Effects of High Magnetic Fields on Diffusion of Biologically Active Molecules

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Abstract

The diffusion of biologically active molecules is a ubiquitous process, controlling many mechanisms and the characteristic time scales for pivotal processes in living cells. Here, we show how a high static magnetic field (MF) affects the diffusion of paramagnetic and diamagnetic species, including oxygen, hemoglobin, ROS and drugs. We derive and solve the equation describing diffusion of such biologically active molecules in the presence of a MF as well as reveal the underlying mechanism of the MF effect on diffusion. We find that a high MF accelerates diffusion of diamagnetic species while slowing the diffusion of paramagnetic molecules in cell cytoplasm. When applied to oxygen and hemoglobin diffusion in red blood cells, our results suggest that a MF may significantly alter the gas exchange in an erythrocyte and cause swelling. Our prediction that the diffusion rate and characteristic time can be controlled by a MF opens new avenues for experimental studies foreseeing numerous biomedical applications.

Significance

We show that diffusion processes of biologically active molecules (hemoglobin, oxygen, reactive oxygen species, etc.) and paramagnetic drugs can be remotely controlled by high static magnetic fields. Since diffusion processes determine the reference time scale for all other processes in living cells as well as the propagation speed of signaling molecules during cell-to-cell communication, our results – the magnetic field dependences of the diffusion rate and characteristic time – may serve as an important key for revealing and understanding the mechanisms of magnetic field action on living cells, tissue and organisms.
Keywords: Interaction between magnetic field and cell; Molecular diffusion; Intracellular ROS; Gas exchange in RBC; Hemoglobin; Drug diffusion

1. Introduction

While humans, animals and plants have always been exposed to natural magnetic fields (MFs), the increasing number of applications of strong MFs and their impact on living beings and the environment are presenting more questions than answers (1). Currently, numerous experimental techniques allow the generation of magnetic fields in the range of thousands of teslas. The world’s strongest resistive 41.4-45 tesla magnet capable of running continuously were engineered in the National High Magnetic Field Laboratory at Florida State University (2017) and the High Magnetic Field Laboratory Hefei Institutes of Physical Science, Hefei, China. Static magnetic fields with a magnetic induction 17.6-21 T are used in MRI instruments for better image resolution and more accurate diagnosis (2, 3). In pulsed regimes, peak fields of 1200 T were generated with newly developed magnetic systems (4-6).

Diffusion is one of the most pervasive processes that controls many mechanisms in cell machinery. Diffusion rate governs the characteristic time scale for intracellular processes, which play pivotal roles in many cell functions, such as regulation of cell membrane potential, cell motility, division, gas exchange, intracellular transport and cell signaling. Thus, since diffusion is often the dynamic basis for a broad spectrum of different intracellular processes, cell functions could be modified by a proper tuning of the diffusion rate of some diffusing species, e.g., tuning of the diffusion coefficient with a magnetic field.

The effects of magnetic field on diffusion has been a topic of investigation since early observations of the effects of static uniform and nonuniform magnetic fields of diffusion on paramagnetic species (7, 8). Interactions between a magnetic field and living cells may result in the appearance of a variety of
Biomagnetic effects at the cellular and organism levels (9-16). Many intriguing mechanisms have been suggested to explain biomagnetic effects (17-21). However, the biological effects related to MF-affected diffusion are poorly understood (8). In this work, we propose the mechanisms of the magnetic control of diffusion in cells and discuss biological consequences related to the diffusion of some biologically active molecules in static uniform magnetic fields.

Let us start with a brief description of the relevant magnetic forces that may affect diffusion in cells. When a static magnetic field (MF) is applied to cell systems, three types of magnetic forces can act on subcellular components, molecules and ions: i) the Lorentz force, \( F_L = q\mathbf{v}\mathbf{B} \) (where \( B \) is the magnetic induction, \( q \) is the ion electric charge and \( \mathbf{v} \) is its velocity); ii) the magnetic gradient force, \( F_{\nabla B} \propto \nabla B^2 \) (22-24) (when the magnetic field is uniform (\( \nabla B \approx 0 \)), the magnetic gradient force is negligible); and iii) the concentration-gradient magnetic force, \( F_{\nabla n} \propto B^2 \nabla n \) (25, 26) (where \( \nabla n \) is the gradient of the concentration of diamagnetic and paramagnetic species and \( \nabla \) is the differential operator nabla).

The concentration-gradient magnetic force will be considered as the main driving force in our model describing the MF effect on diffusion in cells. In fact, living cells are far from thermodynamic equilibrium, and hundreds of diamagnetic and paramagnetic species inside cells may have very large concentration gradients (27). Thus, in the presence of a high MF, a relatively large concentration-gradient magnetic force can be operative in cells. In cells, this force can redistribute paramagnetic free radicals, such as \( O_3 \), NO, and \( NO_2 \) and the molecules \( FeCl_3 \) and \( O_2 \), thereby altering the cell machinery and changing cell fate. However, the effects of a MF on the intracellular reactive oxygen species (ROS) level and ROS trafficking are still perplexing, for a review see work (28).

