Effects of fine-scale population structure on the distribution of heterozygosity in a long-term study of *Antirrhinum majus*

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Abstract

Many studies have quantified the distribution of heterozygosity and relatedness in natural populations, but surprisingly few have examined the demographic processes driving these patterns. In this study we take a novel approach by studying how population structure affects both pairwise identity and the distribution of heterozygosity in a natural population of a self-incompatible plant *Antirrhinum majus*. We look at a measure of the variance in heterozygosity within a population, identity disequilibrium (g_2), together with F_{ST} using a panel of 91 SNPs in 22,353 individuals collected over 11 years. We find that pairwise relatedness (F_{ST}) declines rapidly over short spatial scales, and the excess variance in heterozygosity between individuals (g_2) reflects significant variation in inbreeding. Additionally, we detect an excess of individuals with around half the average heterozygosity, indicating that some are due to selfing or matings between close relatives. We use two types of simulation to ask whether variation in heterozygosity is consistent with fine-scale spatial population structure. First, by simulating offspring using parents drawn from a range of spatial scales, we show that the known pollen dispersal kernel explains g_2. Second, we simulate a 1000-generation pedigree using the known dispersal and spatial distribution and find that the resulting g_2 is consistent with that observed from the field data. In contrast, a simulated population with uniform density underestimates g_2, indicating that heterogeneous density promotes identity disequilibrium. Our study shows that heterogeneous density and leptokurtic dispersal can together explain the distribution of heterozygosity. Furthermore, our study highlights the limitations of making theoretical predictions from simulations that only assume simple density and dispersal distributions.

Keywords

heterozygosity, identity disequilibrium, population structure, isolation by distance

Introduction

Spatial genetic structure is common in natural populations. For many organisms, gene dispersal and therefore relatedness are spatially structured, such that individuals closer in space are more likely to mate, and be more closely related, than individuals further apart [1], [2]. Such spatial population structure should reduce population mean heterozygosity relative to a well-mixed population, generating decreasing genetic similarity over geographic distance – known as isolation-by-distance [3]. Despite the ubiquity of these patterns in nature, the importance of demography and gene dispersal in determining both the spatial pattern and level of genetic variation has not been thoroughly explored. Furthermore, commonly used

models of spatial structure – namely the island model, stepping stone model and models of
continuous population structure – either assume demes or a uniform population density.
However, natural populations are typically patchy, with heterogeneity in both the distribution
and density of individuals. Patchy and heterogeneous spatial distributions within natural
populations should result in spatial variation in inbreeding and, consequently, excess variance
in heterozygosity. Despite this prediction, spatial variation in heterozygosity has rarely been
examined in the population structure literature. Moreover, it is the interplay of heterogeneous
density and dispersal that likely shapes the spatial structuring of genetic relatedness between
individuals. This highlights the importance of understanding the factors (e.g., life history,
demography, population structure) that contribute to shaping the full distribution of
heterozygosity and relatedness in a spatially structured population.
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Understanding the drivers of variation in inbreeding within populations is fundamental given
its importance to genetic diversity and fitness. Quantifying variation in inbreeding and
combining this with measures of fitness (or fitness proxies) makes it possible, in principle, to
estimate inbreeding depression either through pedigrees [4], [5] or Heterozygosity-Fitness
Correlations (HFCs). For HFCs, inbreeding depression is estimated by comparing proxy
measures of fitness against heterozygosity, with the expectation that offspring from related
individuals will have lower heterozygosity. Variance in inbreeding is therefore essential for
HFCs to be detected [6]. In addition, variance in inbreeding is interesting *per se* because it
depends on both demographic history (e.g., [7]) and mating system (selfing, partial selfing or
outcrossing) [8]. For mating system, selfers vs. outcrossers can show contrasting levels of
inbreeding, with different consequences for genetic diversity, depending on population
history. Outcrossing species, with generally low levels of inbreeding, provide an opportunity
to examine factors other than mating system variation that may affect inbreeding variation,
and thus, variance in heterozygosity.
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If there is variation in inbreeding between individuals, heterozygosity at different loci will be
correlated. The covariance between loci in heterozygous state is termed identity
disequilibrium (ID), by analogy with linkage disequilibrium, the covariance in allelic state
between loci. ID can be calculated across individuals and divided by the square of the mean
of heterozygosity to calculate the population statistic g_2, which is a measure of variance in
identity by descent [6]. For an outcrossing organism with fine-scale population structure,
spatial patterns of density and mating could have strong effects on the degree of mating with
related individuals, and thus affect identity disequilibrium and g_2. Furthermore, as sessile
organisms, mating and offspring dispersal in plants are mediated by external vectors
(pollinators and seed dispersal mechanisms) [9]. Consequently, the shape of the distribution
of dispersal of both pollen and seed will also have an impact on g_2. If the sources of variation
in inbreeding are better understood, we may be able to combine g_2 with other statistics of
population structure to improve inferences about demographic history [10], [11]. Thus, g_2 can
be utilized to learn about the effects of population structure on the distribution of
heterozygosity and pairwise identity.
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For over a decade, we have sampled a population of the self-incompatible plant *Antirrhinum*
majus, the long-term aim being to build a pedigree which will allow us to estimate fitness and
dispersal directly. Through that project, we have collected an exceptionally large sample of
marker genotypes, which enables a powerful test of whether the observed density and
dispersal in this population can account for both the decay of pairwise relatedness with
distance, and for the distribution of heterozygosity across individuals. First, we verify that
there is excess variance in heterozygosity, which reflects an underlying variance in

