GENERALIZATION IN DATA-DRIVEN MODELS OF PRIMARY VISUAL CORTEX

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ABSTRACT

Deep neural networks (DNN) have set new standards at predicting responses of neural populations to visual input. Most such DNNs consist of a convolutional network (core) shared across all neurons which learns a representation of neural computation in visual cortex and a neuron-specific readout that linearly combines the relevant features in this representation. The goal of this paper is to test whether such a representation is indeed generally characteristic for visual cortex, i.e. generalizes between animals of a species, and what factors contribute to obtaining such a generalizing core. To push all non-linear computations into the core where the generalizing cortical features should be learned, we devise a novel readout that reduces the number of parameters per neuron in the readout by up to two orders of magnitude compared to the previous state-of-the-art. It does so by taking advantage of retinotopy and learns a Gaussian distribution over the neuron's receptive field position. With this new readout we train our network on neural responses from mouse primary visual cortex (V1) and obtain a gain in performance of 7% compared to the previous state-of-the-art network. We then investigate whether the convolutional core indeed captures *general* cortical features by using the core in transfer learning to a different animal. When transferring a core trained on thousands of neurons from various animals and scans we exceed the performance of training directly on that animal by 12%, and outperform a commonly used VGG16 core pre-trained on imagenet by 33%. In addition, transfer learning with our data-driven core is more data-efficient than direct training, achieving the same performance with only 40% of the data. Our model with its novel readout thus sets a new state-of-the-art for neural response prediction in mouse visual cortex from natural images, generalizes between animals, and captures better characteristic cortical features than current task-driven pre-training approaches such as VGG16.

1 INTRODUCTION

A long lasting challenge in sensory neuroscience is to understand the computations of neurons in the visual system stimulated by natural images (Carandini et al., 2005). An important milestone towards this goal is to achieve general system identification models that can predict the response of large populations of neurons to arbitrary visual inputs. In recent years, deep neural networks have set new standards in predicting responses in the visual system (Yamins et al., 2014; Vintch et al., 2015; Antolík et al., 2016; Cadena et al., 2017; Batty et al., 2016; Kindel et al., 2017; Klindt et al., 2017; Zhang et al., 2018; Ecker et al., 2018; Sinz et al., 2018) and the ability to yield novel response

characterizations (Walker et al., 2019; Bashivan et al., 2019; Ponce et al., 2019; Kindel et al., 2019; Ukita et al., 2019).

High performing predictive models need to account for the increasingly nonlinear response properties of neurons along the visual hierarchy. As many of the nonlinearities are currently unknown, one of the key challenges in neural system identification is to find a good set of characteristic nonlinear basis functions—so called *representations*. However, learning these complex nonlinearities from single neuron responses is difficult given limited experimental data. Two approaches have proven to be promising in the past: *Task-driven* system identification networks rely on transfer learning and use nonlinear representations pre-trained on large datasets for standard vision tasks, such as object recognition (Yamins & DiCarlo, 2016). Single neuron responses are predicted from a particular layer of a pre-trained network using a simple readout mechanism, usually an affine function followed by a static nonlinearity. *Data-driven* models share a common nonlinear representation among hundreds or thousands of neurons, and train the entire network end-to-end on stimulus response pairs from the experiment. Because the nonlinear representation is shared, it is trained via massive multi-task learning (one neuron–one task) and can be learned even from limited experimental data.

Task-driven networks are appealing because they only need to fit the readout mechanisms on top of a given representation and thus are data-efficient in terms of the number of stimulus-response pairs needed to achieve good predictive performance (Cadena et al., 2017). Moreover, as their representations are obtained independently of the neural data, a good predictive performance suggests that the nonlinear features are characteristic for a particular brain area. This additionally offers the interesting normative perspective that the functional representations in deep networks and biological vision could be aligned by common computational goals (Yamins & DiCarlo, 2016; Kell et al., 2018; Kubilius et al., 2018; Nayebi et al., 2018; Sinz et al., 2019; Güçlü & van Gerven, 2014; Kriegeskorte, 2015; Khaligh-Razavi & Kriegeskorte, 2014; Kietzmann et al., 2019). In order to quantify the fit of the normative hypothesis, it is important to compare a given representation to other alternatives (Schrimpf et al., 2018; Cadena et al., 2019). However, while representations pre-trained on ImageNet are the state-of-the-art for predicting visual cortex in primates (Cadena et al., 2017; Yamins & DiCarlo, 2016), recent work has demonstrated that pre-training on object categorization (VGG16) yields no benefits over random initialization for mouse visual cortex (Cadena et al., 2019). Because random representation should not be characteristic for a particular brain area, this raises the questions whether there are better ways to obtain a generalizing nonlinear representation for mouse visual cortex.

