simATAC: A Single-cell ATAC-seq Simulation Framework

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Abstract

Single-cell Assay for Transposase-Accessible Chromatin sequencing (scATAC-seq) identifies regulated chromatin accessibility modules at the single-cell resolution. Robust evaluation is critical to the development of scATAC-seq pipelines, which calls for reproducible datasets for benchmarking. We hereby present the simATAC framework, an R package that generates a scATAC-seq count matrix, highly resembling real scATAC-seq datasets in library size, sparsity, and averaged chromatin accessibility signals. simATAC deploys statistical functions derived from analyzing 90 real scATAC-seq cell groups to model read distributions. simATAC provides a robust and systematic approach to generate *in silico* scATAC-seq samples with cell labels for a comprehensive tool assessment.

Keywords: Single-cell; scATAC-seq; Simulator; Software

Background

Single-cell sequencing has revolutionized and expedited our understanding of the structure and function of cells at unprecedented resolution. This technology resolves a fundamental limitation of bulk sequencing, which averages signals over a large number of cells resulting in obscured biological heterogeneity among individual cells [1]. The assay for transposase-accessible chromatin sequencing (ATAC-seq) measures the openness of chromatin, a proxy for activity of DNA binding proteins [2–4]. Single-cell ATAC-seq (scATAC-seq) has opened up vast fields of applications, including extracting accessibility and co-accessibility patterns of genomic regions to identify cell-type-specific enhancers, chromatin heterogeneity, and transcription factor activities.

The rapid advancement of scATAC-seq technology gives rise to the development of computational tools for scATAC-seq data analysis, and the integrative analysis of transcriptomic and epigenomic profiles [5–7]. Though simulated datasets with known labels have been the most common approach to benchmark the performance of analytical pipelines, there is no existing standard practice or simulation tool available to generate synthetic scATAC-seq datasets. Furthermore, due to the sparsity and noisy nature of scATAC-seq data, generating synthetic samples that resemble real datasets is challenging. Many existing scATAC-seq analytical pipelines assessed their performance solely based on real datasets [8–14]. Some studies generated simulated data by downsampling reads from bulk ATAC-seq data [15–19] or deploying ad-hoc simulation methods [20–23]. However, these simulation methods were implemented as part of the development or evaluation of scATAC-seq pipelines and were usually incompletely documented, resulting in a lack of reproducibility.

scATAC-seq analytical pipelines usually consist of pre-processing (read quality control and alignment), core analysis (feature matrix generation) and downstream analyses (e.g. cell type clustering). A feature matrix summarizes the filtered reads from BAM files by counting the number of aligned reads that overlap within the defined genomic regions. The features represent a subset of genomic regions with specified genomic positions, nucleotide patterns, or biological functions [8, 9, 24]. A commonly used feature matrix for scATAC-seq is the peak-by-cell matrix that captures the highest accessibility signals from genomic regions (peaks) obtained from bulk ATAC-seq or single cells. However, a sufficient number of cells are required to identify such peaks, and consequently, the peak-by-cell feature matrix usually fails to recognize the rare cell type regulatory patterns in aggregated signals [15].

Alternatively, the bin-by-cell feature matrix is generated by segmenting the whole genome into uniformly-sized non-overlapping "bins" and mapping the read counts in each bin [15]. Uniform segmentation of the genome provides unbiased detection of chromatin accessibility, and enables pattern extraction of genome-wide accessibility profiles using both significant and non-significant distinguishable dynamics between cells.

We hereby propose simATAC, a scATAC-seq simulation framework that generates unbiased simulated

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samples resembling real scATAC-seq data. Given a real scATAC-seq feature matrix as input, simATAC estimates the statistical parameters of the mapped read distribution by cell type, and generates a synthetic count array that captures the unique regulatory landscape of a group of cells with similar biological characteristics. We demonstrate that the synthetic samples generated by simATAC highly resemble real scATAC-seq datasets in library sizes, sparsity (proportion of zero entries) and averaged chromatin accessibility signals.

Results

simATAC framework

simATAC deploys statistical distributions to model the properties of a bin-by-cell count matrix for a group of cells with similar biological characteristics. The main modelling parameters include read coverage of cells (library size), non-zero cell proportion in each bin, and the average of counts per bin (bin mean). Bin-by-cell matrix quantifies the number of open chromatin read fragments falling into the non-overlapping fixed-length bins (5 kbp windows) across the whole genome. For each user-input, simATAC performs two core simulation steps: (i) estimating the model parameters based on the input bin-by-cell matrix, including the library sizes of the cells, the non-zero cell proportions of each bin and the read average of each bin; (ii) generating a bin-by-cell matrix that resembles the original input scATAC-seq data by sampling from Gaussian mixture and polynomial models with the estimated parameters. simATAC outputs a count matrix as a SingleCellExperiment (SCE) object [25], with additional options to convert it to other types of feature matrices. Figure 1 summarizes the simulation architecture of simATAC. The statistical modelling of simATAC is discussed in further details in the next sections and Methods.

Library size

Library size refers to the number of aligned reads per cell. simATAC models cells' log-transformed library sizes through a Gaussian mixture model (GMM) with two components whose parameters are estimated based on the user-input real scATAC-seq data. With the estimated parameters, simATAC randomly samples library sizes of C single cells based on Eq. (1).

$$\log_2(l_i') \sim w \times \mathcal{N}(\mu_1, \sigma_1^2) + (1-w) \times \mathcal{N}(\mu_2, \sigma_2^2) \quad (1)$$

where l_i' is the simulated library size for the ith simulated single-cell. See Table 1 for the detailed definition of the Gaussian mixture model parameters.

Previous studies have shown that the library sizes of cells significantly affect the identification of cell types

Table 1 Input parameters in simATAC simulation step.

Parameter	Symbol	Description
Library size mean	μ_1, μ_2	The estimated means of two Gaussian modals of library size.
Library size standard deviation	σ_1, σ_2	The estimated standard deviations of two Gaussian modals of library size.
Library size weight	w	The estimated weight parameter of the first Gaussian modal.
Non-zero cell proportion	P	The proportion of non-zero cells in real bin-by-cell matrix.
Polynomial coefficients	β	The estimated coefficients of polynomial model fitted to the relation between bin non-zero cell proportions and bin means.