inbreeding. Second, to understand the role of spatial patterns of dispersal in generating
variance in heterozygosity, we compare the empirical distribution of heterozygosity with that
of offspring from simulated matings where parents were drawn from different dispersal
scales. Third, we ask whether heterogeneous population density promotes variation in
inbreeding, by comparing simulated pedigrees conditioned on uniform density versus on the
observed locations of plants. Taken together, addressing these questions provides insight into
the underlying drivers of spatial structure and provides novel ways to study the effects of
mating patterns and demography in nature.
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Throughout this paper, it will be important to distinguish between identity by descent (IBD)
and identity in state. We denote the probability that two genes are identical by descent by F;
this is defined relative to an ancestral reference population, and can in principle be calculated
from the pedigree that descends from that population, independent of the actual allelic state.
What we observe are SNP genotypes; the two homologous genes in a diploid individual will
be identical in state if the genes are identical by descent, or if the ancestral genes carried the
same allele. Thus, probabilities of identity by descent (F) can be estimated from observed
identities in state. We denote the heterozygosity at locus i in a particular individual by h_i, with
$h_i=0$ if the genes are identical in state, and $h_i=1$ otherwise. The mean heterozygosity of an
individual is the average of h_i over n loci, denoted $H = \frac{1}{n}\sum_{i=1}^{n} h_i$.
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Methods

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120   <u>Study system</u>
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Antirrhinum majus is a self-incompatible, hermaphroditic, short-lived perennial herb native to
the Iberian Peninsula. It has a seed bank with most individuals' parents recorded 3-4 years
before they are sampled (D. Field, unpublished data). It grows in a variety of microhabitats
with relatively bare soil or frequent disturbance, including rail embankments, rocky cliffs,
and regularly mowed roadsides. Our study includes two "subspecies" that differ only in
flower color: *A. majus pseudomajus* has magenta flowers and occurs in northern Spain and
south-western France, including the Pyrenees. *A. majus striatum* has yellow flowers and a
smaller range, encircled by *A. m. pseudomajus*. The subspecies are parapatric; narrow clines
with intermediate color hybrids form wherever they meet, and there is no evidence for post-
zygotic reproductive barriers [12]. We focus on such a hybrid zone in the Vall de Ribès,
Spain [13], where we have collected demographic data annually since 2009. Across nearly all
of the genome, there is little divergence within our study area between plants with different
flower color, except for limited regions associated with floral pigmentation, which show
steep clines [14]. Thus, the study area can be considered as a single population for studying
neutral genetic variation.
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140 **Figure 1:** Distribution of *A. majus* in Vall de Ribès, Spain from the years 2009 to 2019, each
141 individual is shown as a white circle.

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143 <u>Field sampling</u>

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Genetic samples were obtained annually from 2009-2019 from every accessible flowering
individual in ~5 km stretches of two parallel roads that cross the Vall de Ribès, dubbed the
"lower road" (GIV-4016; ~1150 m elevation) and "upper road" (N-260; ~1350 m) (Fig. 1).
We also sampled along small side roads, railroad embankments, rivers, and hiking trails;
density was very low away from these disturbed areas. In some years, we were limited to
genotyping only in the core area, ~1 km along each road. The total genotyped sample
summed over the eleven years is 22,353 plants, ranging from ~750 plants in the smallest year
(2018), to ~5500 plants in the largest year (2014). Eighteen percent of individuals were
sampled in more than one year. Sampling was conducted during peak flowering (early June
to mid-July). Each year there were fewer than 100 visible but inaccessible plants;
consequently, we estimate that we found the majority of individuals in the sampled area.

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For each plant, we collected leaf samples for genotyping, and recorded spatial locations with
GeoXT handheld GPS units (Trimble, Sunnydale, CA, USA). These devices are accurate to
within 3.7 m, determined by comparing samples that had been inadvertently recorded twice
in the field (individuals with similar geographic location and near-identical genotypes,
allowing for SNP errors). Leaf samples were refrigerated upon return to the field station, and
dried in silica gel within three days.

