# LONG-RANGE SEQUENTIAL DEPENDENCIES PRECEDE COMPLEX SYNTACTIC PRODUCTION IN LANGUAGE ACQUISITION 

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#### Abstract

To convey meaning, human language relies on hierarchically organized, long-range relationships spanning words, phrases, sentences, and discourse. The strength of the relationships between sequentially ordered elements of language (e.g., phonemes, characters, words) decays following a power law as a function of sequential distance. To understand the origins of these relationships, we examined long-range statistical structure in the speech of human children at multiple developmental time points, along with non-linguistic behaviors in humans and phylogenetically distant species. Here we show that adult-like power-law statistical dependencies precede the production of hierarchically-organized linguistic structures, and thus cannot be driven solely by these structures. Moreover, we show that similar long-range relationships occur in diverse non-linguistic behaviors across species. We propose that the hierarchical organization of human language evolved to exploit pre-existing long-range structure present in much larger classes of non-linguistic behavior, and that the cognitive capacity to model long-range hierarchical relationships preceded language evolution. We call this the Statistical Scaffolding Hypothesis for language evolution.


Keywords language • hierarchy • power law • evolution

## 1 Significance Statement

Human language is uniquely characterized by semantically meaningful hierarchical organization, conveying information over long timescales. At the same time, many non-linguistic human and animal behaviors are also often characterized by richly hierarchical organization. Here, we compare the long-timescale statistical dependencies present in language to those present in non-linguistic human and animal behaviors as well as language production throughout childhood. We find adult-like, long-timescale relationships early in language development, before syntax or complex semantics emerge, and we find similar relationships in non-linguistic behaviors like cooking and even housefly movement. These parallels demonstrate that long-range statistical dependencies are not unique to language and suggest a possible evolutionary substrate for the long-range hierarchical structure present in human language.

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## 2 Introduction

Since Shannon's original work characterizing the sequential dependencies present in language, the structure underlying long-range information in language has been the subject of a great deal of interest in linguistics, statistical physics, cognitive science, and psychology [ $\square-20]$. Long-range information content refers to the dependencies between discrete elements (e.g., units of spoken or written language) that persist over long sequential distances spanning words, phrases, sentences, and discourse. For example, in Shannon's original work, participants were given a series of letters from an English text and were asked to predict the letter that would occur next. Using the responses of these participants, Shannon derived an upper bound on the information added by including each preceding letter in the sequence. More recent investigations compute
 or mutual information (MI) functions [ $[\boxed{2}, 5,[\boxed{[1]},[4]$ between elements in a sequence. In both cases, sequential relationships are calculated as a function of the sequential distance between events. For example, in the sequence $a \rightarrow b \rightarrow c \rightarrow d \rightarrow e \rightarrow f$, at a distance of three elements, relationships would be calculated over the pairs $a$ and $d, b$ and $e$, and $c$ and $f$.
On average, as the distance between elements increases, statistical dependencies grow weaker. Across many different sequence types, including phonemes, syllables, and words in both text and speech, the decay of long-
 is thought to derive at least in part from the hierarchical organization of language, and has been variously attributed to human language syntax [5], semantics [3], and discourse structure [4]. To understand the link between hierarchical organization in language and a power-law decay in sequential dependencies, it is helpful to consider both the latent and surface structure of a sequence (Fig. W). When only the surface structure of a sequence is available, as it is for language corpora, a power-law decay in the MI between sequence elements gives evidence of an underlying hierarchical latent structure. This phenomenon can be demonstrated by comparing the MI between elements in a sequence generated from a hierarchically-structured language model, such as a probabilistic context-free grammar (PCFG), to the MI between elements in a sequence generated by a non-hierarchical model, such as a Markov process (Fig. (T). For sequences generated by a Markov process, the strength of the relationship between elements decays exponentially (Eq. [5) as sequential distance increases $[5,[2 T]$ (Fig. $\mathbb{I} A$ ). In the PCFG model, however, linear distances in the sequence are coupled to logarithmic distances in the latent structure of the hierarchy (Fig. $\mathbb{I B}-\mathrm{C}$ ). While information continues to decay exponentially as a function of the distance in the latent hierarchy (Fig. mD ), this log-scaling results in a power-law decay when MI is computed over corresponding sequential distances (Fig. $\mathbb{T E}$ ).
In language, long-range relationships convey meaning across hierarchical levels of organization. This latent linguistic structure is thought to underlie the power-law relationships observed across texts and speech [2-5]. The presence of power-law sequential and temporal relationships in natural phenomena is not restricted to human language, however. Here, we demonstrate that the power law underlying long-range statistical relationships in human speech precedes complex morphosyntactic production in language and is part of a larger set of natural behaviors exhibiting similar temporal relationships. The potentially numerous generative mechanisms for these phenomena remain to be established; however their existence evinces a substrate that may have been exploited in the evolution of a cognitive capacity to represent long-range signals prior to the evolution of language.

Beyond language, power-law temporal relationships are observed in both human-unique behaviors like music production [ $[2 Z]$ and stock market turbulence $[2 Z 3,[24]$ as well as behaviors that are shared with other animals such as sleep patterns in infants [ 2.5$]$ and heart rates in healthy adults [ [Z6, [27]. In fact, the ubiquity of power laws in the physical and biological sciences spreads beyond temporal and sequential relationships and is well documented across a variety of phenomena. $1 / f$ noise, a power law in the spectral density of a stochastic process, is observed in signals ranging from neural oscillations to flocking patterns in birds [ $28-31]$. The relationship between biological variables often scale following a power law, for example, the allometric scaling laws observed between an organisms size and metabolic rate [ 32 ]. A variety of natural distributions such as word frequencies are well described by power-law distributions, a phenomenon termed Zipfs law [33--37]. Power-law distributions are also observed in the connectivity of many biological and social networks, a property called scale-freeness [38-41]. Over much of the past several decades, heated debates have arisen over claims of universal organizing principles of natural phenomena characterized by power laws [ $28,31,34,41-44]$.
Across the diverse phenomena described by power-law relationships in the natural sciences, one commonality is that the origins of the observed power law are still not fully understood and mechanistic implications of power laws are often overstated [ [88, 31, 34, 41, 43, 44]. Although mechanisms have been proposed to

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Figure 1: Comparison between sequences with deep latent relationships and iteratively generated sequences. (A) The MI between elements in an iteratively (Markov model) generated sequence decays exponentially as a function of sequential distance. (B) An example sequence with hierarchical latent structure. The latent distance between the two end elements in the sequence is 6 (blue), while the sequential distance is 17 (red). (C) In sequences with hierarchical latent structure, the sequential distance between elements is logarithmically related to the latent distance (fit model: $a * \log _{x * b}+c$ where $x$ is sequential distance). (D) Like sequential distance in (A), The MI between elements in a hierarchically generated sequence decays exponentially as a function of latent distance. (E) The MI between elements in a hierarchically generated sequence decays following a power law as a function of sequential distance, which is related to the exponential MI decay seen in (D) and the logarithmic relationship between sequential and latent distance seen in (C). In (A), the probabilistic Markov model used to generate the empirical data has 2 states with a self-transition probability of 0.1 . In (C-E) a probabilistic context-free grammar [5] with the same transition probability is used.
account for the various forms of power laws observed in natural phenomena, the presence alone of a power law provides little insight into the underlying generative mechanism [31, 34, 42-44]. This is true of language as well. While the power laws characterized in language are consistent with generative mechanisms posited in syntactic theory [ 5,45$]$, they are not confirmatory. The presence of a power law in language does confirm, however, that relationships spanning long distances exist in the signal. Given the presence of power-law sequential relationships in human language, the question remains whether the power law is a product of linguistic structure, or whether these relationships originate in lower-level phenomena that are not unique to human language. If long-range relationships predate the evolution of language, they may have influenced the structure of temporal relationships that evolved with language.

Beyond human language, numerous other human behaviors [46-51], animal behaviors [52-57], animal vocalizations [ $37,[58-65]$, and other biologically-generated processes [2.5-[27, $31,57-[0]$ have been described as being hierarchically organized or display long-timescale organization. Such behaviors range from the seemingly non-complex patterns of behavior exhibited by fruit flies [52, 56] to tool usage in great apes [53, 54]. For this reason, it has been argued that hierarchical organization is an inherent property of biological processes, including human behavior [50, $[7,72]$ and that the hierarchical structure of behavior is inherited from the lower-level organization of neurophysiological mechanisms that produce it [r73-[76] , which themselves can be characterized by power-law relationships in temporal sequencing [ [2.9, 30, [77]. The developmental and/or evo-

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lutionary dependence of linguistic structure on underlying, domain-general, cognitive and neural processes has been posited by several researchers $[50,151, ~[76, ~[78] . ~$
Despite the numerous observations of hierarchical structure and long-range dependencies in non-human animal behaviors, few studies have examined the statistical dynamics of these behaviors quantitatively. Those that do have found power-law dynamics in the communication and behaviors of animals that are phylogenetically distant from humans [ $[\boxed{Z}, \pi-81]$. This, along with the prevalence of long-range power-law relationships in other natural phenomena [ [ $Z, ~ B I]$, supports the generality of these organizing principles across all behaviors. On the other hand, sequential organization in the vocal communication signals of nonhuman primates may extend over only a few elements [ 82,83$]$, and descriptions of hierarchical non-vocal behaviors in non-human primates tend to only be a few elements long [53, 54, 84], supporting at most a very shallow hierarchical structure. Thus, the extent to which a power-law decay provides a unified description of long-range statistical dependencies in behavior has yet to be determined. This question has particular relevance to human language, where it is unknown whether power-law relationships in sequential organization are present throughout language development, or emerge as linguistic structure develops. Understanding the ubiquity of power-law relationships across non-linguistic and non-human behavior, as well as across human language acquisition, may help to explain the origins of this organizing principle in language.

### 2.1 Present work

In the present work, we perform three groups of analyses exploring whether non-linguistic and pre-linguistic long-range statistical relationships parallel the long-range statistical relationships present in adult language. First, we analyze a series of language development corpora of children learning English, starting at six months of age [ $8.5-48]$, to determine whether long-range relationships are present in human vocalizations prior to the production of hierarchically-organized linguistic structure. Second, we analyze the long-range statistical dependencies of a human non-linguistic corpus of transcribed actions taken by humans while cooking [99], to determine whether power-law relationships are present in the sequential organization of non-linguistic human behaviors. Finally, we analyze the long-range sequential relationships in datasets of freely moving fruit flies (Drosophila melanogaster) [56] and zebrafish (Danio rerio) behavior [ [100], both of which have been previously characterized as being hierarchically organized, to determine whether a power law is present in the sequential organization of non-human non-linguistic behavior.

We show that both human non-linguistic and non-human non-linguistic behavior exhibits long-range powerlaw statistical dependencies like those observed in mature human language. In child language datasets, we observe a power-law as early as 6 to 12 months of age, while children are still in the "babbling" stage of language development. In the animal behavior datasets, we observe long-range power-law decays spanning many minutes ( $>6$ minutes in Drosophila and $>20$ minutes in zebrafish).