Here, we investigate whether such a generalizing representation can instead be obtained from *data-driven* networks. For this purpose, we develop a new data efficient readout which is designed to push all non-linear computations into the core and test whether this core has learned general characteristic features of mouse visual cortex by applying the same criteria as for the task-driven approach: The ability of the trained representation to predict a population of previously unseen neurons in a new animal (transfer learning). Specifically, we make the following contributions: ❶ We introduce a novel readout mechanism that keeps the number of per-neuron parameters at a minimum and learns a bivariate Gaussian distribution for the readout position from anatomical data, taking advantage of retinotopy. With this readout alone, we surpass the previous state-of-the-art performance in direct training by 7%. ❷ We demonstrate that a representation pre-trained on thousands of neurons from various animals and scans generalizes to neurons from a previously *unseen animal* (transfer learning). It exceeds the direct training condition by another 11%, setting the new state-of-the-art. It outperforms a *task-driven* representation—trained on object recognition—by about 33%. ❸ We then show that this generalization can be attributed to the *representation* and not the readout mechanism, indicating that the data-driven core indeed captures generalizing features of cortex: A representation trained on a single experiment (4.5k examples) in combination with a readout trained on anatomically matched neurons from four experiments (17.5k examples) did not achieve this performance. ❹ Lastly, we find that transfer learning with our data-driven core is more data-efficient than direct training, achieving the same performance as direct training with only 40% of its data. Code for the analyses and the weights of the best generalizing representation will be shared in the final version of the paper[1].

[1]URL not shared to not compromise anonymity.

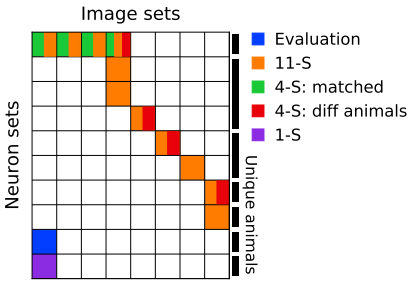

Figure 1: **Scans and training sets.** Overview of the datasets and how they are combined into different training sets. Each scan was performed on a specific set of neurons (rows) using a specific set of unique images (columns). Repeatedly presented test images were the same for all scans. Some scans were performed on the same neuron but with different image sets (first row). Colors indicate grouping of scans into training sets and match line colors in Fig. 5 to indicate which dataset a representation/core (not the readout) was trained on.

2 METHODS

2.1 DATA

Functional data The data used in our experiments consists of pairs of neural population responses and grayscale visual stimuli sampled and cropped from ImageNet, isotropically downsampled to 64×36 px, with a resolution of 0.53 ppd (pixels per degree of visual angle). The neural responses were recorded from layer L2/3 of the primary visual cortex (area V1) of the mouse, using a wide field two photon microscope. The recording methods, stimulation paradigm and data pre-processing followed the procedures described by Walker et al. (2019). A single scan contained the responses of approximately 5000–9000 neurons to up to 6000 images, of which 1000 images consist of 100 unique images which were presented 10 times each to allow for an estimate of the reliability of the neuron (see Appendix for a detailed description of the datasets). We used the repeated images for testing, and split the rest into 4500 training and 500 validation images. The neural data was preprocessed by normalizing the responses of the neurons by their standard deviation on the training set.

All together, we used 13 scans from a total of 7 animals (Fig. 1). Each scan is defined by the set of neurons it was performed on (rows/*neuron sets* in Fig. 1) and the set of images that were shown (columns/*image sets* in Fig. 1). Different image sets had non-overlapping training/validation images, but the same test images. Some of the scans were performed on the same neurons, but with different sets of natural images (first row in Fig. 1). These neurons were matched across scans by cross-correlating the structural scan planes against functionally recorded stacks (Walker et al., 2019). Stitching data from several scans in this way allowed us to increase the number of image presentations per neuron beyond what would be possible in a single scan. We combined these scans into different training sets (one color–one training set in Fig. 1) and named each one of them—*e.g.* `11-S` for a set with 11 **S**cans. The different sets are further explained in the respective experiments they are used in.

2.2 NETWORKS AND TRAINING

The networks are split conceptually into two parts: a *core* and a *readout*. The core captures the nonlinear image representation and is shared among all neurons. The readout maps the features of the core into neural responses and contains all neuron specific parameters.

Representation/Core We model the core with a four-layer convolutional neural network (CNN), with 64 feature channels per layer. In each layer, the 2d-convolutional layer is followed by a batch normalization layer and an ELU nonlinearity (Ioffe & Szegedy, 2015; Clevert et al., 2015). All convolutional layers after the first one are depth-separable convolutions (Chollet, 2017).

Readouts We compared two different types of readouts to map the nonlinear features of the core to the response of each neuron. For each neuron, a tensor of $\mathbf{x} \in \mathbb{R}^{w \times h \times c}$ (**w**idth, **h**eight, **c**hannels) needs to be mapped to a single scalar, corresponding to the target neuron's response. All of our readouts assume that this function is affine with a linear weight tensor $\mathbf{w} \in \mathbb{R}^{w \times h \times c}$, followed by an ELU offset by one (ELU+1), to keep the response positive. Furthermore, both readouts assume that the receptive field of each neuron is the same across features, but differ in how the receptive field location is constrained and learned.

The *factorized readout* (Klindt et al., 2017) factorizes the 3d readout tensor into a lower-dimensional representation by using a spatial mask matrix u_{ij} and a vector of feature weights v_k, i.e. $w_{ijk} = u_{ij} v_k$. The spatial mask u_{ij} is restricted to be positive and encouraged to be sparse through an L1 regularizer.