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164 <u>SNP panel</u>

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Previously, a panel of 248 SNPs spread throughout the genome was designed for the focal
population (see methods in [15]). We follow these methods but include an additional five
years of data (2015-2019) and use a subset of 91 SNPs; the mean sample size per SNP was
21,212, or ~95% of the total. (see Supplemental Material 1.1 (SM1.1) for SNP filtering
methods). We imputed the ~5% missing genotypes for each SNP by randomly assigning
genotypes according to the population-wide allele frequencies at each marker.

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173 <u> Isolation by distance</u>

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The panel of 91 SNPs was used to calculate F_{ST} and isolation by distance, both of which
relate to the mean heterozygosity. F_{ST} is defined as the average identity by descent among

individuals within subpopulation, F_S, relative to the total population, F_T: $F_{ST} = \frac{F_S - F_T}{1 - F_T}$ [16].

These identities are estimated from SNP genotypes since we do not have the full pedigree.
Two genes will have a different allelic state only if they are not identical by descent, and if
they derive from different alleles in the ancestral population. Given overall allele frequencies
p+q=1, the expected heterozygosity ($\overline{H}$) of offspring from parents whose genes have a
probability of identity by descent F is $\overline{H} = (1 - F)\overline{2pq}$, where $\overline{2pq}$ is an average over loci.

Thus, there is a direct relation between F_{ST} and the mean heterozygosity: $F_{ST} = \frac{\overline{H_T} - \overline{H_S}}{\overline{H_T}}$. We

use this relation to compute F_{ST} for this dataset. (Note that here, H is the probability of non-
identity in state, which depends on the SNP genotype. The subscripts S and T refer to the
specified quantity within subpopulation and total population, respectively). A subpopulation
is defined as individuals within 20m.

Isolation-by-distance − the decay of genetic similarity with geographic distance − can be
observed by measuring pairwise relatedness between individuals. If individuals are separated
by a distance r, then pairwise relatedness can be calculated as an extension of F_{ST} (which we
refer to as pairwise F_{ST}) by setting F_S to be the probability of identity by descent and,
correspondingly, $\overline{H_S}$ to be the probability of non-identity in state between genes which are at
a distance r apart. This formulation is used to estimate F_{ST} between every pair of individuals
relative to the total population, as a function of their geographic separation. Pairs of
individuals are binned into distance classes of 20m each and the average F_{ST} and the distance
corresponding to each bin is calculated. This was done for every year from 2009 to 2019, and
the average calculated.

<u>Variation in inbreeding</u>

To describe the variation in heterozygosity in the *A. majus* population, we calculated
multilocus heterozygosity, denoted here by H, pooling across all years. This is defined as the

fraction of heterozygous loci in an individual: $H = \frac{1}{n}\sum_{i=1}^{n} h_i$, where $h_i = 0$ or 1, according to

whether locus *i* is heterozygous, and there are *n* genotyped loci. In this system "generations"
cannot be clearly defined because of seed dormancy and perenniality. However, pooling data
across years only reduced H by 0.08%.

We observed an excess of individuals with around half the mean heterozygosity (see Results).
To check whether the pattern was consistent with rare selfing, we compared the likelihood of
a single Gaussian to a mixture of two Gaussian distributions, one with the observed mean and
variance and the other with half its mean and variance.

The variance in individual heterozygosity consists of two components. The first is due to the
variance in whether an individual locus is heterozygous, and decreases in proportion to the
number of SNP, *n*: it equals $(1 - F)^2 \overline{2pq(1 - 2pq)}/n$. The second is due to covariance in
heterozygosity between loci, which is termed the identity disequilibrium (ID). For a given
pedigree, unlinked genes flow independently. Thus, heterozygosity is independent across
unlinked loci, and so this second component is proportional to the variance in inbreeding
across individuals, var (*F*). The first component can be estimated from the allele frequencies,
or simply by shuffling the data across loci, to eliminate ID. The excess variance is then
proportional to the variance in F across individuals, and is measured by the statistic g_2:

$$g_2 \,=\, \frac{\Sigma_{i \neq j}\ cov[h_i, h_j]}{E[h]^2} \,=\, \frac{var(F)}{(1 - E[F])^2}$$

(from Eq. 1 in [6]). Here, $cov[h_i, h_j]$ is the ID between loci i and j, and the sum over all
distinct i,j is the excess variance in H due to ID. Dividing by the square of the mean
heterozygosity $E[h]^2$ eliminates dependence on allele frequency, such that g_2 estimates the
variance in F across individuals.

