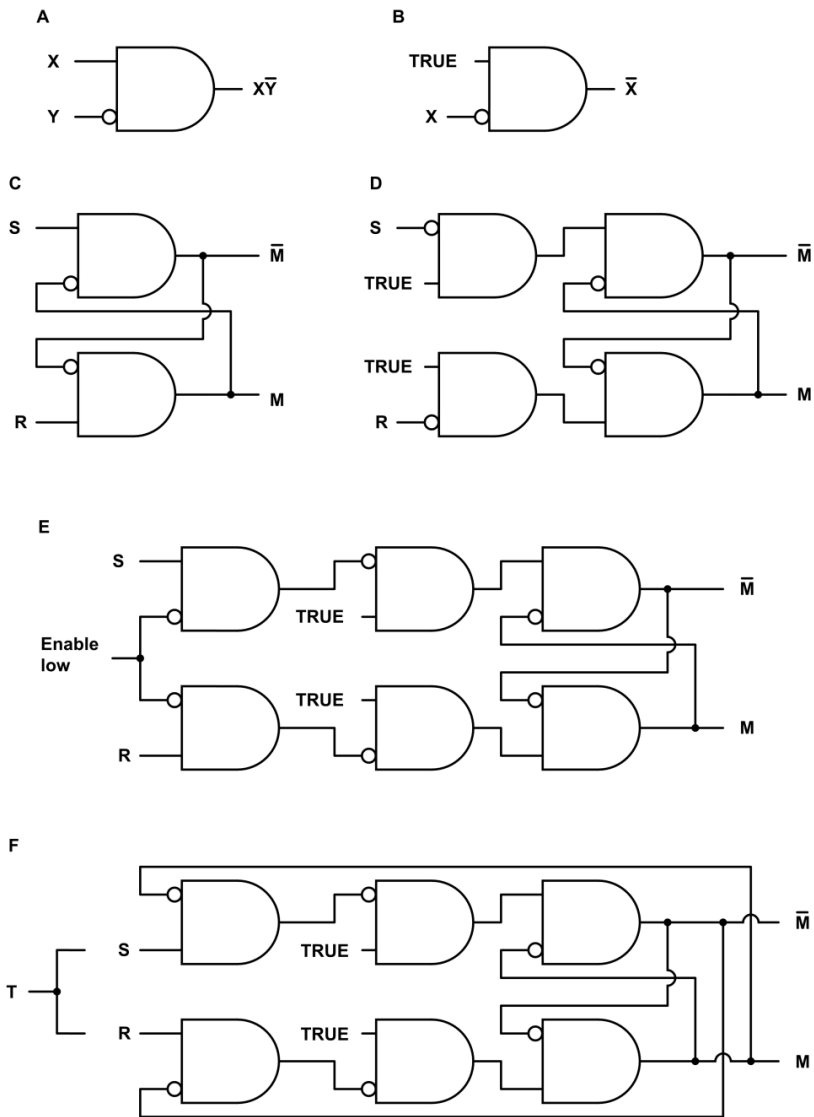
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284 **Fig 1. Noise-reducing AND-NOT function.** The graph shows an example of a neuron  
285 response to analog inputs that reduces moderate levels of additive noise in binary inputs. **A.** A  
286 sigmoid function  $f(x) = (1/2)\sin(\pi(x - 1/2)) + 1/2$ . **B.** Graph of a function that has the noise-  
287 reducing properties 1 and 2. The function is  $F(X, Y) = f(X) - f(Y)$ , bounded by 0. The triangle  
288 lies in the plane  $Z = X - Y$ . The approximate intersection of the plane and the graph of the  
289 response function  $F$  is shown in red. The purple and blue regions in the unit square show  
290 approximately where conditions 1 and 2 hold, respectively.

291 **5.2. Neural logic gates and flip-flops**

292 For several reasons that were detailed in [4], the neural networks in the figures are  
293 illustrated with standard (ANSI/IEEE) logic symbols rather than symbols commonly used in  
294 neuroscience schematic diagrams. One of the reasons is that the symbols can be interpreted in

295 two ways. As a logic symbol, the rectangle with one rounded side in Fig 2A represents the AND  
296 logic function, and the circle represents negation. The input variables X and Y represent truth  
297 values TRUE or FALSE, and the output represents the truth value X AND NOT Y. Second, Fig  
298 2A can also represent a single neuron, with a circle representing inhibitory input and no circle  
299 representing excitatory input. If X and Y are binary inputs, the output is X AND NOT Y by  
300 Table 1. Fig 2B shows that an AND-NOT gate with a continuously high input functions as a  
301 NOT gate, or inverter.  
302



303

304 **Fig 2. Neural logic gates and flip-flops.** **A.** A symbol for an AND-NOT logic gate, with output  
 305 X AND NOT Y. The symbol can also represent a neuron with one excitatory input and one  
 306 inhibitory input. **B.** An AND-NOT gate configured as a NOT gate, or inverter. **C.** An active low  
 307 Set-Reset (SR) flip-flop. **D.** An active high SR flip-flop. **E.** An active high SR flip-flop enabled  
 308 by input from an oscillator. **F.** A JK flip-flop or toggle. If S and R are high simultaneously, the  
 309 flip-flop is inverted.