Here, we demonstrate how the concentration-gradient magnetic force can drive diffusion of paramagnetic and diamagnetic species in cells. We show that even though the concentration-gradient magnetic forces exerted on diffusing molecules are small, they may play an important role in the presence of sufficiently high magnetic fields.
The remainder of the paper is organized as follows. In Section 2.1 we provide the basic formulas for the concentration-gradient magnetic force. In Section 2.2, using calculations of the species concentration as a function of both coordinate and time, we show that a high MF can change the characteristic time of diffusion: accelerating diffusion of diamagnetic molecules and ceasing diffusion of paramagnetic molecules. In Section 2.3, we analyze the role of the magnetic concentration-gradient force in the diffusion of hemoglobin and oxygen in red blood cells (RBC) as well as the diffusion of some biologically active molecules and ROS. The achieved results and prospects for further research are discussed in Section 3.

2. Results

2.1 Magnetic concentration-gradient force

Let us consider a case when a uniform static magnetic field (\( \nabla B = 0 \)) is applied to a cell. In this case, the magnetic concentration-gradient force, \( F_n \), acts on diamagnetic and paramagnetic ions and can either assist or oppose ion movement through the cell. The volume density of the concentration-gradient magnetic force is given by (22):

\[
\vec{f} = \frac{\chi B^2}{2\mu_0} \nabla n,
\]

where \( n \) is the molar concentration of ions with the molar magnetic susceptibility \( \chi \) and \( \mu_0 \) is the vacuum permeability. In a particular case when the concentration only depends on one coordinate, \( x \), the force is determined as follows:

\[
f(x) = \frac{\chi B^2}{2\mu_0} \frac{dn(x)}{dx}.
\]
To analyze the influence of this magnetic force on the diffusion of paramagnetic or diamagnetic molecules we calculate the force exerted per a molecule, $f_1 = f/(nN_A)$. From Eq. 1, this force reads as:

$$f_1 = \frac{\chi B^2}{2\mu_0 n N_A} \nabla n .$$

Under this force (Eq. 3), a molecule moves with the velocity $u = \gamma f_1$, where $\gamma$ is the mobility of a diffusing molecule in a solution. Depending on the sign of the magnetic susceptibility ($\chi<0$ for diamagnetic, and $\chi>0$ for paramagnetic species), the force is either parallel or antiparallel to the concentration gradient. Thus, the magnetic field directly affects diffusion by orienting the diffusion velocity. Several effects related to the role of the force (Eq. 3) in diffusion are considered in detail below.

### 2.2 Magnetic field effect on diffusion of paramagnetic and diamagnetic molecules

The differential equation that describes the diffusion of molecules in a solution moving with velocity $u$ is described as (22, 29, 30)

$$\frac{\partial n}{\partial \tau} = D \nabla^2 n - \left( \nabla \cdot (n \mathbf{u}) \right) ,$$

where $D$ is the diffusion coefficient. Substituting $u = \gamma f_1$ into Eq. 3, one can arrive at

$$\frac{\partial n}{\partial \tau} = D_{eff} \nabla^2 n ,$$

where $D_{eff}$ is the effective diffusion coefficient.
where \( D_{\text{eff}} = \left( D - \frac{\chi B^2}{2\mu_0 N_A} \right) \) is the effective diffusion coefficient. Given that the mobility (\( \gamma \)) of the diffusing molecule in a solution may be calculated using the Nernst-Einstein relation \( \gamma = D/k_B T \) (where \( k_B \) is the Boltzmann constant and \( T \) is the temperature), one can arrive at

\[
D_{\text{eff}}(B) = D(1 - \beta), \tag{6a}
\]

where

\[
\beta = \frac{\chi B^2}{2\mu_0 R T} \tag{6b}
\]

and \( R = 8.31 J/(K \text{ mol}) \) is the gas constant.

Thus, the diffusion process affected by the concentration-gradient magnetic force is described by Eq.5 with \( D_{\text{eff}}(B) \), which is an ordinary differential equation. As seen from Eqs. 6(a,b), a MF decreases (\( \beta > 0 \)) the diffusion coefficient for paramagnetic molecules (\( \chi > 0 \)) and increases it (\( \beta < 0 \)) for diamagnetic molecules (\( \chi < 0 \)). The case \( \beta \ll 1 \) describes the effects of weak magnetic fields on diffusion. The parameter, \( \beta \approx 1 \) corresponds to the suppression of the diffusion of paramagnetic molecules when the concentration flux (Fick’s law) and magnetic flux compensate each other.

