Neural interactions in developing rhythmogenic spinal networks: Insights from computational modeling

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Abstract

The mechanisms involved in generation of rhythmic locomotor activity in the mammalian spinal cord
remain poorly understood. These mechanisms supposedly rely on both intrinsic properties of
constituting neurons and interactions between them. A subset of Shox2 neurons was found to contribute
to generation of spinal locomotor activity, but the possible cellular basis for rhythmic bursting in these
neurons remains unknown. Ha and Dougherty (2018) recently revealed the presence of bidirectional
electrical coupling between Shox2 neurons in neonatal spinal cords, which can be critically involved
in neuronal synchronization and generation of populational bursting. Gap junctional connections found
between functionally-related Shox2 interneurons decrease with age, possibly being replaced by
increasing interactions through chemical synapses. Here, we developed a computational model of a
heterogeneous population of neurons sparsely connected by electrical or/and chemical synapses and
investigated the dependence of frequency of populational bursting on the type and strength of neuronal
interconnections. The model proposes a mechanistic explanation for emergence of a synchronized
rhythmic activity in the neuronal population and provides insights into the mechanisms of the
locomotor rhythm generation.

1   Introduction

The mammalian spinal cord contains neuronal circuits that can generate locomotor-like oscillations in the absence of supraspinal and afferent inputs. These circuits include rhythm-generating kernels capable of producing, maintaining and coordinating populational rhythmic activity. A rhythmogenic kernel on each side of the cord is thought to be comprised of mutually connected excitatory neurons with ipsilateral projections (Kjaerulff and Kiehn, 1996; Kiehn, 2006; Hägglund et al., 2010). Although no single genetically identified neuron type has been found to be solely responsible for rhythm generation in the spinal cord, the genetically identified Shox2 interneurons have been suggested to be involved in locomotor rhythmogenesis (Brownstone and Wilson, 2008; Dougherty et al., 2013). Later investigations provided evidence that a subpopulation of Shox2 neurons, specifically the Shox2 nonV2a neuron type, may belong to the rhythm-generating kernel in the neonatal rodent spinal cord and be involved in generation of locomotor rhythmic activity (Dougherty et al., 2013; Kiehn, 2016).

Although the existing data on the possible cellular basis for rhythmic bursting in the Shox2 neurons remains limited, there is evidence for the expression of several types of potentially rhythmogenic currents in these neurons, including the persistent inward current (Ha et al., 2019). Based on indirect data from multiple groups (Zhong et al., 2007; Tazerart et al., 2007, 2008; Ziskind-Conhaim et al., 2008; Brocard et al., 2010, 2013; Tong et al., 2012) and previous computational models (Rybak et al., 2006a,b; McCrea and Rybak, 2007; Sherwood et al., 2011; Zhong et al., 2012; Brocard et al., 2013; Rybak et al., 2013, 2015; Shevtsova et al., 2014; Danner et al., 2016, 2017, 2019; Shevtsova and Rybak, 2016; Ausborn et al., 2019), we have suggested that the generation of locomotor rhythmic activity in the spinal cord relies on the persistent sodium current (I_{NaP}).

Regardless of the intrinsic bursting properties of single neurons involved in rhythmogenesis, mutual interactions between the neurons are critical to allow synchronization of neuronal activity leading to the generation of populational rhythmic activity. A recent study has shown that functionally related Shox2 interneurons in neonatal mice are locally connected with each other bidirectionally via electrical synapses or gap junctions (Ha and Dougherty, 2018). This bidirectional electrical coupling may represent a mechanism for neuronal synchronization and for populational oscillations in the neonatal spinal cord. Bidirectional gap junctional coupling within each population of genetically identified neurons, i.e. Shox2 nonV2a neurons, is found with high incidence in the neonatal spinal cord. With age, this electrical coupling decreases in both incidence and strength, which may occur in parallel (and possibly in connection) with an increase of the unilateral connections via excitatory chemical synapses (Ha and Dougherty, 2018). This change in the type, probability and strength of neuronal interactions may lead to specific changes in some characteristics of locomotor rhythm and pattern generated and the range of generated frequencies.

To theoretically investigate the potential roles of different (electrical and excitatory chemical) connections between Shox2 interneurons and their interaction with the I_{NaP} in generation of rhythmic populational activity, we developed a model of a population of neurons incorporating I_{NaP} in a subset of cells that are sparsely connected by electrical and/or excitatory chemical synapses and investigated the dependence of frequency of populational bursting on the connection type and strength, the maximal conductance and distribution of I_{NaP}, and other neuronal characteristics. We demonstrated that the frequency of populational bursting activity depends on the relative expression of particular types of connections between neurons. The model proposes a mechanistic explanation for emergence of a synchronized rhythmic activity in a population of Shox2 neurons and provides insights into the mechanisms of the locomotor rhythm generation.

2   Results

The major focus of the present study was on the specific roles of, and possible cooperation between,
neural interactions (through gap junction coupling and/or excitatory chemical synapses) and persistent
(slowly inactivating) sodium current (I_{NaP}) in neuronal synchronization and generation of populational
rhythmic activity related to the locomotor-like oscillations in the mammalian spinal cord. We started
by simulating a pair of neurons operating in different regimes and connected by bidirectional gap
junctions or unidirectional excitatory chemical synapses in order to investigate the effect of the type
and strength of connections and the presence/absence of I_{NaP} conductance on the activity of both
neurons. Then, we considered a heterogeneous population of 100 neurons which incorporated a
subpopulation of neurons containing I_{NaP} and hence could intrinsically generate rhythmic bursting
depending on neuronal excitability. The remaining neurons were simple spiking neurons. The neurons
had parameters randomly distributed over the population and were sparsely connected by electrical and
excitatory chemical synapses. The probabilities of connections between neurons were set based on the
data from Shox2 neurons (Dougherty et al., 2013; Ha and Dougherty, 2018). Our modeling study
focused on neuronal interactions, synchronization of neuronal activity, and control of frequency of
populational bursting depending on the relative expression of different types of neuron connectivity and
connection strength.

2.1   Gap junctional coupling in two-cell model

We first simulated a pair of interneurons (In1 and In2) modelled in the Hodgkin-Huxley style and
coupled bidirectionally by gap junctions with conductance g_{Gap}. Each neuron represented either a
conditionally bursting neuron with I_{NaP} or a simple tonically spiking neuron without I_{NaP}. The equations
describing neuron dynamics and neuron parameters are specified in **Materials and Methods**.

The baseline operating regime of each neuron (prior to coupling) was dependent on its resting
membrane potential, which in turn was defined by the value of the leakage reversal potential, E_L (see
Table 1). With an increase in E_L, the isolated conditionally bursting neuron changed its operating
regime from silence to bursting and then to tonic spiking. The isolated "simple" neuron without I_{NaP}
could switch from silence to tonic spiking when E_L increased. The strength of gap junctional coupling
between the neurons (g_{Gap}) was varied. The time course of the neuron membrane potentials for various
baseline operating regimes and the strength of coupling is illustrated in **Figure 1**. The frequencies of
bursting, as well as neuron resting potentials at various values of g_{Gap} are shown in **Table 1**.