## 3 Results

### 3.1 Language acquisition

Although much work has explored the information content and long-range sequential organization of human language, relatively few studies have examined these properties in speech [Z] or language development directly. Here we investigate the long-range information present in speech during language development using datasets from the TalkBank project [ $85,8,86]$.
We first examined MI decay in sequences of words over nine datasets of natural speech from English speaking children included in the CHILDES repository [ $86,91-48]$ and three datasets of sequences of phonemes from the PhonBank repository [ $8.5,87-8.8]$, both of which are part of the TalkBank repository [ 86$]$. Each dataset within CHILDES and PhonBank was collected in a slightly different manner. In our analyses, we included only transcripts of spontaneous speech that were collected from typically-developing children (usually at an in-home setting with family or an experimenter). The subset of CHILDES we used includes word-level transcripts of speech from children aged 12 months to 12 years of age. The subset of PhonBank we used includes phonetic transcriptions of speech given in the International Phonetic Alphabet (IPA) from children aged 6 months to four years of age. Between the phoneme and word-level datasets, a large range of speech and language development is covered.
For the MI analysis on phonemes, we binned transcripts into five 6 -month age groups (6-12, 12-18, 18-$24,24-30,30-36$ ) and one age group from 3 years to 4 years. Each transcript was analyzed as sequences of phonemes, where phoneme distributions for each transcript are treated independently to account for variation

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Figure 2: Mutual Information decay over words and phonemes during development. (A) MI decay over phonemes for each age group. MI decay is best fit by a composite model (solid grey line) for all age groups across phonemes and words. Exponential and power-law decays are shown as a dashed and dotted grey lines, respectively. (B) The MI decay (as in (A)) with the exponential component of the fit model subtracted to show the power-law component of the decay. (C) The same as in (B), but with the power-law component subtracted to show exponential component of the decay. (D-F) The same analyses as A-C, but for words.
in acquired vocabulary across individuals during development. Because transcript lengths varied between age groups (Fig. S1), we analyzed MI at sequential distances up to the median transcript length for each age group. Across all age groups, the decay in MI over sequences of phonemes is best fit by a composite power-law and exponential decay model (Fig. ZA-C; relative probabilities 0.897 to $>0.999$; Table S2). In each age group, we observe both a clear power law prominent over long distances (Fig. $\mathbb{Z B}$ ) and a clear exponential decay at short word distances (Fig. [ZC), consistent with prior results on adult speech [Z].
For the MI analysis on words, we binned transcripts into four 6 -month age groups (12-18, 18-24, 24-30, 30-36) and one age group from 3 years to 12 years. The MI decay between words is best fit by a composite model of power-law and exponential decay (Eq. [7; relative probability $=0.989$ for $12-18$ months and $>0.999$ for all other age groups; Fig. $\mathrm{ZDD}-\mathrm{F}$; Table S1).
We also computed the MI decay over control sequences of words and phonemes that had been shuffled to isolate sequential relationships at different levels of organization (e.g. phoneme, word, utterance, transcript; Figs. S2, S3, S4). Consistent with Sainburg et al., [Z], we observe that short-range relationships captured by exponential decay are largely carried within words and utterances, while long-range relationships captured by a power-law decay are carried across longer timescales between words and utterances. In particular, long-range relationships are eliminated when between-utterance structure is removed by randomly shuffling the order of utterances within a transcript (Figs. S2E, S3C) and retained when within-utterance structure is removed by shuffling words or phonemes within utterances (Figs. S2D, S3B) or phonemes within words (Fig. S2C). When MI decay is computed over part-of-speech labels for the words in CHILDES, we find

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a transition from MI decay that is best fit by a power-law decay alone at $12-24$ months of age, to MI decay that is best fit by a composite model of power-law and exponential decay after 24 months (Fig S3D). Shuffling word order eliminates all long-range sequential relationships while preserving short timescale exponential relationships (Figs. S2B, S3E), and shuffling phoneme order within transcripts removes all sequential relationships (Figs. S2F). Across each shuffling analysis, we observe that short-range information content captured by exponential decay is largely captured within words and utterances, while long-range information is carried between utterances, even during early language production.

As an additional control to ensure that the observed MI decay patterns are not the product of mixing datasets from multiple individuals, we also computed the MI decay of the longest individual transcripts comprising each age cohort across both phonemes and words. The decay of the longest individual transcripts parallels the results across transcripts from Fig. $\square$ (Figs. S5, S6).

### 3.2 Human behavior



Figure 3: Mutual Information decay over actions in the Epic Kitchens dataset [99]. Data is fit by a power-law decay model (Eq.

To contrast the long-range statistical structure of human language with non-linguistic human behaviors, we require a relatively large dataset of long, discrete, sequences of behavior. We chose the Epic Kitchens dataset [99], as it was the largest available segmented dataset of long sequences of individual actions, and because cooking has previously been described as having complex hierarchical syntactic structure [ [im].

The Epic Kitchens dataset consists of a series of videos in which each section of the video is labeled with an action and noun, for example open door $\rightarrow$ turn-on light $\rightarrow$ close door $\rightarrow$ open fridge $\rightarrow \ldots$. We calculate MI only over the sequences of verb classes, of which there are 119 unique classes. We computed the MI up to a distance of the median sequence length of 45 actions.

In contrast with the speech datasets, we found that the Epic Kitchens dataset was best fit by a power-law decay model with no exponential component (Eq. [7; Fig. [3; relative probability $=0.597$; Table S3). We additionally looked at the MI decay of the longest cooking transcripts and found the MI decay of individual sequences were similar to MI decay across the entire dataset (Fig S7).

### 3.3 Animal behavior

The datasets of animal behavior used in our analyses were videos of zebrafish [ 100 ] and Drosophila [56] movements that had been transcribed in an unsupervised manner, i.e without external reference to a priori state labels. In both datasets, raw data recorded from individual animals were projected into a low-dimensional space and were then clustered into discrete states. These states were then labelled post hoc with humaninterpretable descriptions such as "slow", "side leg", or "anterior" for Drosophila, and "O-bend" or "J-turn" for zebrafish. Drosophila behavior has a long history of being described in hierarchical terms [52, 56, [12], and the dataset used here, in particular, demonstrates long-range relationships extending over hundreds to thousands of states [56]. The zebrafish dataset used here has also previously been shown to contain sequential information that unfolds over multiple timescales [[0], [103]. Both datasets were chosen because they contain large sets of discrete behaviors from individuals over long periods of time.


Figure 4: Mutual Information decay over Zebrafish and Drosophila behavior. Data is displayed in the same manner as Fig. [].

In both the zebrafish and Drosophila datasets, we observe an MI decay that is best fit by a composite power-law and exponential decay model (Fig. 四; relative probabilities $>0.999$; Table S3). The shape of the MI decay differs somewhat between the two datasets, however. In the case of the zebrafish, the relative contributions of the exponential and power-law components of the decay mirror the results obtained in speech. That is, an exponential component to the decay is observed at short distances under 10 elements, which gives way to a power-law at longer distances. In the case of the Drosophila, the power-law component of the decay is dominant throughout the signal, and the exponential component of the decay only captures a small portion of the variance at a distance of around 10-200 elements.
We additionally looked at a subset of the longest individual transcripts of Drosophila (Fig. S8) and zebrafish (Fig. S9) behavior and found that MI decay at the individual level varies between individual transcripts but matches the long-range decay observed across the datasets.

## 4 Discussion

We analyzed the long-range sequential information present in language production during development, and several sequentially organized and putatively hierarchical non-linguistic behaviors in other species. In all cases, the information between behavioral elements decays following a power law as sequential distance increases. For language, we find that that the long-range statistical relationships characteristic of adult usage [ $Z$ ] are present as early as 6 to 12 months in phonemes and 12-18 months in words, preceding the production of complex linguistic structure [84]. We see similar long-range power-law structure in the sequential organization of human food preparation and cooking. Cooking is a relatively modern and human-unique behavior [104], however, and may have arisen after humans developed more deeply hierarchical and highly planned tool usage behaviors [ 84,405$]$. Yet, we also observe similar long-range organization in the movement patterns of Drosophila and zebrafish, consistent with previous reports for birdsong [z]. Long-range statistical relationships are present developmentally in speech before hierarchical linguistic structures are produced, and exist in widely varying animal species. Thus, the long-range statistical relationships present in language are not unique to linguistic behaviors or to humans.

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These results compel reconsideration of the mechanisms that shape long-range statistical relationships in human language. Traditionally, the power-law decay in information between the elements of language (phonemes, words, etc.) has been thought to be imposed by the hierarchical linguistic structure of syntax, semantics, and discourse [3-5]. Early development provides a natural experiment in which one can examine human vocal communication absent the production of complex syntactic and semantic structures. Remarkably, even at a very early age, prior to the production of mature syntactic structures, vocal sequences show adult-like long-range dependencies. This does not rule out the possibility that long-range dependencies in adult language are driven in part by linguistic structure, but this hierarchical organization alone cannot explain our observations. What seems most reasonable to us, is that multiple mechanisms impose long-range dependencies on human speech and language, and that these operate on different developmental timescales. We take our observations of similar power laws in diverse non-linguistic behaviors to reinforce the idea that multiple mechanisms impose power-law dynamics on behavioral sequences. Indeed, power-laws are found in natural phenomena as distant from language as the sequential organization of earthquakes [ [06] ] and river water levels [IIT]. It may be that the power-law structure of human language reflects a very deep embedding of multiple, hierarchically structured complex systems, at varying levels of abstraction from linguistic, to motor control, to even more general underlying processes. Understanding the various power-law relationships in natural phenomena, and their origins, remains an area of active research [ [ $28,31,42]$.
Regardless of any deeper understanding of underlying mechanisms, our results demonstrate clear patterns in the information conveyed across time in both linguistic and non-linguistic behaviors. These patterns exist. Thus, they are potentially available and useful to any cognitive agent that engages with them. For example, in the movement patterns of a housefly, evolutionary fitness may be conferred to individuals (e.g. predators or mates) that can better anticipate the behavior of others by integrating long-range statistical dependencies. For human language, these selective advantages and abilities seem clear, as sensitivity to long-range organization has obvious benefit for comprehension. Outside of language, evidence for long-range sensitivities is more sparse, but humans do show scale invariance in retrospective memory tasks [Ш08] and attention to power-law timescales in anticipation of future events in cognitive tasks [40.9]. The extent to which non-human animals are sensitive to the long-range dynamics (power-law or otherwise) of information in the environment is unknown. If non-human animals can model the long-range statistical dependencies present in their environment, this capacity would constitute a component of the broad faculty of language [III], that is, a necessary, but not uniquely-human, component of language. The presence of long-range statistical dependencies in non-linguistic behaviors and a generalized perceptual sensitivity to them would provide a scaffold on which language could evolve, and where hierarchical syntax and semantics can be understood as later additions that exploit existing long-range structures and sensitivities. We refer to this idea as the Statistical Scaffolding Hypothesis.

## 5 Methods

### 5.1 Mutual information

For each dataset, we calculate the sequential MI over the elements of the sequence dataset (e.g. words produced by a child, actions performed by Drosophila). Each element in each sequence is treated as unique to that transcript to account for different distributions of behaviors across different transcripts within datasets.
Given a sequence of discrete elements $a \rightarrow b \rightarrow c \rightarrow d \rightarrow e$ We calculate mutual information as:

$$
\begin{equation*}
I(X, Y)=S(X)+S(Y)-S(X, Y) \tag{1}
\end{equation*}
$$

Where $X$ and $Y$ are the distributions of single elements at a given distance. For example, at a distance of two, $X$ is the distribution $[a, b, c]$ and $Y$ is $[c, d, e]$ from the set of element-pairs $(a-c, b-d$, and $c-e)$. $\hat{S}(X)$ and $\hat{S}(Y)$ are the marginal entropies of the distributions of $X$ and $Y$, respectively, and $\hat{S}(X, Y)$ is the entropy of the joint distribution of $X$ and $Y$.

