# A model of resource partitioning between foraging bees

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CP, TD and ML designed the study. TD and JG developed the models. CP and TD performed the

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**Abstract**

Central place foraging pollinators tend to develop multi-destination routes (traplines) to exploit several

patchily distributed plant resources. While the formation of traplines by individual pollinators has been stud-

ied in details, how populations of individuals exploit resources in a common area is an open question diffi-

cult to address experimentally. Here we explored conditions for the emergence of resource partitioning

among traplining bees using agent-based models built from experimental data of bumblebees foraging on

artificial flowers. In the models, bees learn to develop routes as a consequence of feedback loops that change

their probabilities of moving between flowers. While a positive reinforcement of route segments leading to

rewarding flowers is sufficient for the emergence of resource partitioning when flowers are evenly distribut-

ed, a negative reinforcement of route segments leading to unrewarding flowers is necessary when flowers are

patchily distributed. In these more complex environments, the negative experiences of individual bees favour

the spatial segregation of foragers and high levels of collective foraging efficiency.

**Keywords:** bumblebees; competition; resource partitioning; trapline foraging; vector navigation

## Introduction

Animals competing for food resources are expected to self-distribute on feeding sites in order to maximize their individual energy gain (Fretwell and Lucas 1969; Giraldeau and Caraco 2000). Resource partitioning between individuals of different species is well documented, and often results from functional (Fründ *et al.* 2010; 2013) or behavioral (Nagamitsu and Inoue 1997; Valdovinos *et al.* 2016) differences. By contrast, how individuals of the same species optimally interact to exploit resources in a common foraging area is less understood (Johst *et al.* 2008; Tinker *et al.* 2012).

For pollinators, such as bees that individually exploit patchily distributed floral resources in environments with high competition pressure, efficient resource partitioning appears a prodigious problem involving the quality of food resources, their spatial distribution, their replenishment rate, and the activity of other pollinators. As central place foragers, bees often visit familiar feeding sites in a stable sequence or trapline (Janzen 1971; Thomson *et al.* 1997). Individual bees with exclusive access to an array of artificial flowers tend to develop traplines minimizing travel distances to visit all the necessary flowers to fill their nectar crop and return to the nest (e.g. bumblebees: Ohashi *et al.* 2008, Lihoreau *et al.* 2012a, Woodgate *et al.* 2017; honey bees: Buatois and Lihoreau 2016). This routing behavior involves spatial memories that can persist several days or weeks (Thomson *et al.* 1996; Lihoreau *et al.* 2010).

How bees partition resources, when several conspecifics exploit a common foraging area, is however still an open question. Experimentally the problem is challenging to address as it requires monitoring the movements of several bees simultaneously over large spatial and temporal scales. In theory, bees should develop individualistic traplines that minimize travel distances and spatial overlap with other foragers, thereby improving their own foraging efficiency and minimizing the costs of competition (Ohashi and Thomson 2005; Lihoreau *et al.* 2016). Best available data supporting this hypothesis come from observations of small numbers of bumblebees foraging on potted plants (e.g. Makino and Sakai 2005, Makino 2013) or artificial flowers (Lihoreau *et al.* 2016, Pasquaretta *et al.* 2019) in large flight tents. In these rather simple foraging conditions, bees tended to avoid spatial overlaps as a consequence of competition by exploitation (when bees visited empty flowers) and interference (when bees interacted on flowers) (Pasquaretta *et al.* 2019).

Computational modeling is a powerful approach to further explore how such partitioning might emerge from spatial learning and competitive interactions. At the individual level, trapline formation has

been modeled using an iterative improvement algorithm by which a bee compares the net length of the route

it has just traveled (sum of the lengths of all movement vectors comprising the flower visitation sequence) to

the length of the shortest route experienced so far (Lihoreau *et al.* 2012b). If the new route is shorter (or

equivalent), the bee increases its probability of using all the movement vectors composing the new route in

its subsequent foraging bout. After several iterations, this route-based learning algorithm typically leads to

the discovery and selection of a short (if not the shortest possible) trapline. While this approach can accurate-

ly replicate observations across a wide range of experimental conditions (Reynolds *et al.* 2013), it makes the

strong assumption that bees can compute, memorize and compare the lengths of multi-leg routes upon return

to their nest. Recently, it was proposed that such behavior could also emerge from vector-based learning (Le

Moël *et al.* 2019), which is more parsimonious and plausible considering the current understanding of spatial

computation in the insect brain (Stone *et al.* 2017). So far, however, none of these traplining models have

accounted for social interactions and current models of pollinator populations do not take into account indi-

vidual specificities of movements based on learning and memory (Becher *et al.* 2014; 2016; 2018). Thus

presently, there has been no realistic exploration of how resource partitioning between interacting bees might

form.

Here, we investigated the behavioral mechanisms underpinning resource partitioning among

traplining bees by comparing predictions of agent-based models integrating route learning and social interac-

tions. First, we developed models implementing biologically plausible vector navigation based on positive

and negative reinforcements of route segments leading to flowers. We used different models to test the indi-

vidual and combined influences of these feedback loops on route learning. Next, we explored how these

simple learning rules at the individual level can promote complex patterns of resource partitioning at the

collective level, using simulations with multiple foragers in environments with different resource distribu-

tions.

**METHODS**

*Model overview*

We developed two agent-based models in which bees learn to develop routes in an array of flowers (Fig. 1).