In our simulations shown in **Figures 1A1-A3**, both neurons (In1 and In2) incorporate I_{NaP}. In all three
panels, In1, if uncoupled, operates in a bursting mode, whereas In2 is silent (at low level of excitation,
panel A1), exhibits bursting (at intermediate level of excitation, panel A2), or is tonic spiking (at a
highest level of excitation, panel A3). The effect of gap junctional coupling depends on the difference
between the membrane potentials of coupled neurons and the strength of coupling, and hence can be
depolarizing for one neuron and hyperpolarizing for the other one. In all three cases, gap junctional
coupling leads to synchronization of neuronal bursting from the burst ratio M:1, M>1 at a lower g_{Gap}
($0.375 < g_{Gap} < 0.66$ nS) to the ratio of 1:1 at higher g_{Gap} ($g_{Gap} \geq 0.66$ nS) values. Note that coupling
may reduce bursting frequency relative to the uncoupled case (see panel **A1**) or increase it (panels **A2**
and **A3**, see also **Table 1**) depending on the relative values of the resting membrane potentials of
coupled neurons. This is seen in **Figure 1A1** when In1 depolarizes In2 and induces bursting in this
neuron with common bursting frequency at higher g_{Gap}. At the same time, In2 hyperpolarizes In1
resulting in a general decrease of common bursting frequency relative to the uncoupled case with
increased g_{Gap} (see **Table 1**). In **Figures 1A2,A3**, we see the opposite situation. In these cases, both

neurons operate in bursting regimes. However, the level of excitation of In1 is lower than that of In2,
and prior to coupling, In2 generates bursts with a higher frequency than In1 in **Figure 1A2** and is
tonically active in **Figure 1A3**. Electrical coupling of these neurons leads to depolarization of In1 and
hyperpolarization of In2. As a result, burst frequency of In1 increases while burst frequency of In2
decreases. In **Figure 1A3**, at lower g_{Gap} In2 switches from tonic to bursting mode, when coupled, with
the burst ratio 1:2. Similar to the simulation shown in **Figure 1A1**, at higher g_{Gap} the two-cell model
shows a synchronized bursting activity; however, the resulting frequency is higher than the initial In1
frequency (see **Table 1**). Hence gap junctional coupling between neurons with I_{NaP} leads to
synchronized rhythmic bursting with bursting frequency dependent on neuronal excitability and the
strength of coupling.

In simulations shown in **Figures 1B1-B3**, only one of the two electrically coupled neurons (In1)
has I_{NaP}. Prior the coupling, this neuron can be silent (panel **B1**) or operate in a bursting regime (panels
B2 and **B3**), whereas the other, "simple" neuron (In2), depending on the level of its excitation, can be
silent (panels **B1** and **B2**) or exhibit tonic spiking (panel **B3**). In all these simulations, the In2 neuron
has higher resting potential if uncoupled and depolarizes In1 if the two neurons are connected by gap
junctions (see **Table 1**). This results in the emergence of bursting activity (as in panel **B1**) or in an
increase of the bursting frequency with increasing g_{Gap} (panels **B2** and **B3**). In all three cases, In1
hyperpolarizes In2 during interburst intervals but induces high-frequency spiking in In2 during bursts,
resulting in synchronized activity of the two-cell model replicating bursting activity of In1.

The two neurons in **Figure 2** are similar to those shown in **Figure 1B1** and only one of the two
electrically coupled neurons (In1) has I_{NaP}. Here, instead of varying the strength of gap junctional
coupling, it was set at 0.1 nS and the effects of varying the strength of I_{NaP} are illustrated. At $\bar{g}_{NaP}$
below the level shown in **Figure 2**, both neurons remain silent. However, with increasing $\bar{g}_{NaP}$, bursting
emerges and increases in frequency. The results demonstrate that the presence of I_{NaP} in one neuron
can initiate synchronized bursting in electrically coupled neurons even if both neurons when uncoupled
are silent.

Overall, gap junctional coupling leads to equilibration of membrane potentials between the
coupled neurons, regardless of the presence/absence of I_{NaP}. Depending on the direction of change
(depolarization or hyperpolarization), this coupling will either increase or decrease bursting frequency
of coupled neurons with I_{NaP} and bring neurons without I_{NaP} from silent or tonic to bursting mode in
synchrony with neurons with I_{NaP}. In turn, I_{NaP} in some neurons can amplify the effect of electrical
coupling of these neurons with other neurons. Finally, both the presence of I_{NaP} in some neurons and
electrical coupling between neurons promotes neuronal synchronization and both are critical for
initiation and support of populational bursting.

2.2   Excitatory chemical synaptic connections in two-cell model

In the case of excitatory connections by chemical synapses, we considered only unidirectional
connections because reported chemical synapses between spinal interneurons have been unidirectional
(Dougherty et al., 2013; Ha and Dougherty, 2018; Chopek et al. 2018). **Figure 3** and **Table 2** illustrate
effects of excitatory chemical synaptic connections in the two-cell model when both neurons (source
neuron In1 and target neuron In2) are bursting neurons incorporating I_{NaP} (panels **A1-A3**), or when I_{NaP}
is incorporated in only In1 (panels **B1** and **B2**) or only In2 neuron (panels **C1** and **C2**).

In **Figures 3A1-A3**, the target neuron (In2) that incorporates I_{NaP} operates in various regimes
without connection: silent (panel **A1**), bursting (panel **A2**), and tonic spiking (panel **A3**). The synaptic
input from In1 to In2 leads to bursting activity in In2 with a burst ratio of 2:1 at a low w_{Syn} (0.5) or

synchronized bursting of both neurons (at higher w_{Syn} values in panel **A1** and in panels **A2** and **A3**, see
also **Table 2**).

In **Figures 3B1,B2**, the target neuron In2 does not have I_{NaP} and when uncoupled is either silent
(panel **B1**) or generates tonic spiking (panel **B2**). In these cases, when In2 receives rhythmic excitatory
synaptic input from the source neuron In1, it follows In1 activity and generates bursts synchronously
with the source. In **Figure 2B2**, the bursting activity in In2 occurs on the background of baseline
spiking activity.

In **Figures 3C1,C2**, the source neuron In1 is a "simple" neuron without I_{NaP} that generates a
sustained spiking activity providing constant excitatory synaptic drive to the target In2 neuron with
I_{NaP}. This drive depolarizes In2 and this depolarization increases with the strength of synaptic input
(w_{Syn}). Therefore, depending on the baseline regime of the target In2 neuron, this input results either in
the emergence of bursting activity (panel **C1**) or the increasing of bursting frequency (panel **C2**, see
also **Table 2**) in the target In2 neuron.

The above simulations have shown that chemical connections in the two-cell model promote
neuronal synchronization and have variable effects on the resultant common bursting frequency.

2.3   Populational models

To study the synchronization and frequency control in a heterogeneous population of neurons
connected by electrical and/or excitatory chemical synapses, we developed a model of a population of
100 neurons consisting of neurons with the intrinsic bursting properties (based on the incorporated
I_{NaP}) and "simple" neurons without such properties (with base ratio of 40/60%). All neurons were
described in the Hodgkin-Huxley style as in the two-cell models described above. The neurons in the
population were sparsely connected by electrical and/or excitatory chemical synapses with probability
of $p_{Gap} = 0.3$ and $p_{Syn} = 0.1$ (Dougherty et al., 2013; Ha and Dougherty, 2018). Following Butera et al.
(1999b), we chose the leakage reversal potential, E_L, the leakage conductance, g_{Leak}, and the maximum
conductance of the persistent sodium current, $\bar{g}_{NaP}$, to be randomly distributed over population to
provide natural heterogeneity between single neuron states. These parameters are the ones that define
the basic level of neuronal excitation and their ability to intrinsically generate bursting activity (Butera
et al. 1999a,b; Del Negro et al., 2002; Koizumi and Smith, 2008). E_L, $\bar{g}_{NaP}$ and g_{Leak} for neurons were
distributed normally with a priory assigned means and standard deviations (see **Materials and**
Methods). The major focus of our studies was on the generation of populational activity and frequency
control of populational bursting for different types of connections and depending on the relative
expression of different types of neuron connectivity and connection strength.