[15–17, 19, 21]. A larger library size usually indicates higher sequencing coverage, thus providing more accurate chromatin accessibility information. Since the library sizes of scATAC-seq usually vary across different experiments, simATAC offers users the flexibility to adjust the library sizes from low to high coverage based on their needs.

Bin non-zero cells proportion

Sparsity is the inherent nature of scATAC-seq data [15, 21, 26], which results in a large proportion of zero entries in the bin-by-cell matrix. Let $M_{j,i}$ denote the number of reads that fall into the bin j of cell i for B bins. If $M_{j,i} > 0$, then it is considered as a non-zero entry. The number of cells with non-zero entries within a bin is associated with the chromatin accessibility in the corresponding genomic region. simATAC estimates the proportion of cells with non-zero entries for the jth bin, p_j, based on the user-input real scATAC-seq bin-by-cell matrix, and determines if the status of an entry in the simulated count matrix is zero or non-zero based on a Bernoulli distribution:

$$X_{j,i} \sim Bernoulli(p_j) \quad (2)$$

If $X_{j,i} = 1$, the read count of cell i at bin j is non-zero, i.e. $M_{j,i} > 0$. If $X_{j,i} = 0$, the read count of cell i at bin j is set to zero, i.e. $M_{j,i} = 0$. The non-zero proportion of bin j, p_j', of the simulated bin-by-cell matrix is then defined as

$$p_j' = \sum_{i=1}^{C} X_{j,i}/C \quad (3)$$

Bin mean

The extent of genome accessibility leads to the variations in the number of sequenced reads falling into the

Figure 1 The simATAC simulation framework. The red circles represent values directly extracted from the user-supplied bin-by-cell matrix, the white squares represent estimated parameters, and the brown circles represent the simulated values. simATAC initially estimates the library sizes, the non-zero cell proportions and the bin means from the input cell group (including cells having similar biological characteristics). simATAC generates the library sizes with a Gaussian mixture distribution, the zero and non-zero status with a Bernoulli distribution, and the bin means with a polynomial regression model linking to the non-zero cell proportion. The synthetic counts are sampled from a Poisson distribution whose mean is the cell library size adjusted by the bin mean. simATAC offers optional sparsity adjustment factor γ and noise parameters to adjusts the sparsity and noise level of the synthetic counts generated from the Poisson distribution. Default values for the main parameters are embedded in the simATAC framework in case no user-supplied input is given.

fixed-length bins, and consequently, the variations in the average of the reads in each bin. More accessible regions potentially lead to a larger bin means, that is, the more cells with non-zero entries are mapped to that

region. We observed a polynomial regression relation between the non-zero cell proportions and bin means in each cell group in the samples used for simATAC modelling. simATAC simulates the average of the read

counts at bin j, m'_j, with a fitted polynomial regression model with the non-zero cell proportion, p'_j, as the explanatory variable,

$$m'_j = \beta_0 + \beta_1 p'_j + \beta_2 p'^2_j \qquad (4)$$

We observed that in real scATAC-seq datasets, for each cell group, there are a few bins (on average, two bins out of hundreds of thousands of bins) with a non-zero cell proportion higher than 0.8. While the polynomial regression model is a good fit for the relation of bin means and non-zero cell proportions, it generally doesn't capture bins having a non-zero cell proportion higher than 0.8. These few bins are excluded in the polynomial modelling. However, the estimated polynomial function is used to simulate all bins through the genome.

Bin-by-cell count matrix
simATAC generates the final count of cell i at bin j, $c_{j,i}$, using a Poisson distribution with $\gamma c'_{j,i}$ as the mean parameter, where $c'_{j,i}$ is the library size of cell i scaled by the bin mean m'_j at bin j.

$$c'_{j,i} = l'_i \times \left(\frac{m'_j}{\sum_{k=1}^{B} m'_k}\right) \qquad (5)$$

$$c_{j,i} \sim Poisson(\gamma c'_{j,i}) \qquad (6)$$

We define γ as the sparsity adjustment factor with a default value of 1, which offers users the flexibility to adjust the sparsity as desired. When γ is set to be smaller than 1, the simulated scATAC-seq data tend to be more sparse, and vice versa.

To reproduce the high noise level of scATAC-seq data, simATAC offers an optional step to include additional noise by adding Gaussian noises (rounded to integer) to the final simulated counts.

$$c_{j,i} = c_{j,i} + int(\mathcal{N}(mean, sd)) \qquad (7)$$

High noise level will blur the difference in the read distributions across different cell types, and mimic real sequencing artifacts. However, as the noise level increases, the distribution of the library sizes and the sparsity in the synthetic dataset may differ from the input scATAC-seq samples. The default setting of simATAC omits the optional adding noise step. However, the users have the flexibility to set their desirable noise level. Table 4 provides the recommended noise parameter settings for simulation.

simATAC writes the final synthesized bin-by-cell matrix as a SCE object, a container for single-cell genomics data, from the SingleCellExperiment R package [25].

Simulating feature matrices
simATAC can generate synthetic scATAC-seq data in the format of different feature matrices. The default bin-by-cell output can be converted to a peak-by-cell matrix by filtering bins enriched in aligned reads (top bins by measuring the bin mean values). simATAC generates a synthetic peak-by-cell count matrix with the "simATACgetCellByPeak" function, given a simulated bin-by-cell matrix by simATAC and a user-specified number of peak bins. simATAC also offers to extract other feature matrices given a user-input list of regions (in a BED format) with the "simATACgetCell-ByRegion" function. Another commonly used feature matrix format is the binary version, which is provided by "simATACgetBinary" function.

simATAC runtime
We assessed the performance of simATAC in terms of running time on a desktop workstation (Intel(R) Xeon(R) CPU @ 3.60GHz processor) for simulating 1,000 human cells at 5 kbp window size, which took on average 43 seconds for five different runs. Benchmark datasets' running times for estimation and simulation steps are provided separately in Additional file 1 Table S1. The running times reported in the Table S1 are the average of three simulations runs without including Gaussian noise.

