Title: Development of a novel connectivity-based electric-field modelling approach for individualized targeting of transcranial magnetic stimulation treatment

Running title: Novel modelling approach for individualized TMS targeting

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Abstract

Background
Transcranial magnetic stimulation has been shown to be effective and approved by the FDA for the treatment of depression. However, it is not standard practice to tailor the treatment to the individual, which can lead to variability in treatment response due to structural and functional differences in cortical organization. The current state of the art in individualized applications of TMS for the treatment of depression use functional connectivity to guide targeting, identifying targets that maximize anti-correlation between the left dorsolateral prefrontal cortex (dlPFC) and the subgenual anterior cingulate cortex (sgACC). This approach has two benefits. First, it accounts for individual subject functional cortical organization. Second, it requires only the collection of a resting state functional magnetic resonance imaging (rs-fMRI) scan, which is common practice for many ongoing research projects. However, this approach also has several limitations. First, it assumes that functional connectivity between the left dlPFC and sgACC is the most important factor for symptom reduction, which may not be the case at the individual level. Second, it does not account for the non-focality in the effect of TMS on functional connectivity.

In this work we propose a novel connectivity-based electric-field (e-field) modeling approach to identify optimal TMS targets at the single-subject level. This approach overcomes the limitations of previous work by 1) mapping the multivariate associations between all whole-brain functional connectivity and depression symptoms, and 2) using a novel application of e-field modelling to estimate the effect of TMS on those connections. By combining these two computational techniques in a single model, we can produce a predicted symptom change estimate that can be used to guide TMS targeting at the single subject level.

Methods
We applied this model to 91 MDD patients and 25 healthy controls. We measured depression symptoms using the Montgomery–Åsberg Depression Rating Scale (MADRS). We recorded 22 minutes of rs-fMRI. rs-fMRI data were preprocessed using the Human Connectome Project Pipelines v4.0.1. E-field models were conducted for 24 equally spaced orientations at 17 sites running along a vector encompassing the anterior-to-posterior axis of the left dlPFC. The result is a 24 x 17 parameter space where MADRS scores are predicted at each entry based on the hypothetical TMS effect (i.e. e-field model) on connectivity and connectivity/symptom correlations. These MADRS scores were then subtracted from the actual MADRS scores to create predicted ΔMADRS scores, which were compared to zero and corrected for multiple comparisons using a single-sample t-test and permutation testing.

Results
In the MDD patients, our model predicted a significant decrease in MADRS and HAMD scores near the junction of BA9 and BA46. In addition, this effect was strongest for coil orientations that ran perpendicular to the cortical gyrus at the stimulation site. In contrast, no site/orientation combination showed a significant relationship with MADRS or HAMD symptoms in the control subjects (all ps < 0.05).

Discussion
These results replicate previous work demonstrating the efficacy of left dlPFC stimulation for reduction of depression symptoms in depressed patients, and that sites near BA46 may be more efficacious than the standard treatment site. Additionally, these results suggest that our novel connectivity-based e-field modelling approach may be an effective way to 1) identify those subjects who will most benefit from rTMS treatment, and 2) individualize TMS targeting for those subject to maximize the therapeutic impact of the treatment.
**Introduction**

Major depressive disorder (MDD) is a mood disorder characterized by depressed mood or loss of interest or pleasure (1). Symptoms include feelings of worthlessness; indecisiveness or difficulty concentrating, change in weight, appetite, and sleep; psychomotor agitation; and suicidal ideation (1). According to the World Health Organization (WHO) World Mental Health (WMH) Surveys Initiative (2), lifetime prevalence rates within the United States average 16.9%, with women showing higher prevalence than men (20.2% vs. 13.2%) (2). The most common treatments for MDD include antidepressant medication, psychotherapy/cognitive behavioral therapy (CBT), or a combination of the two (https://www.nimh.nih.gov/health/statistics/major-depression.shtml). Although antidepressant use is prevalent, there are reports of mixed efficacy.

TMS to the left dlPFC has been approved by the FDA, and has been shown to be effective as an antidepressant treatment in treatment resistant depression, or in a patient population that have not responded to or tolerated previous antidepressant medication trials (3–5). Although many studies find a significant reduction in depressive symptoms (6–12), there have also been studies finding limited efficacy of TMS for major depression (13, 15), leaving room for improvement.

