Effects of fine-scale population structure on inbreeding in a long-term study of snapdragons (*Antirrhinum majus*)

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Abstract
The distribution of heterozygosity in a population is commonly used to quantify
inbreeding depression through the use of heterozygosity-fitness correlations (HFCs), but
the demographic processes shaping variability in inbreeding are not well understood. For
11 years, we measured heterozygosity and six fitness proxies in a population of the self-
incompatible plant *Antirrhinum majus*. Using a panel of 91 SNPs in 22,353 individuals,
we find that relatedness declines rapidly over short spatial scales. Excess variance in
heterozygosity between individuals (identity disequilibrium, g_2) reflects significant
variation in inbreeding. We use two types of simulation to ask whether variation in
heterozygosity is consistent with fine-scale spatial patterns of mating and population
structure. First, we simulate offspring from matings with fathers at different distances,
showing that the pollen dispersal kernel affects expected g_2. Second, we simulate a 1000-
generation pedigree using the known dispersal and spatial distribution and find that g_2 is
consistent with that observed. In contrast, a simulated population with uniform density
underestimates g_2, indicating that heterogeneous density promotes identity
disequilibrium. Finally, we estimate inbreeding depression through HFCs. Only
flowering stem count increases with heterozygosity. Our study shows that heterogeneous
density and leptokurtic dispersal can together explain pairwise F_{ST} and the distribution of
heterozygosity.

Keywords
inbreeding depression, heterozygosity, identity disequilibrium, population structure,
isolation by distance

Introduction

Inbreeding depression is one of the most universal and long-standing observations in
biology: fitness is reduced in offspring of matings between relatives, leading to the
evolution of extraordinary mechanisms for the avoidance of inbreeding [1]. The
avoidance of self-fertilization through outcrossing would be a sufficient mechanism to
avoid inbreeding in a large, randomly mating population. But for many organisms, both

gene dispersal and relatedness are spatially structured, such that individuals closer in space are more likely to mate and more likely to be closely related than individuals further apart. Such spatial population structure should reduce population *mean* heterozygosity, relative to a well-mixed population. Furthermore, real populations are typically patchy rather than uniformly distributed, which should cause spatial variation in inbreeding and hence excess *variance* in heterozygosity. Such variation in heterozygosity has often been used to estimate inbreeding and its fitness effects through heterozygosity-fitness correlations (HFCs) [2, 3]. However, we lack an understanding of what factors (e.g., life history, demography, population structure) are important for shaping the distribution of heterozygosity in a population.

Variation in inbreeding makes it possible, in principle, to estimate inbreeding depression from contemporary samples, without requiring pedigrees. In early studies using allozyme markers, patterns of positive correlations between heterozygosity and fitness proxies were interpreted as being directly due to the allozyme alleles themselves, and therefore, as evidence for superiority of heterozygotes at single loci (overdominance) [4]. However, when such heterozygosity-fitness correlations were also observed with DNA-based markers, it became clear that they reflect an association with inbreeding depression: individuals more heterozygous at marker loci tend to be more heterozygous for the recessive deleterious alleles that are responsible for inbreeding depression [2]. Overdominance is now thought to make a relatively small contribution to inbreeding depression [5].

Given the ubiquity of inbreeding depression due to recessive deleterious alleles, HFCs should be widespread and easily detected in nature, yet meta-analyses have not consistently found significant HFCs (e.g., [3]). A possible explanation is that the study populations lack sufficient variation in inbreeding: if all individuals are equally inbred, then there is no correlation between heterozygosity at unlinked loci, and HFC can only be due to the small fraction of inbreeding depression that is linked to the markers [2]. Miller and Coltman [3] calculated identity disequilibrium (a measure of covariance in heterozygosity between loci) for 50 HFC studies and found that it was rarely significant, indicating that HFC studies usually do not detect sufficient variation in inbreeding. However, their analysis included only studies of vertebrates. Plants, with their sessile nature and often limited dispersal [6], may be likely to show high identity disequilibrium if relatedness declines rapidly with distance and density is heterogeneous, promoting variation in the frequency of biparental inbreeding.

