Worth the effort? A practical examination of random effects in hidden Markov models for animal telemetry data

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Abstract

1. Hidden Markov models (HMMs) that include individual-level random effects have recently been promoted for inferring animal movement behaviour from biotelemetry data. These "mixed HMMs" come at significant cost in terms of implementation and computation, and discrete random effects have been advocated as a practical alternative to more computationally-intensive continuous random effects. However, the performance of mixed HMMs has not yet been sufficiently explored to justify their widespread adoption, and there is currently little guidance for practitioners weighing the costs and benefits of mixed HMMs for a particular research objective.

2. We performed an extensive simulation study comparing the performance of a suite of fixed and random effect models for individual heterogeneity in the hidden state process of a 2-state HMM. We focused on sampling scenarios more typical of telemetry studies, which often consist of relatively long time series ($30 - 250$ observations per animal) for relatively few individuals ($5 - 100$ animals).

3. We generally found mixed HMMs did not improve state assignment relative to standard HMMs. Reliable estimation of random effects required larger sample sizes than are often feasible in telemetry studies. Continuous random effect models were fairly robust to data generated under discrete random effects, but not vice versa. Inclusion of random effects to "mop up" unexplained variation can improve estimation of state transition probabilities and measurable covariate effects, but discrete random effects can be a relatively poor (and potentially misleading) approximation for continuous variation.

4. When weighing the costs and benefits of mixed HMMs, three important considerations are study objectives, sample size, and model complexity. HMM applications often focus on state assignment with little emphasis on heterogeneity in state transition probabilities. Under these circumstances, random effects in the hidden state process simply may not be worth the additional effort. However, if explaining variation in state transition probabilities is a primary objective and sufficient explanatory covariates are not available, then random effects are worth pursuing as a more parsimonious alternative to individual fixed effects.

5. To help put our findings in context and illustrate some potential challenges that practitioners may encounter when applying mixed HMMs, we revisit a previous analysis of long-finned pilot whale biotelemetry data.

Keywords animal biotelemetry, biologging, dependent mixture model, latent Markov

model, `momentuHMM`, state-space model, state-switching, `TMB`

1 Introduction

Hidden Markov models (HMMs; e.g. Zucchini *et al.* 2016) are used extensively in ecology for inferences about unobservable state processes from sequential (e.g. time series) data. Some of the most widely used HMMs in population ecology include capture-recapture (e.g. Pradel 2005), species occurrence (e.g. Gimenez *et al.* 2014), and animal movement (e.g. Franke *et al.* 2004) models. As recent advances in animal-borne biologging technology have permitted the collection of detailed location and biotelemetry data (e.g. Cooke *et al.* 2004), HMMs for inferring animal movement behaviour have become particularly popular (e.g. Morales *et al.* 2004; Jonsen *et al.* 2005; Patterson *et al.* 2009; Langrock *et al.* 2012; McClintock *et al.* 2012). This has been bolstered by user-friendly software specifically tailored to HMMs for these data (Michelot *et al.* 2016; McClintock & Michelot 2018).

While animal movement HMMs were originally formulated as relatively simple 2-state (e.g. "foraging" and "transit") models describing steps and turns between successive locations (e.g. Franke *et al.* 2004; Morales *et al.* 2004), they have since become much more complicated by incorporating location measurement error (e.g. Jonsen *et al.* 2005), > 2 movement behaviour states (e.g. Michelot *et al.* 2017; Pirotta *et al.* 2018), additional biotelemetry data streams (e.g. DeRuiter *et al.* 2017; Isojunno *et al.* 2017), and "mixed HMMs" including individual-level random effects (e.g. Langrock *et al.* 2012; Schliehe-Diecks *et al.* 2012; McClintock *et al.* 2013; McKellar *et al.* 2015). While all of these advances bring the potential for new and exciting inferences about animal movement behaviour, they also pose various challenges (e.g. Patterson *et al.* 2017; Pohle *et al.* 2017). The inferential benefits of accounting for measurement error or including additional data streams to characterize > 2 behavioural states can justify this added complexity (e.g. Bradshaw *et al.* 2007; McClintock 2017), yet the general benefits of mixed HMMs that include individual random effects are less clear.

There is evidence for the benefits of individual random effects on the (conditional) observation process of HMMs in other contexts (e.g. Altman 2007; Rueda *et al.* 2013), but there is surprisingly little evidence for benefits on the hidden state process. In a simulation study, Altman (2007) concluded for their case that there was "far more

information about the parameters associated with the conditional model than those associated with the hidden model" and that mixed HMMs allowing for individual differences in the hidden state process "may explain very little additional variation in the observed data and, hence, may not be worthwhile from a statistical standpoint." Yet understanding individual heterogeneity in behaviour or life history strategies is a fundamental component of ecology and evolution (e.g. Johnson *et al.* 1986; Cam *et al.* 2002; Réale *et al.* 2007; Revilla & Wiegand 2008; Gimenez *et al.* 2018), and accounting for individual variation in the hidden state process is clearly worthwhile for this purpose. Most animal movement mixed HMM applications have employed random effects on the hidden state process more as a statistical tool to "mop up" unexplained variation and improve goodness-of-fit, with little attempt to interpret the mechanisms or implications of this variation (e.g. McKellar *et al.* 2015; Towner *et al.* 2016; DeRuiter *et al.* 2017). Part of the reason for this may be that, unlike effect sizes for explanatory covariates (e.g. age, sex, weight), generic random effects are difficult to interpret (e.g. Altman 2007; Gimenez *et al.* 2018), particularly in biological terms across free-ranging telemetered individuals, each typically with different deployment lengths and being observed in different environmental and behavioural contexts (e.g. Towner *et al.* 2016; DeRuiter *et al.* 2017). Nevertheless, failing to properly account for individual variation could be detrimental to the estimation of effect sizes for any explanatory covariates on the hidden state process (e.g. DeRuiter *et al.* 2017).

In their discussion of the benefits of individual random effects on the hidden state process, DeRuiter *et al.* (2017) claim "it is easy to argue that random effects to account for individual variation are a key component of animal behaviour models." We certainly do not disagree with this, but the empirical performance of these complex models has not yet been sufficiently explored to justify their widespread adoption (*sensu* Hodges 2019), and there is currently little guidance for practitioners to determine when and how they should pursue random effects. This would all be relatively moot if mixed HMMs were easy for practitioners to implement, but they typically are not. Mixed HMMs have historically required custom-coded model fitting algorithms at significant computational cost (e.g. Altman 2007; Maruotti & Rydén 2009; Langrock *et al.* 2012; Schliehe-Diecks *et al.* 2012; McKellar *et al.* 2015; Towner *et al.* 2016) and can be very challenging to reliably fit to time series of animal biotelemetry data (e.g. DeRuiter *et al.* 2017; Isojunno *et al.* 2017). Furthermore, unlike other ecological applications of

mixed HMMs that typically include relatively many individuals (e.g. capture-recapture; Burnham & White 2002; Gimenez & Choquet 2010) or sites (e.g. occupancy; Gimenez *et al.* 2014) and relatively short time series, animal-borne biotelemetry studies typically include relatively few individuals (e.g. due to financial and logistical constraints) and relatively long time series of unequal length for each individual (e.g. due to variable battery life, tag loss, and mortality). Little is currently known about how well mixed HMMs perform under these sampling conditions.

These challenges and uncertainties prompted us to investigate the benefits of accounting for individual variation in the hidden state process of HMMs that are frequently used for inferring animal movement behaviour from biotelemetry data. Using extensive simulation and a case study, our goal is to provide some guidance to aid practitioners in weighing the costs and benefits of mixed HMMs for a particular research objective. We first describe several of the most common HMM formulations and inferential procedures that account for individual variation. We then present a large-scale simulation study evaluating the performance of these various approaches in terms of hidden state estimation, parameter estimation, and detection of individual variation by standard information-theoretic model selection criteria. To help put our findings in context and illustrate some potential challenges that practitioners may encounter when applying mixed HMMs, we then revisit an analysis of long-finned pilot whale biotelemetry data originally performed by Isojunno *et al.* (2017). Finally, we discuss the implications of our findings in establishing some considerations for practitioners contemplating the inclusion of individual random effects in their own analyses.

