Signal processing capacity of the cellular sensory machinery regulates the accuracy of chemotaxis under complex cues

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Key words: chemotaxis, cellular sensory machinery, signal processing capacity, cell migration

Summary

Chemotaxis is ubiquitous in many biological processes, but it still remains elusive how cells sense

and decipher multiple chemical cues. In this study, we postulate a hypothesis that the chemotactic

performance of cells under complex cues is regulated by the signal processing capacity of the

cellular sensory machinery. The underlying rationale is that cells *in vivo* should be able to sense

and process multiple chemical cues, whose magnitude and compositions are entangled, to

determine their migration direction. We experimentally show that the combination of TGF-β and

EGF suppresses the chemotactic performance of cancer cells using independent receptors to sense

the two cues. Based on this observation, we develop a biophysical framework suggesting that the

antagonism is caused by the saturation of the signal processing capacity, but not by the mutual

repression. Our framework suggests the significance of the signal processing capacity in the

cellular sensory machinery.

Introduction

Cell chemotaxis - the biased migration of cells toward a chemical cue - is a critical step in various pathological and physiological processes, including cancer metastasis, embryogenesis, and wound healing (Welch and Hurst, 2019). For multiple cell types, including cancer, cells are exposed to multiple signals within the complex chemical and physical environments during migration (Quail and Joyce, 2013; Roussos et al., 2011). These include multiple cytokines such as transforming growth factor-β (TGF-β), epidermal growth factor (EGF), stromal cell-derived factor-1α (SDF-1α), and CCL2 (Fernandis et al., 2004; Mantovani et al., 2002; Quail and Joyce, 2013; Roussos et al., 2011). Furthermore, the nature of the cytokine signals varies in space and time (Odenthal et al., 2016; Van Haastert and Devreotes, 2004). Cellular sensing is critical for deciphering the complex signals and accurately migrating in the direction of the physical and chemical cues whose temporal and spatial characteristics are tangled.

Prior studies on chemotaxis have focused on identifying molecules to establish the signal transduction network for a given chemical cue. Intracellular signaling networks involve a series of processes relevant to diverse cell physiological responses (Han and Lo, 2012; Ikushima and Miyazono, 2010). Research efforts to identify the associated signaling molecules and systematically construct their networks have advanced our understanding of how cells process the signals that result in a chemotactic response (Miyagawa et al., 2018; Odenthal et al., 2016; Roussos et al., 2011; Swaney et al., 2010). Quantitative modeling involving chemical kinetics or logical circuits has extensively contributed to constructing signaling networks in systems biology (Barberis and Verbruggen, 2017; Le Novère, 2015). These approaches elucidate the behavior of the cellular machinery, in which the physical and chemical components of the cell function

together to carry out sensing, processing, and migration. At the same time, biophysical approaches

have measured cellular sensing capacity in a quantitative manner (Hu et al., 2010; Thomas and

Eckford, 2016; Varennes and Mugler, 2016). Physical limits to the precision of sensing have been

investigated considering the biochemical nature of signal-receptor binding relations (Hu et al.,

2010; Varennes and Mugler, 2016). The effect of receptor crosstalk in enhancing the precision of

chemical sensing of multiple ligands has been demonstrated with quantitative modeling (Carballo-

Pacheco et al., 2019). In cellular signal processing, intracellular protein diffusion and activation

are critical to understanding the cellular sensory function (Soh et al., 2010). Not only the spatial

variation, but also the temporal relations were used to develop a better understanding and

physically predictable models (Gupta et al., 2020).

Cells are exposed to multiple cues whose chemical composition and physical nature are complex.

Cellular capability to process the multiple signals has been addressed in functional crosstalk

between either receptors or pathways (Hart et al., 2005; Lappano and Maggiolini, 2011; Shi and

Chen, 2017; Wang et al., 2011). The EGFR cascade, an example of RTK, cross-communicates

with the GPCR-mediated chemotaxis pathways in breast cancer (Hart et al., 2005). RTKs also

interplay with transforming growth factor-β (TGF-β) through Smad-dependent transcription, or

PI3K/AKT activation (Shi and Chen, 2017). The crosstalk at either the molecular or network level

is reflected in cellular responses. Mosadegh et al. showed that EGF was cooperative in mediating

breast cancer chemotaxis induced by SDF-1α gradient. (Mosadegh et al., 2008).In addition,

Uttamsingh et al. (Uttamsingh et al., 2008) showed a synergistic effect of EGF and TGF-β in

inducing invasion/migration capability in epithelial cells.

However, how cells transduce multiple signals is still poorly understood. This is a significant

knowledge gap since cells *in vivo* need to process complex chemical cues to determine the

migration direction. The question remains: Is there a limit to cellular capacity to process multiple

signals, and if so, what happens when cells exceed it?

In this study, we investigate the effects of the signal processing capacity of the cellular sensory

machinery on chemotaxis. Our central hypothesis is that chemotaxis performance is regulated by

the signal processing capacity of the cellular sensory machinery. This hypothesis is tested by

assessing chemotaxis of human breast cancer cells (MDA-MB-231) and murine pancreatic cells

(eKIC) under single or combined cues of TGF-β1 (denoted as TGF-β) and EGF by use of a

microfluidic platform. On the microfluidic platform, chemical cues of TGF-β and EGF are created

with different gradient strengths and background concentrations. Then, a minimal signal

processing machinery is modeled to address the experimental results. Using mathematical

modeling, we hypothesize that the saturation of the pathways after they converge downstream

limits the chemotactic performance. We further discuss the effects of signal processing on

chemotaxis to lay the groundwork of a general theoretical model. The model based on the

hypothesis reproduces the experimental results and predicts that the suppression of chemotactic

performance can alternatively be caused by saturating the shared pathway with background signal

strength. We confirm this prediction with further experiments on both cell lines. Our results

constitute a biophysical framework of cellular response to multiple inputs and suggest that cellular

capacity determines chemotactic accuracy under complex signals.

Results

The combination of TGF- β and EGF gradients is not synergistic for the chemotaxis of breast cancer cells

To understand the cell chemotactic response to multiple signals, we present gradient signals simultaneously using a microfluidic platform. The chemotaxis platform has been widely used to apply a chemical gradient to the cells embedded in the 3D extracellular matrix (Varennes et al., 2019; Wu et al., 2013). The platform is composed of three microfluidic channels, as shown in **Figure. 1A**. A center channel contains cells with a type I collagen matrix, supplementing nutrients from the two side channels of the source and sink filled with the basic culture medium. A chemical gradient is developed in the center channel by diffusion caused by a concentration difference between source and sink channels . We verify the concentration profiles by simulating the diffusion behaviors of TGF-β with 10kDa FITC-dextran (**Figure. 1A**). The concentration gradient is developed as a linear profile in the center channel, stably retained for more than 9 hours from 3 hours after perfusing FITC-dextran solution through the source channel while the sink channel is filled with FITC-dextran free medium. When we perfuse the FITC-dextran solution with the same concentration for both source and sink channels, the uniform concentration is quickly established in the platform (**Figure. 1A**).

