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Long-term stability of avalanche scaling and integrative network organization in prefrontal and premotor cortex

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Pages/Figures: 6 figures, 4 tables

Running Head: Long-term stability in avalanches and integrative networks

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Keywords: nonhuman primate, resting activity, criticality, brain dynamics, neuronal avalanches, integrative network organization

Abstract

Ongoing neuronal activity in the cortex establishes functional networks of synchronization that reflect normal and pathological brain function. The reconstruction of these networks typically suffers from the use of indirect measures of neuronal activity at low spatiotemporal resolution and a lack of longitudinal tracking. Accordingly, the precise nature of the underlying synchronization dynamics and its translation into robust graph theoretical markers are not well characterized. Here, we studied the stability of cortical dynamics and reconstructed functional networks over many weeks in prefrontal and premotor cortex of awake nonhuman primates. We monitored neuronal population activity directly in the ongoing local field potential (LFP) at high spatial and temporal resolution using chronically implanted high-density microelectrode arrays. Ongoing activity was composed of neuronal avalanches exhibiting stable, inverted parabolic profiles with the collapse exponent of 2 in line with a critical branching process. Avalanche-based functional networks, reconstructed using a Normalized Count estimator, revealed robust integrative properties characterized by high neighborhood overlap between strongly connected nodes and robustness to weak-link pruning. "Entropy of mixing" analysis demonstrated progressive link reorganization over weeks. The long-term stability of avalanche scaling and integrative network organization should support the development of robust biomarkers to characterize normal and abnormal brain function.

Introduction

Ongoing neuronal activity in the mammalian brain gives rise to distinct functional networks that

reflect normal and pathological brain function (Bullmore and Sporns, 2009; Fox and Raichle,

2007; Raichle, 2015). Empirical measures of these networks, however, are often limited in the

precision with which they reflect the organization of neuronal population activity and a lack of

longitudinal follow-up. Networks are either reconstructed from indirect non-neuronal activity at

low temporal resolution using functional magnetic resonance imaging (fMRI), or via more direct

neuronal activity measures such as magnetoencephalography (MEG) and the

electroencephalogram (EEG) which suffer predominantly from low spatial resolution (Bassett

and Sporns, 2017). Accordingly, there is limited knowledge about the stability and nature of the

spatiotemporal dynamics and corresponding functional connectivity of local neuronal

populations that give rise to fluctuations in ongoing cortical activity.

In contrast to macroscopic and indirect methods, neuronal activity measured at single-cell

resolution could in principle allow for precise and robust spatiotemporal reconstruction of

functional networks in cortex. For example, in macaque cortex single-unit activity can be

recorded over many weeks (Nicolelis et al., 2003) and identifies firing statistics of neurons over

days (Dickey et al., 2009; Jackson and Fetz, 2007). Advanced approaches may involve tetrodes,

automated classifiers (Tolias et al., 2007) or second order statistics as classifiers (Fraser and

Schwartz, 2011). Even advanced single-unit approaches, however, limit robust tracking of

activity to small groups of individual neurons. Chronic expression of genetically-encoded

calcium indicators (GECIs) can increase the neuronal count and identify orientation-selective

neurons over months (Li et al., 2017), yet at low temporal resolution. The local field potential

(LFP), alternatively, provides access to an intermediate spatial resolution of cortical activity that

is between the macroscopic scale of fMRI, MEG and EEG and single cell accuracy. It robustly

measures local neuronal population activity with high temporal and reasonable spatial resolution

of several hundred micrometers (e.g. (Bellay et al., 2021; Katzner et al., 2009)) over many

weeks. In nonhuman primates (NHPs), the LFP has been shown to correlate well with local unit-

activity (Donoghue et al., 1998; Petermann et al., 2009; Rasch et al., 2008) and offers robust

brain-machine interface performance (Mehring et al., 2003).

It is now well established that the ongoing LFP in superficial layers of nonhuman

primates organizes into spatiotemporal activity clusters whose sizes and durations distribute

according to power laws (Miller et al., 2019; Shew et al., 2009; Yu et al., 2017), the hallmark of

neuronal avalanches (Beggs and Plenz, 2003). The spatiotemporal correlations underlying

neuronal avalanches give rise to functional "integrative" networks, in which the topology and

weights of links organize such that end-nodes of strong links are more likely to have many

common neighbors, as quantified by a high correlation between the link weight and the link

clustering coefficient ((Pajevic and Plenz, 2012), *cf.* edge-clustering coefficient in (Radicchi et

al., 2004)), while being robust to the loss of weak links, in terms of maintaining the advantages

of a small-world topology (Watts and Strogatz, 1998). This specific arrangement describes many

complex networks ranging from genetic networks to social, i.e. "friendship", networks (Pajevic

and Plenz, 2012). Importantly, integrative networks can form using local plasticity rules that

operate on neuronal avalanches (Alstott et al., 2015) in which weak links provide a large basin

for plastic changes as they can be removed or rewired, permitting flexibility, while preserving

the small-world network property. The stability over days and weeks of cortical avalanche

dynamics and corresponding integrative networks has not been explored for cortex. Size and

duration distributions of avalanches do not consider the spatiotemporal organization of

avalanches, thus multiple functional connectivities could give rise to similar power law statistics.

Likewise, integrative networks allow for the reorganization of individual links while maintaining

global integrative properties (Pajevic and Plenz, 2012).

Here we recorded ongoing LFP activity in prefrontal and premotor cortex of NHPs over

weeks using chronically implanted high-density microelectrode arrays. We demonstrate stable

avalanche dynamics with power law statistics, the temporal avalanche profile of an inverted

parabola and corresponding scaling exponent of 2, which is the expected value for critical

branching process dynamics (di Santo et al., 2017; Miller et al., 2019; Sethna et al., 2001). We

further demonstrate that these avalanches give rise to non-trivial integrative functional networks

despite progressive reorganization of the link strengths as identified using Normalized Count

(NC) estimators (Pajevic and Plenz, 2009) and the "entropy of mixing" analysis (see Material

and Methods). Our results suggest that avalanche dynamics and corresponding integrative

network organization identify a robust cortical state in the adult brain, which should inform

dynamical models of brain function and might allow for the early identification of pathological

brain states.

Results

81   The spatiotemporal organization of the ongoing LFP (1 – 100 Hz) was monitored with

82   chronically implanted high-density microelectrode arrays (~10 x 10 electrodes; interelectrode

83   distance 400 µm) in premotor (PM, n = 2 arrays) and prefrontal cortex (PF, n = 4 arrays) of three

84   macaque monkeys (*Macaca mulatta*; K, V, N; Fig. 1A, B). The animals were awake and seated

85   in a monkey chair during the recording sessions but were not given any specific stimulus or task.