Our novel *Gaussian readout* reduces the number of per-neuron parameters. It computes a linear combination of the feature activations at a single spatial position— parametrized as (x, y) coordinates —via bilinear interpolation (Sinz et al., 2018). To facilitate gradient flow during training, we replace the spatial downsampling used in (Sinz et al., 2018) by a sampling step, which during training draws the readout position of each nth neuron from a bivariate Gaussian distribution $\mathcal{N}(\mu_n, \Sigma_n)$. This is the sampling version of (St-Yves & Naselaris, 2017) where the readout location is weighted spatially with a Gaussian profile. In our case, μ_n and Σ_n are learned via the reparametrization trick (Kingma & Welling, 2014). Initializing Σ_n large enough ensures that there is gradient information available to learn μ_n reliably. During training, Σ_n shrinks as the estimate of the neuron position improves. During evaluation we always use the position defined by μ_n, making the readout deterministic. This version of the Gaussian readout has $c + 7$ parameters per neuron (μ, Σ and bias).

The second innovation of our Gaussian readout is to couple the location estimation of single neurons by exploiting the retinotopic organization of primary visual cortex (V1) and other areas. Since V1 preserves the topology of visual space, we estimate a neuron's receptive field location from its position $\mathbf{p}_n \in \mathbb{R}^2$ along the cortical surface available from the experiments. To that end, we learn a common function $\mu_n = f(\mathbf{p}_n)$ represented by a neural network that is shared across all neurons (Fig. 2). Since we work with neurons from local patches of V1, we model f as a linear fully connected network. This approach turns the problem of estimating each neuron's receptive field location from limited data into estimating a single linear transformation shared by all neurons, and reduces the number of per-neuron parameters to $c + 5$. We initialized the *Readout Position Network* to a random orthonormal 2-2 matrix scaled by a factor which was optimized in hyper-parameter selection.

Finally, when training on several scans of anatomically matched neurons from the same mouse (see Data), we share the feature weights v_k across scans. To account for differences in spike inference between scans, we introduced a scan-specific scale and bias for each neuron after the linear readout. We mention in the respective sections whether features are shared or not. The bias of each readout is initialized with the average response on the training set. The effects of both feature sharing and learning from cortical anatomy on the performance of the readout are shown in the Appendix.

Training The networks were trained to minimize Poisson loss $\frac{1}{m}\sum_{i=1}^{m}\left(\hat{r}^{(i)} - r^{(i)} \log \hat{r}^{(i)}\right)$ where m denotes the number of neurons, $\hat{r}$ the predicted neuronal response and r the observed response. We used early stopping on the correlation between predicted and measured neuronal responses on the validation set (Prechelt, 1998): if the correlation failed to increase during any 5 consecutive passes through the entire training set (epochs), we stopped the training and restored the model to the best performing model over the course of training. We found that this combination of Poisson objective and early stopping on correlation yielded the best results. After the first stop, we decreased the learning rate from 5×10^{-3} twice by a decay factor of 0.3, and resumed training until it was stopped again. Network parameters were iteratively optimized via stochastic gradient descent using the Adam optimizer (Kingma & Ba, 2015) with a batch size of 64. Once training completed, the trained network was evaluated on the validation set to yield the score used for hyper-parameter selection. The hyper-parameters were then selected with a Bayesian search (Snoek et al., 2012) of 100 trials and subsequently kept fixed throughout all experiments. Only the scale of the readout regularization was fine-tuned with additional Bayesian searches for the cases of different amounts of data independently. In transfer experiments, we froze all parameters of the core and trained a new readout only.

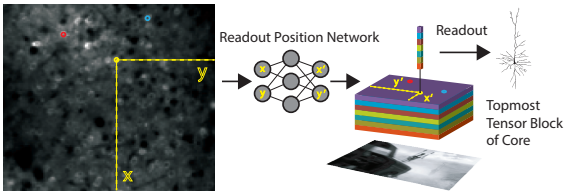

Figure 2: **Using retinotopy to learn the readout position from anatomical data.** Each neuron's coordinates in cortex are transformed to a readout position by a *Readout Position Network* whose weights are shared across neurons and learned during training.

Evaluation We report performance as *fraction oracle* (see Walker et al., 2019), which is defined as the correlation of the predicted response and the observed single-trial test responses relative to the maximally achievable correlation measured from repeated presentations. We estimated the oracle correlation using a jackknife estimator (correlation of leave-one-out mean against single trial). Per data point, we trained 25 networks for all combinations of five different model initializations and five random partitions of the neurons into core and transfer sets. The image subsets were drawn randomly once and kept fixed across all experiments except in Fig. 5 where the full neuron set was used and 5 random partitions of image subsets were drawn instead. We selected the best performing models across initializations and calculated 95% confidence intervals over neuron- or image seeds.

3 RESULTS

We investigated the conditions under which a *data-driven* core generalizes to new neurons in the same or different animals. We did this by pre-training a core on differently composed datasets (core sets, see 3.1) and testing that core in transfer learning to a new set of neurons (transfer set, see 3.1). Our main finding is that transferring a core trained on multiple scans (up to 35k unique images and 70k unique neurons) to a new set of 5335 unique neurons from a single scan (4.5k unique images) yields an improvement in performance of about 12% compared to a network directly trained on the single scan. This result was independent of whether the transferred core was trained on the same animal or not. By carefully choosing the Transfer learning conditions, we can attribute this boost in performance to the generalization of the core.