To describe the variance of inbreeding across individuals, we first check if the variance in the
distribution of individual heterozygosity is significantly greater than the average variance
obtained from 100 replicates. This was done by reassigning heterozygous status randomly
across loci within individuals, which would eliminate correlations between loci generated by
ID. We then computed g_2 using the g2_snps function from the R package InbreedR (in R
version 3.6.1 [17]), which implements a modified formula for large data sets to estimate g_2,
and provides confidence intervals via bootstrapping to account for the finite number of
individuals sampled [18]. We decomposed ID into components due to linked and unlinked
SNPs by comparing correlations of H for all individuals to those with low H, at several
scales: across all pairs, within linkage groups, and between adjacent SNPs (SM1.2: Table
S1).

<u>Effects of pollen dispersal on heterozygosity</u>

With isolation by distance, the distribution of heterozygosity is expected to depend on the
distance between parents: heterozygosity of offspring from nearby parents will have a lower
mean and higher variance compared to offspring from distant parents. To test this prediction,
we simulated offspring using all field individuals as mothers and choosing fathers from a
given distance away (detail in SM1.3). Then, we compared the distribution of H between the
field data and offspring simulated from matings with three models of pollen dispersal: the
nearest neighbor to the mother, a Gaussian distribution ($\sigma = 300$ m), and a leptokurtic
dispersal kernel sampled from 1463 empirical measurements of pollen dispersal, estimated as
the distances between assigned parents (electronic supplementary material; D. Field,
unpublished data). The genotype of the offspring was assigned using Mendelian inheritance,
either without linkage between markers, or using the known linkage map (electronic
supplementary material; courtesy of Yongbiao Xue, Beijing Institute of Genomics). Including
linkage did not substantially change results, so we mainly show results for simulations
without linkage. We compared distributions, means, and variance of H using Kolmogorov-
Smirnov tests, t-tests, and F-tests, respectively. For the leptokurtic pollen dispersal
simulation, we checked for an excess of low-heterozygosity individuals generated by mating
between close relatives by asking whether a mixture of two Gaussian distributions is more
likely than a single Gaussian distribution.

<u>Heterozygosity in a simulated spatial pedigree</u>

In order to compare the actual distribution of heterozygosity with that expected for a spatially
structured population, we simulated a continuous two-dimensional population, conditioned
on the known locations of the individuals and the empirically measured seed and pollen
dispersal distances (electronic supplementary material; D. Field, unpublished data), using
Mathematica 12.0 [19]. Our simulation differs from commonly used models (e.g., island [16],
stepping stone [20] and continuous Wright-Malécot model [3], [21]) in that we include
heterogeneity in density by specifying actual locations to determine relationships in the

pedigree. We only provide a proof-of-principle, by asking whether a plausible model of
spatial structure can explain the observed heterozygosity. We do not include all features of
the actual population – in particular, we extrapolate by repeatedly sampling ten years of
spatial distributions; we ignore linkage; we simplify the self-incompatibility system; and we
assume an annual life cycle (no perenniality or seed bank). Thus, our simulation parameters
should be seen as "effective" values, analogous to the traditional Ne. Additionally, we also
validated our simulation against analytical results for a panmictic population and stepping
stone model (SM1.4: Fig. S5).
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First, however, we simulated a population with uniform density (the continuous Wright-
Malécot model) as a null model, to compare expected heterozygosity with and without
heterogeneous spatial structure. We simulate a region of ~1.1 x 1.8 km that was sampled
consistently in the *A. majus* focal population (SM1.4: Fig. S3). Locations were assigned by
randomly sampling N points from a uniform distribution each generation, for 1000
generations. Genetic diversity is shaped over the coalescent timescale ($2N_e$, ~170,000
generations in *A. majus* [14]), which is far longer than the 1000 generations that we simulate.
However, we are concerned here with the *local* population structure that determines the
variation in inbreeding amongst individuals within an area of a few km^2, which will
equilibrate rapidly. The spatial pedigree was generated by choosing parents for each
individual according to a backwards dispersal distribution measured empirically. The seed
and pollen dispersal distances are estimated respectively as the distance between offspring
and nearest parent (assumed to be the mother) and between parents (electronic supplementary
material; D. Field, unpublished data). For every offspring, the mother and father are chosen
from randomly drawn distances from the seed and pollen dispersal distributions. To choose a
parent from a distance r, 6 points are assigned randomly on a circle of radius r centred at the
focal individual and the nearest individual to each of them are found. The closest individual
to any of these points is then chosen as the parent. The accuracy of our algorithm is verified
by comparing the specified and realised seed and pollen dispersal distributions for the
simulated pedigrees (SM1.4: Fig. S6, Table S4). The same procedure is repeated for the
father, taking the mother as the starting point. Since *A. majus* is self-incompatible, the mother
and father are not allowed to be the same individual.
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305   Once the spatial pedigree is generated, 10 replicate sets of genotypes are assigned by
306   dropping genes down the pedigree, starting with equal expected frequencies of both alleles at
307   each of 91 loci. In fact, one could start with any initial frequencies, since F_{ST}-like measures
308   are independent of them. Population size was adjusted so that F_{ST} matched the empirical data
309   for the simulated sampling area.
310
Next, we simulated a population with realistic heterogeneous spatial structure by using the
individual locations available for the years 2009 to 2019 in the *A. majus* focal population
(SM1.4: Fig. S4). There were fewer individuals from 2017-2018, so these were merged,
giving distribution data for 10 time points. We randomly sample from the ten consecutive
time points, and repeat for 100 cycles, thus iterating for 1000 generations. We sub-sample
from these locations to maintain a constant population size (N). If N is greater than the
number of plants available in a given time point, say k, all k plants are first included and the
remaining N-k locations were re-sampled from the same time point, displaced at a random
angle on a circle of radius 3m to avoid having plants in the same location. This naïve
approach allows us to simulate a spatial structure that is realistic over at least small scales.
We then generated a pedigree following the procedure used for the uniform population, again

