

Unbiased integration of single cell multi-omics data

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1 **Abstract**

2 Acquiring accurate single-cell multiomics profiles often requires performing unbiased *in silico*
3 integration of data matrices generated by different single-cell technologies from the same
4 biological sample. However, both the rows and the columns can represent different entities in
5 different data matrices, making such integration a computational challenge that has only been
6 solved approximately by existing approaches. Here, we present bindSC, a single-cell data
7 integration tool that realizes simultaneous alignment of the rows and the columns between data
8 matrices without making approximations. Using datasets produced by multiomics technologies as
9 gold standard, we show that bindSC generates accurate multimodal co-embeddings that are
10 substantially more accurate than those generated by existing approaches. Particularly, bindSC
11 effectively integrated single cell RNA sequencing (scRNA-seq) and single cell chromatin
12 accessibility sequencing (scATAC-seq) data towards discovering key regulatory elements in
13 cancer cell-lines and mouse cells. It achieved accurate integration of both common and rare cell
14 types (<0.25% abundance) in a novel mouse retina cell atlas generated using the 10x Genomics
15 Multiome ATAC+RNA kit. Further, it achieves unbiased integration of scRNA-seq and 10x
16 Visium spatial transcriptomics data derived from mouse brain cortex samples. Lastly, it
17 demonstrated efficacy in delineating immune cell types via integrating single-cell RNA and
18 protein data. Thus, bindSC, available at <https://github.com/KChen-lab/bindSC>, can be applied in
19 a broad variety of context to accelerate discovery of complex cellular and biological identities and
20 associated molecular underpinnings in diseases and developing organisms.

21 **Introductions**

22 Advances in high-throughput single-cell technology such as single-cell RNA-sequencing (scRNA-
23 seq) ¹ and mass cytometry ² have enabled systematic delineation of cell types based on thousands
24 to millions of cells sampled from developing organisms or patient biopsies. For example, recent
25 application of combinatorial indexing based technology has generated the transcriptomic and
26 chromatin accessibility profiles of millions of cells in developing human fetus samples ³. Rare cell
27 types and complex cellular states, however, remain challenging to discover, which necessitates the
28 development of multiomics technologies to simultaneously measure other cellular features,
29 including DNA methylation ^{4,5}, chromatin accessibility ⁶⁻⁸ and spatial positions ^{9,10} in the same
30 cells. Although available single-cell multiomics technologies ^{8,11-14} can profile thousands to
31 millions of cells per experiment, the cost of the experiments is still quite high ¹⁵; and the data
32 generated are often of lower throughput than those generated by unimodal technologies. These
33 restrictions necessitate the development of computational approaches that can accurately integrate
34 multiple data matrices generated by different technologies from the same biological samples to
35 acquire an accurate characterization of cellular identity and function.

36

37 However, different technologies create data matrices of different rows and columns, which
38 correspond to different sets of cells and different types of features. How to align cells and features
39 simultaneously across matrices is a core computational challenge. When the two sets of cells are
40 sampled uniformly from the same biological sample, it is safe to assume that there exists an optimal
41 way to align together cells of similar identities and features associated with these identities. This
42 is mathematically challenging, however, as there are many possible ways to simultaneously align
43 a large number of cells and features. To address this challenge, existing computational approaches

44 followed two directions: 1) aligning features empirically before aligning cells ¹⁶⁻¹⁹; 2) obtaining
45 separate embeddings for each modality, followed by performing unsupervised manifold alignment
46 ²⁰⁻²². Taking integration of scRNA-seq and single cell assay for transposase accessible chromatin
47 sequencing (scATAC-seq) as an example, the first category of methods require constructing a
48 “gene activity matrix” from scATAC-seq data by counting DNA reads aligned near and within
49 each gene ²³. This strategy considers only the basic cis-regulatory relations and ignores long-range,
50 trans-regulatory relationship established via other regulatory elements such as enhancers ⁶, which
51 are often critical to decipher cell identities. It also substantially simplifies (or loses) multifactorial
52 relations between transcription factors (TF) and target genes ²⁴. Based on pre-aligned features
53 generated by such empirical rules, Seurat applies canonical correlation analysis (CCA) and mutual
54 nearest neighbors (MNNs) to identify cells anchoring the two data matrices ¹⁷; LIGER uses an
55 integrative non-negative matrix factorization (iNMF) to delineate shared and dataset-specific
56 features ¹⁹; Harmony projects cells onto a shared embedding using principle components analysis
57 (PCA) and removes batch effects iteratively ¹⁸. All these programs suffer from the aforementioned
58 limitations and thereby cannot yield a comprehensive, unbiased gene regulatory network,
59 particularly when chromatin changes are asynchronous from RNA transcriptions in cells
60 undergoing state transitions ²⁵. The second category of methods ²⁰⁻²² do not require prior feature
61 alignment and are fully unsupervised. However, they depend heavily on the assumption that
62 feature variation across cells is driven by a few latent variables in both modalities ²². This
63 assumption can get violated easily in datasets of complex biology involving dynamic processes
64 such as differentiation, reprogramming and transdifferentiation ²².

65

66 In this study, we develop a novel computational tool called bindSC (bi-order integration of single-
67 cell data). The key algorithm implemented in bindSC is called bi-CCA (bi-order canonical
68 correlation analysis). Bi-CCA learns the optimal alignment among rows and columns from two
69 data matrices generated by two different experiments. The alignment matrix derived from bi-CCA
70 can thereby be utilized to derive *in silico* multiomics profiles from aligned cells.

71

72 We assess our method on several challenging multimodality integration tasks between 1)
73 transcriptomic and chromatin accessibility data, 2) transcriptomic and spatial transcriptomic data,
74 and 3) transcriptomic and proteomic data. We validate scRNA-seq and scATAC-seq integration
75 accuracy using datasets obtained directly from multiomics technologies, including a novel mouse
76 retina cell atlas created by the 10x Genomics Multiome ATAC+RNA kit. We show that bindSC
77 enables comprehensive characterization of epigenetic regulatory states in a lung adenocarcinoma
78 cell-line A549 in response to dexamethasone treatment. And bindSC can align mouse retina cell
79 types accurately, for multi-subtype bipolar cells and rare horizontal cells. Moreover, bindSC
80 enables unbiased integration of spatial transcriptomics data with scRNA-seq data on mouse brain
81 cortex samples, as well as single-cell RNA data with protein data from peripheral blood
82 mononuclear cells. BindSC is implemented as an open-source R package available at
83 <https://github.com/KChen-lab/bindSC>.

84

85 **Results**

86

87 **Bi-order integration of multi-omics data**

88 BindSC takes as input two single-cell data matrices (\mathbf{X} and \mathbf{Y}) generated uniformly from the same
89 cell population by two different technologies (**Fig. 1a**). In most single-cell multi-omics integration
90 tasks, neither the alignment between the cells in \mathbf{X} and those in \mathbf{Y} , nor the alignment between the
91 features in \mathbf{X} and those in \mathbf{Y} is known. BindSC employs a bi-CCA algorithm developed in this
92 study to address this challenge (**Fig. 1b**). Briefly, bi-CCA introduces a gene score matrix \mathbf{Z} to link
93 \mathbf{X} and \mathbf{Y} . The gene score matrix has the same rows as does \mathbf{X} and the same columns as does \mathbf{Y} . To
94 reduce computational cost, \mathbf{Z} can be initialized based on prior knowledge. Taking integration of
95 scRNA-seq and scATAC-seq as an example, the gene score matrix can be initialized using the
96 “gene activity matrix” estimated by other programs such as Seurat. Bi-CCA then iteratively
97 updates \mathbf{Z} to find an optimal solution which maximizes the correlation between \mathbf{X} and \mathbf{Z} and
98 between \mathbf{Y} and \mathbf{Z} in the latent space simultaneously. Details about this iterative procedure can be
99 found in **Methods** and **Supplementary Fig. 1a**.

100

101 Bi-CCA outputs canonical correlation vectors (CCVs), which project cells from two datasets onto
102 a shared latent space (referring below as “co-embedding”). A K-nearest neighbor (KNN) graph is
103 constructed based on Euclidean distances observed in the latent space, followed by modularity
104 optimization techniques to partition the KNN into highly interconnected subgraphs, each of which
105 corresponds to a putative cell type or state (**Fig. 1c**). Within each cluster, sub-clustering using
106 similar strategies is further performed to derive what we call pseudo-cells (**Methods**). Each
107 pseudo-cell encloses tens of cells from both datasets and thus has a consensus multiomic profile
108 summarized from constituting cells (**Fig. 1c-d**). The joint multiomic profiles thus enable 1)
109 characterizing gene and chromatin-accessibility relations from aligned scRNA-seq and scATAC-
110 seq data; 2) associating transcriptomic profiles with spatial locations from aligned scRNA-seq and

111 spatial transcriptomic data; 3) associating transcriptomic profiles with proteomic profiles from
112 aligned scRNA-seq and CyTOF data, and so on (**Fig. 1e**).

113

114 **Benchmarking bindSC performance on simulation datasets**

115 Existing integration methods such as Seurat, LIGER, and Harmony require pre-aligning features
116 across modalities, i.e., compressing cell-peak matrices obtained from scATAC-seq onto cell-gene-
117 activity matrices based on reference genome annotations. BindSC overcomes that restriction: its
118 generic mathematical formulations allow free alignment amongst features to be established from
119 data.

120

121 Under our formulation (**Methods**), \mathbf{Z} has features (rows) aligned with \mathbf{X} and cells (columns)
122 aligned with \mathbf{Y} . The introduction of \mathbf{Z} enables bi-order alignment of the cells and the features,
123 respectively.

124

125 To quantify how much this step matters to overall integration accuracy, we performed a set of
126 simulation experiments. We started by creating a dataset \mathbf{X} consisting of 3 cell clusters (types),
127 each having 333 cells and 1,000 genes using Splatter²⁶ (**Supplementary Fig. 2a**). We created a
128 second dataset \mathbf{Y} and made it identical to \mathbf{X} : $\mathbf{X} = \mathbf{Y}$. We then constructed a gene score matrix \mathbf{Z}
129 from \mathbf{Y} by permuting a fraction of features (rows), termed misalignment rate (MR), into different
130 orders. The features between \mathbf{Z} and \mathbf{Y} are perfectly aligned if MR equals 1 and are independent if
131 MR equals 0. We further added white noise on all the entries of \mathbf{Z} at a given signal-noise-ratio
132 (SNR) level.

133

134 We then provide (\mathbf{X} , \mathbf{Z}) as input to the other methods (**Supplementary Fig. 2b**), mimicking how
135 they perform integration, while provide both (\mathbf{X} , \mathbf{Z}) and (\mathbf{Y} , \mathbf{Z}) to bindSC (**Supplementary Fig.**
136 **2c**). As described, rather than taking \mathbf{Z} as it is from the input, bindSC will iteratively update \mathbf{Z}
137 until reaching convergence.

138

139 Since we know the true cell type and dataset origin of the cells in these experiments, we can assess
140 the integration performance in terms of cell type classification accuracy and dataset alignment
141 accuracy in the co-embeddings. It is necessary to measure both types of accuracy, as a high cell
142 type classification accuracy can be achieved by simply projecting cells onto local clusters without
143 achieving uniform mixing of the two datasets. Similarly, a high dataset alignment accuracy can be
144 achieved by uniformly mixing cells from the datasets, regardless of their cellular identity. We used
145 Silhouette score for measure cell type classification accuracy and alignment mixing score to
146 measure the dataset alignment accuracy (**Methods**). We compared bindSC, CCA, Seurat, LIGER
147 and Harmony under default settings (**Supplementary Note 1**).

148

149 We obtained results from a range of MRs under SNR = 0.25 (**Fig. 2**). When there was no feature
150 misalignment (MR = 0), all methods achieved good performance. Even under this ideal scenario,
151 bindSC achieved the highest Silhouette score (> 0.75) (**Fig. 2a**). The worse performance of other
152 methods can be explained by the noise introduced to distort the manifold structures between \mathbf{X} and
153 \mathbf{Z} . CCA showed better performance than Seurat, which may be due partly to label transferring
154 errors introduced by Seurat's empirical anchor-based alignment approach. As MR increased from
155 0 to 0.9, the Silhouette score for bindSC remained stable (> 0.7), while all the other methods
156 showed a decreasing trend, especially for LIGER and Harmony. Harmony worked well when MR

157 ≤ 0.15 (**Fig. 2a-b**) but had a substantial drop on Silhouette score (< 0.1) when $MR > 0.15$. In
158 addition, its alignment mixing score dropped to 0 when $MR > 0.2$, with no mixing of cells from **X**
159 and **Z** in the co-embedding UMAP (**Fig. 2b**; $MR = 0.5$). Harmony takes cell coordinates from a
160 reduced dimensional PCA space and runs an iterative algorithm to adjust for dataset-specific
161 effects. When $MR > 0.15$, cells from **X** and **Z** already formed two dis-joint groups, which made
162 the downstream integration impossible for Harmony. The Silhouette score of LIGER showed
163 fluctuations but was always lower than 0.4. LIGER utilizes an integrated nonnegative matrix
164 factorization (iNMF) method to identify shared and dataset-specific metagenes across two datasets.
165 If it worked as designed, the errors caused by feature misalignment should be contained within
166 dataset-specific modules. However, variance explained by the data-specific modules appeared to
167 be small ($< 1\%$). When $MR \geq 0.95$, all methods including bindSC failed to achieve reasonable
168 integration. That was expected as **X** and **Z** (as well as **Y** and **Z**) became nearly independent.