2.3.1 Performance of populational model with electrical coupling

To investigate the role of gap junction in populational bursting, we simulated a population of 100
neurons with bidirectional electrical coupling with coupling probability of 0.3. **Figure 4** shows the
model performance for different values of coupling (g_{Gap}) in the population. In each panel, the upper
row shows the averaged populational activity, the middle row shows raster plots of spikes elicited by
all neurons in the population, and the bottom row shows traces of membrane potentials of several
sample neurons with different excitabilities. Neurons with I_{NaP} are shown by red and neurons without
I_{NaP} are shown by black. In **Figure 4A**, neurons in the population are uncoupled ($g_{Gap} = 0$). Because of
the random distribution of neuronal parameters, neurons operate in different basic regimes: some
neurons with I_{NaP} are silent, some generate bursting activity with different burst frequencies, and some
are tonically active. Similarly, some neurons without I_{NaP} are silent and some demonstrate tonic spiking

activity with different frequencies. The integrated neuron activity is sustained (upper row in **Figure**
4A). With increased electrical coupling (g_{Gap} = 0.033 nS, **Figure 4B**), most of neurons incorporating
I_{NaP} synchronize their bursting activity and some neurons without I_{NaP} become involved in populational
bursting. Further increase of g_{Gap} (g_{Gap} = 0.066 nS, **Figure 4C**) results in synchronization of bursting
activity of all neurons incorporating I_{NaP} and involvement of the majority of neurons without I_{NaP} in
populational bursting, which increases frequency and amplitude of populational bursting activity (see
upper row in **Figure 4C**). However, after all neurons are involved in populational bursting, further
increase of g_{Gap} does not lead to increasing frequency of oscillations. Instead, burst duration starts to
increase and interburst intervals to decrease and eventually all neurons switch to sustained tonic activity
(not shown).

Interestingly, the frequency and amplitude of populational bursting depends on expression of
I_{NaP} in neurons of the population. **Figure 5** shows the dependence of the frequency and amplitude of
populational bursting on the average value of the I_{NaP} conductance ($\bar{g}_{NaP}$) for three different values of
N_{NaP}, defining the number of neurons with I_{NaP} in the population. As N_{NaP} increases, the populational
bursting starts at lower values of $\bar{g}_{NaP}$. The burst frequency increases with increasing values of both
$\bar{g}_{NaP}$ and N_{NaP} (panel **A**), and amplitude of populational bursts is higher at greater N_{NaP} values but
depends on $\bar{g}_{NaP}$ only at lower $\bar{g}_{NaP}$ values (panel **B**).

217　2.3.2 Gap junctional coupling and locomotor-like activity in the spinal cord.

Previous experimental studies have shown that blocking gap junctions with carbenoxolone reduces the
frequency of ventral root bursts of locomotor-like activity in the isolated rodent cord evoked by the
mixture of NMDA and 5-HT (Ha and Dougherty, 2018). **Figures 6A1,A2** show an example of ventral
root recordings during drug-evoked locomotion prior to and 30 min after carbenoxolone application
begins. Burst frequency and amplitude are quantified in **Figures 6B1,B2** demonstrating that blocking
gap junctions in these preparations reduces the frequency of locomotor oscillations and, in most cases,
the amplitude of integrated locomotor activity. To simulate the effect of blocking electrical synapses,
we reduced the strength of gap junctional coupling between neurons by 50% in our model. **Figures**
6C1,C2 demonstrate the average populational activity for a sample simulation when g_{Gap} was reduced
by 50%. To generally estimate the effect of this reduction on frequency and amplitude of synchronized
bursting, we ran several simulations for populations with different randomization of neuron
parameters. As can be seen in **Figures 6D1,D2**, regardless of parameter distribution, our model exhibits
changes in the frequency and amplitude of oscillations with a decrease of g_{Gap} similar to experimental
results shown in **Figures 6A1,A2,B1,B2**.

232　2.3.3 Performance of populational model with chemical coupling

In the next stage of this study, we considered the same population of 100 neurons, but replaced the
bidirectional gap junction connections within the population with unilateral excitatory chemical
connections with probability of p_{Syn} = 0.1 (Dougherty et al., 2013). **Figure 7** shows the model
performance for different weights of excitatory synaptic connections (w_{Syn}) in the population. As can
be seen in these simulations, enhancing w_{Syn} increases the number of tonically active neurons both
among neurons with and without I_{NaP} (**Figures 7A,B**). Simultaneously, the bursting neurons start to
consolidate in clusters including synchronously active neurons with I_{NaP} and partially involving
neurons without I_{NaP} in bursting activity. Further increase of w_{Syn} increases frequency of bursting in
neurons with I_{NaP} and synchronizes all neurons, resulting in populational synchronous bursting of high
frequency and amplitude. In contrast to the population of electrically coupled neurons, in the population
with chemical coupling, an increase in w_{Syn} is accompanied by a simultaneous increase of the
background tonic activity.

2.3.4 Contribution of neuronal coupling by electrical and chemical synapses to populational
activity

Experimental studies have shown that electrical coupling between Shox2 neurons is age-dependent. It
is prevalent between functionally related Shox2 neurons in neonatal spinal cords and decreases in
incidence and strength with age (Ha and Dougherty, 2018). To investigate how the activity of the
population changes when both electrical and excitatory chemical connections are varied, we simulated
a population in which both electrical and excitatory chemical synapses are present and sparsely
distributed among neurons with probabilities of $g_{Gap} = 0.3$ and $p_{Syn} = 0.1$, and introduced two variables
G and W, characterizing in average the total network electrical or chemical synaptic input to each
neuron in the population, respectively (see **Materials and Methods**).

Figures 8A,B show 2D diagrams of color-coded frequency and amplitude of populational
bursts in $[G, W]$ plane. As seen in **Figure 8A**, if W is fixed and G is increasing, for most values of W,
frequency of populational bursting does not increase smoothly but there are distinct areas in which the
frequency does not change much and transition points when frequency increases abruptly. For
example, at lower values of W ($W < 10$) there are one or two distinct transitions from the dark blue to
light blue to cyan or the dark blue to cyan color in the diagram. This frequency transition is even more
sharp at intermediate values of W (i.e. $W = \sim 20$): dark blue abruptly changes to yellow. Our simulations
have shown that in the areas in which frequency does not change much, the increasing G leads
predominantly to synchronization of bursting neurons with I_{NaP} and involving in the populational
bursting some neurons without I_{NaP}. However, at some higher values of G, the remaining tonically
active neurons depolarize neurons with I_{NaP} that have not been initially involved in bursting, leading to
abrupt transitions to a higher frequency. Then again increasing G results predominantly in
synchronization of bursting neurons, this time at a higher frequency of populational bursting.
Depending on particular distribution of neuronal parameters these transitions might happen up to three
times when W is fixed and G is increasing. After all neurons are involved in populational bursting and
synchronized, further increase of G does not produce increases in frequency of populational bursting.
On the contrary, at higher G, the length of the populational bursts is increasing and the interburst
interval is decreasing, leading to smooth transition to the slower populational bursting (shown by
smooth transition from the cyan/yellow to blue in **Figure 8A**) and eventually the population switches
to sustained tonic activity (shown for higher W values by black in **Figures 8A,B**).

With the increase of W, the unilateral excitatory chemical connections allow for a higher
bursting frequency. If W is high enough, (if $W > 20$ in our simulations) the model is capable of
generating synchronous populational bursting at low values of G or even if electrical coupling in the
population is absent. With a fixed G, the frequency of populational bursting is increasing with an
increase of the total strength of the excitatory chemical connections (W). However, the range of G in
which the model generates populational bursting activity decreases with increasing W due to the earlier
transition to sustained tonic activity of the majority neurons (black area in **Figures 8A,B**). **Figure 8B**
shows that the average changes in burst amplitude depending on the values G and W are quite smooth
because the amplitude depends in a greater extent on how well neuron activity in the population is
synchronized and neuronal synchronization directly depends on increasing total strengths of the
electrical and/or excitatory chemical connections (see also **Figures 4,7**).