In both models, all flowers contain the same quality and volume of nectar that is refilled between foraging

bouts (flower visitation sequence, beginning and ending at the colony nest entrance). In simulations with

multiple bees, all bees start their foraging bout synchronously and the flowers are filled after the last bee has

returned to the nest. At each foraging bout, each bee attempts to collect nectar from five different flowers in

order to fill its nectar crop (stomach) to capacity. For simplicity, this rule was set constant across all

simulations. For each bee, flower choice is described using movement vectors (orientated jump between two

flowers or between the nest and a flower). The initial probability of using each possible movement vector is

based on movement vector length. This probability is then modulated through learning when the bee uses a

vector for the first time. The learning rule varied depending on the model. If the ending flower of the vector

contains nectar, it is rewarding and the probability to reuse the vector later increased (positive reinforcement,

models 1 and 2). If the flower is empty, it is not rewarding and the probability to reuse the vector is either

left unchanged (model 1) or decreased (negative reinforcement, model 2). A flower is empty if it has

previously been visited in the same foraging bout by the same bee or another bee (exploitation competition).

If two bees visit a flower at the same time, a fight to secure the possible reward occurs (interference

competition). Only one bee can stay on the flower and access the potential nectar reward with a random

probability. The winner bee takes the reward if there is one. The loser reacts as for an empty flower. Both

bees update their probabilities to reuse the vector accordingly. Route learning thus depends on the experience

of the bee and its interactions with other foragers. For simplicity, we restricted our analysis to two bees, but

the same models can be used to simulate interactions among more bees (see examples with five bees in

Video S1, Appendix S1). The complete R code is available at

*https://gitlab.com/jgautrais/resourcepartitioninginbees/-/releases*.

***Environment***

*Simulations with one foragers*

To calibrate our models, we ran simulations in environments replicating published experimental studies in

which individual bumblebees (*Bombus terrestris*) were observed developing traplines between five equally

rewarding artificial flowers in a large open field (Lihoreau *et al.* 2012b; Woodgate *et al.* 2017). To our

knowledge, these studies provide the most detailed available datasets on trapline formation by bees. Lihoreau

*et al.* (2012b) used a positive array of flowers (regular pentagon, Fig. S1A) in which the distance and

direction between flowers were positively linked, i.e. nearest neighbor flowers could be visited using lowest

angular deviation between consecutive vectors. The authors tracked seven bumblebees, which we judged

enough to run quantitative comparisons with model simulations (raw data are available in Table S1 of

Lihoreau *et al.* 2012b). Woodgate *et al.* (2017) used a negative array of flowers (narrow pentagon, Fig. S1B)

in which the distance and direction between flowers were negatively linked. Here, however, the small sample

size of the original dataset (three bumblebees, data shared by J. Woodgate) only enabled a qualitative

comparison with the model simulations (Appendix S2).

*Simulations with two foragers*

We explored conditions leading to resource partitioning by running model simulations with two foragers.

Here we simulated environments containing 10 flowers (each bee had to visit five rewarding flowers to fill

its crop to capacity). To test whether model predictions were robust to variations in resource spatial

distribution, we simulated three types of environments characterized by different levels of resource

patchiness: (*i*) a patch of 10 flowers, (*ii*) two patches of five flowers each, and (*iii*) three patches of five,

three and two flowers respectively (see examples in Fig. S2). We generated flower patches into a spatial

range comparable to the one used in both experimental setups (Lihoreau *et al.* 2012b; Woodgate *et al.* 2017):

about 500 m$^2$ with a minimum distance of 160 m between each patch center. Within a patch, flowers were

randomly distributed according to two constraints: (i) flowers were at least 20 m apart from each other, (ii)

the maximum distance of each flower from the center of the patch was 40 m. This ensured that each patch

had a maximum diameter of 80 m and inter-flower distances were smaller between all flowers of the same

patch than between all flowers of different patches.

**Movements**

At each step, a bee chooses to visit a target location (flower or nest) based on a matrix of movement

probabilities (Fig. 1). This matrix is initially defined using the inverse of the square distance between the

current position of the bee and all possible target locations (Lihoreau *et al.* 2012b; Reynolds *et al.* 2013). The

probability of moving from location *i* to the location *j* among n possible targets, is initially set to:

(1) $\quad P(i \rightarrow j) = \frac{1}{d^2{}_{ij}} \Big/ \sum_{k \neq j} \frac{1}{d^2_{ik}}$

Where $d_{ij}$ is the distance between locations *i* and *j*. Before choosing its destination, the bee lists all possible

target locations. For simplicity, the bee excludes its current location, thus preventing looping flights to and

from the same flower or nest, which are rare in experienced bumblebee foragers (Ohashi *et al.* 2007; Saleh

and Chittka 2007; Lihoreau *et al.* 2010; Lihoreau *et al.* 2012a; Lihoreau *et al.* 2012b; Woodgate *et al.* 2017).

The bee also excludes the location it had just come from. This simulates the tendency of bumblebees to avoid

recently visited (and thus depleted) flowers (Ohashi *et al.* 2007; Saleh and Chittka 2007; Lihoreau *et al.* 2010;

Lihoreau *et al.* 2012a; Lihoreau *et al.* 2012b; Woodgate *et al.* 2017). The foraging bout ends if: (*i*) the bee

fills its crop to capacity, (*ii*) the bee chooses the nest as a target destination, or (*iii*) the bee reaches a

maximum travelled distance of 3000 m. The latest was added to avoid endless foraging trips in the model. Its

value was chosen based on the observation that bumblebees typically forage within a distance of less than 1

km from their nest (Osborne *et al.* 1999; Wolf and Moritz 2008; Woodgate *et al.* 2016).

