The Internal Structure of Metacommunities

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ABSTRACT:

Metacommunity ecology has become an important subdiscipline of ecology, but it is

increasingly evident that its foundational theoretical and analytical frameworks do not

adequately incorporate a realistic continuum of environmental and biotic process at play.

We propose an approach that develops stronger links between theoretical and statistical

frameworks to shift the focus towards the study of the 'internal structure' of

metacommunities by dissecting how different species and different sites contribute to

overall metacommunity structure. To illustrate this, we simulate data from a model that

includes environmental variation, dispersal, biotic interactions, and stochasticity as the

basic ecological processes that influence species' (co)-distributions. We analyze the

simulated data with hierarchical community models and propose a new method to

visualize and analyze the simultaneous role of species co-distribution, environment, space,

and stochasticity in this emerging statistical approach. We focus in particular on

quantifying how species affect the overall structure of the metacommunity via differences

in their dispersal and niche traits, and how environmental filtering, dispersal and species

interactions varies from site to site in relation to environmental conditions and

connectivity. Although there are still challenges ahead, this framework provides a roadmap

for a more comprehensive approach by jointly developing more mechanistic theory based

on community assembly processes and the analytical tools needed to map these concepts

onto data in diverse landscapes and systems.

Introduction

The assembly of communities and their dynamics are driven by processes that act at both local and regional scales (e.g. Levin 1974, Ricklefs 1987, Lawton 1999, Leibold et al. 2004). The local-regional connection embodied in the metacommunity framework, which examines the role of local (i.e. patch) dynamics and their connectivity at the regional (i.e. metacommunity) scale and, by doing so, has provided important advances to our understanding of the coexistence, diversity and distribution of species in space and time (see Leibold et al. 2004, Logue et al 2011, Brown et al. 2107, Leibold and Chase 2017, Ovaskainen et al. 2019). Nevertheless, our understanding of mechanisms governing these dynamics in diverse systems and in complex landscapes, and our ability to infer them from field surveys, is still poorly developed. In particular, it remains difficult to connect abundance patterns in patches and metacommunities to underlying assembly mechanisms (Leibold and Chase 2018, Ovaskainen et al. 2019).

The classical conceptual framework of metacommunity ecology is based on four idealized models (the so-called 'archetypes') of metacommunity dynamics (e.g., species sorting, neutral, patch dynamics and mass effects; Leibold et al. 2004). Until now, these have mostly been studied by quantifying how the community composition varies, for example in relation to spatial or environmental factors (Cottenie 2005, Peres-Neto et al. 2006), and attributing a given system to one of the archetypes based on this analysis. Although these idealizations served as useful benchmarks to classifying metacommunities according to major drivers such as environmental heterogeneity and dispersal (e.g. Leibold 2011, Logue et al. 2011, Lindstrom and Langenheder 2011), it is increasingly recognized that this

overlooks many important features of metacommunities (e.g. Brown et al. 2017, Leibold

and Chase 2018, Ovaskainen et al. 2019, Thompson et al. 2020). Consequently, it has been

difficult to expand these models and the associated theoretical framework to highly diverse

communities, while still maintaining their general insights and intuitive appeal (e.g.

Fournier et al. 2017, Ovaskainen et al. 2019).

Drawing from parallels with evolutionary biology, Vellend (2010, 2016) proposed an

alternative, more process-oriented theoretical framework for community ecology. In this

view, the assembly of species is the result of the interaction between four main processes:

a) dispersal (analogous to gene flow in evolution), b) speciation (and other ways species

arrive into the regional species pool; analogous to mutations), c) demographic stochasticity

(ecological drift, analogous to genetic drift), and d) species interactions and responses to

environmental factors (analogous to selection, including both frequency-dependent and

frequency independent components). If we adopt this view, and consider that speciation is

beyond the scope of regional metacommunity dynamics, our aim is thus to explain the

distribution of species across sites in a metacommunity by ecological drift, dispersal,

environmental filtering (i.e. responses to 'abiotic' factors) and selection linked to species

interactions (Fig. 1). This links the basic processes identified by Vellend (2010, 2016) to

the classical concepts of community assembly via accessibility (dispersal), abiotic and

biotic 'filters' (Soberon et al. 2005). The additional advantage is that all these components

can be estimated with joint species distribution models (JSDMs), a relatively new and

promising class of statistical community models.

The categorical approach based on archetypes makes the implicit assumption that there is

a dominant assembly process that applies to most species across most local sites in a

metacommunity (Brown et al. 2017, Leibold and Chase 2018). However, it ignores the way

that different species may experience a given metacommunity in different ways, for

example because they differ in dispersal abilities or by having distinct responses to habitat

heterogeneity. It also ignores that different sites within a metacommunity may have

species compositions that are determined by distinct processes. For example, sites that are

very isolated may be occupied by species that occupy neighboring sites due to dispersal

limitation, regardless of how well suited they are to local environmental conditions

whereas sites that are very closely connected in space may be more susceptible to source-

sink relations with neighboring sites.

Furthermore, previous work has not adequately accounted for the role of species

interactions that can act to influence the distribution of species in metacommunities. For

example, variation partitioning (Borcard et al. 1992, Cottenie 2005) only addresses effects

of environmental and spatial factors but does not account for any additional possible

effects of species interactions (Logue et al. 2011). The roles of species interactions other

than interspecific competition has also been largely neglected (Guzman et al. 2019, Gravel

and Massol 2020).

In this article, we explain how these shortcomings might be addressed in a more

comprehensive framework that builds on Vellends (2010) approach and can better account

for species interactions (see also Ovaskainen et al. 2019). We especially focus on

accounting for heterogeneities among species and localities by dissecting overall

metacommunity structure into species-specific and patch-specific components which we

call the 'internal structure' of the metacommunity. We also focus more directly on key

processes that drive community assembly dynamics in metacommunities (e.g., stochastic

drift, dispersal, selection, heterogeneity, Vellend 2010, 2016), recognizing that a continuum

of outcomes can emerge depending on the relative strengths of those processes (see also

Gravel et al. 2006, Leibold and McPeek 2006, Vellend 2010, 2016, Boulangeat et al. 2012,

Munkenmuller et al. 2012, Fournier et al. 2017, Wiegand et al. 2017, Ovaskainen et al. 2019,

Rybicki et al. 2018, Thompson et al. 2019, Shoemaker et al. 2020, Gravel and Massol 2020).

We illustrate this with a flexible theoretical model that captures the key elements and

processes of metacommunity dynamics, including species and patch-level variation.

Although we limit ourselves to interspecific interactions via competition, we recognize that

ongoing and future work will address the full scope of species interactions, including

facilitation and cross-trophic level interactions.

Quantifying the link between process and pattern using a simple metacommunity

simulation and refined statistical approach:

To test and exemplify the analytical power of our framework, we simulate data from a

process-based model, which allows us to create observations with complete knowledge

about the underlying mechanisms. Our process-based model is based on a spatial

implementation of early spatially implicit site occupancy models (e.g., Levins and Culver

1971, Horn and MacArthur 1972, Levin 1974, Hastings 1980, Hanski 1991) to describe

dynamics in heterogeneous, multispecies metacommunities. For each species in each

patch, we model occupancy using two key equations (details in the SI). The first of these

describes the colonization of patch z by species i during a discrete time interval, Δt:

$$P\left(X_{i,z,t+\Delta t} = 1 | X_{i,z,t} = 0\right) \;=\; I_{i,z,t} S_{i,z,t} C_{i,z,t} \tag{1}$$

where $X_{i,z,t}$ is a stochastic variable representing the occurrence of species i at location z at

time t, $I_{i,z,t}$ is the number of immigrants of species, $S_{i,z,t}$ is the effect of environmental

filtering on the probability of establishing a viable local population, and $C_{i,z,t}$ is the effect of

ecological interactions on the establishment probability. Second, we consider the

alternative possibility: the extinction of species i in patch z during the time interval Δt:

$$P\left(X_{i,z,t+\Delta t} = 1 | X_{i,z,t} = 0\right) \;=\; M_{i,z,t} E_{i,z,t} \tag{2}$$

where $M_{i,z,t}$ and $E_{i,z,t}$ are the responses of the extinction probability to the local

environment and to ecological interactions, respectively.