Figures 8C1-C3 demonstrate the results of simulations for three pairs of G and W values shown
by small red circles in **Figures 8A,B**. In **Figure 8C1**, $W = 0$ and $G = 6$ nS. In this case, G is high
enough to generate synchronized populational bursting activity in the absence of excitatory chemical
connections. **In Figure 8C2**, $G = 3$ nS and at that strength of electrical coupling the model cannot
generate synchronized populational bursting in the absence of excitatory chemical connections.

However, populational bursting can be re-established with increasing W, which is illustrated in **Figure**
8C2 for $W = 15$. On the other hand, if W is high enough, populational bursting activity emerges even
without electrical coupling of neurons in the population as can be seen in **Figure 8C3** at $W = 30$ and G
$= 0$ nS. It should be noted that in the latter case, a higher level of background activity is present.

Altogether, our simulations indicate that both electrical and excitatory chemical connections
between neurons in the heterogeneous population incorporating a subset of intrinsically bursting
neurons support synchronization of activities of individual neurons resulting in the rhythmic
populational bursting activity. However, the effects of increasing strength of electrical and excitatory
chemical coupling of frequency of populational bursting are different.

3   Discussion

This study is based on a previous, experimental investigation by Ha and Dougherty (2018) that revealed
the presence of electrical coupling between Shox2 nonV2a interneurons, which have been suggested
to be critically involved in neuronal synchronization and generation of populational bursting in the
neonatal rodent spinal cords. Here, we used computational modeling to investigate the potential roles
of different neural interactions (gap junctional coupling and/or excitatory chemical synapses) and their
interactions with the cellular I_{NaP}-dependent bursting properties in the neuronal synchronization and
generation of locomotor-like oscillations. We simulated and analyzed the behavior of pair of neurons
operating in different regimes as well as heterogeneous populations of 100 neurons in different states,
sparsely connected by either gap junctions or excitatory chemical synapses, and studied the possible
role of electrical and chemical synaptic connection in populational bursting and control of frequency
and amplitude of populational oscillations. The different aspects of our simulation results in connection
with previous experimental findings as well as limitations of current studies are discussed below.

3.1   The role of electrical coupling between spinal interneurons in rhythmic activity in the
**   isolated spinal cord of neonatal rodents**

Electrical coupling between neurons is known to be widely present in different regions of the central
nervous system of mammals, including rodents, especially in the early stages of the development. The
role of gap junctions in neuronal synchronizations and generation of populational oscillations has been
previously studied using computational neuron models of different complexities (Kepler et al., 1990;
Sherman and Rinzel, 1992; Pfeuty et al., 2003; Kopell and Ermentrout, 2004). Gap junctional coupling
has been demonstrated to interconnect spinal Shox2 nonV2a neurons (Ha and Dougherty, 2018) as
well as Hb9 neurons (via other unidentified neurons, Wilson et al., 2007). It has been suggested that
electrical coupling within each of these genetically identified populations significantly contributes to
neuronal synchronization and populational bursting during spinal circuit development. Although the
role of this coupling in the generation of locomotor-like oscillations in neonatal mouse cords has not
been directly demonstrated for the specific spinal neuronal populations, pharmacological suppression
of gap junctions in the cord in general resulted in a decrease of frequency and amplitude of locomotor-
like oscillations recorded from ventral roots of the neonatal spinal cord during drug-evoked fictive
locomotion (Ha and Dougherty, 2018). Our simulations of a heterogeneous population of neurons
connected with gap junctions have demonstrated the dependence of frequency and amplitude of
populational bursting on the strength of electrical coupling and the reduction of both characteristics
with the reduction of this coupling, similar to the experimental results of pharmacological suppression
of gap junctions. This provides additional support for the role of electrical coupling in the locomotor
activity in the spinal cords of neonatal rodents.

3.2   The potential role of persistent sodium current in locomotor-like oscillations in the cord
and its interaction with gap junction neuronal coupling

Despite many years of intensive investigations, the role of intrinsic biophysical neuronal properties in
the generation of locomotor-like oscillations in the mammalian spinal cords remains largely unknown.
Based on the previous data and computational models on the generation of respiratory oscillations in
the mammalian brainstem (Butera et al., 1999a,b; Del Negro et al., 2001; Rybak et al., 2004), a series
of computational models of spinal locomotor circuits has been developed by suggesting the critical
role of I_{NaP} in the generation of locomotor rhythmic activity in the spinal cord (Rybak et al., 2006a,b;
McCrea and Rybak, 2007). This suggestion has been partly supported by several independent studies
confirming the presence of I_{NaP} in the neonatal rodent spinal cords (Zhong et al., 2007; Tazerart et al.,
2007, 2008; Ziskind-Conhaim et al., 2008; Harris-Warrick, 2010; Brocard et al., 2010, 2013; Tong et
al., 2012). Consequently, most of the recent computational models of spinal locomotor circuits which
incorporated I_{NaP} considered this current to be critically involved in the spinal cord rhythmogenesis
(Sherwood et al., 2011; Zhong et al., 2012; Brocard et al., 2013; Rybak et al., 2013, 2015; Shevtsova
et al. 2014; Danner et al., 2016, 2017, 2019; Shevtsova and Rybak, 2016; Ausborn et al., 2019). The
persistent sodium channels, including their voltage-dependent activation, have been characterized in
spinal Hb9 interneurons present in the spinal cord (Brocard et al., 2013) and presumably contribute to
the generation and/or propagation of locomotor-like oscillations (Wilson et al., 2007; Ziskind-Conhaim
et al., 2008; Brocard et al., 2013). Although I_{NaP} has not yet been characterized in Shox2 neurons, there
is evidence for the expression of persistent inward currents in these neurons which likely includes I_{NaP}
(Ha et al., 2019). In this study, we followed the previous computational models of the spinal locomotor
circuits by suggesting that I_{NaP} plays critical role in the generation of locomotor-like oscillations. We,
however, suggested that this current is present in, and randomly distributed over, only a subset of all
neurons involved in generation of populational oscillations (with basic ratio of 40/60%). Our particular
interest was in considering the behavior of neurons with and without I_{NaP} connected by gap junctions
and the possible roles of this current and electrical coupling in initiation of synchronized bursting
activity. We have shown that electrical coupling leads to equilibration of membrane potentials between
the coupled neurons. Depending on the membrane potentials of neurons, the electrical coupling can
increase and decrease bursting frequency and bring neurons without I_{NaP} from silent or tonic to bursting
mode, hence amplifying neuronal synchronization. We have also shown that the presence of I_{NaP} in
coupled neurons can amplify the effect of electrical coupling, leading to emergence of bursting activity
in initially silent neurons (see **Figure 2**). This corresponds to conclusion made from other studies that
I_{NaP} is a strong modulator of electrical synapses (Haas and Landisman, 2012). Finally, we have shown
that the presence of I_{NaP} in some neurons in cooperation with electrical and/or chemical coupling
between neurons promotes neuronal synchronization in heterogenous neuronal population and that this
current can be critical for initiation and support of populational bursting. Since incorporation of I_{NaP}
into only a subset of neurons in the modelled population was enough to generate a synchronized
populational bursting when bidirectional connections at incidences seen electrophysiologically were
incorporated, we would predict that to generate rhythmic locomotor-like oscillations in the neonatal
spinal cord, it is sufficient for I_{NaP} to be present in a subset of rhythm generating neurons but not
necessarily in all of them.