To estimate entropy, we employ the Grassberger [【T] method which accounts for under-sampling true entropy from finite samples:

$$
\begin{equation*}
\hat{S}=\log _{2}(N)-\frac{1}{N} \sum_{i=1}^{K} N_{i} \psi\left(N_{i}\right) \tag{2}
\end{equation*}
$$

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where $\psi$ is the digamma function，$K$ is the number of categories of elements（e．g．words or phones）and $N$ is the total number of elements in each distribution．

We then adjust the estimated MI to account for chance．To do so，we subtract a lower bound estimate of chance MI（ $\hat{I}_{s h}$ ）：

$$
\begin{equation*}
M I=\hat{I}-\hat{I}_{s h} \tag{3}
\end{equation*}
$$

This sets chance MI at zero．We estimate MI at chance $\left(\hat{I}_{s h}\right)$ by calculating MI on permuted distributions of labels $X$ and $Y$ ：

$$
\begin{equation*}
\hat{I}_{s h}(X, Y)=\hat{S}\left(X_{s h}\right)+\hat{S}\left(Y_{s h}\right)+\hat{S}\left(X_{s h}, Y_{s h}\right) \tag{4}
\end{equation*}
$$

$X_{s h}$ and $Y_{s h}$ refer to random permutations of the distributions $X$ and $Y$ described above．Permuting $X$ and $Y$ effects the joint entropy $S\left(X_{s h}, Y_{s h}\right)$ in $I_{s h}$ ，but not the marginal entropies $S\left(X_{s h}\right)$ and $S\left(Y_{s h}\right)$ ．$\hat{I}_{s h}$ is related to the Expected Mutual Information［ $[12-\pi 1]$ which accounts for chance using a hypergeometric model of randomness．
Importantly，MI calculated over a sequence as a function of distance is referred to as a＂mutual information function＂，to distinguish it as the functional form of mutual information，which measures the dependency between two random variables［14］．In the mutual information function，samples from the distributions $X$ and $Y$ are taken from the same sequence，thus they are not independent．MI as a function of distance acts as a generalized form of the correlation function that can be computed over symbolic sequences and captures non－linear relationships［14］．

## 5．2 Fitting mutual information decay

We fit the three following models：
An exponential decay model：

$$
\begin{equation*}
M I=a * e^{-x * b}+f \tag{5}
\end{equation*}
$$

A power－law model：

$$
\begin{equation*}
M I=c * x^{d}+f \tag{6}
\end{equation*}
$$

A composite model of the power－law and exponential models：

$$
\begin{equation*}
M I=a * e^{-x * b}+c * x^{d}+f \tag{7}
\end{equation*}
$$

where $x$ represents the inter－element distance between units（e．g．phones or syllables）．
To fit the model on a logarithmic scale，we computed the residuals between the log of the MI and the log of the models estimation of the MI．We scaled the residuals during fitting by the $\log$ of the distance between elements to emphasize fitting the decay in log－scale because distance was necessarily sampled linearly as integers． Models were fit using the lmfit Python package［ $[5]$ using Nelder－Mead minimization．We compared model fits on the basis of AICc and report the relative probability of each model fit to the MI decay［ $[, \mathbb{L}, ~$ ］．The parameters for each best－fit model for Figs 『，迅，and 四can be found in Table 四．

## 5．3 Shuffling controls

The speech datasets are organized hierarchically into transcripts，utterances，words，and phonemes allowing us to shuffle the dataset at multiple levels of organization．In the Epic Kitchens，Drosophila，and zebrafish datasets no levels of organization were available beyond individual transcripts．To ensure that our MI decay results are a direct result of the sequential organization of each dataset，we performed a control in each dataset in which we shuffled behavioral elements within each individual transcript．In each case，the MI decay is flat confirming that the observed MI decay is a result of sequential organization（Figs S2F，S2E， S10）．To ensure that long－range relationships were not due to trivial repetitions of behaviors，we looked in each dataset at MI decay over sequences in which repeated elements were removed．Removing repeats does not qualitatively alter the pattern of long－range relationships between elements（Fig．S4）．

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### 5.4 Data Availability

The five datasets can be acquired from the TalkBank repository [ $\times 6]$, PhonBank repository [ 8.5$]$, Berman et al. [56], Damen et al., [49], and Marques et al., [00]]. We performed analyses over these transcripts without any modification. Example transcripts for each dataset are displayed in the Supplementary Information. The distribution of sequence lengths of each dataset is shown in Fig. S1. The code necessary for reproducing our results is available on GitHub [【7].

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## 6 Supplementary Materials

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Figure S1: Distribution of sequence lengths for each dataset.

A


B


C


D


Shuffled within utterance






E








Figure S2: MI decay between phones under different shuffling conditions. (A) MI decay for each age group from the entire dataset, as in Fig. 2A. The sequence above the MI decay shows an example set of utterances of the corpus to illustrate the shuffling conditions. Utterances are grouped by color, words are grouped by rounded rectangles, and phones are displayed in bold above orthographic transcriptions. (B) Words are shuffled within each transcript. (C) Phones are shuffled within words. (D) Phones are shuffled within utterances. (E) Utterances are shuffled within each transcript. (F) Phones are shuffled within each transcript. The best fit model is printed above each plot, and is plotted as grey lies alongside the data and in Fig. 1.

A


B


C


D


Figure S3: MI decay between words under different shuffling conditions. (A) MI decay for each age group from the entire dataset, as in Fig. 2D. (B) Words are shuffled within each utterance. (C) Utterances are shuffled within each transcript. (D) MI is calculated over part-of-speech transcriptions of words. (E) Words are shuffled within each transcript. (F) Words are shuffled within each transcript. The best fit model is printed above each plot, and is plotted as grey lies alongside the data and in Fig. 1.


Figure S4: MI decay with repeated elements removed across each dataset.


Figure S5: MI decay and best fit model of five largest transcripts for each age group across PhonBank. Transcript identity and best fit model are displayed above each plot.

12-18 months







24-30 months



30-36 months



$36+$ months


Figure S6: MI decay and best fit model of five largest transcripts for each age group across CHILDES. Transcript identity and best fit model are displayed above each plot.


Figure S7: MI decay over the 20 longest Epic kitchens cooking sequences. Transcript identity and best fit model are displayed above each plot.


Figure S8: MI decay of example individual Drosophila behavioral sequences over one hour. Transcript identity and best fit model are displayed above each plot.


Figure S9: MI decay of several individual Zebrafish behavioral sequences. Each plot corresponds to the continuous behavior of a single Zebrafish. Each row corresponds to a different behavioral setting. The behavioral setting is written above the plot alongside the best fit model.


Figure S10: MI decay of shuffled sequences for Drosophila, Zebrafish, and Epic Kitchens datasets. No information decay is seen between elements of any sequence.

|  |  | $12-18$ months | $18-24$ months | $24-30$ months | $30-36$ months | $3+$ years |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| AICc | exp. | -313.876 | -696.201 | -1464.82 | -735.697 | -2314.6 |
|  | combined | -322.789 | -819.742 | -1737.37 | -951.049 | -2989.21 |
|  | power-law | -296.67 | -746.061 | -1623 | -933.579 | -2939.72 |
| $r^{2}$ | exp. | 0.997 | 0.992 | 0.991 | 0.986 | 0.973 |
|  | combined | 0.998 | 0.998 | 0.998 | 0.998 | 0.995 |
|  | power-law | 0.995 | 0.995 | 0.996 | 0.997 | 0.994 |
| Relative likelihood | exp. | 0.012 | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ |
|  | power-law | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
| Relative probability | exp. | 0.011 | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | 0.989 | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ |
|  | power-law | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |

Table 1: CHILDES dataset model fit results for each decay model as shown in Fig. 2.

|  |  | $6-12$ months | $12-18$ months | $18-24$ months | $24-30$ months | $30-36$ months | $3+$ years |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |
| AICc | exp. | -5687.13 | -4842.29 | -4240.44 | -1371.61 | -1091.13 | -417.621 |
|  | combined | -5998.03 | -5302.25 | -5025.96 | -1903.5 | -1522.77 | -484.369 |
|  | power-law | -5993.7 | -5288.72 | -4971.83 | -1836.16 | -1369.5 | -437.315 |
| $r^{2}$ | exp. | 0.803 | 0.878 | 0.928 | 0.967 | 0.983 | 0.989 |
|  | combined | 0.841 | 0.919 | 0.971 | 0.995 | 0.998 | 0.996 |
|  | power-law | 0.841 | 0.918 | 0.969 | 0.994 | 0.996 | 0.992 |
| Relative likelihood | exp. | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ |
|  | power-law | 0.115 | 0.001 | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
| Relative probability | exp. | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | 0.897 | 0.999 | $>0.999$ | $>0.999$ | $>0.999$ | $>0.999$ |
|  | power-law | 0.103 | 0.001 | $<0.001$ | $<0.001$ | $<0.001$ | $<0.001$ |

Table 2: PhonBank dataset model fit results for each decay model as shown in Fig. 2.

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|  |  | Cooking | Drosophila | Zebrafish |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
| AICc | exp. | -236.312 | -6513.67 | -5125.71 |
|  | combined | -269.057 | -11115.3 | -7340.27 |
|  | power-law | -269.846 | -8894.93 | -6066.59 |
| $r^{2}$ | exp | 0.98 | 0.952 | 0.918 |
|  | combined | 0.991 | 0.999 | 0.991 |
|  | power-law | 0.991 | 0.996 | 0.968 |
| Relative likelihood | exp. | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | 0.674 | $>0.999$ | $>0.999$ |
|  | power-law | $>0.999$ | $<0.001$ | $<0.001$ |
| Relative probability | exp. | $<0.001$ | $<0.001$ | $<0.001$ |
|  | combined | 0.403 | $>0.999$ | $>0.999$ |
|  | power-law | 0.597 | $<0.001$ | $<0.001$ |

Table 3: Epic Kitchens, Drosophila, and Zebrafish model fit results at 45, 1000, and 1000 elements of distance respectively.

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| Dataset | Age (yrs) | $a$ | $b$ | $c$ | $d$ | $f$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| CHILDES | $1-1.5$ | $0.387 \pm 0.101$ | $0.645 \pm 0.113$ | $0.145 \pm 0.038$ | $-1.382 \pm 0.345$ | $0.168 \pm 0.003$ |
|  | $1.5-2.0$ | $0.194 \pm 0.022$ | $0.382 \pm 0.034$ | $0.283 \pm 0.016$ | $-1.461 \pm 0.083$ | $0.057 \pm 0.001$ |
|  | $2-2.5$ | $0.185 \pm 0.022$ | $0.418 \pm 0.033$ | $0.346 \pm 0.014$ | $-1.464 \pm 0.04$ | $0.04 \pm 0.0$ |
|  | $2.5-3.0$ | $0.239 \pm 0.099$ | $0.753 \pm 0.105$ | $0.391 \pm 0.039$ | $-1.367 \pm 0.053$ | $0.027 \pm 0.0$ |
|  | $>3$ | $0.639 \pm 0.065$ | $1.082 \pm 0.047$ | $0.223 \pm 0.022$ | $-1.238 \pm 0.041$ | $0.008 \pm 0.0$ |
| PhonBank | $0.5-1$ | $0.326 \pm 0.065$ | $0.391 \pm 0.045$ | $0.301 \pm 0.041$ | $-1.013 \pm 0.087$ | $0.035 \pm 0.002$ |
|  | $1-1.5$ | $0.404 \pm 0.047$ | $0.463 \pm 0.021$ | $0.446 \pm 0.029$ | $-1.137 \pm 0.027$ | $0.016 \pm 0.0$ |
|  | $1.5-2$ | $0.891 \pm 0.098$ | $0.794 \pm 0.032$ | $0.358 \pm 0.042$ | $-1.234 \pm 0.044$ | $0.005 \pm 0.0$ |
|  | $2-2.5$ | $1.225 \pm 0.136$ | $0.877 \pm 0.054$ | $0.305 \pm 0.043$ | $-1.219 \pm 0.046$ | $0.002 \pm 0.0$ |
|  | $2.5-3$ | $1.112 \pm 0.255$ | $0.908 \pm 0.1$ | $0.38 \pm 0.082$ | $-1.381 \pm 0.07$ | $0.001 \pm 0.0$ |
|  | $>3$ | $1.019 \pm 0.371$ | $0.857 \pm 0.137$ | $0.476 \pm 0.132$ | $-1.433 \pm 0.087$ | $0.001 \pm 0.0$ |
| Drosophila | - | $0.155 \pm 0.002$ | $0.014 \pm 0.0$ | $1.1 \pm 0.004$ | $-0.506 \pm 0.002$ | $0.04 \pm 0.001$ |
| Zebrafish | - | $0.943 \pm 0.054$ | $1.33 \pm 0.051$ | $0.06 \pm 0.005$ | $-0.661 \pm 0.052$ | $0.0 \pm 0.001$ |
| Cooking | - | - | - | $0.227 \pm 0.029$ | $-1.133 \pm 0.18$ | $0.023 \pm 0.003$ |