At steady state the solution to this model is:

$\log \frac{\hat{p}^{i,z}}{1-\hat{p}^{i,z}} = \log I^{i,z} + \log \frac{S^{i,z}}{M^{i,z}} + \log \frac{C^{i,z}}{E^{i,z}}$ (3)

where $\hat{P}^{iz}$ is the expected probability that site *z* is occupied by species *i.*

This formulation supposes that immigration($I^{i,z}$), 'abiotic selection' ($S^{i,z}$ *and* $M^{i,z}$) and

interactions ($C^{i,z}$ *and* $E^{i,z}$) can be separated into distinct effects that do not interact. This

may not apply in all cases in nature if, for instance the strength of species interactions or

dispersal could vary with the environment. Equation 3 naturally follows a log-linear

structure, suggesting that an appropriately structured JSDM can be used to separate the

contributions of these effects into spatial effects (driven by immigration), environmental

filtering (driven by abiotic selection) and species co-distribution unrelated to either space

or environment. This very general analytical model's probabilistic nature suggests that in a

case with a finite number of patches there should be an additional fraction of the variation

that is independent of these factors and thus stochastic within this context (Shoemaker et

al. 2020). Furthermore, the likelihood of every observation can be marginalized over each

species (by summing the likelihoods for a given species across all patches) to describe the

variation among species. Alternatively, the likelihood can be marginalized by patch (by

summing the likelihoods for a patch across all species) to describe the variation across the

region. Doing so, we can quantify the importance of environment, species co-distribution,

and space for predicting metacommunity structure as a whole, as well as their importance

for predicting the abundance of individual species or community composition at individual

patches. In this way, we can study the 'internal structure' of the metacommunity. This can

clarify how these key processes work together in a diverse and complex metacommunity to

explain species distributions within the metacommunity (Figure 1).

Figure 1: A summary of the metacommunity problem. Species distributions, denoted by the

species-by-sites **L** matrix , are the outcome of drift, selection, dispersal, and speciation.

These basic processes can be influenced by species interactions, food web structure,

biogeography, phylogeny and micro-evolution. Metacommunity theory mainly focuses on

drift, selection and dispersal. We view previous approaches based on the four archetypes

of Leibold et al. (2004) as being much more indirect and idealized. Instead, we call for a

more direct evaluation of how the basic processes affect the **L** matrix, and how to dissect

the consequences to the distributions of different species and the occupancy of different

sites, for example by using a JSDM to identify main effects and interspecific variability in

the importance of unstructured, biotic, environmental, and spatial effects on **L**. This

approach allows us to recognize and address the effects of heterogeneities among species

and among patches on the overall structure of the metacommunity.

To illustrate the utility of this approach in a more realistic framework, we implemented the

key processes of drift, environmental filtering, dispersal, and species interactions (Vellend

2010, 2016) in a flexible simulation version of the model (described in more detail in the

SI). The simulation model allows us to vary each process separately for each species in a

heterogeneous spatially explicit landscape. It simulates the dynamics of a metacommunity

across a set of patches and generates a spatial network that specifies the connectivity

among patches. The state variables of the simulation are the occupancy of each species in

every patch (i.e. presence/absence, though future implementations could also address

abundance data, e.g. Rybicki et al. 2018, Ovaskainen et al. 2019, Thompson et al. 2020).

Each patch can be colonized from nearby patches depending on their location in the

landscape, dispersal rate of the species and proximity of extant populations in neighboring

patches. Each species in each patch is subject to extinctions that reflect demographic

and/or environmental stochasticity. Patches can differ in local environmental conditions

that differentially influence baseline colonization and extinction probabilities. Species

interactions are modeled in two ways. First, the presence of other species in a patch can

modify baseline colonization probability (a reduction in the case of competition). Second,

co-occurring species can modify baseline extinction probability (an increase in the case of

competition).

We next apply a JSDM to the resulting distribution of species among patches. Specifically,

we use the package 'Hierarchical Modeling of Species Communities' (HMSC, Ovaskainen et

al. 2017, Ovaskainen and Nerea 2020) that accounts for the effect of the environment,

spatial autocorrelation and species co-distribution. After fitting the model using HMSC, we

partition variation between the model processes into four components (or fractions) using

an approach akin to classic variation partitioning (Borcard et al. 1992; Peres-Neto et al.

2006 – see Box 1 for a historical retrospective of the development of this methodology).

Details about how this type of variation partitioning is computed through HMSC is given in

the Supporting Information. Specifically, the variation was partitioned to quantify the

effects of environment (labeled [E]), spatial patterning (labeled [S]), co-distribution among

species (labeled [C]) and residual (unexplained) variation that cannot be attributed to any

of the three previously mentioned fractions. This is expressed as $1-R^2$, where R^2 is the

proportion of variation explained by the model that includes fractions [E], [S], and [C].

Compared to the classical method, this variation partitioning approach provides two major

advances. The first is that we can infer a third fraction that quantifies co-variation (or co-

distribution) among species using latent variables (fraction [C]), which is distinct from

either the environment effect (fraction [E]) or the spatial effects (fraction [S]). In our model

this fraction reflects the consequences of species association, and we emphasize that this

interpretation must be done with caution (see Dormann et al. 2018 and Blanchet et al.

2020 for critical reviews of this issue). The second advance is that all fractions are

calculated at the species level, where species-specific variation detail the internal structure

of the metacommunity from the perspective of each individual species. Fractions of the

variation at the metacommunity level are then calculated by averaging across all species to

obtain metacommunity level descriptors akin to those obtained from variation partitioning.

This allows us to subsequently examine potential predictors quantifying the variation in

these different effects among species. In addition, we developed a way to partition each

fraction on a site-by-site basis as described in the SI. The technical details for these

calculations are a bit different than those used for the species-level analyses and in

particular they do not allow for averaging the R^2 of the model across patches; rather we

instead use the additive fraction of the models to the overall variation (see the SI for more

details). This way to partition variation among sites informs us about the individual

contribution each site has to variation in the data. The ability to resolve species-specific

and site-specific components means that we can study the 'internal structure' of the

metacommunity in ways that were absent in classic variation partitioning.

Although the analytical model described in equations 1-3 suggests that we can make a link

between process and pattern using JSDMs, we wished to evaluate if this was also likely in

less idealized situations such as those used in our metacommunity model. Our goal here is

to illustrate how this link might be made and we leave a more extensive evaluation of these

methods for future work (see also Ovaskainen and Nerea 2020). To do this, we simulated a

number of scenarios that vary the strength of environmental selection, dispersal and

competition. Comparing scenarios that vary niche breadth and competition (scenarios A-D,

Fig. 2 and Fig 3), and a more complex case where species compete and vary in both

dispersal and response to the environment (scenario G, Figure 4, scenarios E and F in the

SI) highlight how HMSC provides an avenue for distinguishing between underlying

processes based on abundances of species across metacommunity patches.

Simulation Results

In the first set of simulations, we considered a situation where species had distinct

environmental optima along an environmental gradient and had limited dispersal (Figure

2, Table 1). We contrasted the case where the environmental niches were narrow (steep

changes in baseline colonization success and extinction rates with small deviations in

environment) with the case with identical optima, but with wide environmental niches

(much flatter changes in colonization and extinction with environmental value). As

expected, we find that these differences in environmental niche breadth had strong effects

on the relative importance of environmental filtering (fraction [E]) versus spatial

patterning (fraction [S]). Specifically, we find stronger spatial patterning when niche

breadths were broad and stronger environmental filtering when niches were narrower.