3.3   Gap junctions vs. chemical synaptic connections

Electrical transmission has been shown to be prevalent during early postnatal period but decreases as
the animal matures (Walton and Navarret, 1991; Chang et al., 1999). Although the decline is seen
within the first postnatal week in motor neurons (Walton and Navarret, 1991; Chang et al., 1999), gap
junctional coupling within both Shox2 non-V2a neuron and Hb9 neuron populations remains relatively

high throughout the first two postnatal weeks (Ha and Dougherty, 2018; Hinckley and Ziskind-
Conhaim, 2006). The probability of coupling among neighboring neurons was found to be ~0.3 (Ha
and Dougherty, 2018) and this is the value that was chosen for the modeling study. The probability
value of 0.1 was set for chemical synapses and falls more in line with a prior Shox2 connectivity study
(Dougherty et al., 2013). There were a few key differences between the reports of Shox2 connectivity.
First, the experiments showing connectivity by chemical synapses at a rate of ~10% (Dougherty et al.,
2013) was performed in mice where the Chx10 absence/presence was not distinguished, so it included
the entire Shox2 population as a single sampling group. Connections were tested in a dorsal horn
removed preparation and were typically within the field of view of a 60x objective but not necessarily
neighboring neurons and there were no instances of electrical connections reported. In Ha and
Dougherty (2018), pairs of neurons recorded were in close proximity (~50μm on average) and were
selected based on the visualization of processes crossing and in close apposition. Further, these neurons
were distinguished based on the presence/absence of Chx10 expression. Therefore, the 33% incidence
of electrical synapses is only among very close neighboring neurons of the same group. In this study,
chemical connections were only found at 2%, indicating that neighboring neurons are less likely to be
connected by chemical synapses. Both values of chemical connections are likely to be underestimated,
particularly the one in which only near neighboring neurons were recorded. Interestingly, the
discrepancies in the results of these studies reinforces the idea that electrical connectivity is mechanism
for local synchronization.

Gap junctions behave as low pass filters and efficiently convey membrane potential
fluctuations. Additionally, action potentials in one Shox2 neuron reliably lead to spikelets in gap
junctionally connected neurons. However, chemical synapses between neonatal Shox2 neurons had
high failure rates (Ha and Dougherty, 2018). Therefore, it is possible that there is a higher incidence of
chemical synaptic connections in older ages, not due to new synapses but increased efficacy at synapses
established early in development. The experimental study considered single pairs using dual recordings
and responses to current injection in the presynaptic neuron. It is unlikely that the postsynaptic cell
receives input from a single presynaptic Shox2 neuron. Gap junctional coupling between multiple
presynaptic neurons will synchronize their firing, as demonstrated in the current study, likely leading
to a more reliable excitation of the postsynaptic neuron, even if excitatory chemical synapses are sparse
and single synapses have high synaptic failure rates. This could provide a mechanism for increased
efficacy of excitatory transmission not only within the population but in transmission to downstream
targets.

Using our model, we investigated how the activity of the population might change with
changing electrical and chemical synaptic connections. Our simulations demonstrated that both
electrical and excitatory chemical connections between neurons in the heterogeneous population
support synchronization of activities of individual neurons resulting in the rhythmic populational
bursting activity. This implicitly confirms that the locomotor-like oscillations in spinal cord can be
maintained over a continuum. Thus, the results suggest that gap junctional coupling strongly drives
synchronization of the population. As bidirectional electrical coupling declines with age, other
mechanisms can take over to maintain rhythmic bursting within the population. The change to a
dominance of unidirectional chemical synaptic interactions, particularly with I_{NaP} present in a subset
of these neurons, is sufficient to fulfill this role and to expand the range of attainable frequencies.
Interestingly, our simulation results have demonstrated that a strong, synchronous population bursting
can be produced in a population when as low as 10% of neurons are connected by excitatory chemical
synapses.

Our simulations have also demonstrated that the effects of increasing the strength of electrical
and excitatory chemical coupling on the frequency of populational bursting are different. In both cases,
a subset of neurons in the population generates spiking activity and provides an excitatory tonic input
to other neurons which is enhanced with increasing connection strength and results in an increased
frequency of populational bursting. In addition, in the case of bidirectional electrical coupling, tonically
active neurons directly depolarize other neurons, elevating neuronal resting potentials and leading to
an increase in frequency of populational bursting. However, in the case of bidirectional electrical
coupling, bursting neurons have a hyperpolarizing effect on tonically firing neurons and eventually an
increase of g_{Gap} turns spiking activity of majority of tonically firing neurons into bursting, as was shown
in our simulations (see **Figures 1A3,B3** and **4**) and in earlier studies (Sherman and Rinzel, 1992). This
prevents further increase in bursting frequency. After all of the neurons become involved in
populational bursting and their membrane potentials reach equilibrium, further increase of g_{Gap} does
not increase the frequency of populational oscillations (see also Kepler et al., 1990). Instead, the
frequency starts to decrease. In contrast, in populations with chemical coupling, elevation of w_{Syn}
increases the activity of tonically active neurons which depolarize bursting neurons, hence leading to
the increase the frequency of populational bursting.

3.4   Limitations of the present studies and future directions

In this modeling study we limited single neuron models by incorporating only minimal number of ionic
channels necessary for generation of neuronal spiking activity, such as fast sodium (Na) and potassium
rectifier (K), and persistent sodium (NaP) involved in bursting rhythmic activity. Therefore, these
models remain largely generic. At the same time, we know that spinal neurons, and particularly Shox2
neuron types contain other ionic channels, including T-type calcium and h currents and different Ca^{2+}
and Ca^{2+}-dependent potassium currents that can also support pacemaker properties and have been
implicated in locomotor-like activity (Wilson et al., 2005; Anderson et al., 2012; Kiehn, 2016; Brocard,
2019). In addition, there is indirect evidence of an important role of Na^+/K^+ pump in CPG operation
(Kueh et al., 2016) and particularly in the neonatal spinal cords of mice (Picton et al., 2017). The role
of Na^+/K^+ pump current has been previously included in the computational models of Hb9 neurons
(Brocard et al., 2013) and can be included in Shox2 neuron models in the future. This current is known
to interact with h-current (Kuen et al., 2016) and can specifically affect neuronal coupling via electrical
and chemical synapses. This awaits additional experimental and computational investigations. A more
realistic model of different types of spinal interneurons that includes different ionic channels with
experimentally measured characteristics should be developed and investigated (see for example,
Sharples et al., 2020), which represents one of the directions of our future investigations.

The other limitation of the present study is the consideration of only excitatory interactions
within the spinal network. The potential role of electrical coupling between inhibitory interneurons and
the role of inhibitory network interactions in cooperation with gap junction (Bennett, 1997; Bennett
and Zukin, 2004; Connors, 2017; Kopell and Ermentrout, 2004) will also be a focus of our future
investigations.

The contribution of gap junctional coupling within specific populations to locomotor
rhythmicity remains to be tested experimentally. The pharmacological studies are limiting in that the
gap junction blockers are acting at all electrical synapses, which have been shown between several
classes of interneurons (Wilson et al., 2007, Hinckley and Ziskind-Conhaim, 2006, Chopek et al.,
Zhong et al., 2010) and motor neurons (i.e. Walton and Navarret, 1991, Tresch and Kiehn, 2000, Rash
et al., 1996, Chang et al., 1999). Additionally, carbenoxolone, the most common gap junction blocker,
has been shown to have additional actions which may affect rhythmicity (Connors, 2012; Tovar et al.,

2009, Elsen et al., 2008). Therefore, conditional knockout studies are required to determine
implications more precisely.