Table 4: MI decay parameters for Figs [, 远, and 田. The parameters correspond to Equation $\mathbb{\square}\left(a * e^{-x * b}+c *\right.$ $\left.x^{d}+f\right) . a$ and $b$ for the Cooking dataset are not shown because the best-fit model is the power-law model.

| $\mathrm{he} \mathrm{( } \mathrm{xxx}$ ) | $3 \varepsilon$ ( xxx ) | $\varepsilon$ ( xxx ) |
| :---: | :---: | :---: |
| je (xxx) | hnjılalalajæ (xxx) | ? ( xxx ) |
| gig (xxx) | bababa (xxx) | 1e: (xxx) |
| $\varepsilon$ ( xxx ) | 2عow ${ }^{\text {w }}$ (xxx) | 2e ( xxx ) |
| 1e ( xxx ) | bi: (xxx) | $\mathrm{h} \varepsilon$ ( xxx ) |
| PiPe (xxx) | jae (xxx) | $\varepsilon$ ( Xxx ) |
| $\mathrm{h}, ~(\mathrm{xxx})$ | æ ( xxx ) | 2i ( xxx ) |
| jæh¢? (xxx) | he ( xxx ) | 2 $\mathfrak{Z x}$ ( (xxx) |
| Pæ ( xxx ) | $\beta:(x x x)$ | 1e ( xxx ) |
| he? (xxx) | dejehe ( xxx ) | ijẽ: (xxx) |
| he ( xxx ) | eje:he (xxx) | hæi (xxx) |
| he ( xxx ) | æ ( xxx ) | $\mathrm{hcd}{ }^{\text {h }}$ (xxx) |
| 2I ( xxx ) | $\mathrm{d}^{\mathrm{w}} æ(\mathrm{xxx}$ ) | hi (xxx) |
| hi ( xxx ) | 3n:ow (xxx) | læ (xxx) |
| hæ ( xxx ) | m ( $\mathrm{x} x \mathrm{x}$ ) | 3^( xxx ) |
| $\mathrm{he} \mathrm{(xxx)}$ | hæ (xxx) | titıde (xxx) |
| 2e ( xxx ) | 1æP^2di (xxx) | sædı (xxx) |
| 1ع:æ (xxx) | $\mathrm{p}^{\mathrm{h}}$ (xxx) | 1^:æo (xxx) |
| عæ: (xxx) | mbu? (xxx) | २æ ( xxx ) |
| $\varepsilon$ ( xxx ) | bubwi (xxx) | 1ع: (xxx) |
| æа (xxx) | 2e: (xxx) | Puf (xxx) |
| 2عRPi? (xxx) | г̃jæ̃ ( xxx ) | wi (xxx) |
| 18 ( xxx ) | hn: ( xxx ) | he: ( xxx ) |
| 18 ( xxx ) | ms ( xxx ) | $\mathrm{h} \varepsilon$ ( xxx ) |
| di ( xxx ) | $\varepsilon(\mathrm{xxx})$ | २æıj¢: (xxx) |
| عใع:æ: (xxx) | hejæ (xxx) | 1^чо? (xxx) |
| j¢jĩ (j@l) | dæwu (xxx) | 17? (xxx) |
| jæ̃jẽ (xxx) | $\mathrm{w} \mathrm{\varepsilon}$ ( xxx ) | TıPع: (xxx) |
| hæ ( xxx ) | hi ( xxx ) | 2ع:æ¢ (xxx) |
| $\mathrm{h} \varepsilon$ ( xxx ) |  | æ ( xxx ) |
| hæh (xxx) | he:jæย (xxx) | $\varepsilon$ ( XXx ) |
| $\mathrm{h} \varepsilon$ ( xxx ) | 1e? (xxx) | 18 ( xxx ) |
| 2e ( xxx ) | عæ: (xxx) | 18 ( xxx ) |
| hæ (xxx) | PIPE (xxx) | gutf (xxx) |
| $\mathrm{b}^{\mathrm{w}} \mathrm{n}^{2} \beta$ ( xxx ) | jæwع (xxx) |  |

## 7 Example sequences from datasets

### 7.1 PhonBank

A random sample of the transcripts used in this manuscript at different ages. Each line corresponds to an utterance and each utterance is followed by an orthographic representation in parentheses. ' $x x x$ ' in orthographic transcription refers to unintelligible speech and 'yyy' refers to phonological coding. The meanings of other coding symbols such as '@' and '\&' used in orthographic representations can be found in the TalkBank manuals for PhonBank and CHILDES.

### 7.1.1 Davis/Nate/001105.xml 11 months

### 7.1.2 Providence/William/011115.xml 23 months

wə 'di (what's this)
'ni (yyy)
'ı di 'kwomə (are yyy yyy)
u'kwo 'wa: (yyy yyy)
a'kwo 'wa (yyy yyy)
'ma'mi (mommy)
'jami (yummy)
'ðus (juice)
'j $\wedge$ mi: (yummy)
'gu 'd3us (good juice)
'ja (yah)
'au inə 'ta'mei (I wanna Thomas)
'ıwə 'tamut (yyy Thomas)
'tam I'Ifip (Thomas yyy)
'bs'kei (pocket)
'no? 'no 'bagit (yyy no pocket)
'no 'bıg'ct (no pocket)
'no 'bıket (no pocket)
'nu (no)
'okei (okay)
' 5 (yyy)
'okei (okay)
'okei (okay)
'je (yeah)
'oge (okay)
'ei (yyy)
'was (why)
wə 'tow Iz It (what time is it)
'wai 'wai (why why)
no (no)
'okeı (okay)
'je (yeah)
n:o: (no:)
'open (open)
'o (no)
o'ben (open)
'dæ' 1 (daddy)
'dæ'fi (daddy)
'dæ'гi (daddy)
'dæ'si (daddy)
'dæri (daddy)
'dæ'ءi (daddy)
ə'dæri (daddy)
'dæ: (daddy)
'no (no)
'no (no)
'ba'bıs (yyy)
'no (no)
'no 'd3ıkə 'bu bum (no
$\hookrightarrow$ chicka_boom_boom@si)
' $\Lambda$ 'no $\boldsymbol{\jmath}$ 'd $\Lambda$ n (yyy no all done)
'arjə 'nı? ' $\boldsymbol{\sim}$ ' 'nu 'gımə (yyy yyy
$\hookrightarrow \quad$ ууу ууу ууу)

```
'wın 'dæd 'ama (wan dad yyy)
'no (no)
'no 'a 'wa (no ice pop)
'no (no)
' \(\varepsilon\) 'no (yyy no)
'æbəlæs (ambulance)
'hæmbə'lint (hi ambulance)
'æbəlæns (ambulance)
ə'wæ'wiw (yyy)
'farjəz'dzint (fire + engine)
no (no)
'no 't trak (no truck)
'wa də 'tivi (watch the tv)
'boni (Barney)
'boni (Barney)
'nı?'o (no)
'mu? (yyy)
'wı 'hi'jı (right here)
' \({ }^{\prime}\) wns 'i? (yyy what it)
'mı wne 'iz 'it 'twak (yyy what is
\(\rightarrow\) it truck)
'u: 'u (ooh ooh)
'no: (no)
' \(\Lambda\) ? 'o (uhoh)
ðә 'd \(\Lambda \mathrm{m}^{\prime}\) tr \(\wedge \mathrm{k}\) (the dump + truck)
\(\mathrm{t}^{\wedge}{ }^{\wedge} \Lambda \mathrm{k}\) (truck)
i'nait (night + night)
* 't \(\int\) rık ( xxx truck)
```

* 'tsbak (xxx truck)
* 'trak (xxx truck)
* (xxx)
'di jə 'si: (do you see)
'nini 'ditfi 't $\int$ rık (yyy yyy truck)
'mibebit * (yyy xxx)
't ${ }^{\prime} \Lambda \mathrm{k}$ (truck)
'nı 'ninəðəðəə 'tr^k (yyy yyy truck)
* 't fr r k (xxx truck)
* 'trak (xxx truck)
* 't frak (xxx truck)
'd $\Lambda^{\prime} \mathrm{t}$ 「rık (dump + truck)
iz 'dæ ə 't $\int$ rık (is that a truck)
'hiz 'trak (a truck)
'trık 'dæt 't $\int$ rık (truck that truck)
't $\int_{\Lambda}$ * (truck xxx)
'o'hei (okay)
' $\Lambda$ 2 ' $\Lambda$ 'ızə * 'pızə (yyy yyy yyy
$\hookrightarrow \quad x x x$ puzzle)
* (xxx)
* (xxx)
'da (yeah)
'no: 'no 'no 'nop (no: no no no)
'ei 'bi 'si:z (abcs)


### 7.1.3 Goad/Julia/20510.xml 29 months

587
$\mathrm{t}^{\mathrm{h}_{3}} 3 \mathrm{p}^{\mathrm{h}} \mathrm{ap}^{\mathrm{h}}$ (toast pop)
2^ bìlũ:w (a balloon)
bıık ${ }^{\mathrm{h}}$ babo (big bubble)
ə najin (a lion)
wuhəs dat $\mathrm{k}^{\mathrm{h}} \mathrm{ij}$ duwin (what's
$\hookrightarrow \quad$ that kid doing)
$\mathrm{d} \wedge \mathrm{n}^{\mathrm{h}} \varepsilon \mathrm{p}^{\mathrm{h}} \mathrm{k}^{\mathrm{h}}$ (can 0of paint)
wns də mæn dowẽ (what's the
$\hookrightarrow$ man doing)
$\mathrm{k}^{\mathrm{h}} \Lambda$ рfajə (campfire)
$\tilde{\partial}^{\mathrm{h}^{\mathrm{h}}} \mathrm{Epfaj}^{\mathrm{h}} \mathrm{t}^{\mathrm{h}}$ عw maj mam (campfire
$\rightarrow$ tell my mom)
mej $\mathrm{k}^{\mathrm{h}} æ \mathrm{pfaj} \Lambda$ (make campfire)
$\mathrm{t}^{\mathrm{h}} \Lambda$ muw $\mathrm{t}^{\mathrm{h}} \Lambda$ min (camel coming)
di hə bəlow (this is blue)
Rawfit ${ }^{\text {(elephant) }}$
$3 \Lambda$ bejbij $\partial$ fit $^{\mathrm{h}}$ (a baby elephant)
wns ə ne:j duwin (what's the lady $\hookrightarrow$ doing)
wij $\theta$ dow raf (wings fell off) wəhe ə fax duwẽn (what are frogs $\hookrightarrow$ doing)
$\mathrm{t}^{\mathrm{h}} \varepsilon \mathrm{k}^{\mathrm{h}} \mathrm{In}$ dowẽn (chicken doing)
$\mathrm{w} \Lambda \varepsilon \varepsilon^{\mathrm{t}} \Lambda \mathrm{h}$ kijn duwin (what the
$\hookrightarrow$ chicken doing)
 $\hookrightarrow \quad$ the baby talkin about)
jis maj dæ? Ifft $^{\text {h }}$ ?is (yes my dad $\hookrightarrow \quad$ shaved his)
in ə boks (in a books)
w $\Lambda$ s $\mathrm{k}^{\mathrm{h}} æ \mathrm{~m} \Lambda \mathrm{~d} \Lambda$ ?in (what's camel
$\hookrightarrow$ doing)
jes aj duuw (yes I do)
w $\Lambda \mathrm{t}^{\mathrm{h}} æ \mathrm{~m} \wedge$ d $\Lambda$ әĨ (what camel
$\rightarrow$ doing)
$\mathrm{p}^{\mathrm{h}}$ IW mami sej (what mommy $\hookrightarrow$ say)
wə ðә mamij sejı (what the
$\rightarrow$ mommy saying)
wu dædij duwiy (what daddy
$\hookrightarrow$ doing)
Pa du dæ then (I do that too)
æn mij $\mathrm{t}^{\mathrm{h}} \Lambda$ (and me too)
ws him duwəin (what him doing)
h $\Lambda$ bejbij thajin (the baby crying)
ws ðә mæn duwəjın (what the
$\hookrightarrow$ man doing)
?a du dæt ${ }^{\text {h }}$ (I do that)
$\mathrm{k}^{\mathrm{h}} \tilde{\varepsilon} c i ̃ j$ (sixteen)
Rowh je mãk ${ }^{\text {hinn }}$ dowĩ (what the $\hookrightarrow$ monkey doing)

