Factors influencing the accuracy and precision in dating single gene trees

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Abstract

Molecular dating is the estimation of time from genetic sequences. Knowing the time of appearance of a taxon sets the evolutionary context by connecting it with past ecosystems and species. Genomes are made of thousands of genes which can be duplicated or horizontally transfered, thereby providing new material for adaptation. Knowing the time of appearance of genes would provide a context to understand adaptation at the genomic level. However, molecular clock inference faces uncertainty due to the variability of the rate of substitution between species, between genes and between sites within genes. While speciation dating can cope with this variability by concatenating multiple genes and using fossil calibrations, such solutions cannot be applied to date gene-specific events.

This study aims at benchmarking the accuracy of molecular dating applied to single gene trees, and identify how it is affected by gene tree characteristics. We analyze 5204 alignments of genes from 21 Primates in which no duplication or loss is observed, as well as simulated alignments based on characteristics from Primates. The relaxed log-normal clock dating was performed with the bayesian program Beast2.

From the empirical dataset, we find that the precision of dating decreases with shorter alignments, high rate heterogeneity between branches and low average rate, features that underlie the amount of dating information in alignments, hence statistical power. The best precision is associated with core biological functions such as ATP binding, cellular organization and anatomical development. We then investigated the accuracy of dating on simulated alignments, by controlling the three above parameters separately. It confirmed the factors of precision, but also revealed a systematic bias when branch rates are highly heterogeneous. This suggests that the relaxed log-normal clock model is not statistically consistent when calibrations are lacking and rate heterogeneity is high. Our study finally provides a general scale of parameters that influences the dating precision and accuracy, which can be generalized to other taxa. To tackle molecular dating events like gene duplications, future models should overcome the lack of power due to limited information from single genes.

Keywords: molecular clock, molecular dating, uncertainty, gene tree, primates, phylogenetics, phylogenomics

Introduction

The phylogenetic tree is the most prevalent concept for representing evolutionary relationships, but a species tree and a gene tree do not necessarily tell the same story: while nodes in a species tree represent speciations, meaning the divergence of sister species from their parent, in a gene tree they represent the divergence of genes which do not only result from speciation, but also gene duplication, horizontal gene transfer, hybridization, and deep coalescence. Therefore reconstructing a species tree generally requires sequences assumed to be strictly orthologous, without these extra events. However, although gene-specific events might hinder species tree inference, they are also a source of material for natural selection to act upon. In particular, gene duplications generate new loci that may acquire new functions (neofunctionalization, Ohno 1970) or share a set of functions between them (subfunctionalization, Force et al. 1999). Understanding the dynamics of gene duplications can therefore allow us to interpret how novel species form (Lynch and Force 2000) and adapt (Kondrashov 2012). To infer a duplication event, a tree must first be reconstructed based on a single gene, which is then "reconciled" with the tree of species, a procedure by which the duplication nodes are identified and associated with a taxon.

The Ensembl Compara database (Vilella et al. 2009) provides reconciled gene trees at the genomic scale, for a wide sample of species, and thus gives a broad picture of the distribution of gene duplications on the tree of taxa such as Metazoans. However its taxonomic sampling is quite sparse and unbalanced, causing some underrepresented clades to display long branches spanning tens of millions of years. Along these long branches the genetic distances are imprecisely estimated whereas unrepresented sister lineages could subdivide these branches if sampled. In particular, gene duplications on such branches are only assigned to a large time interval of tens of millions of years defined by the flanking nodes. With more precisely dated duplications, it would become possible to test temporal correlations, for example to study the relation between genomic evolution and morphological evolution, environmental conditions, coevolution between several species or species diversification [citation examples]. Such applications require duplication dates refined using molecular clock dating, a set of methods which link absolute time to the number of substitutions observed in sequences (Zuckerkandl and Pauling 1962; Margoliash 1963; Doolittle and Blombäck 1964; Zuckerkandl and Pauling 1965).

The molecular clock considers a DNA or protein sequence that evolves by substitution over a given laps of time t. It states an approximately proportional relationship between time t and the number of substitutions N, by modelling N as a Poisson distributed random variable of expectation $r \times t$, where r is the rate of substitutions per unit of time. Thus on average $r \times t$ substitutions occur in the duration t. In the simplest model the rate is assumed to be constant over the entire phylogenetic tree (Langley and Fitch 1974). The number of substitutions can be obtained from the branch lengths inferred with classic phylogenetic tree inference programs (PhyML, Iqtree, RaxML, Phylobayes, MrBayes, PAUP, etc), but to infer the rate, times must be known, and vice-versa. Fossils typically provide independent dating and are

used to assign ages to some of the speciation nodes, allowing the rate to be derived and all non-calibrated nodes to be dated.