3.1 TRANSFER LEARNING CONDITIONS

To test the generalization performance of the core, we used a separate set of 1000 neurons which we call *transfer set*. These neurons were not used to train the transferred core but only to fine-tune a new readout (note that Fig. 4 and 5 use different transfer sets, for intra- and inter- animal transfer respectively). A transfer set is a subset of neurons, not images. Thus, each transfer set also had a train, validation, and test split of its images. We compared the performance in transfer learning to that of a network directly trained end-to-end on the transfer set or subsets thereof (*direct* condition). Because the core of the *direct* condition was not transferred, it could adapt to the neurons at hand giving it a fair chance to outperform the transferred cores.

In the transfer learning conditions (all except *direct*), the core was always trained on a separate set of neurons (*core set*) and subsequently frozen, while the readout was always trained on top of the frozen core using the transfer set. Again, a core set is a subset of the neurons, not images. In order to quantify the generalization of the core, we needed to decouple the amount of data it takes to train the core from the amount of data it takes to train the readout. We thus considered two transfer conditions: *diff-core/best-readout* and *best-core/diff-readout*. In the *best-core/diff-readout* condition, the core was trained on the core set using all images, while the readout was trained on the transfer set using different numbers of images. This condition tests the data efficiency of the readout. We expect that better cores lead to a higher data efficiency in the readout, *i.e.* require less data to achieve good performance. In the *diff-core/best-readout* condition, we trained the core on the core set using different numbers of images while the readout was trained on the transfer set using all images. Thereby we tested how the generalization of the core is affected by the amount of data used to train it.

3.2 DIRECT TRAINING AND WITHIN ANIMAL/ACROSS NEURON GENERALIZATION

The following transfer experiments (Fig. 3 and 4) aim at investigating how the number of images and neurons provided to the core and the readout affects generalization to new neurons. To this end, we used a dataset that includes as many images as possible while still providing a reasonably large number of neurons. The `4-S:matched` dataset (first row in Fig. 1, green) provides 17596 images and 4597 neurons anatomically matched across 4 scans. Each scan was performed on the same neurons, but showing different sets of images (test set was identical). The dataset was concatenated along the image dimension and split into core and transfer sets of 3597 and 1000 neurons.

Direct training We used the `4-S:matched` core set to compare the performance of the Gaussian and factorized readout in the *direct* condition on the original core set before transfer. We tested both readouts with and without feature sharing (see Networks and training). The performance of

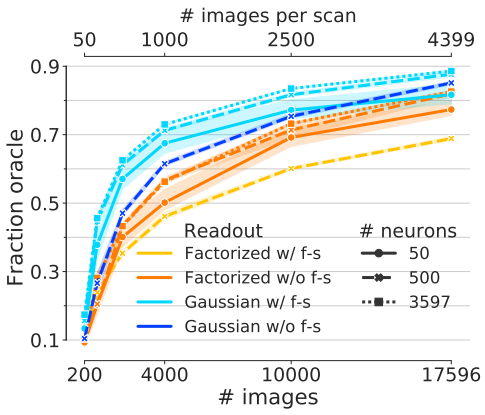

Figure 3: **Performance of end-to-end trained networks.** Performance for different subsets of neurons (linestyle) and number of training examples (x-axis). The same core architecture was trained for two different readouts with and without feature sharing (color) on the matched neurons of the `4-S:matched` core set (Fig. 1, green). Both networks show increasing performance with number of images. However, the network with the Gaussian readout achieves a higher final performance (light blue vs. orange). While the Gaussian readout profits from feature sharing (light vs. dark blue), the factorized readout is hurt by it (yellow vs. orange). Shaded areas depict 95% confidence intervals across random picks of the neuron subsets.

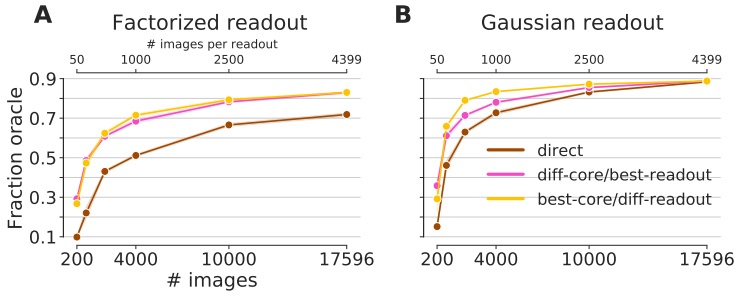

Figure 4: **Generalization to other neurons in the same animal.** A core trained on 3597 neurons and up to 17.5k images generalizes to new neurons (pink and yellow line). A fully trained core yields very good predictive performance even when the readout is trained on far less data (yellow). If the readout is trained with all data, even a sub-optimal core can yield a good performance (pink). Both transfer conditions outperform a network directly trained end-to-end on the transfer dataset (brown). For the full dataset, all training conditions converge to the same performance. Except in the *best-core/diff-readout* condition for very few training data, the Gaussian readout (**B**) outperforms the factorized readout (**A**). The data for both the training and transfer comes from the `4-S:matched` dataset (Fig 1, green). Not that the different number of images can be from the core or transfer set, depending on the transfer condition.