Figure 1: Ongoing cortical dynamics are stable over weeks in superficial layers assessed by pairwise correlations in the LFP. A, Sketch of chronic prefrontal (*PF*) and premotor (*PM*) cortical implantation sites (*red diamonds*) for high-density microelectrode arrays. **B,** Example of simultaneously recorded ongoing LFP (1 – 100 Hz) at single electrodes with correlated activity. **C,** Overview of ~30 min recording sessions per day (*color coded circles*) over several weeks for each NHP. **D, E,** Pair-wise correlations of the continuous LFP distribute similar over time. Normalized histogram of pairwise correlations between all functioning channels for each recording day (*color bar*) in two NHPs (*left*: prefrontal recording in K; *right*: premotor recordings in N). **F, G**, The average correlation, *<R>* (from *D*, *E*), was constant over weeks in PF (*left*) and PM (*right*) arrays.

On average about 4 ± 2 hr of LFP activity during 9 ± 7 recording sessions over the course of $5 \pm$

4 weeks were analyzed per monkey (85 ± 8 electrodes/array; Fig. 1C).

Stability of average pairwise correlation and avalanche dynamics in prefrontal and premotor

cortex

The pairwise Pearson's correlation, R, is a standard measure to quantify the correlation in

neuronal activity between distant cortical sites. We found that for the continuous LFP, the

distribution of R, obtained from ~5,000 electrode comparisons per array, was broad yet similar

across days (Fig. 1D, E). The average correlation, $<R>$, while different between arrays, was

constant over many days and weeks (Fig. 1F, G; linear regression fit of 0.4 ± 0.7 x10^{-2} for all

arrays; see Table 1 for individual arrays).

We next explored the stability of neuronal avalanche dynamics by discretizing the LFP

from ongoing activity in the NHPs (Petermann et al., 2009; Yu et al., 2017). We previously

demonstrated that negative deflections in the continuous LFP signal (nLFPs) track the local

neuronal population activity and correlate with extracellular unit firing (Bellay et al., 2021;

Petermann et al., 2009). Accordingly, discrete nLFPs were defined by crossing a threshold of -2

SD and extracting their peak times (Fig. 2A). nLFPs were then grouped into avalanches at

temporal resolution Δt of the mean time interval of successive nLFPs on the full array, $<IEI>$,

which ranged between $3 - 4$ ms (Fig. 2B; see Material and Methods). We found that the

probability density distribution of avalanche size, which typically ranges from size 1 to the

number of electrodes for each array (Yu et al., 2011), exhibited power laws for each day of

recording (Fig. 2C, D; $\Delta t = <IEI>$, truncated power law vs. exponential, LLR $\gg 1$, $p < 0.005$; or

vs. log-normal, LLR$\gg 1$, $p < 0.005$; constant across all recording days). The stability of the

Figure 2: Neuronal avalanche dynamics is stable over weeks in frontal cortex of NHPs. A,

Sample ongoing LFP at single electrode. A negative threshold (*dashed line*) is applied to identify

significant negative deflections from the mean (nLFPs, *red asterisks*). **B,** Schematic nLFP raster at Δt

$= \langle IEI \rangle$ showing neuronal avalanches identified as concurrent or consecutive nLFPs on the array

separated by at least one empty time bin. Two avalanches (*gray*) of size 3 and 6 are identified. **C, D,**

Power law in size S for nLFP avalanches for all recordings (*color bar*) in two NHP ($\Delta t = \langle IEI \rangle$).

Broken line: power law with slope -3/2 as visual guide. *Color bar*: Recording day. Size distributions

remain power laws for all days (LLR values > 0 significant; vs. exponential distribution; see also

Table 1). **E, F,** Stability of slope α as a function of time (*color coded*).

power law in size was associated with an average slope $\alpha = 1.32 \pm 0.05$ for all arrays (Table 1),

which is close to the expectations for the size exponent of a critical branching process (Fig. 2E,

F) (Harris, 1963). These results demonstrate the presence of avalanche dynamics in all NHPs for

up to 2 weeks in PM and up to 10 weeks in PF.

Long-term stability in the temporal profile of avalanches and corresponding scaling collapse

The temporal profile of a neuronal avalanche describes how avalanches unfold in time by

initiating locally, growing in magnitude, and eventually contracting spatially before ending.

Recent work (Miller et al., 2019) confirmed the prediction that the temporal profile of neuronal

avalanches obeys the characteristic motif of an inverted parabola and that empirically-observed

mean avalanche profiles collapse onto this scale-invariant motif regardless of avalanche duration.

For this analysis, the temporal resolutions were set to $\Delta t = 1$ ms and $\Delta t = 30$ ms respectively,

which demonstrated stable power law size distributions and expected change in slope α (Table

1; 1 ms: all LLR $> 10^4$, all p $<< 0.005$; 30 ms: all LLR > 10, all p $<< 0.005$) as reported

previously (Beggs and Plenz, 2003; Petermann et al., 2009). These resolutions allow for the

collapse of temporal avalanche profiles in the presence of transient γ–oscillations in ongoing PF

and PM activity of NHPs (Miller et al., 2019).

We explored the stability of these scaling predictions over time, finding that the

characteristic motif for mean profiles of avalanche lifetime, L, with $L = 3\Delta t - 5\Delta t$ did trace

inverted parabolas for fine ($\Delta t = 1$ ms, Fig. 3A, B,) and coarse ($\Delta t = 30$ ms, Fig. 3C, D) temporal

resolutions (for statistical comparison see Table 2 for individual arrays). Importantly, the scaling

exponent χ producing these parabolic, collapsed motifs was close to the value of 2 expected for a

critical branching process (di Santo et al., 2017; Miller et al., 2019; Sethna et al., 2001) and did

Figure 3: Collapse in the temporal profiles of neuronal avalanches and corresponding scaling exponent χ = 2 are stable over weeks in frontal cortex. A, Collapse in the temporal profile of avalanches at Δ*t* = 1 ms. Best collapse per recording day (*color bar*) for K-PF1 (*left*) and N-PM (*middle*). Rightmost column summarizes the normalized collapse motif (*norm.*) averaged across days for each NHP and cortical area. Shaded region indicates mean ± standard error per array within line thickness. **B,** The scaling exponent χ at which the best temporal profile collapse is obtained remains close to the theoretical value of 2 predicted for a critical branching process for all recording sessions. **C, D** Same as in *A, B* but at Δ*t* = 30 ms demonstrating the characteristic parabolic profile for coarse-grained temporal scale. **E,** Same as in *A – D*, but nLFP events have been shuffled in time to remove spatial and temporal correlations. Note that the characteristic profile no longer traces a parabola as expected for critical dynamics. **F,** The scaling exponent χ is close to 1 when correlations are destroyed.

not change over time (Fig. 3B, D; for $\Delta t = 1$ ms, $\chi = 1.93 \pm 0.14$, linear regression fit of $1*10^{-2} \pm$

0.2; for $\Delta t = 30$ ms, $\chi = 2.01 \pm 0.24$, linear regression slope of $2*10^{-2} \pm 0.04$; Table 3 for

individual arrays). In contrast, time-shuffled data reliably produced flattened motifs (Fig. 3E, F)

with a scaling exponent close to 1, as found for non-critical dynamics, in which sizes grow

linearly with duration (Villegas et al., 2019).