One possible explanation for the heterogeneity in TMS treatment response for major depression is that the standard scalp-based targeting approach (i.e. the 5cm rule) does not account for individual variations in cortical anatomy, and often selects regions outside the dlPFC, which may explain some of the modest therapeutic effects (14). Image-guided TMS incorporating MRI-neuronavigation, taking into account individual differences in brain anatomy, can target specific functional brain networks with greater precision. Using structural MRI to locate a specific site at the junction of BA 9 and 46 has shown greater efficacy than the traditional 5-cm rule (15). More recent approaches have used functional MRI (fMRI) to target
regions dIPFC that are downstream of the dIPFC, like the subgenual anterior cingulate cortex (sgACC) that are thought to be dysfunctional in MDD patients (16–19). Key to this approach is to use functional connectivity of the downstream site to identify the dIPFC site with the strongest connectivity.

Although this connectivity-based approach represents the current cutting-edge in the field, and is an improvement on the standard scalp-based targeting approach used clinically, it has two fundamental limitations. First, focusing on a single downstream region to define the TMS target does not account for off-target effects in other downstream regions. Second, although there may be ample evidence associating the downstream target with symptoms, there is no guarantee that the net effects of the TMS will move symptoms in the desired direction. To address these limitations, we developed a novel computational model based on whole brain functional connectivity and electric-field modelling. To address the first limitation, we use electric-field modelling to estimate the change in connection strength across the whole brain given a particular site and orientation of stimulation. To address the second limitation, we use multiple linear regression to estimate the net effects of these connection strength changes on symptoms. The overall concept is to generate a predicted symptom change score following neuromodulatory TMS at a particular site and stimulation. We then iterate the model across sites and orientations to find the site/orientation combination that leads to the maximal reduction in MDD symptoms.

Materials and Methods

Participants

One hundred eighteen participant (Age: M=28.42, SD=7.92) entries were pulled from the Dimensional Connectomics of Anxious Misery dataset (20), and included anxious misery
participants (93 total, 64 were females) and healthy controls (25 total, 16 were females; See Table 1). Mean age of the anxious misery cohort was $M=28.29$ (8.2) and of healthy controls $M=28.92$ (6.91). The anxious misery cohort included a range of different diagnoses, namely major depressive disorder ($N = 41$), persistent depressive disorder ($N = 9$), social anxiety disorder ($N = 5$), generalized anxiety ($N = 21$), and PTSD ($N = 17$).

Basic Inclusion/Exclusion criteria were standard for fMRI, and can be found in (20). In addition, participants in the anxious misery cohort needed to score a minimum of one (1) standard deviation above a point estimate of the general adult population mean (distributions for males and females were different) in the NEO Five-Factor Inventory (21) in order to be included in the study. Conversely, healthy controls needed to score within one (1) standard deviation of the point estimates to be eligible to participate. Subject were recruited by means of IRB-approved advertisement and phone calls. All participants signed an informed consent form, and the protocol was approved by the Institutional Review Board for human subject research at the University of Pennsylvania.

**Procedure**

On the initial visit, written consent was obtained from all eligible participants prior to enrolling in the study, then a baseline visit was conducted where a study staff interviewed the participants to ascertain their medical history and demographic information. Next, a research version of the Structured Clinical Interview for DSM-5 (SCID-5-RV) (1) was conducted by a trained member of the staff to document their psychiatric diagnosis and history, and the remaining assessments (See Below) were conducted. In a follow-up visit, a 2-hour fMRI scan was conducted, where structural, diffusion, resting state, and task-based fMRI were collected as part of the larger project.
Assessments

Many clinical measures were used to identify the behavioral and cognitive features of anxious misery. In this project, eligible participants completed 17 self-report and 3 clinician-administered measures. The clinician-administered measures include the Montgomery-Asberg Depression Rating Scale (MADRS) (22) and the Hamilton Depression Rating Scale (HAMD) (23) in order to assess depression severity.

MRI Scans

MRI data was acquired as part of the Dimensional Connectomes of Anxious Misery project (20), one of the Connectomes Related to Human Diseases (CRHD) studies (https://www.humanconnectome.org/disease-studies). Accordingly, data acquisition and scanning parameters were designed to be harmonized with three other CRHD studies: the Mapping Connectomes for Disordered Mental States (24), the Boston Adolescent Neuroimaging of Depression and Anxiety study (25) and the Treatment of Resistant Depression Connectome by Fast-Acting Therapies (26).