the networks increased with the number of images (Fig. 3). It also increased with the number of neurons, but the number of images had a far stronger effect. While the performance saturated quickly with the number of neurons, saturation w.r.t. the number of images did not seem to be reached, even when using all 17.5k images. The Gaussian readout outperformed the factorized readout in predictive performance by 7% fraction oracle for the full `4-S:matched` dataset, reaching 0.886 ± 0.005 and 0.826 ± 0.005 fraction oracle respectively (mean$\pm$std). While the Gaussian readout profits from feature sharing, the factorized readout is hurt by it (Fig. 3, light vs. dark colors). This might be because the spatial masks in the factorized readout are less constrained in contrast to the Gaussian readout where the position network and the usage of only a single readout point exerts a stronger inductive bias. In all future experiments, we thus use feature sharing only for the Gaussian readout.

Within animal/across neuron generalization For both readouts, the generalization performance of the learned core, tested in the *diff-core/best-readout* condition, increased with the number of images used to train the core (Fig. 4, pink). The cores and readouts were trained on the core and transfer set of the `4-S:matched` dataset. As before, the Gaussian readout outperformed the factorized readout, exhibiting a stronger increase in performance with the number of images and a better final performance when the entire dataset was used to train the core. Even for a sub-optimal core, a readout can yield good performance if it has access to enough images (pink line). Importantly, except for very low numbers of images, the fastest increase in performance occurred in the *best-core/diff-readout*

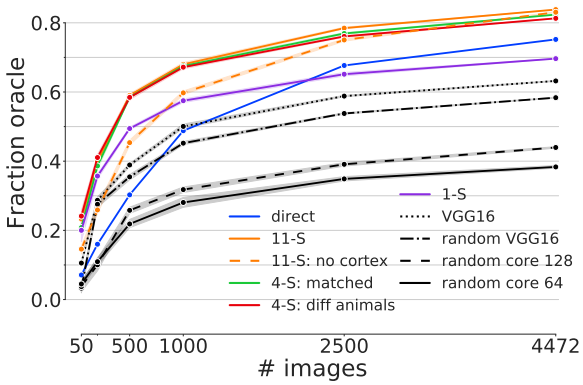

Figure 5: **Generalization across animals.** Prediction performance in fraction oracle correlation as a function of training examples in the transfer set for a Gaussian readout (x-axis) and different ways to obtain the core (colors). The transfer training was performed on the evaluation dataset (blue, Fig 1). Cores trained on several scans used in transfer learning outperform direct training on the transfer dataset (blue line; direct condition).

condition, where a core trained on all images (but different neurons) was frozen and a new readout was trained on the transfer set for varying numbers of images (yellow lines). This result shows that a data-driven core provides general characteristic features for mouse V1, and these features generalize to new neurons. Importantly, for 4k images (about the size of a typical experiment), the performance of the *best-core/diff-readout* was approximately 7% better than the performance of the *diff-core/best-readout* condition (0.834 ± 0.003 and 0.780 ± 0.007 fraction oracle respectively). This observation that a readout on all 17.5k images on a core from 4k images could not reach the performance of a readout on 4k images on a core from 17.5k images suggests that the better performance is due to the generalizing core and not the readout.

3.3 Generalization across animals

So far, we tested generalization performance of data-driven cores to different neurons in the same animal using the `4-S:matched` dataset. A stronger test for generalization is transfer learning across animals, where we may have to deal with inter-subject variability. To this end, we compared several cores derived from different core sets, random initialization, or ImageNet pre-training in terms of their generalization to neurons from a mouse which was not used to train the core. The transfer set consisted of 5335 neurons from a different mouse presented with images that were also in the core set (Fig. 1, blue). Note that performance was still evaluated on a set of test images that were neither used to train core nor readout. Apart from the previously used core set with anatomically matched neurons (`4-S:matched` , Fig. 1, green), we also trained a core on a single scan from another animal (`1-S` , Fig. 1, purple), and on a set of four scans from different animals with different images (`4-S: diff animals` , Fig. 1, red). Finally we also trained a core on all datasets together, without any information on neuron matching or image sets (`11-S` , Fig. 1, orange). For completeness, we also compared to a task-driven VGG core (Simonyan & Zisserman, 2015), a randomly initialized VGG core (reading out from conv2-2 for both) (Cadena et al., 2019), our core (64 features) with randomly initialized weights, and a scaled up version of our core with the same number of features as the VGG (128). As before, we compared the generalization performance to a model trained under the *direct* condition trained on the transfer set. Due to its better performance, we used the Gaussian readout for these experiments but a version with the factorized readout can be found in the Appendix.