Persistence of integrative global network properties

In order to quantify in more detail the spatiotemporal correlations underlying persistent

avalanche activity, we reconstructed functional networks from neuronal avalanches using the NC

reconstruction (Pajevic and Plenz, 2009). This method uses a shortcut to Bayesian estimation of

network connections, making it approximate, but also computationally efficient, and hence

applicable to reconstructing relatively large networks from lengthy event train recordings (Fig.

4A). It also reduces the influence of indirect common input correlations and has been found in

simulations to accurately and efficiently reconstruct the directed networks and weights from

simulated point-process dynamics (Pajevic and Plenz, 2009). An example of the directed

connectivity matrix for a single recording session derived from spontaneous avalanche activity is

shown in Figure 4B. We found that for all arrays and recording sessions, the weights of the

directed functional connections were not particularly heavy-tailed and distributed between an

exponential and lognormal function over more than 3 orders of magnitude (Fig. 4C – E).

Having reconstructed the directed, weighted links in our avalanche-derived functional

networks, we proceeded to calculate several graph theoretical properties. Integrative networks

are characterized by a positive correlation, R_{CL}, between the link cluster coefficient, C_L, and the

corresponding link weight, w, between two nodes (Fig. 5A; (Pajevic and Plenz, 2012)). This

Figure 4: NC reconstruction of directed functional connectivity from ongoing LFPs reveals stable exponential distributions in link weights across time for all NHPs. A, Sketch of the NC algorithm. Active nodes (*filled circles*) at time Δt_{i-1} are evaluated regarding all existing prior probabilities (*solid arrows*) to obtain the pattern of active and inactive nodes at the next time step Δt_i (for details see (Pajevic and Plenz, 2009)). **B**, NC reconstructed network based on 15 minutes of nLFP activity at $\Delta t = 1$ ms from K-PF1 produces an adjacency matrix of weights w_{ij} showing sparse and mostly local functional connectivity. **C,** Normalized distributions in directed link strength for all recording days (*left*, K-PF1; *right*, N-PM). *Color bar*: recording day. **D,** Normalized probability distribution trends were consistent across areas and NHPs. Average distribution over all recording days. *Color code*: NHP-area. **E**, LLR (*open circles*) and *p* values (*asterisks*) for exponential vs. log-normal comparison of daily weight distributions (e.g. *C*) for all arrays and days (color code as in *D*).

positive correlation demonstrates that strongly connected nodes have more common neighbors

compared to weakly connected nodes (Fig. 5B). We employed degree-sequence preserved

randomization to subtract potential contributions to link clustering from the node degree

distribution and report here the resulting excess link clustering, ΔC_L (see Material and Methods).

The monotonic increase in ΔC_L with lowest-to-highest weight rank (Fig. 5C) clearly identifies

integrative functional network organization in both PM and PF that was stable over time (Fig.

5D; linear regression slope of $5 \pm 10 \times 10^{-3}$; 95% confidence limit; see Table 4 for individual

arrays).

Pruning analysis is an efficient approach to study the weight organization of networks

(Onnela et al., 2007; Pajevic and Plenz, 2009). We found that pruning from the bottom, i.e.

pruning weakest links progressively, had negligible effect on the network clustering properties.

This was evidenced by a near constant value of the excess node clustering, $\Delta C,$ until the vast

majority (80 – 90%, Fig. 5E; solid lines) of links were removed. In contrast, pruning from the

top, i.e. removing the strongest links first, rapidly decreased ΔC, a result consistently found for

all NHPs (Fig. 5E). We conclude that the integrative property arises from a "backbone" of strong

links that is robust to weak-link pruning, yet quickly degrades when strong links are removed.

Entropy of mixing identifies link progression over many weeks

Given the stability observed over weeks in the global network dynamics, i.e., $<R>$, α, χ, and

integrative network organization, i.e., R_{CL}, we next sought to analyze in more detail the stability

at the local level of individual link weights. Specifically, we examined whether the stability

identified at the global level simply arises from stability at the local level. To quantify changes at

the local level, we categorize the links, e.g., weak, medium, and strong, and analyze whether

Figure 5: Link-clustering analysis reveals that integrative global network properties are stable over time. A, Schematic clustering diagram depicting two nodes (*blue*) connected by a link with weight w_{ij}. In an integrative network, the proportion of common neighbors (*red*) is expected to positively correlate with w_{ij}. **B,** Sketch of two subnetworks with low and high link clustering C_L respectively. **C,** The excess link clustering ΔC_L (see Methods) increases with link strength in all prefrontal (*left*) and premotor (*right*) cortical arrays (*color coded*; NHP-area). **D,** Analysis of cortical networks showed strongly positive R_{CL} over all recording sessions for up to 73 days. **E,** Link-pruning analysis of excess node clustering ΔC calculated via degree-sequence preserved randomization (Pajevic and Plenz, 2012) showed that the integrative clustering motif was robust to weak-link pruning (*solid lines*; error bars denote mean ± SD over all recordings for an array), while the clustering "backbone" of the network quickly degraded when strong links were pruned first (*dotted lines*; *color code* as in *D*). C – E, Δt = 1 ms.

links switch between categories over time, e.g., from weak to medium or vice versa. As a

measure of mixing, we calculate the entropy of mixing, H_M, (see Methods). Two main factors

contribute to potential changes in H_M, which originate from changes in link categories in a

network from one day to another. First, independent random changes on each day will result in

increased mixing and H_M, but not progressively over time. For example, errors in network

reconstruction alone will result in a constant H_M over many days if the underlying network is not

changing. Second, link weights could gradually evolve over days and weeks, and potentially

change their categories, which is now progressively mixed and therefore is expected to lead to a

monotonic increase in H_M until the maximum in mixing is reached. Because reconstruction errors

are higher for weak links compared to strong links, we quantified potential changes in link

weight from NC reconstructed networks separately for the strongest (top 50%) and weakest

(bottom 50%) links. This separation is also motivated by our results for top- vs. bottom-pruning,

which demonstrated that networks are less robust to link changes in the top half of the link

weight distribution. For each half, we partitioned link weights further into strength quintiles,

yielding 5 categories, and then studied whether members from different categories will mix over

time. In figure 6, we show the data for the top half and bottom half and compare those curves to