Evaluation
In this section, we demonstrate the resemblance of the simulated samples generated by simATAC to the input real scATAC-seq datasets. The simulated samples are compared to the real samples on the distributions of library sizes, sparsity, and bin means. We also evaluated the peak calling and clustering performance of the synthesized matrices. The evaluations are performed on each cell groups (or cell types) from the annotated benchmark scATAC-seq datasets, Buenrostro2018, Cusanovich2018, and PBMCs, representing a wide range of platforms, cell types, and species.

- The Buenrostro2018 dataset contains 1974 cells generated from the Fluidigm C1 platform. Samples are from 9 FACS-sorted cell populations from CD34+ human bone marrow, namely, hematopoietic stem cells (HSCs), multipotent progenitors (MPPs), lymphoid-primed multipotent progenitors (LMPPs), common myeloid progenitors (CMPs), granulocyte-macrophage progenitors (GMPs), megakaryocyte-erythrocyte progenitors (MEPs), common lymphoid progenitors (CLPs), plasmacytoid dendritic cells (pDCs), and monocytes (mono) [27].
- The Cusanovich2018 dataset is a subset of mouse tissues with 12178 cells from 13 different sources

Figure 2 Comparison of the library size distribution. Library size box plots of the simulated (in orange) and real (in green) scATAC-seq data are illustrated for the three benchmarking datasets: Buenrostro2018, Cusanovich2018, and PBMCs. The library size distributions of the synthetic samples (no Gaussian noise is included) closely resemble those of the real samples.

Table 2 Pearson correlation between the simulated and real samples' bin means and the non-zero cell proportion of bins (averaged over 20 simulation runs).

Cell type	Correlation	
	Bin mean	Non-zero cell proportion
Buenrostro2018		
CMP	0.96	0.98
GMP	0.98	0.99
pDC	0.97	0.97
mono	0.92	0.94
Cusanovich2018		
Heart	0.95	0.96
Kidney	0.97	0.97
LargeIntestine	0.93	0.93
Liver	0.98	0.98
PBMCs		
Cell1	0.99	1
Cell3	0.99	1
Cell5	0.98	0.99
Cell7	0.99	0.99

Statistical evaluation

With each of the three real scATAC-seq datasets as benchmark data, we simulate bin-by-cell matrix for each cell group with the same number of cells as in the real datasets. We then compare the distribution of library sizes, bin means, and sparsity of the simulated dataset to the real samples, by cell group. We present four cell groups from each benchmarking dataset to demonstrate the similarity.

Figure 2 depicts the library size distributions of the scATAC-seq data simulated by simATAC using 12 cell groups from the benchmarking datasets as input. The library size distributions of the simulated data highly resemble those of the real datasets. See Additional file 1 Figure S1 for the complete comparison between the real and simulated data for all the cell groups in the three benchmark datasets.

simATAC synthesized bin-by-cell matrices preserve the accessibility of genomic regions with its input real scATAC-seq dataset. Table 2 summarizes the Pearson correlation of the bin mean and non-zero cell proportions between the simulated and the input real scATAC-seq datasets. The high correlations demonstrate that simATAC retains the genomic region accessibility characteristics of the input real data. See Additional file 1 Table S2 for the complete comparison for all cell groups from the benchmarking datasets. All the reported Pearson correlation is averaged over 20 simulation runs.

Figure 3 illustrates the sparsity of the simulated bin-by-cell matrices in 12 cell groups of the benchmark datasets, which demonstrates that the synthetic samples generated by simATAC retains the sparsity of the real samples across bins and cells (see Additional file

[21]. Sequenced cells are from bone marrow, cerebellum, heart, kidney, large intestine, liver, lung, prefrontal cortex, small intestine, spleen, testes, thymus, and whole brain, generated using a sciATAC-seq protocol [28].

- The PBMCs dataset is produced by the 10x Genomics Chromium (10xG) droplet-based scATAC platform and comprises 5335 cells from human peripheral blood mononuclear cells (PBMCs) [29]. There are no true cell type labels for PBMCs cells. However, we used 10x Genomics Cell Ranger ATAC's [29, 30] clustering labels as ground truth and performed simulation on each cluster. Although existing labels are not perfect, we included this data to evaluate how simATAC mimics features of a group of cells with similar biological characteristics from a droplet-based platform [21].

Figure 3 Comparison of the bin sparsity and cell sparsity distributions. Bin sparsity QQ-plots and cell sparsity box plots of the simulated (in green) and real (in purple) scATAC-seq data are illustrated for the three benchmarking datasets: Buenrostro2018, Cusanovich2018, and PBMCs. The sparsity of the synthetic data generated by simATAC (no Gaussian noise is included) closely resembles that of the corresponding real scATAC-seq input data.

1 Figure S2-S3 for other cell groups comparison). To demonstrate the bin sparsity resemblance of the simulated to the real data, we provide the bin sparsity QQ-plots of 12 benchmarking sample groups for sparsity adjustment factor $\gamma = \{0.8, 0.9, 1\}$ (see Additional file 1 Figure S4-S6).

We further investigate the impact of the bin sparsity adjustment parameter γ on the simulated bin-by-cell matrices. We observe that mild changes in the sparsity adjustment factor do not significantly affect the distributions of cell sparsity, library sizes and bin sparsity. See Additional file 1 Figure S7 for a comparison of these distributions under different sparsity adjustment factor values $\gamma = \{0.8, 0.9, 1, 1.1, 1.2\}$ using the LMPP cell type from the Buenrostro2018 dataset.

We also report the median absolute deviation (MAD), mean absolute error (MAE), and root mean square error (RMSE) of the sorted library sizes, bin means

and non-zero cell proportion of each bin between the real and the simulated datasets in Table 3. The reported metrics are averaged over 20 simulation runs. The small values of MAD, MAE and RMSE suggest that the properties of the synthesized bin-by-cell matrices closely resemble those of the input real data.

The main functionality of simATAC is to simulate bin-by-cell scATAC-seq count matrices, yet it also offers additional functionalities such as converting the simulated bin-by-cell matrices to peak-by-cell feature matrices using the "simATACgetCellByPeak" function. We show that the extracted peak-by-cell matrices preserve the chromatin accessibility information of the input real data. We compare the peak overlaps of the simulated data with those extracted from two commonly used non-segmenting peak callers, MACS2 [31] and Genrich [32] (see Additional File 1 Table S3 for details). We further show the results of the clus-

Table 3 Median absolute deviation (MAD), mean absolute error (MAE), and root mean square error (RMSE) average for sorted real and sorted simulated library sizes, real and simulated bin means, and real and simulated non-zero cells proportions across all cell groups in the associated dataset. The reported values are the averages of these metrics $\pm$ the corresponding standard deviations based on 20 simulation runs. The unit of the values is 0.1%.