We also found that the R^2 values were higher for the case with narrow niches than with

wide niches. Finally, we also found non-zero (though relatively weak) variance

components for co-distributions (fraction [C]) in both cases, especially when niches were

broad even though our analytical model would predict the absence of such variation

components since colonization and extinctions were not affected by species interactions in

these simulations. We discuss possible explanations for this observation below.

Table 1: Summary of metacommunity level variation components for the seven different

scenarios modeled in this study.

		Fractions			
Scenario	Corresponding Figure	E (SD)	S (SD)	C (SD)	Residuals 1-R^2 (SD)
A	2, upper panels	0.75 (0.11)	0.026 (0.019)	0.044 (0.062)	0.18 (0.11)
B	2, lower panels	0.019 (0.015)	0.15 (0.037)	0.019 (0.036)	0.81 (0.04)
C	3, upper panels	0.42 (0.31)	0.21 (0.2)	0.14 (0.16)	0.23 (0.12)
D	3, lower panels	0.018 (0.026)	0.35 (0.3)	0.28 (0.33)	0.35 (0.33)
E	Supplement	0.63 (0.21)	0.067 (0.069)	0.13 (0.15)	0.18 (0.089)
F	Supplement	0.74 (0.097)	0.035 (0.025)	0.047 (0.057)	0.18 (0.097)
G	4	0.5 (0.17)	0.08 (0.072)	0.2 (0.16)	0.22 (0.12)

Figure 2: Ternary plots describing the three components of metacommunity internal

structure for two different simulation scenarios with no species interactions (independent

metapopulations): The upper panels correspond to narrow environmental niches whereas

lower panels correspond to wide environmental niches. Each dot represents a species (left

panels) or a site (right panels). The size of the symbol is proportional to the R^2 of the model

(note the different scales used for species and sites) and the location indicates the

proportion of explained variation attributed to environmental factors (E - lower left),

spatial effects (S - lower right) and remaining co-distributions (C - upper apex) (see SI for

details). In the species panels (left side) different symbols indicate different replicate

simulations; generally, these indicate that the distribution of species responses are variable

within replicates but that the overall variation among replicates are repeatable.   In the site

panels (right side), the shading indicate how central (lighter) or extreme (darker) the local

environmental conditions are on the gradient; these also show substantial variation but

indicate that more extreme environmental conditions increase the effects of local

environment on occupancy patterns than more central conditions.

We next simulated metacommunities with identical parameters as above, except with

added interspecific competition effects (Figure 3, Table 1). As in the case without species

interactions (compare with Figure 2), narrow niches enhanced the relative strength of

environmental filtering (fraction [E]) and reduced spatial patterning (fraction [S]) when

compared to wide niches. In these simulations, however, the co-distribution components

(fraction [C]) were much more substantial than without species interactions. We also

found that adding interspecific competition substantially increased the amount of variation

explained (R^2) by the model.

Figure 3: Ternary plots describing the three components of metacommunity internal

structure for different simulation scenarios with competition among the species. Notation

is the same as in Figure 2. The upper panels correspond to narrow environmental niches

whereas the lower panels correspond to wide environmental niches. Left-hand panels

show variation components for different species whereas panels on the right hand side of

the figure correspond to variation components for different sites.

We conducted a number of other simulations to explore if these ternary plots (see Box 1)

that describe interspecific variation in the effects of dispersal, niches breadth, and

interactions on environment (fraction [E]), space (fraction [S]), and co-distributions

(fraction [C]). Illustrative examples are shown in the supplemental information and

summary statistics are shown in Table 1. We illustrated one of these that includes

heterogenous dispersal to show how the internal structure can reveal how dispersal

variation affects distributions (Figure 4). We found that we could distinguish species by

the degree to which their distributions are related to environment (fraction [E]), space

(fraction [S]) and co-distributions (fraction [C]) (Figure 5a). Species with higher dispersal

ability and more specialized environmental niche positions had distributions better

predicted by the environment than those that were dispersal limited and had distributions

that were more spatially autocorrelated (fraction [S]). Species with optima closer to the

middle of the environmental gradient also had a larger fraction [C] than those with more

extreme optima.

Figure 4: Ternary plots for species (left panel) and sites (right panel) for simulations with

species that differ in environmental position along the gradient and dispersal ability. The

size of the symbol indicates the R^2 of the model for each species or site). In the left panel

(species) the color indicates the preferred local environmental conditions for species

(yellow for species that prefer centrally located environmental conditions, purple or

magenta for species with more extreme environmental optima). The symbol indicates the

dispersal rate of the species (circles are more dispersal limited, squares are least dispersal

limited and triangles are intermediate). In the right hand panel the color indicates the

degree of deviation from centrality along the environmental gradient (as in Figure 2).

Figure 5: Effects of species traits (left panel) and site attributes (right panel) on the

environmental fraction of variation in species distributions and site occupancy. A) Higher

dispersal ability and lower niche centrality (i.e. greater deviation from mean niche value)

enhance the degree to which different species (individual symbols) have distributions that

correlate with environmental variation. B) Sites that differ more from the mean

environmental value (environmental deviation) are more likely to be occupied by species

with niche traits that are locally favored.

Sites also differed in how their species composition was related to environmental effects

(fraction [E]), spatial effects (fraction [S]) and co-distributions (fraction [C] - Figure 4b).

Some sites tended to be occupied by locally dominant species (in the lower left of the

ternary plot, nearer to fraction [E]), while others were occupied by species found in nearby

sites (lower right of the ternary plot, nearer to fraction [S]). Some sites were also occupied

by combinations of species that were differentially associated with each other regardless of

environment or dispersal (upper apex of the ternary plot, nearer to fraction [C]). As can

understood from figure 4b, there were also a wide range of intermediate conditions. A

major driver of this variation is the local environmental condition, especially in relation to

how distinct the local environment is from the overall mean environment of the

metacommunity (Figure 5b).

We further investigated the structure of the species co-distribution (fraction [C]). In our

analyses, this covariation can be directly attributable to species interactions due to our

ability to closely model the underlying processes. However, even in our model, species co-

distribution may not directly link to pairwise interaction coefficients, but rather may

emerge as a complex relationship between species interactions and environmental

conditions (Cazelles et al. 2015, Blanchet et al. 2020). To illustrate this, we show the co-

distribution among species as a heat map separately for each of the five individual

simulations presented in Figure 4 and compared them to the actual interaction matrix that

describes interspecific competition in our model (Figure 6; similar heat maps obtained

with the other scenarios are shown in the Supplemental Information). Despite the fact that

the same interaction matrix was used for all five of these simulations, the resulting co-

distribution patterns are inconsistent in their details. However, these matrices show that

there is consistency in several features of the co-distribution pattern. For example, they all

share the predominance of strong negative correlations along the main diagonal that match

the interaction matrix we used. They also share a strong 'checkerboard' pattern with

alternating negative and positive co-distributions between species when these are ranked

against their environmental optima. Given the simple scheme of species interactions we

used (Fig. 5 and SI), these results are consistent with the predictions that direct

interactions are stronger than indirect ones and tend to weaken with the number of links in

indirect chains even if the details of these effects are less predictable.

Figure 6: Comparisons of the interaction matrix (Simulation) with the co-distribution of

species in five replicate runs (Iteration 1-5) of the scenario with interspecific variation in

dispersal and competition among species. In each figure species are ranked by the position

of their environmental optima along the environmental gradient. The co-distributions are

shown as heat maps with the strength of the covariation proportional to the intensity of

color and the color indicating negative (green) or positive (gray) covariation among pairs

of species. These can be compared to the pattern of direct species interactions (left panel

called Simulations). The Xs denote no significant association although the color indicates

the trend.