The mechanism of the suppression of the diffusion process is qualitatively explained as follows. In a diffusion process, particle flux due to the gradient in concentration is directed from the highest concentration to the lowest concentration, \( J_D = -Ddn/dx \) (Fick’s law), which is antiparallel to \( \nabla n \). Note, this flux is driven by the second law of thermodynamics.

In the presence of magnetic fields, a magnetically driven flux \( (J_{\text{mag}}) \) arises to decrease the magnetic energy of the system (which is negative with the volume density \(-c(pB)\), where \( p \) is the vector of the particle’s magnetic moment and \( c \) is the volume concentration of paramagnetic solute) and tends to move paramagnetic molecules towards an area with highest particle concentration. Indeed, the magnetic concentration-gradient force is parallel to \( \nabla n \) as noted in Eq. 1. Thus, the magnetic flux \( (J_{\text{mag}}) \)
is driven by the energy minimization and is parallel to $\nabla n$ (Fig. 1a). Since the $J_D$ and $J_{mag}$ fluxes are antiparallel, the diffusion rate is decreased (for illustration see Fig. 1a).

![Fig. 1. Sketch of magnetically affected diffusion of paramagnetic (a) and diamagnetic molecules (b). The yellow arrows represent the magnetic field lines. The large blue arrow shows the concentration gradient $\nabla n$ of solute. Red arrows show magnetic concentration-gradient forces (Eq. 1) acting on molecules.](image)

In the case of diamagnetic solute ($\chi<0$) the magnetic force (Eq. 1) is antiparallel to the concentration gradient, and therefore, the $J_D$ and $J_{mag}$ fluxes are parallel (Fig. 1b). This finding implies that a magnetic field accelerates the diffusion of diamagnetic molecules. However, since diamagnetic susceptibilities are several orders of magnitude less than paramagnetic susceptibilities, the magnetic effect on diffusion is rather small. However, since $\beta\chi T^{-1}$ (Eq. 6b), the magnetic contribution to the diffusion increases as the temperature decreases. Thus, at low temperatures, one can expect a noticeable effect of high magnetic fields on the diffusion rate of diamagnetic species.

A 3D diffusion problem with spherical symmetry is described by the following equation:

$$\frac{\partial n}{\partial \tau} = D_{eff}(B) \left( \frac{\partial^2 n}{\partial r^2} + \frac{2}{r} \frac{\partial n}{\partial r} \right), \quad (7)$$
where \( r \) is the radial coordinate.

To solve the differential Eq. 7, one should choose boundary conditions that provide significant information for the understanding of the biological phenomena. However, since in the most cases the geometrical parameters of a diffusion zone and intracellular pathways are unknown, the solution of Eq. 7 with accurately defined boundary conditions is practically impossible. In most cases, we do not know where the edges of a system are located and how the system behaves at these edges. A little is also known about how biologically active molecules are organized and constrained inside living cells. That is why, as a starting point we chose simplest boundary and initial conditions:

\[
n(t, 0) = 0, \ n(t, R) = n_0 \text{ and } n(0, r) = g(r) ,
\]

where \( n_0 \) is the constant concentration at the surface of the sphere, \( r=R \) and the function \( g(r) \) is the initial concentration inside the sphere. The solution of the Eqs. 7 and 8 is described by the equation (31)

\[
n(t, r) = n_0 \left( 1 + \frac{2R}{\pi R} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \sin \left( \frac{n\pi r}{R} \right) \exp \left[ -\frac{D(1-\beta)^2\pi^2 n^2}{R^2} t \right] \right)
\]

In Fig. 2 (a-c), we show the solution of Eq. 9 as the density plots of \( n(t,r)/n_0 \), calculated using Wolfram Mathematica 10 software (32), for the three cases: diffusion with no magnetic field (\( \beta=0 \)) and diffusion in a magnetic field (\( \beta=0.5 \) and \( \beta=-0.5 \)). The calculations of \( n(t,r)/n_0 \) were performed for \( R=5 \mu m, D=10^{-9} \text{ m}^2/\text{s} \) which is the \( O_2 \) diffusivity inside a red blood cell (RBC) (33).
Fig. 2. MF effect on diffusion in a sphere: the contour plots of $n(t,r)/n_0$ given by Eq. 9. The sphere is initially at a uniform zero concentration and the surface concentration is maintained constant at $n_0$. The curves represent $n(t,r)/n_0$: a) with no magnetic field ($\beta=0$), b) with a magnetic field corresponding $\beta=0.5$ (paramagnetic species) and c) with a magnetic field corresponding $\beta=-0.5$ (diamagnetic species).

The calculations of $n(t,r)/n_0$ were performed for $R=5 \, \mu m$, $D=10^{-9} \, m^2/s$ in the time interval $0<t<3 \, ms$. The legend shows the concentration, $n(t,r)/n_0$ which varies from 0 to 1. The white arrows show the direction of the diffusion front propagation. Figure (d) shows the total amount of diffusing substance entering or leaving the sphere as a function of time for $\beta=0$, -0.5 and 0.5.