We tested the generalization in the *best-core/diff-readout* condition on a single transfer set (Fig. 5), *i.e.* all performances are reported on the same transfer set (5335 neurons) (blue, Fig. 1 and 5), but differ in where the core was trained (colors, Fig. 5). The most striking finding is that representations trained on several scans not only reached better performances for fewer training images, but they also reached a better overall performance for the available data from a single scan compared to *direct* training (Fig. 5 orange, green, and red vs. blue). Interestingly, this improvement did not require matched neurons in the core set (Fig. 5) and any potential negative effects of inter-subject variability were outweighed by the benefits of using multiple scans to train the core. The two cores trained on a single scan reached about the same final performance (Fig. 5, blue vs. purple), with a slightly better performance for the directly trained model, as expected. However, the final performance of both

single scan models was about 10% smaller than the transfer performance from the models pre-trained on four and eleven scans, respectively (Fig. 5, blue and purple vs. red, green, and orange).

Consistent with previous work (Cadena et al., 2017), pre-trained and random VGG16 cores performed similarly (Fig. 5 gray, dotted vs. dash-dotted). Both VGG cores performed worse than a directly trained *data-driven* core (Fig. 5 blue vs. gray dotted and dash-dotted). Finally, a random core with the same architecture as our network (64 features) performs worst, demonstrating that training on neural data extracts characteristic features. Our random core scaled up to VGG size (128) does not match its performance which could be due to the interaction of the initialization with architectural differences.

Lastly, we investigated the effect of constraining all neurons to share the transformation from cortical location to receptive field location by temporarily deactivating this feature (Fig. 5, `11-S: no cortex` dashed orange), and found that this constraint was particularly useful for small numbers of images. Fig 5 for the factorized readout and a table with an overview over the most important results in numerical form can be found in the Appendix.

4 Related work

The idea of a common cortical feature representation is wide-spread in sensory and systems neuroscience, going back to the idea of V1 as a bank of Gabor filters or edge detectors (Jones et al., 1987; Olshausen & Field, 1996). A substantial body of recent work focuses on feature representations learned by training deep networks on vision tasks such as object recognition (Cadena et al., 2017; Yamins & DiCarlo, 2016; Güçlü & van Gerven, 2014; Kriegeskorte, 2015; Khaligh-Razavi & Kriegeskorte, 2014). The brain-score[2] initiative compares different representations, resulting from pre-training on different tasks or different network architectures, with regards to performance of multiple neural prediction tasks (Schrimpf et al., 2018). In contrast to that, we focused on whether multi-task learning between thousands of neurons leads to a generalizing representation.

While *task-driven* representations perform comparably to *data-driven* representations in primates (Cadena et al., 2017), Cadena et al. (2019) recently demonstrated that they show almost no difference in predictive performance for mice. Our results corroborate this finding (Fig. 5) and show that a *data-driven* representation outperforms a *task-driven* representation by a substantial margin, even when tested on equal grounds with transfer learning.

Sharing a representation between neurons is commonly used to learn *data-driven* system identification networks (Cadena et al., 2017; Batty et al., 2016; Sinz et al., 2018; Antolík et al., 2016; Klindt et al., 2017). Klindt et al. (2017) investigated the effect of the number of neurons and training examples onto the predictive performance of a data-driven network. However, this experiment was done on simulated data only and did not explore the generalization (transfer) performance of the learned representation. To the best of our knowledge, we are the first to systematically investigate the ability of data-driven representations to capture general characteristic features of visual cortex.

A recent study investigates generalization of predictive representations across subjects in human fMRI (Wen et al., 2018). However, the authors use a *task-driven* representation from a ResNet (He et al., 2016) trained on ImageNet (Jia Deng et al., 2009) and test the generalization of the readout only, using a previously trained set of readout weights as a prior in ridge regression. While this is possible for predictive models in fMRI, where voxels can be mapped against standardized brain regions, this is not possible for predicting single neurons. In addition, they only find a small effect, suggesting that the key aspect for generalization is the nonlinear representation.

5 Discussion

Machine learning applications in biology are often faced with limited amount of data. Especially, for recent deep learning approaches this poses a challenging problem. One promising way to approach it is multi-task learning by training a shared nonlinear representation on multiple tasks or subjects. This increases the data volume and can help to extract inductive biases to achieve better generalization.

Here, we investigated a particular instance of this problem: Modeling the responses of thousands of cortical neurons as a function of natural visual stimuli. We demonstrated that nonlinear *data-driven*

[2] https://www.brain-score.org/

representations, trained via massive multi-task learning through parameter sharing among thousands of neurons from mouse primary visual cortex, generalize to other neurons and mice, and significantly outperform common *task-driven* alternatives. We showed that the generalization improves with the number of images and neurons used to train the representation and we introduced a novel readout that facilitates generalization by pushing the non-linear computations into the core. The resulting network sets a new state-of-the-art for neural response prediction in direct training *as well as* transfer learning.

We also showed that representations trained on data from multiple different animals lead to state-of-the-art transfer learning performances. This indicates that inter-subject variability, which could affect the success of multi-task learning, does not seem to be a major problem for this application. As a consequence, our core is the most characteristic representation to date to predict mouse primary visual cortex. As our Gaussian readout can predict novel neurons from this representation with relatively few training examples, we believe that this *data-driven* core can be a great tool to investigate the mouse visual cortex in new experiments such as the *inception loops* introduced by Walker et al. (2019) and Bashivan et al. (2019). To this end, we share the trained representation online[3].