Participants were scanned on a Siemens Prisma 3T using a 64-channel head coil. Structural T1-weighted images were acquired using a magnetization-prepared rapid acquisition with gradient echo (MPRAGE) sequence with TR=2400ms, TE=2.22ms and flip angle of 8 degrees. 208 slices were acquired with a voxel resolution of 0.8mm isometric, resulting in an FOV of 256 x 240 x 167mm. T2-weighted images were acquired using a variable-flip-angle turbo-spin echo (TSE) sequence with TR=3200ms and TE=563ms, with the same voxel resolution and FOV as the T1w acquisition. Resting state fMRI data were acquired with a multiband acceleration of 8, TR=800ms, TE=37ms and flip angle of 52 degrees. Whole-brain coverage was achieved with 72 slices and a voxel resolution of 2.0mm isometric, resulting in an
FOV of 208 x 208 x 144mm. Each resting state scan was paired with another run with the opposite phase encoding direction (AP-PA), and two such pairs were acquired, resulting in 22:24 minutes of data (5:46 min x 4 runs) for each participant. Spin echo field maps were also acquired in opposite phase encoding directions in order to correct susceptibility distortions. During the resting state scan, participants were shown a white screen with a black crosshair in the center and were instructed to remain still with their eyes open and to blink normally.

MRI preprocessing

Computational head modelling for e-field calculations. We used the SimNibs software package to generate 3D head and coil geometries using the finite element method (FEM) (27). T1 and T2 structural MRIs were combined to create an individualized head model and then segmented into scalp, skull, CSF, gray matter, and white matter volumes. These volumes were then converted to tetrahedral meshes using a Gmsh subroutine packaged in SimNIBS (28).

E-field calculations. E-field models were conducted for each site/orientation combination (See Below), and the normalized e-field strength estimate at each surface node was used to model the potential TMS effects (29).

fMRI preprocessing

Data were preprocessed using the Human Connectome Project Pipelines v4.0.1 (retrieved from https://github.com/Washington-University/HCPpipelines/releases/tag/v4.0.1). A full description of preprocessing steps is provided elsewhere (30). In brief, anatomical preprocessing steps included gradient nonlinearity distortion correction, co-registration of T1w and T2w images, bias-field correction using spin-echo field maps and spatial normalization to the Montreal Neurological Institute (MNI) template. Functional image preprocessing steps included removal of spatial distortions via gradient nonlinearity corrections, correction of participant
motion through volume realignment, susceptibility distortion correction using dual-phase encoded spin-echo corrections, registration of fMRI data to T1 space, subsequent transformation to MNI-space and removal of extra-parenchymal voxels.

Timeseries analyses using volumetric data were further conducted using the eXtensible Connectivity Pipeline (XCP Engine) (31). The workflow is summarized as follows: (i) removal of the 10 initial volumes (8 seconds) to achieve signal stabilization, (ii) demeaning and removal of quadratic trends using a general linear model to account for scanner drift, (iii) intensity despiking using 3dDespike from AFNI (32), (iv) bandpass temporal filtering of time series between 0.01 Hz and 0.08Hz using a first-order Butterworth filter (33), (v) regression of nine confounding signals (six motion parameters + global signal + mean white matter signal + mean cerebral spinal fluid signal) and as well as the temporal derivative, quadratic term and temporal derivatives of each quadratic term (resulting in 36 regressors total) (34), and (vi) spatial smoothing with SUSAN from FSL (35) using a 6mm FWHM kernel. Voxelwise timeseries were then downsampled to the 333 parcels in the Gordon atlas (36) and NxN connectivity was calculated using Z-transformed Pearson correlations.

**Model steps**

**PCA regression.** For the first step in our analysis (See Figure 2 and Appendix for detailed equations), we combined a principal component analysis with a multiple linear regression to model the relationship between functional connectivity and symptoms (37). We began by conducting a principal components analysis on the functional connectivity data to reduce noise and minimize collinearity (38). We separated signal and noise components using a geometric approach that identified the eigenvalue at the elbow of the scree plot (i.e. the eigenvalue furthest from the hypotenuse connecting the first and last eigenvalues). The principal
component scores for each of the signal components were then used to predict symptom scores in a multiple linear regression. The resulting beta coefficients were then vectorized and combined with the principal component coefficients using matrix multiplication. The result was an item-length vector where the value at each point represented the overall variability in symptoms accounted for by that particular functional connection.

**Selection of sites and orientations.** A series of 17 sites along the anterior-to-posterior gradient of the L DLPFC were used in the model (See Supplemental Table 1). This site vector was anchored by 3 therapeutic sites described in (39) ([−41, 16, 54] based on 5cm rule, [−36, 39, 43] BA9, [−44, 40, 29] BA46), and extends 12 mm posterior to the 5mm site and 12 mm anterior to the BA46 site. At each site, we generated 24 different e-field models. For each model, the roll and pitch of the TMS coil was defined perpendicular to the scalp. The yaw vector was selected from 24 possible orientation vectors spaced at 15-degree increments.