310 A flip-flop stores a discrete bit of information in an output with values usually labeled 0  
 311 and 1. This output variable is labeled M in Fig 2. The value of M is the flip-flop *state* or *memory*



312 *bit*. The information is stored by means of a brief input signal that activates or inactivates the  
313 memory bit. Input S *sets* the state to  $M = 1$ , and R *resets* it to  $M = 0$ . Continual feedback  
314 maintains a stable state. A change in the state *inverts* the state.

315 Two basic types of flip-flops are the Set-Reset (SR) and JK. Fig 2C shows an active low  
316 SR flip-flop. The S and R inputs are normally high. A brief low input S sets the memory bit M  
317 to 1, and a brief low input R resets it to 0. Adding inverters to the inputs produces the active  
318 high SR flip-flop of Fig 2D. The S and R inputs are normally low. A brief high input S sets the  
319 memory bit M to 1, and a brief high input R resets it to 0. The NFF in Fig 2D was simulated in  
320 [4].

321 Fig 2E shows a flip-flop with an enabling input. The S and R inputs in Fig 2D have been  
322 replaced by AND-NOT gates that allow the S or R input to be transmitted only when the  
323 enabling input is low. In synchronized signaling systems, various logic circuits are enabled  
324 simultaneously by an oscillator to avoid timing errors.

325 For the so-called JK flip-flop in Fig 2F, the enabling input in Fig 2E has been replaced by  
326 input from the flip-flop outputs. A disadvantage of the SR flip-flop is that if S and R are  
327 activating simultaneously, the outputs are unpredictable. The advantage of the JK flip-flop is  
328 that if S and R are both high simultaneously, the flip-flop state is inverted because the most  
329 recent inverting input is inhibited by one of the outputs. This means the JK flip-flop can be  
330 configured as a toggle by linking the Set and Reset inputs, as illustrated by the single input T in  
331 the figure.

332 A problem with the JK toggle is that it functions correctly only for a short duration of  
333 high input. If the duration is too long, the outputs will oscillate. This problem is handled in the  
334 oscillators section below.

### 335 **5.3. Neural oscillators**

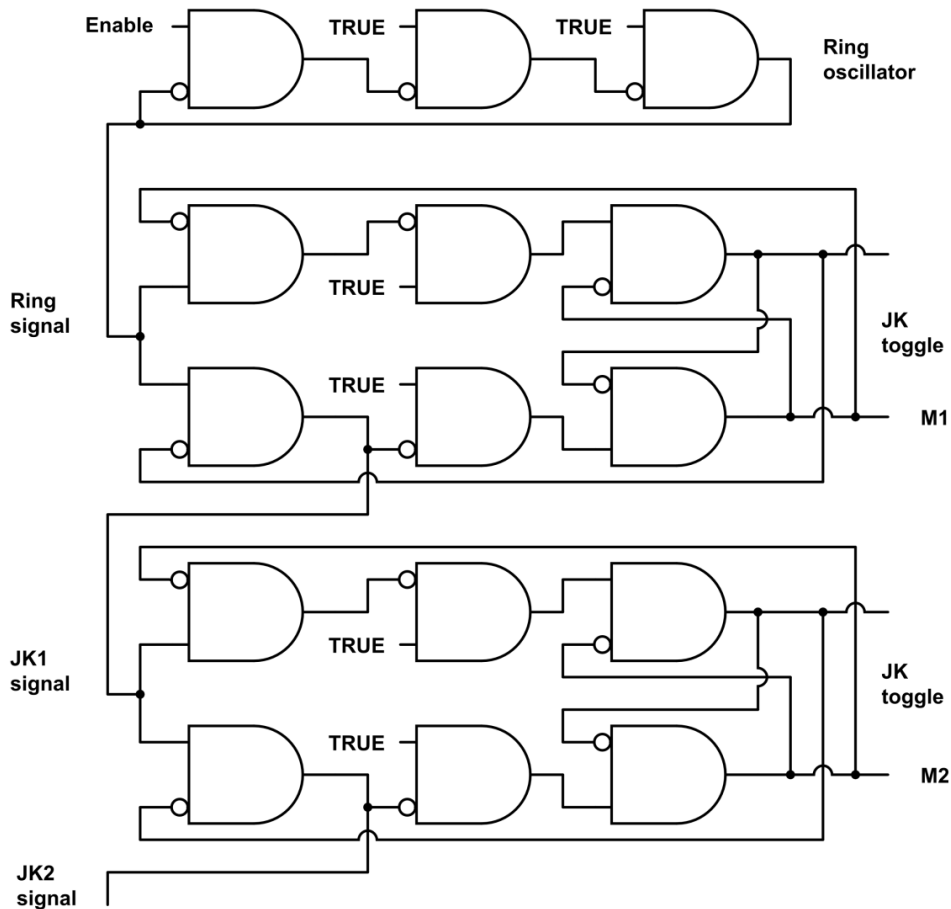
#### 336 **5.3.1. Neural ring oscillators and toggles**

337 An oscillator produces periodic bursts of a high signal followed a quiescent period of a  
338 low signal. It is the basic element of a timing mechanism. An odd number of three or more  
339 inverters connected sequentially in a ring produces periodic bursts as each gate inverts the next  
340 one. The odd number of inverters makes all of the inverter states unstable, so the states oscillate  
341 between high and low. All inverters in the ring produce oscillations with the same frequency.  
342 Their phases are approximately uniformly distributed over one cycle, and the high and low signal  
343 durations are approximately equal. Their common period is twice the sum of the inverters' delay  
344 times. (The sum is doubled because each component inverts twice per cycle.) A ring oscillator  
345 is the simplest type of oscillator implemented with logic gates, and the simplest (and fastest) ring  
346 oscillator consists of three inverters. One inverter is not enough to form a ring oscillator because  
347 the output does not have time to fully invert as it is also the input.