169
170 As expected, increasing SNR level worsened the integration performance for most of the methods
171 except bindSC. For example, both CCA and Seurat had acceptable performance under $MR = 0.5$
172 and $SNR = 0$ (**Supplementary Fig. 3a**), but Seurat failed to separate cell type 2 and 3 accurately
173 when $SNR = 0.25$ or 0.5 (**Supplemental Fig. 4a**; **Fig. 2**). For $SNR = 0.5$, Harmony failed in both
174 alignment mixing (< 0.2) and classification ($= 0$) accuracy, even when MR was as low as 0.1
175 (**Supplementary Fig. 4**).

176
177 We repeated the above experiments by increasing the number of cells to 5,000 and 10,000,
178 respectively. Similarly, bindSC showed robust performance regardless of MR and SNR levels,
179 which was not achieved by other methods (**Supplementary Tables S2-3**). Overall, the simulation

180 results demonstrated that bindSC is robust to bias introduced by noise in the data and via pre-
181 aligning features, thanks to its ability to align both cells and features simultaneously.

182

183 **Integrating single cell epigenomic data with single cell transcriptomic data**

184 Integrating single cell epigenomic data with single cell transcriptomic data obtained from
185 unimodal technologies provides an opportunity to decipher epigenetic regulatory mechanisms
186 underpinning cell transcriptomic identity. We examined the performance of bindSC in integrating
187 the scRNA-seq and scATAC-seq data derived from lung adenocarcinoma (A549) cells after 0, 1,
188 and 3 hours of dexamethasone (DEX) treatment ⁶. This dataset was generated using a
189 combinatorial indexing-based coassay (sci-CAR), which enabled jointly measurement of
190 chromatin accessibility and transcriptome in the same cells. In this dataset, 6,005 cells have sci-
191 RNA-seq profiles and 3,628 cells have sci-ATAC-seq profiles. Among them, 1,429 cells have both
192 RNA-seq and ATAC-seq profiles, which can be used as a gold standard for evaluating integration
193 accuracy of various methods (**Methods**).

194

195 For comparison, we ran the 4 methods on the same data and derived *in silico* co-embeddings. There
196 was relatively clear separation between cells acquired at 0 hour and those at 1 or 3 hours in the co-
197 embeddings (**Fig. 3a**). In terms of classifying cells by time, bindSC achieved the highest Silhouette
198 score and Harmony the second, whereas Seurat had the lowest score with many sub-clusters in its
199 co-embedding (**Fig. 3a-b**). As to alignment accuracy, bindSC and Harmony had similar scores,
200 whereas Seurat received a relatively low score (**Fig. 3b**). Similar trends were observed in a
201 previous study analyzing the same dataset ²⁷. As suggested by simulation, the low alignment
202 mixing score of Seurat was likely attributable to bias introduced in its anchor-based integration.

203
204 A perfect integration method would place the two instances of the 1,429 co-assayed cells onto
205 identical locations in the co-embeddings. We leveraged this expectation to compare the accuracy
206 of various methods. We defined a metric, called anchoring distance that measures the normalized
207 Euclidean distance between the two instances of a co-assayed cell in the co-embeddings
208 (**Methods**). BindSC achieved substantially shorter anchoring distances than the other methods (p
209 $< 2.2e-16$; Student t-test; **Fig. 3b**).

210
211 We further compared how accurately TF (or peak) -gene correlations can be inferred from the co-
212 embeddings produced by each method. For a fair comparison, we applied the same bindSC
213 workflow to derive pseudo-cells for the 4 methods (**Methods; Supplementary Note 2**).

214
215 For each TF-gene (and peak-gene) pair, we calculated a Spearman rank correlation coefficient
216 (SRCC) between the TF activity (and normalized peak) level and the gene expression level in the
217 pseudo-cells (**Methods**). We repeated the same calculation in the co-assayed cells to create a gold
218 standard. For each of the 4 methods in 3 types of relations: TF-gene, cis- peak-gene and trans-
219 peak-gene, we calculated a summary SRCC between the SRCCs obtained from the pseudo-cells
220 and the SRCCs obtained from the co-assayed cells. The summary SRCCs resulting from bindSC
221 were consistently higher than those obtained from Seurat, LIGER and Harmony in all the
222 categories of comparison, indicating that the bindSC multiomic profile had the highest accuracy.

223
224 We further examined the peak-gene association identified from the co-assayed cell profiles and
225 found 585 trans- peak-gene pairs being supported by isogenic Hi-C data generated in an

226 independent study²⁸. Compared with other approaches, bindSC derived peak-gene SRCCs of the
227 highest level of agreement with those observed in the co-assayed cells (**Supplementary Fig. 5**).
228 Among the 585 trans- peaks, 470 appeared more strongly correlated with the corresponding gene
229 expression levels than did the corresponding cis- peaks. One example was the gene *CFLAR* and a
230 trans- peak at chr2:201,770,437-201,770,992, which is 200-kb upstream of *CFLAR* transcription
231 start site, spanning over three genes (**Fig. 3e**). The SRCC of this pair was 0.32 in the co-assayed
232 cells. It was lower but comparable (0.23) in the bindSC pseudo-cells, however, became
233 substantially lower (< 0.11) in the pseudo-cells generated by the other methods (**Supplementary**
234 **Fig. 5**).

235

236 The DEX treatment specifically targets the glucocorticoid receptor encoded by *NR3C1*, a TF that
237 activates the mRNA transcription of a handful of downstream genes. BindSC accurately
238 reconstructed the gene expression and TF activity kinetics of *NR3C1* (**Fig. 3d**), consistent with
239 what was depicted in the original study⁶ using the co-assayed cells: the *NR3C1* expression level
240 decreased over time while its activity level increased; Even the slowing down trend of *NR3C1*
241 activity was captured.

242

243 We further evaluated the performance of bindSC in integrating scRNA-seq and scATAC-seq on
244 another available multi-omics dataset generated recently by SHARE-seq technology¹⁴. There were
245 a total of 37,774 cells from mouse skin tissues that had paired RNA and ATAC profiles. Compared
246 with other methods, bindSC again achieved significantly shorter anchoring distances
247 (**Supplementary Fig. 7; Supplementary Note 4**).

248

249 **Comprehensive evaluation using a novel mouse retinal cell atlas**

250 For comprehensive evaluation and comparison, we generated a novel multi-omics dataset from
251 single nuclei of wild type mouse retina. Mouse retina is heterogeneous, composed of multiple
252 neuronal and non-neuronal cell types, including five major neuron classes: photoreceptors (rods
253 and cones), retinal ganglion cells (RGC), horizontal cells (HC), bipolar cells (BC), amacrine cells
254 (AC), and a non-neuronal Müller glial cell (MG)^{4,29,30}. While we²⁹ and others³¹⁻³³ have provided
255 high-resolution single cell transcriptomic profiles of whole retina or specially sorted cell types on
256 mouse and human retina tissue, little is known on the single-cell chromatin landscape of mouse
257 retina tissue. Numerous studies³⁴⁻³⁶ demonstrate the importance of transcription factors (TFs) on
258 establishing or maintaining the chromatin landscapes that define retina cell identity. Therefore,
259 integration of ATAC and RNA profiles at single cell resolution provides an exciting opportunity
260 to comprehensively characterize cell types and rare cell subtypes in mouse retina.

261
262 We applied the newly released 10x Genomics Multiome ATAC+RNA kit on nuclei suspension
263 acquired from adult mice retina samples. After performing standard quality control, we obtained
264 an atlas of 9,383 nuclei of high-quality ATAC+RNA profiles. To define cell types, we first
265 clustered the RNA and the ATAC data individually. Nineteen (19) clusters were identified from
266 the RNA data alone, which included all the known major cell types with some subtypes identified:
267 rod, BC (BC1~BC10), AC, RGC, cone, HC, MG and retina progenitor cells (RPC) (**Fig 4a and**
268 **Supplementary Fig. 8**). Nineteen (19) clusters were also identified from the peak files of the
269 ATAC data alone (**Fig. 4b**). Although known cell types appeared to be well separated in both
270 modalities, there were some noticeable differences. For example, RGC cells and rod cells were
271 separated clearly in the RNA data but partly blended together in the ATAC data, whereas ACs and

272 RGC cells were blended in the RNA data but well separated in the ATAC data. Interestingly, all
273 the 10 BC cell subtypes, defined based on RNA expression levels, were well separated in the
274 ATAC data except for BC1 and BC6. However, after reducing ATAC data to gene level in a gene
275 activity matrix, the cell types became considerably harder to delineate (**Fig. 4c**).

276

277 To obtain *in silico* multiomics profiles, we ran bindSC together with three other methods on the
278 data without using the known cell correspondence. As shown in the co-embedding UMAP
279 (**Fig. 4d-e**), bindSC successfully aligned cell types across modalities, with most cell types well
280 separated out (**Fig. 4d-f**). Interestingly, bindSC successfully aligned the HCs, which is quite rare
281 in the dataset (23 cells, <0.25% abundance). None of the other methods aligned the HCs correctly
282 as it was already difficult to separate the HCs from the ACs in the gene-level chromatin profiles
283 (**Fig. 4c and Supplementary Fig. 9**), the input to the other methods. Overall, the anchoring
284 distances in the co-embeddings generated by bindSC were considerably smaller than those
285 generated by the other methods in all the cell types assessed (**Fig. 4f**).

286

287 Note that bindSC aligned the 10 BC subtypes reasonably well (**Fig. 4g**), although separations in
288 the ATAC modality were not as clean as they were in the RNA modality. In comparison, Seurat
289 and LIGER failed to generate meaningful alignments among the BC subtypes (**Fig. 4h-j** and
290 **Supplementary Fig. 9**) while Harmony aligned a few subtypes successfully. These were due
291 partly to the fact that these methods used the low precision gene-level chromatin accessibility
292 profiles as the input (**Fig. 4c**).

293

294 Overall, our study demonstrated the power of multiomics in delineating rare cell types and proves
295 that bindSC can generate *in silico* multiomics profiles that are considerably more accurate than do
296 existing tools.

297

298 **Integrating scRNA-seq data with spatial transcriptomics (ST) data**

299 BindSC can integrate scRNA-seq data with spatial transcriptomics data to 1) assign spatial
300 locations to cells in the scRNA-seq data and 2) associate additional RNA features to the spatial
301 data for higher resolution delineation. For demonstration, we applied bindSC to integrate the
302 SMART-Seq2 data with the *in situ* spatial transcriptomics data generated by 10x Visium from the
303 same mouse frontal cortex tissue. These two datasets differ widely in number of cells: 1,072 spots
304 in the ST data versus 14,249 cells in the scRNA-seq data (**Supplementary Fig. 10a**). The spots
305 on the Visium assay are at ~50 um resolution and each spot can contain tens of cells. There were
306 6 clusters identified from the ST data alone, which linked to distinct layers in the corresponding
307 histology images (**Supplementary Fig. 10b-c**) and 23 cell types from the scRNA-seq data alone
308 (**Supplementary Fig. 10d**).

309

310 We used bindSC and other programs to derive co-embeddings containing datapoints from both
311 datasets (**Fig. 5a**). BindSC achieved evidently higher alignment mixing scores than the other
312 programs (**Supplementary Fig. 11c**) while the Silhouette scores were similar (**Supplementary**
313 **Fig. 11b**). For each pseudo-cell in the scRNA-seq data, we calculated its probability to map to a
314 spatial location in the histology image. We then overlaid these cells on the histology image
315 coloring by their probability scores (**Methods**). Noticeably, several cell types in the scRNA-seq
316 data mapped to distinct spatial layers in the histology image, which is consistent with the known

317 cellular anatomy of mouse cortex, particularly for the laminar excitatory neuron cell types such as
318 L2.3 IT, L4, L5.IT, L5.PT, L6.IT, L6.CT, L6B and NP (**Fig. 5b**). Consistent with previous
319 observations, the oligodendrocyte-rich white matter (oligo cells) was mapped below the cortex.
320 BindSC and Seurat were also able to map inhibitory clear cell types such as Lamp5, Vip, Pvalb
321 and Sst in the scRNA-seq data to the histology image, but these cell types did not form distinct
322 spatial patterns. LIGER and Harmony, which had worse alignment mixing scores (**Supplementary**
323 **Fig. 11c**), failed to map these cells (**Supplementary Figs. 13-14**), especially the Vip cells. The
324 poor mapping of the inhibitory cells may also be attributable to the limited resolution of the Visium
325 technology.

326

327 Given that each spot in the ST data may encompass multiple cells from multiple cell types, we
328 hypothesized that the probability scores calculated from the co-embeddings can reveal the
329 composition of the cell types at each spot. **Fig. 5c** showed the relationship between cell type
330 abundance in the scRNA-seq data and abundance estimated based on probability scores in the ST
331 data. Results from bindSC achieved the best correlation (Pearson's $R = 0.9$). L6.IT, Sst and Vip
332 cell types were the top 3 most abundant cell types in both the scRNA-seq data and the ST data.
333 Seurat also performed reasonably well (Pearson's $R = 0.83$) while LIGER and Harmony performed
334 worse. Note that Lamp5 was the cell type that showed the largest discordance in the bindSC result.
335 In examining the spatial distributions of Lamp5 specific gene expressions such as *Lsp1*, *Npy2r*,
336 and *Dock5*, we could not find any spatial patterns (**Supplementary Fig. 11 d-e**). This finding may
337 indicate that Lamp5 does not have a characteristic spatial distribution.