However while rate constancy is a convenient simplification, it has been observed that rates of substitution per unit of time vary across taxa (Wu and Li 1985; Britten 1986; Pagel et al. 2006). The mechanisms at the origin of the variations are diverse and may include population size, impact of selection at the molecular level, generation time, efficiency of the DNA repair system, metabolism, etc. For some of these reasons, rates also vary across the genome (Wolfe et al. 1989). The heterogeneity of the rate across branches and across sites also occurs at the scale of a single sequence. This is called heterotachy (literally "different rates") (Philippe et al. 2003). Some authors (Kumar and Hedges 1998) have argued that by selecting many genes these variations are attenuated, their mean rate is approximately constant and the molecular clock can still be used, especially in recent clades. Elsewhere it is generally accepted that such simple models can generate overconfident but wrong results (Lozano-Fernandez et al. 2017).

Initially, tests of constancy such as the relative rate tests (e.g. in Sarich and Wilson 1966; Fitch and Langley 1976; Gu and Li 1992; Tajima 1993) were developed to assess these rate variations. Nowadays, most models accommodate a non constant molecular clock providing that enough calibrations are specified. How to relax the clock constancy is not settled: autocorrelated rates assume a progressive change between connected branches while uncorrelated clock rates just follow an overall distribution. The "uncorrelated Gamma" is commonly used to model how rates are obtained on each branch, but the "white noise" model further allows intra-branch independence (Lepage et al. 2007). Different empirical studies support either the uncorrelated rates model (Drummond et al. 2006; Rannala and Yang 2007; Linder et al. 2011; Heath et al. 2012) or the autocorrelated clock rates (Thorne et al. 1998; Lepage et al. 2007; dos Reis et al. 2018; Smith et al. 2018), while a mixture of the two models over different timescales has also been proposed (Lartillot et al. 2016; Bletsa et al. 2019). Algorithmic implementations include widely used software such as Beast 2 (Bouckaert et al. 2019) and MCMCTree (Rannala and Yang 2007) which exploit the Bayesian framework through Markov Chain Monte Carlo (MCMC) sampling, while some faster alternatives take advantage of least squares strategies, like LSD (To et al. 2016) and treedater (Volz and Frost 2017).

Our study targets single gene trees, in contrast to the common use of molecular dating to date species divergences using many loci whose sequences are concatenated. The concatenation approach aims to increase the amount of information, thus the accuracy (Bromham et al. 2000; Lanfear et al. 2010; Smith et al. 2018; Bletsa et al. 2019). Even in a favorable situation with many genes, the accuracy of molecular dating has been questioned, because of flawed procedures such as reusing inferred dates as secondary calibrations without propagating uncertainty (Graur and Martin 2004; Schenk 2016), but also because of inherent limitations of the problem (Pulquério and Nichols 2007; Burbrink and Pyron 2008; dos Reis and Yang 2013; Zhu et al. 2015; Kumar and Hedges 2016; Warnock et al. 2017); the most critical limitations are the difficulty of characterizing the type of clock relaxation and the uncertainty in calibration points themselves (dos Reis et al. 2015).

If accurate dating requires sufficient sequence information, this means that inferring dates
in virus, transposable element or single gene evolutionary histories is even more difficult than
with concatenations of hundreds of genes. Indeed, on such short sequences, low statistical
power amplifies the following known limitations of dating by molecular clock:
methodological errors in tree topologies and substitution rates, rate variation of multiple
biological origins and inherent stochasticity in the substitution process, all of which create a
disproportionate amount of noise.

Here we characterize the level of accuracy in dating nodes from single gene trees, and
what characteristics of the gene tree are related to a higher accuracy. We first evaluate a
dataset of primate genes under a cross-validation procedure where we date speciation events
in each tree and compare each individual tree estimate with the median age over all trees. In
these primate gene trees we find characteristics associated with a higher precision, mainly the
length of the sequence alignment, the heterogeneity of the rate between branches and the
mean rate of the tree. In addition to measuring precision, we also compare with reference
ages from TimeTree, and observe a bias towards younger ages. Because several explanations
for such bias cannot be disentangled from the empirical dataset, we simulated gene trees to
measure how the precision and accuracy of dating varies depending on alignment length, rate
heterogeneity between branches and mean rate of substitution. As figure 1 illustrates, the
ultimate goal is dating single gene events such as duplications (fig. 1b), but our study
assesses the accuracy of single gene dating by benchmarking single gene dates of speciations
(fig. 1c).

a) speciation node dating   b) gene tree node dating   c) crossvalidation of
                                                                speciation node dating

Figure 1: Analogies between dating problems. a) Dating a speciation lacking fossil data requires extrapolating from neighboring calibrated nodes; b) the problem of dating duplications is analogous, as they do not leave fossil traces, but are surrounded by speciation nodes linked to fossils; c) here, to benchmark the dates obtained from single genes, we only consider speciation nodes, but we leave out the available calibrations, and we compare the result with its reference age. The reference age is the median age across all gene trees for the empirical trees, while it is the true age in the simulated trees.