Discussion

While metacommunity ecology has made great progress in the past decades, the

assumptions that species and sites were relatively homogeneous in their underlying

processes (reviewed in Leibold and Chase 2017) have limited the applicability of

metacommunity theory to more realistic species pools within complex landscapes. Here,

by combining a tractable process-based model with emerging analytical methods, we have

provided a general approach that accounts for multiple interacting processes that may

operate differently among species or in different parts of landscapes.

Although there are some important challenges to consider, our study illustrates important

insights about the 'internal structure' of metacommunities , including:

456   • Variation partitioning using JSDMs (here implemented using HMSC) can be

457   linked to basic processes of community assembly (e.g. environmental

458   selection, dispersal, biotic selection, and drift).

459   • Quantifying co-distributions of species in metacommunities can improve

460   predictive ability even when the processes that generate these distributions

461   are complex (stochasticity, complex spatial landscapes, and species

462   interactions).

463   • Species can have distributions that are determined by combinations of the

464   basic community assembly processes depending on features of their ecology

465   (dispersal and environmental preferences)

466   • Predominant assembly processes can differ among adjacent sites in a

467   metacommunity (e.g. sites that are occupied by species most fit for

468   environmental conditions vs sites occupied by species in nearby sites that

469   may differ in environmental conditions)

Despite these advances, it is important to emphasize that there remain some substantial

challenges in moving forward with the overall approach we have advocated. This includes

some technical issues (e.g. estimation of parameters, interpretation of results in more

complex models in JSDMs and with real data) as well as conceptual ones (e.g. accounting

for other processes such as speciation, local adaptation, historical biogeography).

Nevertheless, we believe such an endeavor will be fruitful, allowing a deeper

understanding of ecological dynamics in more realistic, but necessarily complex, spatial

landscapes.

Our model simplifies several potentially complex processes (e.g. non-linearities and

interactive effects) into an approximation involving colonization-extinction dynamics. It is

possible that more realistic and complex mechanisms driving these processes will weaken

associations between pattern and process or create biases in the partitioning of the

variation revealed by JSDMs. However, the development of JSDMs are still progressing, and

we anticipate that future developments could solve some of these problems.

The co-distribution component of the JSDMs (fraction [C]) is particularly concerning. We

find that this component can be biased, especially when species have broad environmental

niches (Figure 2). It is widely recognized that there are particular challenges in quantifying

and interpreting species co-distributions (reviewed by Blanchet et al. 2020). Perhaps the

most obvious challenge is that this component can reflect <u>any</u> process that is inadequately

quantified by the environmental (fraction [E]) and spatial components (fraction [S]). In

addition to species interactions, this would include, for example, unmeasured

environmental factors (see Blanchet et al. 2020). Teasing apart the effects of species

interactions from these confounding factors should thus be a major focus for future work.

Nevertheless, it is important to understand that including the co-distribution component in

our analyses allows us to account for them, rather than lumping them with residual

variation where they give an exaggerated impression of stochasticity.

The basic framework we used to address the process to pattern link is most transparent for

mechanisms that focus on interspecific competition because of the analogies with genetic

change in evolutionary genetics (Vellend 2010, 2015). However, species interactions in

metacommunities are much more variable and include consumer-resource interactions,

mutualisms and facilitative interactions. Although such interactions can easily be

incorporated in simulations, the interpretation that might link process to pattern in such

cases becomes more complex. Likewise, future work could include local (co-)evolutionary

dynamics (see Urban et al. 2020) and historical effects of biogeography and speciation (e.g.

Leibold and Chase 2018, Overcast et al. 2020).

In this paper, we have also retained a simple two-level perspective on spatial scale (local

discrete sites in a broader regional landscape). It is increasingly apparent that

metacommunity dynamics occur over multiple nested scales and that habitats can be

continuous and/or nested, rather than discretely patchy (e.g. Munkenmuller et al. 2012,

Rybicki et al 2018, Ovaskainen et al. 2019, Viana and Chase 2019). Refining our approach

to address multiple spatial scales is a logical next step.

Here, we have argued that a focus on the internal structure of metacommunities, by

examining site-specific and species-specific variation components, can enhance our study

of the links between process and pattern in the distributions of species and the occupancies

of sites. We also argue that such developments are essential if metacommunity ecology is

to address the dynamics and structure of realistic metacommunities that have typically

high biodiversity and are in complex landscapes. This focus on internal structure

represents a shift from traditional approaches that used descriptors of overall variation

components at the metacommunity scale that generalizes previous ad hoc approaches to

similar internal variation in metacommunity patterns (e.g. Pandit et al. 2009). The

dynamics and structure of distributions of realistically diverse species in a realistically

structured landscape of sites likely involves the interaction of community assembly

processes including environmental filtering, dispersal, and drift, and these are unlikely to

be adequately described by simple metacommunity level metrics (see Ovaskainen et al.

2019). Consequently, dissecting the internal structure of metacommunities on the basis of

species and site contributions could provide key insights into the processes underlying

metacommunity assembly.

Box 1: Contrasting Analytical Approaches to Metacommunity Ecology:

a) Variation partitioning: The key elements of this approach were developed by Borcard et

al. (1992) and recognized that sets of communities could often show spatial patterning that

was independent of environmental factors in determining local species composition. Since

then the approach has been refined in numerous ways, but the overall idea remains the

same. It models overall community composition (ignoring the individual effects on

different species or sites) as being related to environmental predictors (labeled E in Figure

B1, often considered as fixed and generally suitable for abiotic factors) or to spatial

patterning (labeled S in the figure, often because communities that are close to each other

are likely to have similar species even if environments differ). There results four partitions

of the overall variation in composition: one that is solely predicted by the environmental

conditions, one that is solely predicted by spatial effect, one that is predictive but cannot be

resolved into either environment or spatial factors because they are confounded, and

residual variation that is often interpreted as 'stochastic'.

b) Joint Species Distribution Models used to study overall variation in community structure

and related methods. Here we recognize that there is an additional possible set of

predictors that influence co-distributions of species besides environment and space

(labeled I in the figure). This method recognizes that the 'residuals' of the variation

partitioning method in a) are not necessarily random but may show cross-correlations

among species. The mechanisms are vague but possibly include the influence of

unmeasured environmental variables or the influence of species. They thus add a third

major variation component to the 'variation partitioning' method described in a). To date,

results using these methods have mostly focused on the patterns at the metacommunity

scale to assess metacommunity structure (but see Ovaskainen et al. 2017).

c) Species-specific and Site-specific elaborations on jDSMs: Ovaskainen et al. (2017)

suggested that trait or phylogenetic relations among species could be used as predictors for

the various overall fractions described by b). Here we take this suggestion further by

refining the details of the method to partitioning the overall pattern in b) into contributions

by individual species and/or individual sites. The results can be visualized using ternary

plots (with terminal axes that correspond to E, S and I) that display the relative

contributions of environmental, spatial, and residual covariation among species and among

sites. We further visualize the overall joint predictive effects of all three of these predictors

as proportional to the size of symbol (i.e. small symbols show species who's distribution if

more stochastic than large symbols). We then examine how these components of variation

are correlated with species traits (in relation to species-specific variation) or with site

attributes (in relation to site-specific variation). Only this last approach reveals the

internal structure of the metacommunity and tries to identify the key species- and site-

attributes that might drive these effects.

Figure B1: Highly simplified diagramatic representation of variation partitioning methods

in metacommunity ecology: a) variation partititioning (Borcard et al. 1992), total variation

in community variability is partitioned in relation to environment (E) and space (S). b)

joint-species distribution models (Ovaskainen et al. 2017), latents are used to further

quantify variation due to co-distribution (C) patterns unrelated to E or S. c) internal

structure of metacommunities (current contribution), the elements of E, S and C as well as

the overall explanatory ability to predict distributions of individual species or sites is

dissected (upper panel) and can be related to features of species and sites (lower panels).