By using the chemotaxis platform, we expose the cells to single or combined cues, track cells' migration, and analyze the chemotaxis characteristics of the cell trajectories to compute chemotactic index (CI) and speed (**Movie S1**, and **Figure.S1**). The CI is the cosine of the angle between a cell's displacement and the gradient direction for a trajectory, indicating chemotactic accuracy toward the gradient (**Figure. 1C**). The CI can range between -1 and 1. Higher CI indicates more accurate chemotaxis in response to an attractant. CI = 1 means that the cell perfectly follows

the gradient direction, whereas CI = 0 means that the cell is unbiased. The CI distribution of the

unbiased group of cells is U-shaped with a median of 0. In contrast, cell trajectories showing biased

motions exhibit a biased CI distribution toward 1 with a positive median (**Figure. 1D**).

The signal processing capacity of cells under multiple cues is anticipated to either synergistically

or antagonistically affect the cell chemotactic performance. To elucidate the effect of combined

cues on chemotaxis, we simultaneously expose both TGF-β and EGF gradients to the cells using

the chemotaxis platform.   We use a triple-negative breast cancer cell line, MDA-MB-231,

recognized as a highly metastatic cell type (Chavez et al., 2010). Chemotactic response of MDA-

MB-231 has been reported with several growth factors, including TGF-β and EGF (Varennes et

al., 2019; Wang et al., 2004). Our previous study reported that MDA-MB-231 cells were

significantly biased toward the TGF-β gradient direction (Varennes et al., 2019). Here, we

investigate four groups: no growth factor (control), a 50nM/mm TGF-β gradient, an 800nM/mm

EGF gradient, and the two gradients of TGF-β and EGF combined (**Figure 1B**; **Figure. 2**). In

control, we see that the cell migration shows random movement with uniformly distributed

migratory directions, whose CI distribution is U-shaped (**Figure. 2C gray**). On the other hand, the

CI distribution for cells with either the TGF-β or EGF gradient shows a biased distribution toward

1 with significantly higher median CIs compared to the control (**Figure. 2C red and blue**).

Surprisingly, the CI in response to the combined gradients decreases compared to the response to

each individual gradient (**Figure. 2C, purple**), demonstrating that combining the two gradients

has no synergistic effect on the CI.

It is a remarkable result since many studies have reported the functional cooperation of multiple

signals rather than the antagonism that we see here (Pang et al., 2016; Uttamsingh et al., 2008). In

fact, cells lose their chemotactic ability if the gradient strength is not sufficient. However, we

observe similar CI values when either TGF-β or EGF gradient is applied individually, even though

the gradient strengths are different from each other. This suggests that they are appropriately tuned

to their corresponding receptors. The observed lack of synergy is surprising also because TGF-β

and EGF bind to independent receptors on the cell surface: TGF-β binds to the TGF-β receptors,

which are transmembrane serine/threonine kinase complexes composed of type 1 and type 2

subunits (Ikushima and Miyazono, 2010); whereas EGF binds EGFR which is a receptor tyrosine

kinase superfamily (Han and Lo, 2012). Thus, the combined effect of TGF-β and EGF reflects

cellular signal processing, excluding an interplay in a receptor-binding level.

Interestingly, cells show significantly enhanced speed compared to control in both the individual

gradient cases and under the combined gradients (**Figure. 2D**). In fact, the cell speed is not

significantly enhanced with the combined gradients compared to the individual gradient cases.

This demonstrates that combining the gradients of two chemoattractants does not have a

synergistic nor antagonistic effect on the cell speed.

The multitasking response is not cell-type specific

To evaluate the cell-type dependency in cellular multitasking, we investigate multiple-cue

chemotaxis in pancreatic cancer cells. eKIC is used in this study, which is a murine pancreatic

cancer cell line. eKIC is driven by the genetically engineered mouse model having Kras and p16

mutations showing epithelial phenotype (Bradney et al., 2020; Seeley et al., 2009). The cell line is

known to be responsive to TGF-β, showing invasion features (Bradney et al., 2020). First, we

evaluate the migratory behaviors of eKIC in the chemotaxis platform as a control, excluding any

growth factors. The trajectories show an average CI close to 0, as shown in **Figure. 3** (gray). Then,

we expose a single cue of either a 10 nM/mm TGF-β gradient or a 200 nM/mm EGF gradient. We

find that the eKICs are highly responsive to both TGF-β gradient and EGF gradient (**Figure. 3**,

red and blue). Indeed, the median CI values are significantly enhanced in both gradient groups

compared to the control group. Interestingly, we observe the antagonism in eKIC in the presence

of the combined TGF-β and EGF gradients: the CI is significantly lower than the CIs of both

groups of a single gradient (**Figure. 3C**, purple). The speed is enhanced significantly compared to

the control (**Figure. 3D**), and again the speed under combined TGF-β and EGF gradients does not

show significant differences to the speeds in single gradient groups, neither TGF-β nor EGF

gradient. These results indicate that the lack of synergy in the chemotactic performance is not cell-

type-specific responses. Instead, the present results suggest that the cell's multitasking response

might be governed by physical principles rather than cell-type-specific details.

The multitasking response cannot be explained by mutual repression but can be explained by a shared pathway

Because TGF-β and EGF bind to different receptors (Han and Lo, 2012; Ikushima and Miyazono, 2010), the fact that combining both signals suppresses the CI is not due to receptor saturation, but rather due to the signaling network downstream. To understand this effect, we turn to mathematical modeling. We suppose that the migratory response is ultimately governed by an internal molecular species M. In order for the TGF-β or EGF gradient to be translated into biased migration, there must be a difference in the concentration of M between the front and back halves of the cell (Ellison et al., 2016). Therefore, we take this difference Δm to be a proxy for the CI (**Figure. 4A**). We have seen that the cell speed increases significantly in the presence of either TGF-β or EGF (**Figure. 2D** and **3D**). Therefore, we take the average concentration of M in both halves of the cell, m, to be a proxy for speed (**Figure. 4A**). In principle, the speed could also depend on the bias Δm. However, we have checked experimentally that cell speed for a given background level of TGF-β or EGF is not significantly different whether the corresponding gradient is present or not (**Figure. S2**). Thus, we take speed to be a function of m alone. It now remains to propose a model of the signaling network connecting TGF-β and EGF to M that can explain the data.