Results

Single gene estimates show a high dispersion and a bias towards younger ages

We perform a benchmark on dating speciation nodes from single gene trees with an empirical dataset of trees that include genes from 21 primate species obtained from Ensembl version 93. We focus on the Simiiformes clade as ingroup, which contains all Primates but the Lemuriformes that we use as outgroup. Speciation ages for all nodes have been estimated many times independently based on fossil-calibrated dating on concatenation of genes, and resulting consensus ages can be obtained from TimeTree (Kumar et al. 2017). Because our aim is to replicate the uncertainty in dating nodes that lack fossil calibrations, such as duplication nodes, we do not set any calibration except for the Simiiformes ancestor at 43.2 My (C.I [41.0, 45.7]). We then quantify the uncertainty relative to the surrounding interval of 43.2 My. We selected 5204 gene trees that do not display any duplication or loss in this tree of 21 primate species, so that each gene tree shares exactly the same topology. These were dated with Beast 2, providing 5204 age estimates at each internal node (fig. 2).

Figure 2: Distribution of speciation ages estimated on primate gene trees independently (5204 trees). Each histogram is rescaled to display the same height, but their total count is each equal to 5204. Dating was performed with Beast under the nucleotide substitution model HKY and a relaxed clock rate (see methods).

By comparison with the reference age estimates from TimeTree, we obtain clearly younger estimates on all nodes, sometimes even outside of the confidence interval from the reference (median, fig. 2). The highest shift of 10 My affects Cercopithecidae. This suggests that either our estimates are biased, or that the reference ages themselves are inaccurate. In our dating procedure, several simplifications may bias ages. To start with, calibrating only one node is insufficient, but this is precisely the purpose of our analysis, since we study gene trees for which nodes lack calibrations. With one calibration but variable branch rate, rate and time are unindentifiable because they are conflated into the branch length. Actually, our empirical dataset is expected to display heterogeneous branch rates of different origins. First there are species-specific rate variations, in which all genes experience the same trend in a specific lineage. For example the average branch length of Cercopithecidae is higher than their Hominoidea sister (supp. info. S1). This is consistent with the known generation times in these clades: based on (Pacifici et al. 2013) the averages are 4035 days for Cercopithecidae versus 6132 for Hominoidea. In addition to species trends, each gene tree may experience particular variations of branch rates, therefore producing dispersed ages when compared. Finally, heterotachy also likely occurs within genes, between sites. However, these gene and site heterotachies should just cause dispersion but not loss of accuracy, because we can expect that the average of gene ages should fall on the correct value (after correction for lineage specific rates). Another simplification of our inference is to consider instantaneous segregation of genes at speciations. In reality, speciation takes up to several million years and segregated genes can correspond to older allelic divergence. This phenomenon of deep coalescence should cause speciations to appear older than they are, and not younger as is the case in our results. Conversely, shallow coalescence caused by introgression between recently diverged species would produce younger age, but we deem implausible that introgression would be so pervasive among genes so as to strongly bias ages. In summary, variation in lineage specific rates is the most plausible explanation for our bias towards younger ages, unless the inference obtained from Beast is not statistically consistent.

Aside from comparisons with the reference ages, we quantified the dispersion of the estimates at each node with the following metrics: the mean absolute deviation from the median (MAD) of the node age and the 95% inter-quantile range (IQR95); the averages of these metrics over the 12 speciations yield 3 My and 16 My, respectively. These dispersions are larger for deeper nodes, such as Catarrhini with a MAD of 5.6 My and an IQR95 of 32.4 My. Divided by the Simiiformes calibration of 43.2 My, they represent 13 % and 75 % of this interval, respectively. In other words, the confidence interval for the age of Catarrhini is barely shorter than the age of Simiiformes.

In the following, we break down the causes leading to the dispersion of our estimates by measuring gene features and searching for a relationship with the dating precision.

The dispersion of age estimates is associated with low statistical signal and heterotachy

We computed 71 features from each gene tree related to alignment quality and substitution rate estimations (supp. info. S2). We regressed them against the absolute deviation from the median age averaged across all speciation nodes, a measure of the dating imprecision in a single gene tree. In order to select a restricted set of independent variables we used a Lasso regression with a regularization parameter 'alpha' of 0.02, which retained 9 parameters further fitted by Ordinary Least Squares (adjusted R^2 = 0.211, fig. 3). Variables were normalized so that coefficients can be compared.

Figure 3: Coefficients of regression of the gene tree features against the age dispersion. Features were selected with a Lasso regression with parameter alpha=0.02. Adjusted R^2 = 0.211. Error bars indicate the 95% confidence intervals.