$\rightarrow$ (yeah me too I do that too)
?a duw dæ? thow (I do that too)
?æn niçlıs $\mathrm{t}^{\mathrm{h}} \Lambda$ (and Nicolas too)
Raj owphẽj maj d $\Lambda$ f (I open my
$\rightarrow$ mouth)
w $\mathrm{j}^{\prime} \mathrm{p}^{\mathrm{h}}$ ejn2fif duwəjĩ (what the $\hookrightarrow$ peoples doing)
we ja $\mathrm{p}^{\mathrm{h}_{3}} \int_{\mathrm{I}}$ (what the person)
$l^{1 t} t^{\mathrm{h}} \boldsymbol{\rho} \mathrm{p}^{\mathrm{h}} \varepsilon \mathrm{p}^{\mathrm{h}} \mathrm{I} \int$ dojin (little peoples
$\hookrightarrow$ doing)
$\mathrm{p}^{\mathrm{h}} \boldsymbol{\varepsilon}^{\mathrm{h}}$ Rawu (pet owl)
Pa duw dæt $\mathrm{t}^{\mathrm{h}} \mathrm{uw}$ awu (I do that
$\rightarrow$ too Owl)
$\mathrm{n} \Lambda$ fin (no thanks)
h $\wedge$ ? hım duwəjĩn (what him
$\hookrightarrow$ doing)
maj m $\wedge$ m Jow mij (my mom
$\leftrightarrow$ show me)
?en $\mathrm{k}^{\mathrm{h}} \mathrm{e}: \mathrm{t}^{\mathrm{h}} \mathrm{uw}$ (and Kate too)
$\mathrm{k}^{\mathrm{h}} \varepsilon \mathrm{t}^{\mathrm{h}}$ owm (Kate too)
?esajk ${ }^{\mathrm{h}}$ (outside)
maj dæ duw dæt ( $m y$ dad do
$\rightarrow$ that)
?en maj mam duw de? (and my
$\hookrightarrow$ mom do that)

Sainburg, Mai, and Gentner
bejbij thaje: (baby tired) də bejbi日 thajə (the baby's tired)
dowĩj $\overline{\mathrm{t}} \Lambda$ (drying himself) ${ }_{588}$
hap ${ }^{\text {hij }} \mathrm{t}^{\mathrm{h}} \partial \mathrm{j} \wedge$ : (happy to you)

### 7.1.4 Providence/Alex/021122.xml 36 months

'wo 'wats is ' $\varepsilon$ : (yyy what's this $\hookrightarrow$ yyy)
'is 'pwis 'het (yyy yyy yyy)
'u: (yyy)

* 'prirci (xxx pretty)
'prıi (yyy)
'wo 'ai 'lark 'ðæt (whoa I like
$\hookrightarrow$ that)
ə 'pisələ 'kuki 'tfwe 'ps (yyy yyy
$\hookrightarrow \quad$ yyy yyy yyy)
ә 'pıkin (a pumpkin)
'bu: (yyy)
'wu (yyy)
'w w ts 'Is (what's this)
'wats 'is (what's this)
'wats zis (what's this)
'wats is (what's this)
'ıi (yyy)
'u: (ooh)
ə 't tfwolo (a yyy)
'woz 3r də 'wn (those are the yyy)
'ðoz ə ðә 'warə (those are the
$\hookrightarrow$ water)
ðə 'warə 'sli (the water yyy)
$\partial^{\prime}$ tiho * (yyy xxx)
' $\Lambda \mathrm{m}$ 'w w ts is (\&-um what's this)
'gost 'kukis 'wnts 'is (ghost
$\rightarrow$ cookies what's this)
ə 'kukis (a cookies)
' $\Lambda \mathrm{b}$ (уyy)
ә 'bıg (a bug)
'woa: ' $\Lambda z$ zə 'tSIkin (yyy yyy
$\hookrightarrow$ chicken)
'Sıki 'ar 'lark 'dæt 't fıkın (chicken I
$\hookrightarrow$ like that chicken)
'u (ooh)
'u: (ooh)
'u: (ooh)
'sm (\&-um)
'fwut (fruit)
'alivz (olives)
'weips (grapes)
'blu'bevi (blueberry)
'wats 'is (what's this)
'pupə 'gweips (purple grapes)
'wa: 'pwes^1d^ (yyy pretzels)
'OIs (this)
'pwesə (pretzels)
'wau (wow)
't $\int \mathrm{a}^{\wedge} k ə$ lət (chocolate)
'S:aklət (chocolate)
'tfaklit 'd $\wedge \eta k$ (chocolate yyy)
'u: 'wats is (ooh what's this)
'wnts 'סıs (what's this)
'u: ə 'big 'kerk (ooh a big cake)
'wats 'is (what's this)
' $\Lambda \mathrm{b}$ 'wıts 'is (yyy what's this)
'dзəðəts (ууy)
'wnz 'iz 'ðis (what is this)
'wats 'ðIs (what's this)
' $\Lambda j u$ 'is it (yyy eat it)
'spweikos (sprinkles)
'no ðә 'steizəs (no yyy yyy)
'd3i'd3i (Gigi)
'aı: kə 'du ə 'ðı (I can do yyy it)
o'kei (okay)
'o (oh)
* 'mam (xxx Mom)
'j $\varepsilon$ (yeah)
'd3i'd3i * (Gigi xxx)
'd3ws:3i (yyy)
* 'd3i'd3i (xxx Gigi)
'no 'mami (no Mommy)
'wnz 'dari (where's Daddy)
ə 'spwikəl 'donət (a sprinkle $\hookrightarrow$ donut)
'ai 'lark ə 'spwiŋkəəl 'donət (I like
$\hookrightarrow$ a sprinkle donut)
'mami (Mommy)
'ai 'lark ə 'spweipkəl 'donət (I like
$\hookrightarrow$ a sprinkle donut)
'jæ (yeah)
ə 'd $\Lambda$ n 'plering (are 0we done
$\hookrightarrow$ playing)
әi 'd $\wedge$ n 'pleiin (are we done
$\hookrightarrow$ playing)
'mami (Mommy)
ə'lakət $\Lambda_{\Lambda}^{*}$ (yyy xxx)
'al 'terk ju * (I'll take you xxx)
* 'teik * (xxx take xxx)
* 'terk ju (xxx take you)
'as 'lark ə 'terk ju 'mam (I like yyy
$\hookrightarrow$ take you Mom)
'ai 'terk ju (I take you)
$' \Lambda$ wi 'al 'd $\Lambda n$ (are we all done)
'no 'no (no no)
'no (no)
'æpə'sos 'ja (applesauce yyy)
'at (yyy)
'kãndi (candy)
'dzus (juice)
'wot (yyy)
'piz (peas)
'u: (school)
'sku: (school)
ə'weın (swing)
'sta: (star)
'flæg (flag)
'stez (stairs)
' A vin (oven)
'bentf (bench)
'berəm (bedroom)
'bed (bed)
'tau: (towel)
'twei (tray)
'tæf (trash)
'pleit (plate)
'pleit (plate)
'map (mop)
'kom (comb)
'bwum (broom)
' lgg (leg)
'hãnd (hand)
'i: (ear)
't t In (chin)
'sak (sock)
'Ju (shoe)
'ncklas (necklace)
'hæt (hat)
'kar: (sky)
'pa:rri (party)
'no (no)
'fwend (friend)
'p3sən (person)
'bai (bye)
'hai (hi)
'no (no)
'Sapi (shopping)
' 'eig ju (thank you)
'kæwi (carry)
't JeIs (chase)
'd $\wedge \mathrm{mp}$ (dump)
'finis (finish)
'fit (fit)
'hng (hug)
'1ı日: (listen)
'lark (like)
'pwi'tz:nd (pretend)
'rip (rip)
'Serk (shake)
'teist (taste)
'dzenta (gentle)
'wik (think)

| 'wI ${ }^{\text {(wish) }}$ | 'au: (our) |  | ə 'big 'tfwaieingə (a big triangle) |
| :---: | :---: | :---: | :---: |
| 'If (if) | ta'nait (tonight) |  | 'tfwareıgə: * (triangle xxx) |
| 'wud (would) | $\partial^{\prime} \mathrm{g}$ ¢: (yyy) |  | 'twarəgə (triangle) |
| 'nid (need) | 'æft3'(after) |  | 'sı ә 'big * ə 'bıg 'tfraieıngə (yyy |
| 'kud (could) | 'wet (wet) |  | $\hookrightarrow$ a big xxx a big triangle) |
| 'm:st ${ }^{\text {(much) }}$ | 'tani (tiny) |  | 'u: (ooh) |
| 'a: (all) | 'læst (last) |  | ә 'big 's3rkəl (a big circle) |
| 'nndz (under) | 'hat (hot) |  | ə 'big 'tfraîeıgo ə 'big 'skwe: (a |
| 'daun (down) | 'hæpi (happy) |  | $\hookrightarrow$ big triangle a big square) |
| 'bi'said (beside) | 'fæt (fast) |  | 'u: (ooh) |
| 'we: (where) | 'kot ${ }^{\text {h }}$ (cold) |  | ә 'big 'ovəl (a big oval) |
| ${ }^{\prime} \Lambda s$ (us) | ${ }^{\prime} \mathrm{J}$ 'gan (all gone) |  | 'o: (ooh) |
| '才is (this) | 'Serps (shapes) |  |  |
| 'ðem (them) | ə 'tfwareıgə (a triangle) | 590 | $\square($ continued $)$ - |

### 7.2 CHILDES

A random sample of the transcripts used in this manuscript at different ages. Each line corresponds to an utterance and each utterance is followed by transcribed part-of-speech tags.