A straightforward hypothesis for the observed antagonism in the CI is the presence of mutual repression: TGF-β activates M through pathway one, and EGF activates M through pathway two, but TGF-β also represses pathway two and vice versa. A minimal example of such a mutually repressive network is shown in **Figure. 4B**. Here we have introduced species X and Y, which are the targets of the repression, and dimensionless parameters $\eta_X, \eta_Y, \mu_T, \mu_E, \beta_T$, and β_E which define the strength of the edges. Writing down the rate equations for this network and solving for the steady-state, we find

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$$m \propto \frac{\eta_X (1+\mu_T)}{1+\beta_E} + \frac{\eta_Y (1+\mu_E)}{1+\beta_T}$$

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$$\Delta m \propto \frac{\eta_X (\mu_T - \beta_E)}{(1+\beta_E)^2} + \frac{\eta_Y (\mu_E - \beta_T)}{(1+\beta_T)^2} \quad (1)$$

where the dimensionless parameters are defined in terms of the reaction rates (see **Method**

details). These expressions apply to the case where both signals are present, while specific limits

apply to the case where only the TGF-β gradient is present ($\mu_E = \beta_E = 0$), the case where only the

EGF gradient is present ($\mu_T = \beta_T = 0$), and the control ($\mu_T = \beta_T = \mu_E = \beta_E = 0$).

To investigate whether this model can explain the data in **Figures. 2** and **3**, we focus on parameters

for which Δm is smaller when both gradients are present than when either is present alone (**Figures.**

2C and **3C**). The result, averaged over all such parameters (see **Method details**), is shown in

Figure. 4C, and we see that this model can explain an antagonistic effect on the CI. However, for

these same parameters, we also see an antagonistic effect on m in **Figure. 4D**, which is inconsistent

with the speed data in **Figures. 2D** and **3D**. The reason that antagonism for Δm and m coincide in

this model is that the mutual repression suppresses the front-back bias in the output molecule M

by suppressing the production of M itself. We conclude that crosstalk cannot explain the data.

We, therefore, put forward an alternative hypothesis that the antagonism in the CI is due to a shared

signaling pathway. Specifically, if the pathways by which TGF-β and EGF activate M converge at

a certain point, it could be that the shared pathway is saturated when both signals are present, but

not when each signal is present alone. A minimal example of such a network is shown in **Figure.**

4E. Here X is the shared component, and TGF-β and EGF catalyze the reversible conversion of X

to an activated state X^*, which produces M. The presence of a convertible species introduces the

possibility of saturation, where all X molecules have been converted to the X^* state, and no further

conversion can occur. The dimensionless parameters η_T and η_E define the strengths of the

catalysis reactions, and μ defines the degree to which the conversion reaction is unsaturated (

$\mu \to 0$) or saturated ($\mu \to 1$). Again, writing the rate equations and solving for the steady-state,

we find

$$m \propto \frac{\mu + \eta_T + \eta_E}{1 + \eta_T + \eta_E}$$

$$\Delta m \propto \frac{(1 - \mu)(\eta_T + \eta_E)}{(1 + \eta_T + \eta_E)^2} \qquad (2)$$

where η_T, η_E and μ are defined in terms of the reaction rates, and the limiting cases are the same

as those in Eq. 1. Again, averaging over all parameters for which Δm is smaller with both

gradients than with either alone (Method details), we see that this model can explain both

antagonism for the CI (**Figure. 4F**) and a lack of antagonism for the speed (**Figure. 4G**),

consistent with the data in **Figures. 2** and **3**. The reason that antagonism occurs for Δm but not m

in this model is due to the saturation: as all X molecules become converted to the X^* state, the

difference in the concentration of M molecules from front to back vanishes, while the total

concentration of M molecules remains high. The saturation causes loss of synergy in the value

(m), but it causes antagonism in the slope (Δm). Because gradient sensing depends on the slope

(Δm), a value-saturating function causes slope-antagonism, which indicates a saturation of signal

processing capacity. This can be understood by thinking about what happens to Δm when m is

close to saturation. In our system when only one gradient is present, m is away from saturation,

so there is a large Δm. But if both gradients are applied simultaneously, then m is close to the

saturating value, and Δm is small. Because the response depends on the difference Δm in

molecule number between the front and back of the cell, the decrease in Δm is sufficient to

explain the antagonism behavior in cells. We conclude that the saturation of a shared pathway

can explain the data.

The shared pathway model successfully predicts the cellular response to elevated signal background

The key mechanism behind the shared pathway model is that the presence of a second gradient signal brings the shared pathway too close to its saturation point and therefore reduces the chemotactic bias while not reducing the speed. Given this mechanism, the model makes an important prediction: the second signal need not be graded to bring the shared pathway to its saturation point. Indeed, we see in **Figure. 5** that if the TGF-β gradient is combined with a uniform EGF background alone, then the bias Δm is reduced (**Figure. 5A**, black), whereas the average m is not (**Figure. 5B**, black). In fact, the model also makes a second prediction: the elevated background need not even come from the other signal; it could come from the same signal. Indeed, we also see that if the TGF-β gradient is combined with an additional uniform TGF background, then the bias Δm is reduced (**Figure. 5A**, maroon) whereas the average m is not (**Figure. 5B**, maroon).

To test these predictions, we expose each cell type to its respective TGF-β gradient as in **Figures. 2 and 3**, combined with a uniform EGF background (equal to the EGF concentration in the center of the device in **Figures. 2 and 3**). We see that in both cases, the CI is significantly suppressed (**Figure. 5C**, black), whereas the speed is not (**Figure. 5D**, black), as predicted. Then, we expose each cell type to the TGF-β gradient combined with a uniform TGF-β background concentration. Again, we see that in both cases, the CI is significantly suppressed (**Figure. 5C**, maroon), whereas the speed is not (**Figure. 5D**, maroon), as predicted. These results support the hypothesis that the growth factors are saturating a shared signaling pathway, and therefore that the capacity of the cell to multitask is being exceeded.

274   Notably, the mutual repression model makes predictions in these two cases that are distinct from

275   those of the shared pathway model and, therefore, inconsistent with the data (**Figure. S3**).