By order of coefficient size, the length of the sequence alignment comes first (coefficient -0.38), associating short alignments with high dispersion. It is followed by the rate heterogeneity across branches which is positively associated with the dispersion (0.25). Next comes the mean rate of substitution (-0.10). We hypothesize two distinct causes for these correlations: first, the strength of the statistical signal is linked to the alignment length and to the mean rate, because both influence the number of observable substitutions, thus the amount of information available to infer ages. Second, some model parameters are not completely identifiable individually. As an example of conflated model parameter, the branch-specific rate (coefficient 0.25) cannot be estimated separately when there are no internal calibrations, meaning that it can take arbitrary values as long as the product of rate by time equals the branch length. Here the rate heterogeneity is the standard deviation of the rate across branches, as inferred by Beast. This indicates that while Beast manages to detect a high rate heterogeneity in a given gene tree, the ages it infers in such a tree is quite distinct from the median ages, and probably far from their true age.

Other coefficients have p-values below 0.05, and correspond to characteristics of the substitution process or the alignment, for which we provide the following interpretations. The shape of the site-wise gamma distribution of rates is a parameter in which a lower value means a more skewed gamma distribution. Thus, as indicated by the negative coefficient (fig. 3), rates that are heterogeneous site-wise (not only branch-wise) appear to also increase dating uncertainty. The kappa parameter, or ratio of transitions over transversions, is negatively correlated. It may relate to the degree of saturation: saturation brings this ratio closer to one, and it should increase dating uncertainty, although we think that very few gene trees show saturation in our Primates dataset. For the heterogeneity of the GC-content between sequences of the alignment, the correlation is positive. This could have two causes that are not mutually exclusive, one methodological, one biological: in the substitution model, sequence composition is assumed homogeneous. Only few phylogenetic models can actually model composition changes over the tree (Foster 2004) while this is known to highly impede phylogenetic inferences. Biologically, even if we fitted the appropriate model, genes subject to composition shifts are possibly evolving heterogeneously in other aspects, in particular with heterogeneous rates. For the average proportion of gaps of the alignment, we can similarly suppose that they render substitution rates harder to compute and that they are correlated with heterogeneously evolving genes. The last and smallest coefficient is an approximation of the branch rate heterogeneity that can easily be computed on any tree: the standard deviation of root-to-tip path lengths. It is, as expected, negatively correlated, but weakly. In (Smith et al. 2018) it is used as a criterion for selecting trees which are suitable for dating, but here we see that its predictive power is limited. For the GC-content, we measure a negative correlation, but have not identified clear explanations.

To situate these features in their real scale, we summarized them in the 10% of trees with highest or lowest predicted dispersion (table 1). Additionally, we searched for gene functions overrepresented in these two extreme subsets compared to the full set of 5204 genes, based on human Gene Ontology (GO) annotations (table 2, supp. info. S3). For the most dispersed trees, the function of "signaling receptor regulator activity" could reflect a type of gene which is shorter or evolves with heterogeneous rates; heterogeneous rates are likely to occur for genes that experience episodic positive selection. On the other hand, well dated trees (low dispersion) appear to have constrained functions, possibly under stronger negative selection, making rates slower and more constant. Negative selection on this set is further evidenced by 153 "Human Phenotype Ontology" overrepresented terms related to various developmental abnormalities (nose, nervous system, lower urinary tract, eye, see supp. info. S3).

Subset of gene families	Observed dispersion (My)	Alignment length (nucl)	Rate heterogeneity (10^{-7} subst/nucl/My)	Mean rate (10^{-3} subst/nucl/My)
10% highest predicted dispersion	2.80 ± 1.29	947 ± 451	10.71 ± 25.70	2.39 ± 1.33
10% lowest predicted dispersion	1.33 ± 0.56	5532 ± 3170	2.38 ± 5.07	2.82 ± 1.14

Table 1: Characteristics of gene families whose dispersion is predicted to be the lowest/highest (mean ± standard deviation)

	GO category	GO term IDs	GO term names
10% highest predicted dispersion	Molecular Function	GO:0030545	Signaling receptor regulator activity
10% lowest predicted dispersion	Molecular Function	GO:0005524	ATP binding
		GO:0005198	Structural molecule activity
	Biological Process	GO:0071840	Cellular component organization or biogenesis
		GO:0009653	Anatomical structure morphogenesis
		GO:0048731	System development
		GO:0051056	Regulation of small GTPase mediated signal transduction
	Cellular Compartment	GO:0005604	Basement membrane
		GO:0043228	Non-membrane-bounded organelle

Table 2: Overrepresented Gene Ontology terms in gene families with lowest/highest predicted dispersion, using g:Profiler with default parameters: significance threshold 0.05 and multiple testing correction g:SCS.

In this regression of gene tree characteristics, the explained variable (deviation from the median) is a measure of dispersion, not of accuracy. However we can only measure accuracy if we have access to the "true" age. Besides, the distribution of ages (fig. 2) suggests a bias in our estimates that empirical data alone is powerless to explain. We therefore performed a simulation to confirm the features that impact dating accuracy.