The total amount of diffusing substance entering or leaving the sphere is given in the form (31)
\[
\frac{M(t)}{M_\infty} = 1 - \frac{6}{\pi^2} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp \left[ -\frac{D(1-\beta)\pi^2n^2}{R^2} t \right],
\]

(10)

where \(M_\infty\) is the corresponding quantity after infinite time.

In Fig. 2 (d), we plot the functions \(\frac{M(t)}{M_\infty}\) for \(\beta=0\) (no magnetic field), \(\beta=0.5\) (paramagnetic species in a MF) and \(\beta=-0.5\) (diamagnetic species in a MF). As seen in Fig. 2 (d), the diffusion rate, \(dM/dt\) (which is the curve slope) crucially depends on the magnetic field: for diamagnetic molecules in a MF \(dM/dt\) increases, while for paramagnetic molecules this quantity decreases.

Thus, the magnetic field can significantly inhibit the diffusion of paramagnetic molecules (see Fig. 2 b, d), e.g., \(O_2\); \(FeCl_3\); deoxyHb; intracellular and intercellular free radicals, such as \(O_3\), NO, and \(NO_2\); and paramagnetic vesicles. On the contrary, a MF accelerates the diffusion of diamagnetic molecules (see Fig. 2 c, d). Below, we estimate the characteristic fields and values of the \(\beta\)-parameter (Eq. 6b) corresponding to the onset of the inhibition (or acceleration) of diffusion for paramagnetic and diamagnetic molecules.

We define the characteristic time scale of a diffusion process as \(\tau_0 \approx L^2/D\), which appears in a solution of the equation for the diffusion in one dimension when \(D\) is constant, \(n(x) \sim t^{1/2} \exp(-x^2/4Dt)\). This solution describes the spreading by diffusion of a certain amount of substance deposited at time \(t=0\) in the plane \(x=0\). A characteristic time scale allows assessment of the key parameters influencing the diffusion process. In practice, a crude estimate of \(\tau_0\) can be made knowing the diffusion coefficient and the lengthscale (\(L\)) of a specific diffusion task. The characteristic time scale for diffusion in cells can be estimated from Eq. 7 as follows. The characteristic time for diffusion due to the concentration gradient is \(\tau_0 \approx \frac{L^2}{D}\). In a MF, for paramagnetic species, the characteristic diffusion time is

\[
\tau_{\text{eff}} \approx \frac{L^2}{D_{\text{eff}}} = \frac{\tau_0}{1-\beta},
\]

(11a)

while for diamagnetic species this time is
\[ \tau_{\text{eff}} \approx \frac{\tau_0}{(1 + |\beta|)} \]  \hspace{1cm} (11b)

In the limiting case \( \beta \rightarrow 1 \) (which corresponds to approaching the critical magnetic field \( B_{\text{cr}} = \sqrt{\frac{2\mu_0 RT}{\chi}} \)), the effective diffusion time of paramagnetic molecules goes to infinity, which implies that the magnetic field completely suppresses the concentration diffusion. By setting the change of the characteristic diffusion time \( (\tau_{\text{eff}}-\tau_0)/\tau_0=\beta/(1-\beta)=\pm 5 \% \), in Eqs. 11, we define the parameter \( \beta_0=0.05 \) as the value of the onset of a MF effect on diffusion.

Since diffusion processes determine the reference time scale for all other processes in cells as well as the propagation speed of signaling molecules during cell-to-cell communication (34), our results – the magnetic field dependences of the diffusion rate and characteristic time – may serve as an important key for revealing and understanding the mechanisms of magnetic field action on living cells, tissue and organisms.

2.3. Diffusion of biologically active molecules in specific examples of biomedical applications

In Table 1, for several biologically active molecules we present the MF induction values corresponding to \( \beta_0=0.05 \) at which a MF starts to affect diffusion as calculated from \( B_0 = \sqrt{\frac{2\mu_0 B_0 RT}{\chi}} \). Below, we analyze the MF effects on diffusion of some biologically active molecules, such as oxygen and, reactive oxygen species (ROS), as well as molecules used as contrast agents in MRI and anticancer paramagnetic drugs.
Table 1. Values of the magnetic field induction (in tesla), corresponding to the onsets of the MF effects on diffusion, as calculated from Eq. 6b a for different paramagnetic and diamagnetic molecules and $\beta_0=0.05$. Gray colors indicate diamagnetic molecules.