Discussion

We have investigated cellular multitasking capacity in the context of the migratory response to simultaneous growth factor gradients in a 3D microfluidic environment. Surprisingly, for two different cell types, we have found that the chemotactic bias is suppressed below that for either growth factor alone, whereas the cell speed remains high. Because the growth factors bind to separate receptors, the suppression is not a consequence of simple receptor saturation, rather must result from the signaling network downstream. Using mathematical modeling, we have found that the suppression cannot be explained by a network with mutually repressive crosstalk but can be explained by the convergence to a shared pathway. Our shared pathway model has predicted that the chemotactic bias, but not speed, can be alternatively suppressed by elevating the background level of either growth factor, which our experiments have confirmed. Our results emphasize the fact that the quantitative features, not just the topological features of a signaling network, are necessary to understand a behavioral response, especially a counterintuitive response such as antagonism.

The model successfully predicts the cellular response regardless of cell type. This suggests that chemotaxis is critically moderated by not only specific environmental cues and cell-type-specific biochemistry, but also the intrinsic cell capability to process information within an inherently limited channel. Indeed, genetic mutations commonly observed in cancer cells strongly affect the migration by promoting the invasion process via specific signaling pathways such as Snail and Twist (Muller et al., 2011). Yet, the present results show that the cell response could be predicted from our framework regardless of the cancer type, implying that cellular multitasking capacity is not a cancer type-specific signaling effect.

The antagonistic response to two signals in the model results from the saturation of a shared

pathway. In this saturating regime, we have seen that the model explains the experimental data and

makes predictions that our further experiments confirmed. Yet, the model also predicts more

conventional synergistic behavior outside the saturating regime. Specifically, defining an

amplification factor $\alpha = \eta_T + \eta_E$ and a relative pathway strength $\rho = \eta_T/\eta_E$ in terms of the

parameters of Eq. 2, we see in **Figure. 6A** that the model supports both antagonistic and synergistic

regimes (see **Method details**). Intuitively, antagonism arises when each individual pathway is

amplified ($\alpha \gg 1$) and the two pathways are balanced ($\rho \sim 1$), as illustrated in **Figure. 6B**. In

contrast, synergy arises when the amplification is not as strong, as then the shared pathway is not

saturated, and the capacity of the channel is not exceeded.

The fact that the proposed signaling mechanism supports either antagonism or synergy may help

explain why previous work has observed synergistic effects between growth factors, including

TGF-β and EGF. Both of these growth factors have been identified to regulate cell invasiveness

and motility (Hou et al., 2012; Moustakas and Heldin, 2008; Roussos et al., 2011), with TGF-β in

particular known to promote epithelial-mesenchymal transition, which is a critical step in cancer

invasion (Ikushima and Miyazono, 2010; Moustakas and Heldin, 2008). In fact, TGF-β is generally

considered a cooperative effector when it combines with other growth factors (Pang et al., 2016;

Uttamsingh et al., 2008). Most notably, Uttamsingh, et al. reported that the roles of TGF-β- and

EGF-mediated signaling pathways combine synergistically in inducing cell invasion and migration

(Uttamsingh et al., 2008). However, it is important to note that this study focused on motility and

invasiveness, not directional bias, and indeed here, we do not observe an antagonistic effect on

cell speed. This comparison emphasizes the need to distinguish directional and non-directional

measures of cell motility, as well as the difference between cell-intrinsic motility factors and the

physical aspects of the signaling environment (Clark and Vignjevic, 2015; Endres and Wingreen,

2008; Varennes et al., 2019). Our discovery of antagonism by the cellular capacity suggests the

necessity of a quantitative approach to multiple-cue cell migration studies.

Both TGF-β and EGF are secreted by stromal cells, which typically surround the solid tumors.

(Bulle and Lim, 2020; Roussos et al., 2011; Shibue and Weinberg, 2017) Thus, we anticipate that

these growth factors are usually imposed along with the aligned directions. However, considering

the spatial and temporal heterogeneity of tumor tissue structure, it may depend on the tumor

structure and development stage. The other scenarios for the gradient alignments could be further

investigated with the controllable microfluidic platform, for example, by imposing conflicting

gradients. Nonetheless, the present study provides insight into how combined gradients of multiple

growth factors in the tumor microenvironment could affect cancer cell migration behavior.

Our framework proposes that two receptor-activated signaling pathways converge to a single

pathway to promote migration (**Figure. 6B**), and there is ample biochemical evidence that this

structure is plausible. From a general standpoint, although many signaling pathways regulate

chemotaxis (Charest and Firtel, 2007; Chung et al., 2001; Gandalovičová et al., 2016; Stuelten et

al., 2018), all must converge to activate a set of common cellular responses, including actin

polymerization and organization, cytoskeleton dynamics, and adhesion (Roussos et al., 2011;

Swaney et al., 2010; Van Haastert and Devreotes, 2004). More specifically, complex signaling

pathways are known to converge onto central functional molecules (idealized in our model by the

species X) such as PIP_3 in *Dictyostelium*, cofilin in breast carcinoma cells (Swaney et al., 2010),

Rho GTPases, Smad-dependent transcription, or PI3K/AKT activation cascades (Charest and

Firtel, 2007; Chung et al., 2001; Corallino et al., 2018; Hart et al., 2005; Lappano and Maggiolini,

2011; Li et al., 2013; Miyagawa et al., 2018; Shi and Chen, 2017; Swaney et al., 2010).

Our results suggest that the antagonistic response to two gradient signals in these cells is due to

saturation of the sensory pathway. However, well-characterized networks in other sensory

systems, such as the bacterial chemotaxis network, avoid saturation by adapting their operating

point to the background concentration (Alon et al., 1999; Mello and Tu, 2007). This adaptation

relies on a timescale separation between effector phosphorylation and receptor methylation that,

for whatever reason, may be difficult to achieve in the cells studied here. Alternatively, the growth

factor concentrations at which saturation sets on in our system may be outside of the physiological

range to which these cells are typically exposed. Further characterization of the sensory network

is needed to shed light on the question of adaptation in these cells.

Limitations of study

Although the biophysical framework is capable of illustrating the cellular multitasking capacity

shown in the experiments, further research is warranted. The present framework may limit the

explanation regarding a mode of migration. The physical constraints driven by the extracellular

matrix (ECM) regulates features of cell migration as well. Since the chemotactic response and the

relevant signaling pathways inducing chemotaxis could be varied depending on the mode of the

migration (Clark and Vignjevic, 2015; Gandalovičová et al., 2016), the model may be improved

further by considering migration modes highly regulated by physical confinement.

Acknowledgments

This work was partially supported by grants from the National Institutes of Health (R01 CA

254110 and P30 CA023168). Publication of this article was funded in part by Purdue University

Libraries Open Access Publishing Fund.