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The Internal Structure of
Metacommunities: Supplementary
Information

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Description of Model

Patch locations and environmental variables

In our model, the metacommunity consists of N patches distributed over a spatially
heterogeneous landscape, with multiple environmental variables(although, the current
simulations only have one environmental variable D and 1000 patches) that could either be
randomly distributed or spatially autocorrelated. Each patch has a set of coordinates in a two-
dimensional space, and all possible coordinates are feasible such that this is a continuous space
model that is not restricted to a lattice or some other kind of regular spatial arrangement of
spatial units.

A patch may be empty, or be occupied by a single or by several species. We define $X_{i,z,t}$ as a
stochastic variable representing the occurrence of species i at location z and time t.
Occurrence, $X_{i,z,t}$, takes a value of 1 when species i is present and a value of 0 when it is
absent. Similarly, we define $\mathbf{Y}_{z,t} = X_{1,z,t}, X_{2,z,t}, \dots, X_{R,z,t}$ as a vector containing the presence-
absence of each species from the regional pool R.
The model only tracks the occupancy of the patches (not population densities). Spatial
dynamics occurs because of colonization events, in both empty patches and patches that

are occupied by other species, and because of extinction events. The emerging species co-
distributions are a result of a dynamic balance between these events. Ecological
interactions can impact either or both the colonization and the extinction probabilities. For
instance, the presence of a competitor pre-empting a patch can reduce the colonization
probability by another competitor. Alternatively, the presence of a competitor in a patch
could increase the extinction probability of another species. Similarly, the environment
could influence both the colonization and the extinction probabilities.

Patch Colonization

We consider a discrete-time Markovian process to represent the dynamics of presence-
absence of all species and we incorporate the effect of dispersal, environmental filtering and
ecological interactions in such a way that we could cover all possible scenarios wherein species
differ in any combination of ways. We include interspecific competition along with other types
of spatial dynamics such as predator-prey interactions (Gravel et al. 2011), priority effects
(Shurin et al. 2004), or mutualistic interactions (e.g. Gilarranz et al. 2015). Following a
colonization event from time t to $t + \Delta$ corresponds to:

731
$$P(X_{i,z,t+\Delta t} = 1 \mid X_{i,z,t} = 0) = I_{i,z,t} S_{i,z,t} C_{i,z,t}$$

where $I_{i,z,t}$ is the number of immigrants of species i reaching patch z at time t, $S_{i,z,t}$ is the
effect of environmental filtering on the probability of establishing a viable local population and
$C_{i,z,t}$ is the effect of ecological interactions on the establishment probability. We note that
because we represent a stochastic process, the product of these three functions has to be
bounded between 0 and 1. We consequently define these quantities:

The effect of immigration is given by:
738

739
$$I_{i,z,t} = \frac{\sum k(z, \omega) X_{i,\omega,t}}{\sum k(z, \omega)}$$

which is a weighted average of the occurrence probability of species i in the neighborhood
of z. The function $k(z, \omega)$ is a dispersal kernel that depends on the location of patch z and
the neighborhood ω. For convenience, we consider an exponential function of the
Euclidean distance between localities. We add to the kernel a low distance and
neighborhood-independent constant m in order to account from immigration from outside
the simulated metacommunity. This assumption is required to prevent total extinction by
drift under perfectly neutral dynamics.

The effect of the environment is given by a product of the establishment performance over
all environmental variables E_n:

$$S_{i,z,t} = \prod f(E_{n,z}\, \mu_{i,n}\, \sigma_{i,n})$$

751 In our simulations, for convenience, we consider that the function f has a quadratic form for
752 all species and all environmental variables, though the model is flexible enough to consider
753 other responses that also differ among species.

Ecological interactions on establishment probability

To incorporate all possible ecological interactions, we start by representing the interaction
network by a community matrix $\mathbf{A}$ of R species. The elements α_{ij} of $\mathbf{A}$ quantify the effect of
species j on the dynamics of species i. When α_{ij} is negative, the colonization probability of
species i decreases and/or its extinction probability increases when j is found locally. Inversely,
when α_{ij} is positive, the colonization probability increases and/or the extinction probability
decreases. To account for the cumulative effects of local interactions on transition probabilities,
we make colonization and extinction probabilities community dependent. As explained above,
at a time t, the $\mathbf{Y}_{z,t}$ vector gives the local assemblages. We calculate the sum of interactions at
any time and for each species as $v = \mathbf{A}_{z,t}\mathbf{Y}_{z,t}$. Our approach can be interpreted as a spatial
analogue to the generalized Lotka–Volterra model because it takes into account the impact of
the whole network of interactions on each species dynamics and can deal with any type of
interaction. We now define the function

$$C_{i,z,t} = g(v_i, z, t)$$

768 representing the total effect of ecological interactions on the colonization probability. For
769 convenience, we will use a sigmoid function, with g ranging between c_{min} at high negative
770 interactions and c_{max} at high positive interactions, where c_{max} should be interpreted as the
771 maximal colonization probability when the environmental conditions are optimal and there are
772 no dispersal limitations.

Patch Extinction

774 The definition of the extinction probability follows exactly the same rules as for colonization,
775 except that extinction is independent of the neighborhood composition. We follow the same
776 logic to define the effect of ecological interactions and of variation in the environment.
777 Consequently, we get the Markovian process:

$$P\big(X_{i,z,t+\Delta t} = 1 \,\big|\, X_{i,z,t} = 0\big) = M_{i,z,t}E_{i,z,t}$$

where $M_{i,z,t}$ and $E_{i,z,t}$ are the responses of the extinction probability to the local
environment and to ecological interactions, respectively. The difference with the
colonization functions defined in the previous section is that the extinction probability
must be larger when interactions are negative and smaller when they are positive. In
addition, the extinction rate should be minimal (instead of maximal) at environmental
optimum.

Interpretation

787   To interpret the model, note that, at steady state, for each species, we obtain the expected
788   occurrence probability ($\hat{P}$) at each site as:

789
$$\frac{\hat{P}^{iz}}{1 - \hat{P}^{iz}} = \frac{I^{iz} \cdot S^{iz} \cdot C^{iz}}{M^{iz} \cdot E^{iz}}$$

790   After a log transformation, this yields:

791
$$\log\left(\frac{\hat{P}^{iz}}{1 - \hat{P}^{iz}}\right) = \log(I^{iz}) + \log\left(\frac{S^{iz}}{M^{iz}}\right) + \log\left(\frac{C^{iz}}{E^{iz}}\right)$$

The last equation can be interpreted as a macroscopic description of the expected species
distribution pattern (Thuiller et al. 2013). In this formulation, $\log(I)$ describes the
tendency of a patch to resemble other nearby patches due to the spatial contagion by
dispersal, $\log\left(\frac{S}{M}\right)$ describes the tendency of sites to be occupied by species with similar
fitness responses to environmental gradients, and $\log\left(\frac{C}{E}\right)$ describes the remaining
influence of other species on co-occurrence due to interactions among species. The values
for these indices will depend on what choices are made for the components of eq. 1 (see
Supporting Information for details on how we implemented this simulations model).

This modeling framework can represent the classical archetypes (Box 1), but also permits
more intricate (and likely far more realistic) metacommunity scenarios and predictions.
For example, we could use the model to examine how species traits (and environmental
context) link to metacommunity dynamics. Moreover, continuous mixtures of different
metacommunity extremes (archetypes) can be represented by appropriate choices for
dispersal, competitive abilities, and environmental preferences. For instance, species
sorting would require a relatively large colonization to extinction ratio along with species-
specific environmental requirements and regional similarity (sensu Mouquet and Loreau,
2002). Alternatively, coexistence within competition-colonization trade-offs requires

species to have similar responses to the environment and appropriate heterogeneities in
the I, C and E functions, but no environmental preferences.