H_M obtained if the category labels were fully randomized at each step and also present the

theoretical maximum for H_M (see also Material and Methods). Because all successive

distributions used the link labels derived from Day 1 (making $H_M = 0$), the average entropy of

mixing was plotted beginning from the second recording for each NHP. For all arrays, we found

that H_M for the bottom half of links reaches close to the maximal entropy by the following day

demonstrating that weak links fluctuate randomly. On the other hand, we found

Figure 6: Entropy of mixing analysis demonstrates progressive changes in strong links over time for some networks. Entropy of mixing (H_M) analysis of the link weights obtained with NC reconstructions from $\Delta t = 1$ ms raster recordings. H_M is plotted for the "top" half (strongest 50% of links; *black curves*) and "bottom" half (weakest 50% of links; *green curves*) versus the days after the initial recording. The black and green dashed lines indicate corresponding H_M obtained when the labels were fully randomized, while the red dashed line indicates the theoretical maximum of H_M. The six panels represent six different arrays from the three monkeys shown in two rows. **A**, Arrays for which statistically significant progression of mixing was obtained for "top" links. **B**, Arrays for which no statistically significant progression was observed. The "top" half of the links consistently showed lower H_M than the "bottom" half of the links, which is mainly due to the smaller reconstruction error. The Day 1 points are not plotted because, by default of our labeling, the initial value for H_M is zero.

202   progressive and statistically significant increases of H_M over subsequent days for strong links in

203   three out of six arrays (Figure 6A, B; see Table 4). These findings demonstrate stability in

204   avalanche dynamics and integrative network organization even though the network undergoes

205   significant weight reorganization at the individual link level.

Discussion

Fluctuations in ongoing neuronal activity give rise to functional networks that allow for the

categorization of healthy and pathological brain states (Bullmore and Sporns, 2009; Fox and

Raichle, 2007; Raichle, 2015), yet, the dynamical and graph theoretical markers underlying these

ongoing fluctuations have been challenging to identify. By recording the LFP in prefrontal and

premotor cortex of NHPs over weeks at high spatiotemporal resolution, we established two

robust markers of ongoing activity; the dynamical category of neuronal avalanches and the graph

theoretical category of integrative networks. Avalanche dynamics revealed power law statistics,

parabolic temporal profiles and a scaling exponent of 2 in support of critical branching process

dynamics (di Santo et al., 2017; Miller et al., 2019; Sethna et al., 2001). We further demonstrate

that avalanches form integrative networks despite reorganization of individual link weights as

identified using NC estimators and an entropy of mixing approach (Onnela et al., 2007; Pajevic

and Plenz, 2009, 2012). Our results suggest that avalanche dynamics and corresponding

integrative networks identify a robust state of the awake frontal cortex. This work should be

impactful for computational studies of cortex function and for translational research into the

identification of brain dynamics in healthy subjects and corresponding deviation in brain

disorders.

Recent analysis of evoked cortical activity in nonhuman primates during behavior

demonstrated the preservation of neuronal avalanche dynamics in the face of transient activity

changes, specifically the nLFP rate (Yu et al., 2017). Given the robustness of integrative network

properties observed in combination with avalanche dynamics *in vitro* (Pajevic and Plenz, 2009,

2012) as well as *in vivo* (the present study), we would expect integrative networks properties to

also persist during behavioral tasks.

Stability of LFP based avalanches and relation to neuronal activity

Technical advances in identifying long-term robustness in neuronal activity using cellular

resolution approaches (Dickey et al., 2009; Fraser and Schwartz, 2011; Jackson and Fetz, 2007;

Li et al., 2017; Nicolelis et al., 2003; Tolias et al., 2007) typically suffer from spatial and

temporal subsampling (Levina and Priesemann, 2017; Petermann et al., 2009; Ribeiro et al.,

2010; Ribeiro et al., 2014) limiting proper identification of avalanche dynamics and

corresponding reconstruction of functional connectivity. The LFP, on the other hand, is a robust

neuronal population signal, less prone to spatial subsampling and at high temporal resolution

contains local spike information particularly when recorded from superficial layers (Donoghue et

al., 1998; Mehring et al., 2003; Petermann et al., 2009; Rasch et al., 2008). Indeed, we recently

demonstrated in nonhuman primates and *in vitro* slices that single neurons selectively participate

in expansive, repeated LFP avalanches (Bellay et al., 2021), which suggest that the stability

observed in the present study for LFP-based avalanches might extend to the single neuron level.

Experimental manipulations support a homeostatic regulation of avalanche dynamics in

cortex. Transient pharmacological perturbation *in vitro* (Plenz, 2012) or sensory deprivation *in*

vivo (Ma et al., 2019) initially abolishes avalanche dynamics, which is followed by a recovery

over several days. Developmental findings further support an autonomous regulation of neuronal

avalanches in isolated cortex *in vitro* in the absence of sensory input (Pasquale et al., 2008;

Stewart and Plenz, 2007; Tetzlaff et al., 2010). Identifying the homeostatic regulation of

avalanche dynamics and integrative networks will require precise perturbation approaches

(Chialvo et al., 2020) in combination with advanced cellular techniques suitable for long-term

monitoring such as ratiometric genetically-encoded calcium indicators (GECIs), which naturally

compensate for cell-intrinsic expression variability (Lutcke et al., 2013).

NC reconstruction of integrative networks

Reconstruction of our directed, weighted functional networks utilized a Bayesian-derived NC

approach, which is easily scalable to large networks (Pajevic and Plenz, 2009, 2012) and reduces

correlations from common input. Network simulations demonstrated ground-truth reconstruction

for various small-world topologies from subcritical, supercritical and critical dynamics, the latter

in line with reconstructions from observed avalanche activity (Pajevic and Plenz, 2009).

Here we used significant events in LFP fluctuations, i.e. nLFPs, for the reconstruction of

functional connectivity, which differs from the more common ansatz based on continuous

timeseries. Accordingly, our approach, which selectively reconstructs synchronization dynamics

in the form of avalanches, introduces a time scale Δt to which the NC reconstruction is sensitive.

In order to identify the spatiotemporal spread of avalanches, the use of a microelectrode array

introduces a spatial discretization, which consequently enforces a discretization Δt in time. It was

found empirically that Δt should be linked to the average propagation velocity of neuronal

activity in the network, allowing Δt to be approximated by <IEI> (Beggs and Plenz, 2003;

Petermann et al., 2009). For Δt smaller than < IEI>, errors of prematurely terminating avalanches

increase, whereas errors of concatenating successive avalanches increase for Δt larger than

<IEI>. An approximate balance regarding these two errors is struck for Δt = IEI. With respect to

NC reconstruction, increasing Δt will increase the count in nLFP occurrences on the array per

time step, resulting in an increase in the computational load and increased error in estimating

priors for potentially activated links. Accordingly, we chose a Δt slightly smaller than IEI for a

conservative and balanced estimate of the functional connectivity based on avalanche

propagation.