**E-field connectivity matrices.** The e-field maps were downsampled to the Gordon atlas (36), vectorized, and thresholded using the same geometric approach described in the PCA regression section (See Figure 3 and Appendix for detailed equations). To estimate how stimulation at a specific site and orientation might affect connectivity, the downsampled e-field vector was first rotated, and then averaged to form an NxN matrix where the values in the matrix represent the average current induced in the ROIs for each connection.

**E-field/connectivity symptom estimates**

To model the predicted neuromodulatory effects of TMS on symptoms, the e-field model matrix was combined with the single-subject connectivity matrix and the estimated group-level coefficients derived from the symptom/connectivity regression, according to the equation in Figure 1B. These calculations were iterated across all sites and orientations to create the heatmap
shown in Figure 4, where each value in the heatmap represents the modeled change in symptoms for that subject given hypothetical TMS administered at that particular site and orientation.

**Statistical analysis**

To determine whether our novel modelling approach predicted significant changes at the group level, we conducted paired sample t-tests comparing actual symptoms to the predicted change in symptoms estimated from our model. A significant negative t-score would indicate a predicted decrease in symptoms at the group level. We repeated this process for all site/orientation combinations estimated, and generated heatmaps from the resulting t-scores. To correct for multiple comparisons, we conducted 10,000 permutation tests where the sign of the symptom – predicted symptom change was randomly flipped across subjects and permutations. T-tests against 0 were then conducted at each site/orientation combination within the permuted heatmap. The maximum t-score from each permuted heatmap was then extracted and used to build a null distribution across permutation tests. We used a 2-tailed alpha of 0.05, and thus selected the corresponding t-score (i.e. threshold = t[10,000*0.05/2]) from the null distribution generated from the permutation tests. The heatmap from the actual test was then thresholded with this minimum t-score derived from the permutation tests (See Table 2 for values).

**Results**

**PCA regression**

Separate PCA/regression analyses were conducted for the anxious misery group and the control subjects. For the AM group, 11 signal components were selected, and these components explained 31% of the variability in the functional connectivity signal. For the control group, 6 components were selected, and these components explained 40% of the variability in the functional connectivity signal.
Individual subject predictions

One goal of this project was to determine whether the modeling approach above could be used to make targeting decisions for the application of TMS to single subjects. Accordingly, reliable single subject data is key to achieving this goal. Single subject heatmaps from the AM group show clear systematic patterns of predicted symptom change as a function of both site and orientation (See Figure 5), suggesting that this modelling approach can be used to simultaneously optimize these two parameters at the single subject level. These patterns are characterized by punctate “cool spots” in the heatmap that identify a clear site/orientation combination that yields maximal symptom reduction. Furthermore, consistent with previous literature on remission rates following therapeutic rTMS, our model predicts a reduction in MADRS scores in approximately two-thirds of the patients (n = 59/90) if we extract the predicted MADRS score at the site/orientation combination (5cm anterior to MT at ~45 degrees eccentricity) typically used for therapeutic rTMS. Using our approach to optimize site and orientation results in a modest increase in predicted responders (n = 66/90). Importantly, this pattern seems to be specific to those in the AM group as control subjects do not show the characteristic “cool spots” in their heatmaps (See Figure 6).

Group level predictions for MADRS and HAMD

To determine whether the model made significant predictions at the group level, we calculated the predicted change in MADRS/HAMD for each site/orientation combination by subtracting the predicted MADRS/HAMD scores (i.e. values in Figure 5) from the observed MADRS/HAMD scores. These difference scores represent the predicted change in MADRS/HAMD, given a specific site/orientation of stimulation. We then compared these values to 0 (i.e. no effect of TMS) using a single sample t-test. We corrected for multiple comparisons.
across sites/orientations using permutation tests. As shown in Figure 7 our model predicts a significant decrease in both MADRS and HAMD scores in AM subjects with both left and right dlPFC stimulation. In the left hemisphere, the cool spots are centered on BA46 at 30-45 degrees orientation. In the right hemisphere, the cool spots are positioned slightly anterior to BA46, and strongest at 120 and 135 degrees orientation, roughly perpendicular to the optimal coil angle in the left. Consistent with the results at the single-subject level, these results suggest that there is a significant relationship between both site and orientation and predicted symptom change. Importantly, these results are limited to the AM subjects, as the model predicts no significant changes in MADRS or HAMD scores in the healthy control subjects (See Figure 8).