348 As described in the introduction, an oscillator can be connected in sequence with toggles  
349 to form a cascade of oscillators. Because two high inputs are required for each cycle of a toggle-  
350 as-oscillator (one to set the memory state, another to reset it), a toggle produces a signal whose  
351 period is exactly double that of the toggle's input.

352 The master-slave toggle is the customary choice for cascaded oscillators because of its  
353 ability to invert no more than once regardless of the high input duration. The master-slave toggle  
354 can be implemented with neurons by connecting two JK toggles in the standard way. However,  
355 the problem of JK toggles inverting more than once with a long high input can be resolved by  
356 using an early output in the JK toggle's signal pathway as the input to the next toggle. The JK  
357 toggle's two initial neurons have the same pulse duration as the toggle's input. This means an  
358 entire cascade can be composed of a ring oscillator and JK toggles, which require half as many

359 components as master-slave toggles. This configuration is illustrated in Fig 3. The use of JK  
360 toggles as cascaded oscillators may be new to engineering.

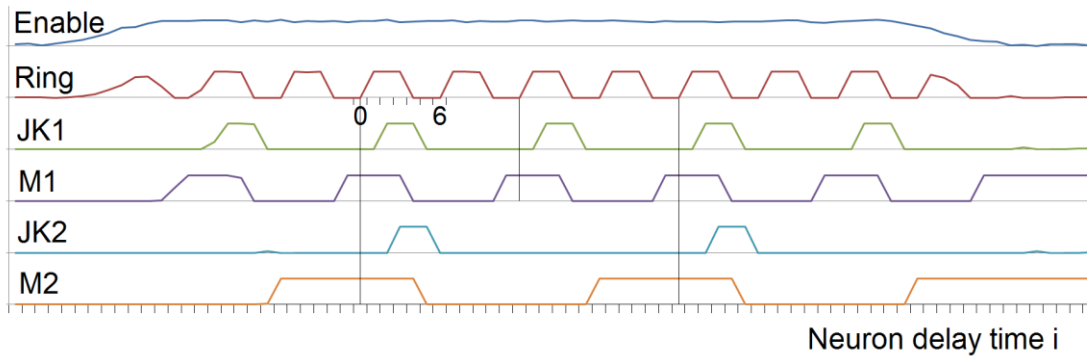


361  
362 **Fig 3. Three cascaded neural oscillators.** The cascade consists of a ring oscillator followed by  
363 two JK toggles connected in sequence. The ring oscillator is composed of three inverters of Fig  
364 2B, with an enabling first input. The toggles are as in Fig 2F. The input to each toggle comes  
365 from one of the first gates in the previous toggle so that the duration of the high signal remains  
366 the same throughout the cascade.

### 367 5.3.2. Cascaded neural oscillators simulation

368 A simulation of the cascaded oscillators in Fig 3 is shown in Fig 4. The simulation was  
369 done in MS Excel.

### Cascaded oscillators signal strengths



370

371 **Fig 4. Simulation of three cascaded neural oscillators.** The simulation of the cascaded  
 372 oscillators in Fig 3 illustrates the main properties of cascaded oscillators: The period of the ring  
 373 oscillator's signal is twice the sum of three neuron delay times. In each toggle, the period of  
 374 every neuron's output is twice the period of the toggle's input. The pulse duration of each  
 375 toggle's two initial neurons is the same as the pulse duration of the toggle's input. Using one of  
 376 these signals as input to the next JK toggle in the cascade prevents it from inverting more than  
 377 once during the input's cycle. The effect of the moderate additive noise in the high inputs to all  
 378 seven inverters is negligible due to the neurons' noise reducing response.

379 The response function  $F(X, Y)$  in Fig 1 was used for the cascaded oscillator simulation as  
 380 follows. The number  $t_i$  represents the time after  $i$  neuron delay times. The neurons' outputs are  
 381 initialized in a stable state at time  $t_0 = 0$ . At time  $t_i$  for  $i > 0$ , the output  $Z_i$  of each neuron that has  
 382 excitatory and inhibitory inputs  $X_{i-1}$  and  $Y_{i-1}$  at time  $t_{i-1}$  is:

$$383 \quad Z_i = F(X_{i-1}, Y_{i-1}) = \max\{0, [(1/2)\sin(\pi(X_{i-1} - 1/2)) + 1/2] - [(1/2)\sin(\pi(Y_{i-1} - 1/2)) + 1/2]\}.$$

384 Additive noise at each time  $t_i$  is simulated by a random number uniformly distributed  
 385 between 0 and 0.1. The Enabling input begins as baseline noise and transitions between 0 and 1  
 386 as a sine function plus noise. During the interval when the Enabling input is high, it is 1 minus  
 387 noise. All six TRUE inputs in Fig 3 are simulated as 1 minus noise. The noise is independent  
 388 for each time  $t_i$  and each input.