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A Appendix

A.1 Two photon scans

The following table lists details about the datasets used. A session marks a continuous experimental session that can comprise several scans and in which the mouse does not leave the scanner. A scan is a single continuous recording of neural activity. Spike inference from the two photon fluorescence signal is performed on the scan level.

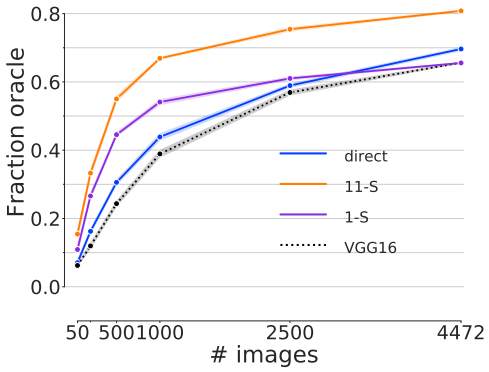
The column **matched** indicates whether neurons were anatomically matched between scans. The four scans from mouse 22564 had 4625 matched neurons.

animal_id	session	scan_idx	neurons	images	matched	in sets
20457	5	9	5335	5993	no	Evaluation
20505	6	1	8367	5996	no	1-S
22564	2	12	8115	5933	yes	4-S, 11-S
22564	2	13	8199	5955	yes	4-S, 11-S
22564	3	8	7916	5986	yes	4-S, 11-S
22564	3	12	8182	5967	yes	4-S, 11-S
22846	2	19	7700	5998	no	11-S
22846	2	21	8044	5947	no	11-S
22846	10	16	7344	5993	no	11-S
23343	5	17	7334	5927	no	11-S
23555	4	20	6848	5957	no	11-S
23555	5	12	6559	5994	no	11-S
23656	14	22	8107	5950	no	11-S

A.2 Generalization across animals (extension)

We showed in Fig 4 in the main paper that the Gaussian readout outperforms the factorized readout in transfer-learning, especially in the low data regime. Consequently we conducted the main transfer experiment, the generalization across animals (Fig 5 in the main paper), with the Gaussian readout. For completeness, we here show the same experiment with the factorized readout for the relevant transfer cores *11-S*, *1-S* and *VGG16* (Fig. 6, left). The exact numeric values for this experiment with full data (5335 neurons, 4472 images) for both readouts can be found in Fig. 6 on the right. Consistent with the previous experiments, the Gaussian readout outperforms the factorized readout for direct

training as well as transfer learning with data-driven cores. Interestingly however, the factorized readout scores higher than the Gaussian readout when compared on the task driven transfer core (VGG16), levelling its performance with the transfer core from one dataset (1-S). We hypothesize that this is caused by the factorized readout's less constrained spatial mask which can pool over more than one pixel in the final tensor and might thus enable it to compensate for the potentially suboptimal features in the VGG16 core.



	Gaussian		Factorized	
	mean	std	mean	std
1-S	0.696	0	0.656	0.002
11-S	0.838	0.001	0.808	0.003
11-S: no cortex	0.831	0.002	-	-
4-S: diff animals	0.813	0.001	-	-
4-S: matched	0.824	0.001	-	-
VGG16	0.632	0.002	0.656	0.002
direct	0.749	0.013	0.696	0.012
random VGG16	0.584	0.001	-	-
random core 128	0.44	0.003	-	-
random core 64	0.383	0.005	-	-

Figure 6: **Generalization across animals** (compare Fig 5 in the main paper). **Left:** Key experiments of Fig 5, conducted with the factorized readout. **Right:** Overview over the performances of the Gaussian and factorized readout models in the transfer-task across animals for full data (5335 neurons, 4472 images).

A.3 Influence of seeds

The performance scores reported in our study are subject to three different sources of statistical uncertainty: The random initialization of the model weights, the specific set of images used to train the model and the specific set of neurons that we wanted to predict. In order to get an estimate of how much each of these factors contribute to the variance in the performance of our models, we trained a total of 90 models, 30 for each source of uncertainty, and varied the respective seeds. While the seed of one source was altered, the seeds of the remaining two sources were kept fixed. Since the impact of the neuron and image seed naturally increases with decreasing amounts of data, we conducted this experiment on a medium range data regime of 1000 images and 1000 neurons. The results can be seen in Fig. 7. While the main contributions to the variance in model performance seem to stem from the model initialization and the random subset of neurons, the image seed did not seem to have a major influence. We thus only used a single value for it in most experiments in the paper. Since we do not consider the variance caused by the random initialization of the model weights as relevant for the underlying scientific problem, we decided to pick the models which performed best on the validation set across 5 model initialization seeds. Finally, we computed 95% confidence intervals across 5 seeds of random neuron subsets. In the cases where all available neurons were used in an experiment, the statistics were computed across 5 image seeds instead (see section Data in the paper). The total number of trained models per data point was thus always 25. In the experiments with simulated data (section **??**), this analysis had not been done yet and three model, neuron and image seeds were used, resulting in 27 trained models per data point. Again, the best models were picked across the three model seeds and statistics were computed across the nine combinations of neuron and image seed.