### 7.2.1 Eng-NA/Braunwald/010511.xml 17 months

| night_night (co) | yeah (co) |
| :--- | :--- |
| night_night (co) | on (adv) |
| here (adv) | Cee (n:prop) |
| it is night_night (pro:per 0cop n) | spider (n) |
| Daddy (n:prop) | Cee (n:prop) |
| spiders (n) | down (adv) |
| oh (co) | byebye (co) |
| me Dwww (pro:obj n:prop) | car (n) |
| on (adv) | car (n) |
| on (unk) | there (adv) |
| no (co) | byebye (co) |
| buttons (unk) | car (n) |
| uh () | car (n) |
| down (adv) | baby (n) |
| water (n) | night_night (co) |
| water (n) | night_night (co) |
| there (adv) | Cee (n:prop) |
| dance there (unk adv) | cookie (unk) |
| ahhah (co) | spoon (n) |
| on (adv) | oh (co) |
| don't (mod~neg) | down (unk) |
| give (v) | down (unk) |
| I want (pro:sub v) | there (adv) |
| Daddy (n:prop) | recorder (n) |
| dance (n) | aya (bab) |
| on (adv) | door (n) |
| I want that that that that | key (n) |
| (Opro:sub v pro:dem) | byebye (co) |
| eh () | car (n) |
| go in there (v prep n) | kitty (n) |
| uhoh (co) | outside (adv) |
| uhoh (co) | bow (on) |
| uhoh (co) | bye (co) |
| yeah (co) | byebye (co) |
| thank you (v pro:per) | bow (on) |
| thank you (v pro:per) | bow (on) |
|  |  |

she lives next door to us (pro:sub
$\leftrightarrow \quad$ v adj $n$ prep pro:obj)
bow (on)
recorder (n)
cookie (n)
no (co)
Deedee (n:prop)
here (adv)
cookie (n)
that that door (det:dem n)
that tata (comp chi)
nose ( n )
eye (n)
ear (n)
Laura (n:prop)
toe ( n )
tickle (n)
toe (n)
ah (co)
uh ()
toe (n)
recorder (unk)
toe ( n )
ah (co)
toe (n)
my toe (det:poss n)
toe ( n )
where (pro:rel)
here (adv)
no (co)
there (adv)

Sainburg, Mai, and Gentner
this is heavy (pro:dem cop adj) saggy baggy doesn't eat a all up $\hookrightarrow \quad$ (adj adj mod~neg v det:art $\rightarrow \quad$ qn adv)
oh no (co co)
le me (v pro:obj)
you going faster (pro:per part
$\rightarrow$ adj)
washer (n)
going go little (part vadv adj)
what is what de the in (pro:int
$\rightarrow$ det:art det:art prep n)
pocket ( n )
dis this one (pro:dem pro:dem
$\hookrightarrow$ pro:indef)
booking (chi)
booking booking booking
$\hookrightarrow$ booking (chi chi chi chi)
booking booking (chi chi)
tease book tease ( n n n )
tease (n)
tease ( n )
tease tease ( n n )
teasing teasing teasing (part part
$\hookrightarrow$ part)
teasing (part)
teasing (part)
tease a Cromer (v det:art n:prop)
what this is car (pro:int det:dem
$\rightarrow$ aux $n$ )
pin (n)
yeah Mommy pin (co n:prop n)
car (n)
yeah (co)
red car (adj n)
yellow car ( n n )
watch ( n )
where horses go (pro:int n v)
where horses (pro:int n)
horse go yes Mommy (n v co
$\rightarrow$ n:prop)
did he (mod pro:sub)
there he is Mommy (adv pro:sub $\hookrightarrow$ cop n:prop)
corral corral (n n)
baby horses ( n n )
horses ( n )
baby horses ( n n )
ready me go (v pro:obj v)
ready me (v pro:obj)
go down dere there ( $v$ prep $n n$ )
go down right side (v adv adj n)
switch ( n )
doing switch (part n)
trick (n)
doin trick (part n)
doing chair tricks (part $n \mathrm{n}$ )
yeah funny (co adj)
chair trick laughing ( n n part)
chair tricks ( $\mathrm{n} v$ )
Mommy chair tricks (n:prop v n $\rightarrow \mathrm{n}$ )
chair tricks chair tricks chair
$\rightarrow \quad$ tricks ( $\mathrm{n} v \mathrm{nvnn}$ )
press a button (v det:art n)
press a button (v det:art n)
yeah (co)
what a happen have a tail
$\hookrightarrow$ (pro:int det:art v v det:art n)
yeah (co)
press a button (v det:art n)
doing rope tricks (part n n)
rope tricks ( $\mathrm{n} v$ )
watch it rope tricks (v pro:per $n$
$\rightarrow$ n)
yeah (co)
watch it (v pro:per)
car car (n n)
fell down Mommy's floor (v prep
$\hookrightarrow \quad \operatorname{adj} \mathrm{n}$ )
throw dat that (v pro:dem
$\leftrightarrow$ pro:dem)
what dat that (pro:int adv adv)
tricks (n)
yep tricks (co v)
press a button (v det:art n )
okay de the horses tail (co det:art
$\hookrightarrow$ det:art n n)
okay horses (co n)
okay horses okay horses (co n adj $\rightarrow$ n)
good night rope tricks (adj n n n )
good night my rope tricks (adj n
$\rightarrow$ det:poss $n$ n)
yeah rope tricks (co $n \mathrm{n}$ )
rope trick fell down ( $\mathrm{n} \mathrm{n} v$ adv)
go tired go tired (v part v part)
Mommy Mommy (n:prop n:prop)
holler doesn't fit in (v mod~neg
$\rightarrow \quad$ v prep $n$ )
horse fit in ( $\mathrm{n} v$ adv prep adv)
ropes ( n )
Mommy roller will stand up
$\hookrightarrow$ (n:prop $n \bmod v a d v)$
try him dere there (v pro:obj adv
$\hookrightarrow$ adv)
Mommy Mommy (n:prop n:prop)
will fit in $(\bmod n$ prep $n)$
see (v)
le me do rope tricks (v pro:obj v
$\rightarrow \quad \mathrm{n}$ n)
let me do ropes (v pro:obj v n)
hello hello hello (co $n \mathrm{n}$ )
what dat that Mommy cowboy
$\hookrightarrow$ (pro:int adv adv n:prop n)
hello cowboy (co n)
wh cowboy (pro:int v n)
wh cowboy (pro:int v n)
happen to him (v prep pro:obj)
wh him (pro:int v pro:obj)
yeah (co)
happen cow watching Rusty
$\hookrightarrow$ down (v n part n:prop adv
$\leftrightarrow$ prep adv)
see him down there (v pro:obj
$\rightarrow$ prep n)
$\qquad$

### 7.2.3 Eng-NA/Carterette/first.xml 72 months

you mean uh um like England or
$\rightarrow$ something (pro:per v conj
$\hookrightarrow$ n:prop coord pro:indef)
when we walk home from school
$\rightarrow \quad$ I walk home with two
$\hookrightarrow \quad$ friends (conj pro:sub v n
$\hookrightarrow \quad$ prep $n$ pro:sub $n$ n prep
$\hookrightarrow$ det:num n)
and sometimes we can't run
$\hookrightarrow$ home from school though
$\hookrightarrow$ (coord adv pro:sub
$\hookrightarrow \quad$ mod $\sim$ neg $v$ adv prep $n$ adv)
because um one girl where every
$\hookrightarrow$ time she wants to runs she
$\rightarrow$ gets the wheezes and stuff
$\hookrightarrow$ (conj det:num n pro:rel qn $n$
$\hookrightarrow$ pro:sub v inf v pro:sub v
$\hookrightarrow$ det:art v coord $n$ )
and then she can't breathe very
$\hookrightarrow$ well and she gets sick (coord
$\rightarrow$ adv:tem pro:sub mod~neg v
$\hookrightarrow$ adv adv coord pro:sub v adj)
that's why we can't run
$\rightarrow$ (pro:dem~cop pro:int
$\leftrightarrow$ pro:sub mod~neg v)
I like to go to my grandmother's
$\rightarrow$ house (pro:sub v inf v prep
$\hookrightarrow$ det:poss adj n)

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well because she gives us candy $\hookrightarrow$ (co conj pro:sub v pro:obj n) well um we eat there sometimes $\hookrightarrow$ (co pro:sub v adv adv) sometimes we sleep overnight
$\hookrightarrow$ there (adv pro:sub vadv $\rightarrow$ adv)
sometime when I go to go to my
$\hookrightarrow$ cousin's I get to play softball
$\hookrightarrow$ or play badminton and all
$\hookrightarrow$ that (adv conj pro:sub vinf v
$\hookrightarrow$ prep det:poss adj pro:sub v
$\hookrightarrow \quad$ prep $n \mathrm{n}$ coord n n coord $q n$
$\hookrightarrow$ pro:dem)
thing I hate to play is doctor ( n $\hookrightarrow$ pro:sub v prep $n$ cop v) oh (co)
I hate to play doctor or house or
$\hookrightarrow$ that (pro:sub v prep n n
$\hookrightarrow$ coord $n$ coord pro:dem)
don't like it or stuff (mod~neg v
$\hookrightarrow$ pro:per coord $n$ )
we've been learning a_lot_of
$\hookrightarrow$ Spanish words (pro:sub~aux
$\hookrightarrow$ aux part qn n:prop n)
our teacher speaks Spanish
$\hookrightarrow \quad$ sometimes (det:poss n v
$\hookrightarrow \quad$ n:prop adv)
so does my father (adv v det:poss
$\hookrightarrow$ n)
yyy ()
well my father doesn't know very
$\hookrightarrow$ much Spanish (co det:poss n
$\hookrightarrow \quad \bmod \sim$ neg $v$ adv adv n:prop)
but he doesn't know what gray is
$\hookrightarrow \quad$ in Spanish (conj pro:sub
$\hookrightarrow \quad$ mod $\sim$ neg v pro:int adj aux
$\hookrightarrow$ prep n:prop)
and its (coord det:poss L2)
and he doesn't and he knows
$\hookrightarrow$ what blue is in Spanish
$\rightarrow$ (coord pro:sub v pro:int n
$\hookrightarrow$ cop prep n:prop)
and he knows what um red is
$\rightarrow$ (coord pro:sub v pro:int n $\rightarrow$ cop)
in Spanish (prep n:prop)
and sometimes I like to go to
$\hookrightarrow$ Mexico but I've never been
$\leftrightarrow$ there before (coord adv
$\hookrightarrow$ pro:sub v inf v prep n:prop
$\hookrightarrow \quad$ conj pro:sub~aux adv cop
$\hookrightarrow$ adv adv)
only when I was a little teeny
$\hookrightarrow$ baby I been there and I don't
$\hookrightarrow$ even remember it (adv conj
$\hookrightarrow$ pro:sub cop det:art adj adj n
$\hookrightarrow$ pro:sub cop adv coord
$\hookrightarrow$ pro:sub mod~neg adv v
$\hookrightarrow$ pro:per)
there this one night I couldn't get
$\hookrightarrow$ any food (adv pro:dem
$\hookrightarrow$ pro:indef $n$ pro:sub
$\hookrightarrow \quad$ mod~neg v qn $n$ )
I mean there was this one day I
$\hookrightarrow$ couldn't get any food at
$\hookrightarrow$ home unless I asked it for
$\hookrightarrow \quad$ Spanish (pro:sub v adv cop
$\hookrightarrow$ det:dem det:num n pro:sub
$\hookrightarrow \quad \bmod \sim$ neg v qn $n$ prep adv
$\hookrightarrow \quad$ conj pro:sub v pro:per prep
$\rightarrow \mathrm{n}$ :prop)
my um my mother and father is
$\rightarrow$ going to pretty soon take us
$\hookrightarrow$ to Philadelphia (det:poss
$\hookrightarrow$ det:poss $n$ coord $n$ aux part
$\rightarrow \quad$ inf adj adv v pro:obj prep
$\rightarrow$ n:prop)
and we're going to see our
$\hookrightarrow$ grandmother there (coord
$\rightarrow$ pro:sub~aux part inf v
$\hookrightarrow$ det:poss $n$ adv)
I wish we went to (pro:sub v
$\rightarrow$ pro:sub v prep)
uh we went to Mexico not
$\hookrightarrow$ Mexico San_Diego once
$\rightarrow \quad$ (pro:sub v prep n:prop adv)
and they had a little um pool that
$\hookrightarrow$ was full of water and it was
$\rightarrow$ two feet (coord pro:sub v
$\hookrightarrow \quad$ det:art adj n pro:rel cop adj
$\hookrightarrow \quad$ prep $n$ coord pro:per cop
$\hookrightarrow$ det:num n)
and then they and then they had
$\leftrightarrow$ another pool (coord adv:tem
$\hookrightarrow$ pro:sub v qn n)
it was five feet eight feet (pro:per
$\hookrightarrow$ cop det:num $n$ det:num $n$ )
Randy my brother went in eight
$\hookrightarrow$ feet and I went in five feet
$\hookrightarrow$ (n:prop det:poss $n$ v prep
$\hookrightarrow$ det:num $n$ coord pro:sub v
$\hookrightarrow$ prep det:num n)
and I think there was a three feet
$\hookrightarrow$ (coord pro:sub v adv cop
$\rightarrow$ det:art det:num n)
there was (pro:exist cop)
and I jumped off and I uh and I
$\hookrightarrow$ jumped off the edge of the
$\hookrightarrow$ swimming pool (coord
$\hookrightarrow$ pro:sub v prep det:art n prep
$\hookrightarrow$ det:art n:gerund n)