*Learning*

Learning modulates the probability of using movement vectors as soon as the bee experiences the chosen

target (online learning) and only once within a foraging bout (the first time the movement vector is used; Fig.

1). This approach has the advantage of implementing vector navigation (Stone *et al.* 2017; Le Moël *et al.*

2019) and thus avoids unrealistic assumptions about computation and comparison of complete routes

(Lihoreau *et al.* 2012b; Reynolds *et al.* 2013). Positive reinforcement was implemented in models 1 and 2. It

occurs when a bee uses a vector leading to a rewarding flower. The probability of using this vector is then

multiplied by 1.5 (other vectors probabilities are scaled accordingly to ensure that all sum up to 1). This

positive reinforcement is based on the well-known tendency of bumblebees to return to nectar rewarding

places through appetitive learning (Goulson 2010). Negative reinforcement was implemented in model 2

only. It occurs when a bee uses a vector leading to a non-rewarding flower. The bee reduces the probability

of using that vector by multiplying it by 0.75 (here also rescaling the other ones). This negative

reinforcement rule is based on the tendency of bumblebees to reduce their frequency of revisits to

unrewarded flowers with experience (Pasquaretta *et al.* 2019). We applied a lower value to negative

reinforcement because bees are much more effective at learning positive stimuli (visits to rewarding flowers)

than negative stimuli (visits to non-rewarding flowers) (review in Menzel 1990). Sensitivity analyses of these

two parameters show that increasing positive and/or negative reinforcement increases the speed and level of

resource partitioning (see Appendix S1).

***Competitive interactions***

We implemented competitive interactions between foragers in the form of exploitation and interference (Fig.

1). Exploitation competition occurs when a bee lands on a flower whose nectar reward has already been

collected by another bee. If the flower is empty, the probability to reuse the vector is either left unchanged

(model 1) or decreased (negative reinforcement, model 2). Interference competition occurs when two bees

encounter on a flower. Only one bee can stay on the flower and access the potential nectar reward with a

random probability (p=0.5). After the interaction, the winner bee takes the reward if there is one. The loser

bee reacts as for an empty flower.

***Statistical Analyses***

All analyses were performed in R version 3.3 (R Development Core Team 2018).

*Simulations with one forager*

For each model, we compared the results of the simulations to the reference observational data, either

quantitatively (for Lihoreau *et al.* 2012b) or qualitatively (for Woodgate *et al.* 2017; see Appendix S2). We

stopped the simulations after 50 foraging bouts to match the experimental conditions of the published data

(22-37 foraging bouts in Lihoreau *et al.* 2012b; 47-61 foraging bouts in Woodgate *et al.* 2017). We run 500

simulations for each model (without and with negative reinforcement) and we estimated how models fitted

the experimental data using two main measures:

(*i*) the quality of each route $QL$, calculated as:

(2)    $QL = \dfrac{\frac{F^2}{d}*1}{QL_{opt}}$

Where $F$ is the number of rewarding flowers visited during a foraging bout and $d$ is the net length of all

vectors traveled during the foraging bout. $QL$ is standardized in [0 ; 1] by the quality of the optimal route in

each array $QL_{opt}$ (shortest possible route to visit all flowers).

(*ii*) a similarity index $SI_{ab}$ between flower visitation sequences experienced during two consecutive foraging

bouts $a$ and $b$ as follows:

(3)        $SI_{ab} = \frac{s_{ab}}{2 l_{ab}}$

Where $s_{ab}$ represents the number of vectors between two flowers found in both sequences, and $l_{ab}$ the

length of the longest flower visitation sequence between $i$ and $j$ multiplied by 2 to make sure that $SI_{ab} = 1$

occurs only when two consecutive sequences sharing the same vectors also have the same length.

235            We applied generalized linear mixed effect models (GLMM) with binomial error, using the g*lmer*

function in 'lme4' package (Bates *et al.* 2014), to assess whether the estimated trends across foraging bouts

for $QL$ and $SI_{ab}$ obtained from model simulations with one forager differed from trends obtained from

observational data. In each model, we used a random structure to account for the identity of bees.

*Simulations with two foragers*

We generated 10 arrays of flowers for each of the three types of environment, and ran 100 simulations for

each of the two models (6000 simulations in total). We compared the simulation outcomes of both models

using four measures:

*i*) the frequency at which each bee experienced exploitation competition (i.e. flower visits when the reward

has already been collected by another bee) and interference competition (i.e. flower visits when two bees

encounter);

*ii*) the similarity index $SI_{ab}$ between successive foraging bouts by the same bee;

*iii*) the degree of resource partitioning among bees, based on network modularity $Q$ (Pasquaretta and Jeanson

2018; Pasquaretta *et al.* 2019). $Q$ is calculated using the *computeModules* function implemented in the R

package 'bipartite' (Dormann *et al.* 2008) using the DIRTLPAwb+ algorithm recently developed by Beckett

(2016). Although $Q$ ranges between 0 (the two bees visit the same flowers) and 1 (the two bees do not visit

any flower in common), the comparison of modularity between networks requires normalization because the

magnitude of modularity depends on network configuration (e.g., total number of flower visits) (Dormann

and Strauss 2014; Beckett 2016). For each network, we computed :

(4) $$Q_{norm} = \frac{Q}{Q_{max}}$$

where $Q_{max}$ is the modularity in a rearranged network that maximizes the number of modules (Pasquaretta

and Jeanson 2018).