## 389 **5.4. Distributions of neuron delay times and cascaded neural oscillators' frequencies**

390 The distributions of cascaded neural oscillators' frequencies are determined by the mean  
391 and variance of neuron delay times of the cascades' initial oscillators.

### 392 **5.4.1. Exact relationships between inverter delay times and cascaded oscillator frequencies**

393 The interest here is in neural inverters and toggles, but the arguments in this section apply  
394 to any implementation of inverters and toggles, including electronic. These results may not be  
395 found in electronics texts because engineers are not normally concerned with the small variances  
396 in component performance.

#### 397 **5.4.1.1. Distributions of oscillator periods and frequencies**

398 As noted earlier, each cycle time of a ring oscillator is the sum of the times it takes for  
399 each inverter to invert twice. If  $X_1, \dots, X_n$  are independent and identically distributed random  
400 variables representing the delay times of  $n$  inverters in a ring oscillator, the ring oscillator's  
401 period is:

$$402 \quad 3. \quad P = 2(X_1 + \dots + X_n)$$

403 If toggles are connected in sequence with the oscillator, each cycle time of each toggle's output is  
404 the sum of two of the input's cycle times. Cascaded toggle number  $k = 1, 2, \dots$  has period:

$$405 \quad 4. \quad P_k = 2^k P$$

406 The mean and standard deviation of the delay times of inverters in ring oscillators are  
407 denoted by  $\mu_d$  and  $\sigma_d$ . By equations 3 and 4 and the elementary properties of random variables,  
408 for  $i = 1, 2, \dots$  (with  $i = 1$  representing the initial ring oscillator), the period of cascaded  
409 oscillator number  $i$  has mean and standard deviation:

$$410 \quad 5. \quad \mu_i = 2^i n \mu_d, \quad \sigma_i = 2^i \sqrt{n} \sigma_d$$

411 The factor  $2^i$  shows the octave relationship between the oscillators' distributions of periods.

412 The oscillators' distributions of frequencies can be derived from the distributions of  
413 periods by straightforward calculus. If periods and frequencies are measured in milliseconds and  
414 hertz, respectively, then frequency =  $k/\text{period}$  for  $k = 1,000$ . If the probability density function  
415 (PDF) of the period of oscillator  $i = 1, 2, \dots$  ( $i = 1$  representing the initial ring oscillator) is  $f_i(x)$ ,  
416 then the PDF of the frequency of oscillator  $i$  is:

417 6.  $g_i(x) = kf_i(k/x)/x^2$

418 Equation 6 shows the oscillator period and frequency distributions are different. For  
419 example, it will be seen that if the periods are normally distributed, the frequency distributions  
420 are skewed to the right. But the intersections of consecutive period PDFs (converted to  
421 frequencies) are the same as the intersections of consecutive frequency PDFs because  $x^2$  and the  
422 initial constant  $k$  in equation 6 drop out of the equation  $g_i(x) = g_{i+1}(x)$ .

#### 423 **5.4.1.2. Normal distributions**

424 If inverter delay times are normally distributed, then by equations 3 and 4 and the  
425 elementary properties of normal distributions, the periods of ring oscillators and cascaded  
426 toggles are also normally distributed.

427 The normal PDF with mean  $\mu$  and standard deviation  $\sigma$ , whose graph is commonly  
428 known as the bell curve, is:

429 7.  $f(x) = \exp[-(x-\mu)^2/(2\sigma^2)]/\sqrt{(2\pi\sigma^2)}$

430 Equation 7 implies that a normal distribution is entirely determined by its mean and standard  
431 deviation. By equations 5 and 6, this means cascaded oscillators' distributions of periods and  
432 frequencies are entirely determined by the number of inverters  $n$  in the initial ring oscillators and  
433 the inverter delay parameters  $\mu_d$  and  $\sigma_d$ .

434 Substituting the cascaded oscillators' period parameters in equation 5 into equation 7 to  
435 obtain the period PDFs  $f_i(x)$ , the intersections of each pair of consecutive period PDFs can be  
436 found by elementary algebra. For  $i = 1, 2, \dots$ , ( $i = 1$  representing the ring oscillator), the  
437 intersection of  $f_i(x)$  and  $f_{i+1}(x)$  occurs at period:

$$438 \quad 8. \text{ Intersection}(i) = 2^i(2/3) \{n\mu_d + \sqrt{[(n\mu_d)^2 + 6n\sigma_d^2 \ln(2)]}\} \text{ ms}$$

439 The factor  $2^i$  shows the intersections also have the octave relationship.

440 By substituting the period PDFs  $f_i$  obtained from equations 5 and 7 into equation 6, the  
441 peak frequency (mode) for PDF  $g_i$  can be found by calculus:

$$442 \quad 9. \text{ mode}(i) = \{250/(2^i n\sigma_d^2)\} \{-n\mu_d + \sqrt{[(n\mu_d)^2 + 8n\sigma_d^2]}\} \text{ Hz}$$

443 Again, the factor  $2^i$  shows the peak frequencies also have the octave property. These peak  
444 frequencies are close to, but not the same as, the peak frequencies  $1,000/\mu_i$  derived from the  
445 means  $\mu_i$  of the period's normal distributions in equation 5.