	Buenrostro2018			Cusanovich2018			PBMCs		
	MAD	MAE	RMSE	MAD	MAE	RMSE	MAD	MAE	RMSE
Non-zero proportion	2.4 ± 2.8	6.5 ± 1.7	15.2 ± 3.8	4.0 ± 1.4	5.8 ± 1.7	8.6 ± 2.3	5.8 ± 9.1	9.0 ± 14	13.9 ± 18
Bin mean	2.4 ± 2.8	9.0 ± 2.5	531.9 ± 21	4.4 ± 1.6	6.6 ± 2.0	32.2 ± 16	7.2 ± 12	13.1 ± 20	57.8 ± 59
Library size	90 ± 46	111.6 ± 47	150.2 ± 60	50.0 ± 18	63.3 ± 17	88.2 ± 23	72.6 ± 38	107.8 ± 44	169 ± 45

tering metrics using the simulated data closely resemble peaks extracted from input real bin-by-cell matrix, and peak-by-cell matrices obtained from using MACS2 and Genrich peak callers (see Additional file 1 Table S4, Additional file Note S1, and Additional file Figure S8).

Clustering evaluation

The ability to cluster cells with similar biological characteristics is one of the major evaluation aspects of many scATAC-seq analytical tools. Many previous studies reported close to perfect cell clustering performance when evaluating scATAC-seq pipelines using simulated scATAC-seq data [15, 16, 21], which is not ideal in evaluating and comparing the performance across different scATAC-seq computational tools.

We here show that the simulated data by simATAC produce realistic downstream analysis results. Further, if the data is simulated based on an input real scATAC-seq dataset, the clustering metrics of the simulated data can be closer to those of the real data. Table 4 summarizes the clustering metrics, Normalized Mutual Information (NMI), Adjusted Mutual Information (AMI), and Adjusted Rand Index (ARI) evaluated on the simulated datasets by simATAC-seq. We adopt the SnapATAC graph-based clustering algorithm here, and all the reported metrics are averaged over 20 simulation runs.

We vary the Gaussian noise levels (mean=0, SD=0; mean=-0.3, SD=0.3; mean=-0.4, SD=0.4) added to the simulated data, representing no noise to high noise levels. We compare the clustering metrics using the simulated data with those using the input real scATAC-seq data, which is listed on the "Real" row. The clustering results in the Table 4 show that the simulated data by simATAC maintain the chromatin accessibility information of each cell group reasonably close to the real data. The clustering metrics of the synthetic data can get very close to the real data when adding Gaussian noise, and achieve realistic clustering performance in contrary to existing simulation methods. We further assess the distributions of the simulated counts under these three noise levels in Additional file 1 Figure S9-S14 and Table S5-S6, which

Table 4 Clustering evaluation results. The NMI, AMI, and ARI scores are the cell type clustering results using SnapATAC software. Real refers to the average of clustering results of input bin-by-cell matrix for 20 different initial seeds. Metrics for simATAC's simulated bin-by-cell matrices for different noise levels are also compared presented for each of the Buenrostro2018, Cusanovich2018 and PBMCs datasets (average of 20 simulation runs).

Mean	Standard deviation	NMI	AMI	ARI
	Buenrostro2018			
0	0	0.71	0.83	0.54
-0.3	0.3	0.72	0.83	0.54
-0.4	0.4	0.67	0.78	0.50
Real		0.54	0.62	0.36
	Cusanovich2018			
0	0	0.96	0.97	0.94
-0.3	0.3	0.79	0.85	0.69
-0.4	0.4	0.62	0.71	0.40
Real		0.41	0.46	0.22
	PBMCs			
0	0	0.78	0.87	0.71
-0.3	0.3	0.61	0.73	0.47
-0.4	0.4	0.56	0.67	0.44
Real		0.45	0.54	0.28

suggests that there is a trade-off between the closeness in clustering performance and the closeness in the distributions of library sizes and the sparsity parameters between the simulated and real samples. We also note that the impact of Gaussian noise level on clustering metrics may vary across different cell types, and thus simATAC offers the flexibility for users to adjust their desirable noise level.

In Table 4, we assume the sparsity parameter $\gamma = 1$ when simulating all the data. We show in Additional file 1 Table S7 the impact of γ on the downstream clustering performance of the simulated data. With all other parameters fixed, the clustering results are generally consistent across different values of γ. Hence, we set the default value of γ to 1 in simATAC.

Discussion and conclusions

The rapid development of scATAC-seq technology has led to a surge of scATAC-seq analytical tools. However, the lack of systematic simulation frameworks hinders the consistent evaluation of the computational

tools and reproducibility of the analytical results. To meet this need, we developed simATAC, a systematic scATAC-seq simulator that generates synthetic samples that closely resemble real scATAC-seq data. simATAC builds upon Gaussian mixture distribution to model cell library sizes, and polynomial regression model to represent the relationship between the average of bin counts and the non-zero cell proportions of bins. Moreover, simATAC grants users the flexibility to adjust parameters manually. simATAC generates a synthetic bin-by-cell matrix given a real scATAC-seq dataset as input. If there are no user-specified count matrix or parameters available, simATAC simulates samples deploying the default parameters derived from simulating the GSE99172 real scATAC-seq data. A list of estimated values for library size Gaussian mixture distribution and polynomial function parameters are provided in Additional file 2 to get the intuition of real data parameters. simATAC also offers additional functions to transform the bin-by-cell matrix into other feature matrices.

We compiled and processed 90 real scATAC-seq cell groups (from eight datasets) from various sequencing platforms, species and cell types to build a generalizable framework. We demonstrated the distributions of the library sizes, bin means, and sparsity parameters of the simATAC synthetic datasets resembling those of the real input examples. simATAC also offers additional options to modify the noise levels to mimic the artifacts in real scATAC-seq data and generate samples with various difficulty levels for downstream analyses assessment.