*iv*) an index of collective foraging efficiency, $QL_{group}$, computed for each foraging bout *i*, to estimate the

cumulated efficiency of all foraging bees, as:

(5) $$QL_{group,i} = \frac{\sum_{j=1}^{n} QL_{j,i}}{QL_{optimal}}$$

where $QL_{j,i}$ is the route quality of the individual *j* during bout *i*, *n* the number of bees and $QL_{optimal}$ is the

maximum value of all the possible sums of individual route qualities.

To assess whether the trends across foraging bouts obtained from simulations with two bees

differed between models (Fig. 1) and type of environments (Fig. S2), we applied GLMMs for each of the

following response variables: (*i*) frequency of competition types (Poisson error distribution), (*ii*) $SI_{ab}$

(Binomial error distribution), (*iii*) $Q_{norm}$ (Binomial error distribution) and (*iv*) $QL_{group}$ (Binomial error

distribution). In each model, we used a random structure to account for bee identity nested in flower arrays

(i.e. 100 simulations of each spatial array for each model). To statistically compare the trends across foraging

bouts we estimated the marginal trends of the models, as well as their 95% confident intervals using the

*emtrends* function in 'emmeans' package (Lenth 2018). When the 95% confidence intervals of the estimated

trends included zero, the null hypothesis was not rejected. Statistical models were run using the g*lmer*

function in 'lme4' package (Bates *et al.* 2014).

**RESULTS**

***Simulations with one forager***

We first tested the ability of our models to replicate trapline formation by real bees, by comparing

simulations with one forager to published experimental data. In the positive array of flowers (Fig. S1A), real

bees developed routes of increasing quality and similarity with experience (GLMM $_{route\ quality}$: *Estimate =*

$0.128 \pm 0.021$, $P < 0.001$; GLMM $_{route\ similarity}$: *Estimate* $= 0.148 \pm 0.027$, $P < 0.001$). Simulated bees with

positive and negative reinforcements (model 2) or positive reinforcement only (model 1) developed routes of

similar qualities as real bees (Fig. 2A; GLMM $_{model\ 1}$: *Estimate* $= 0.024 \pm 0.021$, $P = 0.244$; GLMM $_{model\ 2}$:

*Estimate* $= 0.017 \pm 0.021$, $P = 0.416$). In both models, the simulated bees also increased route similarity as

much as real bees (Fig. 2B; GLMM $_{model\ 1}$: *Estimate* $= 0.048 \pm 0.027$, $P = 0.074$; GLMM $_{model\ 2}$: *Estimate* $=$

$0.044 \pm 0.027$, $P = 0.105$). In the negative array of flowers (Fig. S1B), a qualitative match between the

simulations of both models and the experimental data was also observed (Fig. S5; see Appendix S2). Thus,

overall, positive reinforcement was sufficient to replicate the behavioral observations. The addition of

negative reinforcement had no major effect on route quality and similarity.

***Simulations with two foragers***

*Exploitation and interference competition*

Having calibrated our models with one forager, we next explored conditions for the emergence of resource

partitioning within pairs of foragers. Here experimental data are not available for comparison. We first

analyzed exploitation competition by quantifying the frequency of visits to non-rewarding flowers by each

bee during each foraging bout. Simulated bees with positive and negative reinforcements (model 2)

decreased their frequency of visits to non-rewarding flowers with time, irrespective of the type of

environment (Fig. 3A; GLMM $_{one\ patch}$: *Estimate* = -8.94e-03, *95%CI* = -9.16e-03 | -8.71e-03; GLMM $_{two\ patches}$:

*Estimate* = -1.88e-02, *95%CI* = -1.91e-02 | -1.86e-02; GLMM $_{three\ patches}$: *Estimate* = -1.05e-02, *95%CI* = -

1.07e-02 | -1.03e-02). However, with positive reinforcement only (model 1), bees behaved differently in the

different environments. In the one patch environment, bees decreased their visits to non-rewarding flowers

(Fig. 3A; GLMM $_{one\ patch}$: *Estimate* = -4.26e-03, *95%CI* = -4.47e-03 | -4.05e-03), whereas in the two and three

patch environments, bees tended to increase their visits to non-rewarding flowers (Fig. 3A; GLMM $_{two\ patches}$:

*Estimate* = 6.27e-03, *95%CI* = 6.09e-03 | 6.44e-03; GLMM $_{three\ patches}$: *Estimate* = 6.65e-03, *95%CI* = 6.46e-

03 | 6.84e-03).