I got on the edge and I jumped
$\hookrightarrow$ off (pro:sub v prep det:art n
$\rightarrow$ coord pro:sub v adv)
and then I holded held on to a
$\rightarrow$ edge because I couldn't swim
$\hookrightarrow \quad$ very well (coord adv:tem
$\hookrightarrow$ pro:sub v v adv prep det:art
$\hookrightarrow \quad$ n conj pro:sub mod $\sim$ neg $v$
$\rightarrow$ adv adv)
when I start when I started to
$\hookrightarrow \quad$ swim I was always holding
$\hookrightarrow \quad$ on to the edge (conj pro:sub
$\rightarrow \quad v$ inf $v$ pro:sub aux adv part
$\hookrightarrow$ adv prep det:art n)
I wouldn't dare to go more than
$\hookrightarrow$ this away from the edge or
$\rightarrow$ else I I'd I'd start jumping
$\leftrightarrow$ dancing into the water
$\hookrightarrow$ (pro:sub mod~neg vinf v qn
$\hookrightarrow$ prep pro:dem adv prep
$\hookrightarrow$ det:art n coord post
$\hookrightarrow$ pro:sub~mod v part part
$\hookrightarrow$ prep det:art n)
when my father wanted to take a
$\hookrightarrow$ picture of me with you_know
$\hookrightarrow$ one of those floating things
$\hookrightarrow$ one of those floating rings
$\hookrightarrow$ that you put around you but
$\hookrightarrow$ I don't wanna because
$\hookrightarrow$ you_know I know how to
$\rightarrow \quad$ swim (conj det:poss $n v i n f v$
$\hookrightarrow$ det:art n prep pro:obj prep
$\rightarrow$ co det:num prep det:dem
$\hookrightarrow$ part n pro:indef prep
$\hookrightarrow$ det:dem part $n$ pro:rel
$\hookrightarrow \quad$ pro:per v prep pro:per conj
$\hookrightarrow$ pro:sub mod $\sim$ neg v $\sim$ inf
$\hookrightarrow \quad$ conj co pro:sub v pro:int inf
$\hookrightarrow \quad$ v)
but when I took it off I almost
$\hookrightarrow$ drownded drowned (conj
$\hookrightarrow$ conj pro:sub v pro:per adv
$\hookrightarrow$ pro:sub adv part part)
and I was jumping up and down
$\hookrightarrow$ to see if I could swim or not
$\hookrightarrow$ (coord pro:sub aux part adv
$\hookrightarrow$ coord adv inf v conj pro:sub
$\hookrightarrow \quad \bmod v$ coord neg)
and (coord)
um I live in an apartment and we $\hookrightarrow$ have a big pool and it's eight $\hookrightarrow \quad$ and a half in part and four $\rightarrow$ and a half and three and a $\hookrightarrow$ half (pro:sub v prep det:art n
$\hookrightarrow$ coord pro:sub v det:art adj $n$
$\hookrightarrow$ coord pro:per~cop det:num
$\hookrightarrow$ coord det:art n prep n coord
$\hookrightarrow$ det:num coord det:art n
$\hookrightarrow$ coord det:num coord det:art $\leftrightarrow$ n)
and this summer I get to go
$\hookrightarrow$ swimming in it (coord
$\rightarrow$ det:dem $n$ pro:sub vinf v $\rightarrow$ part prep pro:per)
in the summer we go swimming
$\rightarrow$ (prep det:art n pro:sub v $\rightarrow$ part)
and that's when my birthday is
$\hookrightarrow$ (coord pro:dem~cop conj
$\rightarrow$ det:poss $n$ cop)
we don't go in spring or winter
$\hookrightarrow$ because it's too cold (pro:sub
$\hookrightarrow \quad$ mod $\sim$ neg $v$ prep $n$ coord $n$
$\hookrightarrow \quad$ conj pro:per~cop adv adv)
my my brother can go swimming
$\hookrightarrow$ in the winter though because
$\hookrightarrow$ he gots got his tonsils out
$\hookrightarrow$ you_know (det:poss n mod v
$\hookrightarrow$ part prep det:art $n$ adv conj
$\hookrightarrow$ pro:sub v v det:poss $n$ adv $\rightarrow \quad \mathrm{co}$ )
and he and he gets sick uh sick
$\rightarrow$ um once in a few years
$\hookrightarrow$ (coord pro:sub v adj adv
$\hookrightarrow$ prep det:art qn $n$ )
I get sick just about every day
$\rightarrow$ (pro:sub v adj adv prep qn n)
there's just one thing I can't stand
$\hookrightarrow \quad$ in my family (pro:exist~cop
$\hookrightarrow$ adj det:num $n$ pro:sub
$\hookrightarrow \quad$ mod $\sim$ neg $v$ prep det:poss $n$ )
my baby makes too much noise
$\hookrightarrow$ (det:poss $n$ v adv qn n)
I can't even get get to sleep for a
$\rightarrow$ minute (pro:sub mod~neg
$\hookrightarrow$ adv v prep n prep det:art n)
he won't stop jumping around in
$\rightarrow$ the bath (pro:sub mod~neg
$\hookrightarrow \quad$ v part adv prep det:art n)
in the bath (prep det:art n)
no (co)
in the crib (prep det:art $n$ )
he he keeps jumping around gets
$\hookrightarrow$ tired (pro:sub v part adv v
$\rightarrow$ part)
then he goes to bed then he
$\hookrightarrow$ finally gets to sleep (adv:tem
$\rightarrow$ pro:sub v prep $n$ adv:tem
$\hookrightarrow$ pro:sub adv v prep n)
can't go to sleep in about a hour
$\hookrightarrow \quad(\bmod \sim$ neg $v i n f v a d v$ prep
$\rightarrow$ det:art n)
not with that in the house (neg
$\hookrightarrow$ prep pro:dem prep det:art n)
it would just take two minutes to
$\rightarrow$ get to sleep (pro:per mod
$\hookrightarrow \quad$ adv v det:num $n$ inf v prep
$\hookrightarrow$ n)
just about two minutes (adv prep
$\rightarrow$ det:num n)
if you just um why don't you get
$\hookrightarrow$ some cotton and plug it in
$\hookrightarrow$ your ears and then you can't
$\hookrightarrow$ hear him (pro:int mod~neg
$\hookrightarrow \quad$ pro:per $v$ qn $n$ coord $v$
$\hookrightarrow$ pro:per prep det:poss $n$
$\hookrightarrow$ coord adv:tem pro:per
$\hookrightarrow \quad$ mod $\sim$ neg v pro:obj)
he makes so much noise he
$\hookrightarrow$ makes so much noise it
$\hookrightarrow$ probably sound effect
$\hookrightarrow$ through it (pro:sub v adv qn
$\hookrightarrow \quad \mathrm{n}$ pro:per adv adj n prep
$\rightarrow$ pro:per)
well what does the baby do (co
$\hookrightarrow$ pro:int v det:art n v)
come out get out crawl out_of his
$\rightarrow$ crib and then come along in
$\rightarrow$ your bed and pull out your
$\rightarrow \quad$ ear (v adv v adv n prep
$\hookrightarrow$ det:poss $n$ coord adv:tem v
$\hookrightarrow$ adv prep det:poss $n$ coord $v$
$\rightarrow$ adv det:poss n)
once once he keep jump jumping
$\leftrightarrow$ jumping and then this thing
$\hookrightarrow \quad$ slide down (adv pro:sub v
$\hookrightarrow$ part coord adv:tem det:dem
$\rightarrow \quad \mathrm{n}$ n adv)
and then he fell over to the other
$\hookrightarrow$ bed and he start crying
$\hookrightarrow$ (coord adv:tem pro:sub v adv
$\hookrightarrow$ prep det:art qn $n$ coord
$\hookrightarrow$ pro:sub v part)
and I couldn't get to bed so I I
$\hookrightarrow$ hafta wake up put him back
$\hookrightarrow \quad$ in my crib (coord pro:sub
$\hookrightarrow \quad \bmod \sim$ neg v prep $n$ conj
$\hookrightarrow \quad$ pro:sub mod~inf v adv v
$\rightarrow \quad$ pro:obj adv prep det:poss n)
in your crib (prep det:poss n)
no not in my crib (co neg prep
$\hookrightarrow$ det:poss $n$ )
I don't have a crib (pro:sub
$\hookrightarrow \quad \bmod \sim$ neg v det:art n)
you said put him back in your
$\rightarrow$ crib (pro:per v v pro:obj adv
$\hookrightarrow$ prep det:poss $n$ )
I mean in his crib (pro:sub v prep
$\rightarrow$ det:poss n)
I don't have a crib (pro:sub
$\hookrightarrow \bmod \sim$ neg v det:art n)
uh sometimes I like to go to the I
$\hookrightarrow \quad$ like to go to my
$\hookrightarrow$ grandmothers (adv pro:sub v
$\rightarrow \quad$ inf v prep det:poss n)
I would like to sleep over her at
$\hookrightarrow$ her house every day because
$\hookrightarrow$ she lets me stay up late
$\hookrightarrow$ about ten o'clock or twelve
$\hookrightarrow \quad$ thirty (pro:sub mod vinf v
$\hookrightarrow$ adv prep det:poss $n$ qn $n$
$\hookrightarrow$ conj pro:sub v pro:obj v adv
$\hookrightarrow$ adv prep det:num $n$ coord
$\hookrightarrow$ det:num det:num)
you're lucky (pro:per~cop adj)
I only get to stay up until eight
$\hookrightarrow$ (pro:sub adv v inf v adv prep
$\hookrightarrow$ det:num)
and I only get to stay up until
$\hookrightarrow \quad$ nine (coord pro:sub adv v inf
$\hookrightarrow \quad$ v adv prep det:num)
I get to stay up until um say
$\hookrightarrow$ about between ten o'clock
$\hookrightarrow \quad$ and nine thirty (pro:sub vinf
$\hookrightarrow \quad$ v adv prep v adv prep
$\hookrightarrow$ det:num $n$ coord det:num
$\hookrightarrow$ det:num)
uh and sometimes sometimes I
$\rightarrow$ get to go to bed at twelve
$\hookrightarrow$ thirty (coord adv pro:sub v
$\hookrightarrow \quad$ inf v prep n prep det:num
$\rightarrow$ det:num)
sometimes but most of the times
$\hookrightarrow$ I don't (adv conj qn prep
$\hookrightarrow$ det:art n pro:sub mod~neg)
on holidays and you_know like
$\hookrightarrow$ um weekends (prep n coord
$\hookrightarrow$ co prep n)
on holitinna holidays and I mean
$\hookrightarrow \quad$ on holidays I get to stay up
$\hookrightarrow$ all night (prep n n coord
$\hookrightarrow$ pro:sub v prep n pro:sub v
$\hookrightarrow \quad$ inf vadv qn n)
uh on weekends like when I'm
$\hookrightarrow$ not going to school (prep n
$\hookrightarrow$ prep conj pro:sub~aux neg
$\rightarrow$ part prep n)
see this day I I'm going to school
$\rightarrow$ and then the next day you
$\hookrightarrow$ don't hafta (v det:dem $n$
$\hookrightarrow$ pro:sub~aux part prep $n$
$\leftrightarrow$ coord adv:tem det:art adj $n$
$\hookrightarrow \quad$ pro:per mod~neg mod~inf)