2 Individual-level effects in HMMs

2.1 Model formulations

Under "complete pooling", standard HMMs for M individual time series of length T_m ($m = 1, \ldots, M$) assume no individual effects on parameters. Assuming independence between individuals, the likelihood function for this "null" model ($\mathcal{L}_{null}$) with N hidden states can be succinctly expressed using the forward algorithm:

$$\mathcal{L}_{null} = \prod_{m=1}^{M} \boldsymbol{\delta} \boldsymbol{\Gamma} \mathbf{P}(\mathbf{y}_{m,1}) \boldsymbol{\Gamma} \mathbf{P}(\mathbf{y}_{m,2}) \cdots \boldsymbol{\Gamma} \mathbf{P}(\mathbf{y}_{m,T_m-1}) \boldsymbol{\Gamma} \mathbf{P}(\mathbf{y}_{m,T_m}) \mathbf{1}, \tag{1}$$

where $\boldsymbol{\delta} = (\delta_1, \ldots, \delta_N)$ is a row vector of initial state probabilities $\left(\sum_{j=1}^{N} \delta_j = 1\right)$, $\boldsymbol{\Gamma} = (\gamma_{i,j})$ is a $N \times N$ state transition probability matrix with entries $\gamma_{i,j}$ corresponding to the probability of switching from state i at time t to state j at time $t+1$ $\left(\sum_{j=1}^{N} \gamma_{i,j} = 1\right)$, $\mathbf{P}(\mathbf{y}_{m,t}) = \mathrm{diag}\left(f\left(\mathbf{y}_{m,t} \mid S_{m,t} = 1\right), \ldots, f\left(\mathbf{y}_{m,t} \mid S_{m,t} = N\right)\right)$ is a $N \times N$ diagonal matrix with entries $f\left(\mathbf{y}_{m,t} \mid S_{m,t} = s\right)$ corresponding to the (state-dependent) conditional probability density of the observations $(\mathbf{y}_{m,t})$ given the state $S_{m,t} \in \{1, \ldots, N\}$ at time t, and $\mathbf{1}$ is a column vector of N ones (e.g. Zucchini *et al.* 2016). In HMMs for animal movement data, pooling across M individuals using a joint likelihood has been demonstrated to improve behavioural state assignment (Jonsen 2016). When explanatory individual covariates (e.g. age, sex, weight) are available, the likelihood can be extended to accommodate individual variation attributable to these factors through link functions for the model parameters (e.g. McClintock & Michelot 2018). Link functions (g) relate the natural scale parameters for each individual ($\boldsymbol{\theta}_m$) to a $T_m \times r$ design matrix ($\mathbf{X}_m$) and r-vector of working scale parameters ($\boldsymbol{\beta} \in \mathbb{R}^r$) such that $g(\boldsymbol{\theta}_m) = \mathbf{X}_m \boldsymbol{\beta}$.

Generic individual heterogeneity in HMMs is typically handled using individual-level fixed effects (termed "no pooling"; e.g. Patterson *et al.* 2009), discrete-valued random effects based on finite mixtures (e.g. Maruotti & Rydén 2009; McKellar *et al.* 2015; Towner *et al.* 2016; DeRuiter *et al.* 2017), or continuous-valued random effects (e.g. Altman 2007; Schliehe-Diecks *et al.* 2012). For individual fixed effects in the hidden state process, we have:

$$\mathcal{L}_{fix} = \prod_{m=1}^{M} \boldsymbol{\delta}_m \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,2}) \cdots \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m-1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m}) \mathbf{1}, \qquad (2)$$

where $\boldsymbol{\delta}_m = (\delta_{m,1}, \ldots, \delta_{m,N})$ and $\boldsymbol{\Gamma}_m = (\gamma_{m,i,j})$ is a $N \times N$ state transition probability matrix with entries $\gamma_{m,i,j}$ corresponding to the probability of individual m switching from state i at time $t-1$ to state j at time t. This model is highly parameterized with MN^2 state transition probabilities, but it avoids any distributional assumptions about the individual effects.

For mixed HMMs with discrete-valued random effects, we have:

$$\mathcal{L}_{mix} = \prod_{m=1}^{M} \sum_{k=1}^{K} \boldsymbol{\delta}^{(k)} \boldsymbol{\Gamma}^{(k)} \mathbf{P}(\mathbf{y}_{m,1}) \boldsymbol{\Gamma}^{(k)} \mathbf{P}(\mathbf{y}_{m,2}) \cdots \boldsymbol{\Gamma}^{(k)} \mathbf{P}(\mathbf{y}_{m,T_m-1}) \boldsymbol{\Gamma}^{(k)} \mathbf{P}(\mathbf{y}_{m,T_m}) \mathbf{1} \pi^{(k)}, \quad (3)$$

where $K \in \{1, \ldots, M-1\}$ is the number of mixtures, $\boldsymbol{\delta}^{(k)} = \left(\delta_1^{(k)}, \ldots, \delta_N^{(k)}\right)$, $\boldsymbol{\Gamma}^{(k)} = \left(\gamma_{i,j}^{(k)}\right)$ has entries $\gamma_{i,j}^{(k)}$ corresponding to the probability that an individual belonging to mixture k switches from state i at time $t-1$ to state j at time t, and $\boldsymbol{\pi} = \left(\pi^{(1)}, \ldots, \pi^{(K)}\right)$ are the mixture probabilities $\left(\sum_{k=1}^K \pi^{(k)} = 1\right)$. One would expect finite mixtures to be most appropriate for explaining individual variation attributable to unmeasured categorical covariates, but many such factors (e.g. age class, sex) can be measured in biotelemetry studies where individuals must be captured for tag deployment. It is less clear how appropriate finite mixtures are for "mopping up" unexplained continuous-valued variation.

For mixed HMMs with continuous random effects, we have:

$$\mathcal{L}_{cont} = \prod_{m=1}^{M} \int_{\mathcal{G}} \boldsymbol{\delta}_m \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,2}) \cdots \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m-1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m}) \mathbf{1} f\left(\boldsymbol{\Gamma}_m\right) d\boldsymbol{\Gamma}_m,$$

(4)

where $f\left(\boldsymbol{\Gamma}_m\right)$ is the continuous distribution for $\boldsymbol{\Gamma}_m$ and $\mathcal{G}$ its support. One would expect continuous random effects to be more parsimonious than fixed effects (Eq. 2), but this comes at the cost of additional distributional assumptions and computational complexity.

2.2 Maximum likelihood inference

We focus on maximum likelihood (ML) inference because HMMs can be fitted relatively quickly using ML methods and thereby facilitate large-scale simulation experiments. Standard ML inference by direct numerical maximization of the likelihood is straight-forward in principle for the null (Eq. 1), fixed (Eq. 2), and finite mixture (Eq. 3) models (Patterson *et al.* 2009; McKellar *et al.* 2015; Zucchini *et al.* 2016), and there are R (R Core Team 2020) packages specifically designed for fitting these HMMs (e.g. Visser & Speekenbrink 2010; McClintock & Michelot 2018). Note that to facilitate uncon-strained optimization and avoid overparameterization, $\boldsymbol{\Gamma}$ is typically re-parameterized using a multinomial-logit link function. For example, the state transition probabilities in the fixed effects model (Eq. 2) are parameterized in terms of $\beta_{m,i,j} \in \mathbb{R}$ such that $\gamma_{m,i,j} = \frac{\exp(\beta_{m,i,j})}{\sum_{l=1}^N \exp(\beta_{m,i,l})}$, where $\beta_{m,i,j} = 0$ for $i = j$.

The integral in the continuous random effects model (Eq. 4) poses additional chal-lenges that have historically made fitting by ML largely intractable (e.g. Altman 2007;

181 Schliehe-Diecks *et al.* 2012; DeRuiter *et al.* 2017). The simplest continuous random ef-
182 fect models typically assume independent and identically distributed Gaussian random
183 effects $z_{m,i,j} \overset{\text{iid}}{\sim} \mathcal{N}\left(\mu_{i,j}, \sigma_{i,j}^2\right)$ for $i \neq j$, $z_{m,i,j} = 0$ for $i = j$, and $\gamma_{m,i,j} = \frac{\exp(z_{m,i,j})}{\sum_{l=1}^{N} \exp\left(z_{m,i,l}\right)}$,
184 such that:

$$\mathcal{L}_{cont} = \prod_{m=1}^{M} \int_{\mathcal{Z}} \boldsymbol{\delta}_m \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,2}) \cdots \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m-1}) \boldsymbol{\Gamma}_m \mathbf{P}(\mathbf{y}_{m,T_m}) \mathbf{1} f\left(\mathbf{z}_m \mid \boldsymbol{\mu}, \boldsymbol{\sigma}\right) d\mathbf{z}_m,$$
(5)

where $f\left(\mathbf{z}_m \mid \boldsymbol{\mu}, \boldsymbol{\sigma}\right) = \prod_{i=1}^{N} \prod_{j \neq i} f\left(z_{m,i,j} \mid \mu_{i,j}, \sigma_{i,j}\right)$ is the joint density of $\mathbf{z}_m = (z_{m,i,j})_{i \neq j}$
and $\mathcal{Z} \in \mathbb{R}^{N(N-1)}$ its support. The resulting dimension of the integral is $N(N-1)$, which
for $N > 2$ is generally not feasible for direct maximization of the likelihood using stan-
dard numerical integration techniques such as Gaussian quadrature (e.g. Abramowitz &
Stegun 1964). This largely explains why custom Monte Carlo expectation-maximization
(e.g. Altman 2007) and Bayesian Markov chain Monte Carlo (e.g. McClintock *et al.*
2013) algorithms have often been employed for fitting HMMs with continuous random
effects.