In addition to its importance for detecting HFCs, variation in inbreeding *per se* is interesting because it depends on demographic history. Yet potential sources of variation in identity disequilibrium have not, to our knowledge, been explored. Mating system can influence variation in inbreeding [7]. Outcrossing species, with generally low levels of inbreeding, provide an opportunity to examine other factors that may affect identity disequilibrium. Here, for an outcrossing organism with fine-scale population structure, spatial patterns of density and mating could have strong effects on the degree of mating with related individuals, and thus affect identity disequilibrium. If the sources of variation in inbreeding are better understood, we may be able to combine identity disequilibrium

90 with other statistics of population structure to improve inferences about demographic
91 history [8, 9].
92
Here, we use a detailed long-term study of a plant population to bring together measures
of isolation by distance with variance in inbreeding and to ask whether distributions of
heterozygosity can be explained by spatial population structure. For over a decade, we
have sampled fitness-related traits and SNPs in a population of the self-incompatible
plant *Antirrhinum majus*. Our population-wide sampling permits a powerful test of
whether the observed density and dispersal in this population can account for both the
decay of pairwise relatedness with distance, and for the distribution of heterozygosity
across individuals. First, we verify that there is excess variation in heterozygosity, which
reflects an underlying variance in inbreeding. Second, to understand the role of spatial
patterns of dispersal in generating variation in heterozygosity, we compare the empirical
distribution of heterozygosity with that of offspring from simulated matings with nearby
individuals at different dispersal scales. Third, we ask whether heterogeneous population
density promotes variation in inbreeding, by comparing simulated pedigrees conditioned
on uniform density versus observed locations of plants. Finally, we ask whether fitness
proxies are correlated with heterozygosity, to set limits to the strength of inbreeding
depression. Taken together, addressing these questions provides insight into how mating
patterns and demography contribute to inbreeding and fitness outcomes in natural
populations.
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Methods

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114 <u>Study System and Field Sampling</u>
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Antirrhinum majus is a self-incompatible, hermaphroditic, short-lived perennial herb
native to the Iberian Peninsula. It has a seed bank; most individuals' parents are from 3-4
years before they are sampled (D. Field, unpublished data). It grows in a variety of
microhabitats with relatively bare soil or frequent disturbance, including rail
embankments, rocky cliffs, and regularly mowed roadsides. Our study includes two
"subspecies" defined by flower colour: *A. majus pseudomajus* has magenta flowers and
occurs in northern Spain and south-western France, including the Pyrenees. *Antirrhinum*
majus striatum has yellow flowers and a smaller range, encircled by *A. m. pseudomajus*.
The subspecies are parapatric; narrow hybrid zones form wherever they meet, and there is
no evidence for post-zygotic reproductive barriers [10]. We focus on such a hybrid zone
in the Vall de Ribès, Spain [11], where we have collected demographic data annually
since 2009. Across nearly all of the genome, there is little divergence between the
subspecies in this population, except for limited regions involved in floral pigmentation
[12].
130
Genetic samples and trait measurements were obtained annually from 2009-2019 from
every flowering individual that we could access in ~5 km stretches of two parallel roads
that cross the Vall de Ribès, dubbed the "lower road" (GIV-4016; ~1150 m elevation)
and "upper road" (N-260; ~1350 m). We also sampled along small side roads, railroad
embankments, rivers, and hiking trails; density was very low away from these disturbed

areas. Some years we were limited to genotyping only in the core area, ~1 km along each
road. The total genotyped sample summed over all years is 22,353 plants, ranging from
~750 plants in the smallest year (2018), to ~5500 plants in the largest year (2014).
Eighteen percent of individuals were sampled in more than one year. Each year there
were fewer than 100 visible but inaccessible plants, so we estimate that we sample the
majority of individuals in the study area. Sampling was conducted during peak flowering
(early June to mid-July). Areas adjacent to the roads are mowed multiple times in the
flowering and fruiting season by the municipality.
144
For each plant, we collected leaf samples for genotyping, recorded locations, and
measured several traits (described under Heterozygosity-Fitness Correlations). Leaf
samples were refrigerated upon return to the field station, and dried in silica gel within
three days. Locations were recorded with GeoXT handheld GPS units (Trimble,
Sunnydale, CA, USA) and are accurate to within 3.7 m, determined by comparing
samples that had been inadvertently recorded twice in the field (individuals with similar
geographic location and near-identical genotypes, accounting for SNP errors).
152
153 SNP panel and isolation by distance
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Previously, a panel of 248 SNPs spread throughout the genome was designed for the
focal population (see methods in [13]). We follow these methods but include an
additional five years of data (2015-2019) and a subset of 91 SNPs; the mean sample size
per SNP was 21,212, or ~95% of the total. (See Supplemental Material 1.1 (SM1.1) for
SNP filtering methods). We imputed the ~5% missing genotypes for each SNP by
randomly assigning genotypes according to the population-wide allele frequencies at each
marker. The average F_{ST} over all years is 0.0244 (definition and calculation are detailed
in SM1.1). The average pairwise F_{ST} is calculated each year for individuals separated by
different distance classes and is averaged across years (details in SM1.1). Isolation by
distance is shown by plotting pairwise F_{ST} against pairwise geographic distance (SM1.1:
Fig. S1).
166
167 Variation in inbreeding
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To describe the variation in heterozygosity in the *A. majus* population, we calculated
multilocus heterozygosity, denoted here by H, pooling across all years. (Because of seed
dormancy and perenniality, we cannot clearly define "generations." We do not expect
pooling to have much effect.) This is defined as the fraction of heterozygous loci in an
individual: $H = \frac{1}{n}\sum_{i=1}^{n} h_i$, where $h_i = 0$ or 1, according to whether locus i is
heterozygous, and there are n genotyped loci. Offspring from related individuals tend to
have lower heterozygosity.
176
177 We observed an excess of individuals with around half the mean heterozygosity (see
178 Results). To check whether the pattern was consistent with rare selfing, we compared the
179 likelihood of a single Gaussian to a mixture of two Gaussian distributions, one with the
180 observed mean and variance and the other with half its mean and variance.
181