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I can stay up late because I the
$\rightarrow$ next day I can sleep all I
$\rightarrow$ want (pro:sub mod vadv
$\hookrightarrow \quad$ adv conj pro:sub det:art adj
$\hookrightarrow \mathrm{n}$ pro:sub mod n adv pro:sub $\rightarrow$ v)
that's why we hafta go to bed
$\rightarrow$ early on school days
$\rightarrow$ (pro:dem~cop pro:int
$\rightarrow$ pro:sub mod~inf v prep n
$\rightarrow \quad$ adv prep $n \mathrm{n}$ )
every holiday um um my my
$\rightarrow$ grandmother and my aunt
$\rightarrow \quad$ come over (qn $n$ det:poss $n$
$\rightarrow$ coord det:poss $n$ v adv)
well you_know it's because well
$\hookrightarrow$ you_know it's just about
$\rightarrow$ becoming Easter (co co
$\hookrightarrow$ pro:per $\sim$ cop conj adv co
$\rightarrow$ pro:per~aux adj adv part ${ }^{599}$
$\hookrightarrow$ n:prop)
about just twenty days or twenty
$\rightarrow$ one (adv adv det:num n $\rightarrow$ coord det:num det:num)
on Easter I hafta get all this
$\rightarrow$ gooshy egg (prep n:prop
$\rightarrow$ pro:sub mod~inf v qn
$\rightarrow$ det:dem adj n)

### 7.3 Drosophila

One hour of behavioral state transitions from a single example Drosophila. There are 117 unique behavior states. Behavioral states do not have names but belong to broad categories (Posterior, Side Legs, Anterior, Locomotion, Idle, Slow).

594311211151524652 605965462732334052 433943761067652439 492192111216959
464252439214910
5246806980841036043
9214215269664652
432143525360596846
524052394321102143
5243527652319109
1094435248593265
384552453346334052
39443526553605243
494102151435253
65465552432191021
44340323349461533
3951494352535965
596545524352606265
62605248219514352
535046685950462769
806568594957665965
494441444648535966
656659677760435259
655969775355596454
654446655065493259
504449475065695352
435121515739435265
524565664353658053
432139715243525566
465553524352435260
7760677184106988784
9310893678767605253
59655948523921911
211131524565595243
525359692746271532

343943524352605359 46662747493547491 38143850192549738 461522323844461538 353832446549444647 6959524339211049 11494104394033
192746273233454033 463365717971878469 794654322246152744 273549201946271529 142028351544285047 495741375251614965 435121395266686549 46194031211021421
392028203233223528 461938364665666568 454947494450466869 877787848777877946 272030384649654941 324565564965495744 462723343139213919 381940343332153538 364644663549281547 1514274649141214
191514381513193846 201538203865492746 323321109219219 119109119214352 343249462732233340 3921921921435253 684946273239432143 524840444944324645 655980463332524952 456552454932463846

293820283527352720
381546153244271946
494749354947494432
4944354944385614
352214202835493519
35494449204911514
382814382520254925
352744272520464935
274947493549576544
564635476550594149
44222925142714271
21211520382746
192735384649254928
14382063846153549
441571538148738
462538253828141925
1514382714121538
143814191419381927
381949464965496569
444620381533455559
413679384620141532
1315382984469010584
11587555975981039375
90469987107115655932
462038151323333440
393152485965594644
109105937687103938465
985945536546453352
31091121119119
119311931049
21410219219109

604
(continued)

### 7.4 Zebrafish

Behavioral states for zebrafish. Several behavioral contexts are used in this dataset. The example behavioral sequence shown below is acquired during a phototaxis paradigm (SCS: Short Capture Swims; LCS: Long Capture Swims; BS: Burst type forward Swim with high tail-beat frequency; SLC: Fast C-start escape Swims;

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SAT RT S2 RT S1 S1 RT RT HAT S1 RT RT RT RT RT RT
RT RT S1 S1 HAT RT SAT S2
S2 RT RT RT S2 RT S2 S2
HAT RT SAT RT S1 RT S1 S2
HAT S1 HAT S1 S1 S1 RT S1
HAT RT HAT HAT S2 RT HAT S2
S2 RT RT S1 S2 RT S2 RT
S1 RT SAT S2 SAT RT RT S2
S2 O-bend S1 S2 RT S2 RT S2
RT S2 S2 RT S2 S2 S2 RT
S2 S2 S2 S1 S1 RT RT HAT
RT S2 S1 S2 S2 S2 RT RT
S2 S1 RT RT S2 S2 S2 S2
RT S2 RT RT S2 RT RT S2
RT RT S2 S2 S2 S2 S2 S2
RT S2 HAT HAT RT S1 S2 RT
SAT S2 S2 S2 S2 RT S1 RT
S1 RT S1 S2 S2 S2 S1 S2
S2 S2 J-turn HAT S2 RT S2 S1
S2 RT RT S2 RT RT HAT S2
O-bend HAT S1 S2 S2 S2 S2 S2
S2 S2 S2 RT RT S2 RT HAT
S2 S1 S1 RT RT RT RT RT
RT HAT RT S2 RT RT HAT S1
S1 S1 RT S2 S2 RT S2 SAT
S2 S2 S1 S2 J-turn RT RT HAT
RT S2 S2 S2 HAT RT S2 S2
S2 S2 S2 HAT S1 RT HAT S1
S1 S2 AS HAT S1 S2 S1 RT
HAT RT S1 S1 RT S1 S2 S2
RT RT S2 S1 S2 S2 S1 J-turn
S2 S2 RT RT S1 S1 S2 RT
S2 S1 HAT S1 AS RT RT RT
S2 S2 HAT AS RT S2 RT S1
RT S2 RT S2 RT RT RT S1
S1 S1 S2 HAT S1 AS RT HAT

RT RT S2 S2 S2 S2 RT S2
RT HAT S2 RT S2 RT S2 S2
RT HAT S1 S1 S2 RT RT RT
HAT S1 HAT S2 S2 RT J-turn S2
S2 S2 RT S1 S2 S2 RT RT
HAT S1 S2 RT RT HAT HAT S1
S2 S2 S2 S2 S2 S2 S2 S2
RT S1 S1 S1 HAT HAT S2 HAT
S2 HAT S2 S2 S2 S2 S2 RT
HAT S1 S1 S2 S2 HAT S1 RT
SCS J-turn S2 HAT S1 S2 S2 S2
S2 RT S1 RT S1 AS J-turn RT
RT RT RT O-bend J-turn S1 RT
$\rightarrow$ RT
RT S2 S2 RT S2 RT O-bend S2
S2 S2 S2 S2 J-turn RT RT S2
S2 HAT S1 J-turn RT S2 S2 S2
S1 S2 S2 RT S2 S2 S2 RT
RT S1 S2 S2 S1 S2 HAT S1
RT S2 S2 S2 RT RT HAT S1
SAT HAT HAT S2 S2 HAT HAT $\rightarrow$ S1
S2 S2 S2 S2 S1 S2 S1 S1
S2 S1 S1 RT S2 S2 RT RT
S1 S2 HAT S1 O-bend RT S1 S2
RT RT RT S1 S1 HAT SAT S1
S2 S2 S2 S2 S2 S2 S2 S2
S2 S2 RT HAT S1 S2 S1 RT
S1 S2 S2 S2 S2 RT S2 RT
RT HAT S1 RT RT S2 HAT S1
RT RT RT J-turn AS S2 S1 RT
S2 RT RT S1 S1 S1 S2 RT
HAT RT RT HAT S1 S1 S1 RT
S2 S2 HAT RT RT S1 HAT RT
S2 RT S2 S2 S2 S2 S2 SAT
S2 S2 S2 S2 RT S2 S2 RT

S2 S2 RT S2 S2 RT HAT S1
J-turn S2 RT S2 HAT S1 S2 $\rightarrow$ J-turn
RT S1 RT S2 J-turn HAT RT S2
RT SAT S2 RT HAT HAT S2 S2
S2 HAT S1 S1 S2 S2 RT RT
S2 HAT S1 HAT J-turn S1 RT S2
S2 HAT S2 RT J-turn J-turn SCS $\rightarrow$ S2
J-turn J-turn S1 SAT S2 RT RT S2
S2 J-turn RT S2 RT S2 HAT HAT
S2 S2 S2 S2 SAT S1 S1 S2
S2 RT SAT S1 RT RT S1 S2
S1 S2 S1 S1 S1 S1 S1 S2
S1 RT S2 S2 RT RT S2 S2
S1 S2 S2 S2 S2 S2 S2 S2
S2 S2 RT S2 S2 RT RT RT
S1 RT RT S2 S2 HAT RT HAT
S1 S2 S2 S2 S2 S2 S2 S2
S2 S2 S2 RT RT S2 RT HAT
S1 RT S1 S2 RT S2 S1 RT
S2 S2 S2 S2 RT S2 S2 S2
RT RT S2 S2 HAT RT S1 HAT
SAT RT RT S2 S1 S1 S2 S2
S2 J-turn S1 HAT HAT S1 RT
$\rightarrow$ HAT
S2 RT S2 J-turn AS S1 S2 S1
S2 S2 S1 RT HAT S2 S2 S2
S2 HAT S1 S1 RT RT S2 RT
S1 RT J-turn HAT S1 S1 RT S2
S2 S2 S2 S2 S2 S2 S2 S1
S1 HAT HAT S2 S1 S1 S1 S1
HAT RT S1 RT S1 S1 S2 S2

### 7.5 Epic Kitchens

Each transcript in Epic Kitchens contains a sequence of behaviors consisting of an action and object. One example sequence is shown below.
open door
turn-on light
close door
open fridge
take celery
take container
take tofu
close fridge
open fridge
take carrot
open drawer
close fridge
put-down vegetable
open cupboard take board:cutting
put-down board:cutting
close cupboard
open drawer
take knife
take knife
put-down knife
close drawer
put-down knife
open tap
wash courgette
wash courgette
wash carrot
wash carrot
close tap
put-down vegetable
open cupboard
take grater
take pan
put-down pan
close cupboard
close cupboard
take courgette cut courgette turn-on hob cut courgette cut courgette dice courgette dice courgette dice courgette dice courgette pour courgette throw courgette open drawer close drawer take spatula stir courgette take salt open salt pour salt put-down salt stir courgette put-down spatula take celery wash celery
open tap
wash celery
close tap
put-down celery
cut celery
cut celery
pour celery
put-down board:cutting
take celery
throw celery
open fridge
put celery
close fridge
take spatula
stir spatula
put-down spatula
open container
take onion
take onion put-down onion
close container
take spatula
take knife
cut onion
cut onion
cut onion put-down knife take kettle
open tap
pour water
pour water
close tap
turn kettle
take spatula
stir vegetable
stir vegetable
take glass
take glass
open cupboard
put glass
close cupboard