**Discussion**

Here we present a proof of concept methodological study where we use functional connectivity and electric-field modelling to predict symptom change following a hypothetical course of neuromodulatory treatment with TMS. Our model calculates the relationship between symptoms and connectivity, as well as the effect of TMS on connectivity to yield a predicted change score in the symptom, assuming TMS is delivered at the site and orientation specified in the model. By iterating this process across sites and orientations, we are able to show a systematic effect of both site and orientation on predicted treatment outcome, as measured by MADRS and HAMD scores. Importantly, these effects are apparent at both the single-subject and the group level, suggesting that this approach has sufficient power to identify subject-specific TMS targets to maximize symptom reduction.

Consistent with previous work implicating the junction of BA9 and BA46 as a potentially optimal site of stimulation for depression symptoms, we show with both MADRS and HAMD scores that are model predicts the largest symptom reduction at this location (47). Our model
adds to the work suggesting that targeting rsFC networks can inform TMS targeting (40), and are consistent with the findings that individualized rsFC maps may be most informative (39). Previous research has shown that regions of the dlPFC that are more strongly anticorrelated with sgACC tend to show better clinical efficacy when targeted with therapeutic TMS (41, 42), and the closer the stimulation site is to this optimally anticorrelated dlPFC location, the better the clinical outcome (43–45). Importantly, active rTMS to the l dlPFC has been shown to reduce anticorrelation between the dlPFC and sgACC (46, 48, 49), and prospective targeting based on individualized dlPFC sgACC connectivity leads to a greater reduction in symptoms compared to traditional targeting (45, 46). In addition, there is some research to suggest that individualized targeting of BA46 through a parcel guided approach can improve treatment response in patients who have previously failed standard TMS targeted at the dlPFC using the 5CM rule (47). Based on this work, it could be argued that the current state-of-the-art for individualized TMS targeting for depression is to target sites in the left dlPFC with maximal connectivity with the subgenual cingulate cortex.

However, a review of 33 studies with pre-post resting state shows that although TMS induces robust changes in rsFC, the majority of effects are outside of the stimulated functional network (52). Indeed, the changes in functional connectivity following rTMS treatment for depression can be seen throughout the brain in regions that are important for affective responding (e.g. insula, amygdala, inferior parietal lobule, etc.), suggesting that the net effects on symptoms may be driven by these large scale network connectivity changes (53). Consistent with this idea, treatment response has also been linked to rsFC changes outside of the sgACC (50, 51). Together these results suggest that a whole brain connectivity model may outperform single connection targeting approaches, like the ones described above.
In keeping with these results, our whole brain connectivity approach has several potential benefits over single connection targeting approaches. First, our model uses e-field modelling to account for the variability in electric current spread due to individual differences in cortical anatomy, and uses this information to inform targeting. Second, our approach accounts for other connections in the brain that 1) may be impacted by TMS treatment, and 2) contribute to symptom reduction. Importantly, our model uses a data driven approach to weight these connections by the amount of variability they explain in the depression symptoms. Finally, our approach uses agnostic data-driven estimates between behavioral characteristics and functional connectivity to drive targeting. Therefore, this model can be extended to other symptoms/behavioral characteristics where reliable measures of behavioral markers are available.

The main focus of the paper was on MADRS and HAMD scores, however it is important to note that the model described here can be applied to other symptom measures as well. In previous work, we have used various symptom clustering approaches to extract distinct symptom measures from available clinical data (55), which could potentially be used to direct TMS targeting. Indeed, defining biotypes for depression and anxiety starting with neural circuit dysfunction (56), may yield additional symptom-specific targets. Accordingly, the model presented here could be used not only to individualize targeting at the single subject level, but it could potentially be extended to individualize targeting at the single session level, where each TMS session in a course of treatment is targeted at a specific symptom or set of symptoms, thereby maximizing the therapeutic effect.

Strengths and Limitations

The strength of the work describe here stem from the generality of its applicability. The
model described in this work is both site and symptom independent. Therefore, the methods described here can be used to optimize TMS targeting for a wide variety of disorders shown to be effectively treated with TMS. In addition, this approach could be used prospectively to screen for potential TMS effects within new disorders or for novel symptom dimensions. In addition, the model is able to make predictions at the single-subject level regarding the optimal stimulation site for a given symptom, allowing for single subject optimization of TMS targeting. In all cases, the predictions of the model can be directly tested by applying TMS according to the model predictions.

The primary weakness of this study is that it is a proof of concept study, rather than a confirmatory study, meaning we do not actually administer TMS and measure the pre/post symptom changes in the current work. We understand that this is the necessary next step to validate the current model. Our hope is that publishing the model in its initial state will allow multiple labs to test the predictions of the model, allowing for a more rapid validation/refinement of the work. To facilitate this process, we plan to make the code for our model publicly available.