Author contributions

AM and BH conceived the idea. HM and SS performed the research and acquired the data. All

authors discussed the results and wrote the manuscript.

Declaration of interests

The authors declare no competing interests.

Inclusion and diversity

We worked to ensure diversity in experimental samples through the selection of the cell lines. The

author list of this paper includes contributors from the location where the research was conducted

who participated in the data collection, design, analysis, and/or interpretation of the work.

Figures

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Figure. 1. Chemotaxis platform and chemotaxis characteristics. (A) Schematic description of a

microfluidic chemotaxis platform to induce the chemical gradient. 10kDa FITC dextran (simulating TGF-

β) develops a linear profile when supplied at the sink channel, or a uniform profile when supplied at both

channels in the chemotaxis platform. (B) Representative micrographs of MDA-MB-231 cells with their

trajectories for 9 hours. (C) Characterization of the measured cell trajectory. (D) Schematics of angular (θ)

distribution of cell trajectories and corresponding chemotactic index (CI) distributions of unbiased (gray)

and biased motions (blue).

Figure. 2.Chemotactic performance of breast cancer cells is not synergistically augmented when TGF-β and EGF gradients are simultaneously imposed. (A) Cell trajectories of a representative sample for control, 50nM/mm TGF-β gradient (∇T), 800nM/mm EGF gradient (∇E), and combined gradients of 50nM/mm TGF-β with 800nM/mm EGF (∇T+∇E) collected for 9 hours. Trajectories in a sample include >35 cells. (B) Angular (θ) distribution of cell trajectories from a representative sample for control (gray), ∇T(red), ∇E(blue), and ∇T+∇E(purple). (C) Distribution of chemotactic index (CI) from all trajectories collected from experimental trials (N>3) including 158-233 trajectories per condition. Box represents quartiles with a median line in the middle of the box. (D) Distribution of speed with a median line from all collected trajectories. Box: interquartile range (IQR) ± 1.5 IQR whiskers. A dot represents data from a single trajectory. (***: p<0.001, N.S: no significance with p>0.05 in Mann-Whitney test) (See also Figure S1.)

Figure. 3. Antagonism of pancreatic cancer cells in the combined signal environment. (A) Cell trajectories of a representative sample for control, 10nM/mm TGF-β gradient (∇T), 200nM/mm EGF gradient (∇E), and combined gradients of 10nM/mm TGF-β with 200nM/mm EGF (∇T+∇E) collected for 3 hours. Trajectories in a sample include >35 cells. (B) Angular (θ) distribution of cell trajectories from a representative sample for control (gray), ∇T(red), ∇E(blue), and ∇T+∇E(purple). (C) Distribution of chemotactic index (CI) from all trajectories collected from experimental trials (N>3) including >100 trajectories per condition, respectively. Box represents quartiles with a median line in the middle of the box. (D) Distribution of speed from all collected trajectories. Box: interquartile range (IQR) ± 1.5 IQR whiskers with a median line. A dot represents data from a single trajectory. (***: p<0.001, N.S: no significance with p>0.05 in Mann-Whitney test) (See also Figure S1.)

Figure. 4. Mathematical model explains antagonism by saturation of a shared pathway. (A) In the model the cell speed and chemotactic index (CI) scale with the concentration m of an intracellular species M, and its concentration difference Δm between the front and back of the cell, respectively. (B) In the mutual repression model, TGF-β and EGF mutually repress the other's activation pathway. (C) Δm exhibits antagonism (the response to both gradients is smaller than that of either alone). (D) m also exhibits antagonism. (E) In the shared pathway model, TGF-β and EGF convert a common component to its active state. (F) Δm exhibits antagonism. (G) m does not exhibit antagonism. Only the shared pathway results are consistent with the data in Figures. 2 and 3. C, D, F, and G each shows results averaged over parameter space (see **Method details**) and normalized by the TGF-β gradient case (red). (See also Figure S2.)

Figure. 5. Model predicts and experiments confirm that elevated signal background reduces chemotactic bias but not speed. The model predicts that (A) the bias Δm decreases when a TGF-β gradient is combined with a uniform background of either EGF or TGF-β, whereas (B) the average m does not. (See also Figure S3.) Experiments confirm that for either cell type, (C) the chemotactic index (CI) is significantly suppressed when the TGF-β gradient is combined with a uniform background of either EGF or TGF-β, whereas (D) the speed is not, consistent with the predictions. (*: p<.05, **: p<.01 in Student t-test). In all panels, the values are normalized by the TGF-β gradient case (red). The model uses Eq. 4 with $\Delta e = 0$ (EGF background) or $\{e = 0, \Delta e = 0, t \rightarrow 10t\}$ (TGF background) and the same parameters as in Figure. 4. The experiment uses the same TGF-β gradient as in Figures. 2 and 3 (50 nM/mm for MDA-MB-231, 10 nM/mm

for eKIC) combined with either uniform EGF (400 nM for MDA-MB-231, 100 nM for eKIC) or uniform

TGF-β (200 nM for MDA-MB-231, 50 nM for eKIC). In experiment, bar represents mean of the medians

± S.E (n≥3). The medians are collected from >35 trajectories in a sample, respectively. (*: p<0.05, **:

p<0.01, and N.S: no significance with p>0.05 in student's t-test) (See also Figure S1.)

Figure. 6. Schematic of cellular multitasking capacity for chemotaxis. (A) The shared pathway model

predicts antagonism in the chemotactic response (as in the experiments) for large amplification factor α and

balanced relative pathway strength ρ, but synergy in the response for small α (see **Method details** for phase

boundaries). (B) Illustration of α and ρ in the general context of a signaling network defined by pathway

convergence.

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STAR METHODS

KEY RESOURCE TABLE

Chemicals and recombinant proteins

Experimental models: Cell lines

Software and algorithms

RESOURCE AVAILABILITY

Lead contact

Further information and requests for resources and reagents should be directed to and will be

fulfilled by the lead contact, Bumsoo Han (bumsoo@purdue.edu).

Materials availability

This study did not generate new unique reagents.

Data and code availability

All data reported in this paper will be shared by the lead contact upon request.

All original code has been deposited at Zenodo and is publicly available as of the date of

publication. DOIs are listed in the key resources table.

Any additional information required to reanalyze the data reported in this paper is available from

the lead contact upon request.