338

339 **Integrating single-cell RNA with protein data**

340 Complex interplay exists between mRNAs and proteins³⁷. Single-cell proteomic methods such as
341 mass cytometry (CyTOF)^{2,38} measure abundance of a small set of (often 10-50) surface proteins
342 (epitopes) and provide functional quantification of various cell populations. Integrating single-cell
343 RNA and protein data from the same sample can potentially achieve higher resolution
344 characterization and enable discovery of novel cellular states and associated features. BindSC can
345 be applied for such a task. Notice that this task cannot be achieved by any of the existing tools
346 because the mRNA and protein expression levels derived from the same genes are not well
347 correlated, due to complex post-transcriptional modifications and technological limitations³⁹.
348 CITE-seq⁴⁰ performs jointly profiling of epitope and mRNA levels in the same cells and can be
349 used to evaluate the results of *in silico* integration.

350

351 We used a CITE-seq dataset consisting of 30,672 human bone marrow cells with a panel of 25
352 antibodies¹⁷. We split the data into an RNA matrix and a protein matrix. Unsupervised clustering
353 of the RNA matrix revealed cell types largely consistent with those in the protein matrix, except
354 for some noticeable differences (**Fig. 6a-b**). CD8+ and CD4+ T cells were partly blended together
355 in the RNA data but separated clearly in the protein data. On the other hand, conventional dendritic
356 cells (cDC2) were separated from other clusters in the RNA data but were intermixed with other
357 cell types in the protein data. In contrast, unsupervised clustering of the gene expression levels of
358 the 25 protein-homologous RNAs could not yield meaningful classification (**Fig. 6c**).
359 Consequently, Seurat, LIGER and Harmony, which work with only data matrix of 25 homologous
360 features, failed to produce meaningful co-embeddings (**Supplementary Fig. 15**): the cells from
361 the protein data were well clustered, but those from the RNA data were not meaningfully
362 distributed in the co-embeddings.

363

364 We then tested bindSC on this task. The matrix \mathbf{X} was set as the protein matrix, \mathbf{Y} the RNA matrix
365 of 3,000 highly variable genes, and \mathbf{Z} the RNA matrix containing only the 25 protein-homologous
366 genes. Remarkably, the majority of the cells from the two modalities became well aligned in the
367 co-embedding (**Fig. 6d-e**), as they are expected to be. Similar to our previous experiments, we
368 calculated the anchoring distance between the protein and the RNA cells deriving from the same
369 original cells in the co-embeddings. The overall anchoring distance for bindSC was significantly
370 lower than those obtained by Seurat, LIGER, Harmony, or random guesses (p-value < 2.2e-16;
371 Student t-test; **Fig. 6f**). Notably, the bulk of CD4⁺ and CD8⁺ T cells in the RNA data became well
372 separated in the co-embedding (**Fig. 6d-e**), thanks to the power of integration. Moreover, the
373 anchoring distances revealed the extent of differences between the levels of the RNAs and those
374 of the homologous proteins in individual cell types (**Fig. 6g**). Interestingly, relatively rare cell
375 types such as HSC, Prog/NK, LMPP, and CD16⁺ Mono appeared relatively well anchored,
376 whereas relatively common cell types such as CD8 naïve, CD8 memory, B progenitor, Treg, etc.
377 appeared less well anchored. This indicates that there are higher degrees of post-transcriptional
378 heterogeneity in cell types conducting adaptive immune surveillance ⁴¹.

379

380 **Discussion**

381 Despite the ground-breaking advances in single-cell technologies, including multiomics
382 technologies, there always exists a need to computationally integrate multiple data matrices of
383 different modalities from the same biological samples to derive a more comprehensive
384 characterization of cellular identities and functions.

385

386 Our method bi-CCA and tool bindSC appeared to have addressed this important analytical
387 challenge without compromising biological complexity in the data. In our experiments, bindSC
388 successfully integrated data obtained from a wide variety of vastly different technologies covering
389 transcriptomes, epigenomes, spatial-transcriptomes and proteomes, and clearly outperformed
390 existing tools such as Seurat, LIGER and Harmony, when being evaluated objectively using true
391 single-cell multiomics data derived from the same cells. In particular, Seurat, LIGER, and
392 Harmony are essentially first-order solutions that can be applied to only rows or columns but not
393 both simultaneously. That approach introduced biases in the results and restricted the utility of
394 those tools in discovering complex cell-type relations and molecular interactions. For instance,
395 they consider only the basic cis-regulatory relations and ignores trans-regulatory relations ⁶
396 established via distal enhancers, as exemplified in the interaction between *CFLAR* and a 200 kbps
397 upstream putative enhancer site discovered by bindSC and validated by Hi-C in the DEX-treated
398 A549 data. Other scATAC-seq analysis pipelines such as MAESTRO ¹⁶ and ArchR ⁴² have similar
399 restrictions.

400

401 Similarly, bindSC was able to meaningfully associate the expression levels of mRNAs with those
402 of the surface proteins, a very challenging task due to complexity in post-transcriptional
403 modification. The resulting co-embedding offered deeper biological insights than embeddings
404 derived from single modality or by using other existing approaches. For example, CD4+ T cells
405 became evidently separated from CD8+ T cells and so did pDC cells from other cell types.

406

407 BindSC also achieved meaningful mapping of scRNA-seq data to spatial locations in the brain
408 cortex samples, after integrating with the ST data. Even though the two datasets were not both at
409 single-cell resolution, bindSC was still able to achieve a meaningful integration.

410

411 Bi-CCA made two assumptions: 1) the two sets of cells are sampled uniformly from the same
412 biological sample; 2) the features of the two datasets are linearly correlated. These two
413 assumptions are met under many scenarios of current investigations, however, could be violated
414 when there are insufficient number of cells obtained from a rapidly developing cell population.
415 Consequently, the accuracy of the co-embedding could vary, depending on the sampling density
416 and the complexity of the population. We measured accuracy with respect to data complexity in
417 the simulation experiments, however, accuracy on a real dataset could be complex to gauge *a*
418 *priori* and will require case by case investigation in the context of a specific study, followed by
419 necessary experimental validation. Nonetheless, in this study we clearly proved based on objective
420 ground truth data that bi-CCA substantially avoided bias introduced by existing methods and that
421 bindSC is a robust implementation that can be applied to derive meaningful results on most recent
422 datasets containing thousands to tens of thousands cells (**Supplementary Table 1**).

423

424 BindSC is efficiently implemented in R. The major computational cost for bindSC is from
425 calculating cell/feature co-embedding coordinates using singular value decomposition (SVD)
426 (**Methods**); It typically requires $O(MN)$ floating-point operations to construct MN cell-cell
427 distance matrix as input to SVD decomposition, where M and N are cell number of the two
428 modalities, respectively. To address this computational challenge, bindSC implements the “divide-
429 and-conquer eigenvalue algorithm”. The divide part first splits cells into different blocks specified

430 by users, which can be solved in parallel with lower memory usage (**Supplementary Fig. 1b**). The
431 conquer part then merges results from each block recursively. Therefore, the maximal memory
432 usage of bindSC is independent of the total cell number.

433

434 Taken together, we believe that bindSC is likely the first tool that has achieved unbiased integration
435 of data matrices generated by different technologies and can be applied in broad settings. In the
436 single-cell domain, bindSC can clearly be applied to align cells and features simultaneously, which
437 are important for ongoing investigations in the Human Cell Atlas ⁴³, the NIH HubMap ⁴⁴, the
438 Human Tumor Cell Network ⁴⁵ and on remodeling of tumor microenvironment ⁴⁶. Further, bindSC
439 can potentially be applied to other domains, such as integrating patient sample mRNA profiles
440 with cell-line drug-sensitivity data ⁴⁷.

441 **Methods**

442 **BindSC workflow**

443 BindSC workflow for creating *in silico* single cell multi-omics embeddings consists of five steps:

- 444 1. individual dataset preprocessing including variable feature selection and cell clustering,
- 445 2. initializing feature matching across modalities (i.e., constructing gene score matrix),
- 446 3. identifying cell correspondence using the bi-CCA algorithm,
- 447 4. jointly clustering cells between two modalities in the co-embedding latent space and
- 448 constructing pseudo-cell level multi-omics profiles, and
- 449 5. downstream analysis for various integration tasks.

450 We formulate our method for the case of two modalities. Let $\mathbf{X} \in \mathbb{R}^{M \times K}$ be a single-cell dataset of
451 features g_1, g_1, \dots, g_M by cells c_1, c_1, \dots, c_K and $\mathbf{Y} \in \mathbb{R}^{N \times L}$ be a single-cell dataset of feature
452 p_1, p_2, \dots, p_N by cells d_1, d_1, \dots, d_L . M and N are the numbers of features (e.g., gene expression,
453 chromatin accessibility, protein abundance level) in the two datasets. K and L are the number of
454 cells in the two datasets. Without loss of generality, we assume that features
455 g_1, g_1, \dots, g_M represent the gene expression levels and $M \leq N$. The important component of each
456 step is described as follows.

457

458 **1. Individual modality preprocessing**

459 For each modality, we follow standard processing pipeline, which includes variable feature
460 selection and unsupervised cell clustering. The cluster information derived from each modality is
461 used for downstream parameter optimization.

462

463 **2. Initializing feature matching across modalities**

464 Because features in the two datasets are generally different, bindSC requires one additional
 465 transition matrix $\mathbf{Z} \in \mathbb{R}^{M \times L}$ as input for bridging the integration of \mathbf{X} and \mathbf{Y} . The transition matrix
 466 \mathbf{Z} can be understood as the projection of \mathbf{Y} to the feature space of the first dataset \mathbf{X} . Taking the
 467 integration of scRNA-seq and scATAC-seq as an example, the matrix \mathbf{Z} can be derived from
 468 scATAC-seq profiles by summing reads in gene bodies^{17,19,23}. This can also be input from the
 469 regulatory potential (RP) model in MAESTRO¹⁶. In a simpler case where \mathbf{X} and \mathbf{Y} have matched
 470 features, the integration tasks fall into two categories: 1) batch correction for scRNA-seq data
 471 across individuals, species, or technologies; 2) integration of scRNA-seq with spatial
 472 transcriptome data. In those cases, the transition matrix \mathbf{Z} is initialized as \mathbf{Y} . In bi-CCA, \mathbf{Z} is
 473 updated iteratively. In the following text, the initial value of \mathbf{Z} is denoted by $\mathbf{Z}^{(0)}$.

474

475 **3. Bi-order canonical correlation analysis (Bi-CCA)**

476 The key algorithm implemented in bindSC is Bi-CCA, the concept of which extends traditional
 477 CCA^{17,24,48} to both rows and columns to enable capturing of correlated variables in cells and
 478 features simultaneously. Bi-CCA introduces two cell-level projection matrices $\mathbf{U} \in \mathbb{R}^{K \times E}$, $\mathbf{S} \in$
 479 $\mathbb{R}^{L \times E}$ such that the correlations between indices \mathbf{XU} and \mathbf{ZS} are maximized, and two feature-level
 480 projection matrices $\mathbf{T} \in \mathbb{R}^{M \times E}$, $\mathbf{V} \in \mathbb{R}^{N \times E}$ such that the correlations between indices $\mathbf{Z'T}$ and $\mathbf{Y'V}$
 481 are maximized. The optimization framework can be formulated as:

$$482 \quad \underset{U, S, T, V, Z}{\operatorname{argmax}} \operatorname{tr}\{(\mathbf{XU})' \mathbf{ZS} + (\mathbf{Z'T})' \mathbf{Y'V}\} \quad (1)$$

$$483 \quad \text{subject to } (\mathbf{XU})' \mathbf{XU} = \mathbf{I}, (\mathbf{ZS})' \mathbf{ZS} = \mathbf{I}, (\mathbf{Z'T})' \mathbf{Z'T} = \mathbf{I}, (\mathbf{Y'V})' \mathbf{Y'V} = \mathbf{I}.$$

484

485 If the transition matrix \mathbf{Z} is known, the objective (1) can be divided into two disjoint traditional
 486 canonical correlation analysis (CCA) problems. The left term is performed to identify cells of

487 similar (aligned) features, while the right term is performed to identify features shared by the
 488 (aligned) cells, each of which can be solved in the CCA framework. However, it is difficult to
 489 update transition matrix \mathbf{Z} in equation (1) even when matrices $\mathbf{U}, \mathbf{S}, \mathbf{T}, \mathbf{V}$ are available. This is
 490 because: a) left optimization problem requires \mathbf{Z} as input and the right optimization problem
 491 requires \mathbf{Z}' as input, leading (1) to a non-linear optimization problem; b) transition matrix \mathbf{Z} shows
 492 up in constraints.