A.4 Influence of cortical data and feature sharing on the Gaussian readout

Except for the very low data regime, the models with Gaussian readout performed better than the ones with factorized readout, both in direct and transfer learning (see Fig. 2 and 3 in the paper). Here, we investigate which of its components this can be attributed to. To this end we trained models with Gaussian readout directly on the four matched datasets with 3625 neurons and varying number of images (Fig. 8, compare also Fig. 2 in the paper). We did this with and without using the components *feature sharing* and *cortex-data*: In the *feature sharing* condition, each neuron shared the same

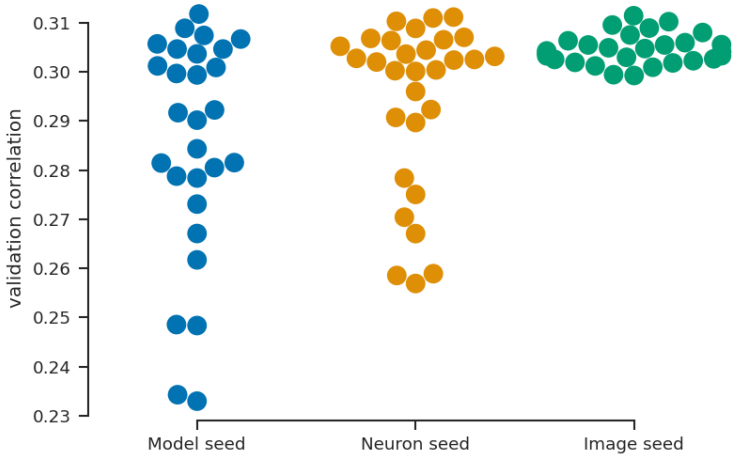


Figure 7: **Variation of model performance across seeds.** Several models (with Gaussian readout) were trained on 1000 neurons and 1000 images each, while varying the initialization of the model (blue), the specific set of 1000 neurons (yellow) and the specific set of 1000 images (green). Since the image seed did not have a major influence on model performance, we decided to only use a single seed value, select the best performing models across 5 model seeds and compute statistics across 5 neuron seeds throughout most of our experiments. In the cases where all available neurons were used in an experiment, the statistics were computed across 5 image seeds instead (see Chapter Data in the paper).

feature weight vector with its anatomical matches across the four datasets. The models with the *cortex-data* condition predicted the receptive field positions from anatomical cortical data via an affine transform. Both, *feature sharing* and *cortex-data* were switched on throughout the paper, and contributed to the good performance of the Gaussian readout. The better performance of the Gaussian readout compared to the factorized readout in Fig. 2 in the paper seems to be mainly due to *feature sharing*. The usage of cortical data to learn the receptive field positions is primarily advantageous for mid-range number of images.

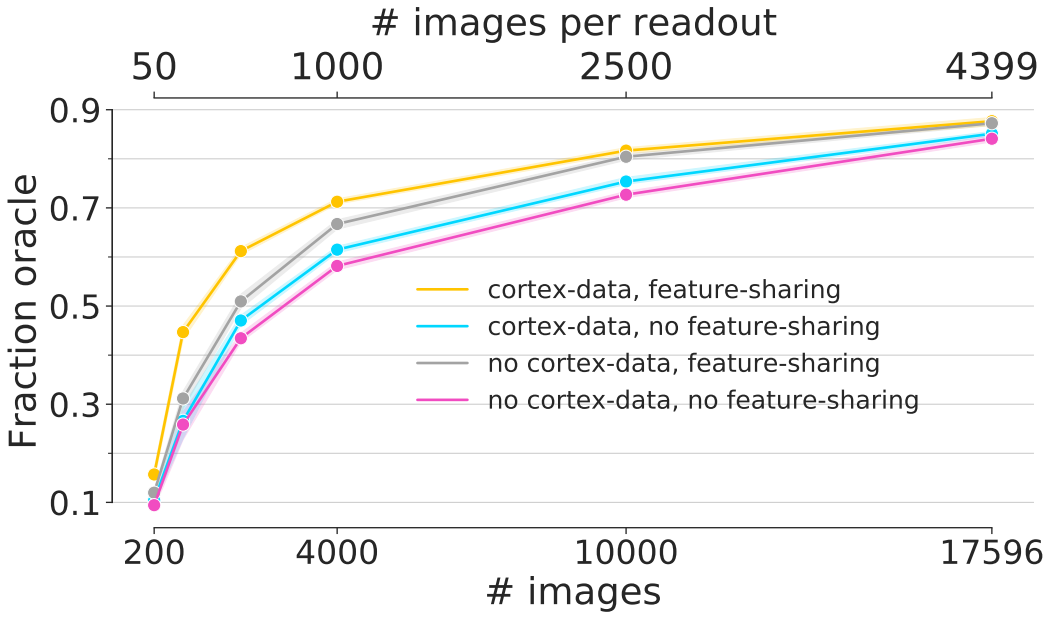


Figure 8: **Gaussian readout with and without feature sharing and position learning from anatomical data.** The training procedure is the same as in Fig. 2 in the paper (yellow and blue lines are identical). The *feature sharing* seems to be the main contributor to the better performance of the Gaussian readout compared to the factorized readout in Fig. 2 in the paper. The usage of cortical data to learn the receptive field positions seems to be primarily advantageous for low and mid range number of images.