adjusting population size to match the empirically observed F_{ST}. Ten replicate sets of
genotypes were run for each of five replicate pedigrees.
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Patterns of isolation by distance, heterozygote deficit (F_{IS}) and identity disequilibrium were
compared between the two simulation types and the field data (calculated from the simulated
sub-area of the field site). As the fitted population sizes were large (see Results), obtaining
direct estimates of identity by descent and thus F_{ST} from the pedigrees was not feasible.
Instead, F_{ST} was obtained for a pedigree as the average of replicate genotype sets generated
from that pedigree. F_{IS} was calculated from the observed and expected heterozygosity. Values
of g_2 were calculated for each replicate from each pedigree using InbreedR (in R version
3.6.1 [17]).
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Results

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<u>Isolation by distance</u>

The average pairwise F_{ST} was calculated each year for individuals separated by different
distance classes and then averaged across years. Pairwise relatedness (F_{ST}) between
individuals decreased rapidly with geographic distance, showing isolation by distance (Fig.
2A). If we consider individuals within geographic separation of 20m, the average F_{ST} over the
eleven years is 0.0244; however, this figure is an average over a quantity that depends
strongly on distance. The sharp decline in pairwise identity over short spatial scales
corresponds precisely to a rapid increase in H with distance between parents (SM1.3: Fig.
S1), since heterozygosity is determined by the probability of identity by descent between the
genes from each parent. Note that over large separations (>1Km), pairwise F_{ST} values are
necessarily negative, because distant individuals are less closely related than the average for
the whole population.

<u>Variation in inbreeding</u>

Excess variance in the distribution of individual heterozygosity (H) in the field data shows
that there is variance in inbreeding in the population (Fig. 2B). Furthermore, there is an
excess of individuals with around half the mean heterozygosity (i.e., with H~0.22, rather than
0.44; Fig. 2B, blue, lower left). These might be due to a low rate of selfing. Indeed, a mixture
between two Gaussian with means ~ 0.22 and 0.44, and variances in the same ratio, fits
significantly better than a single Gaussian (Fig. 2B, compare red and black to blue) with an
increased likelihood of 11.3. However, we shall see in the next section that this excess is also
consistent with matings between close relatives, without the need to invoke a breakdown in
self-incompatibility.
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To examine whether the observed distribution of heterozygosity is significantly different to a
null distribution, we compared the field data with heterozygous values shuffled across
individuals, which eliminates identity disequilibrium (ID) by removing correlations between
loci. We found greater variance in heterozygosity in the observed compared to the randomly
shuffled field data (Fig. 2B, gray). For both data sets, the mean heterozygosity (0.44602)
necessarily remains the same, but the observed variance in the field data (var(H) = 0.00336)
was significantly higher than the average variance in 100 shuffled replicates (mean var(H) =
0.00282, s.d. 0.000029). This excess variance between the observed and shuffled data implies
that the mean standardized ID is g_2 = 0.0029 (95% CI: 0.0026-0.0033), representing a
significant variance in inbreeding between individuals.

Figure 2. A: Pairwise relatedness (F_{ST}) between individuals decreases rapidly with geographic distance showing isolation- by- distance in the field data. **B:** Probit transform of the cumulative distribution function (CDF) of the distribution of individual heterozygosity (H). A Gaussian appears as a straight line on a probit scale, and the y-axis is the number of standard deviations of the standard normal distribution.