493
 494 Therefore, we modify equation (1) in a much more practical way. First, we standardize \mathbf{X} to let it
 495 have $\mathbf{X}'\mathbf{X} = \mathbf{I}$, and standardize \mathbf{Y} so that $\mathbf{Y}\mathbf{Y}' = \mathbf{I}$. The standardization process can be seen in
 496 **Algorithm 1**. Thus, equation (1) could be simplified as

$$497 \quad \operatorname{argmax}_{\mathbf{U}, \mathbf{S}, \mathbf{T}, \mathbf{V}, \mathbf{Z}} \operatorname{tr}\{(\mathbf{X}\mathbf{U})'\mathbf{Z}\mathbf{S} + (\mathbf{Z}'\mathbf{T})'\mathbf{Y}'\mathbf{V}\} \quad (2)$$

$$498 \quad \text{subject to } \mathbf{U}'\mathbf{U} = \mathbf{I}, (\mathbf{Z}\mathbf{S})'\mathbf{Z}\mathbf{S} = \mathbf{I}, (\mathbf{Z}'\mathbf{T})'\mathbf{Z}'\mathbf{T} = \mathbf{I}, \mathbf{V}'\mathbf{V} = \mathbf{I}.$$

499
 500 To eliminate transition matrix \mathbf{Z} from constraints, we introduce two transition matrices $\mathbf{Z}_l \in \mathbb{R}^{M \times L}$
 501 and $\mathbf{Z}_r \in \mathbb{R}^{M \times L}$ and optimize the following problem:

$$502 \quad \operatorname{argmax}_{\mathbf{U}, \mathbf{S}, \mathbf{T}, \mathbf{V}, \mathbf{Z}_l, \mathbf{Z}_r} \operatorname{tr}\{(\mathbf{X}\mathbf{U})'\mathbf{Z}_l\mathbf{S} + (\mathbf{Z}_r'\mathbf{T})'\mathbf{Y}'\mathbf{V}\} + \|\mathbf{Z}_l - \mathbf{Z}_r\|_2 \quad (3)$$

$$503 \quad \text{subject to } \mathbf{U}'\mathbf{U} = \mathbf{I}, \mathbf{S}'\mathbf{S} = \mathbf{I}, \mathbf{T}'\mathbf{T} = \mathbf{I}, \mathbf{V}'\mathbf{V} = \mathbf{I}, \mathbf{Z}_l\mathbf{Z}_l' = \mathbf{I}, \mathbf{Z}_r'\mathbf{Z}_r = \mathbf{I}.$$

504
 505 To solve equation (3), we also standardize $\mathbf{Z}^{(0)}$ to let $\mathbf{Z}^{(0)'}\mathbf{Z}^{(0)} = \mathbf{I}$, and initialized with $\mathbf{Z}_l := \mathbf{Z}^{(0)}$.
 506 The standard singular value decomposition (SVD) can be implemented to obtain the canonical
 507 correlation vectors (CCVs) at cell levels. We used a user-defined number (E) of singular vectors
 508 that approximate the CCVs (**Algorithm 2**). Here we term E to represent the cell-level

509 “dimensionality” in the latent space, which is a parameter required to be optimized (Details seen
 510 in **Parameter optimization**).

$$511 \quad (\mathbf{U}, \mathbf{S}) := \underset{\mathbf{U}, \mathbf{S}}{\operatorname{argmax}} \operatorname{tr}(\mathbf{U}' \mathbf{X}' \mathbf{Z}_l \mathbf{S}) \text{ subject to } \mathbf{U}' \mathbf{U} = \mathbf{I}, \mathbf{S}' \mathbf{S} = \mathbf{I}. \quad (4)$$

512
 513 Having CCV pair (\mathbf{U}, \mathbf{S}) obtained, we have cell correspondence in the latent space between two
 514 datasets. The left transition matrix \mathbf{Z}_l can be updated by:

$$515 \quad (\mathbf{Z}_l) := \underset{\mathbf{Z}_l}{\operatorname{argmax}} \operatorname{tr}(\mathbf{U}' \mathbf{X}' \mathbf{Z}_l \mathbf{S}) \text{ subject to } \mathbf{Z}_l \mathbf{Z}_l' = \mathbf{I}. \quad (5)$$

516
 517 The details of solving optimization problem (5) is in **Algorithm 2**.

518
 519 We then set

$$520 \quad (\mathbf{Z}_r) := \mathbf{Z}_l. \quad (6)$$

521 The similar SVD algorithm (**Algorithm 2**) is used to approximate CCVs:

$$522 \quad (\mathbf{T}, \mathbf{V}) := \underset{\mathbf{T}, \mathbf{V}}{\operatorname{argmax}} \operatorname{tr}(\mathbf{T}' \mathbf{Z}_r \mathbf{Y}' \mathbf{V}) \text{ subject to } \mathbf{T}' \mathbf{T} = \mathbf{I}, \mathbf{V}' \mathbf{V} = \mathbf{I}. \quad (7)$$

524
 525 Once CCV pairs (\mathbf{T}, \mathbf{V}) are obtained, the features are matched in the latent space between two
 526 datasets. The right transition matrix \mathbf{Z}_r could be updated as:

$$527 \quad (\mathbf{Z}_r) := \underset{\mathbf{Z}_r}{\operatorname{argmax}} \operatorname{tr}\{(\mathbf{Z}_r' \mathbf{T})' \mathbf{Y}' \mathbf{V}\} \text{ subset to } \mathbf{Z}_r' \mathbf{Z}_r = \mathbf{I}. \quad (8)$$

529 Next, we set

$$530 \quad (\mathbf{Z}_l) := \mathbf{Z}_r, \quad (9)$$

531 The update process (4) ~ (9) are repeated until convergence. Because each of the subproblems is
532 convex with respect to the block variables being optimized, the algorithm is guaranteed to
533 converge to a fixed point (local minimum).

534

535 In the above framework, the transition matrix \mathbf{Z} (represented by \mathbf{Z}_l and \mathbf{Z}_r) is updated based on
536 original observed matrices \mathbf{X} and \mathbf{Y} . In practice, we introduce the couple coefficient α ($0 \leq \alpha \leq 1$)
537 to assign weights on initialized matrix $\mathbf{Z}^{(0)}$ on transition process (6) and (9).

$$538 \quad (\mathbf{Z}_r): = (1 - \alpha)\mathbf{Z}^{(0)} + \alpha\mathbf{Z}_l \quad (10)$$

539 and

$$540 \quad (\mathbf{Z}_l): = (1 - \alpha)\mathbf{Z}^{(0)} + \alpha\mathbf{Z}_r \quad (11)$$

541 The couple coefficient α can reflect the contribution of initial $\mathbf{Z}^{(0)}$ on linking two modalities.
542 Equations (10) and (11) will be reduced to Equations (6) and (9) if $\alpha = 1$. The bi-CCA algorithm
543 will be reduced to traditional CCA if $\alpha = 0$. Selection of coefficient α can be seen in **Parameter**
544 **optimization**. Notably, the final \mathbf{Z}_r and \mathbf{Z}_l will be converged to different matrices if $\alpha < 1$. The
545 workflow of the iterative process is shown in **Supplementary Fig. 1a**.

546

547 **Jointly clustering cells across datasets in shared latent space and constructing pseudo-cell** 548 **level multi-omics profiles**

549 Equation (4) projects cells of two datasets into a correlated E -dimensional space with cell
550 coordinates $\mathbf{U} = (\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_K)$ and $\mathbf{S} = (\mathbf{s}_1, \mathbf{s}_2, \dots, \mathbf{s}_L)$, respectively. L2-normalization is
551 performed to remove global differences in scale, therefore

$$552 \quad \hat{\mathbf{u}}_i = \mathbf{u}_i / \|\mathbf{u}_i\|_2, i = 1, 2, \dots, K, \quad (12)$$

$$553 \quad \hat{\mathbf{s}}_i = \mathbf{s}_i / \|\mathbf{s}_i\|_2, i = 1, 2, \dots, L.$$

554
555 The shared nearest neighbor (SNN) graph is constructed by calculating the l -nearest neighbors (20
556 by default) based on the Euclidean distance of L2-normlized latent space. The fraction of shared
557 nearest neighbors between the cell and its neighbors is used as weights of the SNN graph. The
558 modularity optimization technique Leiden algorithm ⁴⁹ is used to group cells into interconnected
559 clusters (termed meta-cluster) based on constructed SNN graph with a resolution parameter setting
560 by users (default 0.5).

561
562 To understand the molecular-level interaction among modalities, we construct the pseudo-cell
563 level multi-omics profiles. Briefly, for cells in each meta-cluster identified, the Leiden algorithm
564 is further performed based on SNN graph with a higher resolution (default = 2). In this way, cells
565 in each meta-cluster are further grouped into highly interconnected sub-clusters. We term such
566 sub-clusters as pseudo-cells. Only pseudo-cells that consist of at least n cells (default = 10) are
567 kept for downstream analysis, while the others are considered data-specific and discarded. Profiles
568 of the pseudo-cells are constructed by aggregating the cells included. We denote by $\mathbf{X}^{pseudo} \in$
569 $\mathbb{R}^{M \times P}$ be pseudo-cell profiles of feature g_1, g_1, \dots, g_M and $\mathbf{Y}^{pseudo} \in \mathbb{R}^{N \times P}$ be pseudo-cell profiles
570 of feature p_1, p_2, \dots, p_N . P is the number of pseudo-cells.

571
572 **Algorithm 1. Standardizing inputs**

573 For input matrix \mathbf{X} , we denote $\Sigma_{\mathbf{X}'\mathbf{X}}^{-1}$ as the generalized inverse of matrix $\mathbf{X}'\mathbf{X}$, and redefine $\mathbf{X} :=$
574 $\Sigma_{\mathbf{X}'\mathbf{X}}^{-1/2} \mathbf{X}$. For input matrix \mathbf{Y} , we denote $\Sigma_{\mathbf{Y}\mathbf{Y}'}^{-1}$ as the generalized inverse of matrix $\mathbf{Y}\mathbf{Y}'$, and redefine
575 $\mathbf{Y} := \mathbf{Y}\Sigma_{\mathbf{Y}\mathbf{Y}'}^{-1/2}$. The standardization of \mathbf{Z}_r and \mathbf{Z}_l is the same as above.

576

577 **Algorithm 2. Calculating CCVs using SVD**

578 Take subproblem from the Equation (4) as an example, the goal of this module is to find projection
579 matrix $\mathbf{U} \in \mathbb{R}^{K \times E}$ and $\mathbf{S} \in \mathbb{R}^{L \times E}$ such that the correlations between two indices \mathbf{XU} and $\mathbf{Z}_l \mathbf{S}$ are
580 maximized.

$$581 \quad \operatorname{argmax}_{\mathbf{U}, \mathbf{S}} \operatorname{tr}(\mathbf{U}' \mathbf{X}' \mathbf{Z}_l \mathbf{S}) \quad \text{subject to} \quad \mathbf{U}' \mathbf{U} = \mathbf{I}, \mathbf{S}' \mathbf{S} = \mathbf{I}. \quad (\text{A1})$$

582 We define $\Sigma_{\mathbf{X}' \mathbf{Z}_l} := \mathbf{X}' \mathbf{Z}_l$. Let $\mathbf{U} \in \mathbb{R}^{K \times D}$ and $\mathbf{S} \in \mathbb{R}^{K \times D}$ be the matrices of the first E left- and
583 right singular vectors of $\Sigma_{\mathbf{X}' \mathbf{Z}_l}$. Then the optimum in Equation (A1) is solved.

584

585 **Algorithm 3. Updating transition matrix with orthogonality constraints**

586 Take subproblem from the Equation (5) as an example, the goal of this module is to optimize \mathbf{Z}_l .

$$587 \quad (\mathbf{Z}_l) := \operatorname{argmax}_{\mathbf{Z}_l} \operatorname{tr}(\mathbf{U}' \mathbf{X}' \mathbf{Z}_l \mathbf{S}), \quad \text{subject to} \quad \mathbf{S}' \mathbf{Z}_l' \mathbf{Z}_l \mathbf{S} = \mathbf{I} \quad (\text{A2})$$

588 Equation (A2) is maximized when $\mathbf{Z}_l \mathbf{S} = \mathbf{XU}$. Therefore, we can update \mathbf{Z}_l as

$$589 \quad (\mathbf{Z}_l) := \mathbf{XU} \mathbf{S}' \Sigma_{\mathbf{S}' \mathbf{S}}^{-1}, \quad (\text{A3})$$

590 where $\Sigma_{\mathbf{S}' \mathbf{S}}^{-1}$ denotes the generalized inverse of matrix $\mathbf{S}' \mathbf{S}$.

591

592 **Parameter optimization**

593 There are two key hyperparameters when running bindSC for integration. The first one is the
594 dimensionality E in the latent space and the second one is the couple coefficient α . Similar with
595 previous integration methods, the number of dimension E is very important on cell type
596 classification. We provide heuristics to guide the selection of E based on integration metrics
597 defined below, though sometimes helpful, are not substitute for biological insights. As a general
598 suggestion, we recommend starting with a value of E the same with the minimal number of

599 principle components (PCs) used on single modality clustering. The selection of couple coefficient
600 α depends on whether initialized $\mathbf{Z}^{(0)}$ can represent the gene score of \mathbf{Y} . We devise two metrics to
601 aid in selecting α , which measure integration performance on accuracy (no mixing of cell type)
602 and alignment (mixing of datasets) as defined below.