The variance in individual heterozygosity consists of two components. The first is due to
the variance in whether or not an individual locus is heterozygous, and decreases in
proportion to the number of SNP, n: it equals $(1 - F)^2 \overline{2pq(1 - 2pq)}/n$. The second is due
to covariance in heterozygosity between loci, which is termed the identity disequilibrium
(ID). For a given pedigree, unlinked genes flow independently, thus heterozygosity is
independent across unlinked loci, and so this second component is proportional to the
variance in inbreeding across individuals. The first component can be estimated from the
allele frequencies, or simply by shuffling the data across loci, so as to eliminate ID. The
excess variance is then proportional to the variance in F across individuals, and is
measured by the statistic g_2:
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195　$$g_2 = \frac{\sum_{i \neq j} \text{cov}[h_i, h_j]}{E[H]^2} = \frac{\text{var}(F)}{(1 - E[F])^2}$$
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197
198　(from Eq. 1 in [2]). Here, $\text{cov}[h_i, h_j]$ is the ID between loci i and j, and the sum over all
199　distinct i,j is the excess variance in H due to ID. Dividing by the square of the mean
200　heterozygosity $E[H]^2$ eliminates dependence on allele frequency, such that g_2 estimates
201　the variance in F across individuals.
202
Significant ID is a fundamental condition for the existence of heterozygosity-fitness
correlations [2]. To describe the variance of inbreeding across individuals, we first check
if the variance in the distribution of individual heterozygosity is significantly greater than
the average variance obtained from 100 replicates by reassigning heterozygous status
randomly across loci within individuals, which would eliminate correlations between loci
generated by ID. We then computed g_2 using the g2_snps function from the R package
InbreedR (in R version 3.6.1 [14]), which implements a modified formula for large data
sets to estimate g_2, and provides confidence intervals via bootstrapping to account for the
finite number of individuals sampled [15]. We decomposed ID into components due to
linked and unlinked SNPs by comparing correlations of H for all individuals to those with
low H, at several scales: across all pairs, within linkage groups, and between adjacent
SNPs (SM1.2: Table S1).
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216　<u>Effects of pollen dispersal on heterozygosity</u>
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With isolation by distance, the distribution of heterozygosity is expected to depend on the
distance between parents: heterozygosity of offspring from nearby parents will have a
lower mean and higher variance compared to offspring from distant parents. To test this
prediction, we simulated offspring using all field individuals as mothers and choosing
fathers from a given distance away (more detail in SM1.3). Then, we compared the
distribution of H between the field data and offspring simulated from matings with three
models of pollen dispersal: the nearest neighbour to the mother, a Gaussian distribution
($\sigma = 300$ m), and a leptokurtic dispersal kernel sampled from 1463 empirical
measurements of pollen dispersal, estimated as the distances between assigned parents
(electronic supplementary material; D. Field, unpublished data). The genotype of the
offspring was assigned using Mendelian inheritance, either without linkage between