Integrative networks differ from networks in which the weight is positively correlated

with the node degree (Barrat et al., 2004; Bianconi, 2005; Pajevic and Plenz, 2012). Our

shuffling correction further demonstrates that the organization of weighted links in integrative

networks cannot be simply explained by the link-degree distribution and in which strong links

are part of a continuous, in our case near exponential distribution (*cf*. Fig. 4D). Integrated

networks are also not a simple consequence of critical branching processes generating

avalanches, which can be realized in many topologies and architectures (Pajevic and Plenz, 2009,

2012).

Robust avalanche scaling of χ = 2 over many weeks

Heterogeneous activity in the form of neuronal avalanches has been the hallmark of ongoing

(Beggs and Plenz, 2003; Bellay et al., 2015) and evoked (Yu et al., 2017) brain activity in

superficial layers of the cerebral cortex. The scale-invariant hallmark of avalanches has been

found to capture ongoing neuronal activity in nonhuman primates at the mesoscopic level in the

LFP (Klaus et al., 2011; Petermann et al., 2009; Yu et al., 2014; Yu et al., 2017; Yu et al., 2011)

and macroscopic activity measured with EEG (Meisel et al., 2013), MEG (Shriki et al., 2013)

and fMRI (Fraiman and Chialvo, 2012; Tagliazucchi et al., 2012). The observed power law

distributions in cluster size and duration support the idea that the cortex operates close to a

critical state at which networks gain numerous advantages in information processing (Beggs and

Plenz, 2003; Gautam et al., 2015; Kinouchi and Copelli, 2006; Shew et al., 2009; Shew et al.,

2011; Yang et al., 2012).

Our present demonstration of an inverted-parabolic avalanche shape, collapse exponent

of 2 and size distribution slope >-2 is in line with predictions that the unfolding of avalanches in

the adult brain is governed by a critical branching process (for details see (Miller et al., 2019)).

This profile demonstrates that the initial spatial unfolding of an avalanche in time is truly

expansive and should not be viewed as being dominated by a few strong links. Recently,

avalanches with a scaling factor of 2 have been described for whole-brain neuronal activity in the

zebrafish larvae (Ponce-Alvarez et al., 2018), however, the corresponding size and duration

exponent were significantly steeper compared to reports for the mammalian cortex, suggesting a

different dynamical model for the zebrafish.

Connectome analyses on a time scale of seconds have identified transient fluctuations in

functional connectivity reflecting distinct states (Hutchison et al., 2013; Liu and Duyn, 2013;

Zalesky et al., 2014), which based on computational modeling were found to be intermittent, a

signature of metastability (Deco et al., 2017; Hansen et al., 2015). Because our analysis was

based on nLFPs and not continuous time signals, we were unable to obtain NC reconstructed

networks for shorter time periods than 15 – 30 min. In fact, our entropy of mixing analysis

allowed for an assessment of link weight progression in the face of reconstruction errors due to

limited data availability. Transient fluctuations in functional connectivity estimates are not in

contrast to the reorganization of links reported in our study. Short-term fluctuations in the face of

long-term stability are hallmarks of critical dynamics (Fraiman and Chialvo, 2012; Tagliazucchi

et al., 2012).

Potential advantages of avalanche dynamics and integrative networks for cortex function

Anatomically, the mammalian cortex is a sheet of local, functional modules that dynamically

combine to support complex brain functions (Braitenberg and Schüz, 1991; Honey et al., 2007).

Local connectivity ensures diverse local operations whereas long-range connections support

global coordination (e.g. (Bullmore and Sporns, 2009; Kirst et al., 2016)). These structural

hallmarks are dynamically realized in neuronal avalanches, which support a scale-free and

selective organization of neuronal synchronization over all distances. They are graph

theoretically embedded in integrative networks, which maintain a high level of node clustering

until about 90% of the strongest links are pruned, i.e. about 10% of strong links are used for

long-range connections. Intriguingly, simulations identified a particular local learning rule that

operates on activity cascades such as avalanches to build integrative networks from random

networks (Pajevic and Plenz, 2012). The rule increases link weights at locations of recent

cascade failure, thereby facilitating the unfolding of future avalanches (Alstott et al., 2015). This

mechanism opens bottlenecks in the network and further supports activity propagation over long

distances. We therefore hypothesize that avalanche dynamics in combination with integrative

network organization are beneficial for local operational diversity while supporting long-range,

selective propagation of information.

Material and Methods

Animal procedures

All animal procedures were conducted in accordance with NIH guidelines and were approved by

the Animal Care and User Committee of the National Institute of Mental Health. Three adult

NHPs (*Macaca mulatta*; 1 male, 2 females; 7–8 years old) received two chronic implantations of

high-density 96-microelectrode arrays each (Blackrock Microsystems; 4×4 mm^2; 400 µm

interelectrode distance; 10×10 grid with corner grounds). To direct recordings towards

superficial cortical layers II/III, electrode shanks of 0.6 mm length were used in prefrontal cortex

(PF; n = 4), and shanks of 1 mm length were used for premotor cortex (PM; n = 2). During

recording sessions monkeys sat head-fixed and alert in a monkey chair with no behavioral task

given. Portions of this dataset have been analyzed previously (Bellay et al., 2021; Meisel et al.,

2013; Miller et al., 2019; Yang et al., 2012; Yu et al., 2014).

Local field potential recordings in awake monkeys

Simultaneous and continuous extracellular recordings were obtained for 12 – 60 min per

recording session (2 kHz sampling frequency), band-pass filtered between 1 – 100 Hz (6th-order

Butterworth filter) to obtain the local field potential (LFP), and notch-filtered (60 Hz) to remove

line noise. About $2 \pm 1\%$ of time periods were removed from functional electrodes due to

artifacts introduced by e.g. vocalization, chewing, sudden movements. These artifacts were

identified by threshold crossing (SD > 7) and excised (± 0.25 s). Arrays on average contained 86

± 8 functional electrodes that exhibited 64 ± 50 µV of spontaneous LFP fluctuations (SD).

Channels which had been removed from an array at any recording day were discounted for all

recording days. Electrode LFPs were z-transformed and recording sessions for each array were

analyzed individually. The current study represents a combined 26 hr of ongoing cortical LFP

activity.