603

604 1) Silhouette score

605 To measure integration accuracy, we use the Silhouette score. Cluster for each cell is defined
606 using the cell type labels assigned from single dataset clustering. The Silhouette score assesses the
607 separation of cell types, where a high score suggests that cells of the same cell type are close
608 together and far from cells of a different type. The Silhouette score $s(i)$ for each cell is calculated
609 as following. Let $a(i)$ be the average distance of cell i to all other cells within i 's cluster and $b(i)$
610 the average distance of i to all cells in the nearest cluster, to which cell i does not belong. Cell-cell
611 distance is computed in the L2-normalized co-embeddings (**Equation 12**). $s(i)$ can be computed
612 as:

$$613 \quad s(i) = \begin{cases} 1 - \frac{a(i)}{b(i)} & \text{if } a(i) < b(i) \\ 0 & \text{if } a(i) = b(i) \\ \frac{b(i)}{a(i)} - 1 & \text{if } a(i) > b(i) \end{cases}$$

614 Notably, given accurate correspondence between two modalities unknown, calculating $s(i)$ for cell
615 i in above equation only includes cells from the same dataset. We average values across all cells
616 to obtain an overall silhouette score for integration task.

617

618 2) Alignment mixing score

619 To measure integration mixing level, we use an alignment mixing score similar to those of previous
620 studies⁵⁰. We first build a 20-nearest neighbor graph for each cell from L2-normalized co-
621 embeddings (**Equation 12**). For cell i , assuming proportions of cells from two modalities are p_{1i}
622 and p_{2i} , respectively, the alignment mixing score is calculated as

$$623 \quad H(i) = -p_{1i} \log_2 p_{1i} - p_{2i} \log_2 p_{2i}$$

624 This corresponds to a mixing metric per cell, and we average values across all cells to obtain an
625 overall mixing metric.

626
627 We run bindSC by ranging a from 0 to 1 (with step size 0.1). Silhouette score and alignment
628 mixing score is calculated for each scenario. We select appropriate a that generally has best
629 performance in Silhouette score and alignment mixing score. Parameter values used in this study
630 can be seen in **Supplementary Table S1**.

631

632 **Performance and benchmarking**

633 In our evaluation, in addition to Silhouette score and alignment mixing score, we also consider
634 anchoring distance for evaluation datasets from multi-omics technologies, in which each cell has
635 paired profiles. For cell i from the first data, we calculate its distance (Euclidean distance) with all
636 cells in the second data as \mathbf{D}_i , and its distance with cell i in the second data as d_i . The anchoring
637 distance for cell i is calculated as $2d_i/\max(\mathbf{D}_i)$. We then average anchoring distance across all
638 cells to obtain an overall anchor distance metric. The anchoring distance of cell i is 0 when it is
639 anchored correctly. The overall anchoring distance is 1 if we randomly layout cells on co-
640 embeddings.

641

642 **Simulation dataset**

643 We generated simulation dataset to evaluate method performance in integrating two modalities
644 assuming accurate feature matching unknown. We used Splatter tool ²⁶ to simulate dataset \mathbf{X} with
645 1,000 genes and cells with different sizes (from 1,000 to 10,000). The whole population is
646 consisted of three batches (cell types). To mimic the feature unmatching case, we first generated
647 dataset \mathbf{X}_1 by randomly permutating genes of \mathbf{X} under specified misalignment rates (MR). MR
648 ranges from 0 to 1 with step size being 0.05 in this study. \mathbf{X}_1 is the same as \mathbf{X} if MR = 0. Half of
649 genes are matched between \mathbf{X}_1 and \mathbf{X} if MR = 0.5. No genes are matched between \mathbf{X}_1 and \mathbf{X} if MR
650 = 1. Then we generated matrix \mathbf{Z} by adding \mathbf{X}_1 with white noise at certain level (i.e., Signal-Noise-
651 Ratio; SNR). SNR is set to be three levels (0, 0.25 and 0.5).

652
653 For method comparison, previous methods including traditional CCA, Seurat ¹⁷, Liger ¹⁹, and
654 Harmony tools ¹⁸ take \mathbf{X} and \mathbf{Z} as input assuming that cell correspondence between them is
655 unknown. bindSC takes two parts as input: 1) \mathbf{X} and \mathbf{Z} with cell correspondence unknown; 2) \mathbf{X}
656 and \mathbf{Z} with feature-level matching unknown (**Supplementary Fig. 2**).

657

658 **Preparation of dexamethasone (DEX) treated A549 cell dataset**

659 To investigate the ability of bindSC in integrating scRNA-seq and scATAC-seq profiles, we
660 explored the DEX-treated A549 dataset generated from sci-CAR technology, which uses
661 combinatorial indexing-based assay to jointly profile chromatin accessibility and mRNA on same
662 cell ⁶. In the A549 dataset, DEX is a synthetic corticosteroid which activates glucocorticoid
663 receptor (GR), binds to thousands of locations, and alternates the expression of hundreds of genes
664 ⁵¹. The human lung adenocarcinoma derived A549 cells after 0, 1, or 3 hours of 100nM DEX

665 treatment are assayed. The sci-RNA-seq dataset was from GSE117089
666 (<https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSE117089>) and sci-ATAC-seq data was
667 from GSM3271041 (<https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSM3271041>). The
668 original A549 data includes sci-RNA-seq profiles for 6,150 cells and sci-ATAC-seq profiles for
669 6,260 cells. There are 1,429 cells co-assayed. Following Cao et al., pre-processing pipeline
670 ([https://github.com/KChen-](https://github.com/KChen-lab/bindSC/blob/master/vignettes/A549/A549_preprocess.ATAC.Rmd)
671 [lab/bindSC/blob/master/vignettes/A549/A549_preprocess.ATAC.Rmd](https://github.com/KChen-lab/bindSC/blob/master/vignettes/A549/A549_preprocess.ATAC.Rmd)), we binarized peak count
672 matrix for cells from both ATAC-seq only and co-assay. Loci present in less than 5 cells and cells
673 with less than 300 accessible loci were removed. Peaks within 1kb were merged and reads in
674 merged peaks were aggregated to generate a merged peak matrix, leading to 3,628 cells with
675 32,791 loci. Each locus' accessibility in each cell was calculated by dividing the cell's raw read
676 count by cell specific size factor using *estimateSizeFactors* function in *Monocle 2*⁵². For RNA-
677 seq data, cells with expression counts less than 500 and more than 9100 were removed. The gene
678 expression in each cell was also calculated by dividing the cell's raw read count by cell specific
679 size factor, followed by *log2* normalization. Genes with no variation in expression across cells
680 were further removed. The gene activity matrix was collapsed from the peak matrix by summing
681 all counts with the gene body plus 2kb upstream using *CreateGeneActivityMatrix* function in
682 Seurat3¹⁷. We then picked top 10,000 variable genes in both sci-RNA-seq data and gene activity
683 data and used the overlapped 4,759 genes between them for integration. Finally, the sci-RNA-seq
684 matrix was composed of 6,005 cells with 4,759 genes, the gene activity matrix was composed of
685 3,628 cells with 4,758 genes, and the sci-ATAC-seq matrix was composed of 3,628 cells with
686 24,953 loci. There were 1,429 cells co-assayed.
687

688 **Preparation of the mouse skin cell data**

689 We examined the performance of bindSC in integrating the scRNA-seq and scATAC-seq data
690 derived from mouse skin tissue. This dataset was generated using SHARE-seq (3) which included
691 34,774 cells that have joint profiles of RNA and ATAC profiles. The RNA data was downloaded
692 from <https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSM4156608>. The ATAC data was
693 downloaded from <https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSM4156597>. The final
694 ATAC-seq matrix includes 25,594 cells on 74,161 peaks after quality control (including removing
695 cells with less than 350 genes expressed; peaks that exist in less than 500 cells). In addition, 4,894
696 genes were identified that were highly variable in both gene expression and gene activity profiles.
697 For this evaluation, we only focused on the third metric (e.g., anchoring distance) that represents
698 the chance for the two instances of a co-assayed cell to appear in the co-embeddings.

699

700 **Preparation of the mouse retina 10x Genomics Multiome ATAC+RNA data**

701 One mouse retina was dissociated by papain-based enzymatic digestion as described previously⁵³
702 with slight modifications. Briefly, 45 U of activated papain solution (with 1.2 mg L-cysteine
703 (Sigma) and 1200U of DNase I (Affymetrix) in 5ml of HBSS buffer) was added to the tissue and
704 incubated at 37 °C for 20 minutes to release live cells. Post-incubation, papain solution was
705 replaced and deactivated with ovomucoid solution (15 mg ovomucoid (Worthington biochemical)
706 and 15 mg BSA (Thermo Fisher Scientific) in 10 ml of MEM (Thermo Fisher Scientific)). The
707 remaining tissue clumps were further triturated in the ovomucoid solution and filtered through a
708 20nm nylon mesh. After centrifugation at 300g 10min at 4C, the single cells were resuspended PBS
709 with 0.04% BSA and checked for viability and cell count. About 1 million cells were pelleted and
710 resuspend in chilled lysis buffer (10x Genomics), incubate for 2 minutes on ice while monitored

711 under microscope. 1ml of chilled wash buffer (10x Genomics) was added and sample was spun
712 down at 500g 5min at 4C and washed before resuspended in Diluted Nuclei Buffer (10x Genomics).
713 Nuclei concentration was determined using countess and proceed with transposition according to
714 manufacturer's recommendation (10x Genomics). After incubation for one hour at 37C, the
715 transposed nuclei were combined with barcoded gel beads, RT mix and partition oil on Chromium
716 to generate gel beads in Emulsion (GEMs). Single cell ATACseq library and 3'RNAseq library
717 were subsequently generated following recommended protocol from 10x Genomics. Libraries
718 were quantified and loaded on Novaseq 6000 and run with the following parameter: 151, 8, 8,
719 151bp. Data was analyzed using bcl2fastq (to generate fastq files) and cellranger pipeline (10x
720 Genomics).

721

722 **Preparation of the mouse frontal cortex cell data**

723 We investigate bindSC ability in integrating spatially resolved transcriptomic (ST) with
724 dissociated scRNA-seq. For the ST dataset, we used sagittal mouse brain slices generated from the
725 Visium v1 chemistry. The dataset was downloaded from [https://support.10xgenomics.com/spatial-](https://support.10xgenomics.com/spatial-gene-expression/datasets)
726 [gene-expression/datasets](https://support.10xgenomics.com/spatial-gene-expression/datasets). The pre-processing workflow was guided by the Seurat3
727 (https://satijalab.org/seurat/v3.2/spatial_vignette.html). Briefly, cells were subset from anterior
728 region, followed by *sctransform*⁵⁴. We then proceed to run dimensionality reduction and clustering
729 using standard workflow as did for scRNA-seq. Cluster ID 1,2,3,5,6,7 was extracted, followed by
730 segment based on exact position (Details in **Subset out anatomical regions** part in Seurat3
731 tutorial), leading to 1,072 cortical cells left for the ST data. One cortical scRNA-seq data composed
732 of ~14,000 adult mouse cortical cell taxonomy from the Allen Institute was collected
733 (https://www.dropbox.com/s/cuowvm4vrf65pvq/allen_cortex.rds?dl=1). This dataset was

734 generated using the SMART-Seq2 protocol ⁵⁵. The *sctransform* normalization was performed
735 based on 3,000 variable genes. We used the cell type annotation provided by published meta data
736 available. There was a total of 14,294 cortical cells with 34,617 genes for the scRNA-seq data.
737 Integration of scRNA-seq and ST is based on 2,316 variable genes overlapped between two
738 datasets.

739

740 To predict locations of each cell type from scRNA-seq in the histological images, we built a
741 support vector machine (SVM) that trained on cell profiles from scRNA-seq data. In the training
742 model, features were identified as cell coordinates in co-embeddings and labels were
743 corresponding cell types. The trained SVM was applied to ST data and output predicted probability
744 of each cell type at each spot. The *SpatialFeaturePlot* function in Seurat3 was used to overlay
745 predicted probabilities for each cell type on top of tissue histology.

746

747 **Preparation of human bone marrow cell dataset**

748 We examined the performance of bindSC in integrating the single-cell RNA and protein data
749 derived from human bone marrow tissue. This dataset was generated using the CITE-seq
750 technology ⁴⁰, which included 30,672 cells that have joint profiles of RNA and a panel of 25
751 antibodies. The dataset was downloaded from
752 https://satijalab.org/seurat/v4.0/weighted_nearest_neighbor_analysis.html. We extracted the 25
753 protein-homologous gene expression profile from the RNA data and kept cells that have total
754 expression count > 2. The final protein matrix includes 28,609 cells with 25 protein abundance
755 levels. The gene expression matrix includes 28,609 cells with 3,000 genes. The protein-
756 homologous RNA matrix includes 28,609 cells with the RNA levels of the 25 genes homologous

757 to the 25 proteins. To measure anchoring accuracy for each cell type, we used the third metric,
758 anchoring distance, which measures the distance of protein and gene expression for each cell in
759 co-embeddings.

760

761 **Motif-based Transcription Factors (TFs) activity estimation**

762 To estimate transcription factor activity from scATAC-seq data, we used default settings in
763 chromVAR⁵⁶ package. This approach quantifies accessibility variation across single cells by
764 aggregating accessible regions containing a specific TF motif. It calculated motif-based TF activity
765 by comparing the observed accessibility of all the peaks containing a TF motif to a background set
766 of peaks normalizing against known technical confounders.