Framed as a compromise between null and fixed effect models, Burnham & White
(2002) proposed an approximate but computationally simple method for continuous
random effect estimation based solely on maximum likelihood estimates from fixed ef-
fect models. Little used outside of capture-recapture applications, their approach was
originally developed for temporal random effects in the Cormack-Jolly-Seber model of
survival and, to our knowledge, has not been applied or investigated in contexts other
than capture-recapture. However, standard open population capture-recapture models
are simply special cases of HMMs (e.g. Pradel 2005; McClintock *et al.* 2020). Full tech-
nical details can be found in Burnham & White (2002), but we describe their approach
in the context of individual random effects for the state transition probabilities (Eq. 5)
in Section S1 of the Supplementary Material. Burnham & White (2002) demonstrated
that their approximate random effects estimator worked well for the Cormack-Jolly-
Seber model with a single temporal random effect on survival probability, but, as an
approximate method, it is not immediately clear whether or not its simple extension to
$N(N-1)$ individual random effects for the state transition probabilities in a N-state
HMM would also perform well. One known issue with this approach is that it becomes
unreliable when any $\gamma_{m,i,j}$ for the fixed effects model (Eq. 2) is estimated near 0 or 1,
and we suspect that such boundary issues will become more likely as M increases, T_m

decreases, and N increases. Bayesian analogues to the two-stage approach of Burnham & White (2002) could be less susceptible to these boundary issues (Hooten *et al.* 2016, 2019).

More recently, the R package Template Model Builder (`TMB`; Kristensen *et al.* 2016), which relies on reverse-mode automatic differentiation and the Laplace approximation for high dimension integrals, has made ML inference for continuous random effects much more tractable. `TMB` is less "plug-and-play" than the approach of Burnham & White (2002) because it currently requires advanced programming skills to custom code the HMM likelihood (Eq. 5) based on a `C++` template. In addition, little is currently known about how well the Laplace approximation performs for mixed HMMs or for sample sizes typical of animal telemetry studies (but for relevant applications see Albertsen *et al.* 2015; Auger-Méthé *et al.* 2017; Whoriskey *et al.* 2017; Benhaiem *et al.* 2018). Nevertheless, continuous random effect HMMs implemented using `TMB` can be fitted exceptionally fast, are amenable to more complex correlation structures, and likely do not suffer from the same boundary issues as the approximate approach of Burnham & White (2002). These promising capabilities of `TMB` facilitate large-scale simulation experiments for comparing the performance of these different approaches for modelling individual variation in the hidden state process.

3 Simulation study

3.1 Simulation methods

Based on 2-state HMMs commonly used in analyses of telemetry data (e.g. Franke *et al.* 2004; Morales *et al.* 2004), we performed a simulation experiment to evaluate the performance of models that include no effects, fixed effects, discrete random effects, and continuous random effects to account for individual heterogeneity in state transition probabilities. Data were simulated under five individual heterogeneity scenarios: 1) no individual heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0$) and $\mu_{1,2} = \mu_{2,1} = 0$, corresponding to $\gamma_{m,1,2} = \gamma_{m,2,1} = 0.5$ for $m = 1, \ldots, M$; 2) continuous random effects with "moderate" heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.202$) and $\mu_{1,2} = \mu_{2,1} = 0$, corresponding to a mean of 0.5 and standard deviation of 0.05 on the state transition probability scale; 3) continuous random effects with "high" heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.416$) and $\mu_{1,2} = \mu_{2,1} = 0$, corresponding to a mean of 0.5 and standard deviation of 0.10 on the state transition

probability scale; 4) $K = 2$ discrete random effects with $\pi^{(1)} = 0.6$, $\gamma_{1,2}^{(1)} = 0.5$, $\gamma_{2,1}^{(1)} =$
0.75, $\gamma_{1,2}^{(2)} = 0.75$, and $\gamma_{2,1}^{(2)} = 0.5$ (hereafter "mixA"); and 5) $K = 2$ discrete random
effects with $\pi^{(1)} = 0.6$, $\gamma_{1,2}^{(1)} = 0.75$, $\gamma_{2,1}^{(1)} = 0.75$, $\gamma_{1,2}^{(2)} = 0.25$, and $\gamma_{2,1}^{(2)} = 0.25$ (hereafter
"mixB"). These values were chosen to keep the state transition probabilities reasonably
centred around 0.5 (see Fig. S1 in Supplementary Material), thereby helping to reduce
potential parameter boundary issues during model fitting and prevent either state from
being relatively rare (Beyer *et al.* 2013). In all scenarios, we for simplicity assumed
$\boldsymbol{\delta}_m = (0.5, 0.5)$ for $m = 1, \ldots, M$.

Simulated sample sizes were chosen based on animal-borne telemetry studies that
typically tend to include relatively few individuals, but relatively long time series for
each individual (e.g. Morales *et al.* 2004; Langrock *et al.* 2012; McClintock *et al.* 2013;
Towner *et al.* 2016; DeRuiter *et al.* 2017; Isojunno *et al.* 2017). We included five levels
for the number of individuals $M \in \{5, 15, 30, 50, 100\}$ and three levels for the number
of observations per individual $(30 - 250, 110, 250)$. For scenarios with $30 - 250$ obser-
vations per individual, individuals were assigned to one of $T_m \in \{30, 50, 70, 150, 250\}$
in equal proportions such that $\sum_{m=1}^{M} T_m$ is identical for scenarios with $30 - 250$ or 110
observations per individual.

For the observation process $\mathbf{P}(\mathbf{y}_{m,t})$, we limited simulated observations to a single
data stream generated from a (state-dependent) gamma distribution for "step length",
$y_{m,t} \mid S_t = s \sim \Gamma(\mu_s^y, \sigma_s^y)$ for $S_t \in \{1, 2\}$, with varying degrees of overlap between
the states based on the mean (μ_s^y) and standard deviation (σ_s^y). These correspond to
"little" overlap $(\mu_1^y = 1, \mu_2^y = 10, \sigma_1^y = 1, \sigma_2^y = 2)$, "some" overlap $(\mu_1^y = 5, \mu_2^y = 10, \sigma_1^y =$
$2, \sigma_2^y = 2)$, and "much" overlap $(\mu_1^y = 5, \mu_2^y = 10, \sigma_1^y = 2, \sigma_2^y = 6)$. The Kolmogorov-
Smirnov test statistics for these distributions are respectively 0.99, 0.80, and 0.49,
where 0 indicates the distributions are identical and 1 indicates no overlap (Fig. 1).
Standard HMMs are known to perform poorly when the state-dependent distributions
overlap (e.g. Beyer *et al.* 2013; Jonsen 2016), but we included these scenarios to assess
whether or not the inclusion of individual effects somehow alters this behaviour. While
movement HMMs typically include two data streams (step length and turn angle), the
number of data streams is arbitrary for our purposes. We therefore chose a single
data stream in order to minimize the number of observations and parameters to be
estimated, thereby reducing run times and facilitating interpretation across a large
number of simulated scenarios.

Figure 1. *State-dependent observation distributions for "step length" in simulated scenarios with "little" (top panel), "some" (middle), and "much" (bottom) overlap.*

For each of the $5 \times 5 \times 3 \times 3 = 225$ scenarios, up to nine models were fitted to 400
simulated data sets using maximum likelihood methods. These models included 2-state
HMMs with no individual effects ("null"; Eq. 1), individual fixed effects ("fixed"; Eq.
2), discrete random effects with $K \in \{2, 3, 4, 5, 6\}$ mixtures ("mix2", "mix3", "mix4",
"mix5", and "mix6", respectively; Eq. 3), approximate continuous random effects esti-
mated from the "fixed" model based on Burnham & White (2002; "BW"), and contin-
uous random effects using numerical integration ("TMB"; Eq. 5). To reduce simulation
run times, discrete random effect models with $K = 5$ or $K = 6$ were only fitted if
the $K - 1$ mixture model resulted in a lower bias-corrected Akaike's Information Cri-
terion (AIC_c; Burnham & Anderson 2002) value relative to the $K - 2$ mixture model.
Simulated data were generated using the `simData` function in R package `momentuHMM`
(version 1.5.2; McClintock & Michelot 2018). The R package `TMB` (Kristensen *et al.*
2016) was used for fitting model TMB, and the `momentuHMM` function `fitHMM` was used
for fitting all other models. The `momentuHMM` function `randomEffects` was used for im-
plementing the BW approach based on the maximum likelihood estimates of the fixed
effects model returned by `fitHMM`. Code for simulating data and fitting all models can
be found in the Supplementary Material.

Estimator performance for $\boldsymbol{\sigma} = (\sigma_{1,2}, \sigma_{2,1})$, $\boldsymbol{\Gamma}_m = (\gamma_{m,i,j})$ for $m = 1, \ldots, M$, $\boldsymbol{\mu}^y =$
(μ_1^y, μ_2^y), and $\boldsymbol{\sigma}^y = (\sigma_1^y, \sigma_2^y)$ was evaluated based on mean bias, 95% confidence inter-
val coverage, and standard error (or confidence interval length). We also examined
the performance of the Viterbi algorithm for global state decoding (e.g. Zucchini *et al.*
2016) while accounting for agreement entirely due to chance (Beyer *et al.* 2013), as
well as the proportion of estimated state probabilities (based on local state decoding
using the forward-backward algorithm; e.g. Zucchini *et al.* 2016) with at least 0.05
and 0.20 probability assigned to the true state. To facilitate comparisons across mod-
els, individual-level estimates for state transition probabilities were derived from the
maximum likelihood estimates for the finite mixture models (see Section S2.1.3 in Sup-
plementary Material).