Simulating gene tree variability impact on dating

Simulations allow to measure two facets of the dating quality: first the precision or how fine-grained the estimates are; second and more importantly, the accuracy or how close the estimates are from the true value on average. We focused on the top 3 variables obtained from the regression: alignment length, heterotachy and mean rate of substitution. Our three variables of interest were set to representative values spanning their observed range in the real trees (supp. info. S4). For each set of parameters, we first simulated trees according to a relaxed clock model, then simulated codon sequence evolution along this tree. Dates were then reconstructed from simulated data with the same method as for the empirical dataset.

We expected the three variables to reproduce the same effect on dispersion as with the above empirical dataset. However we expected the accuracy to be unaffected because the model we use to simulate alignments and trees is very similar to the model used to reconstruct dates: Beast dating was thus performed without discrepancy between its inference model and the process that generated the data, and in this condition we expect it to be statistically consistent, i.e. converge to the true value as the amount of data increases.

We ran 1000 simulations for each parametrization, by fixing two parameters and varying the third, around a central point defined by length=3000 nucleotides, mean rate=0.004 substitutions/codon/My and branch rate heterogeneity = ¼ (defined as the standard deviation divided by the mean of the branch rates, abbreviated σ/μ).

The dispersion, as seen by the interquantile range covering 95% of the data (IQR95) (fig. 4) varies with each variable in the same direction as observed in the regression of primate gene trees: it increases for shorter alignments (4b), higher rate heterogeneity (4c) and lower evolutionary rate (4d). In almost all speciation nodes and parameter values, we recover an unbiased median age, falling accurately on the age from the underlying species tree. However, we find a shift towards younger ages for the highest rate heterogeneity between branches (3d, $\sigma/\mu = 1$). This shows that this parameter can be sufficient (if not necessary) to bias age estimates from a single gene tree.

Discussion

Why date divergences based on single gene trees?

Understanding and timing gene duplications could provide interpretations for morphological evolution, adaptation or species diversification. In this regard, our study evaluates molecular dating when applied to single gene trees. The restriction to single genes instead of concatenations makes it possible to study events of sequence evolution beyond the comparison of orthologs only, such as duplications (e.g. Aguileta et al. 2006; Vosseberg et al. 2021) or transfers of genes and dynamics of transposable elements (Boissinot et al. 2000; Ovchinnikov et al. 2002; Khan et al. 2006) or microRNAs (Sempere et al. 2006). While containing several genes, virus genomes are typically short as well but molecular dating is essential to model epidemiological dynamics (e.g. Drummond et al. 2006; To et al. 2016; Volz and Frost 2017; Bletsa et al. 2019). Our study leads to practical guidelines for accurate and precise phylogenetic molecular dating of single gene trees.

Factors of precision

From an empirical dataset of 5204 gene trees in 21 Primates, we identified characteristics related to the dispersion of age estimates. More statistical power, provided by higher rates or longer alignments, lowers the dating dispersion while an increase in rate variation between

Figure 4: Speciation dates on simulated alignments, under a relaxed clock model and a fixed species tree of Simiiformes, under various parameter values. Central dots represent the median date, and the interval represent the range [0.025, 0.975] of the distribution. a) Dated species tree from TimeTree; b) the number of sites in the alignments, in number of nucleotides; c) the diffusion parameter, defining the degree of relaxation of the clock rate, such that the ratio σ/μ (standard deviation of the rates over mean rate) equals one twentieth, one quarter, and one; d) The mean rate of substitution, in number of substitutions per site per million years. When not specified, length is 3000, rate is 40e-4 and σ/μ is ¼.

branches increases the dispersion. This confirms previous observations that the number of sites and substitutions is a limiting factor with regard to statistical power (Bromham et al. 2000; Lanfear et al. 2010; Smith et al. 2018; Bletsa et al. 2019; Bromham 2019), and also that the clock rate does not appear to be constant across branches. In our analysis the dispersion also correlates with characteristics of the substitution process (kappa, GC content), indicating either that the dating model is too simple, or that multiple kinds of heterogeneities (composition, rates) co-occur in some trees. The 5,204 selected gene trees only contain strict orthologs and as such represent a biased fraction of the 24,614 gene trees extracted from Simiiformes: this selection likely represents a more reliable subset for dating, because the absence of gene duplication and loss may be associated with a more stable evolution in terms of constancy of rate and selective pressure.

In the regression based on empirical gene trees, the adjusted R^2 is low (0.21), indicating a low fraction of explained variance. To investigate the missing variance, we should

incorporate additional biological characteristics of the sequences, but as we show in simulations, stochastic properties of the mutational and evolutionary processes already account for a large uncertainty. Furthermore in our empirical dataset, incomplete lineage sorting (ILS), introgression or reciprocal paralog loss may also obfuscate the relationship between molecular change and time, but we have not used models able to identify these processes. Among other simplifications we used, our dating method employs a nucleotide substitution model which cannot distinguish neutral from non-neutral substitutions, the neutral substitutions being usually thought as more clock-like. A codon model would be able to separate synonymous from non-synonymous substitutions and test this hypothesis, but being more complex (using 61 character frequencies instead of 4) it also requires more data, which as we have seen is the limiting factor at the scale of single gene trees.