767

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779

780 **Author contributions**

781 K.C. conceptualized and supervised the project. J.D. designed the bindSC tool, implemented the
782 software and performed analysis. R.C., Y. L., X. C., S.K., J.C., contributed to mouse retina 10x
783 Genomics ATAC+RNA data generation, curation. V.M. contributed to data interpretation. J.D.,
784 S.L. and K.C. drafted the manuscript. All authors reviewed, edited, and approved the manuscript.

785

786 **Competing interests**

787 The authors declare no competing interests.

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- 907

908 **Figure Legends**

909 **Fig. 1 Overview of bindSC.** BindSC takes as input two data matrices produced by different modalities
910 from the same cell population **(a)**. The modalities may include transcriptomes, epigenomes, spatial
911 transcriptomes and proteomes. Bi-order integration of two modalities (**X** and **Y**) with unpaired cells and
912 unmatched features using Bi-CCA algorithm **(b)**. In the data matrices, each row represents one gene/locus,
913 and each column represents one cell. The gene score matrix **Z** that links the first modality with the second
914 one is initialized by prior gene activity modeling (see **Methods**). Bi-CCA algorithm aims to update gene
915 score matrix **Z** iteratively by maximizing the correlation of between **X** and **Z** and between **Y** and **Z**
916 simultaneously. Based on canonical correlation vectors (CCVs) in the derived latent space, K-nearest
917 neighbor (KNNs) clustering is performed to define cell types in both modalities **(c)**. Within each cell-type
918 cluster, KNN clustering is further performed at a higher resolution to define pseudo-cells consisting of 10s
919 cells from both modalities. *In silico* multimodal profiles are constructed from cells assigned to the same
920 pseudo-cell **(d)**. The color in each box indicates the relative level of each feature, with white corresponding
921 to missing values. The multiomics feature profiles enable us to 1) link genes to regulatory elements, 2) map
922 RNA expressions to spatial locations and 3) delineate cells by both RNA and protein signatures **(e)**.

923

924 **Fig. 2 Benchmarking bindSC performance on simulation datasets.** Comparison of bindSC to CCA,
925 Seurat, LIGER, and Harmony based on Silhouette score and alignment mixing score **(a)**. The dataset
926 contains 1,000 genes and 1,000 cells equally distributed in 3 cell types. Signal-to-noise ratio (SNR) was set
927 at 0.25. X-axes denote the misalignment rates (MR) between features in the two datasets, which ranges
928 from 0 to 1. The features between two datasets have perfect match if MR = 0 and are unrelated if MR = 1.
929 UMAP views of the co-embeddings generated by bindSC, CCA, Seurat, LIGER, and Harmony **(b)**. From
930 top to bottom are results with MR = 0.1, 0.5, and 0.9, respectively. Each point denotes one cell that is
931 colored based on its true cell type label (red, green, or cyan).

932

933 **Fig.3 Benchmarking bindSC performance on the DEX-treated A549 cell-line data.** UMAP of cells
934 from DEX-treated A549 cell-line data for bindSC, Seurat, LIGER and Harmony respectively, colored by
935 collection time (red: 0 hour, green: 1 hour and blue: 3 hour) on the top panel and by technologies (grey: sci-
936 RNA and brown: sci-ATAC) on the bottom panel **(a)**. Comparison of the 4 methods based on Silhouette
937 score (top), alignment mixing score (middle) and anchoring distance (bottom) **(b)**. Also included for
938 comparison are metrics from randomly selected cells. Accuracy of *in silico* multiomics profile in pseudo-
939 cells **(c)**. The TF-gene correlation is quantified in each pseudo-cell (top panel) by calculating for each TF-
940 gene pair (1.8 million pairs total) a Spearman's rank-order correlation coefficient (SRCC) between the TF
941 activity level, inferred based on motif enrichment in the ATAC data, and the gene expression level in the
942 RNA data. The peak-gene correlation is quantified by calculating for each peak-gene pair a Spearman's
943 rank-order correlation coefficients (SRCC) between a normalized ATAC peak level and a gene expression
944 levels for the cis-peaks (middle panel, 7,833 pairs) and the trans-peaks (bottom panel, 118.7 million pairs),
945 respectively. X-axes are the SRCCs estimated from the co-assayed cells, which serve as the gold standard,
946 while Y-axes are the SRCCs estimated from the pseudo-cells generated by each method. The overall
947 concordance between X and Y are further quantified using a single SRCC shown on the up-left corner of
948 each subfigure. Cis is defined as gene bodies plus 2,000 bps upstream. Reconstructing the gene expression
949 and the TF activity level (Y-axes) of *NR3C1* using bindSC pseudo-cells **(d)**. X-axis is the averaged
950 treatment time of the cells in each pseudo-cell. A genome browser view showing putative regulatory
951 relations between an accessible distal site chr2:201770437-201770992 and the gene *CFLAR* **(e)**. The 6
952 tracks at the top show ATAC peak levels and gene expression levels at six time points. The track in the
953 middle shows chromatin interactome from published Hi-C data. The bottom track shows the *NR3C1* binding
954 targets (ChIP-Seq) peaks published in an independent study ²⁸.

955

956 **Fig. 4 Integrating single-cell RNA-seq and ATAC-seq on a mouse retinal cell atlas.** UMAP views of
957 9,383 mouse retina cells based on gene expression levels in the RNA-seq data **(a)**, chromatin accessibility
958 peak profiles in the ATAC-seq data **(b)**, gene-level collapsed chromatin accessibility profiles **(c)**. The cells

959 are colored by cell types annotated based on RNA expression levels (**Supplementary Fig. 8**). BindSC co-
960 embeddings for the cells in the RNA-seq data (**d**) and those in the ATAC-seq data (**e**). Anchoring distances
961 resulting from bindSC, Seurat, LIGER and Harmony (**f**). The median anchoring distance for each cell type
962 was highlighted as a bold horizontal bar in the middle of each box in each panel. The dotted line denotes the
963 anchoring distance based on random guesses. Zoomed out UMAP views for the BC cells in the co-
964 embeddings generated by bindSC (**g**), Seurat (**h**), LIGER (**i**), and Harmony (**j**). Integration results for all
965 the cell types can be seen in **Supplementary Fig. 9**. RGC: retinal ganglion cells; HC: horizontal cells; BC:
966 bipolar cells; AC: amacrine cells; MG: Müller glial cell.

967

968 **Fig. 5 Integrating spatially resolved transcriptomic (ST) data with scRNA-seq data from mouse**
969 **frontal cortex.** UMAPs of the gene expression levels for the 14,249 cells profiled by SMART-Seq2 and
970 for the 1,072 spots profiled by the 10x Visium technology (**a**). Cell type labels are from the original
971 publication⁵⁷. Predicted locations of each cell type in the histological images (**b**). Color gradient
972 corresponds to the probability score of a cell being mapped to a particular spatial location. Comparison of
973 cell type frequencies estimated from the ST data (Y-axis) to those estimated from the scRNA-seq data (X-
974 axis) (**c**). Correlation coefficients (R) and P values are calculated based on Pearson's correlation analysis.
975 Each dot corresponds to a cell-type (labeled in different colors). The blue line and the grey shade represent
976 regression lines and 95% confidence intervals from performing linear regressions.

977

978 **Fig. 6 Integrating single-cell RNA with protein data produced by a CITE-seq assay.** The UMAP of
979 30,672 human bone marrow cells based on 25 surface protein levels (**a**), 3,000 highly variable gene
980 expression levels (**b**) and 25 protein-homologous gene expression levels (**c**). The cell type labels are from
981 the original study¹⁷. UMAP of the protein (**d**) and the RNA (**e**) expression data in the co-embedding
982 generated by bindSC. Comparison of anchoring distances generated by bindSC, Seurat, LIGER and
983 Harmony (**f**). The red dotted line denotes the anchoring distance from random guesses. Anchoring distances
984 for each cell type in the bindSC co-embedding (**g**).

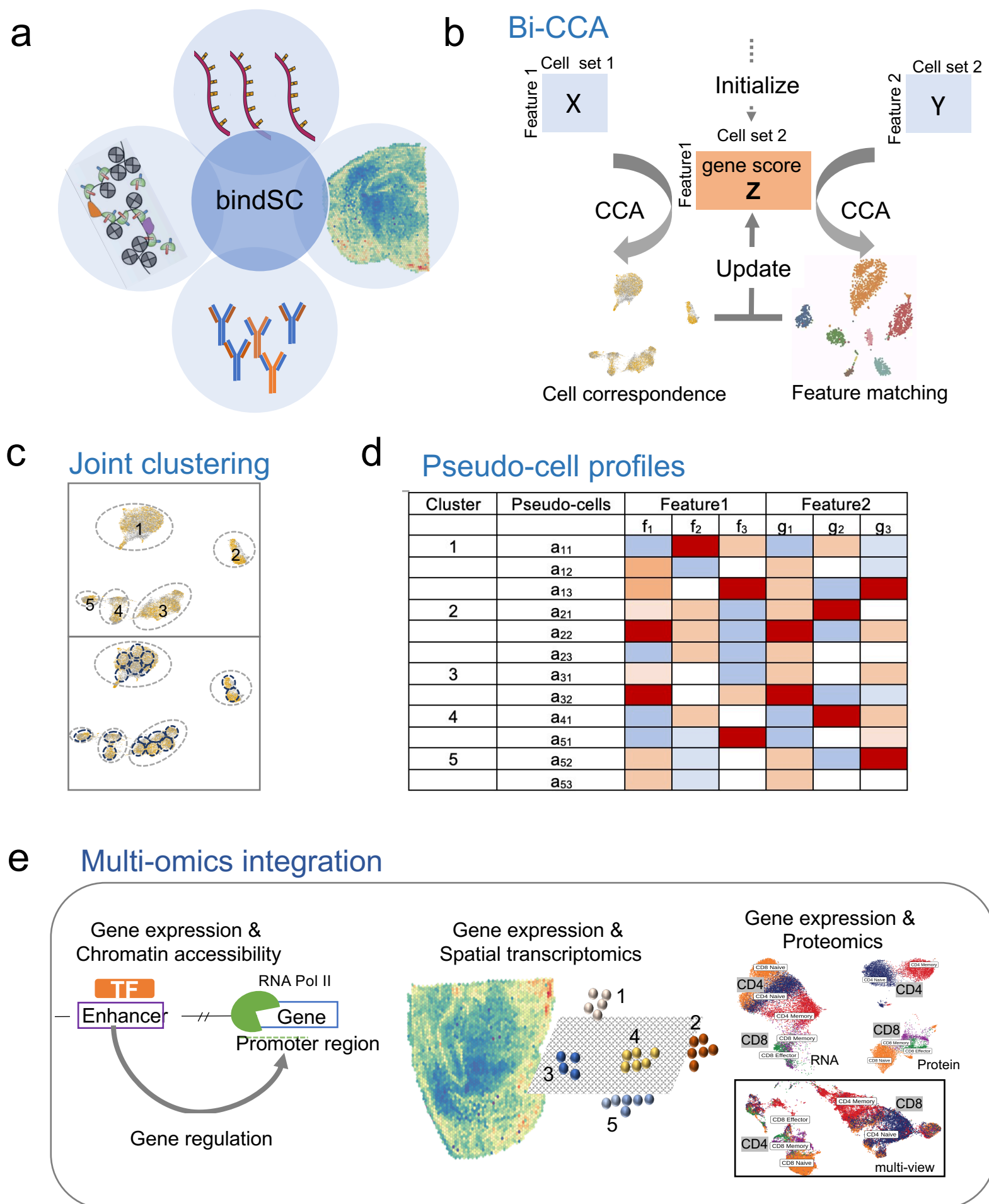
Fig. 1

Fig. 1 Overview of bindSC. BindSC takes as input two data matrices produced by different modalities from the same cell population (**a**). The modalities may include transcriptomes, epigenomes, spatial transcriptomes and proteomes. Bi-order integration of two modalities (**X** and **Y**) with unpaired cells and unmatched features using Bi-CCA algorithm (**b**). In the data matrices, each row represents one gene/locus, and each column represents one cell. The gene score matrix **Z** that links the first modality with the second is initialized by prior gene activity modeling (see **Methods**). Bi-CCA algorithm aims to update gene score matrix **Z** iteratively by maximizing the correlation of between **X** and **Z** and between **Y** and **Z** simultaneously. Based on canonical correlation vectors (CCVs) in the derived latent space, K-nearest neighbor (KNNs) clustering is performed to define cell types in both modalities (**c**). Within each cell-type cluster, KNN clustering is further performed at a higher resolution to define pseudo-cells consisting of 10s cells from both modalities. *In silico* multimodal profiles are constructed from cells assigned to the same pseudo-cell (**d**). The color in each box indicates the relative level of each feature, with white corresponding to missing values. The multiomics feature profiles enable us to 1) link genes to regulatory elements, 2) map RNA expressions to spatial locations and 3) delineate cells by both RNA and protein signatures (**e**).