Neuronal avalanche definition and temporal resolution

For each electrode in the array, peak amplitude and time of negative LFP (nLFP) threshold

crossings (–2 SD) were extracted at the temporal resolution of $\Delta t = 0.5$ ms given our sampling

rate of 2 kHz. We note that the negative peak amplitude of the LFP correlates with the

probability of extracellular unit firing and synchrony in nonhuman primates (Bellay et al., 2021;

Petermann et al., 2009). The mean inter-event interval, <IEI>, defined as the average time

between consecutive nLFPs among all functional electrodes on the array, was calculated. We

then binned nLFP times in steps of Δt = <IEI> for each electrode, which ranged between 3 – 4

ms across NHPs and arrays. All nLFP events from all electrodes were combined into a matrix,

i.e. raster, with rows representing electrodes and columns representing time steps. A population

time vector was obtained by summing nLFPs in the raster for each time step. Avalanches were

defined as spatiotemporal continuous activity in the population vector bracketed on each side by

at least one time bin of duration Δt with no nLFP. The size of an avalanche, *S*, was defined as the

number of nLFPs participating. Multiple nLFPs at an electrode during an avalanche are rare (Yu

et al., 2014) and were counted in size estimates. Scale-invariance of *S* was visualized by plotting

probability distributions P(S) in double-log coordinates. We previously showed that analyzing

nLFP at Δt = <IEI> results in a distribution of avalanches with a slope close to -3/2 in line with

expectations for a critical branching process (e.g., (Beggs and Plenz, 2003)).

The maximum log-likelihood ratio (LLR) was calculated to test potential power law

distributions in avalanche size *S* against the alternatives of exponential or log-normal distribution

models (Clauset et al., 2009; Klaus et al., 2011). When tested positive for power law, the LLR

estimate for best slope α was reported. Here we used the range of $S = 1$ to 40, which excludes the

distribution cut-off (Klaus et al., 2011) close to the total number of functional electrodes on the

array (n >70). We note that analyzing avalanche dynamics at different temporal resolutions, e.g.

at shorter Δt or longer Δt compared to the <IEI>, increases or decreases the slope α respectively,

but not the power law form itself (see also Table 1; (Beggs and Plenz, 2003, Petermann, 2009

#4926)).

Avalanche temporal profile collapse and scaling exponent

Given the difficulty of obtaining robust lifetime distributions in the presence of ongoing

oscillations, the stability analysis for avalanches in the present work focused mainly on the

calculation of size distributions and temporal profile collapse (for details see Miller, 2019 #45}.

The temporal profile, $S(t)$, was described by the number of participating electrodes at each

timestep t $= 1$ up to the avalanche lifetime, L, which was defined by the number of timesteps Δt

that the avalanche persisted. In line with our previous results, profile analysis was carried out at

$\Delta t = 1$ ms and $\Delta t = 30$ ms to avoid profile modulation by ongoing γ-oscillations (Miller et al.,

2019). Avalanches were grouped by L in multiples of Δt and averaged to obtain the mean

temporal profile for a given lifetime, $\langle S \rangle(t, L)$. After normalizing to dimensionless time units,

i.e., the relative lifetime, t/L, amplitudes were then rescaled via Equation 1.

393
$$\langle S \rangle \left(\frac{t}{L} \right) \sim L^{\chi - 1} \, \mathcal{F} \left(\frac{t}{L} \right) \tag{1}$$

The profile collapse function, shown in Equation 1, relates the mean profile for each lifetime L,

$\langle S \rangle(t/L)$, with a characteristic temporal motif $\mathcal{F}(t/L)$, and scaling factor, $L^{\chi-1}$, which is

independent of L according to Equation 1. To perform a shape collapse, we plotted $\langle S \rangle(t, L)$ from

L-1 through L+1 for $L_{min} = 4\Delta t$ (to reduce finite size effects in shape caused by too few data

points). The collapse error, Δ_F, was quantified via a normalized mean-squared error (NMSE) of

height-normalized individual profiles to the combined normalized average of all collapsed

profiles, $\mathcal{F}(t/L)$. Minimized collapse error was calculated by scanning through $\chi = 0.5$ to 3 at

resolution of 0.001 to find the collapse in avalanche waveform associated with the smallest Δ_F

via $\chi_{collapse}$. A value of $\Delta_F > 1$ was considered a failure in collapse.

We note that for fractal objects such as spatiotemporal avalanches, changing the temporal

resolution also partitions avalanches differently. For a $\Delta t = 1$ ms, avalanche durations in

multiples of Δt will exhibit a power law as well as for $\Delta t = 30$ ms (see e.g. (Miller et al., 2019)).

Accordingly, the temporal profile of avalanches must be examined in multiples of generations of

duration Δt. A comparison between timescales in absolute times may not be possible. In the

present study, an avalanche of duration 150 ms encompasses L = 5 generations at $\Delta t = 30$ but

would require L = 150 generations at $\Delta t = 1$, which is highly unlikely to occur.

Fit of the average temporal profile of avalanches

For the parabolic fit we used the approach by (Laurson et al., 2013) as follows:

$$y = A \cdot \frac{t}{T}\left(1 - \frac{t}{T}\right)^{\gamma - 0.5} \tag{2}$$

413   The parabolic fit error, Δ_{parab}, was quantified via a normalized mean squared error (NMSE) of

414   individual profiles to an amplitude-matched parabola which was coarse-grained to match L.

415   Comparison to a semicircle fit was conducted in the same manner to obtain Δ_{semi} using

$$y = A \cdot \sqrt{1 - \left(t/T\right)^2}. \tag{3}$$

Correlation-based network reconstruction

Networks were reconstructed for each recording session individually and the links with low

pairwise correlations were removed before subsequent network analysis. Rather than applying a

strict minimum correlation threshold for removing the links, which would leave our analysis

vulnerable to inter-NHP differences in electrode impedances, etc., we instead sequentially

removed the weakest links in 0.01 increments of the correlation threshold until a predefined

sparsity of approximately 40% was achieved. Weight bins were divided into deciles for pruning

analysis (Fig. 4).

Normalized Count reconstruction of network

To remove the influence of common input to electrodes on the array, which inflates the

Pearson's pairwise correlation, we conducted a network reconstruction. This nonparametric

method, called the NC approach, is used for the network reconstruction because its

computational efficiency is comparable to the correlation analysis yet with much lower

reconstruction error, which are important considerations for analysis of long LFP time series

collected in awake *in vivo* preparations. For this reconstruction, the time-window within which

active nodes can influence each other was examined for 0.5, 1, <IEI>, and 30 ms. For each node

activation (spike), all nodes that were active within Δt, prior to the spike, were deemed as

potential causes. Results were very similar for $\Delta t = 0.5$ and 1 ms (data not shown). For longer Δt,

the precision of the algorithm decreases rapidly due to (1) the increase in ambiguous potential

associations between the number of active nodes in successive frames and (2) a decrease in the

number of transition time steps to estimate link weights (Pajevic and Plenz, 2009). Here we show

results for $\Delta t = 1$ ms, which matches our avalanche scaling analysis.