Limiting the bias when dating single gene trees

In the empirical estimates, we observed a shift towards ages younger than the TimeTree reference. We suspect that species-specific rates could produce this pattern: in such circumstances the model with a relaxed clock requires calibrations on internal nodes to properly infer branch rates. Then we simulated sequences without species-specific rates and we were surprised to produce a similar bias, when the rate was highly variable across gene branches. This is surprising because we used the same model for inference as for generating the data, and thus were expecting statistical consistency. It thus appears that statistical consistency cannot be attained for situations where rates and times are not identifiable separately such as in the absence of calibrations, and when gene trees have independent rate variation, a phenomenon that we could call heterotachy between genes (as opposed to heterotachy occuring between different sites of the same gene). Some studies use the relative ordering of events from different taxa (Lutzoni et al. 2018) or from different gene families (Pittis and Gabaldón 2016; Vosseberg et al. 2021), but heterotachy between genes is a major hurdle to doing so and conditions for applicability need to be rigorously verified (Susko et al. 2021).

How to reduce uncertainty

Stochastic uncertainty is the amount of information that is lost assuming that the model is correct, as opposed to inductive uncertainty due to inadequate modelling (Holland 2013). Inadequate modelling generally produces systematic errors. Our simulations show what level of stochastic uncertainty to expect in gene trees with realistic rate characteristics, and they confirm the drivers of uncertainty identified in empirical gene trees. We highlight the requirement for a high number of sites and substitutions, which is critical for statistical power. This problem can probably only be circumvented by incorporating information beyond single genes, such as genomic context and linked model parameters between multiple gene trees, as recent developments suggest (Duchêne et al. 2020). Our study also reinforces the notion that fossil calibrations are quantitatively more important to accurate dating than sequence data alone. These solutions are unfortunately harder to design for gene trees with duplications or transfers. Some pragmatic approaches that have been proposed to handle

gene specific heterogeneity are the removal of loci with apparently non constant rate prior to the analysis (Jarvis et al. 2014), a "gene-shopping" approach (Smith et al. 2018), but discarding data might be unsatisfactory for genome scale analyses.

Regarding inductive uncertainty, richer models avoid overconfident but erroneous results. Also, when the inference of tree topology, substitutions and clock rates is performed jointly by an integrative method such as Beast, it guarantees that uncertainty is properly cumulated at all steps. However in our experience it appears challenging to run a complex parametric inference such as Beast at the scale of comparative genomics. Such integrative methods might not be numerically tractable because they generally require MCMC which implies prohibitive running times and in addition, MCMC requires a thorough and experimented human inspection to validate the inference output. In the face of this, numerous projects aiming at sequencing broad segments of biodiversity on Earth are emerging, under the auspices of the Earth Biogenome Project (EBP, Lewin et al. 2018; Lewin et al. 2022). Extremely large gene families, composed of tens of thousands of genes, will become common place. Therefore development of faster non-parametric algorithms is still relevant, alongside improvements in the computational footprint of probabilistic algorithms.

Research on the molecular clock enters an exciting time, with huge amounts of data and increasingly sophisticated methods to dissect the hidden mechanisms of sequence evolution. How the rate of molecular evolution varies still holds mysteries, both at the scale of lineagese and at the scale of genomes. Future developments answering this question will be methodologically challenging but shall shed light on important evolutionary processes.

Methods

Source and number of trees

The species tree and gene trees were obtained from Ensembl Compara 93 (July 2018; Zerbino et al. 2018) Metazoa dataset: 99 species descending from Opisthokonta (the last common ancestor of fungi and metazoan) and 23,904 reconciled gene trees. Low quality genomes, aberrant gene branch lengths, split genes were removed (supp. info. S5, Species and gene trees preprocessing).

Nodes from the species tree were assigned an age from TimeTree (data retrieved Jan. 2019; Kumar et al. 2017). The corresponding sequences of the coding domain of the longest transcribed isoforms (fasta format) were downloaded as fasta multiple sequence alignments via the Ensembl Perl API.

Focusing on the 21 primate species (18 Simiiformes and 3 Lemuriformes), we extracted 24,614 subtrees at their Simiiformes node plus two of the outgroup sequences with shortest branch lengths.

From those we selected the 5,235 gene trees without duplications and losses within Simiiformes, so that they share a single tree topology.

Alignment and cleaning

The protein sequences were aligned using FSA version 1.15.9 (Fast Statistical Alignment, Bradley et al. 2009) with default parameters, then back-translated to the corresponding nucleotide alignment.

HmmCleaner (version 0.180750, Di Franco et al. 2019) finds segments of sequence that appear inconsistent with the other aligned sequences, interpreting them as sequencing errors. We apply it and replace the detected segments by gaps. It was applied to the 5,235 amino-acid alignments that do not have duplications or losses. Out of these, 31 alignments caused HmmCleaner to fail, resulting in the 5,204 subtrees under study here.