To evaluate the performance of AIC_c in selecting among competing models for in-
dividual heterogeneity in state transition probabilities, we calculated standard AIC_c
for the null, fixed, and finite mixture models, conditional AIC_c for the BW random
effects model (Burnham & White 2002), and marginal AIC_c for the TMB random ef-
fects model using $n = \sum_{m=1}^{M} T_m$ as the sample size. While the BW conditional AIC_c

is comparable with the AIC_c for the null, fixed, and finite mixture models, it's unclear
how well the marginal AIC_c for TMB will perform for selecting among fixed and ran-
dom effect models (e.g. Bolker *et al.* 2009; Gimenez & Choquet 2010). We therefore
also performed a likelihood ratio test (LRT) comparing the null and TMB models as
suggested by Gimenez & Choquet (2010). To our knowledge, there is currently no
straightforward way to calculate a conditional AIC even for simpler (non-Markov) ran-
dom effect models fitted in `TMB`; for example, the `TMB`-based generalized linear mixed
modelling R package `glmmTMB` (Brooks *et al.* 2017) only provides marginal AIC. We
calculated model-averaged estimates, standard errors, and 95% confidence intervals for
$\boldsymbol{\Gamma}_m$, $\boldsymbol{\mu}^y$, and $\boldsymbol{\sigma}^y$ based on AIC_c weights (Burnham & Anderson 2002) for four sets of
candidate models: 1) null and finite mixture models (hereafter "modMix"); 2) null,
fixed, and finite mixture models ("modFix"); 3) null, fixed, finite mixture, and BW
models ("modBW"); and 4) null, finite mixture, and TMB models ("modTMB").

To investigate estimator performance in the presence of a (measurable) continuous-
valued individual covariate, we performed an additional smaller set of simulations
with "little" overlap, $\sigma_{1,2} = \sigma_{2,1} \in \{0, 0.202, 0.416\}$, $M \in \{5, 15, 30, 50, 100\}$, and
the same three levels for the number of observations per individual ($30 - 250$, 110,
250). Two covariate scenarios were included: 1) $\mu_{0,1,2} = 0$, $\mu_{1,1,2} = 0.5$, $\mu_{0,2,1} = 0$,
and $\mu_{1,2,1} = -0.5$; and 2) $\mu_{0,1,2} = 0$, $\mu_{1,1,2} = 0$, $\mu_{0,2,1} = 0$, and $\mu_{1,2,1} = 0$, where
$z_{m,i,j} \overset{\text{iid}}{\sim} \mathcal{N}\left(\mu_{0,i,j} + x_m \mu_{1,i,j}, \sigma_{i,j}^2\right)$ and x_m is a measurable individual covariate drawn
from a standard normal distribution (Fig. S2). For the $3 \times 5 \times 3 \times 2 = 90$ scenar-
ios each consisting of 400 simulated data sets, we fit the fixed effect model and the
null, finite mixture, and continuous random effect models with and without covariate
effects (up to 17 models total). For the finite mixture models, each of the K mixtures
included context-specific $\mu_{0,i,j}^{(k)}$ and $\mu_{1,i,j}^{(k)}$ parameters (e.g. DeRuiter *et al.* 2017), from
which population-level covariate effects were derived for comparisons with other mod-
els (see Section S2.1.3 in Supplementary Material). Model-averaged estimates for $\mu_{1,i,j}$
were calculated from AIC_c weights for the models that included the covariate effect.
Summaries of estimator bias and precision for $\mu_{1,1,2}$ and $\mu_{1,2,1}$ were based on medians be-
cause with smaller sample sizes the means for these (unconstrained) parameters could
be heavily influenced by a small number of outliers when estimated state transition
probabilities fell on the boundary of the parameter space.

Simulation scenario results are presented using the nested loop plot of Rücker &

Schwarzer (2014). Similar to a time series plot, nested loop plots serve to present a large number of simulation results by putting all scenarios into a lexicographical order and arranging them consecutively along the horizontal axis. The quantity of interest (e.g. bias, coverage) is then plotted on the vertical axis. Although nested loop plots are likely unfamiliar to many ecologists and may initially require some getting used to, we find they can convey general patterns across 315 scenarios more effectively than large tables or trellis plots. For BW and modBW, results are only reported for those scenarios where at least 50 of the simulated data sets yielded admissible $\mathbf{\Gamma}_m$ estimates from the fixed effects model, where we considered any $\hat{\gamma}_{m,i,j} < 0.01$ or $\hat{\gamma}_{m,i,j} > 0.99$ as inadmissible. We expected the propensity of such boundary estimation issues to increase as the number of individuals (M) increased, the lengths of time series (T_m) decreased, and the degree of overlap in the state-dependent distributions (Fig. 1) increased.

3.2   Simulation results

3.2.1   State assignment

The degree of overlap between the (state-dependent) observation distributions was by far the most important factor for state estimation. The performance of each model declined as overlap increased, but, within each level of overlap ("little", "some", "much"), there was little difference among the individual models (Fig. 2). When there was "some" or "much" overlap, performance tended to slightly improve as individual heterogeneity, the number of individuals, and the lengths of the time series increased. The Viterbi algorithm for global state decoding did not perform well with "some" or "much" overlap, but estimated state probabilities based on local state decoding tended to assign at least 0.20 probability to the true state $> 90\%$ of the time. Compared to global state decoding, local state decoding is clearly better able to account for uncertainty in state assignment that is attributable to overlap in state-dependent observation distributions. However, the inclusion of individual fixed, discrete random, or continuous random effects made little difference in state assignment relative to the null model.

3.2.2   Random effect variance

Models that included continuous random effects (BW and TMB) performed best in terms of bias, coverage, and confidence interval length with "little" overlap, "high" heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0.416$), and larger sample sizes (Table 1, Fig. 3). Both

Figure 2. *Nested loop plots for the proportion of Viterbi-decoded states that were correctly classified (top) and the proportion of estimated state probabilities in which the true state included at least 0.20 (middle) or 0.05 (bottom) probability from 225 simulated scenarios. Scenarios are ordered from outer to inner loops by the degree of state-dependent distribution overlap ("Overlap"), individual heterogeneity ("Sigma"), number of individuals ("nbInds"), and length of time series ("nbObs"). Comparisons are for the null (light green), fixed (dark green), mix2 (pink), BW (blue), and TMB (purple) models.*

estimators tended to produce very wide confidence intervals for $\boldsymbol{\sigma}$ as the degree of overlap increased, the number of individuals decreased, and the length of the time series decreased. With "little" overlap and few individuals, BW tended to perform better than TMB, and, because its point estimates and confidence intervals can include zero, BW also tended to perform better than TMB for scenarios with no heterogeneity (i.e. $\sigma_{1,2} = \sigma_{2,1} = 0$; Fig. 3). However, with individual heterogeneity and "some" or "much" overlap, BW tended to underperform relative to TMB as the number of individuals increased and the length of the time series decreased. Under these conditions, the fixed model increasingly tended to estimate at least one state transition probability near a boundary, thereby making it unsuitable for the BW approach. This likely explains the increased negative bias for BW with "some" and "much" overlap, as the subset of simulated data sets that produced admissible $\boldsymbol{\Gamma}_m$ estimates from the fixed model will exhibit truncated tails for the random effect distributions (and hence smaller $\boldsymbol{\sigma}$). However, the fact that the bias tended to be greater for $\sigma_{2,1}$ than for $\sigma_{1,2}$ also suggests that the sampling variance-covariance matrix approximation of Burnham & White (2002) might be inadequate in accounting for the additional state uncertainty under scenarios with non-negligible overlap. TMB therefore appears to be more robust to overlap in state-dependent observation distributions and shorter time series with "moderate" to "high" heterogeneity, but, owing to negative bias and poor precision, neither TMB nor BW performed particularly well except in scenarios with "little' overlap, "high" heterogeneity, and at least $M = 50$ individuals.

3.2.3   State transition probabilities

All models generally exhibited little bias in state transition probabilities with "little" or "some" overlap, but performance was more variable in terms of confidence interval coverage and precision (Table 2, Fig. 4). Although the overall mean bias across all $\boldsymbol{\Gamma}_m$ was close to zero with "much" overlap (Table 2), this is somewhat misleading because the overlap tended to induce increasing negative bias for $\gamma_{m,1,2}$ and positive bias for $\gamma_{m,2,1}$ as the number of individuals decreased (Fig. 4, Tables S1–S2). With "little" overlap, the null model tended to perform best with no heterogeneity and BW tended to perform best with "moderate" to "high" heterogeneity because TMB tended to underestimate uncertainty (except when $M = 100$). The fixed model performed relatively well across all scenarios but, as expected, exhibited the largest variance of

Figure 3. *Nested loop plots for BW (blue) and TMB (purple) mean bias (top), 95% confidence interval coverage (middle), and confidence interval length (bottom) for $\sigma_{1,2}$ and $\sigma_{2,1}$ from 135 simulated scenarios with $\sigma_{1,2} = \sigma_{2,1} \in \{0, 0.202, 0.416\}$. Scenarios are ordered from outer to inner loops by individual heterogeneity ("Sigma"), degree of state-dependent distribution overlap ("Overlap"), number of individuals ("nbInds"), and length of time series ("nbObs"). Missing values for BW indicate scenarios with < 50 data sets producing admissible estimates for the state transition probabilities from the fixed effects model.*