EXPERIMENTAL MODEL AND SUBJECT DETAILS

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Cell lines

A human breast cancer cell line (MDA-MB-231) and a murine pancreatic cell line (eKIC) were

used in this study. MDA-MB-231 cells (ATCC, VA, USA) were maintained in Dulbecco's

Modified Eagle Medium/Ham's F-12 (Advanced DMEM/F-12, Lifetechnologies, CA, USA)

supplemented with 5% v/v fetal bovine serum (FBS), 2 mM L-glutamine (L-glu), and 100 µg ml^{-1}

penicillin/streptomycin (P/S). eKIC was obtained from Dr. Murray Korc's laboratory at the

Indiana University. eKIC was isolated from KIC mice, which were established as a genetically

engineered mouse model of PDAC (GEM). For the KIC mice, *Kras* was combined with the

deletion of the *Ink4a* locus (*Ink4a/Arf$^{L/L}$*) to generate the *Pdx1-Cre;LSL-Kras^{G12D};Ink4a/Arf$^{-/-}$*

GEM (Sempere et al., 2011; Whipple et al., 2011). The eKIC cells were cultured in RPMI 1640

with 2.05mM L-glutamine (GE Healthcare Bio-Sciences Corp., MA, USA) supplemented by 5%

v/v fetal bovine serum (FBS) and 100 µg ml^{-1} penicillin/streptomycin (P/S). Both MDA-MB-231

and eKIC cells were regularly harvested by 0.05% trypsin and 0.53mM EDTA (Lifetechnologies,

CA, USA) when grown to ~80% confluency in 75 cm^2 T-flasks and incubated at 37°C with 5%

CO$_2$. The harvested cell suspensions were used for experiments or sub-cultured. Both cells were

maintained below 15th passage while regularly kept in cryopreservation.

METHOD DETAILS

Chemotaxis assay

For the chemotaxis assay, cells were implanted in the chemotaxis platform, which is an *in vitro*

microfluidic device developed to engineer the chemical environment.as shown in **Figure. 1A**. The

chemotaxis platform was designed for engineering the chemical environment surrounding the cells

embedded in the 3D extracellular matrix. The platform is composed of three microfluidic channels

with 100µm in thickness. A center channel of 1mm wide, which aims to contain cells with a

collagen matrix, is located in between source (top) and sink (bottom) channels with 300µm wide.

At the end ports, the source and sink channels are connected to large reservoirs so that the culture

medium can be supplemented through the channels. For the cell culture, the basic culture medium

is filled in both source and sink channels. In order to develop a concentration gradient in the center

channel, growth factor solution (TGF-β or EGF) based on the medium is added through the source

channel. On the other hand, the sink channel is filled with growth factor-free medium. Assuming

that there is neither flow nor any pressure differences between the channels, the concentration of

the given growth factor (*i*) can be illustrated by the conservation equation of chemical species:

506
$$\frac{\partial C_i}{\partial t} = D_i \cdot \nabla C_i$$

At the steady state, the concentration profile in the center channel goes to a linear. The linear

profile can persist for a while with an assumption that is the concentration at the source and side

channels are constant with a large volume of reservoirs. Consequently, cells cultured in the

collagen matrix are exposed to a linear gradient of a specific soluble factor. The detailed technique

to develop the microfluidic device and the diffusion principle in the platform was described in our

previous study (Varennes et al., 2019).

Cells were embedded uniformly to type I collagen mixture (Corning Inc., NY, USA) supplemented

with 10X PBS, NaOH, HEPE solution, FBS, Glu, P/S, and cell-culture level distilled water. Initial

cell density was consistently 5×10^5 cells/ml for MDA-MB-231 and 8×10^5 cells/ml for eKIC

respectively in the 2mg/ml type I collagen mixture. The cell-collagen mixture was loaded in the

center channel of the microfluidic device. After loading, the cells in the collagen matrix were

cultured with basic mediums for 24 hours. MDA-MB-231 cells were then exposed by serum-

reduced medium for another 24 hours. The serum-reduced medium was supplemented by 1% v/v

FBS instead of 5% v/v FBS in the basic medium. Due to a critical viability change in the serum-

reduced culture condition (data is not shown), serum starvation was not conducted for eKIC. Then,

cells were exposed by concentration gradients of growth factors, either Transforming growth factor

beta-1 (TGF-β1, Invitrogen, CA, USA) or epidermal growth factor (EGF, Invitrogen, CA, USA).

Characterization of cell migration

Live-cell imaging technique with time-lapse microscopy was used to characterize cell migration.

An inverted microscope (Olympus IX71, Japan) was equipped with a stage top incubator as

described in (Varennes et al., 2019), which maintain the microfluidic chemotaxis platform at 37ºC

with 5% CO_2 environment during imaging. MDA-MB-231 cells in the chemotaxis platform were

captured every 15 minutes for 9 hours. eKIC cells were captured every 5 minutes for 3 hours. The

temporal intervals and durations for the time-lapse imaging were optimized for each cell line by

considering the cell motility, ~12μm/h for MDA-MB-231 and ~50μm/h for eKIC in control,

respectively (**Figure. 2D and 3D**). In both cases, the time-lapse imaging was started 3 hours after

applying the growth factors for sufficient adjusting time to develop gradient profiles accordingly

(**Figure. 1B**). The bright-field images were further processed to analyze cell migration. The cell

area was defined by using the contrast differences between cells and background and converted to

monochrome images by using ImageJ. A cell trajectory was illustrated as a collection of the

centroid positions of cell areas at different time points. In tracking the cell movement, we excluded

the cells undergoing division to avoid extra effect for cell polarity (Harley et al., 2008). Also, we

excluded the stationary cells defined when the cells moved less than their diameter.

Biased cell motion is commonly characterized by directional accuracy, persistence, and motility

(Endres and Wingreen, 2008; Roussos et al., 2011; Skoge et al., 2014; Varennes et al., 2019). In

our previous study (Varennes et al., 2019), we have shown that the directional accuracy is a

dominant metric in the chemotaxis of the 3D cultured cells migrating in ECM whereas cell

persistence is barely changed by the chemical gradient. In this study, we therefore focus on

accuracy and motility, not persistence.

We measure directional accuracy y with the commonly used chemotactic index (CI) (Endres and

Wingreen, 2008; Skoge et al., 2014)

$$CI = \cos\theta$$

where θ is the angle between the net displacement of a trajectory and the gradient direction. The

displacement is defined as a straight line connecting the initial and final points of a trajectory where

we measure each trajectory for 9 hours for MDA-MB-231 and 3 hours for eKIC (**Figure. S1B**). In

an experimental trial, multiple cells' CI values are distributed throughout the range of -1 to 1 due

to variations of cell response to the attractant. The CI distribution is U-shaped without any

attractant, indicating that the cell migration directions are uniformly distributed; in contrast, the CI

distribution with an attractant shows a biased distribution toward 1 (**Figure. 1D**) (Varennes et al.,

2019).