Another potential weakness of the current work is that we used Pearson’s correlations, a non-directional measure, to model functional connectivity. However, it is likely that TMS affects upstream and downstream connections differentially. Accordingly, it may be more appropriate to model the functional connections using effective connectivity, and differentially weight the connections based on whether they are upstream or downstream of the stimulation site. Of course this becomes more complicated in our model, given that the stimulation “site” is modelled as a thresholded map of the current induced across the whole brain, given a TMS coil position and orientation. Accordingly, to factor in differential effects for upstream and downstream connections, it would be necessary to generate an NxN effective connectivity map of the entire
brain. While techniques like dynamic causal modelling (DCM) can be used to generate realistic effective connectivity models with a limited number of sites and connections, it remains to be seen whether this approach can be reliably used to generate whole brain effective connectivity models for use at the single subject level.

One final weakness of the current work is that the model assumes that changes in connectivity scale with the magnitude of the electric field induced, given a particular site/orientation of stimulation. This assumption likely holds for little if any in vivo applications of TMS. Indeed, it is well known that the effects of TMS on outcome variables like cortical excitability, functional connectivity, and behavior are dependent on the stimulation parameters used (52, 54). Indeed, amplitude, frequency, pattern, number of sessions, and intervals between sessions are all known to be important determinants of observed TMS effects. We understand that the linear assumption put forth in our model is a massive oversimplification, but we see this as a starting point. Our goal is to state the initial model as parsimonious as possible, to allow the model to be tested with a variety of experimental and clinical TMS protocols.

Conclusions

Individualized targeting is one key to maximizing the efficacy of clinical rTMS, and mapping TMS-induced changes in rsFC to changes in clinical symptoms is critically important for this goal. The model proposed here accomplishes this goal in a manner that is both site and symptom independent. We have validated the model using depression symptoms in a cohort of anxious misery patients, and shown that it replicates the finding that BA46 (an area with strong sgACC anticorrelation) may be maximally effective for treating depression. However, it is our hope that this work will be applied more generally to optimize TMS targeting across psychiatric disorders.
Author contributions: NLB: Designed Study, Conducted analysis, wrote manuscript, provided supervision, edited manuscript. DS: Assisted with data collection and preprocessing. WM: Assisted with data collection and preprocessing. JB: Conducted statistical analysis; edited manuscript. ZD: Assisted with statistical analysis and manuscript preparation. TG: Assisted with data collection and preprocessing. MT: Assisted with data collection and preprocessing, assisted with manuscript preparation. NS: Assisted with data collection and preprocessing. MJ: Assisted with data collection and preprocessing. RTS: Assisted with statistical analysis; edited manuscript. YIS: Assisted with study design, wrote manuscript; provided supervision; edited manuscript.

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Ethical Standards: The authors assert that all procedures contributing to this work comply with the ethical standards of the relevant national and institutional committees on human experimentation and with the Helsinki Declaration of 1975, as revised in 2008.
References


66: 151–160.


Appendix: Equations

Connectivity based model: PCA regression
Let \( \mathbf{Y}^{\text{mood}} \) be the \( n \times 1 \) vector of behavioral symptom scores (e.g., MADRS scores) for \( n \) participants. We assume the behavioral symptom scores can be predicted using a linear combination of connectivity measures, according to the model

\[
\mathbf{Y}^{\text{mood}} = \mathbf{X} \boldsymbol{\beta} + \mathbf{\epsilon},
\]

where \( \mathbf{X} \) is a \( n \times p \) matrix such that each row consists of one participant’s concatenated unique connectivity values from the Z-transformed Pearson correlation functional connectivity matrix, i.e., the upper or lower triangular portion of the \( N \times N \) connectivity matrix (\( p = N(N - 1)/2 \)), for the Gordon atlas, \( N = 333 \); \( \boldsymbol{\beta} \) is a \( p \times 1 \) vector of coefficients, and \( \mathbf{\epsilon} \) is a \( n \times 1 \) vector of error terms. We assume that \( \mathbf{Y}^{\text{mood}} \) and columns of \( \mathbf{X} \) have been centered so as to have zero empirical means.