The overall ID, as measured by g_2, is due to correlations in heterozygosity between all pairs of loci, most of which are unlinked. We expect stronger correlations between linked loci, because relatives will share blocks of genome. We found that the mean covariance in heterozygosity between SNP on the same linkage group is substantially stronger than the overall mean (0.00265 vs. 0.00056). If we restrict attention to those individuals with H<0.3, we find that the covariance in heterozygosity between SNP on the same linkage group is still higher (0.00649), as expected if close relatives share long blocks of genome IBD (SM1.2: Table S1).

Effects of pollen dispersal on heterozygosity

The heterozygosity of simulated offspring depends on distance between their parents, with a rapid increase in mean H with distance (SM1.3: Fig. S1). We compared the observed distribution of heterozygosity with three alternative scenarios for pollen dispersal. There was no significant difference between the mean and variance of heterozygosity between the field data and offspring simulated from the observed leptokurtic dispersal (electronic supplementary material). However, the mean and variance of heterozygosity differed between the field data and simulated matings with either nearest neighbors, or with Gaussian dispersal (Fig. 3A, SM1.3: Tables S2-S3). On the other hand, compared to the field data, all three dispersal schemes differed in the distribution tail as assessed by Kolmogorov-Smirnov tests (SM1.3: Table S3). These comparisons were made for a single replicate, but because each involves 22,353 individuals, there was little variation in the mean and variance between replicates.

We next examined deviations in the left tail of the distribution, where an excess of low heterozygosity individuals might arise from selfing or from matings between close relatives. We focused on the leptokurtic dispersal curve, which was the distribution closest to the field data. We estimated the increase in likelihood between fitting a single versus mixed Gaussian distribution (see "Variation in inbreeding") for 100 replicate simulations. We found that the mixed Gaussian was a better fit than a single Gaussian, with an increase in log likelihood greater than 2 for 69 of 100 replicates. The estimated fraction of putatively "selfed"

individuals was 0.00043, averaged over replicates, which is about half the estimate from the
actual data, 0.00086. In comparison, only 4/100 replicates gave higher estimates than that
observed (SM1.3: Fig. S2). This suggests that the excess of individuals with low
heterozygosity can to a large extent be explained by matings between relatives under
leptokurtic pollen dispersal. Nevertheless, there is a marginally significant excess of such
individuals, with twice as many being seen as expected from our simulations. There is
considerable variation in fit between replicates, simply because deviations in the tail involve
few individuals

The coefficient g_2 reflects excess variation due to identity disequilibrium, and showed similar
patterns as the variance in H. Here, we found no significant difference between g_2 from field
data and offspring from simulated matings with leptokurtic pollen dispersal. However, g_2
from Gaussian and neighbor matings were 80% higher than g_2 from field data and leptokurtic
matings. This nominally represents a significant difference given that the 95% confidence
intervals between these groups do not overlap (Fig. 3B). However, as we discuss below, these
confidence intervals only include sampling error, and not the additional variance due to
random evolutionary realizations.
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Figure 3. A: Probit transform of the CDF of multilocus heterozygosity, H, for the field data
(blue) versus a single replicate of offspring simulated from Gaussian pollen dispersal
(orange), nearest neighbor matings (gray), and leptokurtic pollen dispersal (green). A normal
distribution (black) with the same mean and standard deviation as the field data is included
for comparison **B:** Identity disequilibrium for the same data as above indicating mean and
95% CI.
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433 <u>Heterozygosity in a simulated spatial pedigree</u>
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In the previous section, we simulated offspring across one generation. To examine if the
observed heterozygosity is consistent with a spatially structured model, we simulated a
pedigree over 1000 generations, conditioned on the locations of individuals observed over ten
years, repeated over 100 cycles. The realized seed and pollen dispersal matched the empirical
seed and pollen dispersal distribution for both density types (SM1.4: Fig. S6, Table S4). We
required N = 15500 individuals for the heterogeneous density model and 40000 individuals
for the uniform density, in order to match the observed $F_{ST} \sim 0.022$ calculated over a 20m
scale from the simulated sub-area of the field site (SM1.4: Table S5). Up to distances of 1km,
the decline in pairwise identity with distance matched between the field data and the five
replicate pedigrees simulated with heterogeneous density (Fig. 4A, SM1.4: Fig. S7A). High
variation among replicates suggests that many more SNPs would be needed to match the
pattern from the pedigree (SM1.4: Fig. S7B); moreover, linkage would increase this variance