The implemented mechanisms in the simulation model can be partly mapped onto
variation partitioning components. For instance, at equilibrium, we could expect dispersal
limitation (the $\log(I)$ term in equation 3) to create positive spatial autocorrelation at the
dispersal scale (the [S/E] fraction in variation partitioning). Environmental filtering (the
$\log\left(\frac{S}{M}\right)$ term in equation 3) should lead to a correlation between composition and
environment (the [E/S] fraction in variation partitioning). The last term in equation 3,
however, describing the effect of interactions on distribution (the $\log\left(\frac{C}{E}\right)$), is novel and has
no equivalent in the context of classical variation partitioning.

Description of the Statistical Framework

Hierarchical Community Models

In their simplest form, Hierarchical Community Models (HCMs) resemble standard species
distribution models that regress species presences/absences against environmental predictors.
However, to reduce model complexity, HCMs assume that all species in a metacommunity will
react to environmental heterogeneity following a similar response function (e.g., linear vs
quadratic or Gaussian). To account for spatial autocorrelation, either spatial variables such as
Moran's eigenvectors maps (MEM, Dray et al. 2006) or spatially auto-correlated latent variables
(Ovaskainen et al. 2016b) can be incorporated to the model. To account for biotic interactions,
non-spatially auto-correlated latent variables are used. If we use a linear specification approach
(here, this can also include quadratic terms that capture Gaussian responses to environment as
imposed in our model), we can write:

832
$$\mathbf{L}^{zi} = \mathbf{X}^{zk}\mathbf{B}^{ki} + \boldsymbol{\epsilon}^{zi}$$

834   with

835
$$\mathbf{B}^{ki} N(\boldsymbol{\mu}, \boldsymbol{\Sigma})$$

where $\mathbf{L}^{zi}$ is the presence (or absence) of species i (out of m species) at patch z (out of n
patches), $\mathbf{X}^{zk}$ is the value of the environmental variable k (out of p variables) at site z, $\mathbf{B}$ is
a matrix of regression parameters, $\boldsymbol{\mu}$ is a vector of length p that describes the mean
environmental response of all species, Σ is a $p \times p$ covariance matrix that describes how
species vary (diagonal) and co-vary (off-diagonal) around the mean environmental

response (Ovaskainen and Soininen 2011), and $\boldsymbol{\epsilon}^{zi}$ is a residual value. Estimating species
parameters hierarchically around a community mean reduces the degrees of freedom and
makes the model easier to fit with limited data. Both $\boldsymbol{\mu}$ and Σ can be further informed or
constrained by species traits or phylogeny if desired (Ovaskainen et al. 2017). To account
for biotic interactions, we consider latent variables $\mathbf{H}^{zl}$ (where l refers to a latent variable
measured at site z) and their associated parameters $\boldsymbol{\Lambda}^{li}$ (Ovaskainen et al. 2016a). This
yields:

849                                 $$\mathbf{L}^{zi} = \mathbf{X}^{zk}\mathbf{B}^{ki} + \mathbf{H}^{zl}\boldsymbol{\Lambda}^{li} + \boldsymbol{\epsilon}^{zi}$$

Note that it is not necessary to always include all of these components in one model; they
can be considered in any combination deemed relevant for a particular question. In this
paper, we used Moran's Eigenvector Maps (MEMs; Dray et al. 2006), a powerful and
commonly used method to account for space in statistical models involving species
distributions. Note that we could have also used autocorrelated latent variables
(Ovaskainen et al. 2016b) to account for the space into the model.
Calculating Variation Partitioning for the HCM As in any generalized linear mixed effect
model, we can now partition the explained variation into different components, notably
environmental heterogeneity, co-distribution (biotic interactions), space and unexplained
variation (Figure S1). To estimate the unique contributions of each of these four fractions
for each species, we calculated semi-partial coefficients of determination (i.e., based on
Type III sum-of-squares as specified in Peres-Neto et al. 2006) using the implementation
suggested by Tjur (2009) as being more appropriate for presence-absence data (i.e., logit
link) than the traditional variation partitioning based on an identity link. To adjust for the
number of variables used to quantify each fraction of the variation partitioning analysis, we
applied the adjustment to the coefficient of determination proposed by Gelman and Pardoe
(2006) in the variation partitioning analysis, which is designed for hierarchical models. As
shown in Figure A1, the different partitions were combined so that a unique value was
associated to environment (fractions [a], [d]/2, [f] and [g]/2), co-distribution (fraction [c]),
space (fractions [b], [d]/2, [e] and [g]/2) and the unexplained portion of the variation
(fraction [h]). Latent variables are quite powerful to isolate structure in the data. As such,
in the calculation of the variation partitioning, latent variables will capture almost all
variation associated to the environment and space, giving an artificial inflation of the
overlapping partitions between co-distribution and environment and co-distribution and
space. For this reason, all partitions overlapping with co-distribution (fractions [e], [f] and
[g]) were associated to either environment (fractions [f] and [g]) or space (factions [e] and
[g]). In this calculation, a unique measure of explained variation (in adjusted R2) is
associated to co-distribution (fraction [c]) but this is not the case for environment and

space. To associate a unique value to environment and space, and represent the results as
we did in Figure 2 and 3 we divided the fractions overlapping environment and space
between these two components. As such, the sum of fractions [a], [f], half of fraction [d] and
half of fraction [g] were used to measure the effect of the environment while fractions was
considered [b], [e], half of fraction [d] and half of fraction [g] were used to measure the
effect of space.

Supplementary Figure 1.

Calculation of the coefficient of determination

Classic coefficient of determination

888   The coefficient of determination, R^2, that was partitioned in the variation partitioning analysis
889   is calculated for species j as

$$R_j^2 = 1 - \frac{\sum_{i=1}^{n}(y_{ij} - \hat{y}_{ij})^2}{\sum_{i=1}^{n}(y_{ij} - \overline{y}_{ij})^2)}$$

891   where y_ij is the data associated with species j (out of p species) at site i (out of n sites), $\hat{y}_{ij}$ is
892   the model associated to species j at site i and $\overline{y}_j$ is the average of the data for species j across
893   all sites.

Community-level coefficient of determination

895   Although having an R_j^2 for each species j can be highly informative, it is sometimes useful to
896   also have a single R^2 for the entire community. This is obtained by averaging all R_j^2

$$^C R^2 = \frac{\sum_{j=1}^{p} R_j^2}{p}$$

898   where the $^C R^2$ is the community-level R^2.

Site contribution to the coefficient of determination

In the paper, we use the contribution of each site to R_j^2 to present how each site contributes differently to the environment, space and co-distribution for the community. The calculation of the site i contribution to the R_j^2, is calculated as

$$R_{ij}^2 = \frac{1}{n} - \frac{(y_{ij} - \hat{y}_{ij})^2}{(y_{ij} - \overline{y}_{ij})^2}$$

When studying equation A12, a few considerations can be made. The first part of the equation where the 1 of the classic R_j^2 is divided by n is included to make sure that if we sum all R_{ij}^2 across all sites for species j, the resulting value is R_j^2 and not some other value.

More importantly, what can be noticed is that by calculating R_{ij}^2, the contribution of sites to each species R_j^2, we obtain a matrix that has the same dimension as the site by species matrix (an $n \times p$ matrix). Using this matrix, if we sum across all sites, we obtain the R_j^2. However, if we average across the species for site i we obtain the site's contribution to the community-level $^C R^2$ or $^C R_i^2$.

Pseudo coefficient of determination

There exist different variants of $pseudo - R^2$ that can be applied to specific types of data (e.g. Tjur's D (Tjur 2009) is designed to presence-absence data) or more broadly (e.g. Efron's $pseudo - R^2$ (Efron 1978)). Because all the different variants of $pseudo - R^2$ can be applied to a model with a single response variable (i.e. a single species), community-level $pseudo - R^2$ can be obtained following the approach mentioned above. However, this is not always possible when the interest is to calculate the sites' contribution to a $pseudo - R^2$, especially for variants of $pseudo - R^2$ that do not have a mathematical structure similar to the classical R^2.