#### 446 **5.4.2. Neuron delay times**

447 Since neuron delay times are determined by several factors, the delay times are  
448 approximately normally distributed (by the central limit theorem). For small networks with  
449 chemical synapses, nearly all of the delay occurs at the synapses. Several studies have measured  
450 synapse delay times [e.g., 22, 23], but the literature apparently does not have empirical estimates  
451 of the parameters (mean and variance) of the delay times' distribution. However, a description of  
452 the range of synapse delay times is "at least 0.3 ms, usually 1 to 5 ms or longer" [20]. Although  
453 the description is far from precise, delay time parameters can be estimated.

454 The description of the range has two parts. The first part "at least 0.3 ms" seems to refer  
455 to all observations. The second part "usually 1 to 5 ms or longer" seems to describe the ranges of  
456 typical samples, with "5 ms or longer" representing the ranges' right endpoints. In that case, the

457 interval [1 ms, 7 ms] is at least a reasonable, rough estimate of the range of a moderately sized  
458 sample.

459 If only the range of a sample (minimum value,  $m$ , and maximum,  $M$ ) is known, the  
460 midpoint can be used as an estimate of the mean of a distribution. Simulations have shown that  
461  $(M - m)/4$  is the best estimator of the standard deviation for moderately sized samples [24].  
462 Based on this and the estimated range [1 ms, 7 ms], neuron delay times are estimated to have  
463 distribution parameters:

464 10.  $\mu_d = 4$  ms,  $\sigma_d = 1.5$  ms

465 For a normal distribution with these parameters, about 99.3% of the distribution is at least 0.3  
466 ms. This agrees well with the description “at least 0.3 ms.” About 73% lies between 1 and 5 ms,  
467 and 95% is between 1 and 7 ms. This agrees reasonably well with the description “usually 1 to 5  
468 ms or longer.”

### 469 **5.4.3. Graphs of estimated neural oscillator frequency distributions**

470 To produce oscillations for five EEG frequency bands, four toggles are needed in  
471 addition to the initial ring oscillator. The hypothesis that cascaded oscillators produce EEG  
472 frequencies implies the initial ring oscillator must have the minimum of three inverters, because  
473 an oscillator with more inverters would be too slow to generate EEG oscillations in the gamma  
474 band. This in turn implies, unsurprisingly, that the brain evolved to enable some information to  
475 be processed as fast as possible.

476 As mentioned earlier, the outputs of a JK toggle (Fig 2F) with continually high input  
477 oscillate. The period is six neuron delay times, the same as the three-neuron ring oscillator  
478 (equation 3). Although a JK oscillator would suffice as the initial oscillator in a cascade and  
479 would produce the same frequencies as a three-neuron ring oscillator, natural selection may have  
480 chosen the ring oscillator because the JK oscillator requires twice as many neurons and has

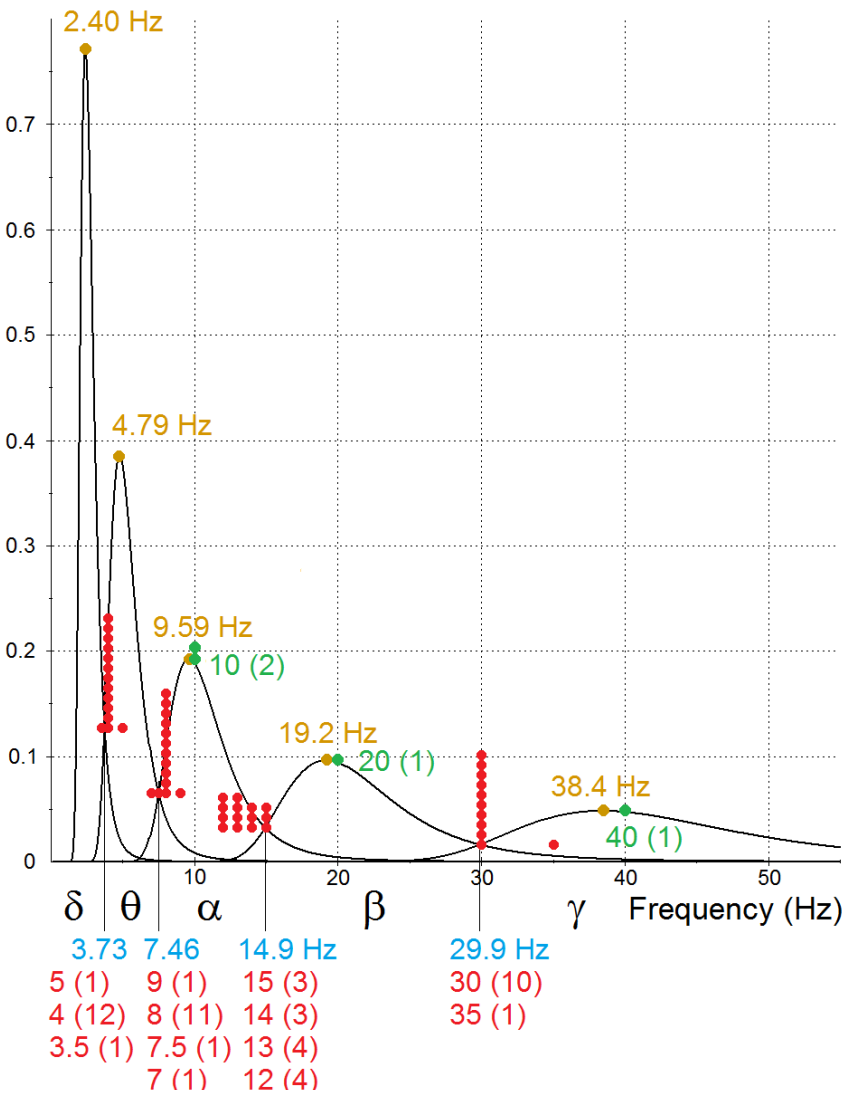


481 somewhat more complexity in synaptic connections. A ring oscillator may also be more robust.  
482 Apparently no other oscillator that can be constructed with neurons is faster or simpler than a  
483 three-neuron ring oscillator.