We analyzed interference competition by quantifying the number of interactions on flowers at each

foraging bout between the two bees. Bees with positive and negative reinforcements (model 2) decreased

their frequency of encounters on flowers with time irrespective of the type of environment (Fig. 3B; GLMM

$_{one\ patch}$: *Estimate* = -1.53e-02, *95%CI* = -1.61e-02 | -1.45e-02; GLMM $_{two\ patches}$: *Estimate* = -1.66e-02, *95%CI*

= -1.73e-02 | -1.59e-02; GLMM $_{three\ patches}$: *Estimate* = -1.01e-02, *95%CI* = -1.07e-02 | -0.94e-02). Here again,

bees with positive reinforcement only (model 1) behaved differently in the different environments. In the one

patch environment, bees decreased their frequency of encounters on flowers (Fig. 3B; GLMM $_{one\ patch}$:

*Estimate* = -4.57e-03, *95%CI* = -5.29e-03 | -3.85e-03), whereas in the two and three patch environments,

bees increased their frequency of interactions (Fig. 3B; GLMM $_{two\ patches}$: *Estimate* = 1.05e-02, *95%CI* =

1.01e-02 | 1.10e-02; GLMM $_{three\ patches}$: *Estimate* = 9.16e-03, *95%CI* = 8.64e-03 | 9.68e-03).

Thus overall, negative reinforcement was necessary for reducing exploitation and interference

competition. By allowing bees to avoid empty flowers, negative reinforcement facilitated the discovery of

new flowers and thus gradually relaxed competition. In the absence of negative reinforcement, both types of

competition increased in environments with several flower patches.

*Route similarity*

We analyzed the tendency of bees to develop repeated routes by comparing the similarity between flower

visitation sequences of consecutive foraging bouts for each individual (Fig. 3C). In the two models, bees

increased route similarity through time in all types of environments (Fig. 3C model 1; GLMM $_{one\ patch}$:

*Estimate* = 8.68e-02 , *95%CI* = 8.56e-02 | 8.80e-02 ; GLMM <sub>two patches</sub>: *Estimate* = 8.07e-02 , *95%CI* = 7.96e-

02 | 8.19e-02 ; GLMM <sub>three patches</sub>: *Estimate* = 6.77e-02 , *95%CI* = 6.66e-02 | 6.88e-02; Fig. 3C model 2;

GLMM <sub>one patch</sub>: *Estimate* = 6.80e-02 , *95%CI* = 6.69e-02 | 6.91e-02 ; GLMM <sub>two patches</sub>: *Estimate* = 5.40e-02 ,

*95%CI* = 5.29e-02 | 5.50e-02 ; GLMM <sub>three patches</sub>: *Estimate* = 3.56e-02 , *95%CI* = 3.46e-02 | -3.65e-02). Note

however that the presence of negative reinforcement (model 2) reduced the final level of route similarity. In

these conditions bees learned to avoid revisits to empty flowers and showed greater variation in their

visitation sequences, as a result of searching for new flowers.

*Resource partitioning*

We analyzed the level of resource partitioning by quantifying the tendency of the two bees to use different

flowers. With positive and negative reinforcements (model 2), pairs of bees showed a significant increase of

resource partitioning with time for all types of environments (Fig. 3D; GLMM <sub>one patch</sub>: *Estimate* = -3.82e-02,

*95%CI* = 3.69e-02 | 3.95e-02; GLMM <sub>two patches</sub>: *Estimate* = 2.91e-02, *95%CI* = 2.78e-02 | 3.04e-02; GLMM

<sub>three patches</sub>: *Estimate* = 2.66e-02, *95%CI* = 2.53e-02 | 2.78e-02). With positive reinforcement only (model 1),

bees showed an increase of resource partitioning in environments with one patch (Fig. 3D; GLMM <sub>one patch</sub>:

*Estimate* = 3.24e-02, *95%CI* = 3.11e-02 | -3.36e-02), and a decrease in environments with two or three

patches (Fig. 3D; GLMM <sub>two patches</sub>: *Estimate* = -1.06e-02, *95%CI* = -1.19e-02 | -0.93e-02; GLMM <sub>three patches</sub>:

*Estimate* = -8.08e-03, *95%CI* = -9.40e-03 | -6.77e-03). In these patchy environments, negative reinforcement

facilitates the movements of bees between more distant flowers in different patches and thus the

establishment of spatially segregated routes.

*Collective foraging efficiency*

To quantify the collective foraging efficiency of bees, we analyzed the capacity of the two foragers to reach

the most efficient combination of route qualities (i.e. minimum distance traveled by a pair of bees needed to

visit the 10 flowers ). With positive and negative reinforcements (model 2), pairs of bees increased their

cumulated foraging efficiency with time in all types of environments (Fig. 3E; GLMM <sub>one patch</sub>: *Estimate* =

3.05e-02, *95%CI* = 2.91e-02 | 3.19e-02; GLMM <sub>two patches</sub>: *Estimate* = 3.05e-02, *95%CI* = 2.91e-02 | 3.19e-02;

GLMM <sub>three patches</sub>: *Estimate* = 1.85e-02, *95%CI* = 1.73e-02 | 1.98e-02). With positive reinforcement only

(model 1), bees increased their cumulated foraging efficiency in environments with one patch (Fig. 3E;

GLMM $_{\text{one patch}}$: *Estimate* = 3.24e-02, *95%CI* = 3.11e-02 | 3.37e-02), but decreased or maintained low levels

in environments with two or three patches (Fig. 3E; GLMM $_{\text{two patches}}$: *Estimate* = -5.05e-03, *95%CI* = -6.33e-

03 | -3.76e-03; GLMM $_{\text{three patches}}$: *Estimate* = 3.07e-03, *95%CI* = -1.42e-03 | 4.32e-03). Cumulated foraging

efficiency thus follows the same pattern as resource partitioning. Note that bees can reach higher levels in

environments with one patch than in environments with two or three patches because the probability to

encounter new flowers within a patch is higher in environments with one patch.