markers, or using the known linkage map (electronic supplementary material; courtesy of
Yongbiao Xue, Beijing Institute of Genomics). Including linkage did not substantially
change results, so we mainly show results for unlinked markers. We compared
distributions, means, and variance of H using Kolmogorov-Smirnov tests, t-tests, and F-
tests, respectively. For the leptokurtic pollen dispersal simulation, we checked for an
excess of low-heterozygosity individuals generated by mating between close relatives by
asking whether a mixture of two Gaussian distributions is more likely than a single
Gaussian distribution.
237
238 <u>Heterozygosity in a simulated spatial pedigree</u>
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In order to compare actual variation in heterozygosity with that expected for a spatially
structured population, we simulated a continuous two-dimensional population,
conditioned on the known locations of the individuals and the empirically measured seed
and pollen dispersal distances (D. Field, unpublished data), using Mathematica 12.0 [16].
Our simulation differs from commonly used models (e.g., island [17], stepping stone [18]
and continuous Wright-Malécot models [19, 20]) in that we include heterogeneity in
density by specifying actual locations to determine relationships in the pedigree. We only
provide a proof-of-principle, by asking whether a plausible model of spatial structure can
explain observed heterozygosity. We do not include all features of the actual population –
in particular, we repeatedly sample ten years of spatial distributions; we ignore linkage;
we simplify the self-incompatibility system; and we assume an annual life cycle (no
perenniality or seed bank). Thus, our simulation parameters should be seen as "effective"
values, analogous to the traditional N_e.
253
First, however, we simulated a population with uniform density (the continuous Wright-
Malécot model) as a null model, in order to compare expected heterozygosity with and
without heterogeneous spatial structure. We simulate a region of ~1.1 x 1.8 km that was
sampled consistently in the *A. majus* focal population (SM1.4: Fig. S4-S5). Locations
were assigned by randomly sampling N points from a uniform distribution each
generation, for 1000 generations. Genetic diversity is shaped over the coalescent
timescale ($2N_e$, ~170,000 generations in *A. majus* [12]), which is far longer than the 1000
generations that we simulate. However, we are concerned here with the *local* population
structure that determines the variation in inbreeding amongst individuals within an area
of a few km^2, which will equilibrate rapidly. The spatial pedigree was generated by
choosing parents for each individual according to a backwards dispersal distribution
measured empirically (see methods for choosing parents in SM1.4). Once the spatial
pedigree is generated, 10 replicate sets of genotypes are assigned by dropping genes
down the pedigree, starting with equal expected frequencies of both alleles at each of 91
loci. In fact, one could start with any initial frequencies, since F_{ST}-like measures are
independent of them. Population size was adjusted so that F_{ST} matched the empirical data
for the simulated sampling area.
271
Next, we simulated a population with realistic heterogeneous spatial structure by using
the individual locations available for the years 2009 to 2019 in the *A. majus* focal
population. There were fewer individuals from 2017-2018, so these were merged, giving

distribution data for 10 time points. We randomly sample from the ten consecutive time
points, and repeat for 100 cycles, thus iterating for 1000 generations. We subsample from
these locations, so as to maintain a constant population size (N). If N is greater than the
number of plants available in a given time point, say k, all k plants are first included and
the remaining N-k locations were resampled from the same time point, displaced at a
random angle on a circle of radius 3m to avoid having plants in the same location. This
naïve approach allows us to simulate a spatial structure that is realistic over at least small
scales. We then generated a pedigree following the procedure used for the uniform
population, again adjusting population size to match the empirically observed F_{ST}. Ten
replicate sets of genotypes were run for each of five replicate pedigrees.
285
Patterns of isolation by distance, heterozygote deficit (F_{IS}) and identity disequilibrium
were compared between the two simulation types and the field data (calculated from the
simulated sub-area of the field site). As the fitted population sizes were large (see
Results), obtaining direct estimates of identity by descent and thus F_{ST} from the pedigrees
was not feasible. Instead, F_{ST} was obtained for a pedigree as the average of replicate
genotype sets generated from that pedigree. F_{IS} was calculated from the observed and
expected heterozygosity. Values of g_2 were calculated for each replicate from each
pedigree using InbreedR.
294
295 Heterozygosity-fitness correlations
296
We recorded traits related to size and reproduction from every individual in select years,
and assessed their utility as fitness proxies by correlating against more complete
measures of fecundity measured on a subset. The traits measured on all individuals were:
(i) number of flowering stems (2009-2019), (ii) number of open flowers (2010-2019),
(iii) height of the tallest stem (cm; 2014-2019), and (iv) number of leaf nodes on the
tallest stem (2014-2019). Depending on accessibility, areas were visited 1-3 times each
year. Thus, trait measurements are a snapshot taken at a random point during the
flowering season. To address the potential added noise from this constraint, we included
measurement date as a covariate in the HFC analyses. For perennial plants, which have
trait measurements in multiple years (18% of individuals), the year with the highest
measured value for each trait was included in the pooled year analyses.
308
We assessed whether traits measured on every individual can be used as fitness proxies
by asking whether they are related to direct measures of fecundity. In 2014-2017, 1047
individuals in un-mowed areas were sampled at the end of the season. The total number
of fruit and flowers borne throughout the season can be inferred from inflorescence nodes
and remains of dehisced fruits. We call the snapshot flower counts performed on all
individuals "estimated flowers" to distinguish them from the "total flower" counts
performed for this subset. We asked whether fitness proxies (flowering stems, estimated
flowers, total flowers, height, leaf nodes) correlate with female fecundity as assessed by
total fruit counts, using Spearman's ρ.
318
To test whether fitness was correlated with heterozygosity, we used Generalized Linear
Models (GLMs) in R, using the MASS package for negative binomial models [21].