Parameterization and Simulation Scenarios

We simulated metacommunity dynamics with a landscape of 1000 patches over 200 time steps and an initial occupancy of 0.8. Patches were placed randomly in a two-dimensional plane with coordinates drawn from a uniform distribution with a minimum of 0 and a maximum of 1. The environment varied spatially, with values drawn from a random distribution between 0 and 1. In the specific simulations we studied in the paper, colonization was the only component of the species that were affected by the environment (i.e. $E_{i,z,t} = 1$). Specifically, colonization reacted to the environment following a quadratic curve.

For all scenarios considered, we simulated 12 species. Niche optimums for the species were evenly distributed between 0.1 and 0.9 while niche breadth was set to 0.8 for simulations with narrow niches (scenarios A, B, E, F, G), and to 2 for simulations where niche was assumed to be broad (scenarios C and D). For dispersal, we considered an exponential

dispersal kernel, with a distance-independent immigration probability of 0.001 and an α
parameter of 0.05. For scenario G, where we have variable dispersal kernels (Figure 3), α
was 0.01 for 1/3 of species, 0.05 for 1/3 of species, and 0.1 for the other 1/3 of species. We
used a sigmoid function to relate the total number of interactions with colonization and
extinction coefficients following the implementation by Cazelles et al. (2016). Colonization
probability in the absence of interactions was set at 0.4, which tends to zero as negative
interactions tend to infinity, while it asymptotes at a 1 with infinite positive interactions.
All other aspects of the colonization-interaction curve were the same for all scenarios.
Similarly, extinction in the absence of interactions was set at 0.025, and tended to 1 with
infinite negative interactions, while its asymptote tended to 0 with infinite positive
interactions. In both cases, the parameter setting the shape of the sigmoid function was set
to 0 for the scenarios without competition (scenarios A, B, and F), and 1.5 in the presence
of competition (scenarios C, D, E, G) . If there were interactions, then a focal species only
interacted with the two species that had the closest niches. For all scenarios, five sets of
metacommunities were simulated and analyzed to obtain the results found in Figures 2, 3,
and 4 in the main text, and supplementary figures.

All scenarios have been implemented in R and the project's repository can be found here:
github.com/javirudolph/testingHMSC

Supplementary Figure 2. Species interactions for all scenarios.

Supplementary Figure 3. In which we have half of the species with interactions and the
other without.

Supplementary Figure 4. In which we change dispersal only, α was 0.01 for 1/3 of species, 0.05 for 1/3 of species, and 0.1 for the other 1/3 of species.

Example of metacommunity simulation functions and analyses

The following example of code shows the overall processes involved in the metacommunity simulation for our model. This example shows the scenario for 20 patches and one environmental variable. The model gives the option for a random or spatially aggregated structure for the patches. In the aggregated case, we determined four clusters, denoted by `NClusters` in the code below. The value of the environmental variable for each patch is shown with the color hue. In this case, the environmental variable is randomly distributed.

```
set.seed(227)
# Random XY coordinates
```

```
968    # Each coordinate is drawn from a random uniform distribution
969    get_XY = function(N) cbind(runif(N),runif(N))
970
971    # Aggregation of XY coordinates
972    get_XY_agg = function(N, Nclusters, sd_xy) {
973
974      Xclust = runif(Nclusters)
975      Yclust = runif(Nclusters)
976
977      X = rnorm(N, rep(Xclust,N/Nclusters), sd_xy)
978      Y = rnorm(N, rep(Yclust,N/Nclusters), sd_xy)
979
980      cbind(X,Y)
981    }
982
983    # Random uniform environmental values
984    get_E = function(D, N) matrix(runif(D*N), nr = N, nc = D)
```

Here, we set N, the number of patches to 20, and D, the number of environmental variables to one.

```
987    N <- 20
988    D <- 1
989
990    rXY <- get_XY(N)
991    agXY <- get_XY_agg(N, 4, 0.02)
992    E <- get_E(D = D, N = N)
```

The following figure shows a side by side comparisson between random and aggregated patches obtained from our functions.

Initial Occupancy

The toy model allows for setitng the initial occupancy in the metacommunity. For example, to create the initial conditions, $t = 0$, of presence absence, species occupancy is drawn from a random uniform distribution, and values smaller than 0.8 are considered as species presence. Patches or locations z are represented by rows in the matrix, whereas each species is a column. Each cell in the matrix is $X_{i,z,t}$ and each row is $\mathbf{Y}_{z,t}$ for $t = 0$. The following figure shows three

1002   different iterations of this process, where areas in black represent occupancy = 1, and white
1003   denotes an absence.

```
1004    #Get your initial conditions:
1005    R <- 8
1006    Y0 = matrix(0, nrow = N, ncol = R)
1007    rand = matrix(runif(N*R), nr = N, nc = R)
1008    Y0[rand < 0.8] = 1
1009
1010    ggplot(melt(Y0), aes(x = Var1, y = Var2, fill = value)) +
1011      geom_tile() +
1012      scale_fill_gradient(low = "white", high = "black")+
1013      labs(x = "Plot number", y = "Species", subtitle = "Iteration 1") +
1014      theme_bw() -> A
1015
1016    # Second iteration for the same initial conditions
1017    Y0 = matrix(0, nrow = N, ncol = R)
1018    rand = matrix(runif(N*R), nr = N, nc = R)
1019    Y0[rand < 0.8] = 1
1020
1021    ggplot(melt(Y0), aes(x = Var1, y = Var2, fill = value)) +
1022      geom_tile() +
1023      scale_fill_gradient(low = "white", high = "black")+
1024      labs(x = "Plot number", y = "" , subtitle = "Iteration 2") +
1025      theme_bw() -> B
1026
1027    # Third iteration
1028    Y0 = matrix(0, nrow = N, ncol = R)
1029    rand = matrix(runif(N*R), nr = N, nc = R)
1030    Y0[rand < 0.8] = 1
1031
1032    ggplot(melt(Y0), aes(x = Var1, y = Var2, fill = value)) +
1033      geom_tile() +
1034      scale_fill_gradient(low = "white", high = "black")+
1035      labs(x = "Plot number", y = "", subtitle = "Iteration 3") +
1036      theme_bw() -> C
1037
1038    # Set the three iterations to be displayed side by side
1039    ggarrange(A, B, C, ncol = 3, common.legend = TRUE, legend = "none")
```

1040

When we consider the immigration component, we need to also consider the connectivity
matrix. In the code below, I_f calculates the probabilty of immigration for each species,

based on the occupancy matrix and the dispersal kernel, K. The argument K is the
connectivity matrix. The argument XY corresponds to the patch coordinates, whereas $alpha$
is the dispersal parameter associated to the exponential distribution used for dispersal. It
can be computed with the following function:

```
1047  # Compute the propagule pressure
1048  I_f = function(Y, K, m) I = (1-m)*(K%*%Y)/(K%*%matrix(1,nr=N,nc=R)) + m
```

1049 The arguments for this function are: Y, K, m. We calculated $\mathbb{Y}$, species presence or absence, in
1050 the previous section with the case for initial conditions. Argument m is set in the parameters as
1051 a value $m = 0.001$ and the connectivity matrix K is calculated below.

```
1052  # Compute the connectivity matrix
1053  get_K = function(XY, alpha) {
1054      N = nrow(XY)
1055      distMat = as.matrix(dist(XY, method = "euclidean", upper = T, diag = T))
1056      ConMat = exp(-1/alpha*distMat)
1057      diag(ConMat) = 0
1058      return(ConMat)
1059  }
```