## Discussion

Central place foraging animals exploiting patchily distributed resources that replenish over time are expected

to develop foraging routes minimizing travel distances and interactions with competitors (Possingham 1989;

Ohashi and Thompson 2005; Lihoreau *et al.* 2016). Here we developed a cognitively plausible agent-based

model to explore the behavioral mechanisms leading to resource partitioning between traplining bees. In the

model, bees learn to develop routes as a consequence of feedback loops that modify the probabilities of

moving between flowers. While a positive reinforcement of route segments leading to rewarding flowers is

sufficient for resource partitioning to develop when resources are evenly distributed, a negative

reinforcement of route segments leading to unrewarding flowers is necessary in environments with patchily

distributed resources.

When considering bees foraging among uniformly distributed plant resources (one patch), the initial

probabilities to encounter each resource are similar (Fig. S6), and the likelihood of bees to discover new

rewarding resources after encountering unrewarding ones is high. Consequently, two bees are very likely,

over time, to learn non-overlapping foraging routes and show resource partitioning. However, in

environments with non-uniformly distributed resources (two or three patches), the added spatial complexity

can interfere with this process. The initial likelihood of moving between distant patches is relatively low.

Thus, the only implementation of positive reinforcement for route segments to rewarded flowers, often does

not enable bees to explore all possible patches, so that the paths of competing bees overlap and interfere

within a subset of the available patches. Adding a negative reinforcement for route segments to unrewarded

flowers increases aversion for these flowers, the spatial segregation of foraging paths between competing

bees and the collective exploitation of all available patches, even if the initial probabilities of moving to

distant patches are low. This interplay between the influences of positive and negative experiences at flowers

on the spatial and competitive decisions of bees is in accordance with behavioral observations (Lihoreau *et al.*

2016; Pasquaretta *et al.* 2019).

The need of negative reinforcement rules to enhance discrimination between different options or

stimuli is well known in both learning theory and behavioral studies (Beshers and Fewell 2001; Garrison *et*

*al.* 2018; Kazakova *et al.* 2020). This is especially notable in collective decisions making by groups of

animals and robots (Sumpter 2010), where negative feedbacks enable individuals to make fast and flexible

decisions in response to changing environments (Robinson *et al.* 2005; Seeley *et al.* 2012). At the individual

level, negative experiences also modulate learning. For both honey bees and bumblebees, adding negative

reinforcement to a learning paradigm (e.g. quinine or salt in sucrose solution) enhances fine scale color

discrimination (Avarguès-Weber *et al.* 2010) and performances in cognitive tasks requiring learning of rules

of non-elemental associations (Giurfa 2004). The insect brain contains multiple distinct neuromodulatory

systems that independently modulate negative and positive reinforcement (Schwaerzel *et al.* 2003) and the

ability of bees to learn negative consequences is well-established (Vergoz *et al.* 2007). Even so, the utility of

negative reinforcement to enhance efficient route learning and the consequences of this for the emergence of

effective resource partitioning has not been commented on previously. It may be that this is a general

phenomenon with applicability to other resource partitioning systems.

Our study implies that some very simple learning and interaction rules are sufficient for trapline

formation and resource partitioning to emerge in bee populations. Several improvements of the model could

be considered for future theoretical and experimental investigations of bee spatial foraging movements and

interactions, for instance by implementing documented inter-individual variability in cognitive abilities and

spatial strategies of bees (Chittka *et al.* 2003; Raine and Chittka 2012; Klein *et al.* 2017), the variability in

the nutritional quality of resources (Wright *et al.* 2018*;* Hendriksma *et al.* 2019*)* and the specific needs of

each colony (Kraus *et al.* 2019), or the well-known ability of bees to use chemical (Leadbeater and Chittka

2005) and visual (Dunlap *et al.* 2016) social information to decide whether to visit or avoid flowers. For

instance, it is well-known that foragers of many species of bees leave chemical cues as footprints on the

flowers they have visited (bumblebees and honeybees: Stout and Goulson 2001; several species of solitary

bees: Yokoi and Fujisaki 2009). Bees learn to associate the presence or absence of a reward to these

footprints and to revisit or avoid scented flowers (Leadbeater and Chittka 2011). Such a pheromone system is

an advantageous signal for all participants in the interaction (Stout and Goulson 2001). Our model suggests

that this additional information could significantly enhance the negative value experienced by a bee thus

increasing resource partitioning to the benefit of all bees coexisting in the patch (Appendix S3), even of

different species that learn to use these cues (Stout and Goulson 2001; Dawson and Chittka 2013).

Our agent-based model thus builds on previous attempts to simulate trapline foraging by individual

bees (Lihoreau *et al.* 2012b, Reynolds *et al.* 2013; LeMoël *et al.* 2019) and fills a major gap of current

pollinator population dynamic models (Becher *et al.* 2014; 2016; 2018). As such, it constitutes a unique

theoretical modeling framework to explore the spatial foraging movements and interactions of bees in

ecologically relevant conditions within and between plant patches. This holds considerable promising tool to

guide novel experiments in a wide range of pollinators exhibiting routing behavior. It can readily be used to

test predictions with more than two bees (see examples Video S1 and Appendix S3), several colonies, or

even different species of bees (e.g. honey bees) and may be used to complement current predictions about

pollinator population dynamics (Becher *et al.* 2014; 2016; 2018). Ultimately, the robust predictions of the

spatial movements and interactions of bees over large spatio-temporal scales, through experimental

validations of the model, has the potential to help illuminate the influence of bees on plant reproduction

patterns and pollination efficiency (Ohashi and Thomson 2009).