472   Finally, the mutual interactions between different classes of genetically identified excitatory
and inhibitory interneurons present in the mammalian spinal cord also awaits further experimental
and computational investigations.

4   Materials and Methods

4.1   Experimental methods

All experimental procedures followed NIH guidelines and were reviewed and approved by the
Institutional Animal Care and Use Committee at Drexel University (protocols 20317 and 20657).

We performed further analysis of ventral root recordings during fictive locomotion (evoked with
NMDA and 5-HT) prior to and after application of 100μM carbenoxolone, collected for **Figure 6** in
Ha and Dougherty (2018) with detailed methods contained therein. Briefly, spinal cords were isolated
neonatal mice (P0-5) in a cold dissecting solution containing in mM: 111 NaCl, 3 KCl, 11 glucose, 25
NaHCO$_3$, 3.7 MgSO$_4$, 1.1 KH$_2$PO$_4$, and 0.25 CaCl$_2$, bubbled with 95%/5% O$_2$/CO$_2$. Cords were then
transferred to a room temperature recording solution containing in mM: 111 NaCl, 3 KCl, 11 glucose,
25 NaHCO$_3$, 1.3 MgSO$_4$, 1.1 KH$_2$PO$_4$, and 2.5 CaCl$_2$, bubbled with 95%/5% O$_2$/CO$_2$. Glass suction
electrodes were used to record activity from 2-3 lumbar (L)2-5 ventral roots, band-pass filtered at 10-
1,000 Hz. Locomotion was evoked by bath application of N-Methyl-D-aspartic acid (NMDA, 7 μM,
Sigma) and serotonin creatinine sulfate monohydrate (5-HT, 8 μM, Sigma). The gap junction blocker
carbenoxolone (Sigma) was applied at 100μM. Here, twenty-five bursts immediately before
carbenoxolone application and 30 min after the start of carbenoxolone application were subjected to
analysis previously described (Dougherty et al., 2013). Briefly, ventral root activity was rectified and
smoothed (time constant 0.2s) in Spike2 (Cambridge Electronic Design). Recordings included either 2
ventral roots or 3 ventral roots. The cycle and amplitude values were taken from a rostral lumbar root
(L1, L2, or L3) ipsilateral to a recorded caudal lumbar root (L4 or L5). The frequency was calculated
from the mean cycle period, each measured from burst onset to onset. Amplitude was the measured
peak amplitude of each burst. The mean values were normalized to the no drug condition to control for
variations inter-experiment variation including root size, suction electrode size and seal.

4.2   Computational methods

4.2.1 Neuron model

All neurons were simulated in the Hodgkin-Huxley style as single-compartment neuron models. The
membrane potential, V, in neurons with I_{NaP} was described by the following differential equation:

502
$$C \times \frac{dV}{dt} = -I_{Na} - I_{NaP} - I_K - I_L - I_{Gap} - I_{Syn}, \tag{1}$$

503 where C is the membrane capacitance and t is time.

504 The membrane potential, V, in neurons without I_{NaP} current was described as follows:

505
$$C \times \frac{dV}{dt} = -I_{Na} - I_K - I_L - I_{Gap} - I_{Syn}, \tag{2}$$

The ionic currents in Equations (1) and (2) were described as follows:

$I_{Na} = \bar{g}_{Na} \times m_{Na}^3 \times h_{Na} \times (V - E_{Na})$;
$I_{NaP} = \bar{g}_{NaP} \times m_{NaP} \times h_{NaP} \times (V - E_{Na})$;
$I_K = \bar{g}_K \times m_K^4 \times (V - E_K)$;   (3)
$I_L = g_L \times (V - E_L)$,

where I_{Na} is the fast sodium current with maximal conductance $\bar{g}_{Na}$; I_{NaP} is the persistent (slowly
inactivating) sodium current with maximal conductance $\bar{g}_{NaP}$; I_K is the delayed-rectifier potassium
current with maximal conductance $\bar{g}_K$; I_L is the leakage current with constant conductance g_L. E_{Na}, E_K,
and E_L are the reversal potentials for sodium, potassium and leakage currents, respectively; m and h
with indexes indicating currents are, respectively, the activation and inactivation variables of the
corresponding ionic channels.

Dynamics of activation and inactivation variables of voltage-dependent ionic channels (Na,
NaP, and K) in Equation (3) was described by the following differential equations:

$$\tau_{mi}(V) \times \frac{d}{dt}m_i = m_{\infty i}(V) - m_i; \tag{4}$$
$$\tau_{hi}(V) \times \frac{d}{dt}h_i = h_{\infty i}(V) - h_i,$$

where $m_{\infty i}(V)$ and $h_{\infty i}(V)$ define the voltage-dependent steady-state activation and inactivation of the
channel i, respectively, and $\tau_{mi}(V)$ and $\tau_{hi}(V)$ define the corresponding time constants. Activation of the
fast and persistent sodium channels is was instantaneous. The expressions for channel kinetics in
Equation (4) are described as follows:

$$m_{\infty Na}(V) = (1 + \exp(-(V + 42.5)/6.5))^{-1}; \tau_{mNa} = 0;$$
$$h_{\infty Na}(V) = (1 + \exp((V + 65.5)/10.2))^{-1};$$
$$\tau_{hNa}(V) = 35.2/\cosh((V + 65.5)/12.8);$$
$$m_{\infty NaP}(V) = (1 + \exp(-(V + 52)/3.2))^{-1}; \tau_{mNaP} = 0; \tag{5}$$
$$h_{\infty NaP}(V) = (1 + \exp((V + 57)/5))^{-1}; \tau_{hNaP}(V) = T_{hmax}/\cosh((V + 57)/8);$$
$$m_{\infty K}(V) = (1 + \exp(-(V + 34.5)/5))^{-1}; \tau_{mK}(V) = 10/\cosh((V + 34.5)/10).$$

Parameters for channel kinetics were derived from Brocard et al. (2013). The maximal conductances
for the fast sodium, delayed-rectifier potassium, leakage currents were, respectively: $\bar{g}_{Na} = 80$ nS,
$\bar{g}_K = 100$ nS, and $g_L = 1$ nS. The maximal conductance and inactivation time constant for I_{NaP},
$\bar{g}_{NaP}$ and T_{hmax}, and the leakage reversal potential, E_L, in different simulation were varied.

The synaptic current (I_{Syn} with conductance g_{Syn} and reversal potential E_{Syn}) for the j-th neuron
was described as follows:

$$I_{Syn,j} = g_{Syn} \cdot (\textstyle\sum_{i=1}^{N} w_{Syn,ij} \cdot s_i) \cdot (V_j - E_{Syn}), \; j = 1,\ldots,N, \tag{6}$$

where for excitatory chemical synapses $g_{Syn} = 1$ nS, $E_{Syn} = 0$, and $w_{Syn,ij} = w_{Syn}$ if the i-th and j-
neurons were synaptically coupled and equal to 0 otherwise. The value of w_{Syn} was varied.

The synaptic variable s was governed by first order activation scheme (Compte et al., 2005):

$$\frac{d}{dt}s = \alpha_s \cdot s_\infty \cdot (1 - s) - \frac{s}{\tau_s}, \text{ where } s_\infty = 1/(1 + \exp(-(V - V_{s12})/k_s)), \tag{7}$$

where $\alpha_s = 1$; $\tau_s = 15$ ms; $V_{s12} = -20$; and $k_s = 2$.