484 To achieve lower frequency oscillations, ring oscillators with more neurons would  
485 suffice. Selective pressure for a wide distribution of frequencies may have resulted in cascaded  
486 toggles because their periods grow exponentially (doubling with each toggle by equation 4)  
487 while a ring oscillator's period grows linearly with the number of neurons (equation 3). Other  
488 toggles besides the JK would suffice, such as the master-slave mentioned above, but any toggle  
489 would double the period of the input.

490 As before, the period PDFs  $f_i(x)$  are obtained by substituting the period parameters in  
491 equation 5 into equation 7. With the estimated delay parameters of equations 10 and  $n = 3$   
492 neurons, the estimated frequency PDFs  $g_i(x)$  of five cascaded oscillators are obtained from  
493 equation 6. Their graphs are shown in Fig 5. The four intersections of consecutive PDFs, shown  
494 in blue, are found by converting the periods given by equation 8 to frequencies. The five PDF  
495 modes, shown in yellow, are obtained from equation 9. Frequencies that are commonly cited [9-  
496 12, 25-42] as partition points separating the EEG frequency bands and peak frequencies of three  
497 of the bands are shown in red and green, respectively. Numbers in parentheses show how many  
498 times each frequency was cited. (Estimates of peak frequencies apparently have not been found  
499 for the lower frequency delta and theta bands.) The graphs illustrate several of the implications  
500 of the cascaded oscillators hypothesis, which are discussed in the results section.

501



502

503 **Fig 5. Estimated frequency distributions of cascaded neural oscillators.** The graphs are the  
 504 estimated PDFs of the frequencies of a three-neuron ring oscillator and four cascaded toggles.  
 505 All of the PDFs were determined by the estimated mean and variance of neuron delay times.  
 506 The five intervals defined by the intersections of consecutive PDFs are labeled with Greek letters  
 507 to distinguish them from EEG frequency bands, which are often written in the Roman alphabet.  
 508 The intersections and modes are labeled in blue and yellow, respectively. Also shown in red and  
 509 green are frequencies that are commonly cited as partition points separating the EEG frequency  
 510 bands and peak frequencies of three of the bands. Numbers in parentheses and numbers of data  
 511 points show how many times each frequency was cited.

## 512 **5.5. Synchronization**

513           The EEG frequency bands and associated behavioral and mental states are consistent with  
514 the advantages of synchronous logic systems.

### 515 **5.5.1. Synchronous logic systems**

516           Logic systems have a timing problem in ensuring the various subcircuits change states in  
517 the correct chronological sequence. Synchronous logic systems generally have simpler circuit  
518 architecture and fewer errors than asynchronous systems. This is the reason nearly all electronic  
519 logic systems are synchronized by an enabling pulse to each component circuit, so that whenever  
520 any components change states, they change simultaneously. The enabling pulse in such systems  
521 is usually produced by an oscillator. The enabling input in Fig 2E and the oscillators in Fig 3  
522 illustrate how such synchronization is possible with neural networks.

523           Timing problems are greater in sequential logic than in combinational logic, and greater  
524 in parallel processing than in serial processing. Much of the information processing in the brain  
525 involves sequential logic and nearly all of it is parallel. The selective pressure for  
526 synchronization in the brain would have been high, and the neural implementation proposed here  
527 is quite simple.

528           The processing speed in a synchronous system depends largely on the enabling  
529 oscillator's speed. A large system like the brain that performs many diverse functions may have  
530 several different processing speed requirements. The trade-off for greater processing speed is a  
531 higher error rate. Functions that can tolerate a few errors, and that need fast results with many  
532 simultaneous small computations, require high processing speeds. Functions that are less  
533 dependent on speed or massive computation, or that require few errors, or whose component  
534 networks are large and complex and therefore slow to change state, call for slower processing.

## 535 **5.5.2. Synchronization and EEG frequency bands**

536 The EEG frequency bands and associated behavioral and mental states are consistent with  
537 the function of multiple frequencies that was suggested in the preceding paragraph. Gamma  
538 waves (high frequencies) are associated with vision [43, 44] and hearing [Mably 14], which  
539 make sense out of massive data input in a few milliseconds. Beta waves are associated with  
540 purposeful mental effort [20], which may involve less data input while requiring few errors and  
541 complex operations. Alpha waves are associated with relaxed wakefulness [20], theta waves  
542 with working memory and drowsiness [20, 45], and delta waves with drowsiness and sleep [20].  
543 These categories require successively slower information processing, and they have  
544 corresponding EEG bands of lower frequencies.