<table>
<thead>
<tr>
<th>Molecules</th>
<th>$\chi$, $m^3$/mol,</th>
<th>Ref.</th>
<th>$B_0$, T</th>
</tr>
</thead>
<tbody>
<tr>
<td>deoxyHb</td>
<td>$+60.4 \cdot 10^{-8}$</td>
<td>(35)</td>
<td>22.8</td>
</tr>
<tr>
<td>metHb</td>
<td>$+7.217 \cdot 10^{-7}$</td>
<td>(35, 36)</td>
<td>20.8</td>
</tr>
<tr>
<td>oxyHb</td>
<td>$-4.754 \cdot 10^{-7}$</td>
<td>(35, 36)</td>
<td>25.7</td>
</tr>
<tr>
<td>$O_2$</td>
<td>$+4.3 \cdot 10^{-8}$</td>
<td>(37)</td>
<td>85.3</td>
</tr>
<tr>
<td>Gd</td>
<td>$+18.5 \cdot 10^{-8}$</td>
<td>(37)</td>
<td>41.2</td>
</tr>
<tr>
<td>FeCl$_3$</td>
<td>$+2.573 \cdot 10^{-8}$</td>
<td>(38)</td>
<td>110</td>
</tr>
<tr>
<td>NO</td>
<td>$+0.146 \cdot 10^{-8}$</td>
<td>(37)</td>
<td>463</td>
</tr>
<tr>
<td>NO$_2$</td>
<td>$+0.0150 \cdot 10^{-8}$</td>
<td>(37)</td>
<td>1445</td>
</tr>
<tr>
<td>$O_3$</td>
<td>$+0.00067 \cdot 10^{-8}$</td>
<td>(37)</td>
<td>6387</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>$-0.0021 \cdot 10^{-8}$</td>
<td>(39)</td>
<td>3862</td>
</tr>
<tr>
<td>$O_2^-$</td>
<td>$-17.3 \cdot 10^{-12}$</td>
<td>(39)</td>
<td>4255</td>
</tr>
<tr>
<td>MnCl$_2$</td>
<td>$+3.8 \cdot 10^{-8}$</td>
<td>(38)</td>
<td>90.8</td>
</tr>
<tr>
<td>Ho(NO$_3$)$_3$</td>
<td>$+11.34 \cdot 10^{-8}$</td>
<td>(38)</td>
<td>52.6</td>
</tr>
</tbody>
</table>

2.3.1 Diffusion of hemoglobin and oxygen in red blood cells

The diffusion of hemoglobin and oxygen inside a red blood cell (RBC) drives the oxygen uptake and release by RBCs. Since deoxyhemoglobin (deoxyHb), methemoglobin (metHb) and oxygen ($O_2$) are paramagnetic species (see Table 1), the diffusion rates of $O_2$, deoxyHb and metHb decrease in a MF, e.g. as shown in Fig. 2(b). The diffusion coefficients of hemoglobin and oxygen at concentrations existing inside RBC are important parameters for quantitative description of oxygen uptake and
release by RBCs. The mean diffusion time of Hb inside a RBC is of the order $\tau_{Hb}=a^2/D_{Hb}=1\text{ s}$, where $D_{Hb} \approx 1.6 \cdot 10^{-11} \text{ m}^2/\text{s}$ (40) or $D_{Hb} \approx 3.4 \cdot 10^{-12} \text{ m}^2/\text{s}$ (41). A large difference in the values of $D$ could be explained as follows. Cell is a living system, which is able to adapt its physical parameters to the alternating environment, e.g. by adjusting the diffusion coefficient, which in its turn can be modulated through conformational distributions in the protein. For instance, for LacI repressor proteins diffusing along with DNA, the measured 1D diffusion coefficients were found to vary in a large range, from $2.3 \cdot 10^{-12} \text{ cm}^2/\text{s}$ to $1.3 \cdot 10^{-9} \text{ cm}^2/\text{s}$ (42). The oxygen diffusion time inside an RBC is of the order $\tau_{ox}=a^2/D_{ox} \approx 10 \text{ ms}$, where $a \approx 3 \mu\text{m}$ is the RBC radius, and $D_{ox} \approx 10^{-9} \text{ m}^2/\text{s}$ is the $\text{O}_2$ diffusivity inside RBC (33). Thus, the characteristic time of oxygen diffusion is short compared with the time $\Delta t_{trap}$ associated with $\text{O}_2$ trapping by Hb, which is a few tens of milliseconds (43, 44). Thus, dynamics of oxygen capture by RBCs is characterized by the following time hierarchy: $\tau_{ox} (\approx 10 \text{ ms}) < \Delta t_{trap} (\approx 10-100 \text{ ms}) < \tau_{Hb} (\approx 1 \text{ s} )$. Of note here, Hb diffusion is the slowest process, and its characteristic time is comparable with the time that erythrocytes spend in the lung alveoli $=800 \text{ ms}$ (45-47). Bearing in mind that the Hb diffusion time could be increased by a sufficiently high MF (see Table 1), one can conclude that a 20 T magnetic field application may decrease the blood saturation by oxygen if $\tau_{Hb}$ becomes greater than 800 ms. Of note, as above mentioned, ~20 T MFs are currently used in ultrahigh resolution MRI scanners.