Cell motility is quantified as an instantaneous speed along the cell trajectory:

$$\text{Cell speed} = \frac{Path \text{ of a trajectory}}{Duration}$$

where the cell path is taken from a trajectory where measurement is taken every $\Delta t = 15$ minutes.

Defining the mathematical models and deriving the equations in the main text

For the mutual repression network in **Figure. 4B**, denoting the concentrations of TGF-β, EGF, X,

and Y as t, e, x, and y, respectively, the rate equations are

568
$$\frac{dx_i}{d\tau} = k_X + k_{TX}t_i - \left(v_X + v_{EX}e_i\right)x_i$$

569
$$\frac{dy_i}{d\tau} = k_Y + k_{EY}e_i - \left(v_Y + v_{TY}t_i\right)y_i$$

570
$$\frac{dm_i}{d\tau} = k_{XM}x_i + k_{YM}y_i - v_M m_i$$

where $i = 1, 2$ denotes the front or back half of the cell, τ is time, k and v denote production and

degradation rates, respectively, and activation and repression are modeled as a linear dependence

of production and degradation on the regulator, respectively. In steady state, the solution takes the

form $m_i = f\left(t_i, e_i\right)$, where f follows algebraically from the rate equations. Because the changes

in TGF-β and EGF concentrations across the cell, $\Delta t = t_2 - t_1 = R\nabla T$ and $\Delta e = e_2 - e_1 = R\nabla E$, are

much smaller than the average concentrations, $t = \left(t_1 + t_2\right)/2$ and $e = \left(e_1 + e_2\right)/2$, for all but the

cells that are within a few cell radii R from the sink channel of the device, the average

$m = \left(m_1 + m_2\right)/2$ and difference $\Delta m = m_2 - m_1$ can be approximated as

579
$$m \approx f\left(t, e\right) = \frac{k_{XM}\left(k_X + k_{TX}t\right)}{v_M\left(v_X + v_{EX}e\right)} + \frac{k_{YM}\left(k_Y + k_{EY}e\right)}{v_M\left(v_Y + v_{TY}t\right)}$$

581
$$\Delta m \approx \frac{\partial f}{\partial t} \Delta t + \frac{\partial f}{\partial e} \Delta e$$

$$= \frac{k_{XM} \left[k_{TX} v_X \Delta t - v_{EX} k_X \Delta e + k_{TX} v_{EX} \left(e\Delta t - t\Delta e \right) \right]}{v_M \left(v_X + v_{EX} e \right)^2} + \frac{k_{YM} \left[k_{EY} v_Y \Delta e - v_{TY} k_Y \Delta t + k_{EY} v_{TY} \left(t\Delta e - e\Delta t \right) \right]}{v_M \left(v_Y + v_{TY} t \right)^2}$$

582   We nondimensionalize these expressions by defining the concentration scale

583
$$m_0 = \frac{k_X k_{XM}}{v_X v_M} + \frac{k_Y k_{YM}}{v_Y v_M}$$

584   and dimensionless ratios

585
$$\varepsilon_T = \frac{\Delta t}{t}; \quad \varepsilon_E = \frac{\Delta e}{e}; \quad \eta_X = \frac{k_X k_{XM}}{m_0 v_X v_M}; \quad \eta_Y = \frac{k_Y k_{YM}}{m_0 v_Y v_M};$$

586
$$\mu_T = \frac{k_{TX} t}{k_X}; \quad \mu_E = \frac{k_{EY} e}{k_Y}; \quad \beta_T = \frac{v_{TY} t}{v_Y}; \quad \beta_E = \frac{v_{EX} e}{v_X}$$

587   with which they become

588
$$\frac{m}{m_0} = \frac{\eta_X \left(1 + \mu_T \right)}{1 + \beta_E} + \frac{\eta_Y \left(1 + \mu_E \right)}{1 + \beta_T}$$

589
$$\frac{\Delta m}{m_0} = \frac{\eta_X \left[\varepsilon_T \mu_T - \varepsilon_E \beta_E + \mu_T \beta_E \left(\varepsilon_T - \varepsilon_E \right) \right]}{\left(1 + \beta_E \right)^2} + \frac{\eta_Y \left[\varepsilon_E \mu_E - \varepsilon_T \beta_T + \mu_E \beta_T \left(\varepsilon_E - \varepsilon_T \right) \right]}{\left(1 + \beta_T \right)^2}$$

590   Because both the TGF-β and EGF concentrations are zero at the sink channel (without the elevated

591   backgrounds), we have $t = d\nabla T$, $\Delta t = R\nabla T$, $e = d\nabla E$, and $\Delta e = R\nabla E$, where d is the distance

592   of the cell from the sink, and R is the cell radius. Therefore, we see that $\varepsilon_T = \varepsilon_E \equiv \varepsilon$, and the

593   previous equation simplifies to

$$\frac{\Delta m}{\varepsilon m_0} = \frac{\eta_X \left(\mu_T - \beta_E \right)}{\left(1 + \beta_E \right)^2} + \frac{\eta_Y \left(\mu_E - \beta_T \right)}{\left(1 + \beta_T \right)^2}$$

595   These expressions for m and Δm are reproduced in Eq. 1 of the main text.

597   For the shared pathway network in **Figure. 4E**, the rate equations are

$$\frac{dx_i^*}{d\tau} = \left(k_X + k_{TX} t_i + k_{EX} e_i \right) \left(x_0 - x_i^* \right) - v_X x_i^*$$

$$\frac{dm_i}{d\tau} = k_{XM} x_i^* - v_M m_i$$

600   (3)

601   where x_0 is the total concentration of X and X^* molecules, which we assume to be constant and

602   equal in both halves of the cell. In steady state we have

$$m = \frac{k_{XM} x_0}{v_M} \left(\frac{k_X + k_{TX} t + k_{EX} e}{v_X + k_X + k_{TX} t + k_{EX} e} \right)$$

$$\Delta m = \frac{v_X k_{XM} x_0}{v_M} \left[\frac{k_{TX} \Delta t + k_{EX} \Delta e}{\left(v_X + k_X + k_{TX} t + k_{EX} e \right)^2} \right]$$

605   where we have applied the same approximations as in the mutual repression model. We

606   nondimensionalize these expressions by defining the concentration scale

$$m_0 = \frac{k_M x_0}{v_M}$$

608   and dimensionless ratios

609
$$\eta_T = \frac{k_{TX}t}{v_X + k_X}; \quad \eta_E = \frac{k_{EX}e}{v_X + k_X}; \quad \mu = \frac{k_X}{v_X + k_X}$$

610   with which they become

611
$$\frac{m}{m_0} = \frac{\mu + \eta_T + \eta_E}{1 + \eta_T + \eta_E}$$

612
$$\frac{\Delta m}{\varepsilon m_0} = \frac{(1-\mu)(\eta_T + \eta_E)}{(1 + \eta_T + \eta_E)^2}$$

where again we take $\dot{o}_T = \dot{o}_E \equiv \dot{o}$ as above. These expressions are reproduced in Eq. 2 of the main

text.