Integrative networks and Pruning analysis

Once the networks were defined, we studied their integrative properties (Pajevic and Plenz,

2012). The link clustering coefficient, C_L, was defined for each link as the ratio of the number of

common neighbors of its end nodes to the number of all neighbors (see Fig. 4A). In an

integrative network, there is a positive correlation R_{CL} between C_L and the weight of the link,

indicating that strongly connected nodes are likely to share more common neighbors. To

visualize this correlation, we divide links based on their weight into equally sized 10 blocks

ranging from the weakest block (rank 1) to the highest rank. For each block, we obtain the

average C_L and subtract the equivalent value that is obtained from the degree preserved

randomized network, yielding the excess link clustering, ΔC_L. We also conducted a "pruning

analysis" in which we studied the robustness of the excess node clustering ΔC upon the

progressive removal of the weakest (bottom pruning) or strongest (top pruning) links. Similarly,

the excess node clustering, ΔC, was defined as the difference of the mean clustering coefficient

of the original network and the corresponding randomized network after the degree-sequence

preserved randomization.

Entropy of mixing analysis

The estimated link weights fluctuated over time in both pairwise correlation and in directed

networks obtained with the NC reconstruction algorithm. We sought to explore whether these

fluctuations predominantly represent an error in the network reconstruction or arise from a

genuine and progressive change in the underlying network weights. To answer this question, we

developed a novel method that utilizes the entropy of mixing to quantify the progression of these

fluctuations in individual link strengths from one day to another. The entropy of mixing is a

concept from thermodynamics and describes the increase in total entropy when partitioned (pure

and equilibrated) sub-systems are allowed to mix. It is quantified using the Shannon entropy in

which probabilities are replaced by the fractions of each of the original species found at different

partitions. Hence, to conduct our entropy of mixing analysis, we need to partition the links into

different categories. Labels are assigned according to the magnitude of their weights obtained

from the Day 1 data, and partitioning them into a finite set of categories, N_c, ranging from the

weakest links to the strongest links. In our case, we used $N_c = 5$, so that the label $c = 1$ marked

the weakest 20% of the sorted links and incrementally, c = 5 marked the strongest 20% of the

links.

We conducted the mixing analysis on two different and complementary sub-networks.

The first is the "top" network, consisting of the 50% of the strongest links, and the second is the

"bottom" network, consisting of the weakest 50% percent of links. This was done mainly to have

some test of the performance of the entropy of mixing analysis, as we expect that the "bottom"

half is more dominated by the reconstruction errors of the NC algorithm than the "top" half. Note

that with this two-stage stratification of the links, the strongest 20% links in the "top" network

are effectively representing the 10% of strongest links in the full network, while the weakest

20% of the "top" network links have still greater magnitude than the strongest quintile of the

"bottom" networks, and, *vice versa*, the weakest 20% of the links in the "bottom" represent the

10% of weakest links in the full network. Once the chosen links were labelled, we then

monitored the changes of their weights over subsequent days. Specifically, we sort them again

based on their new weights, but now partition them over a potentially larger number of weight

groups, $N_g = k N_c$, where k is an integer, in order to make all groups contain a single category

label for the Day 1 stratification (we use k = 3 and $N_g = 15$, meaning that the links in the groups 1

through 3 will all initially carry the label c = 1, the groups g = 4 – 6 will be labeled c = 2, etc).

Due to (1) reconstruction errors and (2) potential actual network weight changes from one day to

another, each of the groups will on the subsequent days contain a mixture of the original labels,

although it is expected that the low group indices, *g*, will early on predominantly carry the labels

of the weak links, and *vice versa*. For each group, we calculate a fraction, f_c, of the links that

carry label *c*, which by definition are normalized to 1, i.e., $\sum_{c=1}^{N_c} f_c = 1$. For each group *g* we then

calculate the Shannon entropy of such mixture according to $H_g = -\sum_{c=1}^{N_c} f_c \log f_c$. Finally, we

report the average and the standard error over all non-edge H_g values, i.e., excluding the extreme

groups, g = 1 and g = 15, as those have only uni-directional mixing ($n = N_g\text{-}2 = 13$). Hence, the

average entropy of mixing reported in our results is $H_M = \frac{1}{N_g-2} \sum_{g=2}^{N_g-1} H_g$.

To evaluate if we have seen a progression in the weight evolution, we test it against the

null hypothesis that there was no significant linear trend across the subsequent days. To do so we

use a Monte Carlo (MC) procedure, in which we generate one million normally-distributed

replicates, $N(0,\sigma_G)$ for each point, where σ_G are the standard deviations of the means obtained

using the non-edge groups described in the previous paragraph. For each of the $N_{MC} = 1000000$

replicates we perform a linear regression and count the number of times the MC slopes were

greater than the slope we obtained using the mean values for H_M. From this count, N_{pos}, our

estimate of the *p* values is $p = (N_{pos}+1)/(N_{MC}+1)$ (see Table 4).

Tables

Table 1. Summary of average estimates for the mean Pearson's pairwise correlation coefficient,

$<R>$, the exponent α of avalanche size distributions for each nonhuman primate and array at

temporal resolutions of $\Delta t = 1$ ms and $\Delta t = 30$ ms respectively. Exponents were derived from

maximum likelihood estimates. Stability of α over all recording days was quantified by the linear

regression slope within 95% confidence limits (CfL).

	$<R>$ Stability	Avalanche size distribution (Δt = 1 ms)	slope α stability (Δt = 1 ms)	Avalanche size distribution (Δt = <IEI>)	slope α stability (Δt = <IEI>)	Avalanche size distribution (Δt = 30 ms)	slope α stability (Δt = 30 ms)
	Regression slope (95% CfL) (x10^{-3})	Exponent α (± SD)	Regression slope (95% CfL) (x10^{-3})	Exponent α (± SD)	Regression slope (95% CfL) (x10^{-3})	Exponent α (± SD)	Regression slope (95% CfL) (x10^{-3})
V-PF	-1 (-3, 2)	1.71 ± 0.00	0 (-1, 0)	1.26 ± 0.01	-2 (-3, 3)	0.65 ± 0.03	-3 (-9, 2)
V-PM	0 (-62, 62)	1.64 ± 0.02	6 (-40, 51)	1.29 ± 0.04	16 (-28, 60)	1.12 ± 0.05	20 (-2, 43)
N-PF	1 (0, 2)	1.71 ± 0.02	-1 (-1, 0)	1.41 ± 0.01	0 (-1, 0)	0.97 ± 0.02	0 (-1, 1)
N-PM	1 (-13, 15)	1.73 ± 0.02	2 (-8, 12)	1.31 ± 0.02	0 (-1, 1)	0.75 ± 0.02	3 (-6, 12)
K-PF1	1 (0, 1)	1.65 ± 0.02	-1 (-1, 0)	1.29 ± 0.01	0 (-1, 0)	0.90 ± 0.02	0 (0, 1)
K-PF2	0 (-20, 20)	1.77 ± 0.03	5 (-33, 43)	1.36 ± 0.02	1 (-27, 29)	0.74 ± 0.03	10 (-16, 35)
Mean ± SD	0 ± 1	1.70 ± 0.05	2 ± 3	1.32 ± 0.05	3 ± 7	0.86 ± 0.17	5 ± 9

510 **Table 2.** Summary of scaling function estimate for the temporal profile of neuronal avalanches.