Response variables were fitness proxies: total fruit, total flowers, estimated fruits, number
of flowering stems, stem height, and leaf nodes. Because not all markers are typed across
individuals, the predictor was standardised multilocus heterozygosity (H^*), defined as the
proportion of heterozygous loci per individual, divided by the population mean
heterozygosity for those typed loci [22], calculated with InbreedR [15]. Each model also
contained fixed-effect covariates of year, road (upper vs. lower, designated by latitude),
and perennial status ("annual" for individuals collected only once; "perennial" if a
genotype or tag was collected in multiple years). Julian day of measurement was an
additional covariate for stem height, estimated flowers, leaf nodes, and flowering stems.
The family and link function for the GLM was assigned according to the distribution of
each trait: gamma with a log link for stem height, and negative binomial (to account for
overdispersion) for all other traits.
333
The residuals of the models indicate spatial autocorrelation (significantly positive
Moran's I), suggesting that the variances are likely underestimated. However, due to a
lack of significant regression coefficients (see Results), we did not correct model
variance for spatial autocorrelation in most models. For the significant result – number of
flowering stems – we accounted for spatial autocorrelation with a Generalised Linear
Mixed Model (GLMM) with an exponential spatial correlation structure nested within
road and year, using the MASS and nlme packages in R [21, 23, 24].
341
342 Correlations between heterozygosity and fitness are due to the product of the correlation
343 of inbreeding with both heterozygosity and fitness (Eq. 2 in [2]). Using this relationship,
344 the results of the HFC analysis can be used to calculate the inbreeding load, $\beta_{f,W}$, for each
345 trait [2]. Although most traits showed non-significant relationships, the potential
346 magnitude of inbreeding load was calculated for each trait (formulas in SM1.5).
347
Results

349
350 <u>Variation in inbreeding</u>
351
Variance in the distribution of individual heterozygosity (H) in the field data suggests
that there is variance in inbreeding in the population (Fig. 1). Furthermore, there is an
excess of individuals with around half the mean heterozygosity (i.e., with H~0.22, rather
than 0.44; Fig. 1, blue, lower left). These might be due to a low rate of selfing. Indeed, a
mixture between two Gaussian with means ~ 0.22 and 0.44, and variances in the same
ratio, fits significantly better than a single Gaussian (Fig. 1, compare red and black to
blue) with an increased likelihood of 11.3. However, we shall see in the next section that
this excess is also consistent with matings between close relatives, without the need to
invoke a breakdown in self-incompatibility.
361
The observed distribution of heterozygosity can be compared with the distribution when
heterozygous status is shuffled across loci by random reassignment within individuals
(Fig. 1, grey). Shuffling removes correlations between loci and thus eliminates identity
disequilibrium (ID). The mean heterozygosity (0.44602) necessarily remains the same,
but the observed variance (var(H) = 0.00336) is significantly higher than the average

variance in 100 shuffled replicates (mean var(H) = 0.00282, s.d. 0.000029). This excess
variance between the observed and shuffled data implies that the mean standardised ID is
$g_2 = 0.0029$ (95% CI: 0.0026-0.0033), representing a significant variance in inbreeding
between individuals.
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373
374
375 **Figure 1.** Probit transform of the cumulative distribution function (CDF) of the
376 distribution of individual heterozygosity (H). The y-axis is the number of standard
377 deviations of the standard normal distribution.
378
379 <u>Effects of pollen dispersal on heterozygosity</u>
380
Figure S2 shows that the heterozygosity of simulated offspring depends on distance
between parents (SM1.3). Next, we checked whether real offspring have a distribution of
heterozygosity consistent with three simulated pollen dispersal scenarios. The mean and
variance of heterozygosity do not significantly differ between the field data and simulated
offspring from leptokurtic dispersal, but do differ from simulated matings with nearest
neighbours and with Gaussian dispersal (Fig. 2A, SM1.3: Tables S2-S3). On the other
hand, all three dispersal schemes differ in the tail as assessed by Kolmogorov-Smirnov
tests (SM1.3: Table S3). These comparisons were made for a single replicate, but because
each involves 22,353 individuals, there is little variation in mean and variance between
replicates.
391
We next examined deviations in the left tail of the distribution, where an excess of low
heterozygosity individuals might arise from selfing or from matings between close
relatives. We focused on the leptokurtic dispersal, which gave a bulk distribution
consistent with the field data. We estimated the increase in likelihood between fitting a
single versus mixed Gaussian distribution (see "Variation in inbreeding") for 100
replicate simulations. The mixed Gaussian is a better fit than a single Gaussian, as we
find a significant increase in likelihood for 69 of 100 replicates. The estimated fraction of
putatively "selfed" individuals was 0.00043, averaged over replicates, which is about half
the estimate from the actual data, 0.00086. In comparison, only 4/100 replicates gave

higher estimates than that observed (SM1.3: Fig. S3). This suggests that the suspected
selfed offspring (see "Variation in inbreeding") in the field data, indicated by an excess
of individuals with low heterozygosity, can largely be explained by matings between
relatives under leptokurtic pollen dispersal, though there is a marginally significant
excess of such individuals. There is considerable variation in fit between replicates,
simply because deviations in the tail involve few individuals.