to some extent. We also compared the pattern of isolation by distance from the field data to
that from the pedigrees generated for both the heterogeneous and uniform density scenarios
(Fig 4B, SM1.4: Fig. S8); the heterogeneous density is a much better fit than the uniform
density (SM1.4: Table S5).
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452
453 **Figure 4. A:**. Isolation by distance compared between the field data (blue) and five replicate
454 simulated pedigrees (gray) based on a heterogeneous population density. **B:** Isolation by
455 distance from the field data (blue) compared between the simulated pedigree with a
456 heterogeneous (gray) and uniform (orange) population density.
457
Identity disequilibrium (g_2) estimates from the genotypes from pedigrees simulated with
heterogeneous density showed substantial variation between the five simulated pedigrees, and
between the ten draws of 91 SNPs from each pedigree (Fig. 5). The average g_2 estimated
from the five pedigrees (each with 10 replicates) is 0.00264, which is consistent with the
observed mean annual g_2 from the field of 0.00262. On the other hand, when assuming a
uniform density, the average g_2 of 0.00171 is significantly lower than the field data. Note that
the confidence limits for the field data, generated by InbreedR, only include error due to
sampling a limited number of individuals. These errors do not account for sampling a limited
number of SNPs, or the random variation between evolutionary realizations (see Discussion).

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Figure 5. Identity disequilibrium (g_2) calculated from field data versus simulated pedigrees.
Five of ten replicates per pedigree are shown (gray: heterogeneous density, with five
simulated pedigrees; orange: uniform density, with one simulated pedigree). Mean from the
field (light blue) is across 2009-2019, while mean from the heterogeneous (black) and
uniform (yellow) simulations is across all replicates. The final year of field data (dark blue) is
comparable to g_2 calculated from the final year of pedigree replicates (gray and orange).
474
475 **Discussion**
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An enduring problem in evolutionary biology is understanding how demographic processes,
such as heterogeneous density and dispersal, interact with spatial structure to determine the
distribution of heterozygosity within populations. In this study of a long-term dataset,
including more than 20,000 plants sampled over 11 years, we combine field data and
simulations to address questions central to understanding how demography can influence
patterns of heterozygosity. Namely, can we predict the distribution of heterozygosity for an
outcrossing species from key demographic parameters? To address this question, we first
confirmed that there was significant correlation in heterozygosity between markers (g_2, a
measure of identity disequilibrium), which implies variation in inbreeding. By simulating
offspring from matings between geo-referenced, genotyped individuals, we show that the
mean heterozygosity increases, and the variance of heterozygosity decreases, with increasing
distance between parents; strikingly, these changes occur over very short scales (~10m,
SM1.3: Fig. S1). We found that the observed distribution of heterozygosity is consistent with
the known leptokurtic distribution of pollen dispersal. We also simulate the population over
1000 generations using the actual seed and pollen dispersal kernels, and the observed
heterogeneous density. We found that this model matches the observed identity
disequilibrium, whereas a null model with uniform density substantially underestimates the
observed patterns. Moreover, our results also highlight the limitations of making theoretical
predictions from simulations that only assume simple demographies. Taken together, our
findings highlight the potential for using the observed demography to explain the distribution
of diversity, and specifically the variance in inbreeding in spatially continuous populations.
498
Variation in heterozygosity within populations provides the potential for selection to reduce
the frequency of less fit, inbred individuals. The association between inbreeding and fitness is
often tested through Heterozygosity-Fitness Correlations (HFC), which quantify inbreeding
depression in natural populations by correlating measures of fitness with heterozygosity [6].
Many studies that test for HFCs find that the excess variation in heterozygosity, g_2, which
arises from identity disequilibrium, is low and rarely significant [22]. In our study, we
estimate a significant g_2 of 0.0029 (95% CI: 0.0026-0.0033). Although low, this estimate is of
the same order as most of the g_2 values found across 105 vertebrate populations in a meta-
analysis of 50 HFC studies (average of 0.007) [22], and on the same order as ~60% of the
local populations surveyed in a long-lived tree [23]. Our estimate of significant variation in
heterozygosity provides the opportunity to examine potential drivers of this variance and
examine how density, spatial structure and dispersal contribute to a non-uniform distribution
of heterozygosity.
512
In our study, beyond simply estimating identity disequilibrium, we use two types of
simulation to explore how demography shapes variation in inbreeding. The first simulation
shows how the spatial pattern of pollen dispersal affects the distribution of heterozygosity.
Simulated matings with the empirically measured leptokurtic pollen dispersal curve were
consistent with the actual g_2, compared to matings with nearest neighbors or a Gaussian
pollen dispersal. This result is somewhat surprising because we did not include the
complexities of the mating system of *A. majus*. *Antirrhinum majus* has a gametophytic self-
incompatibility system (GSI [24]), whereby the pollen detoxifies secretions from the style
unless the pollen and style genotypes share alleles at the S-locus [25]. This system not only
prevents selfing, but also reduces mating among relatives (i.e., biparental inbreeding) because
related plants are more likely to share S-alleles [4], [26]. Thus, we might expect that our
simulated matings would have lower mean heterozygosity than the empirical measurement;
yet we found no evidence for such an effect. Indeed, we found that the excess of individuals
with low heterozygosity, around half the mean, can be explained largely by a small amount of