Fig. 2

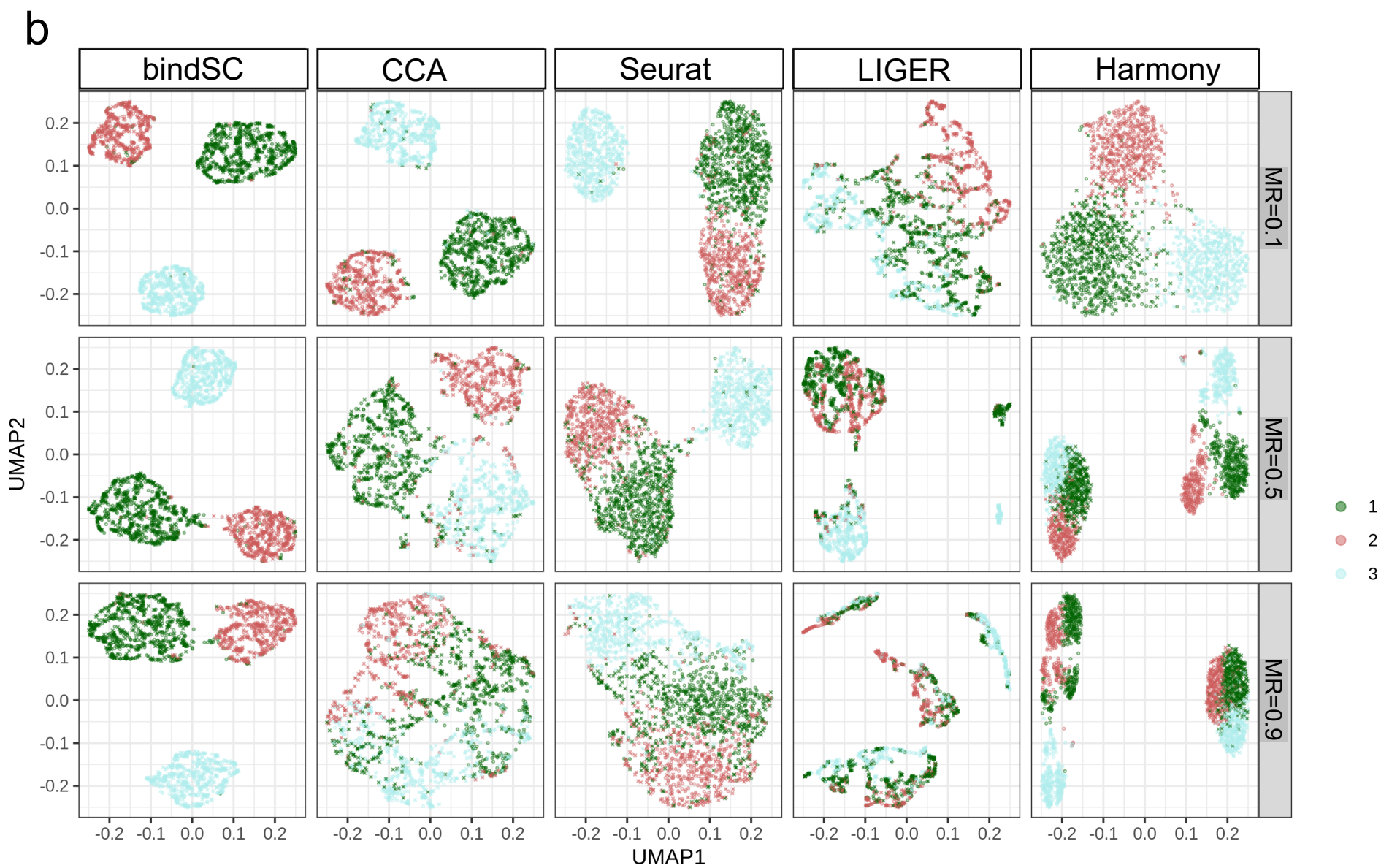
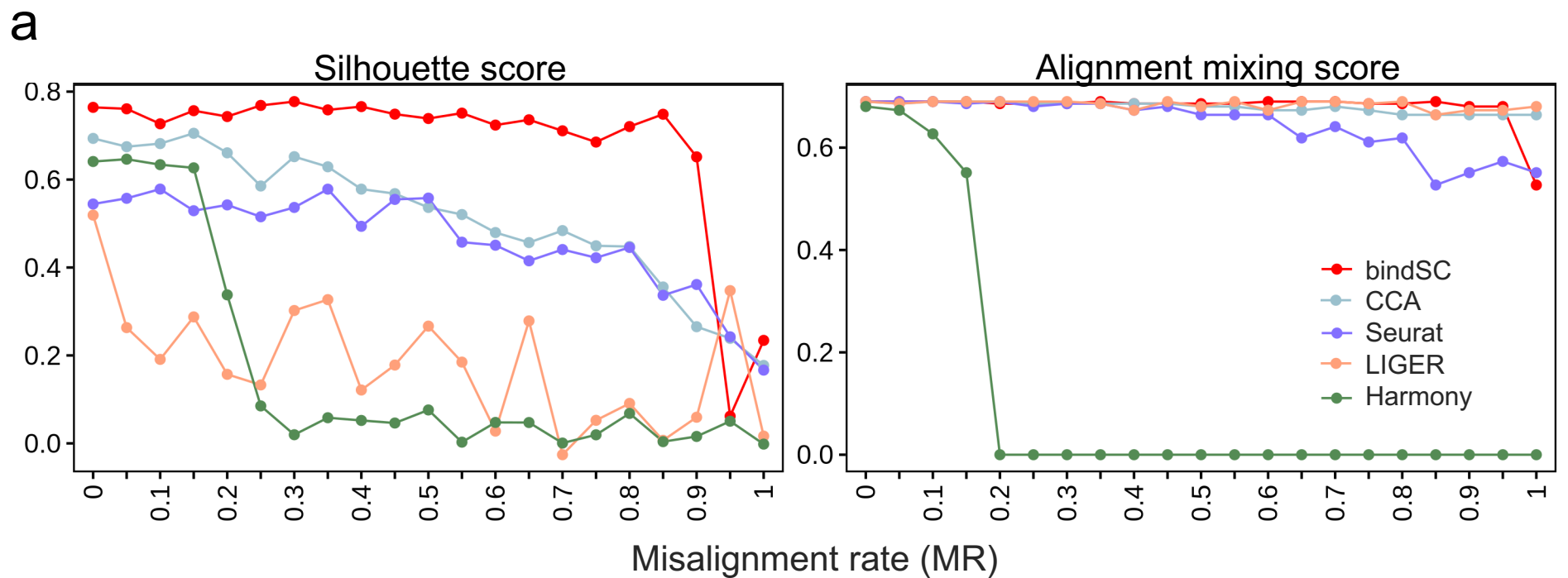


Fig. 2 Benchmarking bindSC performance on simulation datasets. Comparison of bindSC to CCA, Seurat, LIGER, and Harmony based on Silhouette score and alignment mixing score **(a)**. The dataset contains 1,000 genes and 1,000 cells equally distributed in 3 cell types. Signal-to-noise ratio (SNR) was set at 0.25. X-axes denote the misalignment rates (MR) between features in the two datasets, which ranges from 0 to 1. The features between two datasets have perfect match if MR = 0 and are unrelated if MR = 1. UMAP views of the co-embeddings generated by bindSC, CCA, Seurat, LIGER, and Harmony **(b)**. From top to bottom are results with MR = 0.1, 0.5, and 0.9, respectively. Each point denotes one cell that is colored based on its true cell type label (red, green, or cyan).

Fig. 3

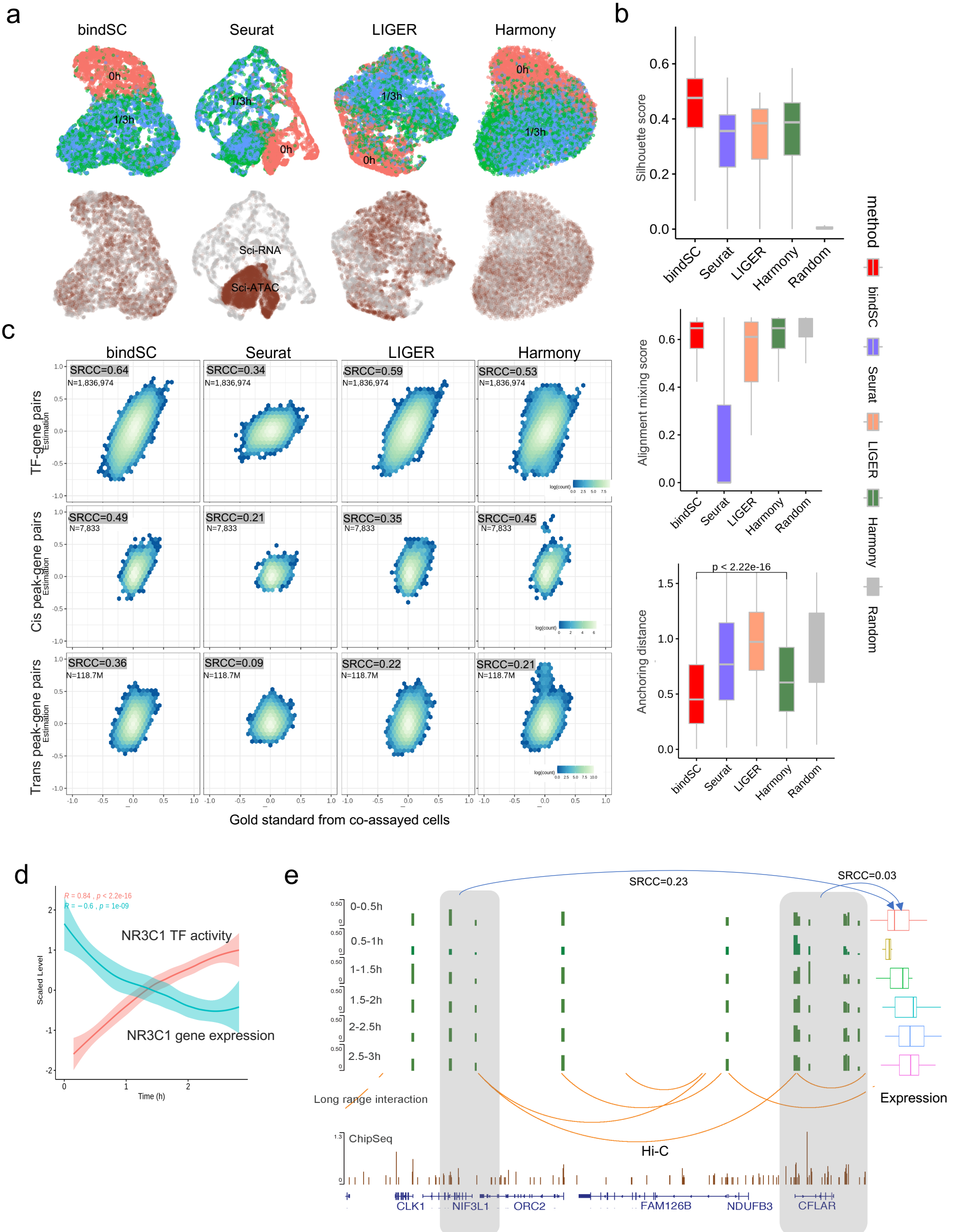


Fig.3 Benchmarking bindSC performance on the DEX-treated A549 cell-line data. UMAP of cells from DEX-treated A549 cell-line data for bindSC, Seurat, LIGER and Harmony respectively, colored by collection time (red: 0 hour, green: 1 hour and blue: 3 hour) on the top panel and by technologies (grey: sci-RNA and brown: sci-ATAC) on the bottom panel **(a)**. Comparison of the 4 methods based on Silhouette score (top), alignment mixing score (middle) and anchoring distance (bottom) **(b)**. Also included for comparison are metrics from randomly selected cells. Accuracy of *in silico* multiomics profile in pseudo-cells **(c)**. The TF-gene correlation is quantified in each pseudo-cell (top panel) by calculating for each TF-gene pair (1.8 million pairs total) a Spearman's rank-order correlation coefficient (SRCC) between the TF activity level, inferred based on motif enrichment in the ATAC data, and the gene expression level in the RNA data. The peak-gene correlation is quantified by calculating for each peak-gene pair a Spearman's rank-order correlation coefficients (SRCC) between a normalized ATAC peak level and a gene expression levels for the cis-peaks (middle panel, 7,833 pairs) and the trans-peaks (bottom panel, 118.7 million pairs), respectively. X-axes are the SRCCs estimated from the co-assayed cells, which serve as the gold standard, while Y-axes are the SRCCs estimated from the pseudo-cells generated by each method. The overall concordance between X and Y are further quantified using a single SRCC shown on the up-left corner of each subfigure. Cis is defined as gene bodies plus 2,000 bps upstream. Reconstructing the gene expression and the TF activity level (Y-axes) of *NR3C1* using bindSC pseudo-cells **(d)**. X-axis is the averaged treatment time of the cells in each pseudo-cell. A genome browser view showing putative regulatory relations between an accessible distal site chr2:201770437-201770992 and the gene *CFLAR* **(e)**. The 6 tracks at the top show ATAC peak levels and gene expression levels at six time points. The track in the middle shows chromatin interactome from published Hi-C data. The bottom track shows the *NR3C1* binding targets (ChIP-Seq) peaks published in an independent study ²⁸.