Bayesian node dating with Beast 2

Using the alignments as input for Beast 2.6.3 (Bouckaert et al. 2019) we ran the following model: a HKY nucleotide substitution model with two site partitions corresponding to the codon positions {1,2} and 3. A Yule Birth-Death process models the branching pattern, and a relaxed uncorrelated lognormal clock rate is fitted on branches, with mean and standard deviation being estimated. All Simiiformes clades (see species tree in fig. 2) as well as Primates and Lemuriformes were constrained to be monophyletic. Only Primates and Simiiformes were calibrated precisely, the other having uninformative priors. The calibrations were specified as gamma distributions manually tuned to match TimeTree point estimate and 95% interval: location 70.8 My, α=4.6 and β = 0.656 for Primates, and location 40.9 My, α=4.6 and β = 0.656 for Simiiformes. The MCMC was run in one chain of 50,000,000 iterations in order for all ESS (effective sample size) to be above 200, and 5% of the chain was discarded as burn-in. The resulting mean dates were annotated on the species tree using TreeAnnotator from Beast 2.

Simulating alignments

500 replicates of alignments were generated by simulating the evolution of a sequence along the above tree of Primates, using INDELible v1.03 (Fletcher and Yang 2009). The three tested parameters were the mean rate, the rate heterogeneity across branches and the alignment length, with each set of parameter values being simulated 500 times. For the branch rates, we applied an independent log-normal relaxed clock simulation with the 'simclock' R package; the tested mean rates were 5×10^{-4}, 40×10^{-4} and 80×10^{-4} substitutions.site^{-1}.My^{-1}. To obtain the desired rate heterogeneities, we tuned the "diffusion" parameter s^2 so that the standard deviation of the branch rates is comparable with empirical estimates, as per the relation between standard deviation σ, mean μ and diffusion s^2 of a log-normal distribution:

$$s^2 = \log\left(1 + \frac{\sigma^2}{\mu^2}\right)$$

The chosen diffusion values of 0.6931, 0.0606 and 0.0025 correspond to a standard deviation of the branch rate equal to 1, 1/4 and 1/20 of the mean rate, respectively. These parameters were chosen to represent the extent of variation in the real data of 5,235 trees. For the alignment length, we set the root sequence lengths to 300, 3000 or 30,000 nucleotides in INDELible. The evolutionary model includes insertions and deletions, which were parametrized to occur at a rate of 8.4×10^{-7} and 16.8×10^{-7} My^{-1} respectively (corresponding to 1/14 and 2/14 of the median substitution rate 1.177 $codon^{-1}.My^{-1}$, a ratio taken from Fletcher and Yang 2009), with lengths following a Lavalette distribution with parameters (2, 300). The sequences evolve according to a codon model with *kappa* = 4 (transitions/transversions), *omega* = 0.175 (dN/dS), and codon frequencies taken from the concatenated alignments of Simiiformes genes. The random seed was set to 9342.

We then dated Primates speciations from these simulated sequences with Beast 2, as for the real Primates dataset above.

Global age dispersion from all primate trees

Given that all speciation nodes in the primate species tree are replicated in our set of 5204 gene trees, we measured the dispersion of estimated ages for each speciation. We used two metrics of dispersion, the MAD and the IQR95. The mean absolute deviation from the median (MAD) is a robust estimate of dispersion: it is less influenced by skewed distributions than when using the mean as center, and less influenced by outliers than the standard deviation. It is also still sensitive enough compared to median deviation from the median or interquartile range. The IQR95, or interquantile range covering 95% of the data (between percentiles 2.5 and 97.5) is more robust but less sensitive.

Regression

Statistical analyses on the output dates were performed with Python 3.8 and additional scientific computing packages including Numpy, Pandas, Statsmodels, Scikit-learn, Biopython and Ete3 (supp. info. S6).

Quantifying the average deviation of ages for a single gene tree

As the dependent variable to regress, we used the average deviation of ages in each gene tree: for one gene tree, the absolute deviation from the median speciation age is obtained at each node, then the deviations of the 12 nodes are averaged.

Collecting features of the gene families

We measured 71 characteristics of the gene families as explanatory variables in the regression. They include (full list in supp. info. S2) :

- Tree features:
    - mean bootstrap values of nodes, from Ensembl;
    - standard deviation of the root-to-tip lengths, from Ensembl branch lengths.

- alignment features:
    - global statistics such as alignment length and proportion of pairs of sequences that do not share sites;
    - statistics over sequences like the mean frequency of gaps, the mean percentage of ambiguous nucleotides, the mean GC-content, the mean CpG content;
    - statistics over sites, like the column entropy and the parsimony score;
    - proportions of sequences cleaned by HmmCleaner;

- substitution rate features:
    - proportion of synonymous substitutions at equilibrium, based on measured codon frequencies and the fitted substitution matrix with the program 'codeml' from PAML 4.9e (Yang 2007);
    - median and standard deviation of ω (dN/dS) from 'codeml' free-ratio model;
    - the ratio of transitions over transversions (kappa) estimated by Beast;
    - the tree length in number of substitutions by Beast;
    - the gamma shape for site variable rates by Beast;
    - the mean clock rate by Beast;
    - the standard deviation of the clock rate by Beast;

- other reported values from program executions:
    - log-likelihood, computation time and convergence warnings from 'codeml'.