The electrical coupling current I_{Gap} for the j-th neuron was described as follows:

$$I_{Gap,j} = \textstyle\sum_{i=1}^{N} g_{Gap,ij} \cdot (V_i - V_j), \; j = 1,\ldots,N, \tag{8}$$

where the coupling strength $g_{\text{Gap},ij} = g_{\text{Gap}}$ if the i-th and j-th neurons share a gap junction and is equal
to 0 otherwise. The value of g_{Gap} was varied.

The following general neuronal parameters were assigned: $C = 40$ pF; $E_{\text{Na}} = 55$ mV; $E_{\text{K}} = -80$
mV.

4.2.2 Two-cell model

Each neuron in the two-cell model represented either a bursting neuron incorporating the persistent
sodium current, I_{NaP}, or simple tonically spiking neuron without I_{NaP}. Dynamics of the membrane
potential of the neurons was described by Equations (1-5) where $\bar{g}_{\text{NaP}} = 4$ nS, if not otherwise stated.
These neurons were coupled either bidirectionally by electrical synapses as described by Equation (8)
($g_{\text{Gap}} = \{0.05, 0.1, 0.2\}$) or unidirectionally by AMPA synapse (see Equations (6) and (7), $w_{\text{Syn}} =$
$\{0.5, 1, 2\}$). The initial operational regime of each neuron was defined by the value of its leakage
reversal potential, E_{L}, indicated in **Tables 1,2**.

4.2.3 Neuron population

The neuron population contained 100 neurons and included two subpopulations: neurons incorporating
I_{NaP} (subpopulation 1) and neurons non-incorporating I_{NaP} (subpopulation 2). In our simulations, N_{NaP},
number of neurons incorporating I_{NaP}, varied from 10 to 40 and the observed results were qualitatively
similar.

Heterogeneity of neurons within the population was provided by random distributions of the
baseline values of the mean conductance of the leakage channel, g_{L}, and the leakage reversal potentials,
$E_{\text{L0}i}$ ($i = 1,2$) for two subpopulations, mean maximal conductance of the persistent sodium channel,
$\bar{g}_{\text{NaP}}$, in the subpopulation of neurons incorporating I_{NaP}, and initial conditions for the values of
membrane potential and channel kinetics variables. The baseline values of distributed parameters and
initial conditions were assigned prior to simulations from their defined average values and variances
using a random number generator (normal distribution), and a settling period of 10-40 s was allowed
in each simulation. In our simulations we varied $E_{\text{L01}} = \{-73, -74, -75\}$ for subpopulation of neurons
with I_{NaP}; $E_{\text{L02}} = \{-68, -70, -72\}$ for subpopulation of neurons without I_{NaP}; parameter $\bar{g}_{\text{NaP}}$ was varied
in the range of [2, 5]. We also run simulation with different values of the maximal time constant of the
persistent NaP$^+$ current inactivation, $T_{h\text{max}} = \{7, 9, 10\}$ seconds. In simulations for the populational
model shown in this paper: $N_{\text{NaP}} = 40$; $E_{\text{L01}} = -74 \pm 14.8$ mV; $E_{\text{L02}} = -70 \pm 14$ mV; $g_{\text{L}} = 1 \pm 0.2$; $\bar{g}_{\text{NaP}} =$
4 ± 0.8; $T_{h\text{max}} = 9$ s, if not stated otherwise.

Random connections between neurons in the population were assigned prior to each simulation
based on probability of connections. A random number generator was used to define the existence of
each synaptic connection. Typically, we used $p_{\text{Gap}} = 0.3$ for gap junctional connections and $p_{\text{Syn}} = 0.1$
for excitatory chemical connections. After the distribution of connections was set, the connection
strengths of electrical and/or excitatory chemical synapses (g_{Gap} and w_{Syn}) were altered. To estimate
dependence of the model behavior on coupling strength and type when both types of connections were
present on the model, we introduced two variables G and W, ($G = N \times p_{\text{Gap}} \times g_{GaP}$ and $W = N \times p_{\text{Syn}} \times$
w_{Syn}), characterizing the average total network electrical or chemical synaptic input to each neuron in
the population. To define electrical and chemical synapses in the populational model we used standard
definition of these synapses by Brain2 (Stimberg et al., 2014, 2019). The coupling strengths for
electrical and chemical connection (g_{Gap} and w_{Syn} or G and W) are specified for each simulation.

4.2.4 Computer simulations

586
The simulations for the two-cell model were run by using a custom Matlab script (The Mathworks, Inc.,
Matlab 2020a). The simulations for the populational model were performed using the custom script
written in Python and implemented in Brian2 environment (Stimberg et al., 2014, 2019). Differential
equations were solved using the second order Runga-Kutta integration method. Simulation results were
saved as the ASCI file containing the values of g_{Gap} and w_{Syn} and calculated mean values and standard
deviation over simulation time for the period and amplitude of populational bursting. We also saved
the figures showing populational activity, raster plot of neuron spiking, and voltage traces of sample
neurons over simulation time to visually estimate the results of simulations. The scripts and model
configuration files to create the simulations presented in the paper are available at the [NAME OF
REPOSITORY and LINK to be added upon acceptance of manuscript].

4.2.5 Data analysis in computer simulations

597
The results of simulations were processed by custom Matlab scripts (The Mathworks, Inc., Matlab
2020a). For each neuron period of bursting was estimated as the difference between two consecutive
burst onsets and averaged for the time course of simulation. Frequency was calculated as reciprocal to
the period. To assess the populational model behavior, the averaged integrated activity of neurons in
the population (average number of spikes per neuron per second) was used to calculate the oscillation
period. The timing of burst onsets was determined at a threshold level equal to 30% of the average
populational burst amplitude in the current simulation. For some simulation with less stable
populational activity we determined the threshold level by visual inspection of the results. The bursting
period was defined as the duration between two consecutive burst onsets. Duration of individual
simulations depended on the values of parameters g_{Gap} and w_{Syn}, and to robustly estimate average
value of the oscillation period, the first 10–20 transitional cycles were omitted to allow stabilization of
model variables, and the values of the bursting period and amplitude were averaged for the next 10–20
consecutive cycles. To build 2D diagrams we estimated stability of the populational bursting activity
by calculating values of the period and amplitude of populational bursting and their standard
deviations. All simulations were divided in four groups: no populational activity, low amplitude (less
than 10 spikes per neuron per second) or highly unstable populational activity (SD of calculated period
$\geq$ 50%), stable populational bursting, and tonic populational activity. For the stable populational
bursting, frequency of populational oscillations was determined as reciprocal to the mean period. The
calculated frequency and amplitude were color-coded to build 2D diagrams in G x W parameter space.
Re-initialization of the randomized parameters within the same ranges resulted in qualitatively similar
simulation results.

5   Conflict of Interest

620 *The authors declare that the research was conducted in the absence of any commercial or financial*
621 *relationships that could be construed as a potential conflict of interest.*

6   Author Contributions

NAS, NTH, IAR, and KJD: conceptualization and investigation. NAS, IAR, and KJD: writing (original
draft). NAS, NTH, IAR, and KJD: writing (review and editing). NTH and KJD: experiments and data
curation. NAS: modeling, formal analysis and software. NAS and KJD: visualization.   IAR and KJD:
supervision, project administration, and funding acquisition.

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This   manuscript   has   been   released   as   a   pre-print   at
https://www.biorxiv.org/content/10.1101/2020.09.15.298281v1 (Shevtsova et al., 2020).

8   Data Availability Statement

The experimental and modeling datasets for this study can be found in the [NAME OF REPOSITORY]
[LINK] [will be uploaded after revision].