Fig. 4

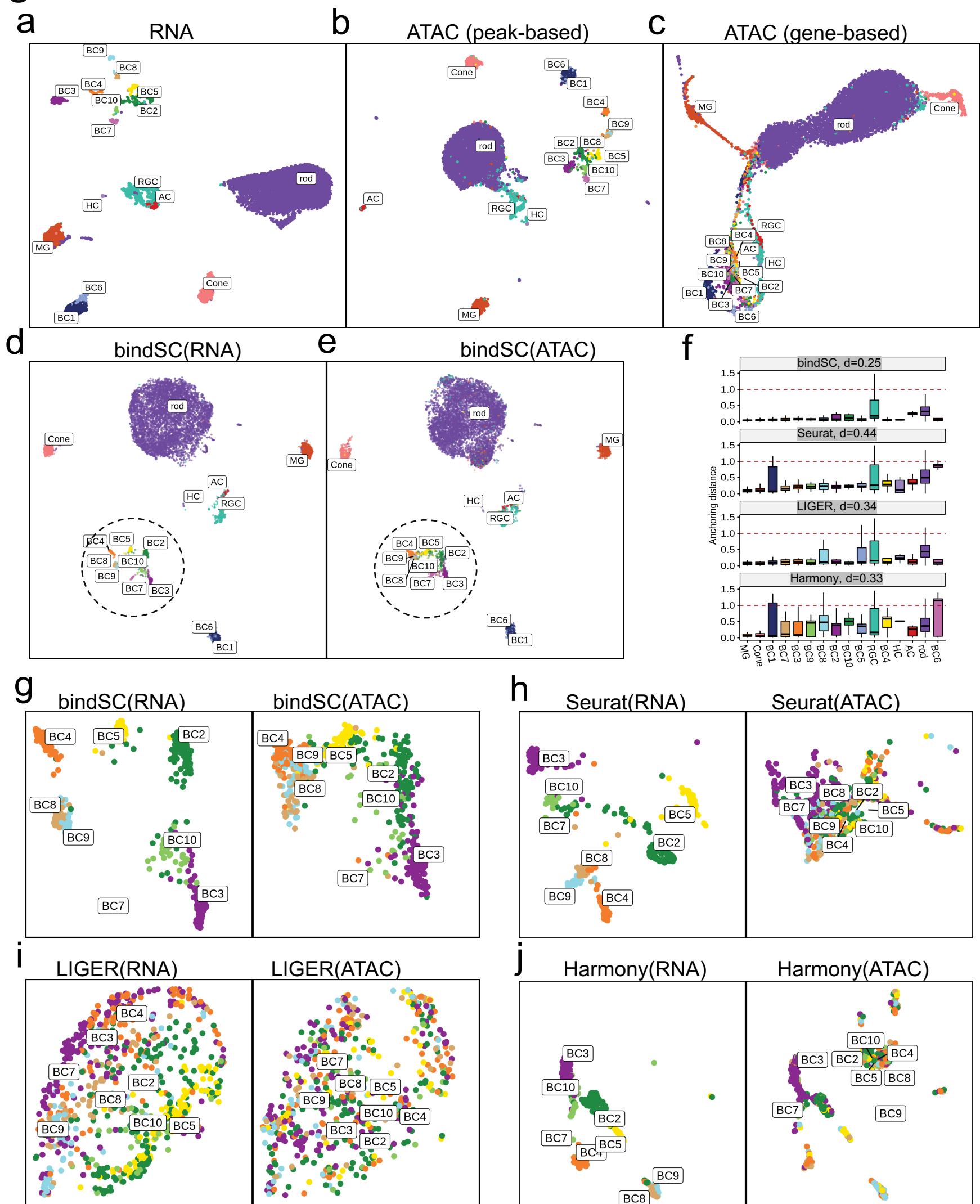


Fig. 4 Integrating single-cell RNA-seq and ATAC-seq on a mouse retinal cell atlas. UMAP views of 9,383 mouse retina cells based on gene expression levels in the RNA-seq data (a), chromatin accessibility peak profiles in the ATAC-seq data (b), gene-level collapsed chromatin accessibility profiles (c). The cells are colored by cell types annotated based on RNA expression levels (Supplementary Fig. 8). BindSC co-embeddings for the cells in the RNA-seq data (d) and those in the ATAC-seq data (e). Anchoring distances resulting from bindSC, Seurat, LIGER and Harmony (f). The median anchoring distance for each cell type was highlighted as a bold horizontal bar in the middle of each box in each panel. The dotted line denotes the anchoring distance based on random guesses. Zoomed out UMAP views for the BC cells in the co-embeddings generated by bindSC (g), Seurat (h), LIGER (i), and Harmony (j). Integration results for all the cell types can be seen in Supplementary Fig. 9. RGC: retinal ganglion cells; HC: horizontal cells; BC: bipolar cells; AC: amacrine cells; MG: Müller glial cell.

Fig. 5

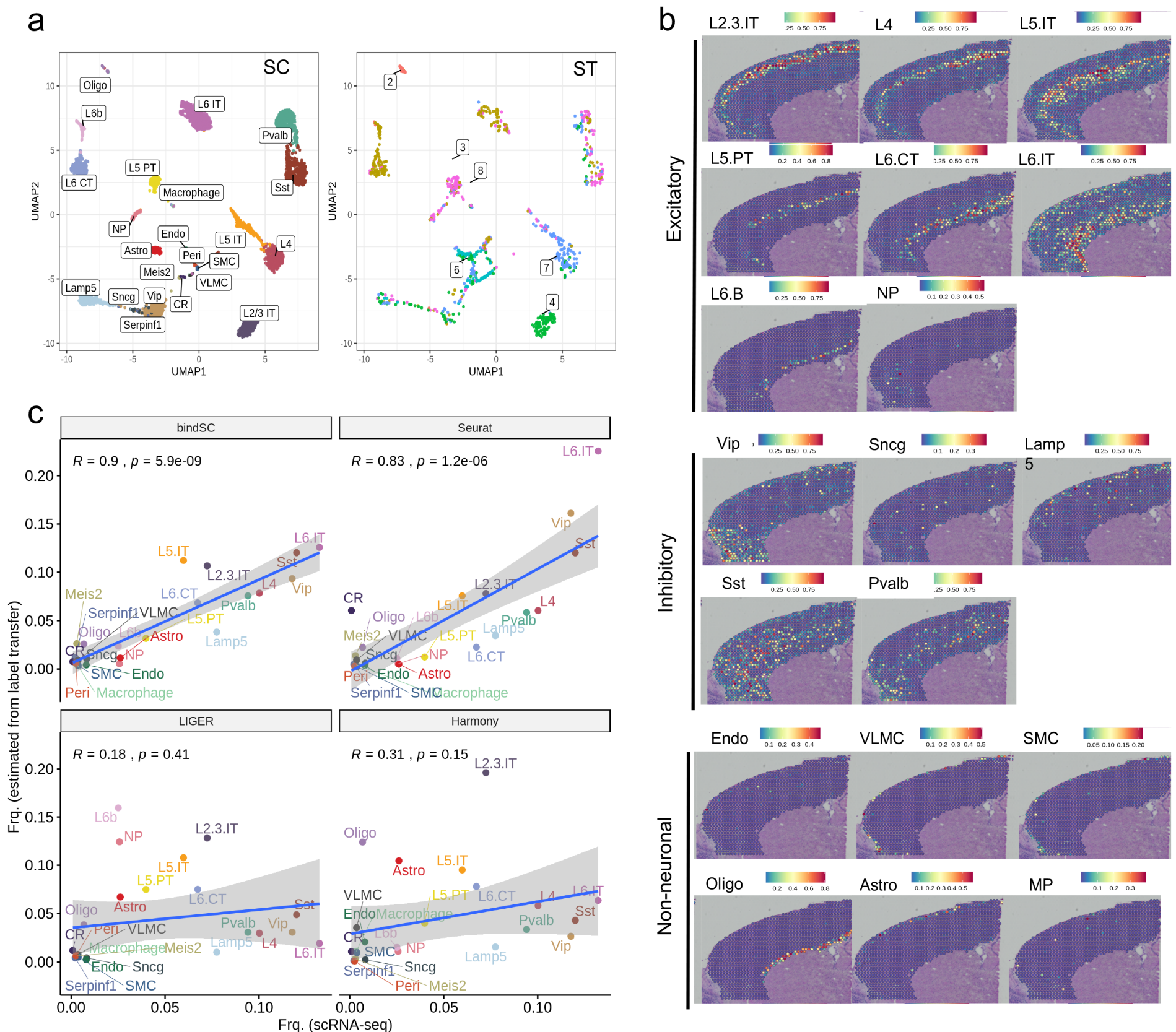


Fig. 5 Integrating spatially resolved transcriptomic (ST) data with scRNA-seq data from mouse frontal cortex. UMAPs of the gene expression levels for the 14,249 cells profiled by SMART-Seq2 and for the 1,072 spots profiled by the 10x Visium technology **(a)**. Cell type labels are from the original publication⁵⁷. Predicted locations of each cell type in the histological images **(b)**. Color gradient corresponds to the probability score of a cell being mapped to a particular spatial location. Comparison of cell type frequencies estimated from the ST data (Y-axis) to those estimated from the scRNA-seq data (X-axis) **(c)**. Correlation coefficients (R) and P values are calculated based on Pearson's correlation analysis. Each dot corresponds to a cell-type (labeled in different colors). The blue line and the grey shade represent regression lines and 95% confidence intervals from performing linear regressions.

Fig. 6

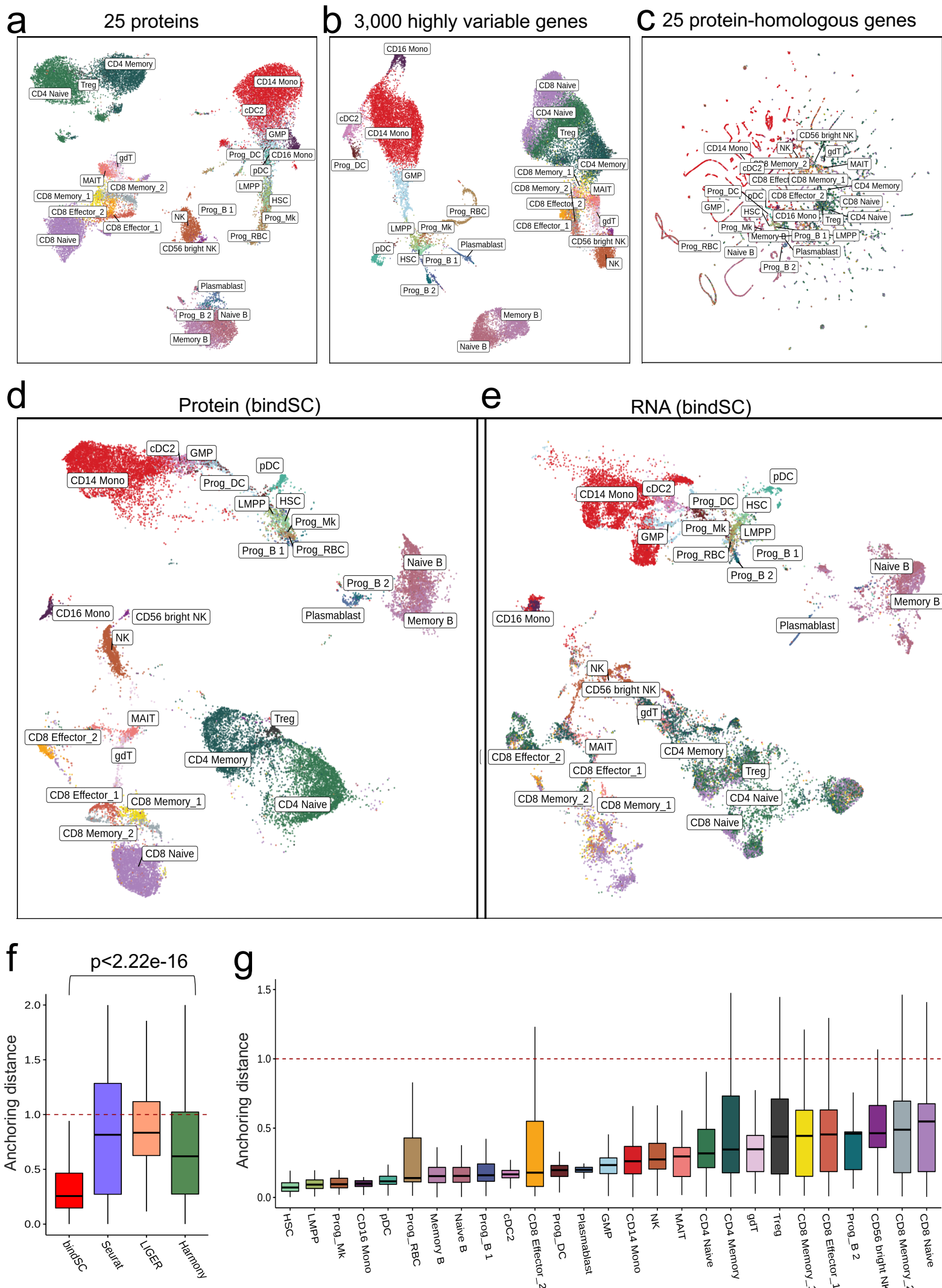


Fig. 6 Integrating single-cell RNA with protein data produced by a CITE-seq assay. The UMAP of 30,672 human bone marrow cells based on 25 surface protein levels **(a)**, 3,000 highly variable gene expression levels **(b)** and 25 protein-homologous gene expression levels **(c)**. The cell type labels are from the original study ¹⁷. UMAP of the protein **(d)** and the RNA **(e)** expression data in the co-embedding generated by bindSC. Comparison of anchoring distances generated by bindSC, Seurat, LIGER and Harmony **(f)**. The red dotted line denotes the anchoring distance from random guesses. Anchoring distances for each cell type in the bindSC co-embedding **(g)**.