Quality control steps in most scATAC-seq pipelines apply filters on the raw feature matrices, such as removing cells with library sizes less than a fixed threshold, or filtering regions based on the number of mapped reads. As the denoising thresholds may affect the downstream analyses, simATAC offers users the flexibility to manually set the quality control filtration thresholds on the simulated raw count matrix and subsequent computational analyses such as binarization, dimensionality reduction, clustering, and visualization.

We show that cell-specific accessibility information of the input real bin-by-cell and extracted peak-by-cell matrices are well preserved in the simulated matrices. We included downstream analyses of the simulated bin-by-cell and peak-by-cell matrices and compared the clustering metrics of the simulated data with those of the real data using Seurat and SnapATAC.

simATAC generates count matrices using a 5 kbp bin window. However, there is no standard agreement on the optimal bin size for all samples, and bin size selection induces a trade-off between the ability to capture chromatin accessibility signals and computational

cost. For instance, at a 5 kbp window size, which is the recommended window size by SnapATAC for cell counts that we used [15], each human cell spans more than 600,000 bins. Smaller bin length leads to more computational and memory costs.

The feature matrices generated by simATAC cover regions spanning the whole genome without discarding the off-peak reads, leading to superior sensitivity for identifying rare cell types in complex tissues. While the peak-by-cell matrix has been the common version of scATAC-seq feature matrix to be analyzed, recent studies challenged this strategy and proposed the bin-by-cell version for downstream analyses. Peak calling pipelines perform differently in defining accessible genomic regions based on the approach they deploy. Therefore, we believe genome binning is an optimal approach to simulate scATAC-seq data, providing a standard representation for samples from different sources that mitigates comparison.

To our best knowledge, simATAC is the first scATAC-seq simulator that directly simulates bin-by-cell count matrices that are reproducible and closely resemble real data. Though the availability of real scATAC-seq data has been increasing, real scATAC-seq data with annotated labels ("ground truth") remains lacking. simATAC offers users the convenience to generate scATAC-seq data with known cell types and desirable number of single cells, yet closely resemble the real data. Further, simATAC provides the users the flexibility to adjust the library size, bin sparsity and noise level of the simulated data. We envision that simATAC empowers users to develop scATAC-seq analytical tools effectively and reproducibly.

Methods
simATAC statistical modelling
We compiled and processed each of the 90 scATAC-seq cell groups as well as each of the eight datasets (considering all cell groups together) separately to model the library size parameter. We conducted the Kolmogorov-Smirnov test [33] and the Chi-squared test [34] to test the goodness of fitness of the log-transformed library sizes from the Gaussian probability distribution, using the stats and fitdistrplus R packages [35, 36]. The p-values of the goodness of fitness tests showed that non-10xG samples generally follow a Gaussian distribution. Our preliminary statistical analysis of the 10xG scATAC-seq data showed that many of them are sampled from a mixture of probability distributions. We tested the null hypothesis if the 10xG samples' library sizes are sampled from a unimodal probability distribution using Hartigan's dip test [37] from the diptest R package [38]. Most of the modelling datasets rejected the null hypothesis that the library sizes are sampled

from a unimodal probability distribution at a significance level of $\alpha = 0.05$. Considering the probability density function and the cumulative distribution function plots, we modelled the log-transformed library sizes with a Gaussian mixture model with two modes and estimated the parameters using the mixtools R package [39]. Statistical parameters of the aforementioned tests for library size modelling are provided in Additional file 3.

We observed a significant difference in the distribution of library sizes between the real scATAC-seq data generated by the 10xG platform and other platforms. Library sizes of the non-10xG samples generally fit a unimodal Gaussian model, while those of the 10xG samples fit a bimodal GMM better. All the statistical analyses results are provided in the Additional file 3. simATAC simulates the library size using a bimodal GMM for samples from all platforms, and for non-10xG samples, the weight of the second Gaussian distribution can be set to zero.

To recover the scATAC-seq data sparsity, simATAC first assigns zero or non-zero labels to the bin-by-cell matrix using a Bernoulli distribution for each bin. The probability that a cell at bin j is non-zero is the estimated non-zero cells proportion at the corresponding bin of the input real scATAC-seq dataset.

Based on the 90 real scATAC-seq cell groups used for modelling, we observed a polynomial relationship between the non-zero cell proportions and the bin means in the normalized real bin-by-cell arrays. The input matrix is normalized by dividing primary counts by the cells' library size and multiplying by the median of library sizes. The quadratic relation between bin means and non-zero cell proportions for the 12 sampled cell groups of benchmarking datasets are provided in Additional file 1 Figure S15.

simATAC estimates the regression parameters using the lm function from the stats package [35], and calculates bin means based on Eq. (4). Note that the parameters in Eq. (4) are estimated by cell types/groups, as the chromatin accessibility patterns of different cell types vary biologically. A few bins with non-zero cell proportions higher than 0.8 were filtered out in fitting the regression model in the modelling process. The average number of excluded bins is two by considering all 90 cell groups.

Evaluation metrics
We assessed simATAC generated feature matrices by calculating the absolute difference between sorted real and sorted simulated library size vectors, real and simulated bin means, and non-zero cell proportion vectors of original and synthetic count matrices. We obtained

MAD, MAE, and RMSE of these vectors by the following equations, where R are the real values and S are the simulated values:

$$MAD = median(|R - S|) \quad (8)$$

$$MAE = mean(|R - S|) \quad (9)$$

$$RMSE = \sqrt{mean((R - S)^2)} \quad (10)$$

We used three metrics to evaluate the clustering performance, Normalized Mutual Information (NMI), Adjusted Mutual Information (AMI), and Adjusted Rand Index (ARI). Considering gt and $pred$ as the ground truth and predicted labels, NMI is calculated using

$$NMI(gt, pred) = \frac{MI}{max(H(gt), H(pred))}, \quad (11)$$

where $MI = MI(gt, pred)$ denotes the mutual information (MI) between gt and $pred$, and H is the entropy.

AMI is defined as

$$AMI(gt, pred) = \frac{MI - E[MI]}{mean(H(gt), H(pred)) - E[MI]}, (12)$$

where $E(\cdot)$ is the expectation function.