Table 1. *BW and TMB overall mean percent relative bias, 95% confidence interval coverage, and percent confidence interval length for $\sigma_{1,2}$ and $\sigma_{2,1}$ by simulation design points for state-dependent distribution overlap, individual heterogeneity ($\boldsymbol{\sigma}$), number of individuals, and time series length.*

Model	Parm.	Overlap			$\boldsymbol{\sigma}$		No. individuals (M)					Time series length (T_m)			Overall
		Little	Some	Much	0.202	0.416	100	50	30	15	5	250	110	30 - 250	
							Percent relative bias								
BW	$\sigma_{1,2}$	-4.8	-12.0	-66.4	-25.3	-20.5	-15.7	-22.1	-25.3	-26.2	-23.9	-22.8	-26.2	-19.2	-22.9
BW	$\sigma_{2,1}$	-5.6	-27.0	-33.1	-23.5	-17.5	-16.5	-19.2	-21.4	-21.8	-22.8	-12.2	-25.4	-25.5	-20.5
TMB	$\sigma_{1,2}$	-10.8	-13.8	-24.4	-18.6	-14.0	-6.1	-9.2	-12.1	-18.9	-35.2	-13.0	-16.7	-19.3	-16.3
TMB	$\sigma_{2,1}$	-11.3	-14.6	-21.6	-19.1	-12.6	-5.9	-8.2	-12.4	-17.7	-35.1	-12.4	-16.6	-18.5	-15.8
							Coverage								
BW	$\sigma_{1,2}$	0.96	0.96	0.83	0.93	0.92	0.89	0.90	0.92	0.94	0.97	0.91	0.92	0.96	0.93
BW	$\sigma_{2,1}$	0.96	0.93	0.96	0.95	0.95	0.91	0.94	0.95	0.96	0.97	0.96	0.94	0.94	0.95
TMB	$\sigma_{1,2}$	0.94	0.93	0.93	0.91	0.96	0.96	0.96	0.95	0.93	0.88	0.96	0.92	0.92	0.94
TMB	$\sigma_{2,1}$	0.94	0.94	0.93	0.92	0.95	0.96	0.97	0.95	0.92	0.88	0.97	0.92	0.92	0.94
							Percent confidence interval length								
BW	$\sigma_{1,2}$	390	483	668	1274	371	182	250	324	472	1114	396	515	599	495
BW	$\sigma_{2,1}$	390	467	793	1340	388	190	279	354	501	1141	424	564	592	519
TMB	$\sigma_{1,2}$	341	467	916	1608	368	283	420	497	661	1012	447	654	622	574
TMB	$\sigma_{2,1}$	345	471	960	1647	384	287	430	505	683	1056	468	655	654	592

the estimators. Consistent with its performance for $\boldsymbol{\sigma}$ estimation, BW did not perform as well as TMB under "some" or "much" overlap, often exhibiting larger variances and asymmetric biases for $\gamma_{m,1,2}$ and $\gamma_{m,2,1}$.

The mix2 model generally performed best in the "mixA" and "mixB" finite mixture scenarios, but coverage was increasingly below nominal as the number of individuals increased, the length of time series decreased, and the degree of overlap increased. Underestimation of uncertainty by the mix2 model was unexpected under these scenarios, but the finite mixture models did not appear to always be able to adequately distinguish individual-level variability from sampling variability when estimating mixture probabilities for individuals with shorter time series. However, the mix2 model was less prone to reduced coverage for shorter time series under the more distinct "mixB" scenario with "little" or "some" overlap, so this behaviour also appears to depend on the specific characteristics of the mixture distributions. With larger sample sizes, all models except the null were fairly robust to data generated under $K = 2$ finite mixtures (albeit with inflated standard errors relative to mix2), but the finite mixture models were not robust to data generated under continuous random effects.

Figure 4. *Nested loop plots for mean bias (top row), 95% confidence interval coverage (middle row), and standard error (SE; bottom row) for $\gamma_{m,1,2}$ and $\gamma_{m,2,1}$ from 135 simulated scenarios with $\sigma_{1,2} = \sigma_{2,1} \in \{0, 0.202, 0.416\}$ (left column) and 90 scenarios with "mixA" or "mixB" finite mixtures (right column). Scenarios are ordered from outer to inner loops by the degree of state-dependent distribution overlap ("Overlap"), individual heterogeneity ("Sigma"), number of individuals ("nbInds"), and length of time series ("nbObs"). Comparisons are for the null (light green), fixed (dark green), mix2 (pink), BW (blue), and TMB (purple) models. Missing values for BW indicate scenarios with < 50 data sets producing admissible estimates for the state transition probabilities from the fixed effects model.*

Table 2. *Overall mean bias, 95% confidence interval coverage, and standard error (SE) for both $\gamma_{m,1,2}$ and $\gamma_{m,2,1}$ by simulation design points for state-dependent distribution overlap, individual heterogeneity, number of individuals, and time series length.*

Bias

Model	Overlap			Individual heterogeneity					No. individuals (M)					Time series length (T_m)			Overall
	Little	Some	Much	0	0.202	0.416	mixA	mixB	100	50	30	15	5	250	110	30 - 250	
null	-0.01	0.00	0.00	0.00	0.00	-0.01	-0.02	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
fixed	0.00	0.01	0.01	0.01	0.01	0.01	0.00	0.01	0.01	0.01	0.01	0.01	0.01	0.00	0.01	0.01	0.01
mix2	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
modMix	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
modFix	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
BW	0.00	-0.01	-0.05	-0.02	-0.02	-0.02	-0.02	-0.01	-0.01	-0.01	-0.02	-0.02	-0.02	-0.02	-0.02	-0.01	-0.02
modBW	0.00	-0.01	-0.02	0.00	0.00	-0.01	-0.01	0.00	0.00	0.00	0.00	-0.01	-0.01	0.00	-0.01	-0.01	-0.01
TMB	0.00	0.00	0.00	0.00	0.00	0.00	-0.01	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
modTMB	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

Coverage

Model	Overlap			Individual heterogeneity					No. individuals (M)					Time series length (T_m)			Overall
	Little	Some	Much	0	0.202	0.416	mixA	mixB	100	50	30	15	5	250	110	30 - 250	
null	0.32	0.46	0.57	0.93	0.59	0.40	0.22	0.11	0.32	0.37	0.42	0.50	0.64	0.40	0.47	0.47	0.45
fixed	0.95	0.95	0.90	0.94	0.94	0.94	0.93	0.93	0.95	0.95	0.94	0.93	0.91	0.95	0.94	0.92	0.94
mix2	0.75	0.81	0.81	0.92	0.69	0.54	0.89	0.91	0.72	0.76	0.79	0.82	0.86	0.79	0.80	0.78	0.79
modMix	0.80	0.84	0.82	0.94	0.72	0.65	0.90	0.91	0.76	0.80	0.83	0.85	0.87	0.83	0.83	0.80	0.82
modFix	0.89	0.88	0.83	0.94	0.74	0.83	0.91	0.93	0.81	0.85	0.87	0.90	0.92	0.90	0.87	0.85	0.87
BW	0.96	0.95	0.90	0.97	0.94	0.93	0.93	0.94	0.95	0.95	0.94	0.94	0.92	0.94	0.94	0.94	0.94
modBW	0.96	0.95	0.90	0.98	0.91	0.93	0.94	0.95	0.93	0.94	0.94	0.95	0.93	0.94	0.94	0.94	0.94
TMB	0.93	0.93	0.88	0.95	0.89	0.91	0.93	0.90	0.93	0.93	0.92	0.91	0.89	0.93	0.91	0.91	0.92
modTMB	0.92	0.91	0.87	0.95	0.85	0.88	0.90	0.91	0.90	0.90	0.90	0.90	0.89	0.92	0.90	0.88	0.90

SE

Model	Overlap			Individual heterogeneity					No. individuals (M)					Time series length (T_m)			Overall
	Little	Some	Much	0	0.202	0.416	mixA	mixB	100	50	30	15	5	250	110	30 - 250	
null	0.01	0.03	0.06	0.03	0.03	0.03	0.04	0.04	0.02	0.02	0.03	0.04	0.07	0.03	0.04	0.04	0.04
fixed	0.06	0.09	0.14	0.10	0.10	0.10	0.10	0.09	0.10	0.10	0.10	0.10	0.10	0.07	0.10	0.12	0.10
mix2	0.02	0.04	0.06	0.04	0.04	0.04	0.04	0.03	0.02	0.03	0.03	0.05	0.07	0.03	0.04	0.04	0.04
modMix	0.02	0.04	0.06	0.04	0.04	0.05	0.04	0.03	0.02	0.03	0.03	0.05	0.07	0.03	0.05	0.05	0.04
modFix	0.03	0.04	0.07	0.04	0.05	0.07	0.05	0.04	0.02	0.03	0.04	0.06	0.09	0.04	0.05	0.05	0.05
BW	0.06	0.08	0.14	0.08	0.08	0.09	0.09	0.08	0.07	0.08	0.08	0.09	0.10	0.07	0.09	0.10	0.08
modBW	0.04	0.06	0.09	0.05	0.06	0.08	0.05	0.05	0.03	0.04	0.05	0.07	0.09	0.05	0.06	0.07	0.06
TMB	0.04	0.06	0.09	0.04	0.06	0.07	0.08	0.08	0.06	0.06	0.06	0.07	0.08	0.05	0.07	0.07	0.07
modTMB	0.03	0.04	0.07	0.04	0.05	0.07	0.04	0.04	0.03	0.04	0.05	0.05	0.08	0.04	0.05	0.05	0.05

3.2.4 State-dependent distributions

There was not much variability in the performance of the models when estimating state-dependent probability distribution parameters $(\mu_1^y, \mu_2^y, \sigma_1^y, \sigma_2^y)$. With "little" overlap, all models performed well (see Figs S4–S5 and Tables S3–S6 in Supplementary Material). With smaller sample sizes under "some" or "much" overlap, bias tended to increase and coverage tended to decrease. Under these scenarios, increasing overlap generally resulted in positive bias for μ_1^y, large positive bias for μ_2^y, positive bias for σ_1^y, and negative bias for σ_2^y. Although coverage remained near-nominal under these scenarios, none of the models were able to recover unbiased point estimates of the state-dependent distribution parameters. As with state assignment (see Section 3.2.1), the inclusion of individual fixed, discrete random, or continuous random effects generally made little difference.