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## Figure legends

**Figure 1.** Flowchart summarizing the agent-based models (1 and 2). Rectangles represent actions performed by a bee. Diamonds indicate conditional statements. Arrows connect the different modules. Colored rectangles describe the negative reinforcement rule specific to model 2. R code is available in GitLab: *https://gitlab.com/jgautrais/resourcepartitioninginbees/-/releases*

**Figure 2.** Comparisons of route qualities (A) and similarities (B) between simulations and experimental data for one forager (positive array of flowers as in Lihoreau *et al.* 2012b). Model 1: positive reinforcement only. Model 2: positive and negative reinforcements. For each dataset, we show the estimated average trends across foraging bouts (colored curves), along with their 95% CI (gray areas). For the sake of eye comparison, in the simulation plot we represent estimated 95% confidence intervals for a random subsample of 7 simulated bees (N = 7 bees in Lihoreau *et al.* 2012b). Average trends were estimated over 100 simulation runs, using GLMM Binomial model with bee identity as random effect (bee identity nested in simulation identity for simulated data).

**Figure 3.** Results of simulations with two foragers in environments with 10 flowers. Light blue: simulations with positive reinforcement only (model 1). Dark blue: simulations with positive and negative reinforcement (model 2). The x axis is the number of completed foraging bouts by the two foragers. The y axis represents respectively: A) the estimated mean frequency of visits to empty flowers; B) the estimated mean frequency of encounters on flowers; C) the similarity index $SI_{ab}$ between two successive flower visitation sequences; D) the index of resource partitioning $Q_{norm}$ (0: both bees visit the same set of flowers; 1: bees do not visit any flower in common); E) the collective foraging efficiency index $QL_{group}$. Average trends for each model are estimated across all types of environments (one patch, two patches and three patches; see Fig S2).

# Supplementary materials

**Appendix S1.** *Sensitivity analysis of positive and negative reinforcements.*

We ran a sensitivity analyses for the two main parameters: the positive and negative reinforcement. As we

had no a priori understanding of how the model behaved with different values of the two main parameters of

the model (positive and negative reinforcement), we explored the spectrum of potential outcomes with

different sets of parameters. We ran simulations on ranges of positive (1, 1.2, 1.4, 1.6, 1.8, 2) and negative (0,

0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1) reinforcement factors for a total of 66 sets of parameters, for each

environment type explored (one, two and three patches, Fig. S2). We simulated 10 environments for each

environment type and computed 100 simulations of 50 foraging bouts per iteration (i.e. 1000 simulations per

environment type and set of parameters).

Since our observations focused on resource partitioning, we extracted the $Q_{norm}$ index values for

these simulations and compared them. We plotted a heatmap showing the value of the mean $Q_{norm}$ index at

the last foraging bout for each set of parameters and environment type (Fig. S3). In all types of environments,

the positive reinforcement has a strong effect on the final $Q_{norm}$ index value. High values of resource parti-

tioning are obtained for positive reinforcement values > 1.5. For the negative reinforcement factor, however,

it appears that high values of resource partitioning were obtained for negative reinforcement values larger

than 0.75. Negative reinforcement has little to no impact on the environment type with only one patch.

We also looked at how this same index evolved over successive foraging bouts, for each pair of

bees. Fig. S4 shows the dynamics of mean $Q_{norm}$ index across 50 foraging bouts for each combination of

positive reinforcement (1.0, 1.2, 1.4, 1.6, 1.8, 2.0) and negative reinforcement (0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6,

0.7, 0.8, 0.9, 1) parameters, and each environment type (one patch, two patches, three patches). Higher val-

ues of both positive and negative reinforcement factors most often lead to faster resource partitioning (with

some uncertainty due to the probabilistic nature of the model). Combinations of values in which the negative

reinforcement factor is missing (violet gradient curves) led to a decrease in partitioning.

**Appendix S2.** *Qualitative analysis for the negative array case.*

We ran simulations with one forager to compare model outcomes to observational data using a second

reference field study (Woodgate *et al.* 2017). In this study, the authors used a 'negative array' (narrow

pentagon, Fig. S1B) in which the distance between flowers and the directionality of movement were

negatively linked, i.e. moving between nearest neighbor flowers required bees to make sharp deviations

between consecutive vectors. Four bumblebees were tested during 27 to 61 foraging bouts each (flower

visitation sequences were provided by Joe Woodgate). One of these bumblebees was tested over different

days and was therefore removed from the analyses. In these conditions, none of the bumblebees developed a

stable trapline, although all individuals significantly increased their foraging efficiency with time (e.g.

reduced travel distance and duration, increased similarity between two consecutive flower visitation

sequences).