Diffusion is closely related to cell homeostasis. Indeed, when homeostasis is threatened in a cell, diffusion helps to maintain balance in cellular concentrations. Thus, a MF applied to a whole cell body can disturb its dynamic equilibrium (homeostasis) and change the both cell shape and its volume. The concentration-gradient magnetic force (Eq. 1) pushes Hb-molecules towards the RBC membrane and creates a magnetic pressure on it. In fact, the RBC membrane is impermeable to hemoglobin. Knowing the volume density of the magnetic force (Eq. 2), one can calculate the magnetic pressure of Hb on the cell membrane as $P=\mathbf{f}V/S$, where $V$ is the cell volume and $S$ is the membrane area. For a spherical cell one can arrive at the following equation:
\[
P_{\text{mag}} = \frac{x R_c B^2 \nabla n}{6 \mu_0}
\]  

(12)

where \( R_c \) is the mean cell radius. For deoxyHb the magnetic susceptibility is \( x_{\text{Hb}} = 60.4 \times 10^{-8} \) (m\(^3\)/mol) (35). Magnetic susceptibilities for Hb and metHb are \( x_{\text{Hb}} = -4.754 \times 10^{-7} \) (m\(^3\)/mol) and \( x_{\text{metHb}} = 7.217 \times 10^{-7} \) (m\(^3\)/mol)(36), respectively. The other relevant parameters of Hb are: the molecular weight of deoxyHb is \( M_{\text{Hb}} = 64450 \) g/mol (48), the molar volume of Hb in solution is \( v_m = 48277 \) mL/mol (49) and Hb concentration is \( n_{\text{Hb}} = 5.5 \) mol/m\(^3\) (50). Eq. 12 describes the ability of the magnetic pressure to disturb the cell pressure balance and change the RBC volume. The RBC volume magnetic susceptibilities were determined by SQUID (51): \( x_{\text{RBC}} = -9.23 \times 10^{-6} \) (oxy RBC), \(-5.72 \times 10^{-6}\) (deoxy RBC), and \(-5.27 \times 10^{-6}\) (met RBC), in the SI units system.

Now, we estimate the magnetic pressure exerted on deoxyHb in RBCs. The above shown Hb susceptibility and intracellular concentration, \( R_c = 4 \) \( \mu \)m and the volume averaged concentration gradient \( \nabla n = n_{\text{Hb}} / R_c \) (a layer of absorbed deoxyHb is located on the inner surface of an erythrocyte as depicted in Fig. 3), for a completely deoxygenated RBC in a static MF with \( B = 100 \) T are inserted in Eq. 12. Thus, we obtain magnetic pressure \( P_{\text{mag}} \approx 4000 \) Pa. We suppose that a magnetic pressure of hundreds Pa magnitude can disturb the cell pressure balance determined by osmotic pressure, hydrostatic pressure and membrane and cortical tension (52). For example, mitotic HeLa cells exert a rounding pressure (pressure generated by mitotic cells to create space to divide) of 10–150 Pa (53).

As noted in Eq. 12, the magnetic pressure is proportional to the square of magnetic induction and the concentration gradient of the deoxyHb. We conclude that in a sufficiently high magnetic field a completely deoxygenated red blood cell exhibits swelling due to magnetic pressure (Fig. 3), while a completely oxygenated red blood cell does not change its volume. Thus, the swelling effect could be well pronounced only for completely deoxygenated erythrocytes. Despite this findings, the cell
membrane integrity is preserved with a strain as high as 40-50 % (54). In sufficiently high magnetic fields (~100 T) magnetic pressure (Eq. 12) and swelling can cause RBC membrane rupture.

![Diagram of a deoxygenated red blood cell under magnetic pressure on deoxyHb. The white radial arrows show directions of the magnetic concentration-gradient forces. Small white circles represent deoxyHb molecules, while the large white circle represents a layer of absorbed deoxyHb on the inner surface of the membrane of a RBC.](image)

Fig.3. Scheme of a deoxygenated red blood cell under magnetic pressure on deoxyHb. The white radial arrows show directions of the magnetic concentration-gradient forces. Small white circles represent deoxyHb molecules, while the large white circle represents a layer of absorbed deoxyHb on the inner surface of the membrane of a RBC.

It should be noted here that regardless of the above described swelling mechanism, magnetically induced swelling and shape changing of cells (with no paramagnetic agents) have been observed
under the following conditions: i) osteoblasts adhered to glass substrates in the presence of a 5 T-magnetic field (55) and ii) human THP-1 leukemia cells (volume increase up to 90%) after 24 hours of exposure to a spatially modulated high-gradient magnetic field (56).

An interesting aspect of magnetically induced RBC swelling that deserves further study is the diffusion of oxygen ($O_2$) through the RBC membrane. Given that $O_2$ is paramagnetic, the concentration-gradient magnetic force (Eq. 1) pushes $O_2$-molecules either outside or inside an RBC depending on the direction of the gradient $\nabla n_{O_2}$, thereby facilitating/complicating oxygen transport in capillaries. Moreover, mitochondrial function in cells is also crucially dependent on the diffusion rate of $O_2$-molecules, which could be decreased by a sufficiently high magnetic field (see Table 1).