3.2.5 Model selection and multi-model inference

When the candidate model set was limited to null and finite mixture models, AIC_c model selection performed well for data generated under no heterogeneity ($\sigma_{1,2} = \sigma_{2,1} = 0$) and the finite mixture scenarios, with the generating model (null and mix2, respectively) generally receiving the most AIC_c support (Fig. S6) and the modMix model-averaged parameter estimates performing well (Figs S3–S5, Tables 2 and S3–S6). However, with moderate to high individual heterogeneity ($\sigma_{1,2} = \sigma_{2,1} > 0$), AIC_c tended to favor models with increasingly more finite mixtures as individual heterogeneity and sample sizes increased, with poor performance of model-averaged $\boldsymbol{\Gamma}_m$ estimates. When the candidate set of models was expanded to include the fixed model, performance was similar for the no heterogeneity and finite mixture scenarios, but the fixed model tended to receive greater support as individual heterogeneity increased, sample sizes increased, and the degree of overlap decreased (Fig. S6), resulting in improved (but still less than nominal) performance of the modFix model-averaged $\boldsymbol{\Gamma}_m$ estimates (Fig. S3, Tables 2 and S1–S2).

For the full candidate model set including the null, fixed, finite mixture, and BW models, AIC_c model selection generally performed well across most simulation scenarios, but support for the generating model tended to decline with smaller sample sizes and higher degrees of overlap (Fig. S6). In terms of $\boldsymbol{\Gamma}_m$ estimation, modBW generally exhibited less bias and greater precision than BW, but performance relative to TMB

declined with moderate or high heterogeneity as sample sizes and the degree of overlap increased (Tables 2 and S1–S2, Figs. 4 and S3). However, under these scenarios modBW tended to perform better than BW, indicating that AIC_c model averaging can help mitigate poorer performance of BW in scenarios with "some" or "much" overlap that tend to produce inadmissible Γ_m estimates from the fixed model.

The marginal AIC_c for TMB performed better than we expected, but proved to be conservative when selecting among fixed and random effect models for scenarios with moderate or high individual heterogeneity (Fig. S7). Under these scenarios, AIC_c tended to favor the null model as individual heterogeneity decreased, the degree of overlap increased, and sample sizes decreased. Unlike modBW, modTMB generally reduced coverage of Γ_m estimates relative to TMB except for the "mixB" scenarios (Tables 2 and S1–S2, Figs. 4 and S3). Likelihood ratio tests between the null and TMB models were less conservative and not as sensitive to the degree of overlap and sample sizes under these scenarios (Fig. S7). However, LRTs do not provide a means for selecting between discrete and continuous random effect models, and LRTs tended to strongly favor TMB over the null model when data were generated from finite mixtures (scenarios "mixA" and "mixB").

3.2.6   Covariate effects

In our limited set of simulations examining continuous-valued individual covariate effects, similar performance patterns to our full set of simulations (without covariate effects) were found for the the null, fixed, finite mixture, and continuous random effect models in terms of state assignment, parameter estimation, and AIC_c model selection (see Figs S8–S14). Both BW and TMB performed well in estimating the covariate effects ($\mu_{1,i,j}$), although for ($\mu_{1,1,2}, \mu_{1,2,1}$) = (0.5, −0.5) with smaller sample sizes and moderate to high heterogeneity, BW exhibited a small negative bias for $\mu_{1,1,2}$ and a small positive for $\mu_{1,2,1}$ that was mitigated by AIC_c model averaging (Figs 5 and S15, Tables S7–S8). In terms of coverage, BW again tended to perform slightly better than TMB under smaller sample sizes and higher levels of individual heterogeneity. While the finite mixture models performed better than the null model in terms of coverage, they generally exhibited greater bias and performance became increasingly poor as individual heterogeneity increased. While coverage of $\mu_{1,i,j}$ for the discrete random effect models increased with the number of mixtures, it was still well below nominal with

$_{484}$ $K = 4$ mixtures under higher levels of heterogeneity (Fig. 5, Tables S7–S8). Under
$_{485}$ these scenarios, coverage of the finite mixture models actually tended to become worse
$_{486}$ as sample sizes increased. Because coverage of the finite mixture models was poor when
$_{487}$ $\mu_{1,i,j} = 0$, there was clearly a greater risk of Type I error (i.e. inferring a covariate effect
$_{488}$ when there is none) when discrete random effects were used to "mop up" continuous
$_{489}$ individual variation. With fewer individuals ($M < 30$), we also found that using finite
$_{490}$ mixture models for this purpose can in some cases reduce correct state assignments by
$_{491}$ nearly 20% (Fig. S8). With AIC_c for the modMix candidate set tending to support
$_{492}$ models with both covariate effects and a large number of mixtures (Fig. S14), model
$_{493}$ averaging did little to mitigate this risk under these scenarios (Fig. S15, Tables S7–S8).

4   Example: long-finned pilot whales

$_{495}$ To help put our findings in context and illustrate some potential challenges that practi-
$_{496}$ tioners may encounter when applying mixed HMMs to animal telemetry data, we revisit
$_{497}$ a $N = 4$ state multivariate mixed HMM analysis of long-finned pilot whale biotelemetry
$_{498}$ data originally performed by Isojunno $et\ al.$ (2017). Full details can be found therein,
$_{499}$ but the data consist of 11 data streams believed to characterize "exploratory" (state 1),
$_{500}$ "foraging" (state 2), "crowded" (state 3), and "directed" (state 4) diving behaviours
$_{501}$ for $M = 15$ individuals, with T_m ranging from $50 - 254$ (median $= 148$). In order
$_{502}$ to limit the number of models in the candidate set, Isojunno $et\ al.$ (2017) first used
$_{503}$ model selection criteria to determine $N = 4$ was the optimal number of states under
$_{504}$ the null ($K = 1$) model, then used model selection criteria to choose among finite mix-
$_{505}$ ture random effect models (up to $K = 3$), and finally used this model to investigate
$_{506}$ individual and time-dependent explanatory covariates (e.g. size class, sonar exposure)
$_{507}$ for the state transition probabilities.

$_{508}$ We focus on the second stage of this analysis, where they used AIC and the Bayesian
$_{509}$ Information Criterion (BIC; e.g. Burnham & Anderson 2002) to select the best-supported
$_{510}$ random effect model for subsequent covariate modelling and model selection. They
$_{511}$ found conflicting results based on AIC and BIC, with AIC favoring $K = 3$ mixtures
$_{512}$ (5.2 unit decrease in AIC relative to the null model) and BIC strongly favoring the
$_{513}$ null model with $K = 1$. Faced with this apparent conundrum, Isojunno $et\ al.$ (2017)
$_{514}$ sided with BIC to "avoid selection of overly complex models" given the relatively "weak

Figure 5. *Nested loop plots for median bias (top row), mean 95% confidence interval coverage (middle row), and median standard error (SE; bottom row) for covariate effects $\mu_{1,1,2}$ and $\mu_{1,2,1}$ from 90 simulated scenarios with "little" overlap and $(\mu_{1,1,2}, \mu_{1,2,1}) \in \{(0,0), (0.5, -0.5)\}$. Scenarios are ordered from outer to inner loops by the data-generating values for the covariate effect ("Covariate", where "No" = $(0,0)$, "Yes" = $(0.5, -0.5)$), individual heterogeneity ("Sigma"), number of individuals ("nbInds"), and length of time series ("nbObs"). Comparisons are for the null (light green), mix2 (pink), mix3 (light orange), mix4 (dark orange), BW (blue), and TMB (purple) models.*

support for any random effects" afforded by AIC, and proceeded with covariate model fitting and selection under the null model ($K = 1$) with no individual random effects on state transition probabilities.