Using the same notations, ARI is defined as

$$ARI(gt, pred) = \frac{RI - E(RI)}{max(RI) - E(RI)}, \quad (13)$$

where the Rand Index (RI) is a similarity measure between two lists of labels. See more details of NMI, AMI and ARI in Additional file Note S2 [40].

Availability of data and materials
We built the simATAC statistical model and estimated the default input parameters based on 90 cell groups from eight publicly available real scATAC-seq datsets from various platforms, including Fluidigm C1, 10x Genomics Chromium (10xG), single-cell combinatorial indexing ATAC-seq (sciATAC-seq), multi-index single-cell ATAC-seq (MI-ATAC), and single-nucleus ATAC-seq (snATAC-seq) to ensure a generalizable simulation framework. The datasets supporting the modelling and evaluation of this article are all available publicly. All datasets used in this study are available from NIH GEO: (1) 63 10xG sample groups from GSE129785 [29], (2) GSE99172 [8], (3) GSE74310 [41], (4) GSE65360 [42], (5) GSE68103 (GSM1647122) [12], (6) GSE68103 (GSM1647123) [12], (7) GSE112091 (series GSE112245) [43], and (8) GSE100033 (GSM2668124) [44].

The datasets used for assessing and supporting the findings of this study are available publicly: (1) a dataset of sorted human bone marrow hematopoietic cells (Buenrostro2018) [27], (2) a subset of 13 sciATAC-seq adult mouse tissues (Cusanovich2018) [26, 28] provided by [21], and (3) human hematopoiesis II (PBMCs) [29] provided by 10xG, which are described in the Evaluation section in detail. The detailed information of all samples with cell groups and numbers are provided in the Additional file 1 Table S8. We also provide a table of abbreviations in Additional file 1 Table S9.

Dataset pre-processing
The raw FASTQ or BAM files were downloaded from the links provided and bin-by-cell matrices used in simATAC development were generated using the Snap-Tools (version: 1.4.6) [15, 45]. SnapTools is a Python module that pre-processes scATAC-seq data. Snap-Tools aligns raw FASTQ files to a reference genome using the Burrows-Wheeler aligner. Reads that were properly paired according to the SAM flag value, uniquely mapped with mapping quality > 30, and had a length less than $1,000$ base pairs were filtered for further analyses. SnapTools groups the reads with the same barcode and removes PCR duplicate reads in each group. SnapTools outputs a .snap file, which is an hdf5 file that stores the input scATAC-seq data, including cell-by-bin matrix used in the development and analyses of simATAC modelling [15]. For 10xG samples, we started from the fragment.tsv file provided by 10x website, which is a barcoded and aligned fragment file processed, with an implemented option by SnapTools for 10xG samples. The rest of the samples were processed from FASTQ or provided BAM files, and unique randomly generated barcodes were added to the samples that did not have barcodes themselves.

We used samtools (version 1.10) [1] for some of our pre-processing. Bedtools (version 2.27.1) was used for generating peak-by-cell matrices, and Picard tool (version 2.23.3) for removing duplicate reads. Snap-ATAC (version 1.0.0) R package was used for data pre-processing, loading bin-by-cell matrices, and clustering analysis [2]. We also used Signac R package (version 1.0.0), which is an extension of Seurat for the clustering analysis of peak-by-cell matrices [3]

The code and dataset files used for benchmarking are available at https://github.com/bowang-lab/simATAC under an GPLv3 license.

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[1]http://samtools.github.io
[2]https://github.com/r3fang/SnapATAC
[3]https://satijalab.org/signac/index.html

Declarations
Competing interests
The authors declare that they have no competing interests.

Availability of data and materials
The datasets analyzed during the current study are available from the repositories specified in the methods. The code used to analyze them is available under an GPLv3 license from the repository for this paper https://github.com/bowang-lab/simATAC. Copies of the benchmarking datasets are also provided in this repository.

Author contributions
ZN developed the software and performed the analyses. LZ contributed to the statistical analyses and writing the manuscript. BW oversaw all aspects of the project. All authors contributed to drafting the manuscript. All authors read and approved the final manuscript.

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References
1. Olsen, T.K., Baryawno, N.: Introduction to Single-Cell RNA Sequencing. Current Protocols in Molecular Biology (2018). doi:10.1002/cpmb.57
2. Thurman, R.E., Rynes, E., Humbert, R., Vierstra, J., Maurano, M.T., Haugen, E., Sheffield, N.C., Stergachis, A.B., Wang, H., Vernot, B., Garg, K., John, S., Sandstrom, R., Bates, D., Boatman, L., Canfield, T.K., Diegel, M., Dunn, D., Ebersol, A.K., Frum, T., Giste, E., Johnson, A.K., Johnson, E.M., Kutyavin, T., Lajoie, B., Lee, B.K., Lee, K., London, D., Lotakis, D., Neph, S., Neri, F., Nguyen, E.D., Qu, H., Reynolds, A.P., Roach, V., Safi, A., Sanchez, M.E., Sanyal, A., Shafer, A., Simon, J.M., Song, L., Vong, S., Weaver, M., Yan, Y., Zhang, Z., Zhang, Z., Lenhard, B., Tewari, M., Dorschner, M.O., Hansen, R.S., Navas, P.A., Stamatoyannopoulos, G., Iyer, V.R., Lieb, J.D., Sunyaev, S.R., Akey, J.M., Sabo, P.J., Kaul, R., Furey, T.S., Dekker, J., Crawford, G.E., Stamatoyannopoulos, J.A.: The accessible chromatin landscape of the human genome. Nature (2012). doi:10.1038/nature11232
3. Stergachis, A.B., Neph, S., Reynolds, A., Humbert, R., Miller, B., Paige, S.L., Vernot, B., Cheng, J.B., Thurman, R.E., Sandstrom, R., Haugen, E., Heimfeld, S., Murry, C.E., Akey, J.M., Stamatoyannopoulos, J.A.: Developmental fate and cellular maturity encoded in human regulatory DNA landscapes. Cell (2013). doi:10.1016/j.cell.2013.07.020
4. Buenrostro, J.D., Wu, B., Chang, H.Y., Greenleaf, W.J.: ATAC-seq: A method for assaying chromatin accessibility genome-wide. Current Protocols in Molecular Biology (2015). doi:10.1002/0471142727.mb2129s109
5. Jin, S., Zhang, L., Nie, Q.: scAI: an unsupervised approach for the integrative analysis of parallel single-cell transcriptomic and epigenomic profiles. Genome biology (2020). doi:10.1186/s13059-020-1932-8
6. Stuart, T., Butler, A., Hoffman, P., Hafemeister, C., Papalexi, E., Mauck, W.M., Hao, Y., Stoeckius, M., Smibert, P., Satija, R.: Comprehensive Integration of Single-Cell Data. Cell (2019). doi:10.1016/j.cell.2019.05.031
7. Butler, A., Hoffman, P., Smibert, P., Papalexi, E., Satija, R.: Integrating single-cell transcriptomic data across different conditions, technologies, and species. Nature Biotechnology (2018). doi:10.1038/nbt.4096