The coefficient g_2 reflects excess variation due to identity disequilibrium, and showed
similar patterns as the variance in H. Here, g_2 from field data and offspring from
simulated matings with leptokurtic pollen dispersal did not differ significantly, but g_2
from Gaussian and neighbour matings were 80% higher than g_2 from field data and
leptokurtic matings – nominally this represents a significant difference, as the 95%
confidence intervals do not overlap (Fig. 2B). However, as we discuss below, these
confidence intervals only include sampling error, and not the larger variance between
evolutionary realisations.

418
Figure 2. A: Probit transform of the CDF of multilocus heterozygosity, H, for the field
data (blue) versus a single replicate of offspring simulated from Gaussian pollen dispersal
(orange), nearest neighbor matings (grey), and leptokurtic pollen dispersal (green). A
normal distribution (black) with the same mean and standard deviation as the field data is
included for comparison **B:** Identity disequilibrium for the same data as above indicating
mean and 95% CI.

<u>Heterozygosity in a simulated spatial pedigree</u>

To examine if the observed g_2 is consistent with a spatially structured model, we
simulated a pedigree over 1000 generations, conditioned on the locations of individuals
observed over ten years, repeated over 100 cycles. The realized seed and pollen dispersal
matched the empirical seed and pollen dispersal distribution for both density types
(SM1.4: Fig. S6, Table S4). We required N = 15500 individuals for the heterogeneous
density model and 40000 individuals for the uniform density, in order to match the
observed F_{ST}~0.022 calculated from the simulated sub-area of the field site (SM1.4:
Table S5). Up to distances of 1km, the decline in pairwise identity with distance matched
between the field data and the five replicate pedigrees simulated with heterogeneous

density (SM1.4: Fig. S8A, B). High variation among genotypes suggests that many more
SNPs would be needed to match the pattern from the pedigree (SM1.4: Fig. S8C);
moreover, linkage would increase this variance to some extent. We also compared the
pattern of isolation by distance from the field data to that from the pedigrees generated
for both the heterogeneous and uniform density scenarios (SM1.4: Fig. S9); we found
that the heterogeneous density is a much better fit than the uniform density (Table S5).
443
Identity disequilibrium (g_2) estimates from the genotypes from simulated pedigrees with
heterogeneous density showed substantial variation between the five simulated pedigrees,
and between the ten draws of 91 SNPs from each pedigree (Fig. 3). The average g_2
estimated from the five pedigrees (each with 10 replicates) is 0.00264, which is
consistent with the observed mean annual g_2 from the field of 0.00262. On the other
hand, when assuming a uniform density, the average g_2 of 0.00171 is significantly lower
than the field data. Note that the confidence limits for the field data, generated by
InbreedR, only include error due to sampling a limited number of individuals. These
errors do not account for sampling a limited number of SNPs, or the random variation
between evolutionary realisations (see Discussion).
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Figure 3. Identity disequilibrium (g_2) calculated from field data versus simulated
pedigrees. Five of ten replicates per pedigree are shown (grey: heterogeneous density,
with five simulated pedigrees; orange: uniform density, with one simulated pedigree).
Mean from the field (light blue) is across 2009-2019, while mean from the heterogeneous
(black) and uniform (yellow) simulations is across all replicates. The final year of field
data (dark blue) is comparable to g_2 calculated from the final year of pedigree replicates
(grey and orange).
463
464   Heterozygosity-fitness correlations
465
466   All size- and fecundity-related traits (stem height, leaf nodes, estimated flowers, number
467   of flowering stems, and total flowers) were significantly positively correlated with total
468   fruits (Spearman's ρ; SM1.5: Fig. S10), justifying use of these traits as fitness proxies.
469   The highest correlation with total fruit was with the number of flowering stems (0.65),
470   which was even higher than with total flowers (0.41).
471
Even without considering spatial auto-correlation, the standardised heterozygosity H^* was
only a significant predictor for one of the six fitness proxies: plants with higher
heterozygosity had more flowering stems (Fig. 4, SM1.5: Table S6). This result was still
significant after accounting for spatial autocorrelation (data not shown), although it
should be noted that the model assumptions for normality of residuals was not met. In