Our simulation study may be able to help shed some light on the discrepancy between AIC and BIC in this case. When comparing AIC_c and BIC for simulation scenarios with "little" overlap, the biggest discrepancies between these model selection criteria occur with data generated under moderate to high individual heterogeneity (see Fig. S16 in Supplementary Material). When the candidate model set is limited to null and finite mixture models, BIC strongly supports the null model under moderate heterogeneity and finite mixture models only under high heterogeneity with larger sample sizes. Conversely, AIC_c tends to favor finite mixture models except under moderate heterogeneity with smaller sample sizes. When the "true" TMB model is included in the candidate set, this discrepancy between AIC_c and BIC largely disappears (Fig. S16). There are of course fundamental inferential differences between AIC_c and BIC (e.g. Aho *et al.* 2014), but the model selection discrepancy in the pilot whale analysis of Isojunno *et al.* (2017) could therefore be in part attributable to individual heterogeneity that is not well explained by the null or finite mixture models.

To explore this further, we re-analyzed the pilot whale data by fitting the null, fixed, finite mixture (up to $K = 4$), and TMB models using the same methods described in Section 3, but with $\boldsymbol{\delta}_m$ assumed to be the stationary distribution (as in Isojunno *et al.* 2017) instead of freely estimated (see Supplementary Material for data and R code). In addition to AIC_c, we calculated standard BIC for the null, fixed, and finite mixture models, as well as the marginal BIC for TMB, using $n = \sum_{m=1}^{M} T_m = 2314$ for the sample size (as in Isojunno *et al.* 2017). Unfortunately, the fixed model yielded $\boldsymbol{\Gamma}_m$ estimates on the boundary, thereby making this data set inadmissible for the BW model. With boundary issues becoming more likely as the number of individuals increases, the lengths of time series decrease, and the number of states increases, this highlights a key limitation of the BW approach in practice.

Despite due diligence by Isojunno *et al.* (2017) in exploring the likelihood surface using 50 sets of randomly drawn starting values for optimization, we found that their finite mixture models failed to converge to global maxima. Relative to those reported by Isojunno *et al.* (2017), our fits increased the log likelihood for the mix2 and mix3 models by 14.6 and 36.7 units, respectively (Table 3). This highlights a common pitfall

Table 3. *Model selection results for the long-finned pilot whale example. Results include* AIC_c *weights,* ΔAIC_c, *BIC weights,* ΔBIC, *negative log-likelihood value (NLL), and number of parameters (nPar).*

Model	AIC_c weight	ΔAIC_c	BIC weight	ΔBIC	NLL	nPar
TMB	0.65	0.00	0.99	0.00	18459.69	84
mix3	0.35	1.27	0.00	79.37	18445.14	98
mix4	0.00	15.75	0.00	166.03	18438.12	111
mix2	0.00	45.37	0.00	50.96	18481.29	85
null	0.00	75.71	0.01	8.47	18510.40	72
fixed	0.00	86.78	0.00	933.87	18322.38	240

⁵⁴⁸ when attempting to fit complex mixed HMMs to relatively small data sets, where flat
⁵⁴⁹ likelihood surfaces, local minima, and numerical instability can become increasingly
⁵⁵⁰ problematic as the number of states and/or parameters increase. Indeed, it's certainly
⁵⁵¹ possible that our fits also failed to converge to the global maxima, although we were
⁵⁵² unable to improve them any further using hundreds of random normal perturbations
⁵⁵³ of the maximum likelihood estimates as starting values for the optimization.

⁵⁵⁴   With both AIC_c and BIC now favoring TMB (Table 3), this behaviour is consistent
⁵⁵⁵ with our simulation results when candidate model sets limited to null and finite mixture
⁵⁵⁶ models were fitted to data generated under continuous random effects (Fig. S16).
⁵⁵⁷ The LRT between the null and TMB model with $N(N-1) = 12$ random effects also
⁵⁵⁸ favors TMB $(\sum_{r=0}^{12} 2^{-12}\binom{12}{r}\chi_r^2 = 101.4,\ P < .001)$. Thus whether one prefers AIC_c,
⁵⁵⁹ BIC, or LRT, there is clearly evidence of individual variation in the state transition
⁵⁶⁰ probabilities that is not well explained by null or finite mixture models. As could be
⁵⁶¹ expected for relatively short time series with $N = 4$ states, some of the random effect
⁵⁶² variance estimates were imprecise (Table 4), particularly for state transitions that were
⁵⁶³ relatively rare (Fig. 6). Evidence of individual variation was greatest for transitions
⁵⁶⁴ from the "exploratory" and "directed" states, and, based on the results of Isojunno
⁵⁶⁵ *et al.* (2017), this variation was not well explained by any of the individual covariates
⁵⁶⁶ included in their analysis. However, it is possible that these explanatory covariates
⁵⁶⁷ could now better account for any additional variation that is not already well explained
⁵⁶⁸ by the individual random effects.

⁵⁶⁹   Although we have found new evidence of individual variation in the state transition
⁵⁷⁰ probabilities, accounting for this heterogeneity made little impact on state assignment
⁵⁷¹ and estimated activity budgets. Consistent with our simulation results (see Fig. 2),

Figure 6. *Estimated state transition probabilities (and 95% confidence intervals) among $N = 4$ states (1 = "exploratory", 2 = "foraging", 3 = "crowded", 4 = "directed") for $M = 15$ long-finned pilot whales from the TMB model including continuous individaul-level random effects. Each of the $4 \times 4 = 16$ state transition probabilities is labeled on the y-axis as "$i\ ->\ j$", indicating the probability of switching from state i to state j.*

Table 4. *Estimates, standard errors (SE), 95% confidence intervals (Lower, Upper), percent coefficient of variation (%CV), and percent confidence interval length (%CIL) for individual random effect variance parameters (σ) from the TMB model fitted to the long-finned pilot whale data.*

Parameter	Estimate	SE	Lower	Upper	%CV	%CIL
$\sigma_{1,2}$	0.47	0.27	0.17	1.35	58	251
$\sigma_{1,3}$	1.17	0.69	0.40	3.39	59	256
$\sigma_{1,4}$	1.16	0.30	0.71	1.92	26	104
$\sigma_{2,1}$	0.56	0.41	0.15	2.03	74	336
$\sigma_{2,3}$	0.25	2.96	0.00	19.63	1173	7766
$\sigma_{2,4}$	0.03	0.34	0.00	2.26	1195	7895
$\sigma_{3,1}$	0.02	0.38	0.00	2.35	1926	11773
$\sigma_{3,2}$	0.22	7.62	0.00	40.52	3498	18611
$\sigma_{3,4}$	0.91	0.39	0.41	2.04	43	179
$\sigma_{4,1}$	0.55	0.18	0.29	1.04	34	138
$\sigma_{4,2}$	1.14	0.40	0.58	2.24	36	146
$\sigma_{4,3}$	0.79	0.32	0.37	1.68	40	166

Viterbi-decoded states for the null and TMB models were in agreement 94% of the time. However, while "foraging" and "crowded" state assignments were largely unchanged, estimated overall activity budgets changed slightly for the "exploratory" state (36% for null, 33% for TMB) and the "directed" state (36% for null, 40% for TMB).

We do not intend to be critical of Isojunno *et al.* (2017) for limiting their candidate model set to finite mixtures or failing to achieve convergence for these complex models. They focused on discrete random effect models presumably because maximum likelihood inference for HMMs with continuous random effects has historically been very difficult (e.g. Altman 2007; Langrock *et al.* 2012; Schliehe-Diecks *et al.* 2012). Discrete random effects have been promoted as a practical alternative for movement HMMs (e.g. McKellar *et al.* 2015; Towner *et al.* 2016; DeRuiter *et al.* 2017), and the potential for TMB (Kristensen *et al.* 2016) as a tool to overcome such problems has only recently begun to be recognized by movement ecologists (e.g. Auger-Méthé *et al.* 2017). False convergence is notoriously difficult to assess, and it was entirely due to luck that our random draws of starting values for the finite mixture models happened to converge to parameter estimates with higher likelihood. Finally, as state assignment and calculating activity budgets was the primary purpose of the mixed HMM analysis performed by Isojunno *et al.* (2017), their main results and conclusions would likely be largely

unaltered if they were instead based on a model that accounted for this individual variation. However, this would not be the case had their primary objective been to quantify individual heterogeneity in state transition probabilities.

If the primary objective of this analysis had been to gain an understanding of heterogeneity in individual movement behaviour, it is not clear how one would proceed with such a complex random effects model. Interpreting generic individual variation is already difficult in simpler finite mixture models (e.g. Towner *et al.* 2016; DeRuiter *et al.* 2017), and it would be challenging to concoct a biological story explaining these various pieces of evidence for individual heterogeneity across $N(N-1) = 12$ continuous random effects (Table 4) and $MN^2 = 240$ state transition probabilities (Fig. 6). The random effects could reflect unexplained population-level behavioural heterogeneity attributable to different animal personalities (e.g. Réale *et al.* 2007; Hertel *et al.* 2020), but they could also simply be an artifact of deployments of differing lengths being observed in different environmental and behavioural contexts (e.g. Towner *et al.* 2016; DeRuiter *et al.* 2017). This is very difficult to determine, and we will not attempt to do so here. However, this highlights the challenge of interpreting random effects in biological terms.