### 2.3.2 Diffusion of ROS

Cytoplasmic and mitochondrial ROS play a dual (harmful and beneficial) role in the cell machinery and are important regulators of cellular life processes in health and disease (57). The intracellular ROS level is dependent on the dynamic balance between ROS generation and elimination, and ROS diffuse between sources and sinks in cytoplasm. Importantly, in most cases, the application of a MF results in increased the ROS level in cells and tissues (28). The possibility of MF effects on ROS diffusion relies on the fact that intracellular and intercellular free radicals, such as $O_3$, NO, and NO$_2$, are paramagnetic (for their paramagnetic susceptibilities see Table 1) and can be redistributed by magnetic concentration-gradient forces (Eq. 3). The following question arises: does static uniform MF significantly contribute to the diffusion of the paramagnetic ROS? Here, we determine that the answer to this question is probably, no at least for MFs with magnitudes less than hundreds of tesla (see Table 1).
2.3.3 Diffusion of molecules used in medicine and paramagnetic drugs

The study of MF effects on diffusion of paramagnetic molecules used as contrast agents in MRI and paramagnetic drugs is especially important in the field of diagnostic and therapeutic. For example, FeCl$_3$-induced arterial thrombosis is used to control bleeding from damaged blood vessels. The experiments (58) showed that ferric chloride (FeCl$_3$) compared to the current standard method, which includes suturing the bleeding site, requires significantly less time to control bleeding with even the lowest concentration of ferric chloride. Ultrastructural analysis revealed that FeCl$_3$ diffused through the vessel wall, resulting in endothelial cell denudation without exposure of the inner layers (59).

Let us analyze how diffusion of FeCl$_3$ through the blood vessel wall can be affected by an MF. Ferric chloride is paramagnetic with a magnetic susceptibility $\chi$=+1.345·$10^{-8}$ m$^3$/mol (see Table 1). As described in Section 2.2 a sufficiently high MF will hinder and slow FeCl$_3$ diffusion. Thus, magnetically hindered thrombosis with FeCl$_3$ will require a greater concentration of FeCl$_3$ compared with its application with no magnetic field. The effects of MF on the FeCl$_3$-induced thrombosis were studied in rat model experiments (60). In the group of rats exposed to a static 600-mT magnetic field thrombus protein content (0.28 ± 0.14 mg/ml) was downregulated compared with the model control group (0.47 ± 0.10 mg/ml). This MF effect has been putatively explained by MF-induced vascular smooth muscle relaxation and blood viscosity reduction. In light of that mentioned above, it is unlikely that the observed decrease in thrombus protein content in 600 mT - MF could be caused by impaired diffusion of FeCl$_3$ to the bleeding site. Indeed, as noted in Table 1, MFs with induction greater than one hundred teslas affect FeCl$_3$ diffusion.

The paramagnetic ion gadolinium Gd(III) is used commonly in MRI contrast agents to provide increased contrast (3, 61). Importantly, this agent is paramagnetic with a sufficiently high magnetic susceptibility, $\chi$=18.5·$10^{-8}$ m$^3$/mol, see Table 1. Thus, for MFs with induction $B$< 40 T, the MF effect on Gd diffusion is expected to be negligible. Thus, no inexpedient diffusional effects on the required distribution of Gd contrast agent are observed from a MF in an MRI machine.
Two paramagnetic species with the highest magnetic susceptibility values are found in the last two rows of Table 1: MnCl₂ and Ho(NO₃)₃. Manganese chloride is used as a nutraceutical and an MRI contrast agent. Holmium (Ho¹⁶⁶) and holmium nitrate are used in medicine for various therapeutic applications, including intratumoural cancer treatment, targeted therapies, skin patches, bone-seeking agents in bone marrow transplantation, and selective internal radiation therapy (SIRT) (62). After injection of drug into a specific site or organ, the drug concentration decreases due to diffusion and biodistribution. Thus, the drug efficacy decreases with time. Therefore, the following important question arises: Is it possible to prevent drug diffusion from the target with a MF. The answer is probably yes. However, this requires applications of MFs with an induction of 50-100 T (see Table 1). Importantly, such a high MF would prevent common drug side effects related to undesirable drug biodistribution outside the target site. Of note, as mentioned in the introduction, currently, static 40-50 T- magnetic fields are reachable in the lab, while MFs of thousand teslas are only attainable using a pulsed regime.