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10   Figure legends

Figure 1. Effects of electrical coupling on activity of two neurons (In1 and In2). **(A1-A3)** Both neurons
incorporate the persistent sodium current (I_{NaP}). In1 is in a bursting mode and In2 is silent if uncoupled
(A1), operates in a bursing regime **(A2)**, or is tonically active **(A3)**. **(B1-B3)** Only In1 incorporates I_{NaP}
and, if uncoupled, is silent **(B1)** or operates in a busting regime (**B2** and **B3**). In2, if uncoupled, is either
silent (**B1** and **B2**) or tonically active (**B3**). The strength of electrical coupling increases from left to
right.

Figure 2. Effects of increasing I_{NaP} conductance (g_{NaP}) on activity of two neurons mutually connected
via gap junction. In these simulations, $E_{L1} = -71.4$ mV, $E_{L2} = -58.4$ mV, and the strength of the electrical
connection (g_{Gap}) is 0.1 nS.

Figure 3. Effects of the excitatory chemical coupling on activity of two neurons (In1 and In2). **(A1-**
A3) Both neurons incorporate the persistent sodium current (I_{NaP}). In1 is in a bursting mode and In2,
if uncoupled, is silent **(A1)**, or operates in a bursing regime **(A2)**, or is tonically active **(A3)**. **(B1,B2)**
Only In1 incorporates I_{NaP} and operates in a busting regime and In2, if uncoupled, is either silent **(B1)**
or tonically active **(B2)**. **(C1,C2)** In1 does not incorporate I_{NaP} and and is tonically active. In2
incorporates I_{NaP} and if uncoupled, is either silent **(C1)** or operates in a bursting regime **(C2)**. The
weight of synaptic connection increases from left to right.

Figure 4. Model performance at different values of electrical connection strength in the population
(g_{Gap}). $g_{Gap} = 0$ in **A**, 0.033 in **B**, and 0.066 in **C**. The probability of connection is 0.3. The upper row in
each panel shows populational activity as an averaged histogram of neuron spiking [spikes/($N \times$ s),
where $N = 100$ is the number of neurons in population; bin = 100 ms]. The middle rows show raster
plots of spikes elicited by neurons in the population. The lower rows show traces of the membrane
potential of sample neurons. 40% of neurons in the population incorporate I_{NaP} and are shown by red
and neurons without I_{NaP} are shown by black.

Figure 5. Dependence of bursting frequency **(A)** and amplitude **(B)** on the average value of the I_{NaP}
conductance (g_{NaP}) for three values of N_{NaP}, the number of neurons incorporating I_{NaP} in the population.
In these simulations, $g_{Gap} = 0.06$ nS.

Figure 6. Blocking gap junctions decreases locomotor frequency. **(A1,A2)** Extracellular recordings
from ventral roots at lumbar level 2 (L2)-flexor dominant root- and level 5 (L5)-extensor dominant
root- on the right (r) and left (l) sides of the spinal cord after application of NMDA (7 mM) and
serotonin (8 mM) in control case and after addition of carbenoxolone (100 μM). **(B1,B2)** Effect of
carbenoxolone application on frequency **(B1)** and normalized amplitude **(B2)** of locomotor activity for
6 spinal cord preparations. Each circle represents the mean value of estimated parameter for one
recording. Thinner lines connecting two circles represent parameter change in one cord. Thick red lines
represent the means. The black lines in **B1** and **B2** correspond to the experimental recordings shown
in **A1** and **A2**. **(C1,C2)** Effect of decreased strength of electrical coupling (g_{Gap}) on populational
activity. In **C2**, g_{Gap} is reduced by 50%. **(D1,D2)** Effect of g_{Gap} reduction on frequency **(D1)** and
normalized amplitude **(D2)** of locomotor activity for 5 simulations with different randomizations of
model parameters (simulation time 60 s). Each circle represents the average value of estimated
parameter for one simulation. Light colored lines connecting two circles represent parameter change

in simulation. Thick red lines represent the means. The black lines in **D1** and **D2** correspond to the
simulations shown in **C1** and **C2**.

Figure 7. Model performance at different values of excitatory chemical connection strength in the
population (w_{Syn}). The probability of connection is 0.1. Arrangement and notation are the same as in
Figure 4.

Figure 8. Role of electrical vs chemical coupling in generation of synchronized populational activity.
(A,B) 2D diagrams showing color-coded frequency **(A)** and amplitude **(B)** of populational bursting
when the averaged total electrical (G) or chemical (W) synaptic input to each neuron in the population
was varied. **(C1-C)** Examples of simulations for three pairs of G and W values indicated in **A** and **B** by
small red circles. Arrangement and notation in **C1-C3** are the same as in **Figure 4**.

11 Tables

Table 1 Effect of electrical coupling on neuron activity in two-cell model

| Neuron | I_{NaP} | E_L | Regime | Resting potential, mV | | | | Frequency, Hz | | | |
| | | | | Connection strength (g_{Gap},nS) | | | | Connection strength (g_{Gap},nS) | | | |
				0	0.05	0.1	0.2	0	0.05	0.1	0.2
In1	+	-69	B	-66	-66	-66.1	-66.4	0.2	0.2	**0.16**	**0.14**
In2	+	-72.2	S	-71	-70.5	-70.2	-70	N/A	0.08		
In1	+	-69	B	-66	-66.4	-66.4	-66.4	0.2	0.2	**0.35**	**0.33**
In2	+	-65.5	B	-62.7	-62.8	-62.9	-62.9	0.43	0.36		
In1	+	-69	B	-66	-65.8	-67	-66.5	0.2	0.2	**0.39**	**0.36**
In2	+	-64.9	T	-55.4	-61.8	-61.9	-62.7	N/A	0.44		
In1	+	-71.4	S	-69.3	-67	-66.5	-66	N/A	**0.05**	**0.1**	**0.13**
In2	-	-59.6	S	-57	-58.5	-59.1	-59.9	N/A			
In1	+	-69	B	-66	-65.8	-65.6	-65.2	0.2	**0.22**	**0.23**	**0.25**
In2	-	-59.6	S	-57	-58.3	-58.7	-59.8	N/A			
In1	+	-69	B	-66	-65.8	-65.6	-65	0.2	**0.22**	**0.24**	**0.26**
In2	-	-59.3	T	-56.1	-57.7	-58.5	-58.3	N/A			

865 *"+" – neuron incorporating the persistent sodium current (I_{NaP}); "-" – neuron non-incorporating I_{NaP}; "B" – neuron*
866 *generating bursting activity; "S" – neuron in a silent mode; "T" – neuron generating tonic activity; frequency of*
867 *synchronized activity of two neurons is shown by bold.*

868 **Table 2** Effect of chemical coupling on neuron activity in two-cell model

| Neuron | I_{NaP} | E_L | Regime | Resting potential, mV | | | | Frequency, Hz | | | |
| | | | | Connection strength (w_{Syn}) | | | | Connection strength (w_{Syn}) | | | |
				0	0.5	1	2	0	0.5	1	2
In1	+	-65.5	B	62.7				0.43			
In2	+	-71.4	S	-69.3	-70.5	-63.1		N/A	0.2	**0.43**	
In2	+	-69	B	-66	-68.3			0.2	**0.43**		
In2	+	-64.9	T	-55.4	-61.7			N/A	**0.43**		
In2	-	-59.6	S	-57				N/A	**0.43**		
In2	-	-59.3	T	-56.1				N/A	**0.43**		
In1	-	-58.4	T	-55.2				N/A			
In2	+	-72.2	S	-71	-70.5	-70	-68.5	N/A	N/A	N/A	0.12
In2	+	-69	B	-66	-65.6	-65.1	-64.5	0.2	0.22	0.25	0.33

869 *Notation is the same as in **Table 1**.*

Figure 1

FIGURE 2

FIGURE 3

FIGURE 4

FIGURE 5

FIGURE 6

FIGURE 7

FIGURE 8