5 Discussion

We have investigated the benefits of accounting for individual variation in the hidden state process of HMMs from a practical perspective, with emphasis on data sets common to animal movement behaviour biotelemetry studies. While our simulations covered a wide range of scenarios, they were by no means exhaustive. For example, we did not investigate pathological or degenerate cases with "bathtub-shaped" distributions for the state transition probabilities and instead focused on less extreme forms of individual heterogeneity. We did not examine sampling scenarios more typical of capture-recapture (Pradel 2005) or species occurrence (Gimenez *et al.* 2014) HMMs, which often involve a larger number of individuals and shorter time series than the scenarios examined here. We also limited our study to maximum likelihood inference via direct numerical maximization of the likelihood, although we believe similar patterns would emerge using expectation-maximization (e.g. Altman 2007) or Bayesian analysis methods (e.g. Turek *et al.* 2016).

We focused on individual-level random effects in the hidden state process because these have received the most attention in the movement modelling literature so far (e.g. McKellar *et al.* 2015; Towner *et al.* 2016; DeRuiter *et al.* 2017; Isojunno *et al.* 2017). Importantly, we have not examined individual effects on the (state-dependent) observation distribution parameters and would not necessarily expect the same patterns to emerge from a similar investigation of individual variation in the observation process. While this also warrants further investigation, there is already some evidence for the importance of accounting for individual variation in the state-dependent distributions (e.g. Altman 2007; Langrock *et al.* 2012; Schliehe-Diecks *et al.* 2012; McClintock *et al.* 2013; Rueda *et al.* 2013; Carter *et al.* 2020). In particular, we would expect unexplained individual variation in the observation process to be more consequential for state assignment.

To help avoid boundary estimation issues and state rarity with higher levels of heterogeneity, we largely centred state transition probabilities around 0.5 in our simulation scenarios. This could be viewed as a "worst-case scenario" in terms of state persistence because these time series will on average have relatively short sojourn times. HMMs tend to perform better as serial dependence in the data increases, particularly when state-dependent observation distributions overlap (e.g. Beyer *et al.* 2013; Langrock *et al.* 2018). Thus there may be specific conditions (e.g. "much" overlap with much stronger serial dependence) where discrete random effects may perform better as an approximation for continuous variation. However, the consequences of this model misspecification will be dependent on the form of heterogeneity, the amount of serial dependence, and other qualities of the data. We showed that this approximation is not generally robust, and, in practice, it may be very difficult to determine if it is reliable when truth is unknown.

Our simulations and case study have highlighted some important considerations for practitioners contemplating the inclusion of individual random effects in their own analyses. As our results have provided much to digest, we break down these considerations under the following themes: 1) When to account for individual variation?; 2) How to account for individual variation?; 3) Is there evidence of individual variation?; and 4) How to interpret individual variation?

5.1 When to account for individual variation?

Accounting for generic individual variation comes at significant cost in terms of implementation and computation, particularly for random effects. When weighing the costs and benefits of random effects, three primary considerations are the study objectives, sample size, and model complexity. If the objective is strictly state assignment, then the inclusion of individual effects on the hidden state process makes little difference in terms of inference. Many movement HMM applications primarily focus on state assignment for inferences about behaviour, activity budgets, and/or resource selection (e.g. Beyer *et al.* 2013; Roever *et al.* 2014; Pirotta *et al.* 2018), with little emphasis on quantifying or understanding heterogeneity in state transition probabilities. Under these circumstances, random effects in the hidden state process simply may not be worth the additional effort.

With smaller sample sizes typical of animal biotelemetry studies (e.g. $M < 50$ and $T_m < 250$), inferences about individual heterogeneity based on continuous random effects will tend to be weak. This is due to poor precision for the random effects variance parameters, which also tend to be underestimated with smaller sample sizes. However, if inference about individual variation in state transition probabilities is a primary objective of a study, then random effect models should certainly be explored as part of the analysis. When properly specified and fitted, individual random effects never hurt and tend to decrease bias and increase coverage (relative to the null model) and increase precision (relative to the fixed effects model). Using individual random effects to "mop up" unexplained variation can also improve our ability to reliably estimate the effects of measurable covariates on the hidden state process.

5.2 How to account for individual variation?

Continuous random effect models (BW and TMB) proved more robust to the underlying form of individual heterogeneity than null or discrete random effect models. The approximate approach of BW generally performed as well as (or better) than TMB when there was little overlap in the observation distributions, but the TMB model proved more robust to higher degrees of overlap. Thus if custom coding a continuous random effects model using TMB is beyond the skill set of a practitioner, the BW approach can be a reliable alternative in limited cases with very distinct observation

distributions. This often applies to animal movement HMMs describing very different modes of movement (e.g. "foraging" and "transit"), but the degree of overlap should be investigated (e.g. Beyer *et al.* 2013) before proceeding with the BW approach. As demonstrated in the long-finned pilot whale example, BW is also of limited utility due to boundary issues that are more likely to occur as the number of states increases, the number of individuals increases, the lengths of time series decrease, and the degree of overlap increases. The TMB model does not suffer from these limitations, and we generally found the Laplace approximation as implemented in TMB to perform reasonably well across all HMM scenarios examined.

Discrete random effects are generally the best option only when individual heterogeneity is attributable to unmeasured categorical factors. While many categorical factors (e.g. sex, age class) can often be measured when deploying telemetry tags, others such as disease or breeding status often cannot. We do not advise using discrete random effects to "mop up" continuous individual variation as this can underestimate uncertainty in state transition probabilities, lead to spurious inferences about covariate effects, and negatively impact state assignment based on global state decoding. If inference about individual variation in state transition probabilities is the primary objective, then investigating both discrete and continuous random effect models appears to be worth the effort for potential gains in terms of parameter estimation and state assignment. Yet care must be taken when fitting these complicated models. As illustrated by the long-finned pilot whale example, false convergence of random effect models can be particularly problematic as the number of states increases and sample sizes decrease.

Individual covariates are arguably the best way to account for (and learn about) potential factors driving individual heterogeneity in the hidden state process. Relative to random effect models, covariate models are also much easier to implement using existing software (Table 5). When designing telemetry studies, careful thought should be put towards identifying and collecting any measurable individual covariates that may be informative. When available covariates do not sufficiently explain individual heterogeneity, then random effects are certainly worth pursuing as a more parsimonious alternative to individual fixed effects. Discrete random effects and the approximate continuous random effect approach of Burnham & White (2002) can be implemented using R package momentuHMM (McClintock & Michelot 2018). If the user is familiar

Table 5. *R packages for fitting HMMs with individual variation in the hidden state process using maximum likelihood methods.*

Package	Individual covariates	Random effects Discrete	Random effects Continuous	Reference
moveHMM	✓			Michelot *et al.* (2016)
msm	✓			Jackson (2011)
depmixS4	✓			Visser & Speekenbrink (2010)
momentuHMM	✓	✓	✓[†]	McClintock & Michelot (2018)
TMB	✓	✓	✓	Kristensen *et al.* (2016)

[†] Continuous random effects are limited to the approximate approach of Burnham & White (2002).

enough with the `C++` template to custom code HMMs from scratch, then `TMB` (Kristensen *et al.* 2016) can be used to implement any of the models. `TMB` will also often be faster than optimization routines that rely on numerical differentiation.

5.3 Is there evidence of individual variation?

There are several ways to evaluate the strength of evidence for individual variation. These can include null hypothesis tests for the estimated coefficients of individual effects (for covariate, fixed, or discrete random effect models) or random effect variance estimates (for continuous random effect models). Estimated coefficients or random effect variances that are significantly different from zero typically indicate evidence of individual variation. Model selection criteria such as AIC or BIC can also be used for selecting or averaging models from a candidate set. We found the conditional AIC to work well for selecting among null, fixed, finite mixture, and BW models when sample sizes were larger and the observation distributions more distinct. The marginal AIC also worked reasonably well for selecting among the null, finite mixture, and TMB models under these scenarios, but it was conservative relative to the null likelihood ratio test. If inference about individual variation in the hidden state process is the primary objective and the exact form of any unexplained heterogeneity is unknown, our results suggest that candidate model sets should include models with both discrete and continuous random effects. This was evident in the long-finned pilot whale example, where we found stronger evidence for continuous random effects than for finite mixture models.

5.4 How to interpret individual variation?

Interpretation of measured individual covariate effects is straightforward, but it can be difficult to interpret generic individual-level effects. Discrete random effect models are sensitive to small sample sizes and can tend to identify spurious "behavioural contexts" that are an artifact of shorter time series (e.g. Towner *et al.* 2016; DeRuiter *et al.* 2017). In our simulation study, we also found individual fixed effect models to be susceptible to these small sample issues. Care should therefore be taken to avoid overinterpretation of individual fixed effects or finite mixture distributions. Continuous random effect models will tend to be less susceptible to small sample issues because they will shrink effect sizes for individuals with shorter time series toward the population mean. However, as demonstrated in the long-finned pilot whale example, this makes continuous random effects no less difficult to interpret in biological terms. Unlike explanatory individual covariates, we do not learn that much from generic individual random effects. We can learn that there appears to be evidence of individual variation in the hidden state process, but from evolutionary theory we already understand that biological parameters must in reality vary across individuals. Perhaps the most useful inference from evidence of generic individual heterogeneity is that there remains a need to identify and collect more informative covariates that can help explain the drivers of the underlying variation in the hidden state process.

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Data accessibility

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