545 Cascaded oscillators can produce this neural activity. A neural oscillator can synchronize  
546 state changes in neural structures by enabling them simultaneously. The enabling oscillator  
547 pulse by itself does not produce any state changes. It only forces states to change simultaneously  
548 when they do change. So the initial ring oscillator's high frequency signal could simply be  
549 connected directly and permanently to the enabling gates (as illustrated in Fig 2E) of networks in  
550 the visual and auditory cortexes, the first toggle's signal to networks in the prefrontal cortex for  
551 purposeful mental effort, etc. A large number of neural structures synchronized in this way by  
552 cascaded oscillators would exhibit the bands of matched periods found in EEGs.

## 553 **6. Results and explanations of known phenomena**

### 554 **6.1. Short-term memory controversy**

555 Cascaded oscillators and NFFs suggest a resolution to the question of whether short-term  
556 memory depends on neurons firing persistently or in brief, coordinated bursts [7, 8]: Memory is  
557 stored by persistent firing in flip-flops [4], and the coordinated bursts observed along with the  
558 persistent firing are due to the stored information being processed by several neural structures

559 whose state changes are synchronized by a neural oscillator. An example of such short-term  
560 memory processing is a telephone number being reviewed in a phonological loop.

## 561 **6.2. Electroencephalography**

### 562 **6.2.1. EEG frequency bands' peaks and boundaries**

563 Fig 5 shows that the cascaded oscillators hypothesis is supported by the available data for  
564 neuron delay times and EEG frequency band peaks and boundaries. The graphs in Fig 5 are the  
565 estimated oscillator PDFs derived from a description of the range of neuron delay times. The  
566 cascaded oscillators hypothesis implies that the EEG frequency band boundaries are the  
567 intersections of consecutive oscillator frequency PDFs. The graphs show the intersections of the  
568 estimated oscillator PDFs (in blue) are within the ranges of estimated EEG frequency band  
569 boundaries (red). The hypothesis also implies the EEG band peaks are the same as the oscillator  
570 PDF peaks. Fig 5 shows the available estimates of three EEG band peaks (green) are close to the  
571 peaks of the estimated oscillator PDFs (yellow).

572 These close fits also show that the available data support the main implication of the  
573 cascaded oscillators hypothesis (that the EEG bands have the same distributions of frequencies  
574 as the cascaded oscillators) and the implication that the ratios of peaks and boundaries of the  
575 major EEG bands are powers of two.

### 576 **6.2.2. EEG phenomena**

577 The cascaded oscillators hypothesis answers the EEG questions raised in the section on  
578 unexplained phenomena.

579 *What produces the widespread, synchronized, periodic firing?* The firing is periodic  
580 because neural structures are being enabled by an oscillator. The periodic firing is widespread

581 because many neural structures are being enabled. The firing is synchronized because the neural  
582 structures are being enabled by the same oscillator.

583 *What is the function of this widespread synchronization?* The function of  
584 synchronization is timing error avoidance in processing information.

585 *What produces and what is the function of the wide distribution of EEG frequencies in*  
586 *bands?* The frequencies occur in bands because the frequencies are produced by different  
587 oscillators. The wide distribution of frequencies is due to the octave relationship between  
588 cascaded oscillators (100% exponential growth in periods with each successive oscillator by  
589 equation 4) and several oscillators. The distribution of frequencies within each band is due to the  
590 variance of neuron delay times in the initial oscillators in the cascades (equations 5). The  
591 function of the wide distribution of frequencies is meeting the needs of different brain functions  
592 in the trade-off between speed and accuracy.

593 *What produces the unimodal distribution in each band and the octave relationships*  
594 *between the peaks and boundaries?* The unimodal distributions are due to the normal  
595 distribution of neuron delay times in the initial ring oscillators in cascades of oscillators. This  
596 makes the distribution of periods of each oscillator normal and the distributions of frequencies  
597 unimodal. The ratio of consecutive boundaries and peak locations is 2 because consecutive  
598 cascaded oscillators increase the oscillation period by a factor of 2 (equations 4, 8, 9).

599 *What determines the specific frequencies of the peaks and boundaries?* The number of  
600 neurons in the ring oscillators must be the minimum of 3 to produce the high frequencies in the  
601 gamma band. Equations 8 and 9 show the EEG band boundaries and peaks are determined by  
602 this number ( $n = 3$ ), the ring oscillators' delay parameters  $\mu_d$  and  $\sigma_d$ , and the boundary or peak  
603 number  $i$ .

604           *Why do gamma oscillations peak at about 40 Hz?* The three-neuron ring oscillator is the  
605 fastest neural ring oscillator. The estimated peak frequency from equation 9 is 38.4 Hz  
606 (illustrated in Fig 5).

607           *Why does the gamma band contain frequencies that are considerably faster than 40 Hz?*  
608 The frequencies vary because of the variance in neuron delay times in the initial oscillators. As  
609 Fig 5 illustrates, all of the oscillator frequency distributions are skewed to the right, with the  
610 initial oscillator producing frequencies substantially greater than 40 Hz. In the particular  
611 estimate of Fig 5, 2% of the frequencies are greater than 75 Hz, and 0.4% are greater than 100  
612 Hz.

613           *Why is there little agreement on the boundaries separating the EEG bands?* The  
614 oscillators hypothesis implies that the estimates of EEG band boundaries are estimates of the  
615 intersections of the oscillators' PDFs. This makes estimating boundaries difficult for two  
616 reasons.