1060 As an example, using the aggregated XY coordinates for 20 patches and our initial occupancy
1061 matrix with 8 species ,we can see the connectivity between patches, and can calculate the
1062 contribution of immigration from each species to each patch.

```
1063  # We can use the aggregated XY coordinates for this example:
1064  XY <- agXY
1065
1066  # Connectivity matrix
1067  alpha <- 0.005
1068  K <- get_K(XY, alpha)
1069  plot_K <- cbind(rownames(K), stack(as.data.frame(K)))
1070  names(plot_K) <- c("X", "Fill", "Y")
1071  plot_K %>%
1072    as_data_frame() %>%
1073    mutate(X = factor(X, levels = c(1:20)),
1074           Y = factor(Y, levels = c(1:20))) -> plot_K
1075  ggplot(plot_K, aes(x = X, y = Y, fill = Fill)) +
1076    geom_raster() +
1077    scale_fill_gradient(low = "black", high = "white") +
1078    #scale_fill_viridis_c() +
1079    labs(title = "Connectivity among patches") +
1080    theme(legend.title = element_blank(),
1081          axis.text.x = element_text(angle = 90)) -> A
1082  # Immigration
1083  m <- 0.001
1084  Y <- Y0
1085  I <- I_f(Y, K, m)
1086  rastPlot(I, title = "I - Immigration to each plot", x = "Patches", y = "Species") +
1087    theme(legend.title = element_blank()) -> plot_I
1088  ggarrange(A, plot_I, ncol = 2)
```

1089

1090 The effect of the environment on each species, depending on each species niche optima, is
1091 computed in the following code section. The argument E corresponds to the vector of values
1092 for the environmental variable in each patch. The other two arguments in this function are
1093 the niche optima (u_s) for each species and niche breadth(s_c).

```
1094   # Compute the local performance of propagules
1095   S_f_quadratic <- function(E, u_c, s_c) {
1096     R <- ncol(u_c)
1097     N <- nrow(E)
1098     D <- ncol(E)
1099     S <- matrix(1, nr = N, nc = R)
1100     for(i in 1:D){
1101       optima <- matrix(u_c[i,],nrow = N,ncol = R,byrow = TRUE)
1102       breadth <- matrix(s_c[i,],nrow = N,ncol = R,byrow = TRUE)
1103       S <- S * ((-1 / (breadth/2)^2) * (E[,i] - optima)^2 + 1)
1104       S <- ifelse(S < 0, 0 , S)
1105
1106     }
1107     return(S)
1108   }
1109
1110   # Understood as niche optima for each species, for each environmental variable
1111   u_c = matrix(nr = D, nc = R)
1112   u_c[1,] = seq(0.1,0.9, length=R)
1113   # Understood as niche breadth
1114   s_c = matrix(0.2, nr = D, nc = R)
1115
1116   # Local performance, colonization
1117   S <- S_f_quadratic(E, u_c, s_c)
1118   plot_S <- rastPlot(S, title = "S - Local performance colonization", x = "Patches", y = "Specie
1119   s") +
1120     guides(fill = guide_colorbar(title = ""))
1121   plot_S
```

1122

1123 When incorporating species interactions into the toy model, we use the following
1124 interaction matrix **A**, where the colored black sections show species with potential of
1125 interacting:

```
1126    # # Interaction matrix
1127    A = matrix(0,nr=R,nc=R)
1128    d = as.matrix(dist(c(1:R),upper=TRUE,diag=T))
1129    A[d<=1] = -1
1130    diag(A) = 0
1131
1132    plot_A <- rastPlot(A, title = "A - Interaction matrix", x = "species", y = "species") +
1133      scale_fill_gradient(low = "black", high = "grey") +
1134    theme(legend.position = "none")
1135    # Compute the sum of ecological interactions for every location and every species
1136    sum_interactions = function (A, Y) t(A%*%t(Y))
1137    # this is considered to be "v"
1138    v <- sum_interactions(A, Y)
1139
1140    plot_v <- rastPlot(v, title = "v - Sum of interactions", x = "patches", y = "species") +
1141      guides(fill = guide_colorbar(title = "")) +
1142      scale_fill_gradient()
1143
1144    ggarrange(plot_A, plot_v, ncol = 2)
```

1145

1146 We compute the effect of ecological interactions on colonization probability with the
1147 function below.The arguments for this function are v as the resulting matrix from the sum
1148 of interactions, d_c as the sensitivity to interactions, c_0 and c_max as the colonization
1149 parameters:

```
1150  C_f = function(v, d_c, c_0, c_max) c_max*(1 +(1/c_0 - 1)*exp(-v*d_c))^-1
1151
1152    # # Colonization function
1153    c_0 = rep(0.4, R) # Colonization at 0 interactions
1154    c_max = rep(1, R) # Colonization at max interactions
1155
1156    # # Sensitivity to interactions
1157    d_c = 0.2
1158
1159  C <- C_f(v, d_c, c_0, c_max)
1160  plot_C <- rastPlot(C, title = "C - Interactions on colonization", x = "Patches", y = "Species
1161  ") +
1162    guides(fill = guide_colorbar(title = "")) +
1163    scale_fill_gradient()
1164  plot_C
```

1165

1166   With all the components calculated, we can now compute the colonization probability

1167 $P\left(X_{i,z,t+\Delta t} = 1 \mid X_{i,z,t} = 0\right) = I_{i,z,t}S_{i,z,t}C_{i,z,t}$

1168

1169   The following function calculates the effect of the environment on the extinction, with E

1170   being the environmental variable, and u_e and u_s being species level effect and the

1171   assymptote.

```
1172   M_f = function(E, u_e, s_e) {
1173       R = ncol(u_e)
1174       N = nrow(E)
1175       D = ncol(E)
1176       M = matrix(1, nr = N, nc = R)
1177       for(i in 1:D){
1178         M = M*(1-exp(-(E[,i]-matrix(u_e[i,],nr=N,nc=R,byrow=TRUE))^2 / matrix(s_e[i,],nr=N,nc=R,
1179   byrow=TRUE)^2))
1180           }
1181       return(M)
1182   }
1183
1184   # Set the function arguments
1185     # # Effect of the environment on extinction
1186     u_e = matrix(nr = D, nc = R)
1187     u_e[1,] = c(rep(0.5, R-1), 0.05) # One species having a lower level of extinction from envir
1188   onmental effect
1189     s_e = matrix(Inf, nr = D, nc = R)
1190
1191     #u_e
1192     #head(s_e)
```

1193 The following shows the effect of ecological interactions on extinction, using the same v matrix
1194 calculated above.

```
1195  E_f = function(v, d_e, e_0, e_min) {
1196
1197      e_min_mat = matrix(e_min, nr = N, nc = R, byrow=TRUE)
1198
1199      e_min_mat+(1/(1-e_min_mat)+(1/(e_0-e_min_mat)-1/(1-e_min_mat))*exp(d_e*v))^-1
1200
1201  }
1202
1203
1204  #With the arguments computed as:
1205
1206
1207  # # Extinction function
1208    #e_0 = c(rep(0.025, R-1), 0.5) # Extinction at 0 interactions, with one species having a hig
1209  her value.
1210  e_0 = rep(0.025, R)
1211  e_min = rep(0, R) # Exinction at max interactions
1212
1213    # # Sensitivity to interactions
1214
1215    d_e = 0
```

1216 We can now compute the probability of extinction $P\bigl(X_{i,z,t+\Delta t} = 1 \mid X_{i,z,t} = 0\bigr) = M_{i,z,t}E_{i,z,t}$

1217 The figure shows these as identical graphs, since we have made all species have the same
1218 probability of extinction and the environment not having an effect on extinction.

1219 The way
1220 parameters are set, the extinction component is the same for all species in every patch.

Testing and changes

```
1222  # Perform the test
1223  delta <- matrix(0, nr = N, nc = R)
```

```
1224   rand <- matrix(runif(N*R), nr = N, nc = R)
1225   delta[Y == 0 & rand < P_col] <- 1
1226
1227   # Perform the test
1228   rand = matrix(runif(N*R), nr = N, nc = R)
1229   delta[Y == 1 & rand < P_ext] = - 1
```

1230

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