We perform principal components analysis (PCA) on the predictor matrix \( \mathbf{X} \). Let \( \mathbf{X} = \mathbf{U} \mathbf{\Delta} \mathbf{V}^T \) denote the singular value decomposition of \( \mathbf{X} \), where \( \mathbf{\Delta}_{p \times p} = \text{diag}(\delta_1, \ldots, \delta_p) \) is a diagonal matrix of non-negative singular values, and columns of \( \mathbf{U}_{n \times p} \) and \( \mathbf{V}_{p \times p} \) are orthonormal sets of vectors, i.e., the left and right singular vectors of \( \mathbf{X} \). The spectral decomposition of \( \mathbf{X} \) is given by \( \mathbf{\Lambda} \mathbf{\Delta} \mathbf{V}^T \), where \( \mathbf{\Lambda}_{p \times p} = \text{diag}(\lambda_1, \ldots, \lambda_p) = \text{diag}(\delta_1^2, \ldots, \delta_p^2) = \mathbf{\Delta}^2 \) is a diagonal matrix of the non-negative eigenvalues of \( \mathbf{X}^T \mathbf{X} \) and columns of \( \mathbf{V}_{p \times p} = [\mathbf{v}_1, \ldots, \mathbf{v}_p] \) are the corresponding eigenvectors. The \( j^{\text{th}} \) principal component and \( j^{\text{th}} \) principal component direction (i.e., PCA loading) corresponding to the \( j^{\text{th}} \) largest eigenvector are \( \mathbf{X} \mathbf{v}_j \) and \( \mathbf{v}_j \), respectively, for each \( j \in \{1, \ldots, p\} \).

For PCA regression (PCR), we use the first \( k \leq n \) components as predictors. Let \( \mathbf{V}_k \) represent the \( p \times k \) matrix comprising the first \( k \) columns of \( \mathbf{V} \), and \( \mathbf{W}_k = \mathbf{X} \mathbf{V}_k \) be the \( n \times k \) matrix with the first \( k \) principal components as columns. We estimate regression coefficients \( \mathbf{\gamma}_k \) in \( \mathbf{Y}^{\text{mood}} = \mathbf{W}_k \mathbf{\gamma}_k + \mathbf{\epsilon}_k \) by ordinary least squares, i.e., \( \mathbf{\gamma}_k = (\mathbf{W}_k^T \mathbf{W}_k)^{-1} \mathbf{W}_k^T \mathbf{Y}^{\text{mood}} \in \mathbb{R}^k \). Then the PCR estimator of \( \boldsymbol{\beta} \) based on the first \( k \) principal components is given by \( \hat{\boldsymbol{\beta}}_k = \mathbf{V}_k \hat{\mathbf{\gamma}}_k \in \mathbb{R}^p \).

E-field augmented model
Once \( \hat{\boldsymbol{\beta}}_k \) is obtained from the connectivity based model, the e-field augmented model will be used to identify the optimal coil orientation and stimulation sites to generate the greatest reduction in behavioral symptom score for each participant. Let \( \Delta \mathbf{Y}^{\text{mood}} \) be the \( n \times 1 \) vector of changes in score between the pre- and post-treatment assessments for \( n \) participants. We model \( \Delta \mathbf{Y}^{\text{mood}} \) as follows:

\[
\Delta \mathbf{Y}^{\text{mood}} = \mathbf{Y}^{\text{mood}}_{\text{post}} - \mathbf{Y}^{\text{mood}}_{\text{pre}} = (\mathbf{X}_{\text{post}} - \mathbf{X}_{\text{pre}}) \hat{\mathbf{\beta}} + \mathbf{\epsilon}',
\]

where \( \mathbf{\epsilon}' = \mathbf{\epsilon}_{\text{post}} - \mathbf{\epsilon}_{\text{pre}} \).

For each site and orientation \( l \), let \( \mathbf{E}_l \) be a \( n \times p \) matrix, where rows correspond to participants,
columns correspond to pairs of regions in the Gordon atlas, and entries equal the average e-field model values at each pair of regions for the given participant, site, and orientation. We assume that $X_{post}^l = C \cdot E_i \circ X_{pre}$, where $C$ is a positive proportionality constant, and $\circ$ denotes the Hadamard product. Thus, for a given stimulation site and coil orientation combination $l$,

$$
\Delta Y^{mod} = (C \cdot E_i \circ X_{pre} - X_{pre})\beta + \epsilon'.
$$

With these assumptions, and substituting the $\hat{\beta}_k$ estimated from the PCR described above, it is possible to compare relative differences in the predicted change in behavioral symptom score across sites and orientations $l$. 
### Table 1: Demographic information and clinical measures

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<td><strong>Clinical measures</strong></td>
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<tr>
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**Table 3: Permutation test thresholds**

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<th>Control Right</th>
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<td>HAMD</td>
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<td>2.6</td>
<td>2.62</td>
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</table>
Figure Legends

**Figure 1. Theoretical basis for current model.** A) Depicts a basic linear relationship between a hypothetical symptom and a hypothetical functional connection in the brain. B) Depicts a revised equation where the slope of the relationship is modified by a weighting factor “E”, which represents the change in connectivity induced by a TMS treatment, estimated from the electric (e)-field model.