bi-parental inbreeding with leptokurtic pollen dispersal (Fig. 3, SM1.3: Fig. S2). However,
we have little statistical power to distinguish this from rare selfing, which can occur in self-
incompatible species.
530
Our second simulation approach asked whether heterogeneous density promotes variation in
inbreeding, given strong fine-scale population structure indicated by a rapid decay in pairwise
F_{ST} (over a few metres, Fig. 2A). Indeed, simulated pedigrees with uniformly distributed
plants gave less identity disequilibrium than we observed. In contrast, simulated pedigrees
conditioned on the actual, heterogeneous density of plants were consistent with identity
disequilibrium measured in the field. This indicates that patchiness, combined with
leptokurtic dispersal shapes the distribution of heterozygosity. Simulations with
heterogeneous density also better capture empirical isolation-by-distance patterns than those
with a uniform density (Fig 4B, SM1.4: Fig. S8). However, the effective population size of
15,500 individuals in the heterogeneous-density simulations is an order of magnitude larger
than the average number of plants observed in a year (~2500). We believe that most plants
are sampled each year, so that this discrepancy is more likely to be due to a seed bank, which
is expected to substantially increase the effective population size [27]. Nevertheless, despite
simplifications such as non-overlapping generations, no seed bank, and a simple SI system,
the heterogeneous-density simulation accurately captures patterns of identity disequilibrium
and isolation-by-distance.
547
Our estimation of identity disequilibrium illustrates a general problem with statistical
comparisons in evolutionary biology. There are three sources of error in estimating g_2: firstly,
error generated from sampling a limited number of individuals, secondly, from sampling a
limited number of SNPs, and thirdly from random variation between evolutionary realizations
or trajectories. In our study, the first source (a limited number of individuals) is shown by the
confidence intervals in Fig. 5, obtained by bootstrapping across individuals [18]. The second
source of error (a limited number of SNPs) is shown by the substantial variation in g_2 of the
ten replicates of each of five pedigrees. Here, variation is generated by random meiosis
amongst unlinked markers on a fixed pedigree. This variation could be reduced by increasing
the number of SNPs, but the effective number of segregating sites that can be included in the
analysis is fundamentally limited by the length of the genetic map. Finally, there is additional
variation between pedigrees, due to the random assignment of parents in the simulations,
which generates a random pedigree. The wide variation in estimates of g_2 due to random
meiosis, and to the random generation of the pedigree (Fig. 5) is an important reminder that
estimates of parameters are typically limited by the randomness of evolution. The
stochasticity of evolution can potentially generate error variance far higher than that due to
the limited number of individuals or SNPs sampled.
565
In addition to analyzing the effect of population structure on the distribution of
heterozygosity, our study highlights the potential of utilizing multiple statistics to estimate
population structure. We have shown that the variance of heterozygosity due to identity
disequilibrium can distinguish alternative dispersal and density distributions, which implies
that in combination with pairwise F_{ST} as a function of distance, g_2 can help estimate the
demography. Genetic data contain far more information than is described by F_{ST} and g_2; for
example, the mean squared disequilibrium can be used to estimate effective population size
[28], [29], and this extends naturally to the covariance of pairwise linkage disequilibrium as a
function of distance. We could simply use a set of such statistics to inform demographic
inference via ABC [30]. However, our preference would be to first develop a theoretical

understanding of how realistic demographies influence statistical measures of spatial covariance in allele frequency, identity disequilibria, and linkage disequilibria.

The distribution of heterozygosity has often been measured to estimate inbreeding depression and examine correlation with fitness. Yet, this type of data has rarely been used to investigate population structure *per se* and as a complement to the more widely used pairwise identity, F_{ST}. By bringing together local inbreeding and isolation-by-distance, our study provides a novel assessment of how dispersal and population density can explain both pairwise identity and the distribution of heterozygosity in spatially continuous populations. However, we have only begun to investigate how the distribution of heterozygosity can be shaped by population structure and demographic parameters. Our future work will focus on understanding how other features such as a seed bank influence genetic diversity, with the ultimate goal of deriving information about demographic history from the distribution of heterozygosity in populations that have fewer measured parameters. New models that include these complexities, as well as ecological, mating system and life history factors are required to extend our understanding of the drivers of population structure in natural populations.

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