Retrieving mean rate and rate heterogeneity per tree

Beast outputs different types of rates. First, it outputs the infered parameters of the uncorrelated log-normal clock model (its mean and standard deviation). Additionally, it computes a posteriori a rate for each branch and each site partition (codon positions {1,2} and {3} in our case). For each sampled tree, it then produces the mean and variance. We use the latter rate statistics as variables in the regression. Since there are as many values as sampled trees of the MCMC chain, we take the median over the chain as final value.

As we estimated separately the mean rates $m_{1,2}$ and m_3 for the corresponding codon positions, we finally combined them to obtain the rate of substitutions per codon:

$$m = 2 \times m_{1,2} + m_3$$

Similarly as measure of branch heterogeneity, we obtained the rate standard deviation s from the returned variances $v_{1,2}$ and v_3:

$$s = 2 \times \sqrt{v_{1,2}} + \sqrt{v_3}$$

Transforming regressed features

We chose the appropriate transformation of features in order to stay close to the assumptions of a linear modelling framework with ordinary least squares, that is explanatory variables with low skew. For this, a semi-automated procedure was set up, where a the transform that minimizes the skew was selected from the predefined set with 'no transform', 'logarithm base 10', and 'square root', with additional increment or sign modification if needed by the function domain of validity. Some variables were binary encoded in cases where a large proportion of values was constant, or where distributions were clearly bimodal. Transforms for each variable can be found in supp. info. S7.

Reducing multicollinearity

Multicollinearity being known to impede ordinary least squares fitting, we reduce it prior to the regression with two strategies:

• first we obtained covariances from a Factor Analysis (analogous to Principal Component Analysis, but accounting for discrete and ordinal data). From the results, we removed some features from clusters of heavily correlated features. We also "decorrelated" pairs of features by dividing one by the other or by computing the residues of the simple regression between the two linked variables. For instance we decorrelated standard deviation metrics when they correlate with the mean of the same variable (supp. info. S7).

• Afterwards we checked the multicollinearity condition number, which is the square root of the highest eigenvalue divided by the smallest eigenvalue of X^TX (X being the design matrix). Since the multicollinearity condition number was already less than the usual cutoff of 20, it was not needed to remove additional features.

Removing trees with outlier values

To avoid a misleading impact of outliers on the linear regression, trees with excessive rates computed by Beast were excluded. The cutoffs were chosen based on the histograms, which display very long tails. Additionally, alignments including pairs of sequences which do not share any common site, i.e. unaligned pairs, were also excluded, as this can lead to meaningless branch lengths. In total these filters removed 85 outlier gene trees (supp. info. S8).

Final feature selection with Lasso and OLS refitting

Lasso (Tibshirani 1996) is a regression fitting algorithm which simultaneously performs feature selection, thus dealing with highly dimensional design matrices. We therefore apply it in a first pass to discard coefficients with an absolute value inferior to 0.01, using a penalty value (alpha parameter) of 0.02. However Lasso coefficients are biased (by design), so that p-values and R^2 cannot be readily computed. For this reason we subsequently refit by ordinary least squares (OLS) using the selected features, with a covariance set to MacKinnon and

White's (1985) heteroscedasticity robust type 1. Statsmodels 0.13.2 implementations were used.

Gene functional annotation overrepresentation

From the 5204 gene trees without duplication or loss, human genes were used as the reference set of functions. Overrepresentation of the 511 human genes from the most dispersed and least dispersed trees was done with the online tool g:Profiler version e109_eg56_p17_1d3191d (Raudvere et al. 2019) using default parameters (significance threshold 0.05 and multiple testing correction by g:SCS).

As specified in the table 1, the set of most (or least) dispersed trees is obtained from the fitted regression line. It is therefore a predicted dispersion, distinct from the observed dispersion displayed in column 1.

Code and data availability

The Python statistical analysis, the source data and the intermediate data are archived at Zenodo.org with the DOI: 10.5281/zenodo.8235767). The core phylogenetics/bioinformatics library is also available at https://github.com/DyogenIBENS/Phylorgs (version 0.1.0).

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Conflict of interest disclosure

The authors declare that they comply with the PCI rule of having no financial conflicts of interest in relation to the content of the article.

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a) speciation node dating

calibrated
uncalibrated

b) gene tree node dating

speciation (calibrated)
duplication (uncalibrated)

c) crossvalidation of speciation node dating

Simiiformes ancestor

Simiiformes species

error

known age

?

calibrated
ignored calibration

a) Reference species tree

b) Simulated lengths

c) Simulated rate variability

d) Simulated mean rates μ