<u>Parameter selection in the mathematical models</u>

In the mutual repression model, we sample the ratios η_X, η_Y, μ_T, μ_E, β_T, and β_E

logarithmically in the range $\left[10^{-3}\ 10^3\right]$ and accept each sample if Δm is smaller than (i) its value

with only the TGF-β gradient ($\mu_E = \beta_E = 0$) and (ii) its value with only the EGF gradient (

$\mu_T = \beta_T = 0$), (iii) and both i and ii are positive. The result, averaged over 10^7 samples, is shown

in **Figure. 4C** and **D**.

In the shared pathway model, we sample the ratios η_T and η_E logarithmically in the range

$\left[10^{-3}\ 10^3\right]$ and μ uniformly in the range $\left[0\ 1\right]$, and accept each sample if Δm is smaller than (i)

its value with only the TGF-β gradient ($\eta_E = 0$) and (ii) its value with only the EGF gradient (

$\eta_T = 0$), (iii) and both i and ii are positive. The result, averaged over 10^7 samples, is shown in

Figures. 4F and **G** and **5A** and **B**. єε

Derivation of the phase diagram in Figure. 6A

The boundaries in the phase diagram in **Figure. 6A** follow from the expression for Δm in Eq. 2

of the main text as

632
$$\frac{(1-\mu)(\eta_T+\eta_E)}{(1+\eta_T+\eta_E)^2} < \frac{(1-\mu)\eta_T}{(1+\eta_T)^2}; \quad \frac{(1-\mu)(\eta_T+\eta_E)}{(1+\eta_T+\eta_E)^2} < \frac{(1-\mu)\eta_E}{(1+\eta_E)^2}$$

633 where the righthand sides are the cases with only the TGF-β gradient ($\eta_E=0$) and only the EGF

634 gradient ($\eta_T=0$), respectively. If both conditions are true, it is antagonism; if neither is true, it is

635 synergy. Defining the amplification factor and relative pathway strength

636
$$\alpha = \eta_T + \eta_E; \quad \rho = \frac{\eta_T}{\eta_E}$$

637 as in the main text, or equivalently

638
$$\eta_T = \frac{\alpha\rho}{1+\rho}; \quad \eta_E = \frac{\alpha}{1+\rho}$$

639 the conditions become

640
$$\frac{\alpha}{(1+\alpha)^2} < \frac{\alpha\rho}{(1+\rho)\left(1+\frac{\alpha\rho}{1+\rho}\right)^2}; \quad \frac{\alpha}{(1+\alpha)^2} < \frac{\alpha}{(1+\rho)\left(1+\frac{\alpha}{1+\rho}\right)^2}$$

641 which simplify to

642
$$\alpha > \sqrt{1+\rho^{-1}}; \quad \alpha > \sqrt{1+\rho}$$

These curves are plotted in **Figure. 6A**.

QUANTIFICATION AND STATISTICAL ANALYSIS

In evaluating the chemotactic characteristics, more than 30 trajectories were analyzed in an

experimental trial, which was repeated at least three times for all experimental groups. Each

trajectory produced a value of CI and speed. All collected CIs and speeds in each group were

reported in the box plots. A data point in the box plots indicates each metric of a cell trajectory

showing the distribution characteristics of the metric in a group. Differences in median CIs and

speeds presented in the box plots were statistically analyzed by Mann-Whitney U-test. The

significant changes between comparisons were examined when the p value <0.05. To evaluate the

chemotactic accuracy and cell motility, medians of CIs and speeds from the repetitions (n>3) were

averaged and reported in a bar with an error bar representing a standard estimated error (S.E.).

Differences in CIs presented in the bar graphs were statistically analyzed by student t-test. The

significant changes between comparisons were examined when the p value < 0.05.

Movie S.1 Time-lapse of cell migration, Related to Figure1.

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    SUPPLEMENTAL INFORMATION

Figure. S1. CI and Speed of all collected trajectories, Related to Figure2, Figure3, and Figure 5. (A) Distribution of chemotactic index (CI) from all trajectories of MDA-MB-231 collected from experimental trials (N>3) including >100 trajectories per condition, respectively. Box represents quartiles with a median line in the middle of the box. (B) Distribution of speed from all collected trajectories of MDA-MB-231. Box: interquartile range (IQR) ± 1.5 IQR whiskers with a median line. (C) Distribution of chemotactic index (CI) from all trajectories of eKIC. (D) Distribution of speed from all collected trajectories of eKIC. A dot represents data from a single trajectory. (*: $p < 0.05$ for comparison with ctrl, N.S: no significance with $p > 0.05$ in Mann-Whitney test)

Figure. S2. Speed of MDA-MB-231 in the uniform background concentration of corresponding
gradient, Related to Figure 4. Control, 50nM/mm TGF-β gradient (∇T), 25nM uniform TGF-β (T_0),
800nM/mm EGF gradient (∇E), and 400nM uniform EGF (E_0). Speed of all treatment groups (∇T, T_0, ∇E,
and E_0) increase compared to Ctrl, while T_0 or E_0 is not significantly different from the corresponding
gradient (∇T or ∇E). Bar represents mean of the medians ± S.E (n≥3). The medians are collected from >35
trajectories in a sample, respectively. (*: $p < 0.05$, and N.S: no significance with $p > 0.05$ in student's t-test)

Figure. S3. The crosstalk model prediction, Related to Figure 5 (A) The bias Δm decreases when a
TGF-β gradient ∇T is combined with a uniform background of EGF ($\nabla T+E_0$), but not with a uniform
background of TGF-β ($\nabla T+T_0$). The prediction is not comparable with the experimental results (**Figure. 5C**).
(B) The average m decreases in $\nabla T+E_0$, and significantly increases in $\nabla T+T_0$, which is a different tendency
from the experimental results (**Figure. 5D**) showing comparable speeds each other when ∇T is combined
with either $\nabla T+E_0$ or $\nabla T+T_0$.