3. Conclusions and Prospects

We have analyzed the roles of static MFs and the magnetic concentration-gradient forces in diffusion of paramagnetic and diamagnetic molecules. It was shown that a high magnetic field accelerates the diffusion of diamagnetic molecules and reduces the diffusion of paramagnetic molecules. We have revealed the underlying mechanisms of magnetically affected diffusion and the key parameter that determines the strength of the MF effect on diffusion, namely, the ratio between the magnetic field energy and that of thermal fluctuations (see Eq. 6b). As above mentioned, at low temperatures, one can expect a sufficient acceleration of the diffusion of diamagnetic molecules by a MF. This effect might be important for cryobiology, in particular, for magnetic cryoconservation of cells and tissues. Indeed, numerous experimental studies have demonstrated the enhanced cells and organisms survival after freezing in presence of magnetic fields. For example, in 0.2-0.4 T static magnetic field,
human erythrocytes were frozen to the temperature of −20°C (63). Rat mesenchymal stem cells were slowly frozen and cryopreserved for 7 days at −150 °C (64). In spite of physical and biological mechanisms of magnetofreezing still being poorly understood, it is obvious that since the diffusion serves as the reference time scale for all other processes in cells, the diffusion of biologically active molecules plays a key role in the survival of cells during freezing and thawing.

Magnetic field effects are also expected in reaction-diffusion systems with paramagnetic solutes. Although there is a curious and incompletely understood way in which these reactions seem to be magnetic field – dependent, direct effects of the magnetic concentration-gradient forces exerted on diffusing molecules may result in novel reaction pathways and MF-driven pattern formation.

We have theoretically predicted a new biological effect of homogeneous high magnetic fields: magnetically induced swelling of deoxygenated red blood cells. A deoxygenated erythrocyte contains deoxygenated hemoglobin, which is paramagnetic. In a high magnetic field, due to the large radial gradient of deoxyHb, the magnetic pressure (Eq. 12) exerted on deoxyHb causes erythrocytes swelling as depicted in Fig.3. As the erythrocyte volume increases, the surface of its membrane also increases. The increase of the membrane area subsequently leads to an increase in the amount of oxygen molecules diffusing into the erythrocyte. Through a chain of chemical reactions, these oxygen molecules bind to Hb making it diamagnetic. Then the magnetic pressure falls to zero, and the initial volume is restored in the erythrocyte. RBC swelling and shape alternations in MFs could affect (probably hinder) oxygen transport from capillaries to tissue. Experimental verification of the prediction of magnetically induced RBC swelling could answer the following important question: how does high magnetic field (e.g., in ultrahigh resolution MRI scanners) affect human health?

Our study has gleaned new insights into the potential biomedical applications of high and ultrahigh magnetic fields and provided new perspectives on the control of diffusion in cells and tissues. In terms of future directions for the development of magnetotherapy (65), our findings argue that cell-to-cell communication can also be directly affected by MFs. Indeed, the propagation time of chemical signals
across the cell envelope, extracellular matrix and tissue is limited by diffusion. Therefore, changes in characteristic diffusion time and subsequent cell signaling alterations induced by a MF represent an intriguing perspective to improve the understanding molecular signaling pathways and develop new treatment approaches for cell therapy. Thus, the application of the elaborated diffusion model and MFs is of vital importance for future studies of cell signaling processes, cell therapy, disease modeling, tissue regeneration, magnetic surgery (66) and tissue engineering using magnetic fields (67).

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Conflict of interest

The authors declare that they have no conflicts of interest with the contents of this article.

Figures Captions

Fig.1. Sketch of magnetically affected diffusion of paramagnetic (a) and diamagnetic molecules (b). The yellow arrows represent the magnetic field lines. The large blue arrow shows the concentration gradient \( \nabla n \) of solute. Red arrows show magnetic concentration-gradient forces (Eq. 3) acting on molecules.

Fig. 2. MF effect on diffusion in a sphere: the contour plots of \( n(t,r)/n_0 \) given by Eq. 9. The sphere is initially at a uniform zero concentration and the surface concentration is maintained constant at \( n_0 \). The curves represent \( n(t,r)/n_0 \): a) with no magnetic field (\( \beta=0 \)), b) with a magnetic field corresponding
\( \beta = 0.5 \) (paramagnetic species) and \( c \) with a magnetic field corresponding \( \beta = -0.5 \) (diamagnetic species).

The calculations of \( n(t,r)/n_0 \) were performed for \( R=5 \mu m, D=10^{-9} m^2/s \) in the time interval \( 0<t<3 \text{ms} \).

The legend shows the concentration, \( n(t,r)/n_0 \) which varies from 0 to 1. The white arrows show the direction of the diffusion front propagation. Figure \((d)\) shows the total amount of diffusing substance entering or leaving the sphere as a function of time for \( \beta = 0, -0.5 \) and 0.5.

Fig.3. Scheme of a deoxygenated red blood cell under magnetic pressure on deoxyHb. The white radial arrows show directions of the magnetic concentration-gradient forces. Small white circles represent deoxyHb molecules, while the large white circle represents a layer of absorbed deoxyHb on the inner surface of the membrane of a RBC.

**References**