**Figure 2. The PCA-Regression data reduction approach used to summarize the relationship between symptoms and connectivity in the current model.** A) Resting state functional connectivity (rsFC) is calculated using Pearson’s correlations across all subjects for all regions in the Gordon atlas (36). B) A Principal component analysis is used to identify orthogonal components in the rsFC data, and a geometric approach is used to identify a minimal number of components that explain a maximal proportion of the variability. C) Component scores for the selected components are extracted and entered into a multiple linear regression to predict symptoms (D). The item coefficients from the selected components (E) are combined with the beta vector from the regression (F) using matrix multiplication to create the output vector (G), which is used to represent the slope of the line relating connectivity and symptoms.

**Figure 3. Methods used to summarize electric (e)-field models in NxN connectivity space.** Normalized e-field models were first downsampled to the Gordon atlas (36). The results were then converted to a 1 x N vector. This vector was then rotated by 90 degrees, averaged, and thresholded to create an N x N matrix with the same dimensions and sorting as the rsFC matrices.

**Figure 4. Iteration of model across site and orientation.** To understand how placement and orientation of the TMS coil might impact symptoms, we computed our model across multiple sites and orientations. Sites were defined at equally spaced points along the anterior to posterior axis of the middle frontal gyrus. Roll and pitch were defined orthogonal to the scalp at each stimulation site. Multiple equally spaced yaw vectors were defined at each stimulation site, representing all possible coil orientations. Electric (e)-field models were conducted at each site/orientation combination, entered into our symptom prediction model, and the results were plotted in this site x orientation heatmap.

**Figure 5. Individual subject data for the anxious misery group. (A, C, E, G)** Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the left dlPFC. (B, D, F, H) Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. Colors represent the predicted MADRS scores. Y axis represents coil orientation. X axis represents location along the Z-axis of the middle frontal gyrus. “X” in heatmaps represent the site and orientation of stimulation predicted to have the maximal reduction in symptoms for each subject.
**Figure 6. Individual subject data for the healthy control group. (A, C, E, G)**
Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the left dlPFC. (B, D, F, H) Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. Colors represent the predicted MADRS scores. Y axis represents coil orientation. X axis represents location along the Z-axis of the middle frontal gyrus. “X” in heatmaps represent the site and orientation of stimulation predicted to have the maximal reduction in symptoms for each subject.

**Figure 7. Group-level data for the anxious misery group. A)** Heatmap representing the predicted MADRS scores following a hypothetical course of TMS treatment to the left dlPFC. **B)** Heatmap representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. **C)** Heatmap representing the predicted HAMD scores following a hypothetical course of TMS treatment to the left dlPFC. **D)** Heatmap representing the predicted HAMD scores following a hypothetical course of TMS treatment to the right dlPFC. Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. Colors represent the predicted MADRS scores. Y axis represents coil orientation. X axis represents location along the Z-axis of the middle frontal gyrus. “X” in heatmaps represent the site and orientation of stimulation predicted to have the maximal reduction in symptoms across the group. Diagonal hatching represents sites where the change in MADRS/HAMD scores was not statistically different from 0.

**Figure 8. Group-level data for the healthy control group. A)** Heatmap representing the predicted MADRS scores following a hypothetical course of TMS treatment to the left dlPFC. **B)** Heatmap representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. **C)** Heatmap representing the predicted HAMD scores following a hypothetical course of TMS treatment to the left dlPFC. **D)** Heatmap representing the predicted HAMD scores following a hypothetical course of TMS treatment to the right dlPFC. Heatmaps representing the predicted MADRS scores following a hypothetical course of TMS treatment to the right dlPFC. Colors represent the predicted MADRS scores. Y axis represents coil orientation. X axis represents location along the Z-axis of the middle frontal gyrus. “X” in heatmaps represent the site and orientation of stimulation predicted to have the maximal reduction in symptoms across the group. Diagonal hatching represents sites where the change in MADRS/HAMD scores was not statistically different from 0.
A

Connectivity based modelling

Symptom

\[ Y_{\text{symptom}} = f(M, X) + \epsilon \]

B

E-field augmented modelling

\[ \Delta Y_{\text{symptom}} = f(M, E, X) + \epsilon \]
Scale models to whole brain using Gordon atlas

Reshape e-field to match $N \times N$ connectivity graph

- Compute e-field
- Downsample to atlas
- Vectorize results
- Convert to graph