8. Schep, A.N., Wu, B., Buenrostro, J.D., Greenleaf, W.J.: ChromVAR: Inferring transcription-factor-associated accessibility from single-cell epigenomic data. Nature Methods (2017). doi:10.1038/nmeth.4401

9. de Boer, C.G., Regev, A.: BROCKMAN: Deciphering variance in epigenomic regulators by k-mer factorization. BMC Bioinformatics (2018). doi:10.1186/s12859-018-2255-6

10. Ji, Z., Zhou, W., Ji, H.: Single-cell regulome data analysis by SCRAT. Bioinformatics (2017). doi:10.1093/bioinformatics/btx315

11. Pliner, H.A., Packer, J.S., McFaline-Figueroa, J.L., Cusanovich, D.A., Daza, R.M., Aghamirzaie, D., Srivatsan, S., Qiu, X., Jackson, D., Minkina, A., Adey, A.C., Steemers, F.J., Shendure, J., Trapnell, C.: Cicero Predicts cis-Regulatory DNA Interactions from Single-Cell Chromatin Accessibility Data. Molecular Cell (2018). doi:10.1016/j.molcel.2018.06.044

12. Cusanovich, D.A., Daza, R., Adey, A., Pliner, H.A., Christiansen, L., Gunderson, K.L., Steemers, F.J., Trapnell, C., Shendure, J.: Multiplex single-cell profiling of chromatin accessibility by combinatorial cellular indexing. Science (2015). doi:10.1126/science.aab1601

13. Zamanighomi, M., Lin, Z., Daley, T., Chen, X., Duren, Z., Schep, A., Greenleaf, W.J., Wong, W.H.: Unsupervised clustering and epigenetic classification of single cells. Nature Communications (2018). doi:10.1038/s41467-018-04629-3

14. Baker, S.M., Rogerson, C., Hayes, A., Sharrocks, A.D., Rattray, M.: Classifying cells with Scasat, a single-cell ATAC-seq analysis tool. Nucleic acids research (2019). doi:10.1093/nar/gky950

15. Fang, R., Preissl, S., Hou, X., Lucero, J., Wang, X., Motamedi, A., Shiau, A.K., Mukamel, E.A., Zhang, Y., Behrens, M.M., Ecker, J., Ren, B.: Fast and Accurate Clustering of Single Cell Epigenomes Reveals Cis-Regulatory Elements in Rare Cell Types. bioRxiv (2019). doi:10.1101/615179

16. Bravo González-Blas, C., Minnoye, L., Papasokrati, D., Aibar, S., Hulselmans, G., Christiaens, V., Davie, K., Wouters, J., Aerts, S.: cisTopic: cis-regulatory topic modeling on single-cell ATAC-seq data. Nature Methods (2019). doi:10.1038/s41592-019-0367-1

17. Urrutia, E., Chen, L., Zhou, H., Jiang, Y.: Destin: toolkit for single-cell analysis of chromatin accessibility. Bioinformatics **35**(19), 3818–3820 (2019). doi:10.1093/bioinformatics/btz141. https://academic.oup.com/bioinformatics/article-pdf/35/19/3818/30061708/btz141.pdf

18. Li, B., Li, Y., Li, K., Zhu, L., Yu, Q., Cai, P., Fang, J., Zhang, W., Du, P., Jiang, C., Lin, J., Qu, K.: APEC: an accesson-based method for single-cell chromatin accessibility analysis. Genome biology (2020). doi:10.1186/s13059-020-02034-y

19. Zhao, C., Hu, S., Huo, X., Zhang, Y.: Dr.seq2: A quality control and analysis pipeline for parallel single cell transcriptome and epigenome data. PLoS ONE (2017). doi:10.1371/journal.pone.0180583

20. Xiong, L., Xu, K., Tian, K., Shao, Y., Tang, L., Gao, G., Zhang, M., Jiang, T., Zhang, Q.C.: SCALE method for single-cell ATAC-seq analysis via latent feature extraction. Nature Communications (2019). doi:10.1038/s41467-019-12630-7

21. Chen, H., Lareau, C., Andreani, T., Vinyard, M.E., Garcia, S.P., Clement, K., Andrade-Navarro, M.A., Buenrostro, J.D., Pinello, L.: Assessment of computational methods for the analysis of single-cell ATAC-seq data (2019). doi:10.1101/739011. https://doi.org/10.1101/739011

22. Yu, W., Uzun, Y., Zhu, Q., Chen, C., Tan, K.: scATAC-pro: a comprehensive workbench for single-cell chromatin accessibility sequencing data. Genome biology (2020). doi:10.1186/s13059-020-02008-0

23. Duren, Z., Chen, X., Zamanighomi, M., Zeng, W., Satpathy, A.T., Chang, H.Y., Wang, Y., Wong, W.H.: Integrative analysis of single-cell genomics data by coupled nonnegative matrix factorizations. Proceedings of the National Academy of Sciences of the United States of America (2018). doi:10.1073/pnas.1805681115

24. Li, Z., Schulz, M.H., Look, T., Begemann, M., Zenke, M., Costa, I.G.: Identification of transcription factor binding sites using ATAC-seq. Genome Biology (2019). doi:10.1186/s13059-019-1642-2

25. Lun, A., Risso, D.: SingleCellExperiment: S4 Classes for Single Cell Data. (2019). R package version 1.4.1

26. Xiong, L., Xu, K., Tian, K., Shao, Y., Tang, L., Gao, G., Zhang, M., Jiang, T., Zhang, Q.C.: SCALE method for single-cell ATAC-seq analysis via latent feature extraction. Nature Communications (2019). doi:10.1038/s41467-019-12630-7