contrast to heterozygosity, the covariates typically were highly significant predictors of
fitness proxies (Table S6; further discussed in SM1.5).
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480
481 **Figure 4.** Regression coefficients with 95% confidence intervals for H* as a predictor of
482 various fitness proxies. Note that coefficients show the percentage change in each trait as
483 H* increases, since the analysis used a log link function.
484
The regression coefficient of inbreeding on heterozygosity was $\beta_{f,H}$ = -0.173. The
maximum magnitude of the inbreeding load, $\beta_{f,W}$, for each trait is shown in SM1.5: Table
S7 – this represents the percentage change in each trait value with increasing inbreeding.
For the one trait with a significant HFC – number of flowering stems – individuals have
approximately 70% fewer flowering stems for each unit increase in inbreeding (mean $\beta_{f,W}$
= -0.70, upper CI = -0.20, lower CI = -1.20; s.d. of flowering stems = 3.47).
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492 **Discussion**
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The negative fitness consequences of inbreeding are well known; what is less well
understood is how demographic processes, such as heterogeneous density and the
dispersal distribution, influence the distribution of heterozygosity in a population. In this
study of over 20,000 plants sampled over 11 years in a natural population, we address
two questions central to understanding how demography can influence patterns of
heterozygosity and fitness in the field: (i) can the distribution of heterozygosity be
predicted for an outcrossing species using key demographic parameters?, and (ii) are
there negative effects of inbreeding on fitness proxies? We first confirmed that there is
significant correlation in heterozygosity between markers (g_2, a measure of identity
disequilibrium). This implies that there is variation in inbreeding, providing the
opportunity for inbreeding depression to cause heterozygosity-fitness correlations
(HFCs). By simulating offspring from matings between georeferenced, genotyped

individuals, we show that the mean heterozygosity increases, and the variance of
heterozygosity decreases, with the distance between parents; strikingly, these changes
occur over very short scales (~10m, SM1.3: Fig. S2). We found the observed
distribution of heterozygosity is consistent with the known leptokurtic distribution of
pollen dispersal. We also simulate the population over 1000 generations using the actual
seed and pollen dispersal kernels, and the observed heterogeneous density. We found that
this simple model matches the observed identity disequilibrium, whereas a null model
with uniform density underestimates it. Despite significant variation in inbreeding, only
one of six fitness proxies (number of flowering stems) increased significantly with
heterozygosity. This one significant value ($\beta_{f,W} = -0.70$) indicates quite strong inbreeding
depression, but we have low power to detect inbreeding depression in the other traits
(SM1.5: Table S7). Taken together, our findings highlight the potential for using
demographic parameters to explain variance in inbreeding in spatially continuous
populations.
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Many studies that test for HFCs find that the excess variation in heterozygosity, g_2, which
arises from identity disequilibrium, is low and rarely significant [3]. In our study, we
estimate a significant g_2 of 0.0029 (95% CI: 0.0026-0.0033). Although low, this estimate
is of the same order as most of the g_2 values found across 105 vertebrate populations in a
meta-analysis of 50 HFC studies (average of 0.007) [3], and on the same order as ~60%
of the local populations surveyed in a long-lived tree [25]. In our study, beyond simply
estimating identity disequilibrium, we use two types of simulation to explore potential
demographic factors shaping variation in inbreeding. The first simulation shows that the
spatial pattern of pollen dispersal affects the distribution of heterozygosity within a
population. Simulated matings with the empirically measured leptokurtic pollen dispersal
curve were consistent with the actual g_2, compared to matings with nearest neighbors or a
Gaussian pollen dispersal. This result is somewhat surprising because we did not include
the complexities of the mating system of *A. majus*. *Antirrhinum majus* has a
gametophytic self-incompatibility system (GSI [26]), whereby the pollen detoxifies
secretions from the style unless the pollen and style genotypes share alleles at the S-locus
(Fuji et al. 2016). This system not only prevents selfing, but also reduces mating among
relatives (i.e., biparental inbreeding) because related plants are more likely to share S-
alleles [27, 28]. Thus, we might expect that our simulated matings would have lower
mean heterozygosity than the empirical measurement; yet, we found no evidence for such
an effect. Indeed, we found that a small amount of biparental inbreeding with leptokurtic
pollen dispersal may explain an excess of individuals with low heterozygosity, around
half the mean (Fig. 2, SM1.3: Fig. S3), although we have low statistical power to
distinguish this from rare selfing.
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Our second simulation approach asked whether heterogeneous density promotes variation
in inbreeding, given strong fine-scale population structure (i.e., pairwise F_{ST} decays
rapidly over a few metres, SM1.1: Fig. S1). Indeed, simulated pedigrees with uniformly
distributed plants underestimated identity disequilibrium compared to the empirical
value. In contrast, simulated pedigrees conditioned on the actual, heterogeneous density
of plants were consistent with identity disequilibrium measured in the field, indicating
that patchiness combined with leptokurtic dispersal may contribute to observed patterns