617           The oscillators hypothesis implies that the probability of an EEG frequency being  
618 observed has a local minimum near each intersection of consecutive oscillator PDFs. This  
619 means that in a random sample of observed EEG frequencies, relatively few will be near the  
620 intersections. A small number of data points has a negative effect on the accuracy of estimates.

621           The overlapping oscillator PDFs (Fig 5) imply the distributions of EEG frequencies  
622 associated with the various behavioral and mental states have overlapping ranges rather than  
623 discrete bands. Because two PDFs are equal at their intersection, a frequency near the  
624 intersection of two PDFs is almost equally likely to be produced by either of two oscillators.  
625 That is, an observed EEG frequency near a band "boundary" is almost equally likely to be  
626 observed along with the behavioral and mental state that defines the band on either side of the  
627 intersection. This makes obtaining accurate estimates of band "boundaries" especially difficult.

## 628 **7. Testable predictions**

### 629 **7.1. Constructed neural networks**

630 Any of the networks in the figures could be constructed with actual neurons and tested  
631 for the predicted behavior. Constructing and testing NFFs was discussed in [4]. The ring  
632 oscillator of Fig 3 may be simple to construct and test. The predicted behavior is oscillating  
633 outputs for all three neurons with a period that is twice the sum of the neurons' delay times, and  
634 phases uniformly distributed over one cycle.

### 635 **7.2. A statistical test of the cascaded oscillators hypothesis**

#### 636 **7.2.1. The data problem**

637 Although the hypothesis that cascaded oscillators produce EEG phenomena is consistent  
638 with available data, as illustrated in Fig 5, the data are too imprecise for a rigorous statistical test  
639 of the hypothesis. The estimates found here for the neuron delay time parameters  $\mu_d$  and  $\sigma_d$  were  
640 based on a rough description of the range of synapse delay times. Available estimates of the  
641 EEG frequency bands' peak frequencies are few, estimates of band boundaries vary widely, and  
642 both types of estimates are routinely rounded to whole numbers. Some researchers do not  
643 attempt to estimate a boundary between bands, instead giving a whole number as the upper  
644 endpoint of one band and the next consecutive whole number as the lower endpoint of the next  
645 band. Estimates of means and variances of both neuron delay times and EEG frequency bands  
646 are apparently nonexistent.

#### 647 **7.2.2. A simple test of the cascaded oscillators hypothesis from sampling data**

648 A simple, rigorous test of the cascaded oscillators hypothesis is possible. As stated in the  
649 introduction, all predicted EEG phenomena follow from the main implication that the EEG bands  
650 and cascaded oscillators have the same distributions of frequencies. This implication can be



651 tested statistically with random samples and the distribution relations of equations 5. As  
652 discussed previously, neuron delay times should be approximately normally distributed by the  
653 central limit theorem. This implies cascaded oscillator periods are also approximately normally  
654 distributed. A normal distribution is completely determined by its mean and variance. So it  
655 remains to be shown that EEG band periods are normally distributed, and that EEG band periods  
656 and oscillator periods have equal means and variances.

657         The neuron delay time parameters  $\mu_d$  and  $\sigma_d$  can be estimated from a random sample of  
658 neuron delay times. These estimates can be used to estimate the oscillator period distribution  
659 parameters  $\mu_i$  and  $\sigma_i$  from equations 5. The mean and variance of the periods of one or more  
660 EEG bands can be estimated from a random sample of EEG periods (or frequencies). With  
661 standard tests for equal means and variances, the EEG estimates can be compared to the  
662 oscillator estimates of  $\mu_i$  and  $\sigma_i$ . The EEG sampling data can also be used to test EEG band  
663 periods for normal distributions. If the application of the central limit theorem to neuron delay  
664 times may be questionable, neuron delay times can also be tested for a normal distribution with  
665 the neuron delay time sampling data.

### 666 **7.2.3. Caveats**

667         Because the oscillators' frequency ranges overlap (Fig 5), the band to which an observed  
668 EEG period or frequency is assigned should be determined by the observed behavioral and  
669 mental state that defines a band, not by predetermined endpoints of bands. If EEG sampling data  
670 are measured in frequencies, they must be converted to periods before computing the sample  
671 mean and variance. (The period of the sample mean of frequencies is not the same as the sample  
672 mean of periods.) Sampling data should not be rounded to whole numbers. In using equations 5  
673 to find the estimated oscillator parameters, recall that the value of  $n$  must be the minimum of 3.  
674 Sampling data for neuron delay times and EEG periods (or frequencies), or even estimates of  
675 means and variances, may already be available in some database.

676           Although it is possible that EEG frequencies are produced by cascaded oscillators with  
677 initial oscillators that are made up of specialized neurons whose delay times are different from  
678 the general population of neurons, this appears to be unlikely. Fig 5 shows the EEG frequency  
679 distributions are at least close to the values predicted by the general description of the range of  
680 neuron delay times that was used here to estimate oscillator neuron delay time parameters.  
681 Moreover, neurons in general and initial oscillator neurons in particular may have both evolved  
682 under selective pressure to function as fast as possible.

## 683 **8. Acknowledgements**

684           The simulation was done with MS Excel. Network diagrams were created with  
685 CircuitLab and MS Paint. Graphs were created with MS Excel, Converge 10.0, and MS Paint.  
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