667           The addition of a negative reinforcement had no major effect on route quality nor on route

similarity trends (Fig. S5). Model simulations showed good qualitative fit the traplining behavior observed in

real bees exploiting a negative array of flowers – i.e. there is a trend of increasing route similarities across

foraging bouts. Note however that the model tends to overestimate the bee ability to develop stable routes in

arrays of flowers where proximity and directionality are negatively linked (Woodgate *et al.* 2017). This

imperfect match could be due to the low amount of available experimental data (three individuals in

Woodgate *et al.* 2017). Alternately, the model does not integrate any kind of stochastic exploration so that at

each new step, bees do not provide the possibility to choose unknown spatial targets. Real bees, on the

contrary, show phases of stochastic explorations during and after trapline formation (Woodgate *et al.* 2017;

Kembro *et al.* 2019). Future experiments with more bees in a larger diversity of arrays of flowers will be

useful to further quantitatively calibrate the model.

**Appendix S3.** *Predictions with more than two bees.*

Here we explored the emergence of resource partitioning in groups of 5 bees, and how this varies as a

consequence of number of available flowers and number of foraging bees in environments of 20, 25, 30, 40,

50, 70 and 100 flowers, thus encompassing a gradient of competition pressures from conditions where there

is not enough flowers for all bees (20) to conditions where there is four times more flowers than necessary

for all bees (100). For simplicity, in all these environments, flowers were evenly distributed (i.e. environment

with one patch). The positive reinforcement factor was set at 1.5, and the negative reinforcement factor was

set at 0.75. For each flower density, we generated 10 environments, and ran 100 simulations of 100 foraging

bouts, for a total of 1000 simulations per density value. We extracted the resource partitioning index ($Q_{norm}$)

at each foraging bout. Unsurprisingly, the mean final $Q_{norm}$ was higher in environments with most flowers

(Fig. S7). Plotting the mean final $Q_{norm}$ (final foraging bout) as a function of the number of available

flowers confirms that bees converge to a plateau where increasing the number of flowers only provokes

increase of partitioning (i.e. around 50 flowers) (Fig. S7).

**Figure S1.** Arrays of artificial flowers for the experimental dataset. A. 'Positive array' (regular pentagon) in

which the distance between flowers and the directionality of movement are positively linked, i.e. nearest

neighbor flowers can be linked using lowest angular deviation between consecutive vectors. Modified from

Lihoreau *et al.* (2012b). B. 'negative array' (narrow pentagon) in which the distance between flowers and the

directionality of movement are negatively linked, i.e. moving between nearest neighbor flowers requires bees

to make sharp deviations between consecutive vectors. Modified from Woodgate *et al.* (2017)

**Figure S2.** Examples of simulated environments. Distribution of 10 flowers (gray circles) and a nest (black

pentagon) in three environments defined by different levels of resource patchiness. A flower patch was

characterized by: 1) a uniform distribution of flowers, 2) a lower distance between flowers within the patch

than between all flowers from different patches.

**Figure S3** Heatmap showing the mean $Q_{norm}$ Index value after 50 foraging bouts (mean over 1000 simula-

tions on 10 arrays of the same environment type), for each combination of positive reinforcement (1.0, 1.2,

1.4, 1.6, 1.8, 2.0) and negative reinforcement (0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1) parameters, and

for each environment type (one patch, two patches, three patches). For simplicity we inverted the values of

negative reinforcement here. 0 being models without negative reinforcement.

**Figure S4.** Dynamic of the mean $Q_{norm}$ Index across foraging bouts for each combination of positive (1.0,

1.2, 1.4, 1.6, 1.8, 2.0) and negative (0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1) reinforcement factors and

for each environment type (one patch, two patches, three patches). For simplicity we inverted the values of

negative reinforcement here. 0 being models without negative reinforcement.

**Figure S5.** Qualitative comparisons of route qualities (A) and similarities (B) between simulations and

experimental data (negative array of flowers as in Woodgate *et al.* 2017) for one forager. Light blue:

simulations with positive reinforcement only (model 1). Dark blue: simulations with positive and negative

reinforcement (model 2). For each dataset, we show the estimated average trends across foraging bouts

(colored curves), along with their 95% CI (gray areas). For simplicity, in the simulation plot we only

represent a subsample of three random bees with their estimated 95% CI. Average trends were estimated

using GLMM Binomial model with bee identity as random effect (bee identity nested in simulation identity

for simulated data).

**Figure S6.** Boxplot representing the distribution of the initial probabilities of visiting each flower in different

environments (one patch with uniformly distributed flowers; two patches with five uniformly distributed

flowers per patch; three patches of five, three and two uniformly distributed flowers; see examples Fig. S1).

Median (solid horizontal line), first and third quartiles (box) and maximum and minimum values are

represented.

**Figure S7.** Evolution of the mean final $Q_{norm}$ index (after 100 foraging bouts) as a function of increase

resources availability. The model run has the positive reinforcement factor set at 1.5, and the negative rein-

forcement factor set at 0.75 with 5 bees in environments of one patch.

**Video S1.** Example of simulation of five bees foraging in an environment with one patch of 50 flowers. Both

positive and negative reinforcement rules are implemented (model 2). Bees performed 100 foraging bouts.

760    **Figure 1**

762 **Figure 2**

773 **Figure 3**

782 **Figure S1**

## A. Lihoreau et al. 2012b

Coordinate Y

Coordinate X

## Positive array

## B. Woodgate et al. 2017

Coordinate Y

Coordinate X

## Negative array

797    *

798    **Figure S2**

801    **Figure S3**

803    **Figure S4**

814 **Figure S5**

825 **Figure S6**

835    **Figure S7**

836