of heterozygosity. Simulations with heterogeneous density also better capture empirical
isolation by distance patterns than those with a uniform density (SM1.4: Fig. S9).
However, the effective population size of 15500 individuals in the heterogeneous-density
simulations is an order of magnitude larger than the average number of plants observed in
a year (~2500). We estimate that the majority of plants in the population are sampled
each year, so the discrepancy is likely not due to significant under-sampling but rather to
a seed bank, which is expected to substantially increase the effective population size [30].
Despite simplifications such as non-overlapping generations, no seed bank, and a simple
SI system, the heterogeneous-density simulation accurately captures patterns of identity
disequilibrium and isolation by distance.
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Our estimation of identity disequilibrium illustrates a general problem with statistical
comparisons in evolutionary biology. There are three sources of error in estimating g_2:
firstly, from sampling a limited number of individuals, secondly, from sampling a limited
number of SNP, and thirdly from random variation between evolutionary realisations.
The first source (a limited number of individuals) is shown by the confidence intervals in
Fig. 3, obtained by bootstrapping across individuals [15]. The second source of error (a
limited number of SNPs) is shown by the substantial variation in g_2 of the ten replicates
of each of five pedigrees, with variation generated by random meiosis amongst unlinked
markers on a fixed pedigree. This variation could be reduced by increasing the number of
SNPs, but the effective number of segregating sites that can be included in the analysis is
fundamentally limited by the length of the genetic map. Finally, there is additional
variation between pedigrees, due to the random assignment of parents in the simulations,
which generates a random pedigree. The wide variation in estimates of g_2 due to random
meiosis, and to the random generation of the pedigree (Fig. 3) is an important reminder
that estimates of parameters are typically limited by the randomness of evolution, and can
be far higher than that due to the limited number of individuals or SNPs sampled.
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Inbreeding depression is expected to be strong, especially in self-incompatible (SI)
species such as *Antirrhinum majus* [31]; this prediction is borne out for many SI species
when inbreeding depression is measured through experimental crosses [7]. We found
strong inbreeding depression for the number of flowering stems, but HFCs were not
significant for the five other fitness proxies. Our g_2 value corresponds to a coefficient of
variation of non-identity (1-F) of only $\sqrt{0.0029}$ =0.054. Whilst this identity
disequilibrium is significant, it is still too low to allow detection of weak HFCs, despite
our exceptionally large sample size. Moreover, although the fitness proxies available in
our complete dataset are correlated with total fruit set measured on a subset of plants,
these relationships are noisy. Estimates of total lifetime fitness are not possible for such a
large sample, but future work will improve over using the largest measurement for
perennials by integrating fitness proxies across years and comparing to fitness estimates
from a pedigree. Environmental and stochastic effects on traits related to size and
fecundity (e.g., the strong covariate effects in SM1.5: Table S6) may swamp fitness
effects due to heterozygosity. A further potential explanation for the lack of HFCs is the
"invisible fraction," the many individuals that die before their fitness can be evaluated
[32]. We can only detect variation in heterozygosity and fitness among flowering
individuals, which are typically a very small portion of the total number of individuals

counted from seeds. For example, in the short-lived perennial *Olearia flocktoniae*, < 1% of viable seeds survive to germination and only 2.5% of those survive the earliest seedling stage [33]. In a previous study of paternity in *A. majus*, seeds were randomly collected from our field site, germinated in the greenhouse, and genotyped at 70 SNPs [34]. The heterozygosity of 1127 seedlings from 59 mothers shows the same distribution as the flowering adults sampled in our dataset (T. Ellis, unpublished data; data not shown), suggesting that our sampling method is not missing a significant fraction of seedlings with low heterozygosity that fail to reach flowering. However, our methods still would not detect early-acting inbreeding depression that would cause seed abortion or germination failure.

The distribution of heterozygosity has often been measured to estimate inbreeding depression via HFC. Yet, this type of data has been rarely used to investigate population structure in its own right, as a complement to the more widely used pairwise identity, F_{ST}. By bringing together local inbreeding and isolation-by-distance, our study provides a novel assessment of how dispersal and population density can explain both pairwise identity and the distribution of heterozygosity in spatially continuous populations. However, we have only begun to investigate how the distribution of heterozygosity can be shaped by population structure and demographic parameters. Our future work will focus on understanding how other features such as a seed bank influence genetic diversity, with the ultimate goal of deriving information about demographic history from the distribution of heterozygosity in populations that have fewer measured parameters.

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