511 A parabolic fit (Δ_{parab}) is compared to a semicircle fit (Δ_{semi}) at temporal resolutions $\Delta t = 1$ ms

512 and $\Delta t = 30$ ms for each nonhuman primate and array and its corresponding phase-randomized

513 profile (*random*) at $\Delta t = 1$ ms.

	Temporal Profile Fit: Parabola vs. Semicircle RMSE (Δt = 1 ms)		Temporal Profile Fit: Parabola vs. Semicircle RMSE (Δt = 30 ms)		Random Profile Fit: Parabola vs. Semicircle RMSE (Δt = 1 ms)	
	Paired t-Test (*p*-value)	ANOVA (F)	Paired t-Test (*p*-value)	ANOVA (F)	Paired t-Test (*p*-value)	ANOVA (F)
V-PF	4.36E-05	110.44	2.00E-04	62.26	5.96E-10	4832.54
V-PM	3.87E-04	121.17	3.40E-05	417.07	7.82E-07	2776.65
N-PF	6.12E-11	460.49	2.66E-13	1156.15	3.74E-14	1607.96
N-PM	6.81E-08	991.66	3.15E-06	272.38	2.41E-10	6533.12
K-PF1	2.76E-22	472.2	2.41E-25	715.09	1.98E-50	18530.05
K-PF2	2.60E-06	290.68	9.64E-06	186.09	1.91E-09	3277.87
Fit Error Δ	$\Delta_{\text{parab}} < \Delta_{\text{semi}}$	$\Delta_{\text{parab}} < \Delta_{\text{semi}}$	$\Delta_{\text{parab}} < \Delta_{\text{semi}}$	$\Delta_{\text{parab}} < \Delta_{\text{semi}}$	$\Delta_{\text{parab}} > \Delta_{\text{semi}}$	$\Delta_{\text{parab}} > \Delta_{\text{semi}}$

515   **Table 3.** Summary of estimates for the scaling exponent χ to optimally collapse temporal

516   avalanche profiles at temporal resolutions Δt = 1 ms and Δt = 30 ms for each nonhuman primate

517   and array. The stability of χ across all recording days was quantified by the linear regression

518   slope reported and 95% confidence limits. *Random*: Phase randomized control of temporal

519   avalanche profile.

	Scaling Exponent χ (*Δt* = 1 ms)	χ Stability (*Δt* = 1 ms)	Scaling Exponent χ (*Δt* = 30 ms)	χ Stability (*Δt* = 30 ms)	Scaling Exponent χ Random (*Δt* = 1 ms)	χ Stability Random (*Δt* = 1 ms)
	Mean χ (± SD)	Regression slope (95% CfL)	Mean χ (± SD)	Regression slope (95% CfL)	Mean χ (± SD)	Regression slope (95% CfL)
V-PF	1.78 ± 0.05	0.002 (-0.019, 0.022)	1.61 ± 0.09	-0.01 (-0.02, 0.01)	1.15 ± 0.01	0.001 (-0.001, 0.003)
V-PM	1.93 ± 0.15	0.051 (-0.3, 0.4)	2.25 ± 0.20	0.06 (-0.6, 0.7)	1.15 ± 0.00	0.000 (-0.001, 0.002)
N-PF	2.10 ± 0.06	0.002 (-0.000, 0.004)	2.15 ± 0.15	-0.00 (-0.01, 0.00)	1.14 ± 0.03	0.000 (-0.001, 0.002)
N-PM	2.05 ± 0.13	0.011 (-0.053, 0.075)	1.85 ± 0.05	0.005 (-0.016, 0.027)	1.14 ± 0.01	0.002 (-0.005, 0.008)
K-PF1	1.92 ± 0.03	0.000 (-0.001, 0.001)	2.11 ± 0.1	-0.000 (-0.003, 0.003)	1.15 ± 0.01	0.000 (-0.000, 0.000)
K-PF2	1.76 ± 0.02	0.007 (-0.004, 0.018)	2.12 ± 0.20	0.086 (-0.029, 0.2)	1.15 ± 0.00	0.000 (-0.004, 0.005)
Mean ± SD	**1.93 ± 0.14**	**0.012 ± 0.19**	**2.01 ± 0.24**	**0.02 ± 0.04**	**1.15 ± 0.01**	**0.001 ± 0.001**

521   **Table 4.** Functional network stability based on NC reconstruction algorithm at $\Delta t = 1$. Shown is

522   the stability of R_{CL} over time (see also Fig. 5D). H_M p-values given for top 50% and bottom 50%

523   for significant trend in mixing observed.

	R_{CL} Stability (Δt = 1 ms)	H_M Trend (Δt = 1 ms)	
	Regression slope (95% CfL) (x10^{-3})	Top 50% *p*	Bottom 50% *p*
V-PF	-1 (-28, 18)	0.46	0.34
V-PM	0 (-62, 62)	0.007	0.05
N-PF	1 (0, 0.002)	<10^{-5}	0.03
N-PM	14 (-13, 15)	0.08	0.54
K-PF1	1 (0, 1)	0.003	0.2
K-PF2	0 (-20, 21)	0.27	0.35
Mean ± SD	5 ± 10		

Acknowledgements

We thank members of the Plenz lab and attendees of the "*Critical brain dynamics: 5th*

International Workshop on Criticality and the Brain", 2016, NIH, USA for their support and

useful discussions.

Funding sources

This research was supported by the Intramural Research Program of the National Institute of

Mental Health ZIAMH002797, USA to D.P. and the *Eunice Kennedy Shriver* National Institute

of Child Health and Human Development to S.P. This research utilized the computational

resources of the NIH HPC Biowulf cluster (http://hpc.nih.gov).

Author Contributions

S.Y. collected the data; S.R.M. , S.Y. and S.P. analyzed the data; S.R.M., S.Y., S.P. and D.P.

wrote the manuscript.

Supplementary Information

No Supplementary Information.

Competing interests:

The authors declare no competing interests.

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