27. Buenrostro, J.D., Corces, M.R., Lareau, C.A., Wu, B., Schep, A.N., Aryee, M.J., Majeti, R., Chang, H.Y., Greenleaf, W.J.: Integrated Single-Cell Analysis Maps the Continuous Regulatory Landscape of Human Hematopoietic Differentiation. Cell (2018). doi:10.1016/j.cell.2018.03.074

28. Cusanovich, D.A., Hill, A.J., Aghamirzaie, D., Daza, R.M., Pliner, H.A., Berletch, J.B., Filippova, G.N., Huang, X., Christiansen, L., DeWitt, W.S., Lee, C., Regalado, S.G., Read, D.F., Steemers, F.J., Disteche, C.M., Trapnell, C., Shendure, J.: A Single-Cell Atlas of In Vivo Mammalian Chromatin Accessibility. Cell (2018). doi:10.1016/j.cell.2018.06.052

29. Satpathy, A.T., Granja, J.M., Yost, K.E., Qi, Y., Meschi, F., McDermott, G.P., Olsen, B.N., Mumbach, M.R., Pierce, S.E., Corces, M.R., Shah, P., Bell, J.C., Jhutty, D., Nemec, C.M., Wang, J., Wang, L., Yin, Y., Giresi, P.G., Chang, A.L.S., Zheng, G.X.Y., Greenleaf, W.J., Chang, H.Y.: Massively parallel single-cell chromatin landscapes of human immune cell development and intratumoral T cell exhaustion. Nature Biotechnology **37**(8), 925–936 (2019). doi:10.1038/s41587-019-0206-z

30. Cell Ranger ATAC. https://support.10xgenomics.com/single-cell-atac/software/pipelines/latest/what-is-cell-ranger-atac

31. Zhang, Y., Liu, T., Meyer, C.A., Eeckhoute, J., Johnson, D.S., Bernstein, B.E., Nusbaum, C., Myers, R.M., Brown, M., Li, W., *et al.*: Model-based analysis of chip-seq (macs). Genome biology **9**(9), 1–9 (2008)

32. M. Gaspar, J.: Genrich (2019). https://github.com/jsh58/Genrich

33. Hassani, H., Silva, E.S.: A Kolmogorov-Smirnov based test for comparing the predictive accuracy of two sets of forecasts. Econometrics (2015). doi:10.3390/econometrics3030590

34. F.R.S., K.P.: X. on the criterion that a given system of deviations from the probable in the case of a correlated system of variables is such that it can be reasonably supposed to have arisen from random sampling. The London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science **50**(302), 157–175 (1900). doi:10.1080/14786440009463897. https://doi.org/10.1080/14786440009463897

35. R Core Team: R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria (2019). R Foundation for Statistical Computing. https://www.R-project.org/

36. Delignette-Muller, M.L., Dutang, C.: fitdistrplus: An R package for fitting distributions. Journal of Statistical Software **64**(4), 1–34 (2015)

37. Hartigan, J.A., Hartigan, P.M.: The Dip Test of Unimodality. The Annals of Statistics (1985). doi:10.1214/aos/1176346577

38. Maechler, M.: Diptest: Hartigan's Dip Test Statistic for Unimodality - Corrected. (2016). R package version 0.75-7. https://CRAN.R-project.org/package=diptest

39. Benaglia, T., Chauveau, D., Hunter, D.R., Young, D.: mixtools: An R package for analyzing finite mixture models. Journal of Statistical Software **32**(6), 1–29 (2009)

40. Clustering. https://scikit-learn.org/stable/modules/clustering.html

41. Corces, M.R., Buenrostro, J.D., Wu, B., Greenside, P.G., Chan, S.M., Koenig, J.L., Snyder, M.P., Pritchard, J.K., Kundaje, A., Greenleaf, W.J., Majeti, R., Chang, H.Y.: Lineage-specific and single-cell chromatin accessibility charts human hematopoiesis and leukemia evolution. Nature Genetics (2016). doi:10.1038/ng.3646

42. Buenrostro, J.D., Wu, B., Litzenburger, U.M., Ruff, D., Gonzales, M.L., Snyder, M.P., Chang, H.Y., Greenleaf, W.J.: Single-cell chromatin accessibility reveals principles of regulatory variation. Nature (2015). doi:10.1038/nature14590

43. Chen, X., Litzenburger, U.M., Wei, Y., Schep, A.N., LaGory, E.L., Choudhry, H., Giaccia, A.J., Greenleaf, W.J., Chang, H.Y.: Joint single-cell DNA accessibility and protein epitope profiling reveals environmental regulation of epigenomic heterogeneity. Nature Communications (2018). doi:10.1038/s41467-018-07115-y

44. Preissl, S., Fang, R., Huang, H., Zhao, Y., Raviram, R., Gorkin, D.U.,

Zhang, Y., Sos, B.C., Afzal, V., Dickel, D.E., Kuan, S., Visel, A., Pennacchio, L.A., Zhang, K., Ren, B.: Single-nucleus analysis of accessible chromatin in developing mouse forebrain reveals cell-type-specific transcriptional regulation. Nature Neuroscience (2018). doi:10.1038/s41593-018-0079-3

45. Fang, R.: SnapATAC: Single Nucleus Analysis Package for ATAC-Seq. (2019). R package version 1.0.0. https://github.com/r3fang/SnapATAC

Additional Files

Additional file 1 — Figure S1-S15, Table S1-S9, Note S1-S2
Figures of parameter comparison for cell groups that are not provided in the main manuscript, comparison of real and simulated parameters' polynomial relation for 12 sample cell groups, parameter plots for simATAC simulated data with different parameters' adjustment, cell type clustering results, table of benchmarking datasets' simulation time, table of correlations, and table of all datasets' detailed information, table of abbreviations, description of the pipeline used for generating cell-by-peak matrix, and description of clustering parameter equations (provided in PDF format).

Additional file 2
Table of estimated values for Gaussian mixture model and polynomial function parameters obtained for benchmarking cell groups (provided in XLSX format).

Additional file 3
Table of statistical analysis parameters of simATAC library size modelling (provided in XLSX format).